Filamentary Velocity Scaling Validation in the TCV Tokamak

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Abstract

A large database of reciprocating probe data from the edge plasma of TCV (Tokamak à Configuration Variable) is used to test the radial velocity scalings of filaments from analytical theory [J. R. Myra, D. A. Russell, and D. A. D’Ippolito, Phys. Plasmas 13, 112502 (2006)]. The measured velocities are mainly scattered between zero and a maximum velocity which varies as a function of size and collisionality in agreement with the analytical scalings. The scatter is consistent with mechanisms that tend to slow the velocity of individual filaments. While the radial velocities were mainly clustered between 0.5 and 2 km/s, a minority reached outward velocities as high as 5km/s or inward velocities as high as -4km/s. Inward moving filaments are only observed in regions of high poloidal velocity shear in discharges with $B_x \nabla B$ away from the X-point, a new finding. The filaments have diameters clustered between 3 and 11mm, and normalized sizes $\hat{a}$ clustered between 0.3 and 1.1, such that most filaments populate the resistive-ballooning regime, therefore, most filaments in TCV have radial velocities with little or no dependence on collisionality. Improvements in cross-correlation techniques and conditional averaging techniques are discussed which reduce the sizes determined for the largest filaments, including those larger than the scrape-off layer (SOL).

1 Introduction

The radial transport in the tokamak edge and Scrape-Off Layer (SOL) is turbulence-dominated[1–7]. This is clearly demonstrated by the L-mode to H-mode transition where the quenching of edge turbulence is correlated[8,9] to a decrease in radial transport and increased confinement[10], forming the pedestal and resulting in steep profiles in the SOL[11,12], which lead to very high heat and particle fluxes at the divertor plate that will exceed the engineering limits in future devices. On the other hand, an increase in the turbulent transport is associated with a strong broadening of the far-SOL resulting in a wide and flat density profile called the “density shoulder” which can substantially increase the particle flux arriving at the first wall[13–18]. Turbulence can also affect the momentum[19,20], and energy[16] fluxes throughout the SOL, so a detailed understanding of turbulent transport is necessary in order to develop predictive SOL models.

The turbulence in the edge and SOL consists of broadband plasma density fluctuations with correlated fluctuations in potential and temperature [5,6,21–23]. The largest turbulent events were named ‘filaments’ from their elongated field-aligned appearance when first observed using fast cameras[24] as well as ‘blobs’ from their 2d appearance as measured using probe arrays[22,25] and Gas Puff Imaging (GPI)[26]. Curvature drifts and $\nabla B$ drifts drive electrostatic polarization within the
filament causing them to advect radially outward by the $\mathbf{E} \times \mathbf{B}$ drift, \cite{27,28}. The radial motion of these filaments has been shown to strongly enhance cross-field transport with the largest $\sim 1\%$ of turbulent fluctuations accounting for $\sim 50\%$ of the cross-field radial $\mathbf{E} \times \mathbf{B}$ convection in the scrape-off layer\cite{29–31}.

In order to understand filamentary transport, a model was developed by the progressive work of many theoreticians\cite{27,32–41} and was used to create a radial velocity scaling, which was first described in ref \cite{32}. The model and associated velocity scaling represent a fairly comprehensive understanding of the filament dynamics, but the scaling is based on reduced models and ignores many known processes. For example, filament-neutral interaction can act to increase\cite{42,43} or decrease\cite{44} filament velocity depending on the contribution from charge-exchange neutrals. Filaments can interact with each other when they are in close proximity, causing the electric fields to merge or cancel each other out \cite{45}. The background plasma density has a slowing effect\cite{46,47}. Hot filaments can form a net monopole potential which induces filament rotation, mixing the filament dipoles and slowing them down \cite{48,49}. Kinetic effects can modify the parallel electron response and introduce drift wave dynamics\cite{50}.

Parallel variation along the filaments and magnetic shear introduces 3D physics\cite{51–54}. High ion temperature increases the filament drive and modifies the vorticity\cite{55–57}. Regions of diamagnetic and paramagnetic plasma are known to attract and repel filaments\cite{58}. The ellipticity of the filament can act to increase or decrease the radial velocity depending on the tilt of the ellipse\cite{59}. And finally, recent works have also included the role of ion kinetic physics \cite{60,61} and strong density gradients\cite{62,63}. It is hoped that future models that use tested velocity scalings with some statistical spread due to these processes could be successful on increasing model predictability. Such stochastic models are currently under development \cite{64}.

The goal of this paper, therefore, is to test the velocity scalings from \cite{32} and to provide information about the statistical spread caused by the other processes. A comprehensive database of thousands of samples is used in order to provide a statistically relevant comparison between experimental data and theory.

We extend previous studies of turbulence in the Tokamak à Configuration Variable (TCV)\cite{17,65–71} by characterizing the size and velocities of the filaments over a range of collisionality. Our paper complements other comprehensive filament velocity scaling studies performed in basic plasma devices\cite{47,72}. More recently, an experimental study of filament motion in NSTX based on GPI data was carried out\cite{73}, and a few comparisons with theoretical predictions were made. In contrast to the probe measurement presented here, the GPI analysis provides spatial resolution in two dimensions, but the density and temperature of individual filaments were not available.

1.1 Background

Filaments have been modeled as equivalent electrical circuits with a voltage source located at the outer midplane (OMP) and a resistive return path located downstream\cite{37,38}. The velocity scaling was thus developed by balancing the polarizing voltage source against several distinct return current paths. The normalized radial velocity of the filament is defined as in \cite{39},

$$\hat{v} = \frac{v_r}{\left(\frac{2L_e\rho^2_e}{R^2}\right)^{1/5}c_s} \quad (1.1)$$

which depends on two main normalized parameters; the normalized filament radius \cite{40}, which is described by two related variables,

$$\hat{a} = \frac{a_e R^{1/5}}{\rho^2_e} \quad \text{or} \quad \Theta = \hat{a}^{3/2} \quad (1.2)$$

and the dimensionless collisionality\cite{41}, which one would ideally calculate as an integral along the field line between the OMP and the outer target.

$$\Lambda = \int_{\text{outer target}}^{\text{OMP}} \frac{v_{ei}}{\Omega_e \rho_s} ds \quad (1.3)$$

Where $v_r$ is the radial filament velocity, $s_i$ is the parallel distance from the target, $L_i$ is the parallel connection length from the OMP to the outer target, $\rho_s$ is the ion gyroradius, $R$ is the major radius, $c_s$ is the sound speed, $a_e$ is the filament radius, $v_{ei}$ is electron-ion collision frequency, and $\Omega_e$ is the electron gyrofrequency. In this paper, we will assume the ion temperature $T_i = T_e$. $\Lambda$ is used to determine the parallel extent of the filament towards the outer target, i.e. whether the filament’s electrical dipole terminates before reaching the x-point, if it reaches into the divertor, or if it extends all the way to the target. Unfortunately, the plasma parameters are not known as a function of $s_i$, so we will consider two estimates for $\Lambda$ following the definitions in \cite{74}. $\Lambda_{\text{mid}}$ will be
calculated using the full connection length and the plasma parameters measured at the OMP by the reciprocating probe, and \( \Lambda_{\text{div}} \) will be calculated using the conditions measured in the divertor by the target Langmuir probes.

\[
\Lambda_{\text{mid}} = L_{||} \frac{V_{el}}{\Omega_{\mu} \rho_{||}} \quad \text{OMP} \quad \Lambda_{\text{div}} = L_{||}^{x-p} \frac{V_{el}}{\Omega_{\mu} \rho_{||}} \quad \text{ARG} \quad (1.4)
\]

where \( L_{||}^{x-p} \) is the parallel distance from the X-point to the outer target. \( \Lambda_{\text{div}} \) is meant to represent the collisionality from the high-density region just in front of the target, which can dominate the entire system.

The magnetic field line fanning parameter \( \epsilon_x \) represents the effects of elliptical magnetic distortion and from magnetic shear [33]. We will take an approximate value of \( \epsilon_x \sim 0.5 \) for limited plasmas and \( \epsilon_x \sim 0.3 \) for diverted plasmas based on the maximum poloidal flux expansion \( f_{x \text{max}} \) typically found for those shapes when averaged across the SOL. Note that \( \epsilon_x \) is strictly less than one.

\[
\epsilon_x \sim \frac{1}{f_{x \text{max}}} \quad \text{for} \quad f_{x \text{max}} > 1 \quad (1.5)
\]

The velocity scaling is defined for four regimes in the \( \Lambda - \hat{a} \) space shown in Figure 1 and each regime has a characteristic expression for \( \hat{v} \). These expressions are solved and plotted in Figure 2 with \( \epsilon_x \) set to 0.3.

![Figure 1](image1.png)

**Figure 1** The \( \Lambda-\Theta \) regime diagram with the normalized velocity scalings for each regime. Reproduced from [J. R. Myra, D. A. Russell, and D. A. D’Ippolito, Phys. Plasmas 13, 112502 (2006)], with the permission of AIP Publishing.

![Figure 2](image2.png)

**Figure 2** (Color online) The normalized velocity \( \hat{v} \) solved for relevant ranges of \( \hat{a} \) and \( \Lambda \), and with \( \epsilon_x = 0.3 \), which is a typical value for diverted plasma configurations.

The different regimes are classified as follows:

- **Cs**: sheath-connected regime
  - At sufficiently low collisionality \( (\Lambda < 1) \), large filaments extend all the way to the outer target, and the dominant return current flows through the sheath and is limited by sheath resistivity [27,28].

  \[
  \hat{v} \sim \hat{a}^{1/2} 
  \]

- **Ci**: connected ideal-interchange regime
  - These filaments are small enough that the ion polarization drift is the dominant return current path. Elliptical distortion due to magnetic shear is able to compress the filament, shortening the cross-field path of the return current, slowing the filaments [32,38].

  \[
  \hat{v} \sim e_x \hat{a}^{1/2} \quad (1.7)
  \]

- **RX**: Resistive x-point regime
  - In this regime, the dominant return current path is the cross-field resistivity, which is magnified by the strong squeezing of the magnetic flux tubes near the X-point due to magnetic shear and poloidal flux expansion[75]. The magnetic shear acts to compress the filament, shortening the return current path[76]. The parallel current is limited by the plasma resistivity \( \eta \) (represented by the collisionality \( \Lambda \)). This is the only regime where the velocity has a direct dependence on \( \Lambda \).
\[ v \sim \Lambda / \hat{a}^2 \] (1.8)

- RB: Resistive Ballooning regime
  - When the collisionality is sufficiently high (\( \Lambda > \Theta \)) the filaments are not electrically connected to the divertor region. Therefore, the ion polarization drift is the dominant return current path \([38,77]\). The magnetic distortion is assumed to be negligible since the filaments do not extend past the X-point if one exists.

\[ v \sim \hat{a}^{1/2} \] (1.9)

It is important to be aware that these velocity scalings are analytical approximations, utilize asymptotic expressions and were developed by approximating gradients as inverse scale lengths. As such, the scalings and the normalized quantities have uncertainties greater than order unity\([38]\), though seeded filament simulations\([32,78,79]\) and experiments in magnetized torus devices\([47,72]\) suggest that the uncertainties may be smaller.

2 Experimental Setup

Due to the stochastic nature of the filaments, a large sample size is needed to provide a statistically relevant comparison between experimental data and theory. To this end, a large database of conditionally averaged samples has been assembled from data taken in the SOL from density scans in both forward and reverse Bt, in diverted and inner wall limited (IWL) configurations, with collisionality varying from the sheath-limited to detached regimes.

Databases of similar size have been studied in TORPEX\([47,72]\), NSTX \([73,80]\), and TCV\([81]\). Filaments measured inside the Last Closed Flux Surface (LCFS) have been omitted from the database since the analytic models discussed are only relevant in the SOL.

Data was taken from 18 ohmic L-mode IWL plasma discharges across a range of line-averaged densities with \( 1 \times 10^{19} \text{ m}^{-3} < n_e < 6 \times 10^{19} \text{ m}^{-3}, \) plasma current \( 85 \text{ kA} < |I_p| < 210 \text{ kA}, B_t = \pm 1.4 \text{ T} \) (forward and reverse field), ellipticity \( 1.2 < \kappa < 1.5 \), and with triangularity \( \delta = 0 \). Approximately 600 conditional averaged entries exist for these discharges. The discharges were described in \([82,83]\), and an example equilibrium is shown in Figure 3a).

Approximately 1200 conditionally averaged data entries were taken in 69 ohmic L-mode lower single null discharges with \( 2.3 \times 10^{19} \text{ m}^{-3} < n_e < 1.5 \times 10^{20} \text{ m}^{-3} \) (ranging from conduction limited to detached conditions), \( 240 \text{ kA} < |I_p| < 360 \text{ kA}, B_t = \pm 1.4 \text{ T} \) (forward and reverse field), and with divertor flux expansion factors \( 2.1 < f_{\text{exp}} < 14 \) as shown in Figure 3b) and c). The discharge conditions were described in detail in \([67,84–86]\). Included in these discharges was an \( f_{\text{exp}} \) scan in order to manipulate \( L_{\phi}^x \) within the divertor. This allowed the divertor conditions (including \( \Lambda_{\text{div}} \)) to be modified with minimal impact on the upstream conditions. If the dominant return current path occurs in the divertor, as is described for the \( C_i, C_s \) and RX regimes, then significant changes in filament behavior should be observed by modifying \( f_{\text{exp}} \) alone. This hypothesis was tested in ref \([67]\), and it was found that the scan in \( f_{\text{exp}} \) did not affect filament size, filament radial velocity or the upstream density profile in TCV.

![Figure 3 Example equilibria for (a) an inner wall limited plasma, (b) a lower single null with small flux expansion at the outer target and (c) a lower single null with large flux expansion and flux flaring in the outer target. The reciprocating probe enters horizontally at the OMP.](image-url)
An electrode measuring the ion saturation current $I_{sat}$ is straddled by two electrodes measuring the floating potential $V_f$ (see Figure 4). The $V_f$ electrodes provide the local poloidal electric field $E_\theta$ and radial drift velocity $v_r$ centered over the $I_{sat}$ electrode (assuming that $T_e$ is constant over the three electrodes). $E_\theta$ and $v_r$ are zero on average, so net radial transport only occurs if the fluctuations in $V_f$ are in phase with the fluctuations in $n_e$. In order to determine the radial velocity for the filaments, they need to be isolated from the broadband turbulence. This was accomplished using the conditional averaging procedures described in [25] for the general case, and in [29] for a similar electrode geometry.

All signals were first filtered with a bandpass between 12 kHz and the Nyquist frequency. The low cutoff frequency is just above the 10 kHz typical switching frequency of the fast power supply that drives TCV’s vertical stabilization coils[89]. This removes the contributions from MHD, oscillations in the plasma position, the motion of the reciprocating probe, as well as the background non-fluctuating components before conditional averaging. $|\delta I_{sat}/I_{sat}|$ was typically ~50% with a skewness ~0 near the LCFS and increasing to 2-3 in the far-SOL.

Peaks in $I_{sat}$ exceeding $\pm 2.5$ standard deviations ($\sigma$) were sampled from 2ms windows of data. The peaks were aligned and averaged along with the surrounding 100$\mu$s of $I_{sat}$ and $E_0$ data, see Figure 5.

Simulations show that filaments feature a rapidly advecting cell and a density wake which is left behind (see e.g. [40,78,90]). This trailing wake does not advect with the same velocity as the rest of the filament. This can be seen in the example shown in Figure 5. The $I_{sat}$ trace remains elevated above average after the peak has passed ($+10$ to $+20$ $\mu$s), which is long after the $E_0$ trace (and thus, the radial velocity) has returned to zero. The poloidal velocity was also found to be near zero in this example (methodology discussed below) suggesting that the decrease in $I_{sat}$ which occurs after $t=5\mu$s is due to diffusion rather than advection. The filament equivalent circuit model discussed above only pertains to the strongly polarized high-density region. Therefore, in this study, we will define our filament width to ignore these trailing wakes. The filament temporal width $\tau_{FWHM}$ was taken by fitting a Gaussian centered at the $I_{sat}$ peak (shown in black), with the fit weighted preferentially towards the steep front edge of the signal. The filament’s $E_0$ was taken at the time of the peak in $I_{sat}$, and the radial velocity was calculated using $v_r = (E_x \times B_t) / B^2$. We find that these trailing wakes can increase the measured $\tau_{FWHM}$ by up to a factor of 2 if they are not ignored.

In order to calculate the size of the filament, an estimate of the poloidal velocity $V_{pol}$ is also needed. This was determined by assuming that the filaments are entrained in the poloidal flows, the velocity of which was determined using the cross-correlation method [29,91,92] which was applied to 2 ms time-slices of $V_f$ data. However, it was found that the poloidal velocity could be greatly over-estimated when using 1D time delay cross-correlation methods since the 1D method has a non-unique solution (See [93,94] for more details). This was especially true where $V_{pol}$ is small, which is typically true in the far-SOL, and in the center of the shear layer. Therefore, the poloidal flow velocity was determined using 2D cross-correlation [93,94] using all 5 $V_f$ electrodes.
identified in Figure 4. This results in $V_{pol}$ values agree with the force balance equation[95], which dictates that the radial electric field must be balanced against the poloidal ion diamagnetic drift and the poloidal rotation velocity. This will be shown in section 3. Compared to the 1D method, 2D cross-correlation was observed to reduce the $V_{pol}$ by as much as a factor of 5.

The filament radius is then calculated by assuming a circular cross-section, since we lack the ability to measure the shape of the filaments.

$$a_r = \frac{t_{solv}}{2} \sqrt{\frac{\theta_e^2}{\theta_{pol}^2} + \frac{\theta_{pol}^2}{\theta_{rad}^2}} \quad (1.10)$$

We find that ignoring the trailing wake and using 2D cross-correlation significantly reduces the size estimates for large filaments but has relatively little effect ($< 20\%$) for the filaments which were already smaller than 1 cm in diameter. As a result, the filament sizes reported are all smaller than or approximately equal to the outer wall gap. Without these improvements, many filaments were larger than the outer wall gap, a result which has been shown in other conditional averaging studies[14,15].

We will now attempt to quantify the experimental uncertainties for the conditionally averaged sizes and radial velocities in the database. The largest uncertainty for the determination of $a_r$ likely stems from the fact that we cannot infer the shape of the filaments. Filament velocity depends chiefly on the vertical size of the filament ($L_{pol}$) rather than the radial size ($L_{rad}$). The circular cross-section assumption is supported by early 2D Beam Emission Spectroscopy videos of filaments[29] and fluid modeling[28] which shows that filaments can be elongated near the LCFS where Reynolds stress is high, but that the internal rotation tends to cause the filaments to return to a circular cross-section and maintain that shape (on average) through most of the SOL. However, a recent and more detailed gas puff imaging surveys at NSTX report an average height to width ratio of $L_{pol}/L_{rad} = 1.5$ across the whole SOL for ohmic plasmas[73]. We can estimate a reasonable uncertainty in $a_r$ for TCV by assuming an even distribution of the velocity angle $\tan(v_r/v_{pol})$ for an elliptical filament with $L_{pol}/L_{rad} = 1.5$. This would result in a systematic underestimation of $a_r$ by 29% with a random uncertainty of 18% ($1\sigma$). The systematic uncertainty will not affect the conclusions of this paper, but we will consider a random uncertainty of $\pm 20\%$ when considering the scatter in the measurements presented in sections 3 and 4.

The uncertainty in $v_r$ was estimated by comparing the velocities calculated using the ExB method described above and by using 1D cross-correlation of the conditionally averaged signals between the radially separated $V_f$ electrodes shown in Figure 4. The two methods agreed well in sign and magnitude with an error distribution of $\pm 0.3km/s$ ($1\sigma$).

One also needs to consider whether the filaments or the background plasma are perturbed by the presence of the probe. Perturbation of $T_e$ and $n_e$ within the filaments by the presence of a solid limiter such as the probe head should be negligible since these perturbative effects should occur on the timescale of the SOL particle dwell time ($\tau_{SOL} \sim L_d/c_s \sim 300\mu$s for TCV). Meanwhile, $V_{pol}$ and $v_r$ are on the order of 1km/s (verified in section 3) such that filaments traverse the probe-head poloidally ($w_{probe} \approx 2.5cm$ wide) or the width of the SOL radially ($w_{SOL} = 3-5cm$) in ($w/v \approx 30\mu$s) or in about $0.1\tau_{SOL}$. The background plasma should also experience little perturbation (at least from the sink of plasma particles to the probe head) since it also rotates at $v_{pol}$, such that the flux tubes advect past the probe head in $\sim 0.1\tau_{SOL}$. This suggests that the presheath “shadow” does not have time to reach a steady-state particle balance and does not therefore need to be ‘filled in’ by enhanced cross-field fluxes as suggested in [96]. However, the non-perturbative hypothesis has yet to be demonstrated experimentally or by detailed modeling.

Perturbative effects of the probe head to $V_f$, $E_0$, and $v_r$ are more difficult to quantify, but radial velocities, filament sizes, and the skewness of the density signals measured with reciprocating probes were found to agree with those measured by non-perturbative diagnostics including Beam Emission Spectroscopy[29] and by Gas puff Imaging[97] suggesting that these effects are small.

$T_e$ is also known to fluctuate in the SOL and the peaks in $T_e$ have been shown to correlate with the peaks in $I_{sat}$ [29,31,98] demonstrating that filaments often have a higher temperature than the surrounding plasma. Our estimates of $E_0$, and $v_r$, assume that $T_e$ is the same at the two $V_f$ electrodes, which should be a reasonable approximation if 1) the conditional averaging method selects for filaments that pass with their centers directly over the $I_{sat}$ tip, and 2) if $T_e$ is peaked symmetrically about the center of the averaged filaments. We believe therefore that the $T_e$ fluctuations do not have a direct effect on $v_r$ measurements.

The filamentary transport models being evaluated assume that $T_e$ is constant and are known to be
inaccurate when the filament temperature exceeds a critical ratio:[37]

\[
\left( \frac{\Delta T}{T_{bg}} \right)_{crit} = \left( \frac{\rho_c T_{crit}^3}{R^4} \right)^{1/5} \quad (1.11)
\]

Where \( \Delta T \) is the change in temperature above the background temperature \( T_{bg} \). The right-hand side of the definition evaluates to \(-0.9\) for the conditions considered in this paper. The elevated filament temperature causes the filament to contain a higher electric potential than the surrounding plasma, and the radial electric field causes the filaments to rotate[48]. Above the critical temperature ratio, the filament spins sufficiently quickly to reduce the vertical charge separation and can greatly reduce the radial velocity[48]. \( \Delta T/T_{bg} \) has been measured to exceed 0.9[98], and one conditional averaging example has been shown with \( \Delta T/T_{bg} \sim 2[29] \).

Unfortunately, we lack the ability to measure \( T_e \) within the filaments. The ramifications of this and other known processes which are not included in the velocity scaling (described in section 1) will be discussed in section 4, while the size and velocity distributions are discussed in the next section.

3 Size and Velocity Distribution

Electrostatic simulations for filaments predict that filaments are most stable at an optimal size of \( \hat{a} = 1[40] \) since smaller filaments (\( \hat{a} < 1 \)) are vulnerable to the Kelvin-Helmholtz instability[77], and larger filaments (\( \hat{a} > 1 \)) are vulnerable to curvature-driven instabilities[34]. It is expected therefore that the filaments should be observed to cluster around this optimal size. This is a useful point of comparison between experimental data and theory [99].

The size distribution is shown in Figure 6 for the IWL discharges and in Figure 7 for the lower single null discharges with typical outer wall gaps shown by the dashed lines. Filaments which are smaller than the 4mm distance between the electrodes used to measure \( E_\theta \) are shaded in red. Since the \( E_\theta \) measurement may be underestimated, \( v_r \) and thus \( a_b \) could also be underestimated for those data points. In both cases, the population distribution has a peak FWHM diameter \( 2a_b \sim 5 \text{mm} \) (Figure 6a & Figure 7a), and \( \hat{a} \) peaks between 0.3 and 0.5 for the limited discharges (Figure 6b), and between 0.5 and 0.8 for the diverted discharges (Figure 7b).

To check if the conditional averaging method was biasing the sample population towards larger filaments, the sampling threshold was lowered from 2.5\( \sigma \) down to 2.1\( \sigma \). This did not change the shape or peak of the normalized size distribution. The number of collected filaments approximately doubles, but new events are added evenly across the size distribution, maintaining the peak at \( \hat{a} \sim 0.5 \). The sampling threshold was therefore kept constant at 2.5\( \sigma \) for all conditions.

The multi-machine database in ref [99] shows a distribution of \( 1.5 < \hat{a} < 15 \) and \( 0.5 \text{ cm} < a_b < 4 \text{ cm} \) as measured by a wide range of techniques, so the filaments in TCV are considerably smaller in normalized size than those typically reported in other tokamaks. The definition of the filament width used in this paper contributes but is not sufficient to explain the difference in size. In section 4, we will discuss the ramifications of the small filament sizes, which may explain why some of the density shoulder evolution trends appear to be weak in TCV.

Next, we will consider the radial velocities of the filaments. The radial velocity distribution for the IWL plasmas is shown in Figure 8 where the velocities range from 0-3 km/s and where most filaments have velocities clustered between 0.5 and 1.5 km/s. The radial velocity distribution for the diverted plasmas is shown in Figure 9 where most filaments have velocities clustered between 0.5 and 2 km/s, with a total range between -4 km/s to +5 km/s.

Filaments with negative velocity have been observed with GPI before [80], but the negative velocities have much smaller magnitudes than the positive velocities. To our knowledge, this is the first experimental evidence of rapid inward filamentary convection. The inward moving filaments were only found in diverted plasmas in reverse field (\( B \times V_B \) away from the X-point) close to the LCFS. An example is shown in Figure 10a) where the radial velocities are plotted as a function of the distance from the separatrix (R-Rsep). The radial velocities are positive for the majority of the SOL and are negative for R-Rsep < 0.5 cm. At the same radii, the poloidal velocity as measured using 2D cross-correlation (see Figure 10b) also changes rapidly. We find that the largest inward velocity measurements typically occur in the region of highest poloidal velocity shear. Note that we are only considering the conditionally averaged radial velocities for positive \( I_{sat} \) peaks, so the radial velocities of density holes do not contribute to the values shown here.

The thick red line in Figure 10b) is the expected poloidal rotation velocity calculated using the single-ion force-balance equation[95], with the \( E_\times B_\parallel \) component shown by the blue line.
\[ V_{pol} = \frac{\vec{E} \times \vec{B}}{B^2} - \frac{\nabla p_i \times \vec{B}}{q_i n B^2} \]  

(1.12)

Where \( p_i \) is the ion pressure and \( q_i \) the charge of the ion. \( V_{pol} \) was calculated from the background \( T_e, n_e, \) and \( V_f \) measurements from the double probe, assuming that the ion temperature \( T_i = T_e \) and that the plasma potential \( V_p = V_f + 2.5kT_e \). The agreement between the poloidal velocities and the force balance equation line suggests that the 2D cross-correlation method is accurate.

At this time, we are unaware of any theories which may explain the rapid inward velocities observed. SOLT simulations occasionally show inward motion of some filaments which are caught in the wake of much larger filaments [100], but the magnitude of the inward velocities are a small fraction of the outward velocities. Regions of diamagnetic plasma are known to exist at the plasma edge that can attract filaments since they are also diamagnetic [58]. This effect only takes place on closed field lines, which could explain why inward moving filaments are not observed in the far-SOL. However, this effect is likely too small to explain the magnitude of the velocities observed.

Finally, simulations show that filaments within a poloidal velocity shear layer can become trapped, with their radial velocity tending towards zero[101], so it is known that the shear layer can affect the radial velocities of filaments. Since our measurements of inward advecting filaments only occur in regions of high poloidal velocity shear, it is likely that this trapping effect plays a role, but it is unclear how they would cause inward motion.

Figure 6 A histogram showing the distribution of the calculated filament diameters (a) and the normalized filament radii (b) for inner-wall limited discharges. The sample population decreases rapidly with increasing size. Filaments with a diameter below 4mm are shown in red. The dashed line in (a) indicates the typical gap between the LCFS and the outer wall. The uncertainty for \( a_b \) is estimated to be ±20% (1σ).

Figure 7 A histogram showing the distribution of the calculated filament diameters (a) and the normalized filament radius (b) for lower single null discharges. The sample population decreases rapidly with increasing size. Filaments with a diameter below 4mm are shaded red. The dashed line in (a) indicates the typical gap between the LCFS and the outer wall. The uncertainty for \( a_b \) is estimated to be ±20% (1σ).
Figure 8 A histogram showing the distribution of radial velocities for inner-wall limited discharges. The horizontal error-bars represent the typical measurement uncertainty (±1σ).

Figure 9 A histogram showing the radial velocity distribution for the lower single null discharges. A small population of filaments was found to be moving inward. The horizontal error-bars represent the typical measurement uncertainty (±1σ).

Figure 10 The radial velocities for conditional averaged measurements are shown in (a) and the poloidal velocity determined by 2D cross-correlation are shown in (b) as a function of the distance from the separatrix (R-Rsep). The thick red line in (b) is the expected rotation velocity calculated from the force balance equation. The blue line shows the E_x*B_y contribution. The estimated uncertainty in \( V_r \) is shown by the example errorbars (1σ), while the uncertainty in \( V_{pol} \) is represented by the scatter.

4 Velocity Scaling Validation

We now proceed to investigate the velocity scaling itself, starting by sorting the database entries throughout the collisionality-size \( \Lambda - \hat{a} \) space. Figure 11 shows the filament distribution (black dots) throughout the \( \Lambda_{mid} - \hat{a} \) space for the IWL plasmas. For these discharges, the glancing field angle with the flush mounted wall Langmuir probes prevents accurate determination of \( n_e \) at the target, so we will not consider \( \Lambda_{div} \). The red ‘o’s represent filaments which are smaller than the separation between the \( E_0 \) electrodes. The magnetic distortion factor \( \epsilon_x \) was set to 0.5 based on a typical poloidal flux expansion at the top and bottom of the plasma. Note that the filaments predominately populate the Resistive-Ballooning RB regime in the \( \Lambda_{mid} - \hat{a} \) space (66% of the black points).

For diverted plasmas, recent work[14,15] suggests that the collisionality in the divertor \( \Lambda_{div} \) is more important than \( \Lambda_{mid} \). This should be especially true if the transition between the sheath connected and sheath disconnected regimes is important since \( \Lambda_{div} \) is meant to represent the high collisionality region just in front of the target which serves as the final barrier preventing the filaments from connecting to the target.

The filament distribution throughout the \( \Lambda_{div} - \hat{a} \) space for the diverted plasmas is plotted in Figure 12. As above, the red ‘o’s show filaments with diameters < 4mm. \( \epsilon_x \) was taken as 0.3. The approximate values for \( \Lambda_{mid} \) are shown on the right axis. Once again, the filaments are predominately found to populate the RB regime, which contains ~80% of the black points, or ~90% if one uses \( \Lambda_{mid} \) instead of \( \Lambda_{div} \).

The small average size of the filaments means that very few populate the regions of the \( \Lambda_{div} - \hat{a} \) space where \( \hat{v} \) depends most strongly on collisionality (The part of the RX regime with \( \hat{a} > 1.6, \Theta > 3.3 \)). \( \hat{v} \) should only change very modestly as a function of \( \Lambda \) for small filaments, and \( \hat{v} \) is predicted to be constant with \( \Lambda \) in the RB regime (see Figure 2). This likely explains why modifying the collisionality was not found to have a straightforward relationship to the upstream density profiles in TCV [67].
4.1 Velocity Scaling in the Resistive Ballooning Regime

The sample size is large enough to consider an experimental validation of the RB velocity scaling for both the IWL discharges and the diverted discharges. A velocity scaling comparison for the IWL discharges is shown in Figure 13, where we plot only the database entries found to populate the RB regime in Figure 11. The shaded region identifies the filaments which are smaller than the separation between the $E_\theta$ electrodes. The measured radial velocities show a scatter which is larger than the experimental uncertainty and is approximately bounded by the RB velocity scaling eq (1.9) with $\hat{v} \sim \hat{a}^{1/2 - 0.6}$ (this notation signifies that $\hat{v}$ ranges from $\hat{a}^{1/2 - 0.6}$ up to $\hat{a}^{1/2 + 0.2}$). The experimental uncertainties were assessed to be ~50% for $a_b$ and ~20% for $v_r$ in section 2.

Low $V_r$ measurements exist for all values of $\hat{a}$. These measurements are consistent with the fact that the scalings estimate the polarization attainable for the idealized filament, while mechanisms exist which can prevent individual filaments from reaching this electric field strength. As discussed in section 1, most of these interactions act to limit the vertical polarization of the filaments and to decrease their radial velocity. Elevated temperatures within the filaments, in particular, could drastically reduce the radial velocities below the scaling.

The magnitude of the scatter around and below the theoretical scaling is similar to that found using a database of similar size taken from the magnetized torus TORPEX comparing filament velocities against the $C_i$ and $C_s$ scalings [72], confirming that the scatter in velocities is intrinsic to the filaments. Therefore, we can conclude that the filament database is consistent with the RB scaling for IWL discharges, but that only a fraction of the filaments are able to reach their ideal polarization and ExB velocity.

The RB velocity scaling comparison for the diverted plasmas is shown in Figure 14a), showing only the database entries in the RB regime as calculated using $\Lambda_{\text{div}}$. The small population (7%) of filaments with negative radial velocities appear to roughly follow $\hat{v} = -\hat{a}$. As discussed in section 3, the filaments with negative radial velocities are only measured in the shear layer close to the LCFS. The color of the data points corresponds to the distance from the separatrix (R-R$_{\text{sep}}$) in Figure 14a).

The heat map in Figure 14b) shows the density of the data points more effectively than part a). Here, we see that the normalized velocities are clustered predominately in the region $\hat{v} \sim \hat{a}^{1/2 - 0.6}$, roughly scattered around the RB velocity scaling. Again, we can conclude that the velocities are consistent with the RB velocity scaling within its expected uncertainty range. These measurements show a higher average radial velocity and a larger scatter than the IWL dataset for any given size. This difference is not predicted by the model, which contains no geometric effects for the filaments in the RB regime. We can see that the average radial velocity increases with size as predicted, though it is not clear within the scatter if the velocities follow the proportionality of the $\hat{v} \sim \hat{a}^{1/2}$ scaling.
4.2 Velocity Scaling for Large Filaments

Outside of the RB regime, there are fewer measurements in the database, which are split between the C<sub>i</sub>, C<sub>s</sub>, and RX regimes. This makes it more difficult to evaluate the data against the velocity scaling, but we will present a few useful comparisons in this subsection.

For the IWL discharges, \( \hat{v} \) is plotted as a function of \( \hat{a} \) in Figure 15 for all the filaments outside of the RB regime. The red dashed line shows the velocity scaling for the C<sub>i</sub> and C<sub>s</sub> regimes, while the blue dot-dashed lines show the velocity scaling for \( \Lambda = 1 \) and \( \Lambda = 2 \) (the bottom and top branches respectively) which covers the RX regime. For \( \hat{a} > 1.8 \), \( \hat{v} \) is expected to decrease with size following the \( \hat{v} \propto 1/\hat{a}^2 \) contours. The dataset does indeed show that \( \hat{v} \) decreases as a function of \( \hat{a} \) for large values of \( \hat{a} \) and shows a peak near \( \hat{a} = 1 \) in agreement with the model. Additionally, this decreasing trend demonstrates that the relationship observed for the RB regimes in section 4.1 is not an artifact of the way the filament sizes are calculated using \( v_r \).

Next, we will consider the large filaments from the diverted discharges. The \( \hat{v} \propto 1/\hat{a}^2 \) relation is less clear for this dataset since it lacks the largest \( \hat{a} \approx 6 \) filaments. Instead, we will consider the relationship between \( \hat{v} \) and \( \Lambda \) for filaments with \( \hat{a} > 1/e^2 \approx 1.6 \) (equivalent to \( \Theta > 1/e^2 = 3.3 \)) since filaments in this size range exist in even distribution for the C<sub>i</sub>, RX, and RB regimes. i.e. the distribution of \( \hat{a} \) stays roughly constant as a function of \( \Lambda_{\text{div}} \) in Figure 12 in the region where \( \hat{a} > 1.6 \).

\( \hat{v} \) is plotted as a function of \( \Lambda_{\text{div}} \) in Figure 16a) and as a function of \( \Lambda_{\text{mid}} \) in Figure 16b). The red dashed line in both subplots is the velocity scaling for \( \hat{a} = 1.6 \), \( \Theta = 3.3 \), and the blue dotted line shows the velocity scaling for \( \hat{a} = 3.3 \), \( \Theta = 20 \), the upper bound in size for the single null database. Since \( \Lambda \) varies by 3 orders of magnitude, it dominates over \( \hat{a} \) when determining \( \hat{v} \) (this can be seen in Figure 2). Because the population density decreases rapidly with filament size, the red dashed line is more applicable to the dataset.

In Figure 16a), \( \hat{v} \) increases as expected for \( 10^0 < \Lambda_{\text{div}} < 10^4 \), and appears to be constant (as expected) for \( \Lambda_{\text{div}} < 10^0 \) in the C<sub>i</sub> regime. However, the average velocity in the C<sub>s</sub> regime exceeds the velocity scaling by a factor of 3 or more and \( \hat{v} \) changes as a function of \( \Lambda_{\text{div}} \) much more weakly than described by the
scaling in the RX regime. Alternatively, in Figure 16b, \( \hat{v} \) is plotted as a function of \( \Lambda_{\text{mid}} \), and \( \hat{v} \) agrees more closely with the scaling with \( \hat{v} \sim \hat{v}_{\text{scaling}}^{-0.6} \), which is approximately the same scatter seen in the RB regime.

This could be because TCV has a very long outer divertor leg relative to the size of the plasma, and a very open divertor compared to other tokamaks. As such, the collisionality in the divertor may not dominate the system as it does in tokamaks with closed divertors. \( \Lambda_{\text{div}} \) is meant to represent the region of high collisionality in front of the target, but there is no reason to expect that this region extends to the x-point when the outer leg is so long. This could explain why modification of \( L_{||x\text{-pt}} \) was not found to have an effect on the upstream density profiles or on filament sizes and velocities in TCV [67]. In order to fully understand the role of collisionality in TCV, it may be necessary to use an estimate of \( \Lambda \) that accounts for parallel gradients in \( \nu_{ei} \). Such 3D filament models are under development[102].

Figure 15 The normalized filament radial velocities as a function of the normalized filament radius for all filaments outside of the RB regime for the IWL discharges. The red dashed line is the velocity scaling for \( \hat{a} = 1 \) (bottom) and \( \hat{a} = 2 \) (top).

Figure 16 The normalized filament radial velocities as a function of the \( \Lambda_{\text{div}} \) (a) and \( \Lambda \) (b). The dashed red lines are the velocity scaling for \( \hat{a} = 1.6 \), and the dotted blue lines are the velocity scaling for \( \hat{a} = 3.3 \).

5 Conclusions

Using a large database of conditionally averaged measurements in the TCV tokamak, the filament normalized radial velocities \( \hat{v} \) were found to be scattered between ~0 and an upper bound, where this upper bound varies as a function of normalized filament size \( \hat{a} \) and the collisionality \( \Lambda \) in rough agreement with the velocity scalings. The scatter in the database is larger than the experimental uncertainties, which are estimated to be ~50% for \( \hat{a} \) or \( \hat{v} \), and ~20% for \( v_{r} \) or \( \hat{v} \). For filaments sorted into the RB regime for IWL plasmas, the upper bound in \( \hat{v} \) is confirmed to increase with \( \hat{a} \) in agreement with the \( \hat{a}^{1/2} \) scaling. For filaments in diverted plasmas in the RB regime, the \( \hat{v} \) measurements are higher on average and have a larger scatter than the IWL cases, but \( \hat{v} \) is again found to increase with size approximately in agreement with the \( \hat{a}^{1/2} \) scaling. These measurements are consistent with the concept that the velocity scaling correctly estimate of the polarization that can be sustained by an ideal filament, but that many mechanisms exist which can act to decrease radial velocity (e.g. filament rotation or filament-filament collisions) or to increase the radial velocity (e.g. filament ellipticity or neutral wind) of any given filament, which randomizes the velocity distribution over a wide range. The role of
high $T_e$ within the filaments compared to the background plasma may be especially important, since it has been shown that $\Delta T/T_{bg}$ can reach sufficiently high ratios to drastically reduce the radial velocity. Future predictive modeling of filamentary transport which use the tested velocity scalings of the filament equivalent circuit model will need to include the statistical spread resulting from these processes, and further study is needed to quantify the magnitude of their effects.

Due to the smaller sample sizes outside of the RB regime, it was more difficult to test the velocity scalings for the other regimes, but the data which is available does appear to be consistent with the velocity scalings. In the IWL discharges for the large filaments in the RX and C$\text{\textsubscript{r}}$ regimes, $\hat{v}$ was found to decrease with filament size which is consistent with the $\hat{v} \propto \hat{a}^{-2}$ velocity scalings. In the diverted discharges for filaments with $\hat{a} > 1/\epsilon_{\text{C}}$, the $\hat{v}$ upper bound has been found to increase with $\Lambda$ in agreement with the velocity scaling of the RX regime. The $\Lambda_{\text{mid}}$ approximation produces a more convincing agreement than $\Lambda_{\text{div}}$, especially in the Cs regime where the $\hat{v}$ measurements exceeded the $\Lambda_{\text{div}}$ scaling by a factor of 3 or more. This could be explained by TCV’s open divertor and long outer divertor leg. Due to this geometry, the collisionality in the divertor may not dominate over the main chamber collisionality as it does in tokamaks with closed divertors. Furthermore, the use of $L_{\perp}^{\text{Cs}}$ in the definition of $\Lambda_{\text{div}}$ implies that the region of high collisionality just in front of the target extends up to the x-point, which seems inappropriate when $L_{\perp}^{\text{Cs}}$ is not small compared to $L_{\parallel}$. A more complete approximation for $\Lambda$ (allowing $v_{\parallel}$ to change along the field line) and more data at lower collisionality are needed in order to fully understand the role that collisionality plays in TCV.

We find that the majority of filaments populate the RB regime in TCV. The RB regime contains 66% of the measured filaments from IWL plasmas and 80% or 90% of those from diverted discharges (when sorted using $\Lambda_{\text{div}}$ or $\Lambda_{\text{mid}}$, respectively). This is because the filament in TCV have a size distribution peaking at a diameter of 0.5cm and $\hat{a} \sim 0.5$, which is smaller than the ‘most stable blob size’ expected to have $\hat{a} \sim 1$, though this discrepancy is still within the order unity accuracy that might be expected for the analytic expression for $\hat{a}$. The fact that 80%-90% of the filaments populate the RB regime (where $\hat{v}$ is expected to be independent of $\Lambda$) likely explains why the filament radial velocity was not found to increase with line average density in [67]. This also explains why increasing the connection length in the divertor was not found to affect the average filament size or radial velocity since the filaments in the RB regime do not extend into the divertor, as well as why the upstream density profiles were not found to have a straightforward relationship to $\Lambda_{\text{div}}$ in [67].

The filament sizes calculated in this paper are smaller than those reported in previous work [29,67] due to the introduction of 2D cross-correlation for determining the poloidal velocity, and because the trailing wake following the filament is not included when determining the size. The poloidal velocities calculated using the 2D method agree with the force balance equation and are up to 5x slower than those determined using 1D cross-correlation, suggesting that the 2D methods are necessary in order to determine the filament sizes accurately. Filament diameters are mainly clustered between 3 and 11mm though some filaments are observed to have diameters as large as the distance between the LCFS and the outer wall. Without these improvements, a significant fraction of filaments were found to be much wider than the SOL.

Radial velocities were found mainly clustered in the range of 0.5 to 2 km/s, but with some filaments having radial velocities as high as 5 km/s and as low as -4 km/s. The measurements of rapidly inward moving filaments is both surprising and unique as far as we know. It awaits a theoretical explanation, as the theories which do predict inward velocities estimate that the inward velocities should be small compared to the outward ones. The inward moving filaments are only observed in diverted plasmas, with $B_t > 0$ (unfavorable direction for H-mode), and in the region of high poloidal velocity shear within 5mm of the LCFS. This measurement is not related to the motion of density holes.

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