

A semi-supervised approach for the semantic segmentation of trajectories

Soares Júnior A.^{*}, Times V. C.[†], Renso C.[‡], Matwin S.^{*} and Cabral L. A. F.[§]

^{*}Dalhousie University (Canada) [†]Federal University of Pernambuco (Brazil) [‡]ISTI-CNR (Italy) [§]Federal University of Paraíba (Brazil)

Abstract—A first fundamental step in the process of analyzing movement data is trajectory segmentation, i.e., splitting trajectories into homogeneous segments based on some criteria. Although trajectory segmentation has been the object of several approaches in the last decade, a proposal based on a semi-supervised approach remains inexistent. A semi-supervised approach means that a user labels manually a small set of trajectories with meaningful segments and, from this set, the method infers in an unsupervised way the segments of the remaining trajectories. The main advantage of this method compared to pure supervised ones is that it reduces the human effort to label the number of trajectories. In this work, we propose the use of the Minimum Description Length (MDL) principle to measure homogeneity inside segments. We also introduce the *Reactive Greedy Randomized Adaptive Search Procedure for semantic Semi-supervised Trajectory Segmentation* (RGRASP-SemTS) algorithm that segments trajectories by combining a limited user labeling phase with a low number of input parameters and no predefined segmenting criteria. The approach and the algorithm are presented in detail throughout the paper, and the experiments are carried out on two real-world datasets. The evaluation tests prove how our approach outperforms state-of-the-art competitors when compared to ground truth.

Index Terms—Trajectory segmentation; Semantic annotation; Semantic trajectory; Semi-supervised learning.

I. INTRODUCTION

Research on trajectory management and analysis is a broad and mature area [16] since positioning devices are now commonly used to track people, vehicles, vessels, and animals. These devices produce trajectory samples representing the object movement as a discrete collection of spatiotemporal points, or samples. An important step that is a prerequisite to several analysis tasks on these tracks is the *trajectory segmentation* [14, 17]. Segmenting a trajectory means splitting the spatiotemporal sequence of points into segments based on some properties or criteria that identify a similar behavior in the segment. Examples of segment splitting criteria are based on the temporal component like the day of the week or based on whether the object is moving or not, thus identifying the *stop* segments from the *move* segments [17]. Segmenting a trajectory with clear criteria is a first step to *semantically enrich trajectories* (or *semantic annotation*), a process to enrich trajectory parts with meaningful contextual information [14, 12].

The segmentation task is therefore based on methods capable of distinguishing the homogeneous or similar parts of a trajectory based on some criteria. We can distinguish two

cases: *supervised* and *unsupervised* segmentation. In supervised segmentation, the criteria are already known *a priori*. This can be implemented with algorithms based on simple thresholds (e.g., speed) or machine learning techniques that learn the correct segmentation from a set of labeled segments. When the segmentation criteria are unknown, the unsupervised algorithm derives the homogeneity of segments based on some cost function. Both supervised and unsupervised methods have complementary benefits and drawbacks. The supervised methods rely on user-defined rules, labels or thresholds; therefore the segmentation is user-driven. This kind of segmentation is particularly suitable for semantic annotation, thanks to the human labeling phase that can associated complex semantic labels to trajectory parts (e.g. activity performed or transportation means). The drawback is that, in some cases, these criteria are not clear, they may depend on the characteristics of the trajectory dataset and the expertise of the domain specialist to correctly label a set of trajectories and/or configure the thresholds. Also, obtaining a high quality labeled trajectory dataset is difficult as it relies on a huge effort by domain experts and this is one reason why the supervised methods are not widespread in this field.

Unsupervised algorithms, on the contrary, avoid any control from the user and automatically detect segments using a cost function which represents the homogeneity of the segments. Although these algorithms can produce segments with high homogeneity, they lack semantics and any connection to the specific application, making the interpretation task difficult. Despite the broad spectrum of trajectory segmentation approaches already proposed in the literature (see for example [16, 14]), there is still a lack of methods attempting to combine the benefits of both supervised and unsupervised strategies. As a possible solution to this, a *semi-supervised* approach to the segmentation task is proposed in this work.

Semi-supervised means essentially that a user labels manually a small set of trajectories based on some criteria, thus giving the semantics of the segmentation and, from that, the method infers, in an unsupervised way, the segmentation of the remaining part of the trajectory dataset. Such approach offers a balance between methods which are entirely supervised, where the user precisely defines the splitting criteria, and unsupervised, where the method infers a good splitting based on a cost function. We observe that when the segmentation is semantic-based (e.g., representing the activity of the moving object), in contrast to the geometric-based segmentation (e.g., the speed of the object), the need for manually annotated

trajectories is crucial: minimizing the number of these human-labeled trajectories, as stated in [8], is fundamental to keep this task feasible.

This paper comes as advancement and extension of a previous work [7] based on an unsupervised method named GRASP-UTS (Greedy Randomized Search Adaptive Search Procedure for Unsupervised Trajectory Segmentation). Compared to that paper, which introduces an unsupervised algorithm for trajectory segmentation, here we propose a new semi-supervised segmentation algorithm called RGRASP-SemTS (*Reactive Greedy Randomized Adaptive Search Procedure for Semantic semi-supervised Trajectory Segmentation*).

We summarize below the original contributions of this paper:

- Proposal of the RGRASP-SemTS as a semi-supervised algorithm to segment trajectories that uses a small set of labeled trajectory data during the trajectory segmentation task to drive the unsupervised segmentation of unlabeled trajectory data.
- Unlike previous related works, RGRASP-SemTS focuses on performing semantic trajectory segmentation using features evaluation, non-monotone criteria, semantic annotation, cost function and meta-heuristics.
- Description of a feature evaluation step that aims to find the best set of features for increasing the RGRASP-SemTS's performance.
- Proof that using labeled data helps speeding up the RGRASP-SemTS's performance when compared to our previous unsupervised algorithm, GRASP-UTS.
- Description of experiments with two real world datasets showing that the performance of RGRASP-SemTS is superior when compared to other unsupervised and supervised approaches of the literature.

The remainder of the paper is organized as follows. Section II surveys the related work. Section III shows concept definitions, terminologies, and theories used in the proposed solution. Section IV presents the novel semantic semi-supervised algorithm for trajectory segmentation named RGRASP-SemTS. Section V presents the metrics and the results obtained by the novel approach when applied to real datasets. Finally, Section VI concludes the paper.

II. RELATED WORKS

As the interest in the literature is increasing, new methods to segment trajectories are being proposed. Pioneering work is the *stop and move* definition given by [17] where the segmentation was used to identify the parts of the trajectories where the object stays still and separate it from the moving parts. We later come to a broader definition of semantic trajectory, where the segments may identify and be annotated not only as *stops and moves*, but also with more meaningful and *context-aware* labels such as transportation means or activities [2, 14, 12]. The need to identify segments based on some semantics fostered the developments of different segmentation methods. A possible classification of these methods is based on the characteristics of the algorithm: supervised or unsupervised, application-oriented or general purpose, monotone criteria

or non-monotone criteria and with a predefined number of segments versus a non-predefined number of segments.

Supervised means that the segmentation criteria are based on ad-hoc standards and predefined rules. This is the case when the rules are clear and predefined by experts of the domain as in works [13, 11, 20]. The second line of approaches follows an unsupervised methodology, where no predetermined criteria are imposed in the segmentation process, and the segment split is based on data properties as in works [9, 18, 7]. To the best of our knowledge, no works found in the trajectory segmentation literature tried to combine both supervised and unsupervised criteria as we are doing in the present paper.

Another possible classification of segmentation algorithms is to distinguish between application-oriented and general purpose methods [9]. Application-oriented algorithms for trajectory segmentation are designed for a specific purpose and, consequently, they are difficult to reuse in different domains. Examples of application-oriented algorithms for trajectory segmentation are described in [18, 19, 20]. On the other hand, the general purpose algorithms for trajectory segmentation are easily reused in many different domains. Examples of general purpose algorithms for trajectory segmentation are explained in [4, 7, 9, 13, 11]

Trajectory segmentation algorithms can also be monotone or non-monotone, and this affects the results of the splitting task [4]. Indeed, a criterion is monotone if any sub-segment S' of a segment S always fulfills the whole segment criterion. Monotone criteria are found when values of the features fall within a range or ratio. On the other hand, values computed from means and standard deviations are non-monotone. Trajectory segmentation algorithms with monotone criteria includes works [4, 1], while the approaches with non-monotone criteria include [9, 13, 11, 7, 20]

Another issue related to the segmentation of trajectories is the number of segments that must be found. In [9], the number of segments is given as input to the algorithm, so it is already predefined, whereas, in [7, 13, 11, 20], the number of segments is found automatically by the algorithm during its execution.

The RGRASP-SemTS algorithm proposed in this paper is classified as being semi-supervised, general purpose, non-monotone and lacking a predefined number of segments. To the best of our knowledge, none of the segmentation algorithms proposed in the literature has such classification.

III. BASIC CONCEPTS

This section addresses concepts and terminologies used in this work. A trajectory is a representation of the spatiotemporal movement of an object. Trajectories are usually collected by tracking devices into discrete samples and represented as a sequence of spatiotemporal points [7]:

Definition 1: A *trajectory sample* is a list of spatiotemporal points $\tau_N = \{tp_0, tp_1, \dots, tp_N\}$, where $tp_i = (x_i, y_i, t_i, \omega_i)$.

A *point feature* (ω_i in Definition 1, is a set of *point features* with $\omega_i = \{p_{f_0}, p_{f_1}, \dots, p_{f_A}\}$) is any numeric information that can be extracted from a trajectory sample and associated to a spatiotemporal point. A *point feature* can be acquired

by a geolocation device (e.g., the instantaneous speed) or calculated using the trajectory sample (e.g., the direction variation between two consecutive points) and is assigned to a single point of the trajectory.

A *segment feature* is any numeric information computed from the *trajectory sample* and associated with a segment (e.g., average or maximal speed). The difference between *point feature* and *segment feature* is that, while the former is static, the latter is more dynamic. Once a point feature information is collected or computed it will not change over time. The *segment features* depend on the segment definition and when the segment is recomputed by adding or removing points, then the *segment feature* has to be recomputed too.

A *semantic label* (or semantic annotation) is any additional semantic and/or contextual information that can be added to a trajectory segment [14]. Such information can be, for example, an activity (e.g., walking, studying or driving) or a behavioral pattern (e.g., foraging or running from a predator). Henceforth, the term label refers to a *semantic label*. A trajectory dataset is called a labeled dataset when its trajectories' segments have been annotated with semantic labels. More formally:

Definition 2: A *labeled trajectory segment* s is a sublist of τ and $s = (tid, sid, \{tp_u, \dots, tp_v\}, semantic\ label, \zeta_{sid})$, where: (i) tid is the trajectory identifier; (ii) sid is the segment identifier; (iii) tp_u, \dots, tp_v represent a sublist of τ_N starting from tp_u and ending at tp_v ($1 \leq u \leq v \leq N$); (iv) *semantic label* is the additional information that characterizes the segment and (v) ζ_{sid} is a list of segment features, with $\zeta_{sid} = \{s_{f_0}, s_{f_1}, \dots, s_{f_B}\}$.

Two more concepts are used in the segmentation algorithm definition to refer to the *representative* points inside a segment and inside a labeled dataset: the *segment landmark* in Definition 3, already introduced in [7] and *semantic landmark* in Definition 4, introduced here for the first time:

Definition 3: A *segment landmark* lm_r is a representative point of a trajectory sample τ_N , where $lm_r = tp_s$ and $1 \leq r \leq s \leq N$, used to represent a trajectory segment in terms of its point features.

A *segment landmark* is a point inside the segment that is chosen to represent the whole segment: it is used as reference point to characterize the behavior of a part of the trajectory. After defining a set of *segment landmarks*, it is possible to create segments by partitioning the points in the neighborhood where each *segment landmark* is defined (i.e. the trajectory's consecutive points respecting a time constraint). The decision of which point to choose as a *segment landmark* depends on a cost function that should be optimized.

Definition 4: A *semantic landmark* $sem_lm = (semantic\ label, \omega_A, \zeta_B)$ is a set that represents a pattern extracted from a labeled dataset consisting of: (i) a *semantic label*; (ii) ω_A is a list of *point features* values; and (iii) a list ζ_B of *segment features* values.

Differently from *segment landmarks* that are decided by the cost function, the *semantic landmarks* are computed from a set of examples given by the user. Example of *semantic landmarks* are segments labeled as *fishing* or *not fishing* for vessels or *foraging* and *traveling* for animals.

IV. SEMANTIC AND SEMISUPERVISED TRAJECTORY SEGMENTATION

This section introduces the novel RGRASP-SemTS process for semantic and semi-supervised trajectory segmentation. This process is summarized in Figure 1 where we specify the process tasks and their input and output. Starting with a set of trajectories, the domain expert labels a subset of them using some criteria (e.g., the activity performed). The first step of the process is the features evaluation step where the features that will be used in the learning phase are generated and selected for a particular domain. This step is detailed later in Section IV-A. The second task is the actual segmentation performed by RGRASP-SemTS. The input parameters of RGRASP-SemTS are: (i) a set of labeled segment examples; (ii) a reactive proportion (rp) to update internal list of parameters values for $minTime$ and α , and (iii) the maximal number of iterations (max_it) to execute RGRASP-SemTS over a trajectory sample. This algorithm and the input parameters are detailed in Section IV-B. Finally, the output of RGRASP-SemTS is a set of semantically segmented trajectories produced in a semi-supervised way by considering both the examples provided by the user (supervised phase) and the similarities computed by the algorithm in the neighborhood of the segments (unsupervised phase).

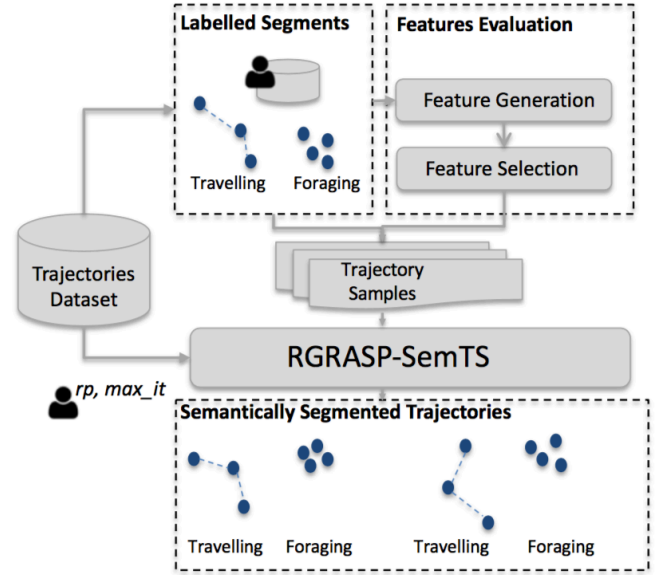


Fig. 1. The semantic and semi-supervised trajectory segmentation process of RGRASP-SemTS

A. Feature evaluation

The feature evaluation follows two steps: (i) the feature generation and (ii) the selection of a subset of features enabling the algorithm to achieve its best performance. In the features generation step, the objective is to create as many features as possible to characterize the behavior of the moving object for each dataset. The features created for each dataset used in the experiments of this work are detailed in Section V-B.

As the number of features can grow very fast, it is necessary to select the most representative point and segment features

to perform the segmentation, and this is the second step of features evaluation. In this work, the Weka package and the filtering χ^2 algorithm [10] were used to select the features. The χ^2 feature selection algorithm evaluates the value of a feature by computing the value of the χ^2 statistic concerning the label. The advantages of this method are that it is fast, scalable and independent from the chosen segmentation algorithm.

B. The RGRASP-SemTS Segmentation Algorithm

Semi-supervised strategies take advantage of both unsupervised and supervised strategies, thus exploiting labeled and unlabeled data. In fact, we want to achieve homogeneity inside a segment using an unsupervised strategy (*segment landmarks*), while obtaining a degree of similarity between the segments using a supervised strategy on a labeled dataset (*semantic landmarks*). The properties we want to optimize in the segments (e.g., *minimal distortion* and *maximal compression*), previously presented in [7], and the extended cost functions we use in this work are discussed below.

1) *Desirable properties and Cost function definition*: In this work, achieving *minimal distortion* in a trajectory segmentation task is to achieve as much homogeneity as possible inside the trajectory segments regarding its *point* and *segment features*. On the other hand, achieving *maximal compression* for the trajectory segments means that the resulting segments (i.e. number of *segment landmarks*) should be as few as possible and as similar as possible to a *semantic landmark* extracted from the labeled dataset.

The concepts of *maximal compression* and *minimal distortion* are inversely correlated since when one increases, the other decreases. For example, selecting all the spatiotemporal points as segment landmarks naturally decrease the *minimal distortion* increasing the *maximal compression* since many segment landmarks will be chosen. Conversely, choosing one point as a segment landmark for the entire trajectory lowers *maximal compression*, but increases the distortion produced by the segmentation since a single segment landmark will be compared to all the points of the trajectory. As these concepts are inversely correlated, it is necessary to define a function that represents the trade-off between them. We propose to use the MDL principle to compute this trade-off as detailed below.

To achieve homogeneity inside a trajectory segment we use Equation 1 which represents a Euclidean distance between the trajectory *point features* (ω_A) of two points tp_1 and tp_2 . In Equation 1, ω_{1_i} represents the *i-th point feature* value of tp_1 and ω_{2_i} the *i-th point feature* value of tp_2 .

$$sim_{tf}(\omega_1, \omega_2) = \sqrt{\sum_{i=1}^A (\omega_{1_i} - \omega_{2_i})^2} \quad (1)$$

The *segment cohesiveness* is shown in Equation 2 and measures the similarity between the *point features* of a chosen *segment landmark* ω_{lm} and all the points between tp_u and tp_v (ω_k).

$$S_Cohe(\omega_{lm}, \{\omega_u, \dots, \omega_v\}) = \sum_{k=u}^v sim_{tf}(\omega_{lm}, \omega_k) \quad (2)$$

As *segment feature* is a new concept defined in this work and as it is necessary to compare the *segment features* of different segments, Equation 3 defines a similarity between the *segment features* (ζ) of two segments s_1 and s_2 , where ζ_{1_i} represents the *i-th segment feature* of s_1 and ζ_{2_i} represents the *i-th segment feature* of s_2 .

$$sim_{sf}(\zeta_1, \zeta_2) = \sqrt{\sum_{i=1}^B (\zeta_{1_i} - \zeta_{2_i})^2} \quad (3)$$

In the MDL theory, the best model is the one that minimizes the result of $L(H) + L(D|H)$ [5]. In this work, the hypothesis H consists of choosing an optimal set of *segment landmarks* that are more similar to the *semantic landmarks* included in the labeled dataset and also contains high homogeneity rates in its neighborhood. Finding the optimal set of *segment landmarks* reflects the decision of finding the best hypothesis according to the MDL principle. It is crucial also to consider the use of unsupervised and supervised data in both $L(H)$ and $L(D|H)$.

Given a *trajectory sample* $\tau_N = (tp_1, tp_2, \dots, tp_N)$, a set of *segment landmarks* $\phi_T = \{lm_1, lm_2, \dots, lm_T\}$, a set of *semantic landmarks* $\lambda_V = \{s_lm_1, s_lm_2, \dots, s_lm_V\}$, and a set of *trajectory segments* $\theta_T = \{s_1, s_2, \dots, s_T\}$, the cost function is formally defined as follows.

The cost of the hypothesis ($L(H)$) is computed by comparing, regarding their point features: (i) the chosen consecutive *segment landmarks* (unsupervised measure); and (ii) each *segment landmark* to the most similar *semantic landmark* found in the labeled dataset (supervised measure). Equation 4a represents the cost of encoding a hypothesis of a *trajectory sample* τ_N when a set ϕ_T of *segment landmarks* are chosen. If T is equal to 1, $L(H) = 0$. Otherwise, Equation 4a is used. The *max* represents the maximum possible similarity between two *trajectory features*. The first part of Equation 4a represents the unsupervised measure (Equation 4b) that takes into account the unlabeled data. This value will decrease when the consecutively chosen *segment landmarks* are dissimilar; hence, this Equation identifies less similar movement behaviors by comparing the current segment to the next one. The second part of the $L(H)$ function (Equation 4c), which stands for the supervised measure, computes the similarity between the chosen *segment landmark* and the closest *semantic landmark* regarding their point features.

$$L(H) = Uns\ L(H)(\phi_T) + Sup\ L(H)(\phi_T, \lambda_V) \quad (4a)$$

$$Uns\ L(H) = \log_2(1 + \sum_{j=1}^{T-1} max - sim_{tf}(\omega_{lm_j}, \omega_{lm_{j+1}})) \quad (4b)$$

$$Sup\ L(H) = \log_2(1 + \sum_{j=1}^T \arg \min_{i \in [1, V]} sim_{tf}(\omega_{lm_j}, \omega_{s_lm_i})) \quad (4c)$$

The $L(D|H)$ cost function, representing the cost of bits for encoding a dataset D when testing a hypothesis H , is defined in Equation 5a. The cost of encoding a dataset given a hypothesis ($L(D|H)$) is computed by comparing: (i) the

segment cohesiveness (Equation 2) between all the points of each segment ($\{\omega_u, \dots, \omega_v\}_k$) and its respective *segment landmark* (ω_{lm_k}) in terms of *point features* values; and (ii) the *segment features* similarity (Equation 3) between each segment found and the more similar *semantic landmark*. The first part of Equation 5a is the unsupervised measure (Equation 5b) that will compare the chosen *segment landmark* of each segment with all *point features*' values inside this segment. This value increases when fewer segments are found and decreases when more segments are found. The supervised measure of our $L(D|H)$ is shown in Equation 5c. Each segment θ_T found is compared to all *semantic landmarks* of the set λ_V and the closest one is selected. This is the part of the cost function where semantic enrichment is performed. Since the unsupervised measure of $L(D|H)$ (Equation 5b) compares all the *point features*' values of each segment with the respective *segment landmark*, it is necessary to multiply this similarity by the number of points located inside this segment ($|s_k|$) and subtract one, since the *segment landmark* is a point of the segment and the similarity between them is equal to 0. If such approach is not adopted, the $L(D|H)$ value will consider the unsupervised measure more costly when compared to the supervised measure since greater similarity costs would be computed.

$$L(D|H) = Uns L(D|H)(\theta_T) + Sup L(D|H)(\phi_T, \lambda_V) \quad (5a)$$

$$Uns L(D|H) = \log_2(1 + \sum_{k=1}^T SCohe(\omega_{lm_k}, \{\omega_u, \dots, \omega_v\}_k)) \quad (5b)$$

$$Sup L(D|H) = \log_2(1 + \sum_{k=1}^T \arg \min_{i \in [1, V]} sim_{sf}(\zeta_{sl_i}, \zeta_{s_k}) * |s_k|) \quad (5c)$$

2) *The Algorithm*: In this section, we present the algorithm RGRASP-SemTS. Two issues must be considered: (i) the number of segments that makes the cost function minimum is not known *a priori*; (ii) switching the *segment landmarks* implies that the segment configuration will also be affected, since the cost function value must be recomputed every time a modification in the set of *segment landmarks* is performed. To manage these issues, we adopt the *Reactive Greedy Randomized Adaptive Search Procedure* (RGRASP) meta-heuristic[15], aiming at determining the number of segments and the boundaries between the consecutive segments.

RGRASP-SemTS is detailed in Algorithm 1. The trajectory τ_N to be segmented is read in Line 1. In Line 2, the algorithm extracts a *semantic landmark* for each type of *semantic label* that must be found by finding the average of each *point* and *segment feature* contained in the segment examples considering the semantic label. Lines 3 and 4 initialize $minTime_{list}$ and α_{list} for possible values for $minTime$ and α using equal width binning. In the case of α_{list} , the minimum and maximum values are predetermined and range from 0.1 to 0.6. These values were determined because, for values below 0.1, the algorithm chooses the same *segment landmarks* in each iteration. For values above 0.6, the *segment landmarks* chosen by RGRASP-SemTS were completely random. From

Algorithm 1 RGRASP-SemTS

Input: A set of segment examples $\psi_E = (ex_1, ex_2, \dots, ex_T)$
A reactive proportion value rp
A number of iterations max_it
Output: A set of semantically enriched segments $\theta_T = (s_1, s_2, \dots, s_T)$

- 1: $\tau_N \leftarrow$ read trajectory data;
- 2: $\lambda_V \leftarrow$ extract all semantic landmarks from examples ψ_E ;
- 3: $minTime_{list} \leftarrow$ initialize the $minTime$ values;
- 4: $\alpha_{list} \leftarrow$ initialize the α values;
- 5: **for** $k = 1 \rightarrow max_it$ **do**
- 6: $minTime \leftarrow$ randomly select from $minTime_{list}$;
- 7: $\alpha \leftarrow$ randomly select from α_{list} ;
- 8: $\theta_T \leftarrow$ Greedy Randomized Construction Procedure(τ , $minTime$, α, λ_V);
- 9: $\theta_T \leftarrow$ Local Search Procedure(θ_T , $minTime, \lambda_V$);
- 10: Update Best Solution(θ_T , Best θ_T);
- 11: **if** $mod(k, rp) == 0$ **then**
- 12: Update $minTime_{list}$ and α_{list} probabilities;
- 13: **end if**
- 14: **end for**

return Best θ_T ;

Lines 5 to 14, max_it iterations are executed aiming at building and evaluating different segmentations. Values for α and $minTime$ are randomly selected from the lists α_{list} and $minTime_{list}$ (Lines 6 and 7). Then, a first feasible solution (θ_T segments) is built by executing the procedure shown in Algorithm 2 (Line 8). After building the first set of feasible segments θ_T , Local Search Procedure (Algorithm 3) is applied to optimize the segments (Line 9) locally. RGRASP-SemTS (Algorithm 1) verifies if the new set of optimized segments θ_T is the best one found by evaluating the cost according to the MDL function (Line 10). If the cost of these segments is lower, it updates the set of best segments (Best θ_T).

The *reactive* part of this algorithm is concluded by updating the probabilities of $minTime_{list}$ and α_{list} (Lines 11 to 13). If the modulo (mod) of the multiplication between it and rp is equal to 0, the probabilities of α_{list} and $minTime_{list}$ are updated using Equation 6 [15]. Equation 6 (a) determines the probability of selecting a determined value of α_{list} or $minTime_{list}$. Equation 6 computes the values for p_i (i.e. probability of selecting an element of the α_{list} or $minTime_{list}$) when all values for q_i are established. This is achieved by dividing each value of q_i by the total sum of all q_i s.

$$q_i = \left(\frac{\text{best mdl value found}}{\text{average mdl value for } i^{th} \text{ element of the list}} \right)^{10} \quad (6a)$$

$$p_i = q_i / \sum_{j=1}^m q_j \quad (6b)$$

Finally, Algorithm 1 returns the best set of semantically enriched segments (Best θ_T) found by max_it iterations. The procedure for building the initial solutions (Algorithm 2) of the RGRASP-SemTS is explained as follows.

Algorithm 2 Greedy Randomized Construction Procedure

Input: A set of points ordered by time $\tau_N = (tp_1, tp_2, \dots, tp_N)$
 A minimum time threshold $minTime$
 An α threshold to define the amount of greediness of the construction algorithm
 A λ_V set of semantic landmarks

Output: A set of semantically enriched segments $\theta_T = (s_1, s_2, \dots, s_T)$

- 1: **while** $candidate_{list}$ is not empty **do**
- 2: $RCL_{list} \leftarrow$ add points of $candidate_{list}$ from index 0 to RCL_{size} ;
- 3: $candidate \leftarrow$ randomly select a point from RCL_{list} ;
- 4: $semanticLandmark \leftarrow$ get the most similar semantic landmark from λ_V in terms of point features;
- 5: $segment \leftarrow$ add $candidate$;
- 6: **while** $minTime$ threshold condition not satisfied **do**
- 7: $best_neighbor \leftarrow$ evaluate left and right neighbor;
- 8: $segment \leftarrow best_neighbor$;
- 9: **end while**
- 10: $\theta_T \leftarrow$ add $segment$;
- 11: remove from $candidate_{list}$ unfeasible points;
- 12: sort points of $candidate_{list}$ according to the closer semantic landmark in terms of point features;
- 13: **end while**
return θ_T ;

Algorithm 2 starts in Line 1 by considering all points as candidate *segment landmarks* ($candidate_{list}$). In the initialization of all GRASP-based algorithms, the creation of a restricted candidate list (RCL) is necessary. This list is used to manage the amount of greediness of the initialization method that is determined by the parameter α . This procedure is executed until all points in $candidatePoints_{list}$ are considered landmarks (Lines 2 to 15). In this work, the RCL is built by sorting all points inside τ according to its distance (Equation 1) to the closest *semantic landmark* regarding the point features values (Line 1). The size of the RCL (RCL_{size}) is determined by multiplying the size of the $candidate_{list}$ by the value of α , thereby creating a variable RCL_{list} with all points spanning from the first element of the $candidate_{list}$ to the position determined in RCL_{size} . Afterward, a point from the RCL_{list} is randomly chosen as *candidate segment landmark* (Line 3) and the closest *semanticLandmark* for this point is chosen by computing the trajectory features distance (Equation 1) between this *candidate* and all *semantic landmarks* of the set ψ_V (Line 4).

A new *segment* is created in Line 5 with the initial point being the *candidate* and its *semantic label* being the one determined by the *semanticLandmark* (Line 8). From Lines 6 to 9, the size of the *segment* is increased by adding points to the segment's neighborhood (respecting the chronological order) until the time threshold ($minTime$) is reached. This is done by determining the most suitable neighbor in terms of *point features'* values (i.e. $segment_{u-1}$ and $segment_{v+1}$) of the *segment* (Line 7) and adding this *bestNeighbor* to the *segment* (Line 8). When *segment* contains at least the

$minTime$ threshold, this *segment* is added to the set θ_T (Line 10). After, all points of the *segment* (Line 10) and the neighborhoods that could not be used to build a feasible segment regarding the time constraint (Line 11) are removed from the $candidate_{list}$. After removing all these points, the $candidatePoints_{list}$ is re-sorted (Line 12), and the same procedure is applied until there are no candidate points in this list. Subsequently, all points that were not assigned to a segment are placed in the neighbor segment (segment in the point's right or left). From that point on, the algorithm detects which position, among a set of consecutive points that had not been assigned to a segment, is the best one - that is, the one which reduces the cost function. These points are then added to the respective segment (i.e., a segment on the left or the right) whose cost function was minimized. Finally, feasible and semantically enriched θ_T segments are returned.

Algorithm 3 Local Search Procedure

Input: A set of semantically enriched segments $\theta_T = (s_1, s_2, \dots, s_T)$
 A minimum time threshold $minTime$
 A ψ_V set of semantic landmarks

Output: A set of optimized semantically enriched segments $optimized_theta_R = (s_1, s_2, \dots, s_T)$

- 1: $optimized_theta_R \leftarrow \{\}$;
- 2: $c_segment \leftarrow \theta_0$;
- 3: $p_sem_label \leftarrow c_segment_{label}$;
- 4: **for** $i = 1 \rightarrow T$ **do**
- 5: **if** $p_sem_label \neq \theta_i$'s semantic label **then**
- 6: update segment landmark of $c_segment$;
- 7: $optimized_theta \leftarrow$ add $c_segment$;
- 8: $p_sem_label \leftarrow c_segment_{label}$;
- 9: $c_segment \leftarrow \theta_i$;
- 10: **else**
- 11: $current_segment \leftarrow$ insert all points from θ_i ;
- 12: **end if**
- 13: **end for**
- 14: **for** $i = 0 \rightarrow R - 1$ **do**
- 15: $bpp \leftarrow$ Find the best position to partition points between $index_{lm_1}$ and $index_{lm_2}$;
- 16: $optimized_theta_i \leftarrow$ create segment from $optimized_theta_i$'s first index position to bpp ;
- 17: $optimized_theta_{i+1} \leftarrow$ create segment from $bpp + 1$ to $optimized_theta_{i+1}$'s last index;
- 18: update segment landmark of $optimized_theta_i$ and $optimized_theta_{i+1}$;
- 19: **end for**
return $optimized_theta_R$;

The procedure to locally optimize the initial solution (Algorithm 3) of the RGRASP-SemTS is explained as follows. Line 1 initializes a list of optimized segments named $optimized_theta_R$ that will be the output of this procedure. Lines 2 and 3 initialize the current segment ($c_segment$) to be analyzed with all the points contained in θ_0 and stores this segment's semantic label in p_sem_label .

The objective of lines from 4 to 13 is to merge segments with the same *semantic labels*. For all the remaining segments

θ_T , if the consecutive labels (i.e., labels from the previous segment and the current) are not equal (Line 5), the algorithm updates the $c_segment$'s *segment landmark* (Line 6), adds this segment to the output list of segments $optimized_theta$ (Line 7), sets the previous *semantic label* as the actual one in the current segment (Line 8), and finally sets $c_segment$ as being equal to θ_i (Line 9). If the p_sem_label is equal to the θ_i 's *semantic label*, all points from θ_i are added to the $c_segment$ (Line 10).

From Lines 14 to 19, Algorithm 3 optimizes the MDL based cost function $L(H) + L(D|H)$. The optimization is carried out by finding the best partitioning position (bpp) between the consecutive segments on the set $optimized_theta$ (Line 15). This method verifies for all points between consecutive *segment landmarks*, which one causes a sharper decrease in the MDL-based cost function result, and considers this position as the local optimum for these successive segments. The $optimized_theta_i$ and $optimized_theta_{i+1}$ boundaries in Lines 16 and 17 are updated, as well as their *segment landmarks* in Line 18. Finally, a set of $optimized_theta_R$ is returned by this procedure.

Since RGRASP-SemTS works with distances, the standardization of the data is a crucial step because features can have different variances. Indeed, when there is a feature with a very high variance, the distances computed between the features will be greater than the distances computed for features with smaller variances. This difference would impact the RGRASP-SemTS by raising the cost of the features with higher variances and decreasing the cost of features with lower variances. In this work, each feature was normalized using the well-known statistical method known as *standard score*. This method produces a dimensionless number that is obtained by subtracting a raw value from the mean and then, dividing this difference by the standard deviation.

At this point, the complexity analysis of the RGRASP-SemTS is explained. The complexity of the construction procedure (Algorithm 2) is defined by the *while* structure from Lines 2 to 17. This structure has a complexity of $O(N)$, and it evaluates, for each point from the trajectory τ_N , the possibility of it being selected as a segment landmark. When these lines are executed, every time a new segment is created, points from the list of candidate points ($candidatePoints_{list}$) are removed in Lines 14 or 15. At maximum, all the points from trajectory τ_N could be selected as segment landmarks to generate segments. The complexity of the local optimization procedure (Algorithm 3) is defined by the *for* structure from Lines 13 to 21. Observe that the θ_R segments evaluated by Algorithm 3 contain all the points from τ_N . Note also that all the possibilities for partitioning the N points between two consecutive *segment landmarks* are analyzed, determining a complexity of $O(N)$ for Algorithm 3. Finally, the RGRASP-SemTS (Algorithm 1) complexity is defined as $O(N * max_it)$. It results from the multiplication of Lines 7 or 8 and the number of iterations the algorithm executed (max_it), since all the previous Lines of this algorithm have lower complexities.

V. EXPERIMENTS

This section details the experiments performed in this work and is organized as follows. Section V-A presents the datasets and evaluation metric, while Section V-B details the features evaluation. Finally, Section V-C compares the semantically enriched segments generated by RGRASP-SemTS with other state-of-the-art supervised and unsupervised algorithms.

A. Datasets and evaluation metric

We used two real world datasets: (i) the Atlantic hurricane track dataset and (ii) tracked grey seals dataset.

The Atlantic hurricane track dataset¹ contains information regarding hurricanes collected from 2000 to 2012 and it was divided into segments labeled *low intensity* hurricanes (e.g., surface wind ≤ 63 knots) and *high intensity* hurricanes (e.g., surface wind > 64 knots). Trajectories with less than 20 points were discarded to avoid the segmentation of very small trajectories and because most of them only contained the semantic label *low intensity*.

The grey seals dataset contains information regarding seals' trajectories collected from Argos satellite tags deployed from Sable Island, Nova Scotia, Canada. This dataset contains segments with labels *foraging* and *traveling*, assigned by domain specialists [3].

In the experiments we evaluate the segments generated by the segmentation algorithms using the Area Under the Curve (AUC) of the Receiver Operating Characteristic (ROC) analysis. The *semantic label* was registered for each *trajectory point* of all datasets with the ground truth in the datasets used in the experiments. The ground truth is the data classification stored in the database by domain specialists, and it is used to validate the segmentation results. This validation aims at verifying if the assignment of the *semantic label* to each point of the segment done by a segmentation algorithm is correct. Thanks to this information, it is possible to build the confusion matrix of the ROC analysis and compute the AUC.

B. Features evaluation tests

The first step of the features evaluation is the features generation. This step is very important for RGRASP-SemTS because many *point* and *segment features* can be generated from trajectory raw data and relevant features are unknown *a priori* for a given domain. The key idea is to generate a large set of *point* and *segment features* and verify in a subsequent step which of them better characterizes a *semantic label*.

For the hurricanes dataset, we generated as *point features*: the maximum sustained surface wind at six-hour intervals, the estimated speed in meters per second and the direction variation between points from 0 to 180 degrees. For *segment features*, we computed: average, minimum and maximum values of surface wind, estimated speed, and direction, the ground distance between the first point and the last point of the segment and the elapsed time for each segment. For the grey seals dataset, the *point features* extracted were the depth, the distance from the shore in km, and a binary column

¹<http://weather.unisys.com/hurricane/atlantic/>

indicating whether the seal was near the shore using a distance threshold of 15km, estimated speed, and direction variation. For *segment features*, we computed: average, minimum and maximum values of all the 5 point features and the ground distance between the first point and the last point of the segment and the elapsed time for each segment.

Finally, for the features selection we used the feature ranking method χ^2 [10] implemented in the Weka [6] package. We selected the best set of features, by analyzing the RGRASP-SemTS's performance in terms of AUC values. In particular, five trajectories were randomly selected, and their segment features were extracted. Sequentially, an ARFF file (the Weka input format) was generated, containing the acquired information. It is worth noticing that we used here only segment features due to a Weka package limitation since this software only allows the representation of each labeled segment as a single example. The χ^2 algorithm has been executed, and stored the rank of each segment feature. Subsequently, we executed RGRASP-SemTS with the maximum number of features, and stored the AUC value. Finally, the last ranked segment feature from the χ^2 was removed and the AUC value measured once again. The procedure was repeated until only one segment feature remained.

Figures 2(a) and 2(b) show the AUC performance of the RGRASP-SemTS using this approach. It is worth noticing that, for the hurricane dataset, 3 segment features (e.g., average, minimum and maximum surface wind) have generated the best result in terms of AUC value (0.9545). For the grey seals dataset, 8 segment features (e.g., average, maximum and minimum direction variation, maximum and minimum speed and the distance between the first and last point of the segment) have produced the best AUC performances, which was 0.9101.

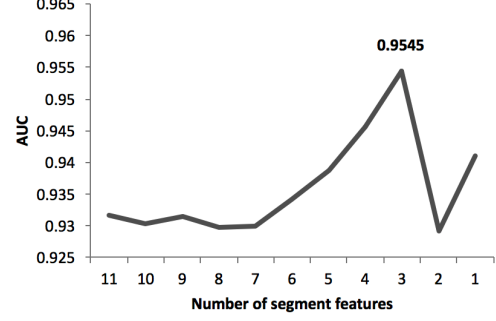
Based on these results, the decision was to use three *segment features* and the *point feature* surface wind for the hurricane dataset. For the grey seals dataset, the decision was to use the eight *segment features* and the estimated speed and direction variation as *point features*.

C. Evaluating RGRASP-SemTS

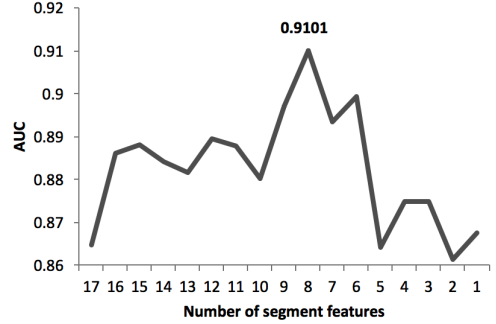
This section evaluates the performance of the RGRASP-SemTS when compared to other approaches from the literature. Section V-C1 compares RGRASP-SemTS's execution time to the unsupervised approach GRASP-UTS. Finally, in Section V-C2, the performance of RGRASP-SemTS is compared with other state-of-art algorithms.

1) *Runtime analysis of RGRASP-SemTS*: In this section we evaluate the execution time of RGRASP-SemTS by comparing with the unsupervised version GRASP-UTS. The objective is to show how the information provided by the user improves the execution time when compared to the unsupervised GRASP-UTS. In this experiment, one trajectory of each dataset was randomly selected, and both the RGRASP-SemTS and the GRASP-UTS were executed one hundred times (100 iterations). A *minTime* value was used for both algorithms (12 hours for both datasets), and a full search (partitioning factor input parameter for GRASP-UTS) was ensured for both algorithms.

Fig. 2. Learning curve for the features selection via χ^2 method.



(a) Learning curve for the hurricanes dataset.



(b) Learning curve for the grey seals dataset

Figure 3(a) and Figure 3(b) summarize the results. For the hurricanes dataset, on average, the RGRASP-SemTS was 0.064 seconds faster than GRASP-UTS, while it was 6.7 seconds faster for the grey seals dataset. After one hundred iterations, it is possible to notice that 1 second was saved for executions of the hurricane dataset and 600 seconds were saved for the grey seal dataset. It is important to observe that this difference is probably because the hurricanes' trajectories are smaller in point length (between 80 and 140 points), while the grey seals' trajectories contain more points to be evaluated (each trajectory contains more than 1000 points).

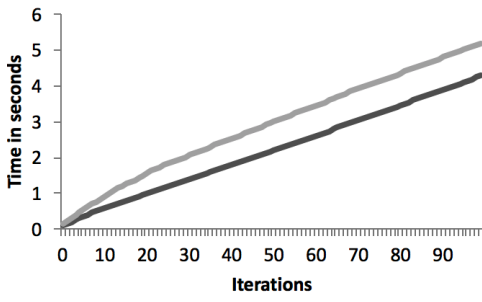
Although RGRASP-SemTS and GRASP-UTS have the same complexity $O(N * max_it)$, the runtime difference between them is a result of the necessary time for the GRASP-UTS to re-build all the solution when landmarks are modified (i.e. inserted, removed or had positions switched). Since RGRASP-SemTS uses some information provided by the user, fewer modifications in the segments are made when an iteration is executed.

2) *Comparison of RGRASP-SemTS with state-of-art algorithms*: This section presents a performance comparison assessed in terms of AUC between RGRASP-SemTS and other state-of-art unsupervised (GRASP-UTS [7] and WK-Means [9]) and supervised (e.g., CB-SMoT [11] and SPD [20]) segmentation algorithms.

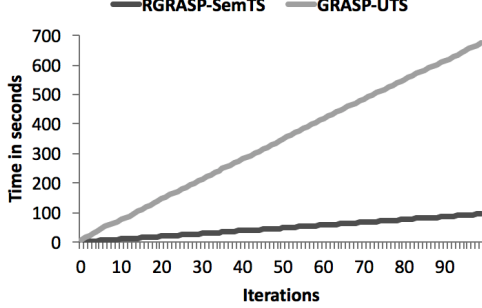
The objective was to evaluate the performance of the algorithms when only small amount of data are available for training therefore we limit the analysis to one sub-dataset. We divided both the hurricanes and grey seals dataset into 10 subsets.

The RGRASP-SemTS was executed in the testing set, using

Fig. 3. Execution time analysis of RGRASP-SemTS



(a) Time analysis for the hurricanes dataset.



(b) Time analysis for the grey seals dataset

as input for the segment landmarks the labeled examples contained in the *training set*. For the other algorithms, parameters' values estimated in the training set were used in the testing set. This procedure was repeated using each single sub-dataset as the training set and tested in the remaining pieces of data. We computed the AUC values using all single sub-datasets as training data and executing the algorithms on the best set of input parameters' values found for each method in the test dataset. We computed an average AUC value (avg. AUC) for all the combinations of training and testing datasets.

Tables I and II show the results obtained by all methods, where one sub-dataset was used to train the algorithms and the remaining 9 sub-datasets were used to test the average AUC. We verified whether any substantial difference existed between the means obtained by RGRASP-SemTS and the means obtained by the other algorithms using a *paired t-test*. A confidence level of 5% with 9 degrees of freedom was required to determine that the differences between the means are significant. If the *t-value* computed by the RGRASP-SemTS and the other algorithms is greater than 2.82, the evidence that the means are equal is rejected, allowing to draw the conclusion that there is a substantial evidence that the two algorithms had significant differences in their performances.

Table I shows the results of the comparison between RGRASP-SemTS and the other algorithms.

For the hurricane dataset, RGRASP-SemTS had the best average AUC performance achieving 0.94. Compared to the unsupervised algorithms GRASP-UTS and WK-Means, which achieved an average AUC of 0.81 and 0.87 for testing, respectively, the RGRASP-SemTS offers an improvement of at least 0.06 in terms of average AUC. The differences in the

TABLE I
COMPARISON OF UNSUPERVISED, SUPERVISED AND SEMI-SUPERVISED ALGORITHMS FOR THE HURRICANES DATASET.

Algorithm	avg. AUC	t-score	mean difference
RGRASP-SemTS	0.94	-	-
GRASP-UTS	0.81	22.51	0.13
WK-Means	0.87	14.04	0.06
CB-SMoT	0.47	136.13	0.47
SPD	0.45	130.39	0.48

mean AUC are significant since the *t-score* was higher than 2.82, amounting to 22.51 when compared to GRASP-UTS and 14.04 when compared to the WK-Means. It is important to point out that the WK-Means algorithm received exactly the number of segments that should be found on each trajectory, while the RGRASP-SemTS did not. When compared to the supervised methods named CB-SMoT and SPD, the gains were at least 0.47 in terms of avg. AUC.

For the grey seal dataset, RGRASP-SemTS also achieved the best average AUC performance, as depicted in Table II. When RGRASP-SemTS is compared to GRASP-UTS, gains of 0.08 in were obtained. This difference has significance since the *t-score* was 14.08 (higher than 2.82). The difference between RGRASP-SemTS and WK-Means were 0.07 on average AUC in testing. This difference also has a significance, as the *t-score* was 6.23. When compared to the supervised methods, namely CB-SMoT and SPD, gains of at least 0.37 of average AUC were obtained.

TABLE II
COMPARISON OF UNSUPERVISED, SUPERVISED AND SEMI-SUPERVISED ALGORITHMS FOR THE GREY SEALS DATASET.

Algorithm	avg. AUC	t-score	mean difference
RGRASP-SemTS	0.88	-	-
GRASP-UTS	0.80	14.08	0.08
WK-Means	0.81	6.23	0.07
CB-SMoT	0.19	128.69	0.69
SPD	0.53	74.38	0.35

VI. CONCLUSIONS

The research field of trajectory segmentation, although well studied in the literature, has not explored the concept of semi-supervised learning deeply: the use a small set of segments labeled by the user combined with an unsupervised segmentation driven by the training set. The objective is to achieve high accuracy even when few labeled examples are available. This is particularly useful for segmenting trajectories based on semantics.

This paper gives a contribution in this direction since it proposes RGRASP-SemTS, a reactive and semi-supervised algorithm for semantically segmenting trajectory data. This algorithm exploits labeled and unlabeled data to find an optimal segmentation of a trajectory by modifying segment landmarks

to achieve homogeneity in the segments using a cost function based on the MDL principle. We performed experiments with two real-world datasets to assess the effectiveness of our approach. The results show that the proposed algorithm outperforms the state-of-art competitors. We intend to extend this work towards several directions. For example we can improve the overall performance by generating better sets of semantic landmarks, instead of just computing averages.

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