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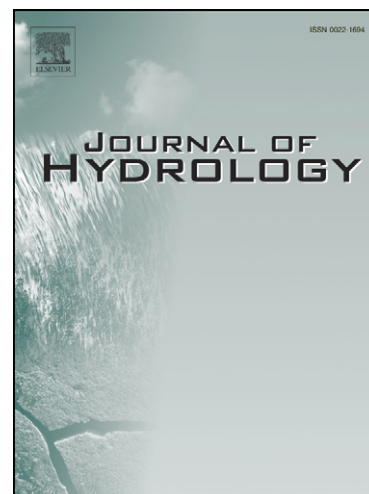
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**Sobol's sensitivity analysis for a distributed hydrological  
model of Yichun River Basin, China**

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21 **Abstract**

22 This paper aims to provide an enhanced understanding of the parameter sensitivities  
23 of the Soil and Water Assessment Tool (SWAT) using a variance-based global  
24 sensitivity analysis, i.e., Sobol's method. The Yichun River Basin, China, is used as a  
25 case study, and the sensitivity of the SWAT parameters is analyzed under typical dry,  
26 normal and wet years, respectively. To reduce the number of model parameters, some  
27 spatial model parameters are grouped in terms of data availability and multipliers are  
28 then applied to parameter groups, reflecting spatial variation in the distributed SWAT  
29 model. The SWAT model performance is represented using two statistical metrics -  
30 Root Mean Square Error (RMSE) and Nash-Sutcliffe Efficiency (NSE) and two  
31 hydrological metrics – RunOff Coefficient Error (ROCE) and Slope of the Flow  
32 Duration Curve Error (SFDCE). The analysis reveals the individual effects of each  
33 parameter and its interactions with other parameters. Parameter interactions contribute  
34 to a significant portion of the variation in all metrics considered under moderate and  
35 wet years. In particular, the variation in the two hydrological metrics is dominated by  
36 the interactions, illustrating the necessity of choosing a global sensitivity analysis  
37 method that is able to consider interactions in the SWAT model identification process.  
38 In the dry year, however, the individual effects control the variation in the other three  
39 metrics except SFDCE. Further, the two statistical metrics fail to identify the SWAT  
40 parameters that control the flashiness (i.e., variability of mid-flows) and overall water  
41 balance. Overall, the results obtained from the global sensitivity analysis provide an  
42 in-depth understanding of the underlying hydrological processes under different  
43 metrics and climatic conditions in the case study catchment.

44

45 **Keywords** Climate conditions; Sensitivity analysis; Hydrological modeling; Sobol's

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## 47 1. Introduction

48 Distributed hydrological models have gained increasing attention in recent years due  
49 to the increasing availability of spatially distributed data and advances in computing  
50 power (Beven and Kirkby, 1979; Abbott et al., 1986; Boyle et al., 2001; Panday and  
51 Huyakorn, 2004; Duffy, 2004). These models have been applied to advance scientific  
52 understanding of underlying hydrological processes, analyse the potential impacts of  
53 land use and climate change, and develop water quantity and quality management  
54 options for informed decision making (e.g., Beven and Binley, 1992; Tang et al.,  
55 2007a).

56 The Soil and Water Assessment Tool (SWAT) is a particular example of complex,  
57 spatially distributed hydrological models (Arnold et al., 1993). To determine the most  
58 influential parameters of a SWAT model, the Latin Hypercube-One factor At a Time  
59 (LH-OAT) algorithm is often applied, as this method is incorporated in SWAT (van  
60 Griensven et al., 2006). The LH-OAT method provides an estimation of the  
61 parameters' ranking according to their influence on the model output. However, it  
62 does not provide an estimation of the proportion of the total influence that one  
63 parameter has on the output, nor its interactions with other parameters. Therefore, this  
64 method might not be able to identify some influential parameters, whose effects are  
65 mainly from interactions with other parameters.

66 Sobol's method is a global sensitivity analysis method and is able to provide the  
67 impacts of each parameter and its interactions with other parameters on the model  
68 output (Sobol', 1993). Recently Sobol's method has become increasingly popular in  
69 hydrological modeling due to its ability to incorporate parameter interactions and the  
70 relatively straightforward interpretation of its indices (e.g., Pappenberger et al., 2008;  
71 van Werkhoven et al., 2008; Yang, 2011; Fu et al., 2012). Tang et al. (2007b)

72 comprehensively compared Sobol's method with three other sensitivity analysis tools  
73 including the Parameter Estimation Software (PEST) (Doherty, 2004), Regional  
74 Sensitivity Analysis (RSA) (Young, 1978; Hornberger and Spear, 1981), and Analysis  
75 of Variance (ANOVA) (Neter et al., 1996; Mokhtari and Frey, 2005). They found that  
76 Sobol's method is the most effective approach to globally characterize single- and  
77 multi-parameter interactive sensitivities for lumped watershed models. Build on this  
78 prior study, Tang et al. (2007a) used Sobol's method to a distributed hydrological  
79 watershed model termed as the Hydrology Laboratory Research Distributed  
80 Hydrologic Model (HL-RDHM), and the sensitivity analysis results obtained  
81 demonstrated that the method provides robust sensitivity rankings and that these  
82 rankings could be used to significantly reduce the number of parameters when  
83 calibrating the HL-RDHM. Further, Wagener et al. (2009) highlighted the importance  
84 of using multiple performance metrics to analyse the sensitivities of a distributed  
85 hydrological model using the Sobol's method.

86 More recently the Sobol's sensitivity analysis method has been applied to SWAT  
87 (e.g., Cibin et al., 2009; Nossent et al., 2011). Cibin et al. (2009) used Sobol's method  
88 to analyse the sensitivities of SWAT models for two watersheds with different climatic  
89 settings and flow regimes, by considering each parameter's individual contribution  
90 (first order index) and the total contribution (total order index) to the model output in  
91 terms of two commonly used statistical metrics, i.e., Root Mean Square Error (RMSE)  
92 and Nash-Sutcliffe Efficiency (NSE). The results indicated that modeled stream flows  
93 show varying sensitivity to parameters in different climatic settings and flow regimes.  
94 Nossent et al. (2011) presented a Sobol's sensitivity analysis for a SWAT model of the  
95 Kleine Nete River watershed, Belgium, by analyzing the first order, second order and  
96 total sensitivity effects of model parameters on one single model performance metric -

97 NSE. The results indicated that the curve number factor is the most important  
98 parameter of the model and that no more than 9 parameters (out of 26) are needed to  
99 have an adequate representation of the model variability. It is also shown that there are  
100 significant interactions between three pairs of variables, which otherwise cannot be  
101 revealed by other methods only analyzing the impacts of individual parameters. The  
102 prior researches have demonstrated the benefits of Sobol's method in identification of  
103 SWAT models, but are limited in analyzing multiple model performance metrics (such  
104 as hydrological metrics) and discussing the detailed interactions between model  
105 parameters.

106 In this paper, Sobol's method is used to perform a detailed sensitivity analysis  
107 for a SWAT model of Yichun River Basin, China, by analyzing the individual effects  
108 of each parameter and its interactions with other parameters on the model output  
109 regarding four different metrics: RMSE, NSE, runoff coefficient error (ROCE) and  
110 slope of the flow duration curve error (SFDCE). Further, the model parameter  
111 sensitivities are evaluated for wet, moderate, and dry years with the intent of  
112 identifying the key parameters and parameter interactions under different climate  
113 conditions. The results from this study provide an in-depth understanding of the  
114 sensitivity of the SWAT parameters and highlight the significance of the interactions  
115 between model parameters. In addition, this paper also shows the effectiveness of the  
116 variance-based Sobol's method in sensitivity analysis of SWAT models.

117

## 118 **2. Methodology**

### 119 **2.1 Overview of SWAT Model**

120 The SWAT model is a catchment-scale distributed hydrological model developed by  
121 the Agricultural Research Service of the United States Department of Agriculture

122 (Arnold et al., 1998). The model is based on physical processes and is capable of  
123 continuous simulation over long time periods. SWAT was developed with an aim to  
124 predict the impact of land management practices on water, sediment and agriculture  
125 chemical yields in large complex watersheds with varying soils, land use and  
126 management conditions over long periods of time. The model is a catchment-scale  
127 dynamic simulation model and thus can use the spatial information provided by  
128 Geographic Information System and Remote Sensing to simulate a number of  
129 hydrological response units. SWAT was designed as a long-term yield model.  
130 Although the model can be run at a daily time step when the Soil Conservation  
131 Service (SCS) curve number method is used to calculate surface runoff, the simulation  
132 results can be reported on a daily, monthly or yearly basis. It is not designed to  
133 accurately simulate detailed, single-event flood routing (Neitsch et al., 2001).

134 The SWAT model has been widely used to evaluate the impact of climate, land  
135 use, and land management decisions on stream flow and water quality, and gained  
136 international recognition as is evidenced by a large number of applications of this  
137 model (Arnold et al., 1998; Arnold and Fohrer, 2005; Confesor and Whittaker, 2007;  
138 Zhang et al., 2008; Anand et al., 2007; Gassman et al., 2007). Take China as a  
139 particular example, the SWAT applications include the Heihe Basin (Huang and  
140 Zhang, 2004; Wang et al., 2003), the Luohe Watershed (Zhang et al., 2003a and b), the  
141 Yuzhou Reservoir Basin (Zhang et al., 2004), the Luxi Watershed (Hu et al., 2003),  
142 the Huai River Basin (Wang and Xia, 2010), the Biliu River Basin (Chu et al., 2012;  
143 Zhang et al., 2012), and the Huifa River Basin (Zhang et al., 2012). However, none of  
144 the above applications includes a global sensitivity analysis to advance the  
145 understanding of the effects of model parameters on the model performance in terms  
146 of traditional model evaluation metrics (statistical error) and additional hydrological



147 metrics.

## 148 2.2 Sobol's Method

149 Sobol's method (Sobol', 1993) is a global sensitivity analysis approach based on  
 150 variance decomposition. Non-linear and non-monotonic models could be represented  
 151 in the following functional form:

$$152 \quad Y = f(X) = f(X_1, \dots, X_p) \quad (1)$$

153 where  $Y$  is the goodness-of-fit metric of model output, and  $X = (X_1, \dots, X_p)$  is the  
 154 parameter set. In Sobol's method, the total variance of function  $f$ ,  $D(y)$ , is  
 155 decomposed into component variances from individual parameters and their  
 156 interactions:

$$157 \quad D(y) = \sum_i D_i + \sum_{i < j} D_{ij} + \sum_{i < j < k} D_{ijk} + \dots + D_{12 \dots p} \quad (2)$$

158 where  $D_i$  is the amount of variance due to the  $i$ th parameter  $X_i$ , and  $D_{ij}$  is the  
 159 amount of variance due to the interaction between parameter  $X_i$  and  $X_j$ . The  
 160 sensitivity of single parameter or parameter interaction, i.e. Sobol's sensitivity indices  
 161 of different orders, is then assessed based on their percentage contribution to the total  
 162 variance  $D$ :

$$163 \quad \text{First-order index } S_i = \frac{D_i}{D} \quad (3)$$

$$164 \quad \text{Second-order index } S_{ij} = \frac{D_{ij}}{D} \quad (4)$$

$$165 \quad \text{Total-order index } S_{T_i} = 1 - \frac{D_{-i}}{D} \quad (5)$$

166 where  $D_{-i}$  is the amount of variance due to all of the parameters except for  $X_i$ ,  $S_i$   
 167 measures the sensitivity from the main effect of  $X_i$ ,  $S_{ij}$  measures the sensitivity

168 from the interactions between  $X_i$  and  $X_j$ , and  $S_{T_i}$  measures the main effect of  
 169  $X_i$  and its interactions with all the other parameters.

170 The variances in Eq. (2) can be evaluated using approximate Monte Carlo  
 171 numerical integrations, particularly when the model is highly nonlinear and complex.  
 172 The Monte Carlo approximations for  $D$ ,  $D_i$ ,  $D_{ij}$ , and  $D_{-i}$  are defined as  
 173 presented in the following prior studies (Sobol', 1993, 2001; Hall et al., 2005):

$$174 \quad \hat{f}_0 = \frac{1}{n} \sum_{s=1}^n f(X_s) \quad (6)$$

$$175 \quad \hat{D} = \frac{1}{n} \sum_{s=1}^n f^2(X_s) - \hat{f}_0^2 \quad (7)$$

$$176 \quad \hat{D}_i = \frac{1}{n} \sum_{s=1}^n f(X_s^{(a)}) f(X_{(-i)s}^{(b)}, X_{is}^{(a)}) - \hat{f}_0^2 \quad (8)$$

$$177 \quad \hat{D}_{ij}^c = \frac{1}{n} \sum_{s=1}^n f(X_s^{(a)}) f(X_{(-i, \sim j)s}^{(b)}, X_{(i,j)s}^{(a)}) - \hat{f}_0^2 \quad (9)$$

$$178 \quad \hat{D}_{ij} = \hat{D}_{ij}^c - \hat{D}_i - \hat{D}_j \quad (10)$$

$$179 \quad \hat{D}_{-i} = \frac{1}{n} \sum_{s=1}^n f(X_s^{(a)}) f(X_{(-i)s}^{(a)}, X_{is}^{(b)}) - \hat{f}_0^2 \quad (11)$$

180 where  $n$  is the sample size,  $X_s$  is the sampled individual in the scaled unit  
 181 hypercube, and superscripts  $(a)$  and  $(b)$  represent two different samples. All of the  
 182 parameters take their values from sample  $(a)$  are represented by  $X_s^{(a)}$ . The variables  
 183  $X_{is}^{(a)}$  and  $X_{is}^{(b)}$  denote that parameter  $X_{is}$  uses the sampled values in sample  $(a)$   
 184 and  $(b)$ , respectively. The symbols  $X_{(-i)s}^{(a)}$  and  $X_{(-i)s}^{(b)}$  represent cases when all of the  
 185 parameters except for  $X_{is}$  use the sampled values in sample  $(a)$  and  $(b)$ ,  
 186 respectively. The symbol  $X_{(i,j)s}^{(a)}$  represents parameters  $X_{is}$  and  $X_{js}$  with sampled

187 values in sample (a). Finally,  $X_{(-i, \sim j)s}^{(b)}$  represents the case when all of the  
188 parameters except for  $X_{is}$  and  $X_{js}$  utilize sampled values from sample (b).

189 Although Sobol's method has intensive computational requirements, its  
190 sensitivity indices have been shown to be more effective than other approaches in  
191 capturing the interactions between a large number of variables for highly nonlinear  
192 models (Tang et al., 2007a and b). Building on the recommendations of Tang et al.  
193 (2007a), the Latin Hypercube sampling method (McKay et al., 1979) was used for  
194 implementing Sobol's method. Overall computing the first-order, second-order and  
195 total-order sensitivity indices requires  $n \times (m + 2)$  model evaluations where  $n$  is  
196 the number of Latin Hypercube samples and  $m$  is the number of parameters being  
197 analyzed.

### 198 **2.3 Latin Hypercube Sampling**

199 Monte Carlo sampling is in general robust, but may require a high number of samples  
200 and consequently a large amount of computational resources (time and disk memory).  
201 The concept of the Latin Hypercube Sampling (LHS) (McKay et al., 1979; McKay,  
202 1988) is based on the Monte Carlo Simulation but uses a stratified sampling approach  
203 that allows efficient estimation of the output statistics. LHS divides the distribution of  
204 each parameter into  $N$  ranges, each with a probability of occurrence equal to  $1/N$ .  
205 Random values of the parameters are generated such that each range is sampled only  
206 once, that is,  $N$  samples are generated for each parameter. The process can be  
207 repeated  $p$  times for all the variables so that a sample of total size  $N \times p$  is created  
208 with random sample combinations of different variables. The LHS method was  
209 chosen in this paper due to its popularity and effectiveness in hydrological and water  
210 quality modeling (Tang et al., 2007a and b; Fu et al., 2009; Fu et al., 2011).

## 211 2.4 Bootstrap method

212 The bootstrap method (Efron and Tibshirani, 1993) was used to provide confidence  
213 intervals for the parameter sensitivity rankings for the Sobol's method. Essentially,  
214 the samples generated by LHS were resampled  $n$  times when calculating the  
215 sensitivity indices for each parameter, resulting in a distribution of the indices. The  
216 percentile method and the moment method were used for attaining the bootstrap  
217 confidence intervals. The moment method is based on large sample theory and  
218 requires a sufficiently large resampling dimension to yield symmetric 95% confidence  
219 intervals. The percentile method is very simple, but a higher number of resamples are  
220 necessary for the moment method to achieve a reliable estimate of the percentiles. The  
221 moment method can result in a poorly estimated confidence interval if the bootstrap  
222 distribution is skewed (Archer et al., 1997).

223

## 224 3. Case Study

### 225 3.1 Yichun River Basin Description

226 The SWAT model is used to simulate the case study catchment, Yichun River Basin,  
227 China, with a daily time step. The basin boundary and the associated SWAT model  
228 sub-watershed boundaries are presented in **Error! Reference source not found.**  
229 Yichun River Basin has a drainage area of 2405.7km<sup>2</sup>, and is a major tributary to the  
230 Tang-Wang River. Yichun River Basin is dominated by dark brown soils (>71%) and  
231 forest land use (>74%). There are 10 sub-watersheds defined in Yichun River Basin,  
232 where 7 rain gauges and 1 streamflow gauge are located. The Tang-Wang River is the  
233 first level tributary of the left bank of the Song-Hua River. The total length of the  
234 Tang-Wang River is approximately 509km. Its basin drains an area of 20383km<sup>2</sup>. The  
235 climate of the Tang-Wang River basin, located in the middle and high latitudes, is

236 continental monsoon of cold temperate zone. The seasonal change of the Tang-Wang  
237 River basin is obvious, and the mean annual precipitation and evaporation is about  
238 617.4mm and 541mm respectively.

### 239 **3.2 Data Set**

240 The data requirement for SWAT modeling primarily includes: the Digital Elevation  
241 Model (DEM), the digital river network, the land use and soil data, the  
242 hydrometeorological data (precipitation, temperature, solar radiation, wind speed,  
243 relative humidity and stream flow).

244 (1) DEM data (raster resolution: 90m×90m) were obtained from the International  
245 Scientific Data Service Platform of the Computer Network Information Center,  
246 Chinese Academy of Sciences (<http://srtm.csi.cgiar.org>).

247 (2) Soil data (scale = 1:10<sup>6</sup>) and land use data (scale = 1:10<sup>5</sup>) for the 1980s were  
248 collected from Data Center for Resources and Environmental Sciences Chinese  
249 Academy of Sciences (RESDC, <http://www.resdc.cn/>).

250 (3) Digital river network data (scale = 1:2.5×10<sup>5</sup>) were obtained from 1:4M-scale  
251 Topographic Database of the National Fundamental Geographic Information System  
252 of China.

253 (4) Daily Meteorological data (temperature, solar radiation, wind speed, relative  
254 humidity) were obtained from China Meteorological Data Sharing Service System  
255 (<http://cdc.cma.gov.cn/>) and presented in Table 1.

256 (5) Daily precipitation data and stream flow data were obtained from  
257 Hydrological Administration of Heilongjiang Province and presented in Table 1.

### 258 **3.3 Model Setup and Parameterization**

259 To evaluate SWAT model parameter sensitivities for wet, moderate, and dry years  
260 with the intent of identifying the key parameters impacting different years (wet,

261 moderate, and dry years), three scenarios are constructed: (1) daily sensitivity analysis  
262 using a wet year of observations, (2) daily sensitivity analysis using a moderate year  
263 of observations, and (3) daily sensitivity analysis using a dry year of observations. Fig.  
264 2a shows the annual precipitation time series of Yichun River Basin between 1979  
265 and 2001. Fig. 2b shows the exceedance probabilities of annual precipitation for  
266 Yichun River Basin. It can be seen that years 1982-1985 are a typical representation  
267 of the catchment climate from wet to dry, that is, year 1982 is dry, years 1983 and  
268 1984 are moderate, and year 1985 is wet. The time series of the four years'  
269 precipitation and observed streamflow are presented in Fig. 3.

270 The flow-related parameters of the SWAT and their ranges are listed in Table 2.  
271 These 28 model parameters impact snowmelt, surface runoff, groundwater, lateral  
272 flow and evapotranspiration predictions. The parameter ranges were based mainly on  
273 the default ranges in the SWAT2000 model documentation.

274 Note that some SWAT model parameters in this case study are not regarded as a  
275 spatial variable but instead a constant value across all model spatial units, for example,  
276 those parameters related to snowmelt. Many other parameters such as SCS curve  
277 numbers and soil properties are spatially varied and therefore can be assigned  
278 different values for different spatial units. If all parameters of different spatial units  
279 are considered for model calibration, the total number of parameters increases to more  
280 than 100. This could significantly increase the complexity and computational  
281 requirement of a sensitivity analysis. Since the analysis in this paper is based on one  
282 monitoring location only due to data availability, thus spatially varying model  
283 parameters were not analyzed for each spatial unit. Instead, a single factor was used to  
284 represent spatial variation, by increasing or decreasing spatially varying parameter  
285 values from their base or default values. For each parameter, this approach maintains

286 the relative differences in the base or default parameter values assigned to different  
287 spatial units.

288 For each scenario, the first two months (January and February) are used as a  
289 warm up period for model simulation. And the rest of time periods in each scenario  
290 are used to assess the model's performance in the sensitivity analysis process.

### 291 3.4 Goodness-of-fit metrics

292 The sensitivity analyses for SWAT model with Sobol's method consider four  
293 goodness-of-fit metrics: two statistical metrics and two hydrological metrics. This  
294 allows for a more accurate capture of model performance from different aspects.  
295 Statistical metrics focus on the hydrograph (i.e., errors and trends), while hydrological  
296 metrics focus on different functional behaviors of the basin (e.g., peakedness and flow  
297 duration curve).

298 The two statistical metrics - root mean squared error (RMSE) and Nash-Sutcliffe  
299 Efficiency (NSE) - are used to address flow prediction errors and trends, respectively.  
300 The RMSE and NSE metrics are computed using equations (12) and (13),  
301 respectively,

$$302 \quad RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Q_{pi} - Q_{ii})^2} \quad (12)$$

$$303 \quad NSE = 1 - \frac{\sum_{i=1}^n (Q_{pi} - Q_{ii})^2}{\sum_{i=1}^n (Q_{ii} - \bar{Q}_t)^2} \quad (13)$$

304 where  $Q_{pi}$  and  $Q_{ii}$  are the simulated and measured flows on day  $i$ ,  $n$  is the total  
305 number of days and  $\bar{Q}_t$  is the mean daily measured flows in the analyzed period.

306 The runoff coefficient error (ROCE) and slope of the flow duration curve error  
307 (SFDCE) metrics are used to evaluate the model's accuracy in simulating a basin's

308 water balance and flashiness (i.e., variability of mid-flows), respectively. The ROCE  
 309 metric is computed as the absolute difference between the simulated and observed  
 310 average annual runoff coefficient:

$$311 \quad ROCE = abs\left(\frac{\overline{Q}_p}{\overline{P}} - \frac{\overline{Q}_t}{\overline{P}}\right) \quad (14)$$

312 where  $\overline{Q}_p$  represents the simulated average annual flow and  $\overline{Q}_t$  is the observed  
 313 average annual flow. Both flows are normalized by the observed average annual  
 314 precipitation  $\overline{P}$ .

315 The SFDCE metric is computed as the absolute error in the slope of the flow  
 316 duration curve between the 30<sup>th</sup> and 70<sup>th</sup> percentiles of predicted and observed flows  
 317 to measure the error of the model generated distribution of mid-range flows:

$$318 \quad SFDCE = abs\left(\frac{Q_{p,70} - Q_{p,30}}{40} - \frac{Q_{t,70} - Q_{t,30}}{40}\right) \quad (15)$$

319 where  $Q_{p,30}$  and  $Q_{p,70}$  are the simulated 30<sup>th</sup> and 70<sup>th</sup> percentile flows within the  
 320 simulated flow duration curve and  $Q_{t,30}$  and  $Q_{t,70}$  are the observed 30<sup>th</sup> and 70<sup>th</sup>  
 321 percentile flows within the simulated flow duration curve.

### 322 **3.5 Sensitivity Analysis Implementation**

323 Statistical sample size is a key parameter for Sobol's method. Tang et al. (2007b)  
 324 used a sample size of 8192 for Sobol' analysis when considering 18 model parameters,  
 325 and suggested that this number is extremely conservative. Fu et al. (2012) used a set  
 326 of 2000 LHS samples for 21 parameters in a hydraulic analysis of water distribution  
 327 network. Tang et al. (2007a) used a sample size of 2000 for 403 variables in a  
 328 distributed hydrologic model and this number was proved sufficient to maintain the  
 329 accuracy and repeatability of Sobol' analysis. On the basis of these prior studies, a



330 LHS sample size of 2000 was used in this study for all three scenarios resulting in  
331  $2000 \times (28 + 2) = 60,000$  model runs for each scenario. A comparison of results with  
332 smaller sample sizes show this sample size is sufficient and the sensitivity indices are  
333 reliable.

334

#### 335 **4. Results and Discussion**

336 The first- and total-order sensitivity indices of 28 parameters are shown in Fig.4. In  
337 Fig.4, each column of panels represents one of the three scenarios: dry year (1982),  
338 moderate year (1983-1984) and wet year (1985), and each row represents one of the  
339 four metrics. In each panel, the  $x$ -axis represents parameter numbers, and  $y$ -axis  
340 represents first- and total- order sensitivity indices. The first order indices are  
341 represented by black bars, which measure individual parameter contributions to the  
342 variance of the four goodness-of-fit metrics. The total-order indices are presented by  
343 the total height of bars measuring individual and interactive parameter contributions  
344 to the variance of the four goodness-of-fit metrics. It should be noted that the grey  
345 bars measure the total interactive contribution of one parameter with all the other  
346 parameters. Fig.5 provides a detailed description of the second-order indices, i.e., the  
347 contributions of the interactions between two parameters to the variance of the four  
348 goodness-of-fit metrics in the three scenarios. Sensitive parameters are defined with a  
349 10% threshold of total order index in Fig.4, and similarly significant second-order  
350 interactions are defined with a 1% threshold in Fig.5. These thresholds are subjective  
351 and their ease-of-satisfaction decreases with increasing numbers of parameters or  
352 parameter interactions (Tang et al., 2007a and b). The main findings are analysed for  
353 each metric below.

#### 354 **4.1 Statistical metrics: RMSE and NSE**

355 For the RMSE metric, there are three sensitive parameters (total order index>10%) for  
356 the 1982 dry year scenario, i.e., the lateral flow travel time (LAT\_TTIME), base flow  
357 alpha factor (ALPHA\_BF), and maximum canopy storage (CANMX). However, in  
358 the 1983-1984 year scenario, the metric variance is attributed to more parameters, that  
359 is, there are a total of seven parameters with a total-order index greater than 10%,  
360 including deep aquifer percolation fraction (RCHRG\_DP), runoff curve number  
361 multiplicative factor (CN2), groundwater delay time (GW\_DELAY), and threshold  
362 groundwater depth for return flow (GWQMN) in addition to the three parameters  
363 LAT\_TTIME, ALPHA\_BF, and CANMX in the dry year scenario. Similarly, in the  
364 wet year scenario, five parameters are highly sensitive with a total-order index bigger  
365 than 10%. Amongst these sensitive parameters, LAT\_TTIME is the most sensitive  
366 parameter, accounting for 59%, 27%, and 36% of the total variance in the dry,  
367 moderate, and wet scenarios, respectively. The above results confirm the finding by  
368 Nossent et al. (2011) that only a small number of parameters are highly sensitive in  
369 SWAT.

370 The amount of lateral flow discharged to the main channel on any given day is  
371 controlled by LAT\_TTIME. The sensitivity of daily runoff simulations to  
372 LAT\_TTIME in Yichun River Basin was expected due to lesser mean annual  
373 precipitation in the basin. The moderate and wet scenarios have smaller total-order  
374 sensitivity indices of LAT\_TTIME than the dry scenario due to more precipitation.  
375 Furthermore, it should be noted that the parameters related to groundwater flow, i.e.,  
376 GW\_DELAY, ALPHA\_BF, GWQMN, and RCHRG\_DP have a more significant  
377 interactions with other parameters from a dry year 1982 through transition years  
378 1983-1984 to a wet year 1985. This is because the interactions between regional

379 surface water and groundwater become more and more frequent with the increase of  
380 precipitation and water in soil profile and shallow aquifer in a wetter year. These  
381 interactions could not be revealed by using other methods such as LH-OAT.

382 Additionally, it should be noted that first-order indices of parameters account for  
383 most proportion of their total-order indices for the 1982 dry year scenario in Yichun  
384 River Basin due to few interactions between parameters, especially the few  
385 interactions between regional surface water and groundwater, in the situations where  
386 little precipitation occurs and stream flow is generated. From dry year through  
387 moderate year to wet year, the proportions of the effects of parameter interactions on  
388 the model output to their total-order indices increase gradually, especially the  
389 parameters related to groundwater flow and having substantial interactions with  
390 surface water, e.g., ALPHA\_BF and GWQMN. However, some parameters related to  
391 groundwater flow, such as GW\_DELAY and RCHRG\_DP, having a highly interactive  
392 effect on the model output for the 1983-1984 year scenario, have less interactive  
393 effects on the model output for the 1985 wet year scenario. The reason is that the soil  
394 and shallow aquifer have been saturated in a wetter year, and the changes of these  
395 parameter values tend to have less influence on other parameters.

396 It is interesting to note the similarity of the sensitivity results for the two  
397 statistical metrics (RMSE and NSE) for every scenario analyzed due to their focus on  
398 addressing flow prediction errors and trends with the simulated and measured flows.

#### 399 **4.2 Hydrological metrics: ROCE and SFDCE**

400 For the ROCE metric, there are three sensitive parameters (total order index>10%) for  
401 the 1982 dry year scenario, i.e., LAT\_TTIME, CANMX, and GWQMN. In the  
402 1983-1984 year scenario, three parameters, i.e., GWQMN, RCHRG\_DP, and  
403 CANMX, are highly sensitive. In the wet year scenario, three parameters, i.e.,

404 GWQMN, RCHRG\_DP, and GW\_DELAY, are highly sensitive. Amongst these  
405 sensitive parameters, LAT\_TTIME is the most sensitive parameter in the dry scenario,  
406 accounting for 34% of the total variance, and GWQMN is the most sensitive  
407 parameter in the moderate and wet scenarios, accounting for 53% and 59% of the total  
408 variance, respectively.

409       The overall parameter sensitivity for the long-term water balance metric (ROCE)  
410 is distinctly different from those statistical metrics. Rather than addressing flow  
411 prediction errors and trends with the simulated and measured flows, the model  
412 performance in terms of ROCE is controlled by parameters that affect the volume of  
413 ET losses across all watersheds, i.e., LAT\_TTIME, CANMX, GWQMN, RCHRG\_DP,  
414 and GW\_DELAY. This result reflects the fact that these parameters largely control the  
415 volume (rather than the shape in the case of statistical metrics) of the hydrograph,  
416 which impacts the long-term water balance. In the SWAT model, ET losses occur  
417 primarily from stream flow, water intercepted by the plant canopy, water in soil  
418 profile and shallow aquifer. The amount of losses from each of the above processes  
419 depends on the demand (potential ET for that time of year) and the supply (water  
420 content of the storage). The parameters that are sensitive to the long-term water  
421 balance are those affecting not only the size of these storages (i.e., the potential  
422 volume of losses) but also the amount of water that goes into these storages. The  
423 amount of lateral flow discharged to the main channel on any given day is controlled  
424 by LAT\_TTIME. The values of LAT\_TTIME and CANMX are more influential on  
425 the model output as compared to the other parameters for the 1982 dry year scenario  
426 in the Yinchun River Basin because the stream flow and water intercepted by the plant  
427 canopy are effectively available for ET losses for the dry year scenario. In the  
428 moderate and wet years, the water that goes into soil profile and shallow aquifer are

429 more effectively available for ET losses. Therefore, it is reasonable that GWQMN is  
430 more sensitive than other parameters, and the parameters related to groundwater flow  
431 have significant interactions with other parameters affecting stream flow for the  
432 1983-1984 year and the wet year scenarios in Yichun River Basin. Some parameters  
433 related to lateral flow and groundwater flow, such as LAT\_TTIME and RCHRG\_DP,  
434 have many interactive effects on the model output for the 1983-1984 year scenario  
435 similarly, however, have less interactive effects on the model output for the 1985 wet  
436 year scenario because the soil and shallow aquifer have been saturated in a wetter year,  
437 and the changes of these parameter values tend to have less influence on ET losses.

438 For the SFDCE metric, there are six sensitive parameters (total order index>10%)  
439 for the 1982 dry year scenario, i.e., CANMX, GWQMN, GW\_DELAY, LAT\_TTIME,  
440 ALPHA\_BF, and RCHRG\_DP. In the 1983-1984 year scenario, five parameters, i.e.,  
441 GWQMN, CANMX, LAT\_TTIME, RCHRG\_DP, and GW\_DELAY, are highly  
442 sensitive. In the wet year scenario, three parameters, i.e., GWQMN, RCHRG\_DP, and  
443 GW\_DELAY are highly sensitive. Amongst these sensitive parameters, CANMX is  
444 the most sensitive parameter in the dry scenario, accounting for 49% of the total  
445 variance, and GWQMN is the most sensitive parameter in the moderate and wet  
446 scenarios, accounting for 37% and 76% of the total variance, respectively.

447 It is interesting to note the similarity and difference of the sensitivity results for  
448 the two hydrological metrics (ROCE and SFDCE) for every scenario analyzed. The  
449 similarity of the sensitivity results for the two hydrological metrics is due to their  
450 common characteristics of hydrological metrics. The difference of the sensitivity  
451 results for the two hydrological metrics is due to their focuses on different functional  
452 behaviors of the basin. The metric, SFDCE, evaluates the error in the slope of the  
453 flow duration curve between the 30 and 70 percentile flow magnitudes. It thus

454 captures the parameter impacts on the variability in flow magnitudes (rather than their  
455 impact on long-term runoff volume as for ROCE). Comparing sensitivities across the  
456 basin for this metric, it is seen that the ET controlling parameters (CANMX and  
457 GWQMN) again become sensitive for SFDCE as they do for ROCE. However, the  
458 number of sensitive parameters for SFDCE is larger than that for ROCE and more  
459 interactions between parameters in the 1982 dry year scenario, e.g., the interactive  
460 effects of GWQMN with great influences on the interactions between groundwater  
461 flow and stream flow, and the number of sensitive parameters for SFDCE is less with  
462 the increase of precipitation for the 1983-1984 year and the 1985 wet year scenarios  
463 because the SFDCE metric is computed to capture the parameter sensitivities for the  
464 30-70 percentile range of flows, i.e., the sensitivities of the parameters more  
465 frequently 'activated' over the 30-70 percentile range of flows. Wagener et al. (2009)  
466 found that the sensitivities of hydrological metrics are more evenly distributed to  
467 model parameters compared to the two statistical metrics under a single rainfall event.  
468 However in this case study the same finding is revealed for the dry year only and is  
469 not shown for the moderate and wet years. This highlights the importance of  
470 considering different climate conditions in analyzing the sensitivities of model  
471 parameters.

472 The Sobol's sensitivity indices can have a high degree of uncertainty due to the  
473 difficulty in numerical approximation (Tang et al., 2007a & b). In this study, we used  
474 statistical bootstrapping to provide 95% confidence intervals for Sobol's method.  
475 Figure 4 provides the confidence intervals for the total-order indices computed for  
476 different metrics in the three climate scenarios. It can be seen from Figure 4 that  
477 similar to the findings from Tang et al. (2007a & b) the intervals are rather large,  
478 which cannot be reduced even when a larger number of samples are used. However,

479 with the presence of the confidence intervals, the uncertainty of the sensitivity indices  
480 could be revealed, informing the selection of sensitive model parameters.

#### 481 **4.3 Interactive effects**

482 The pairwise interactions that are revealed by the Sobol's method elucidate some  
483 important model processes and in particular how one process influences another.

484 Recall from Fig.4 that RCHRG\_DP has a lot of interactive effects on all the four  
485 metrics in the case of 1983-1984 year scenario. In Fig.5, it can be seen that this  
486 parameter interacts with LAT\_TTIME and CANMX only, particularly LAT\_TTIME,  
487 for the two statistical metrics. The above interactions could be expected, as these  
488 parameters have a large influence on the interactions between groundwater flow and  
489 stream flow, particularly the interactions between lateral flow and water flow in  
490 shallow aquifer, and the definition on the stream flow response of the system. The  
491 more water is diverted to stream flow from plant canopy and lateral flow, the less  
492 water is diverted from groundwater. This also leads to a trade-off between the  
493 parameter values. GWQMN also has a lot of interactive effects on all the four metrics  
494 for 1983-1984 year scenario in Fig.4, but Fig.5 shows that GWQMN has few  
495 interactions with other parameters for the two statistical metrics. That means that the  
496 interactive effect of GWQMN do not come from second-order interactions, so it might  
497 come from higher order interactions (3-order, 4-order ...). For the two hydrological  
498 metrics in the case of 1983-1984 year scenario, the RCHRG\_DP vs. GWQMN  
499 interaction has a significant influence on the model output variability and system ET  
500 losses. The relation between RCHRG\_DP and GWQMN gives more insight on how  
501 the groundwater flow is regulated in the SWAT model and how both parameters  
502 contribute to the simulated outflow and storage in shallow aquifer. RCHRG\_DP  
503 defines the fraction of the recharge that goes to the deep aquifer, and the remaining

504 goes to the shallow aquifer and partly determines the amount of water in this storage.  
505 If this amount of water is higher than the GWQMN value, return value occurs and  
506 contributes to the total outflow. In this way, RCHRG\_DP and GWQMN have an  
507 interactive influence on the simulated flow, as RCHRG\_DP has an impact on the  
508 storage in the shallow aquifer and thus on GWQMN.

509 Similarly, Fig.4 shows that GWQMN and ALPHA\_BF have a lot of interactive  
510 effects on two statistical metrics in the case of the 1985 wet year scenario. In Fig.5,  
511 these interactions can be further revealed and mainly come from five pairwise  
512 interactions: GWQMN vs. GW\_DELAY, GWQMN vs. RCHRG\_DP, GWQMN vs.  
513 LAT\_TTIME, ALPHA\_BF vs. LAT\_TTIME, and ALPHA\_BF vs. CN2. These  
514 parameters have a large influence on the interactions between groundwater flow and  
515 stream flow, and the definition on the stream flow response of the system. This also  
516 leads to a trade-off between the parameter values. Additionally, Fig.4 shows that  
517 GW\_DELAY, GWQMN and RCHRG\_DP have a lot of interactive effects on two  
518 hydrological metrics in the case of the 1985 wet year scenario. In Fig.5, these  
519 interactions can be further revealed and mainly come from three pairwise interactions:  
520 GW\_DELAY vs. GWQMN, GW\_DELAY vs. RCHRG\_DP, and GWQMN vs.  
521 RCHRG\_DP. These interactions have a significant influence on the groundwater flow  
522 and storage in the shallow aquifer, and determine the amount of water in the shallow  
523 aquifer and system ET losses.

524 The results from this study indicate that the sensitivity of the SWAT parameters  
525 varies significantly in the dry, normal and wet years simulated, and suggest that a  
526 single set of parameter values may not appropriately represent hydrologic processes  
527 during various flow regimes. Dynamic updating of parameters during the simulation  
528 may be viable in such situations, however, further studies are needed to evaluate if



529 such approaches could improve the SWAT performance.

530 The results from this study also indicate that the use of the two commonly used  
531 statistical metrics RMSE and TRMSE fails to identify the SWAT model's parameters  
532 that control the flashiness (measured by SFDCE) and water balance (measured by  
533 ROCE) of Yichun River Basin. This confirms the finding by Wagener et al. (2009)  
534 that the choice of performance metrics has a significant impact on the parameter  
535 sensitivities of a distributed hydrological model. Further study is currently in progress  
536 to investigate how the results obtained from this study can be used to improve the  
537 optimization efficiency in the model calibration process.

538

## 539 **5. Conclusions**

540 This paper provides a variance-based sensitivity analysis for a SWAT model of Yichun  
541 River Basin, China. The analysis reveals the individual effects of each parameter and  
542 its interactions with other parameters on the model performance regarding two  
543 statistical metrics - RMSE and NSE and two hydrological metrics - ROCE and  
544 SFDCE. Model parameter sensitivities are analysed under three difference climate  
545 conditions: wet, moderate, and dry years. The main findings from the results obtained  
546 are summarized below.

547 (1) The results obtained in this paper confirm that only a small number of model  
548 parameters are highly sensitive for all the four metrics considered in SWAT. This is  
549 also true when different climatic conditions are considered.

550 (2) The sensitivity of the SWAT parameters varies significantly in the dry,  
551 normal and wet years simulated. For example, the lateral flow travel time is very  
552 sensitive in most cases, but has little impact on SFDCE in the dry year. Further, the  
553 curve number factor, identified as the most important parameter in prior study, is not

554 sensitive in most cases considered in this study when parameter interactions are  
555 considered.

556 (3) Parameter interactions contribute to a significant portion of the variation in  
557 all metrics considered under moderate and wet years. In particular, the variation in the  
558 two hydrological metrics is mainly dominated by the interactions. Sensitive  
559 parameters could not be identified if the interactions are discounted. However, in the  
560 dry year, the individual effects control the variation in the other three metrics except  
561 SFDCE.

562 (4) The two statistical metrics (RMSE and NSE) have a very similar  
563 performance in terms of sensitive parameters identified. This is because both of them  
564 measure flow prediction errors and trends with the simulated and measured flows.  
565 However, the two statistical metrics fail to identify the SWAT parameters that control  
566 the flashiness and water balance, illustrating the importance of considering the two  
567 hydrologic metrics, i.e., SFDCE and ROCE, in the model identification process.

568

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572

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717 **List of Figure Captions**

718 **Fig. 1** Yichun river catchment.

719 **Fig. 2** Distinction of annual rainfall for Yichun River Basin between different years.

720 Fig. 2a shows annual rainfall for Yichun River Basin from year 1979 to 2001, Fig. 2b

721 shows the exceedance probability plot of annual rainfall for Yichun River Basin.

722 **Fig. 3** Hydrographs for Yichun River Basin from year 1982 to 1985.

723 **Fig. 4** First-order indices, total-order indices and their confidence intervals

724 computed using different measures for the 28 parameters in the three scenarios. The

725 parameter numbers in the  $x$ -axis are shown in Table 2.

726 **Fig. 5** Second-order indices computed using the four goodness-of-fit metrics in the

727 three scenarios. The parameter numbers in the  $x$ -axis are shown in Table 2.

728

729

Table 1 Hydrometeorological data for Yichun river basin

Time Scale	Hydrological/meteorological element	Station	Period
Daily	Precipitation	7 gauges, such as Kaiyuan	1979~2001
	Streamflow	Yichun	1979~2001
	Temperature, relative humidity, wind speed and solar radiation	Yichun	1979~2001

730

731

732

Table 2 Parameter list

No.	Name	Brief Description (units)	Minimum	Maximum
1	SFTMP	snow fall temperature (°C)	-5	5
2	SMTMP	snowmelt temperature threshold (°C)	-5	5
3	SMFMX	melt factor for snow on June 21 (mm/°C)	1.5	8
4	SMFMN	melt factor for snow on December 21 (mm/°C)	0	10
5	TIMP	snowpack temperature lag factor	0.01	1
6	ESCO	soil evaporation compensation factor	0.001	1
7	EPCO	plant uptake compensation factor	0	1
8	SURLAG	surface runoff lag coefficient	1	24
9	GW_DELAY	groundwater delay time (days)	0.001	500
10	ALPHA_BF	base flow alpha factor	0.001	1
11	GWQMN	threshold groundwater depth for return flow (mm)	0.001	500
12	GW_REVAP	groundwater “revap” coefficient	0.02	0.2
13	REVAPMN	threshold depth of water in the shallow aquifer for “revap” or percolation to the deep aquifer to occur (mm)	0	500
14	RCHRG_DP	deep aquifer percolation fraction	0	1
15	SLSUBBSN <sup>a</sup>	average slope length multiplicative factor	0.75	1.25
16	SLOPE <sup>a</sup>	average slope steepness multiplicative factor	0.75	1.25
17	LAT_TTIME	lateral flow traveltime (days)	0.001	180
18	CANMX	maximum canopy storage (mm)	0	100
19	BIOMIX	biological mixing efficiency	0	1
20	CN2 <sup>a</sup>	runoff curve number multiplicative factor	0.75	1.25
21	BLAI <sup>a</sup>	maximum potential leaf area index	0.75	1.25
22	CH_N2	manning’s “n” value for the main channel	-0.01	0.3
23	CH_K2	effective hydraulic conductivity in main channel alluvium (mm/hr)	-0.01	500
24	SOL_Z <sup>a</sup>	soil profile total depth multiplicative factor	0.75	1.25
25	SOL_AWC <sup>a</sup>	available water capacity multiplicative factor	0.75	1.25
26	SOL_K <sup>a</sup>	saturated hydraulic conductivity multiplicative factor	0.75	1.25
27	SOL_A1b <sup>a</sup>	moist soil albedo multiplicative factor	0.75	1.25

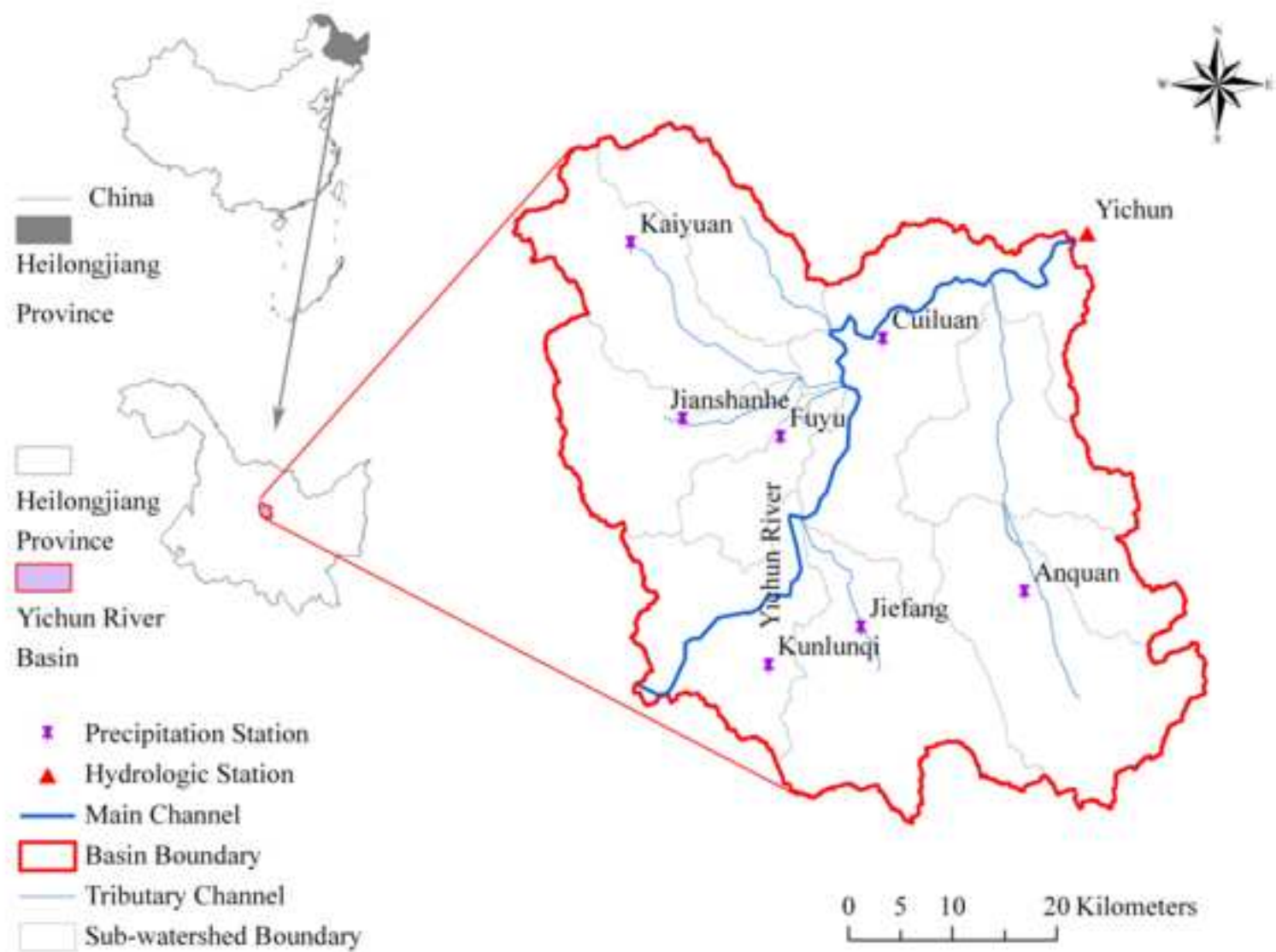
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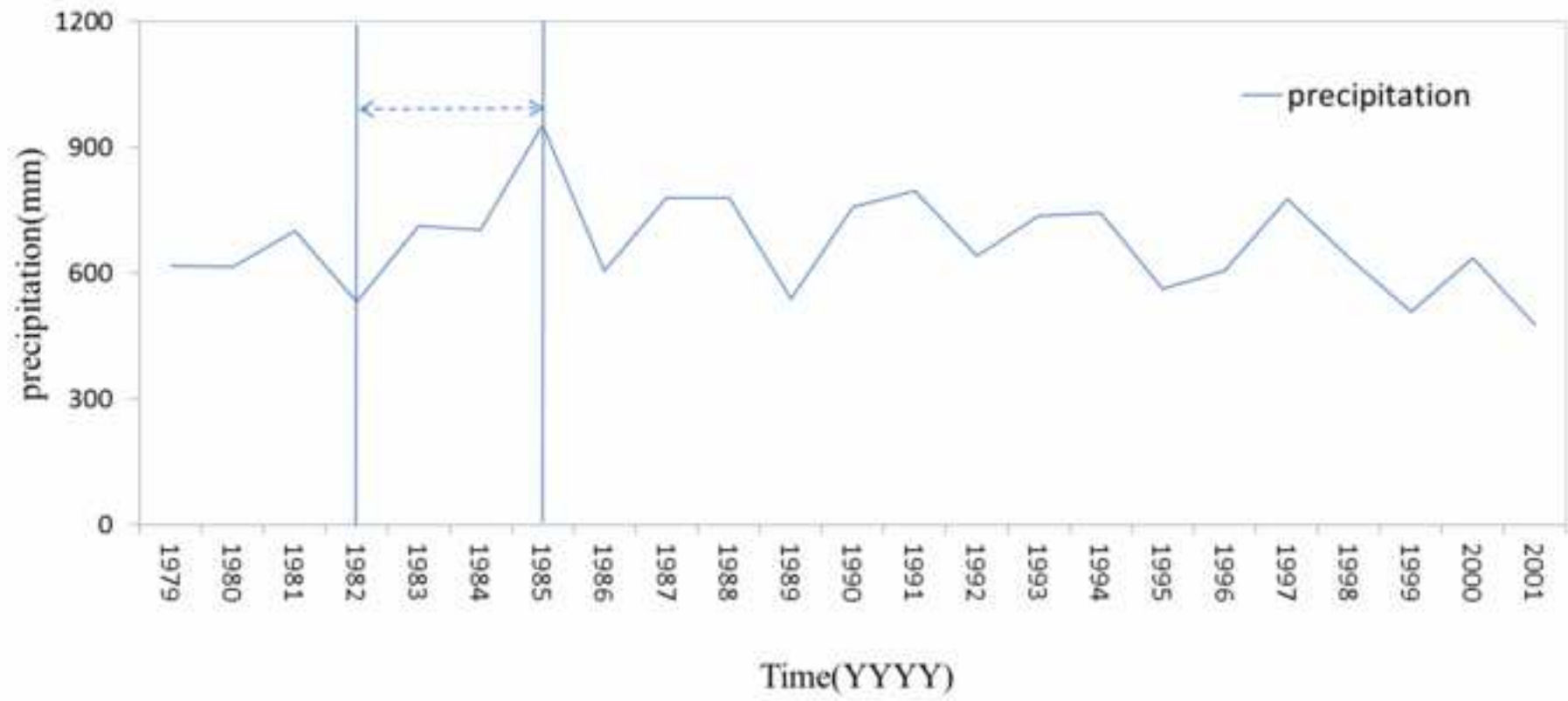
28	TLAPS	temperature lapse rate (°C/km)	0	50
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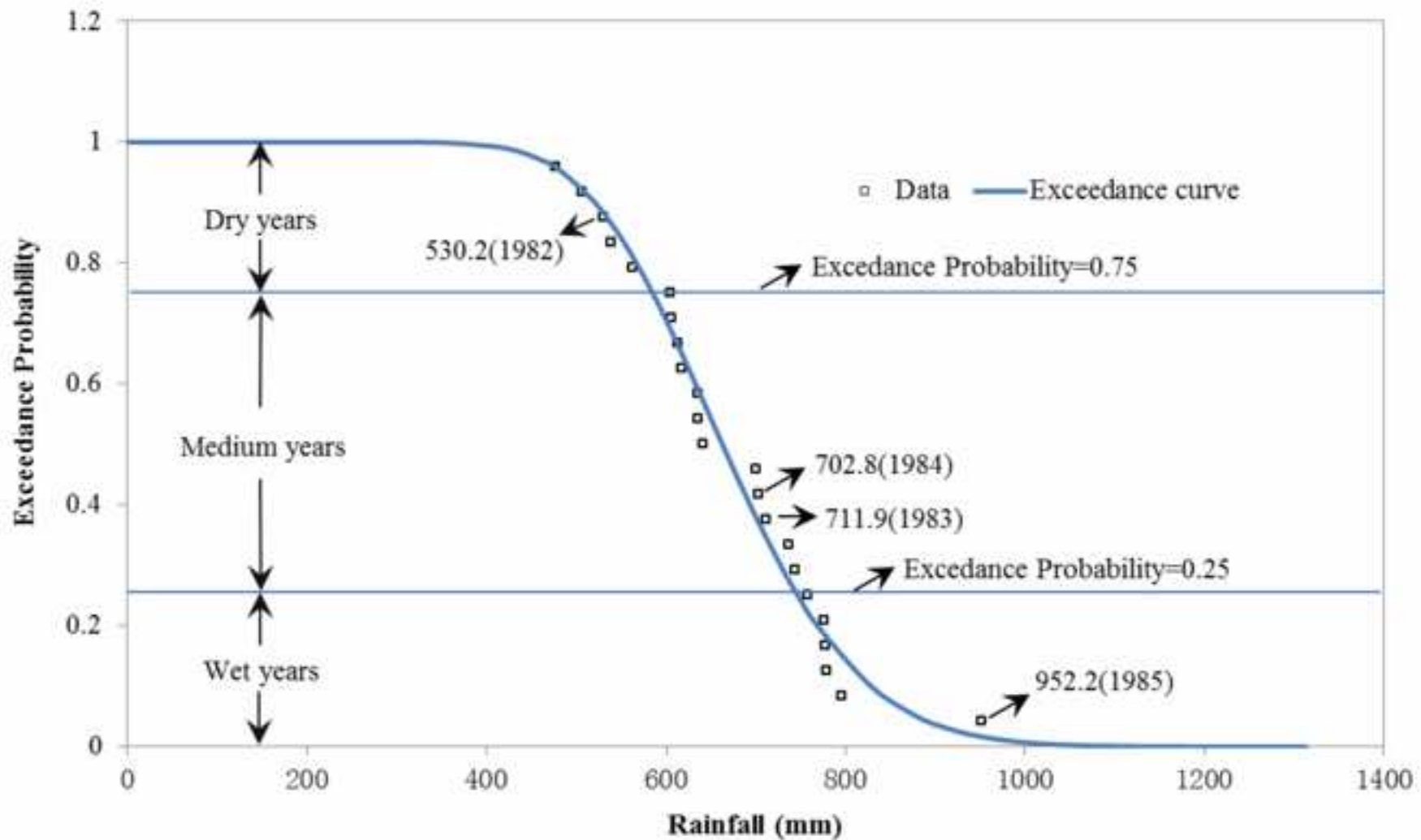
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733 <sup>a</sup>Parameters are multiplicative factors used to adjust the spatial variation across all model units.

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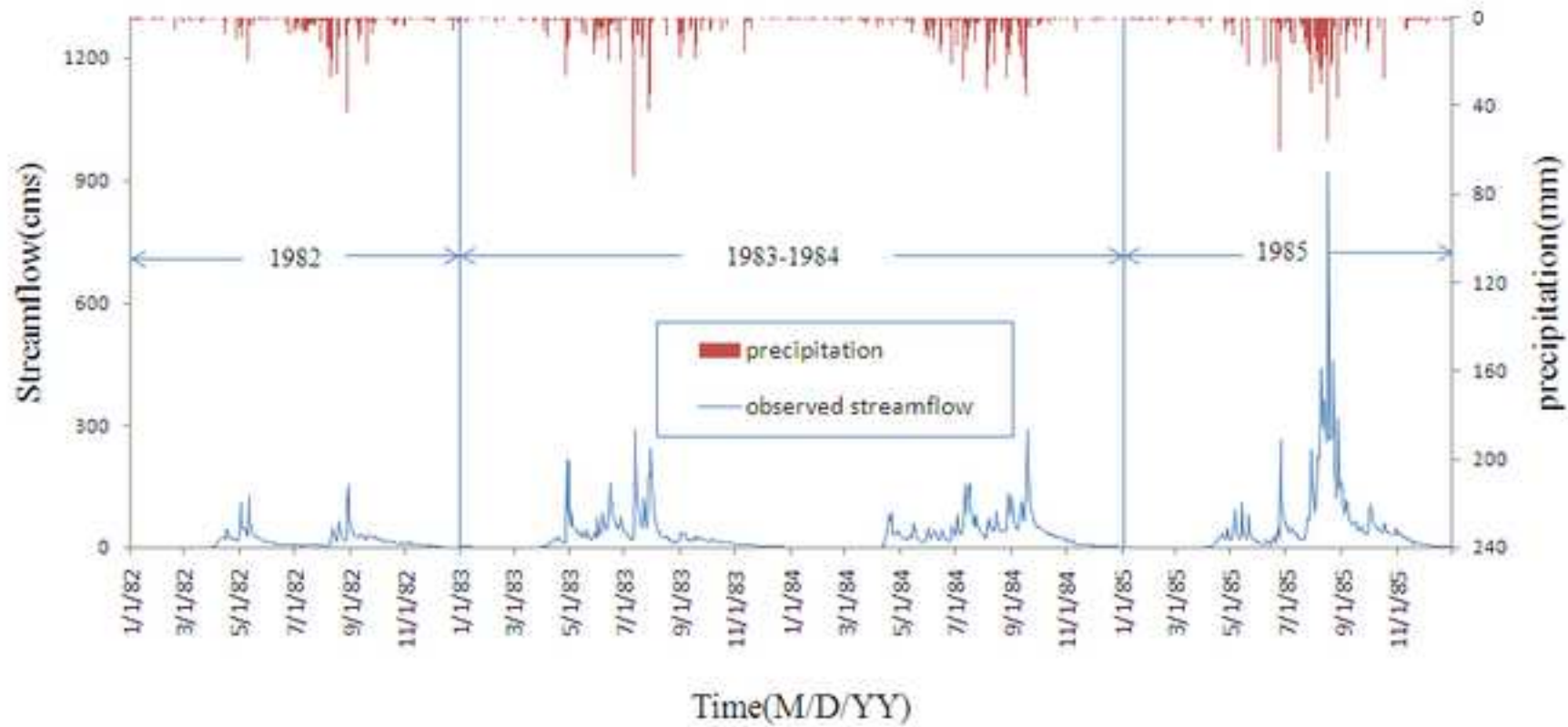


Fig. 4

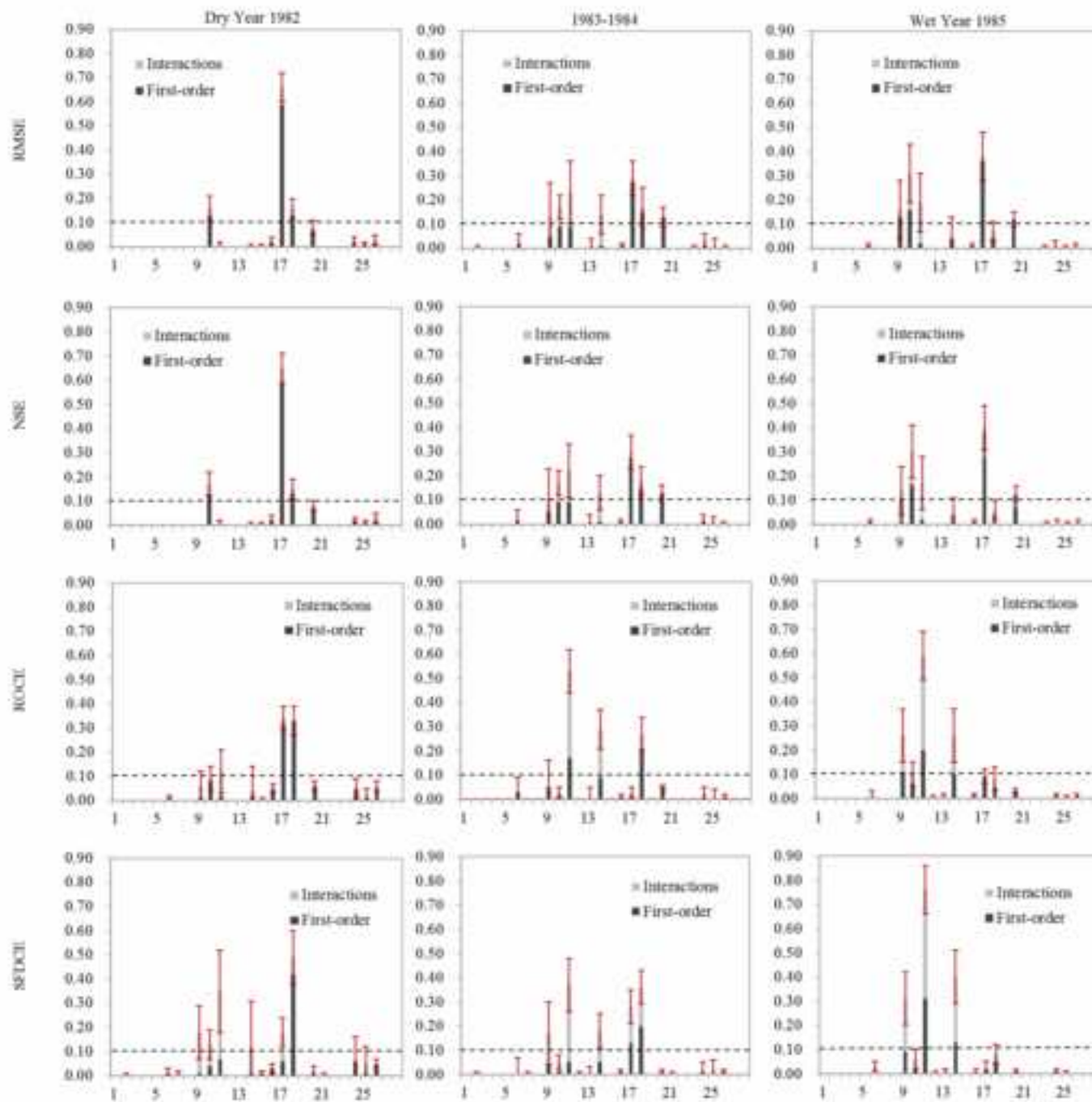
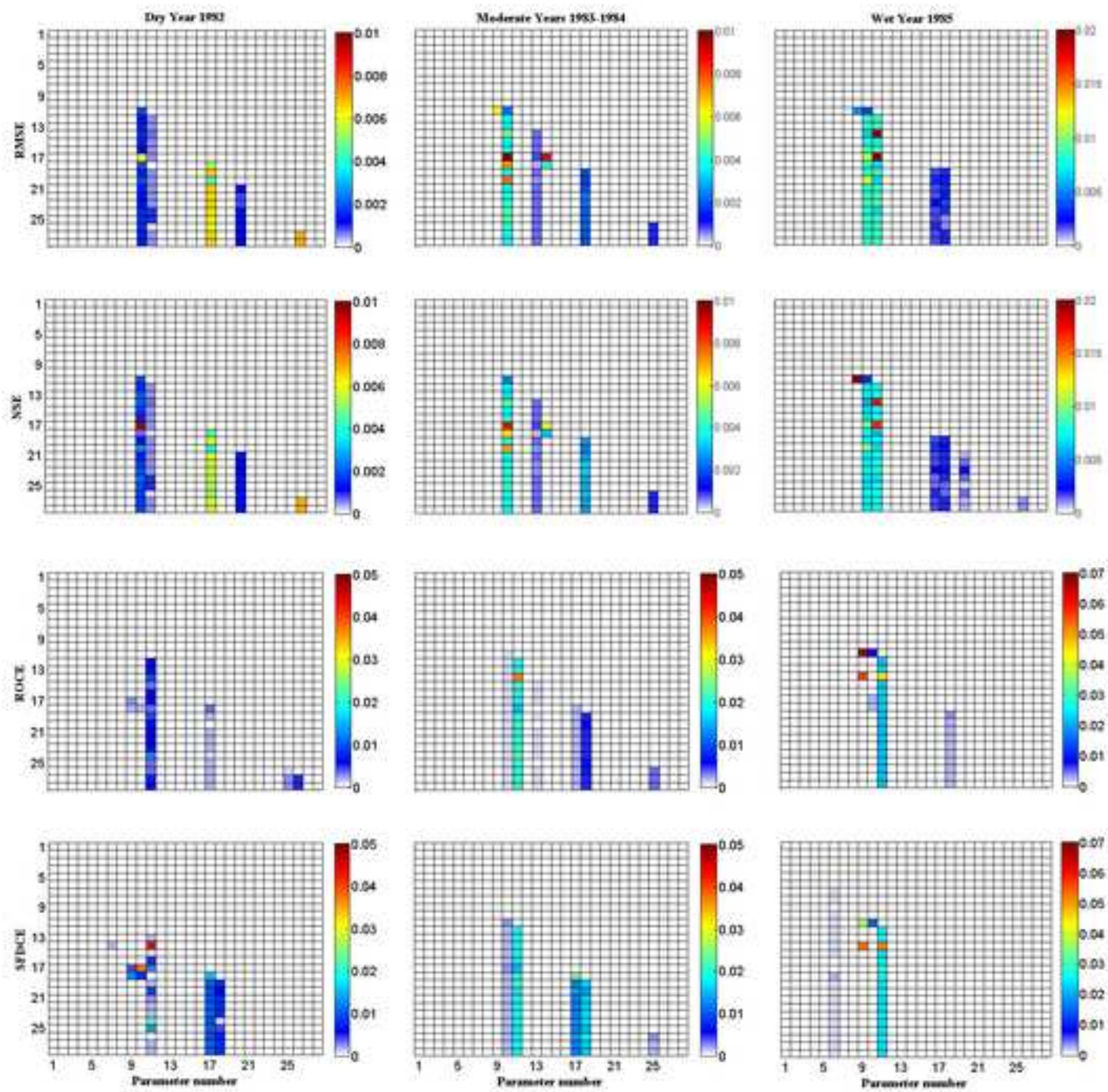


Fig. 5



734

735 We analysed the effects of key parameters and their interactions on four metrics.

736 The parameter sensitivities vary significantly in different climate conditions.

737 Increasing precipitation can lead to more interactive effects between parameters.

738 Statistical metrics fail to identify the parameters related to hydrological metrics.

739 Sobol's method advances our understanding of the underlying hydrological  
740 processes.

741

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