

Nonstandard neutrino interactions in reactor and superbeam experiments

Joachim Kopp,^{*} Manfred Lindner,[†] and Toshihiko Ota[‡]

Max-Planck-Institut für Kernphysik, Postfach 10 39 80, 69029 Heidelberg, Germany

Joe Sato[§]

Department of Physics, Saitama University, Shimo-Okubo 255, Sakura-ku, Saitama, 338-8570, Japan

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The formalism of nonstandard four-fermion interactions provides a convenient, model-independent way of parametrizing a wide class of “new physics” scenarios. In this article, we study the performance of reactor and superbeam neutrino experiments in the presence of such nonstandard interactions (NSI). Because of interference between the standard and nonstandard amplitudes, sizeable effects are to be expected if the NSI parameters are close to their current upper limits. We derive approximate formulas for the relevant oscillation probabilities including NSI, and show how the leading effects can be understood intuitively even without any calculations. We will present a classification of all possible NSI according to their impact on reactor and superbeam experiments, and it will turn out that these experiments are highly complementary in terms of their sensitivity to the nonstandard parameters. The second part of the paper is devoted to detailed numerical simulations, which will demonstrate how a standard oscillation fit of the mixing angle θ_{13} may fail if experimental data is affected by NSI. We find that for some nonstandard terms, reactor and superbeam experiments would yield seemingly conflicting results, while in other cases, they may agree well with each other, but the resulting value for θ_{13} could be far from the true value. This offset may be so large that the true θ_{13} is even ruled out erroneously. In the last section of the paper, we demonstrate that reactor and superbeam data can actually establish the presence of nonstandard interactions. Throughout our discussion, we pay special attention to the impact of the complex phases, and of the near detectors.

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I. INTRODUCTION

At the dawn of the era beyond the standard model, a plethora of new theoretical models has been devised to resolve many of the experimental and theoretical shortcomings of our current picture of elementary particles. However, in the context of future experiments, it is often desirable to describe new physics in a more model-independent way. One possibility to achieve this is through effective four-fermion operators, so-called nonstandard interactions (NSI), which arise naturally in the presence of heavy mediator fields. In this article, we shall focus, in particular, on NSI in the neutrino sector, which have been discussed on general phenomenological grounds in [1–8], and in the context of specific models in [9–12]. The importance of NSI for neutrino oscillation physics has been pointed out in a pioneering work by Grossman [13], and many authors have studied their impact on solar neutrinos [14–17], atmospheric neutrinos [18–23], conventional and upgraded neutrino beams [24–30], neutrino factories [8,25,31–37], beta beams [38], supernova neutrinos [39–41], cosmological relic neutrinos [42], e^+e^- colliders [43], neutrino-electron scattering [44], and

neutrino-nucleus scattering [45,46]. Existing experimental bounds are presented in [47].

Our main interest in this work will be on nonstandard interactions in upcoming reactor and accelerator neutrino experiments. Although the main design goal for these experiments is the precision measurement of the standard oscillation parameters, the search for deviations from the standard framework is an equally interesting part of their physics program. Moreover, while in the race for the standard oscillation parameters, reactor and beam experiments are competing, we will show that their results will be highly complementary when one is interested in nonstandard physics.

In the numerical simulations which we are going to present, we will focus on the experiments T2K [48,49], NO ν A [50], Double Chooz [51,52], and a hypothetical 200 t reactor experiment [53]. Of course, the analytical results apply also to other experiments such as T2HK [48] and Daya Bay [54].

We will first introduce our formalism in Sec. II, and give a detailed discussion of the different possible Lorentz structures and their relevance for reactor and superbeam experiments. Although this discussion may seem rather technical, it will ultimately allow us to greatly simplify the problem and considerably reduce the number of parameters. In Sec. III, we will then present approximate expressions for the oscillation probabilities including NSI for the $\bar{\nu}_e \rightarrow \bar{\nu}_e$, $\nu_\mu \rightarrow \nu_e$, and $\nu_\mu \rightarrow \nu_\mu$ channels. We will also show in an intuitive way why certain NSI terms appear

*:jkopp@mpi-hd.mpg.de

†:lindner@mpi-hd.mpg.de

‡:toshi@mpi-hd.mpg.de

§:joe@phy.saitama-u.ac.jp

in these expressions, and others do not. Sec. IV is devoted to a discussion of numerical simulation techniques, and of the specific experiments which we have simulated. In Sec. V, we show how the data from these experiments may be misinterpreted, if NSI are not taken into account in the fits. We will finally demonstrate in Sec. VI that a combined analysis of reactor and superbeam data may allow for the actual discovery of a wide variety of nonstandard interactions by goodness-of-fit arguments. Our conclusions will be presented in Sec. VII.

II. THE FORMALISM OF NONSTANDARD INTERACTIONS

A. The NSI Lagrangian

It is well-known that in the low-energy regime, weak neutrino interactions can be described by effective four-fermion operators like

$$\mathcal{L}_\nu = \frac{G_F}{\sqrt{2}} [\bar{\nu}_\alpha \gamma^\rho (1 - \gamma^5) \ell_\alpha] [\bar{f}' \gamma_\rho (1 - \gamma^5) f], \quad (1)$$

and

$$\mathcal{L}_{\text{MSW}} = \frac{G_F}{\sqrt{2}} [\bar{\nu}_\alpha \gamma^\rho (1 - \gamma^5) \nu_\alpha] [\bar{f} \gamma_\rho (1 - \gamma^5) f], \quad (2)$$

where ν_α is the neutrino field of flavor α , ℓ_α is the corresponding charged lepton field, and f, f' are the components of an arbitrary weak doublet.

The low-energy fingerprint of many ‘‘new physics’’ scenarios has a structure similar to Eqs. (1) and (2), and the corresponding operators are called nonstandard interactions. If we consider only lepton number conserving operators, the most general NSI Lagrangian reads

$$\mathcal{L}_{\text{NSI}} = \mathcal{L}_{V\pm A} + \mathcal{L}_{S\pm P} + \mathcal{L}_T, \quad (3)$$

where the different terms are classified according to their Lorentz structure in the following way:

$$\begin{aligned} \mathcal{L}_{V\pm A} &= \frac{G_F}{\sqrt{2}} \sum_{f,f'} \tilde{\varepsilon}_{\alpha\beta}^{s,f,f',V\pm A} [\bar{\nu}_\beta \gamma^\rho (1 - \gamma^5) \ell_\alpha] \\ &\quad \times [\bar{f}' \gamma_\rho (1 \pm \gamma^5) f] \\ &\quad + \frac{G_F}{\sqrt{2}} \sum_f \tilde{\varepsilon}_{\alpha\beta}^{m,f,V\pm A} [\bar{\nu}_\alpha \gamma^\rho (1 - \gamma^5) \nu_\beta] \\ &\quad \times [\bar{f} \gamma_\rho (1 \pm \gamma^5) f] + \text{H.c.}, \end{aligned} \quad (4)$$

$$\mathcal{L}_{S\pm P} = \frac{G_F}{\sqrt{2}} \sum_{f,f'} \tilde{\varepsilon}_{\alpha\beta}^{s,f,f',S\pm P} [\bar{\nu}_\beta (1 + \gamma^5) \ell_\alpha] [\bar{f}' (1 \pm \gamma^5) f], \quad (5)$$

$$\mathcal{L}_T = \frac{G_F}{\sqrt{2}} \sum_{f,f'} \tilde{\varepsilon}_{\alpha\beta}^{s,f,f',T} [\bar{\nu}_\beta \sigma^{\rho\tau} \ell_\alpha] [\bar{f}' \sigma_{\rho\tau} f]. \quad (6)$$

Here, G_F is the Fermi constant, ν and ℓ are the neutrino

and charged lepton fields, and the f 's represent the interaction partners of the neutrinos. The dimensionless parameters $\tilde{\varepsilon}$ give the strength of the nonstandard interactions relative to G_F , where an upper index s stands for NSI in the neutrino source or detector, while m denotes nonstandard matter effects, i.e. NSI affecting the propagation. In general, the $\tilde{\varepsilon}^s$ can be arbitrary complex matrices, while the $\tilde{\varepsilon}^m$ have to be Hermitian.

Note that we have required the neutrino fields to be purely left-handed, since processes involving right-handed neutrinos would require either a neutrino helicity flip, or their amplitudes would have to contain at least two NSI terms (e.g. one to create the right-handed neutrino and one to absorb it), and would therefore be strongly suppressed. This constraint on the neutrino chirality, in particular, forbids $\nu\nu f f$ terms in $\mathcal{L}_{S\pm P}$ and \mathcal{L}_T .

Before proceeding, let us give a simple estimate which relates the magnitude of the $\tilde{\varepsilon}$ parameters to the corresponding new physics scale M_{NSI} [31]: If we assume the nonstandard interactions to be mediated by some intermediate particles with a mass of order M_{NSI} , the effective vertices in Eqs. (4)–(6) will be suppressed by $1/M_{\text{NSI}}^2$ in the same way as the standard weak interactions are suppressed by $1/M_W^2$. Therefore we expect

$$|\tilde{\varepsilon}| \sim \frac{M_W^2}{M_{\text{NSI}}^2}. \quad (7)$$

B. Relevance of the different NSI terms to reactor and superbeam experiments

We see from Eqs. (4)–(6) that the number of possible NSI terms is very large. However, the number of parameters for our discussion of reactor and superbeam experiments can be greatly reduced by a few simple, but rather technical arguments. Many of these arguments are based on constraints coming from the requirement of interference between the standard and nonstandard amplitudes. Of course, the total interaction rate will also contain pure NSI terms, for which these constraints do not apply, but they are suppressed by $\tilde{\varepsilon}^2$, and can therefore be assumed to be negligible compared to the interference terms, which are linear in $\tilde{\varepsilon}$. The following arguments are also summarized in Table I.

- (1) The standard production and detection processes of reactor and superbeam neutrinos are, on the fundamental level, decays of u quarks into d quarks, or vice-versa. Since interference of standard and nonstandard amplitudes requires the external particles to be identical, only the $\tilde{\varepsilon}^{s,f,f'}$ terms with $f = u, f' = d$ will be relevant, and we will henceforth simply omit the indices f and f' .
- (2) For the nonstandard matter effects, only coupling to electrons, up quarks, and down quarks is important.
- (3) Nonstandard couplings involving τ leptons are irrelevant since τ production is impossible in reactor

TABLE I. Classification of the vertices from Eqs. (4)–(6) according to their impact on reactor and superbeam experiments. Terms marked with \checkmark can give a sizeable contribution; for all other terms, the reason for their suppression is given (see text for details).

	Reactor source and detector ($f = u, f' = d$)					
	$\ell_\alpha = e$	Source $\ell_\alpha = \mu$	$\ell_\alpha = \tau$	$\ell_\alpha = e$	Detector $\ell_\alpha = \mu$	$\ell_\alpha = \tau$
$V - A$	\checkmark	No μ production	No τ production	\checkmark	No μ production	No τ production
$V + A$	\checkmark	No μ production	No τ production	\checkmark	No μ production	No τ production
$S - P$	Strong constraints	No μ production	No τ production	Strong constraints	No μ production	No τ production
$S + P$	Strong constraints	No μ production	No τ production	Strong constraints	No μ production	No τ production
T	Strong constraints	No μ production	No τ production	Strong constraints	No μ production	No τ production

	Superbeam source and detector ($f = u, f' = d$)					
	$\ell_\alpha = e$	Source $\ell_\alpha = \mu$	$\ell_\alpha = \tau$	$\ell_\alpha = e$	Detector $\ell_\alpha = \mu$	$\ell_\alpha = \tau$
$V - A$	No e production	\checkmark	No τ production	\checkmark	\checkmark	No τ detection
$V + A$	No e production	\checkmark	No τ production	\checkmark (Mild supp.)	\checkmark (Mild supp.)	No τ detection
$S - P$	No e production	\checkmark	No τ production	Strong constraints	Chiral supp.	No τ detection
$S + P$	No e production	\checkmark	No τ production	Strong constraints	Chiral supp.	No τ detection
T	No e production	No P -odd part	No τ production	Strong constraints	Chiral supp.	No τ detection

Propagation ($f = e, u, d$)		
	$V - A$	\checkmark
	$V + A$	\checkmark

and beam sources, and is not considered as a detection process here, although it might in principle be possible for high energy superbeam neutrinos. Hence we take

$$\tilde{\varepsilon}_{\tau\beta}^{s,V\pm A} = \tilde{\varepsilon}_{\tau\beta}^{s,S\pm P} = \tilde{\varepsilon}_{\tau\beta}^{s,T} = 0. \quad (8)$$

For the same reason, processes involving muons can be neglected in reactor experiments, and processes involving electrons can be neglected in the superbeam source, since they constitute subdominant backgrounds even in the standard framework.

- (4) In the couplings to muons, there is still room for non- $(V - A)(V - A)$ contributions. For neutrino production in pion decay, the effect of $(S + P) \times (S \pm P)$ type NSI is even enhanced by a factor of [55,56]

$$\omega = \frac{m_\pi}{m_\mu} \frac{m_\pi}{m_u + m_d} \sim 20, \quad (9)$$

and the importance of this enhancement for accelerator neutrino experiments has been pointed out in [26]. However, there exist limits on the muon helicity in pion decay [57,58], which ensure that, in spite of the enhancement, $(S + P)(S \pm P)$ type NSI cannot affect the neutrino oscillation amplitude by more than a few percent.

- (5) Tensor interactions are impossible in pion decay since the decay operator must have a parity-odd component.

- (6) In the detection processes involving muons, the $(S + P)(S \pm P)$ and TT terms are chirally suppressed by the smallness of m_μ compared to the typical superbeam energies of $\mathcal{O}(1 \text{ GeV})$. As mentioned above, the leading effect in the total event rate is given by the interference of the nonstandard amplitude and the standard $(V - A)(V - A)$ amplitude. This interference can only occur if the initial and final state particles have identical helicities, so for $(S + P)(S \pm P)$ and TT type nonstandard interactions, a mass-suppressed helicity flip of the muon is required. We can also see the emergence of the suppression factor explicitly by considering the Dirac traces, which have to be evaluated when calculating the cross section. For example, in the case of $(S + P)(S + P)$ NSI, the spin sum in the interference term of standard and nonstandard amplitudes is

$$\begin{aligned} & \sum_{\text{spins}} \text{Tr}[\gamma^\rho(1 - \gamma^5)\mu\bar{\mu}(1 - \gamma^5)\nu\bar{\nu}] \\ & \cdot \text{Tr}[\gamma_\rho(1 - \gamma^5)u\bar{u}(1 - \gamma^5)d\bar{d}] \\ & = \sum_{\text{spins}} \text{Tr}[\gamma^\rho(1 - \gamma^5)(\not{p}_\mu + m_\mu)(1 - \gamma^5)(\not{p}_\nu + m_\nu)] \\ & \cdot \text{Tr}[\gamma_\rho(1 - \gamma^5)(\not{p}_u + m_u)(1 - \gamma^5)(\not{p}_d + m_d)]. \end{aligned} \quad (10)$$

Similar equations can be derived for $(S + P)(S - P)$ and TT interactions. Because of the orthogonality

property of the chirality projection operators, a contribution proportional to m_μ remains of the first trace in Eq. (10), and a contribution proportional to m_u from the second. This leads to a suppression factor of $\mathcal{O}(m_\mu m_u/E^2)$. Low-energy neutrinos ($E \lesssim 1$ GeV) interact with whole nucleons, rather than single quarks, therefore m_u should be replaced by the much larger nucleon mass m_n , so that in this case, the overall chiral suppression is only of $\mathcal{O}(m_\mu/E)$. At typical superbeam energies around 1 GeV, we are in the transition regime between neutrino-nucleon interactions (quasielastic scattering and resonance scattering) and neutrino-quark interactions (deep-inelastic scattering) [59,60].

- (7) For $(V - A)(V + A)$ interactions involving muons in the detector, chiral suppression occurs only for the hadronic interaction partners, and according to our above discussion, it is not very pronounced for them. Therefore, $(V - A)(V + A)$ type interactions may in general be important for the cross sections, and modify their overall magnitude as well as their energy dependence.
- (8) From measurements of the electron angular distribution in nuclear β decays, $(S + P)(S \pm P)$ and TT couplings to electrons are strongly constrained [61–65]. Consequently, we take

$$\tilde{\varepsilon}_{e\beta}^{s,S\pm P} = \tilde{\varepsilon}_{e\beta}^{s,T} = 0 \quad (11)$$

for $\beta = e, \mu, \tau$.

- (9) There is still room for $(V - A)(V + A)$ type terms involving electrons, because these terms differ from the standard model term only in the quark current, which cannot be directly measured. Limits exist only for the effective vector and axial-vector couplings of protons and neutrons [65], but due to the nonperturbative nature of the strong interactions, these cannot be easily related to the couplings of the fundamental quarks.

If $(V - A)(V + A)$ couplings to electrons exist, the processes in which they appear will in general have an energy dependence different from that of the corresponding standard processes. For antineutrino production in nuclear reactors, however, this difference is completely negligible because the neutrino spectrum from nuclear β decay is governed by kinematical effects and by the Fermi function, which describes final state Coulomb interactions.

The cross section for the inverse β decay process, which is used to detect reactor antineutrinos, is derived from empirical values for the effective vector and axial-vector couplings, so any possible $(V - A)(V + A)$ contribution is automatically taken into account properly.

Finally, $(V - A)(V + A)$ interactions involving electrons in the beam detector, are mildly chirally

suppressed, in analogy to $(V - A)(V + A)$ interactions involving muons.

- (10) As we have seen in Eqs. (4)–(6), nonstandard matter effects can only have a $(V - A)(V - A)$ or $(V - A)(V + A)$ Lorentz structure, as long as we restrict the discussion to left-handed neutrinos. For the computation of the coherent forward scattering amplitude, the factor $[\bar{f}\gamma_\rho(1 \pm \gamma^5)f]$ has to be averaged over the neutrino trajectory, and for unpolarized matter at rest, the only contribution is $N_f = \bar{f}\gamma^0 f$, the fermion density appearing in the matter potential. Since N_f is independent of the axial current, we conclude that both possible Lorentz structures would have the same impact on the nonstandard matter effects.

To conclude this discussion, we would like to emphasize again that non- $(V - A)(V - A)$ Lorentz structures can play an important role in reactor and superbeam experiments. However, these experiments do not have the capability to distinguish different Lorentz structures, unless the spectral distortion caused by $(V - A)(V + A)$ terms in the superbeam detector is taken into account. In the following, we will neglect this spectral distortion for simplicity, assuming that it is anyway hidden by the systematical uncertainties in the neutrino cross sections.

C. Hamiltonian approach to nonstandard interactions in neutrino oscillations

The observations from the previous section can be exploited to further reduce the number of free parameters in our problem. To this end, we define effective couplings $\varepsilon_{\alpha\beta}^s$, $\varepsilon_{\alpha\beta}^d$, and $\varepsilon_{\alpha\beta}^m$, corresponding to nonstandard interactions in the production, detection, and propagation processes. $\varepsilon_{\alpha\beta}^s$ describes a nonstandard admixture of flavor β to the neutrino state which is produced in association with a charged lepton of flavor α . This means that the neutrino source does not produce a pure flavor neutrino eigenstate $|\nu_\alpha\rangle$, but rather a state

$$|\nu_\alpha^s\rangle = |\nu_\alpha\rangle + \sum_{\beta=e,\mu,\tau} \varepsilon_{\alpha\beta}^s |\nu_\beta\rangle. \quad (12)$$

Similarly, the detector is sensitive not to the normal weak eigenstates, but to the combination

$$\langle\nu_\beta^d| = \langle\nu_\beta| + \sum_{\alpha=e,\mu,\tau} \varepsilon_{\alpha\beta}^d \langle\nu_\alpha|. \quad (13)$$

Note that in $\varepsilon_{\alpha\beta}^s$, the first index corresponds to the flavor of the charged lepton, and the second to that of the neutrino, while in $\varepsilon_{\alpha\beta}^d$, the order is reversed. We have chosen this convention to be consistent with the literature.

In general, the matrices $(1 + \varepsilon^s)$ and $(1 + \varepsilon^d)$ are non-unitary, i.e. the source and detection states are not required to form complete orthonormal sets of basis vectors in the

Hilbert space:

$$\sum_{\alpha=e,\mu,\tau} |\nu_\alpha^s\rangle\langle\nu_\alpha^s| \neq 1, \quad \sum_{\beta=e,\mu,\tau} |\nu_\beta^d\rangle\langle\nu_\beta^d| \neq 1, \quad (14)$$

$$\langle\nu_\alpha^s|\nu_\beta^s\rangle \neq \delta_{\alpha\beta}, \quad \langle\nu_\alpha^d|\nu_\beta^d\rangle \neq \delta_{\alpha\beta}. \quad (15)$$

We can read off from Table I that the 3×3 coupling matrix $\varepsilon_{\alpha\beta}^s$ receives contributions from $\tilde{\varepsilon}_{\alpha\beta}^{s,u,d,V\pm A}$ and $\tilde{\varepsilon}_{\alpha\beta}^{s,u,d,S\pm P}$, while $\varepsilon_{\alpha\beta}^d$ and $\varepsilon_{\alpha\beta}^m$ are built up only from $(V - A)(V \pm A)$ contributions.

Since the coefficients $\varepsilon_{e\alpha}^s$ and $\varepsilon_{\alpha e}^d$ (for $\alpha = e, \mu, \tau$) both originate from $\tilde{\varepsilon}^{s,u,d,V\pm A}$, the $(V - A)(V \pm A)$ coupling to up and down quarks, we have the constraint

$$\varepsilon_{e\alpha}^s = \varepsilon_{\alpha e}^{d*}, \quad (16)$$

which again reduces the number of independent parameters by 3. The aforementioned spectral distortion and mild chiral suppression in the superbeam detector could invalidate Eq. (16), but we will neglect it in the following.

Similarly, the $(V - A)(V \pm A)$ part of $\varepsilon_{\mu\alpha}^s$ and $\varepsilon_{\alpha\mu}^d$ are the same, and since the $(S + P)(S \pm P)$ Lorentz structures have less impact in $\varepsilon_{\alpha\mu}^d$ than in $\varepsilon_{\mu\alpha}^s$, we will typically have

$$|\varepsilon_{\mu\alpha}^s| \gtrsim |\varepsilon_{\alpha\mu}^d| \quad (17)$$

(barring fine-tuned cancellation effects). If we assume all nonstandard interactions to be of the $(V - A)(V - A)$ type, as is sometimes done in the literature, the constraints from Eqs. (16) and (17) are tightened to $\varepsilon^s = (\varepsilon^d)^\dagger$.

It is clear from Table I that coupling to τ leptons is irrelevant in our case, so we can also take

$$\varepsilon_{\tau\beta}^s = \varepsilon_{\alpha\tau}^d = 0 \quad (18)$$

for all α, β .

ε^m is an additive contribution to the Mikheyev-Smirnov-Wolfenstein (MSW) potential in the flavor basis, $V_{\text{MSW}} = a_{\text{CC}} \text{diag}(1, 0, 0)$, which now becomes

$$\tilde{V}_{\text{MSW}} = a_{\text{CC}} \begin{pmatrix} 1 + \varepsilon_{ee}^m & \varepsilon_{e\mu}^m & \varepsilon_{e\tau}^m \\ \varepsilon_{e\mu}^{m*} & \varepsilon_{\mu\mu}^m & \varepsilon_{\mu\tau}^m \\ \varepsilon_{e\tau}^{m*} & \varepsilon_{\mu\tau}^{m*} & \varepsilon_{\tau\tau}^m \end{pmatrix}, \quad (19)$$

with $a_{\text{CC}} = 2\sqrt{2}G_F N_e E$. Recall from Eq. (4) that the diagonal entries in this matrix have to be real, so that the Hamiltonian will remain Hermitian, and can be diagonalized by a unitary mixing matrix.

Since we are interested in a combined analysis of reactor and superbeam experiments, it is important to keep in mind that the effective ε matrices are *the same* for both types of experiments, because, under the assumptions and approximations discussed above, those entries which may be relevant in both of them ($\varepsilon_{\alpha\beta}^m$ and $\varepsilon_{\alpha e}^d$) are identical in both cases.

The oscillation probability is obtained as

$$\begin{aligned} P_{\nu_\alpha^s \rightarrow \nu_\beta^d} &= |\langle\nu_\beta^d|e^{-iHL}|\nu_\alpha^s\rangle|^2 \\ &= |(1 + \varepsilon^d)_{\gamma\beta} (e^{-iHL})_{\gamma\delta} (1 + \varepsilon^s)_{\alpha\delta}|^2 \\ &= |[(1 + \varepsilon^d)^T e^{-iHL} (1 + \varepsilon^s)^T]_{\beta\alpha}|^2, \end{aligned} \quad (20)$$

where

$$H_{\alpha\beta} = \frac{1}{2E} \left[U_{\alpha j} \begin{pmatrix} 0 & & \\ & \Delta m_{21}^2 & \\ & & \Delta m_{31}^2 \end{pmatrix} (U^\dagger)_{k\beta} + (\tilde{V}_{\text{MSW}})_{\alpha\beta} \right]. \quad (21)$$

The Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix U is parametrized as

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{\text{CP}}} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta_{\text{CP}}} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta_{\text{CP}}} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta_{\text{CP}}} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta_{\text{CP}}} & c_{13}c_{23} \end{pmatrix}. \quad (22)$$

As usual, s_{ij} and c_{ij} denote the sine and cosine of the mixing angle θ_{ij} , and δ_{CP} is the (Dirac) CP phase.

For antineutrinos, we have to replace ε^s , ε^d , and ε^m by their complex conjugates in the above equations, and reverse the signs of a_{CC} and δ_{CP} .

D. Perturbative calculation of oscillation probabilities

In practice, it is very convenient to expand the oscillation probabilities in a perturbative series with respect to the small quantities θ_{13} , $\Delta m_{21}^2/\Delta m_{31}^2$, and $|\varepsilon_{\alpha\beta}^{s,m,d}|$ instead of

attempting to evaluate Eq. (20) exactly. Following a procedure similar to the one explained in the appendix of [66], the first order expansion reads

$$P_{\nu_\alpha^s \rightarrow \nu_\beta^d} = P_{\nu_\alpha^s \rightarrow \nu_\beta^d}^{(0)} + P_{\nu_\alpha^s \rightarrow \nu_\beta^d}^{(1)} + \dots, \quad (23)$$

where

$$P_{\nu_\alpha^s \rightarrow \nu_\beta^d}^{(0)} = |[e^{-iH^{(0)}L}]_{\beta\alpha}|^2, \quad (24)$$

$$\begin{aligned}
P_{\nu_\alpha^s \rightarrow \nu_\beta^d}^{(1)} &= [e^{-iH^{(0)}L}]_{\beta\alpha}^* [e^{-iH^{(0)}L}(1 + \varepsilon^s)^T]_{\beta\alpha} + [e^{-iH^{(0)}L}]_{\beta\alpha}^* [(1 + \varepsilon^d)^T e^{-iH^{(0)}L}]_{\beta\alpha} \\
&\quad - i [e^{-iH^{(0)}L}]_{\beta\alpha}^* \left[\int_0^L dx e^{-iH^{(0)}(L-x)} H^{(1)} e^{-iH^{(0)}x} \right]_{\beta\alpha} + \text{H.c.},
\end{aligned} \tag{25}$$

and

$$H_{\alpha\beta}^{(0)} = \frac{1}{2E} \left[U^{(0)} \begin{pmatrix} 0 & & \\ & 0 & \\ & & \Delta m_{31}^2 \end{pmatrix} U^{(0)\dagger} + a_{\text{CC}} \begin{pmatrix} 1 & & \\ & 0 & \\ & & 0 \end{pmatrix} \right], \tag{26}$$

$$\begin{aligned}
H_{\alpha\beta}^{(1)} &= \frac{1}{2E} \left[U^{(0)} \begin{pmatrix} 0 & & \\ & \Delta m_{21}^2 & \\ & & 0 \end{pmatrix} U^{(0)\dagger} + U^{(1)} \begin{pmatrix} 0 & & \\ & 0 & \\ & & \Delta m_{31}^2 \end{pmatrix} U^{(0)\dagger} + U^{(0)} \begin{pmatrix} 0 & & \\ & 0 & \\ & & \Delta m_{31}^2 \end{pmatrix} U^{(1)\dagger} \right. \\
&\quad \left. + a_{\text{CC}} \begin{pmatrix} \varepsilon_{ee}^m & \varepsilon_{e\mu}^m & \varepsilon_{e\tau}^m \\ \varepsilon_{e\mu}^{m*} & \varepsilon_{\mu\mu}^m & \varepsilon_{\mu\tau}^m \\ \varepsilon_{e\tau}^{m*} & \varepsilon_{\mu\tau}^{m*} & \varepsilon_{\tau\tau}^m \end{pmatrix} \right].
\end{aligned} \tag{27}$$

By $U^{(0)}$, we denote the PMNS matrix for $\theta_{13} = 0$, and $U^{(1)}$ contains the first order terms in θ_{13} . The unperturbed Hamiltonian, $H_{\alpha\beta}^{(0)}$, can be easily diagonalized exactly, so that the matrix exponentials in the above equations can be evaluated. It is straightforward to extend the expansion to higher orders.

III. MODIFIED NEUTRINO OSCILLATION PROBABILITIES FOR REACTOR AND SUPERBEAM EXPERIMENTS

To study the impact of nonstandard interactions on reactor and superbeam experiments, we need, in particular, the oscillation probabilities $P_{\bar{\nu}_e^s \rightarrow \bar{\nu}_e^d}$, $P_{\nu_\mu^s \rightarrow \nu_e^d}$, and $P_{\nu_\mu^s \rightarrow \nu_\mu^d}$, to which these experiments are sensitive. We will first present approximate analytic formulas for these quantities in Secs. III A to III C, and then discuss them in Sec. III D. All approximations were carried out with the perturbative method described in the previous section. We have checked that the expressions presented in this section reduce to the well-known standard oscillation results if NSI are absent by comparing them to the expressions derived in [66–68]. Moreover, we have verified all formulas numerically, term by term, using Mathematica.

To simplify the notation, let us make the abbreviations $s_{ij} = \sin\theta_{ij}$, $c_{ij} = \cos\theta_{ij}$, $s_{2\times ij} = \sin 2\theta_{ij}$, and $c_{2\times ij} = \cos 2\theta_{ij}$. Moreover, it will be convenient to split the ε

parameters into their real and imaginary parts by writing $\varepsilon_{\alpha\beta}^{s,m,d} = |\varepsilon_{\alpha\beta}^{s,m,d}| \exp(i\phi_{\alpha\beta}^{s,m,d})$. To keep our results as general as possible, we will *not* impose the constraint from Eq. (16), but treat ε^s and ε^d as completely independent matrices. Thus, our formulas will be also applicable to experiments with fundamentally different production and detection processes, e.g. to a neutrino factory, where the production occurs through a purely leptonic $\nu\nu e\mu$ vertex, while the detection process $\nu l u d$ involves coupling to quarks. For reactors and superbeams, it is, of course, straightforward to impose Eq. (16) *a posteriori*.

A. The $\bar{\nu}_e \rightarrow \bar{\nu}_e$ channel

In a reactor experiment, the ratio L/E is chosen close to the first atmospheric oscillation maximum, so we can safely neglect terms proportional to $\Delta m_{21}^2/\Delta m_{31}^2$. Moreover, matter effects are irrelevant, i.e. we can take $a_{\text{CC}} = 0$. Finally, we will neglect terms suppressed by s_{13}^3 , εs_{13}^2 , or ε^2 . The last approximation implies that we only consider the interference terms between standard and non-standard contributions, but not the pure, incoherent, NSI effect. This is justified for most realistic extensions of the standard model, where $\varepsilon \ll 1$, but it has been pointed out in [28] that, from current model-independent experimental limits, the NSI might even dominate over the standard oscillations in some situations. We find for the oscillation probability

$$\begin{aligned}
P_{\bar{\nu}_e^s \rightarrow \bar{\nu}_e^d} = & 1 - 4s_{13}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + 2|\epsilon_{ee}^s| \cos \phi_{ee}^s + 2|\epsilon_{ee}^d| \cos \phi_{ee}^d - 4|\epsilon_{e\mu}^s| s_{13} s_{23} \cos(\delta_{\text{CP}} - \phi_{e\mu}^s) \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& + 2|\epsilon_{e\mu}^s| s_{13} s_{23} \sin(\delta_{\text{CP}} - \phi_{e\mu}^s) \sin \frac{\Delta m_{31}^2 L}{2E} - 4|\epsilon_{e\tau}^s| s_{13} c_{23} \cos(\delta_{\text{CP}} - \phi_{e\tau}^s) \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& + 2|\epsilon_{e\tau}^s| s_{13} c_{23} \sin(\delta_{\text{CP}} - \phi_{e\tau}^s) \sin \frac{\Delta m_{31}^2 L}{2E} - 4|\epsilon_{\mu e}^d| s_{13} s_{23} \cos(\delta_{\text{CP}} + \phi_{\mu e}^d) \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& - 2|\epsilon_{\mu e}^d| s_{13} s_{23} \sin(\delta_{\text{CP}} + \phi_{\mu e}^d) \sin \frac{\Delta m_{31}^2 L}{2E} - 4|\epsilon_{\tau e}^d| s_{13} c_{23} \cos(\delta_{\text{CP}} + \phi_{\tau e}^d) \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& - 2|\epsilon_{\tau e}^d| s_{13} c_{23} \sin(\delta_{\text{CP}} + \phi_{\tau e}^d) \sin \frac{\Delta m_{31}^2 L}{2E} + \mathcal{O}\left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right) + \mathcal{O}(\epsilon s_{13}^2) + \mathcal{O}(s_{13}^3) + \mathcal{O}(\epsilon^2). \tag{28}
\end{aligned}$$

It is interesting to remark that, due to the ϵ_{ee}^s and ϵ_{ee}^d terms, this expression can be different from unity even for $\Delta m_{31}^2 L/4E \ll 1$, i.e. at the near detector (ND) site. Indeed, we obtain in this case

$$\begin{aligned}
P_{\bar{\nu}_e^s \rightarrow \bar{\nu}_e^d}^{\text{ND}} = & 1 + 2|\epsilon_{ee}^s| \cos \phi_{ee}^s + 2|\epsilon_{ee}^d| \cos \phi_{ee}^d + |\epsilon_{ee}^s|^2 + |\epsilon_{ee}^d|^2 + 2|\epsilon_{ee}^s| |\epsilon_{ee}^d| [\cos(\phi_{ee}^s + \phi_{ee}^d) + \cos(\phi_{ee}^s - \phi_{ee}^d)] \\
& + 2|\epsilon_{e\mu}^s| |\epsilon_{\mu e}^d| \cos(\phi_{\mu e}^s + \phi_{e\mu}^d) + 2|\epsilon_{e\tau}^s| |\epsilon_{\tau e}^d| \cos(\phi_{e\tau}^s + \phi_{e\tau}^d) + \mathcal{O}\left(\frac{\Delta m_{31}^2 L}{4E}\right) + \mathcal{O}(\epsilon^3), \tag{29}
\end{aligned}$$

where we have taken into account also second order terms in ϵ , which may be important in the near detector due to the large event rates. Equation (29) corresponds to an overall rescaling of the neutrino flux, which, however, will be hard to detect in a realistic experiment due to the systematical flux uncertainty.

B. The $\nu_\mu \rightarrow \nu_e$ channel

In the derivation of $P_{\nu_\mu^s \rightarrow \nu_e^d}$, we will relax our approximations from the previous section, and take into account also terms of $\mathcal{O}(s_{13} \Delta m_{21}^2 / \Delta m_{31}^2)$, $\mathcal{O}([\Delta m_{21}^2 / \Delta m_{31}^2]^2)$, and $\mathcal{O}(\epsilon \Delta m_{21}^2 / \Delta m_{31}^2)$, to reproduce the correct δ_{CP} dependence. For experiments with a relatively short baseline, such as T2K, it is justified to assume vacuum oscillations, if the ϵ^m parameters are $\leq \mathcal{O}(0.1)$ (in Sec. V, we will discuss cases where this is not true, and we will see that nonstandard matter effects can then be large in T2K). The vacuum oscillation probability reads

$$\begin{aligned}
P_{\nu_\mu^s \rightarrow \nu_e^d}^{\text{vac}} = & 4s_{13}^2 s_{23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right)^2 c_{23}^2 s_{2 \times 12}^2 \left(\frac{\Delta m_{31}^2 L}{4E}\right)^2 \\
& + \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{13} s_{2 \times 12} s_{2 \times 23} \cos \delta_{\text{CP}} \frac{\Delta m_{31}^2 L}{4E} \sin \frac{\Delta m_{31}^2 L}{2E} - 2 \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{13} s_{2 \times 12} s_{2 \times 23} \sin \delta_{\text{CP}} \frac{\Delta m_{31}^2 L}{4E} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& - 4|\epsilon_{\mu e}^s| s_{13} s_{23} \cos(\phi_{\mu e}^s + \delta_{\text{CP}}) \sin^2 \frac{\Delta m_{31}^2 L}{4E} - 2|\epsilon_{\mu e}^s| s_{13} s_{23} \sin(\phi_{\mu e}^s + \delta_{\text{CP}}) \sin \frac{\Delta m_{31}^2 L}{2E} \\
& - 4|\epsilon_{\mu e}^d| s_{13} c_{2 \times 23} s_{23} \cos(\phi_{\mu e}^d + \delta_{\text{CP}}) \sin^2 \frac{\Delta m_{31}^2 L}{4E} - 2|\epsilon_{\mu e}^d| s_{13} s_{23} \sin(\phi_{\mu e}^d + \delta_{\text{CP}}) \sin \frac{\Delta m_{31}^2 L}{2E} \\
& + 4|\epsilon_{\tau e}^d| s_{13} s_{2 \times 23} s_{23} \cos(\phi_{\tau e}^d + \delta_{\text{CP}}) \sin^2 \frac{\Delta m_{31}^2 L}{4E} - |\epsilon_{\mu e}^s| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} c_{23} \sin \phi_{\mu e}^s \frac{\Delta m_{31}^2 L}{2E} \\
& + 2|\epsilon_{\mu e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23}^2 c_{23} \cos \phi_{\mu e}^d \frac{\Delta m_{31}^2 L}{4E} \sin \frac{\Delta m_{31}^2 L}{2E} \\
& - |\epsilon_{\mu e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} c_{23} \sin \phi_{\mu e}^d \frac{\Delta m_{31}^2 L}{2E} \left[1 - 2s_{23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{2E}\right] \\
& + 2|\epsilon_{\tau e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \cos \phi_{\mu e}^d \frac{\Delta m_{31}^2 L}{4E} \sin \frac{\Delta m_{31}^2 L}{2E} + 2|\epsilon_{\tau e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \sin \phi_{\mu e}^d \frac{\Delta m_{31}^2 L}{2E} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& + \mathcal{O}\left(\left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^3\right) + \mathcal{O}\left(\left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^2 s_{13}\right) + \mathcal{O}\left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{13}^2\right) + \mathcal{O}(s_{13}^3) + \mathcal{O}\left(\epsilon \left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^2\right) + \mathcal{O}\left(\epsilon \tilde{s}_{13} \frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right) \\
& + \mathcal{O}(\epsilon s_{13}^2) + \mathcal{O}(\epsilon^2). \tag{30}
\end{aligned}$$

The corresponding expression for the near detector is

$$P_{\nu_\mu^s \rightarrow \nu_e^d}^{\text{vac,ND}} = |\epsilon_{\mu e}^s|^2 + |\epsilon_{\mu e}^d|^2 + 2|\epsilon_{\mu e}^s||\epsilon_{\mu e}^d| \cos(\phi_{\mu e}^s - \phi_{\mu e}^d) + \mathcal{O}\left(\frac{\Delta m_{31}^2 L}{4E}\right) + \mathcal{O}(\epsilon^3). \quad (31)$$

If the baseline is longer, as is the case e.g. in NO ν A, matter effects are important. To keep the notation concise in this case, we define the effective 13-mixing angle in matter, which is given to lowest order by

$$\tilde{s}_{13} \equiv \frac{\Delta m_{31}^2}{\Delta m_{31}^2 - a_{\text{CC}}} s_{13} + \mathcal{O}(s_{13}^2). \quad (32)$$

The oscillation probability is then

$$\begin{aligned} P_{\nu_\mu^s \rightarrow \nu_e^d}^{\text{mat}} = & 4\tilde{s}_{13}^2 s_{23}^2 \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} + \left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right)^2 c_{23}^2 s_{2\times 12}^2 \left(\frac{\Delta m_{31}^2}{a_{\text{CC}}}\right)^2 \sin^2 \frac{a_{\text{CC}}L}{4E} \\ & - \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \tilde{s}_{13} s_{2\times 12} s_{2\times 23} \cos \delta_{\text{CP}} \frac{\Delta m_{31}^2}{a_{\text{CC}}} \left[\sin^2 \frac{a_{\text{CC}}L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & - \frac{1}{2} \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \tilde{s}_{13} s_{2\times 12} s_{2\times 23} \sin \delta_{\text{CP}} \frac{\Delta m_{31}^2}{a_{\text{CC}}} \left[\sin \frac{a_{\text{CC}}L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \\ & - 4|\epsilon_{\mu e}^s| \tilde{s}_{13} s_{23} \cos(\phi_{\mu e}^s + \delta_{\text{CP}}) \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} - 2|\epsilon_{\mu e}^s| \tilde{s}_{13} s_{23} \sin(\phi_{\mu e}^s + \delta_{\text{CP}}) \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \\ & + 4|\epsilon_{\mu e}^d| \tilde{s}_{13} s_{23} \cos(\phi_{\mu e}^d + \delta_{\text{CP}}) \left[c_{23}^2 \sin^2 \frac{a_{\text{CC}}L}{4E} - c_{23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + s_{23}^2 \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & + 2|\epsilon_{\mu e}^d| \tilde{s}_{13} s_{23} \sin(\phi_{\mu e}^d + \delta_{\text{CP}}) \left[c_{23}^2 \sin \frac{a_{\text{CC}}L}{2E} - c_{23}^2 \sin \frac{\Delta m_{31}^2 L}{2E} - s_{23}^2 \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \\ & - 4|\epsilon_{\tau e}^d| \tilde{s}_{13} s_{23}^2 c_{23} \cos(\phi_{\tau e}^d + \delta_{\text{CP}}) \left[\sin^2 \frac{a_{\text{CC}}L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} - \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & - 2|\epsilon_{\tau e}^d| \tilde{s}_{13} s_{23}^2 c_{23} \sin(\phi_{\tau e}^d + \delta_{\text{CP}}) \left[\sin \frac{a_{\text{CC}}L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \\ & - 4|\epsilon_{e\mu}^m| \tilde{s}_{13} s_{23} c_{23}^2 \cos(\phi_{e\mu}^m + \delta_{\text{CP}}) \left[\sin^2 \frac{a_{\text{CC}}L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & - 2|\epsilon_{e\mu}^m| \tilde{s}_{13} s_{23} c_{23}^2 \sin(\phi_{e\mu}^m + \delta_{\text{CP}}) \left[\sin \frac{a_{\text{CC}}L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \\ & + 8|\epsilon_{e\mu}^m| \tilde{s}_{13} s_{23}^3 \cos(\phi_{e\mu}^m + \delta_{\text{CP}}) \frac{a_{\text{CC}}}{\Delta m_{31}^2 - a_{\text{CC}}} \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \\ & + 4|\epsilon_{e\tau}^m| \tilde{s}_{13} s_{23}^2 c_{23} \cos(\phi_{e\tau}^m + \delta_{\text{CP}}) \left[\sin^2 \frac{a_{\text{CC}}L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & + 2|\epsilon_{e\tau}^m| \tilde{s}_{13} s_{23}^2 c_{23} \sin(\phi_{e\tau}^m + \delta_{\text{CP}}) \left[\sin \frac{a_{\text{CC}}L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \\ & + 8|\epsilon_{e\tau}^m| \tilde{s}_{13} s_{23}^2 c_{23} \cos(\phi_{e\tau}^m + \delta_{\text{CP}}) \frac{a_{\text{CC}}}{\Delta m_{31}^2 - a_{\text{CC}}} \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \\ & + 2|\epsilon_{\mu e}^s| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2\times 12} c_{23} \cos \phi_{\mu e}^s \frac{\Delta m_{31}^2}{a_{\text{CC}}} \sin^2 \frac{a_{\text{CC}}L}{4E} - |\epsilon_{\mu e}^s| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2\times 12} c_{23} \sin \phi_{\mu e}^s \frac{\Delta m_{31}^2}{a_{\text{CC}}} \sin \frac{a_{\text{CC}}L}{2E} \\ & - 2|\epsilon_{\mu e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2\times 12} c_{23} \cos \phi_{\mu e}^d \frac{\Delta m_{31}^2}{a_{\text{CC}}} \left[c_{23}^2 \sin^2 \frac{a_{\text{CC}}L}{4E} - s_{23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + s_{23}^2 \sin^2 \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E} \right] \\ & - |\epsilon_{\mu e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2\times 12} c_{23} \sin \phi_{\mu e}^d \frac{\Delta m_{31}^2}{a_{\text{CC}}} \left[c_{23}^2 \sin \frac{a_{\text{CC}}L}{2E} + s_{23}^2 \sin \frac{\Delta m_{31}^2 L}{2E} - s_{23}^2 \sin \frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E} \right] \end{aligned}$$

$$\begin{aligned}
& + 2|\epsilon_{\tau e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \cos \phi_{\tau e}^d \frac{\Delta m_{31}^2}{a_{CC}} \left[\sin^2 \frac{a_{CC} L}{4E} + \sin^2 \frac{\Delta m_{31}^2 L}{4E} - \sin^2 \frac{(\Delta m_{31}^2 - a_{CC}) L}{4E} \right] \\
& + |\epsilon_{\tau e}^d| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \sin \phi_{\tau e}^d \frac{\Delta m_{31}^2}{a_{CC}} \left[\sin \frac{a_{CC} L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{CC}) L}{2E} \right] \\
& + 4|\epsilon_{e\mu}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} c_{23}^3 \cos \phi_{e\mu}^m \frac{\Delta m_{31}^2}{a_{CC}} \sin^2 \frac{a_{CC} L}{4E} \\
& - 2|\epsilon_{e\mu}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23}^2 c_{23} \cos \phi_{e\mu}^m \frac{\Delta m_{31}^2}{\Delta m_{31}^2 - a_{CC}} \left[\sin^2 \frac{a_{CC} L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \sin^2 \frac{(\Delta m_{31}^2 - a_{CC}) L}{4E} \right] \\
& + |\epsilon_{e\mu}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23}^2 c_{23} \sin \phi_{e\mu}^m \frac{\Delta m_{31}^2}{\Delta m_{31}^2 - a_{CC}} \left[\sin \frac{a_{CC} L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{CC}) L}{2E} \right] \\
& - 4|\epsilon_{e\tau}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \cos \phi_{e\tau}^m \frac{\Delta m_{31}^2}{a_{CC}} \sin^2 \frac{a_{CC} L}{4E} \\
& - 2|\epsilon_{e\tau}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \cos \phi_{e\tau}^m \frac{\Delta m_{31}^2}{\Delta m_{31}^2 - a_{CC}} \left[\sin^2 \frac{a_{CC} L}{4E} - \sin^2 \frac{\Delta m_{31}^2 L}{4E} + \sin^2 \frac{(\Delta m_{31}^2 - a_{CC}) L}{4E} \right] \\
& + |\epsilon_{e\tau}^m| \frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{2 \times 12} s_{23} c_{23}^2 \sin \phi_{e\tau}^m \frac{\Delta m_{31}^2}{\Delta m_{31}^2 - a_{CC}} \left[\sin \frac{a_{CC} L}{2E} - \sin \frac{\Delta m_{31}^2 L}{2E} + \sin \frac{(\Delta m_{31}^2 - a_{CC}) L}{2E} \right] \\
& + \mathcal{O}\left(\left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^3\right) + \mathcal{O}\left(\left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^2 s_{13}\right) + \mathcal{O}\left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2} s_{13}^2\right) + \mathcal{O}(s_{13}^3) \\
& + \mathcal{O}\left(\epsilon \left[\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right]^2\right) + \mathcal{O}\left(\epsilon s_{13} \frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right) + \mathcal{O}(\epsilon s_{13}^2) + \mathcal{O}(\epsilon^2). \tag{33}
\end{aligned}$$

Most of the $\mathcal{O}(\Delta m_{21}^2/\Delta m_{31}^2)$ terms contain factors of $\Delta m_{31}^2/a_{CC}$, which can be large at low matter densities, and might therefore seem to spoil the accuracy of the expansion in this case. However, the oscillatory terms in square brackets become small as $\Delta m_{31}^2/a_{CC}$ becomes large, so that overall, the $\mathcal{O}(\Delta m_{21}^2/\Delta m_{31}^2)$ terms remain subdominant even if the vacuum limit is approached.

C. The $\nu_\mu \rightarrow \nu_\mu$ channel

For $P_{\nu_\mu^s \rightarrow \nu_\mu^d}$, we obtain

$$\begin{aligned}
P_{\nu_\mu^s \rightarrow \nu_\mu^d}^{\text{vac}} &= 1 - s_{2 \times 23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + 2|\epsilon_{\mu\mu}^s| \cos \phi_{\mu\mu}^s + 2|\epsilon_{\mu\mu}^d| \cos \phi_{\mu\mu}^d \\
& - [2|\epsilon_{\mu\mu}^s| \cos \phi_{\mu\mu}^s + 2|\epsilon_{\mu\mu}^d| \cos \phi_{\mu\mu}^d] s_{2 \times 23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} - 2(|\epsilon_{\mu\tau}^s| \cos \phi_{\mu\tau}^s + |\epsilon_{\tau\mu}^d| \cos \phi_{\tau\mu}^d) c_{2 \times 23} s_{2 \times 23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& + (|\epsilon_{\mu\tau}^s| \sin \phi_{\mu\tau}^s + |\epsilon_{\tau\mu}^d| \sin \phi_{\tau\mu}^d) s_{2 \times 23} \sin \frac{\Delta m_{31}^2 L}{2E} + \mathcal{O}\left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right) + \mathcal{O}(s_{13}) + \mathcal{O}(\epsilon^2) + \mathcal{O}(\epsilon^2) \tag{34}
\end{aligned}$$

in vacuum, and

$$\begin{aligned}
P_{\nu_\mu^s \rightarrow \nu_\mu^d}^{\text{mat}} &= 1 - s_{2 \times 23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} + 2|\epsilon_{\mu\mu}^s| \cos \phi_{\mu\mu}^s + 2|\epsilon_{\mu\mu}^d| \cos \phi_{\mu\mu}^d - [2|\epsilon_{\mu\mu}^s| \cos \phi_{\mu\mu}^s + 2|\epsilon_{\mu\mu}^d| \cos \phi_{\mu\mu}^d] s_{2 \times 23}^2 \sin^2 \frac{\Delta m_{31}^2 L}{4E} \\
& - 2(|\epsilon_{\mu\tau}^s| \cos \phi_{\mu\tau}^s + |\epsilon_{\tau\mu}^d| \cos \phi_{\tau\mu}^d) c_{2 \times 23} s_{2 \times 23} \sin^2 \frac{\Delta m_{31}^2 L}{4E} + (|\epsilon_{\mu\tau}^s| \sin \phi_{\mu\tau}^s + |\epsilon_{\tau\mu}^d| \sin \phi_{\tau\mu}^d) s_{2 \times 23} \sin \frac{\Delta m_{31}^2 L}{2E} \\
& - |\epsilon_{\mu\tau}^m| \left[s_{2 \times 23}^3 \cos \phi_{\mu\tau}^m \frac{a_{CC} L}{2E} \sin \frac{\Delta m_{31}^2 L}{2E} + 4s_{2 \times 23} c_{2 \times 23}^2 \cos \phi_{\mu\tau}^m \frac{a_{CC}}{\Delta m_{31}^2} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \right] \\
& + \frac{1}{2} |\epsilon_{\mu\mu}^m| \left[s_{2 \times 23}^2 c_{2 \times 23} \frac{a_{CC} L}{2E} \sin \frac{\Delta m_{31}^2 L}{2E} - 4s_{2 \times 23}^2 c_{2 \times 23} \frac{a_{CC}}{\Delta m_{31}^2} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \right] \\
& - \frac{1}{2} |\epsilon_{\tau\tau}^m| \left[s_{2 \times 23}^2 c_{2 \times 23} \frac{a_{CC} L}{2E} \sin \frac{\Delta m_{31}^2 L}{2E} - 4s_{2 \times 23}^2 c_{2 \times 23} \frac{a_{CC}}{\Delta m_{31}^2} \sin^2 \frac{\Delta m_{31}^2 L}{4E} \right] + \mathcal{O}\left(\frac{\Delta m_{21}^2}{\Delta m_{31}^2}\right) + \mathcal{O}(s_{13}) + \mathcal{O}(\epsilon^2) \tag{35}
\end{aligned}$$

in matter.

D. Interpretation

To understand the physical origin of the formulas derived in the previous sections, let us consider Figs. 1–3, where we show schematically the possible reaction chains that a neutrino can follow before its detection. We also indicate the respective suppression factors of the transition amplitude, but to simplify the discussion and to improve the clarity of the figures, we do not explicitly show contributions proportional to $\Delta m_{21}^2/\Delta m_{31}^2$, which would appear in concurrence to the θ_{13} -suppressed processes if θ_{13} is very small. Dotted lines indicate suppression due to standard effects, while dashed lines represent transitions that are suppressed by the nonstandard parameters. The thick paths are those followed by the standard oscillation channels, while light gray lines indicate paths that are suppressed by more than one ε parameter, and are therefore mostly negligible. In Table II we summarize the same considerations in tabular form. In the first part of the discussion, we will assume ε^s and ε^d to be completely independent in order to keep the discussion as general as possible. The constraints from Eqs. (16) and (17) will only be implemented afterwards.

On the reactor side, we can read off from Fig. 1 and Table II, that, in the presence of just one type of non-

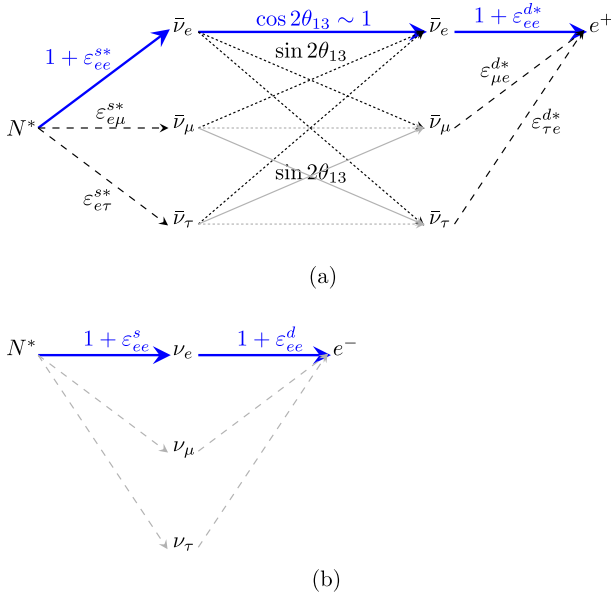


FIG. 1 (color online). Possible contributions of ε^s and ε^d to the event rate in the far detector (a), and the near detector (b) of a reactor $\bar{\nu}_e$ disappearance experiment. Thick lines indicate the reaction chain for standard oscillations. Dotted lines indicate processes that are suppressed by standard three-flavor effects proportional to θ_{13} or $\Delta m_{21}^2/\Delta m_{31}^2$, while dashed lines represent transitions that are suppressed due to nonstandard interactions. Paths which would only be accessible in the presence of two different nonstandard effects, are shown in light gray since they are usually subdominant.

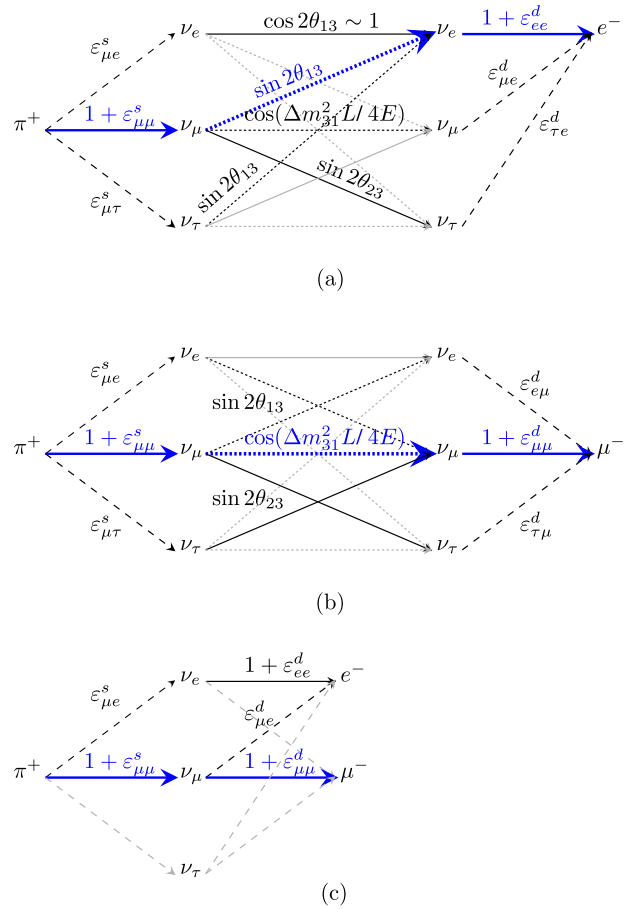


FIG. 2 (color online). Possible contributions of ε^s and ε^d to the event rate in a superbeam experiment for the appearance channel (a), the disappearance channel (b), and in the near detector (c). The meaning of the line styles is the same as in Fig. 1.

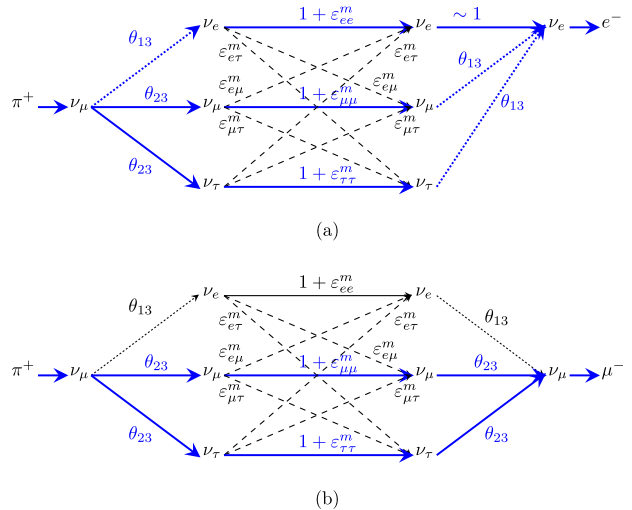


FIG. 3 (color online). Possible contributions of ε^m to the event rate in the superbeam appearance channel (a), and in the corresponding disappearance channel (b). The meaning of the line styles is the same as in Fig. 1.

TABLE II. Classification of the reparametrized nonstandard interactions ε^s , ε^d , and ε^m according to their impact on the transition amplitudes for reactor and superbeam experiments. For each NSI coupling, only the leading order effect is shown. The framed entries highlight those terms that are the most relevant to the determination of θ_{13} (see text for details).

NSI	Reactor		Superbeam		
	$\bar{\nu}_e$ disappearance	Effect in ND	ν_e appearance	ν_μ disappearance	Effect in ND
None	1		$\sin 2\theta_{13}$	$\cos(\Delta m_{31}^2 L/4E)$	
ε_{ee}^s $\varepsilon_{e\mu}^s$ $\varepsilon_{e\tau}^s$ $\varepsilon_{\mu e}^s$ $\varepsilon_{\mu\mu}^s$ $\varepsilon_{\mu\tau}^s$ $\varepsilon_{\tau e}^s$ $\varepsilon_{\tau\mu}^s$ $\varepsilon_{\tau\tau}^s$	ε $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$	Modified $\bar{\nu}_e$ flux	ε $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$	$\varepsilon \sin 2\theta_{13}$ $\varepsilon \cos(\Delta m_{31}^2 L/4E)$ ε	Modified ν_e flux Modified ν_μ flux
ε_{ee}^d $\varepsilon_{e\mu}^d$ $\varepsilon_{e\tau}^d$ $\varepsilon_{\mu e}^d$ $\varepsilon_{\mu\mu}^d$ $\varepsilon_{\mu\tau}^d$ $\varepsilon_{\tau e}^d$ $\varepsilon_{\tau\mu}^d$ $\varepsilon_{\tau\tau}^d$	ε $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$	Modified $\bar{\nu}_e$ flux	$\varepsilon \sin 2\theta_{13}$ $\varepsilon \cos(\Delta m_{31}^2 L/4E)$ ε	$\varepsilon \sin 2\theta_{13}$ $\varepsilon \cos(\Delta m_{31}^2 L/4E)$ ε	Modified ν_e flux Modified ν_μ flux
$\varepsilon_{ee}^s = \varepsilon_{ee}^{d*}$ $\varepsilon_{e\mu}^s = \varepsilon_{e\mu}^{d*}$ $\varepsilon_{e\tau}^s = \varepsilon_{e\tau}^{d*}$ $\varepsilon_{\mu e}^s = \varepsilon_{\mu e}^{d*}$ $\varepsilon_{\mu\mu}^s = \varepsilon_{\mu\mu}^{d*}$ $\varepsilon_{\mu\tau}^s = \varepsilon_{\mu\tau}^{d*}$	ε $\varepsilon \sin 2\theta_{13} + \varepsilon^2$ $\varepsilon \sin 2\theta_{13} + \varepsilon^2$	Modified $\bar{\nu}_e$ flux Modified $\bar{\nu}_e$ flux Modified $\bar{\nu}_e$ flux	$\varepsilon \sin 2\theta_{13}$ $\varepsilon \cos(\Delta m_{31}^2 L/4E)$ ε $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$	$\varepsilon \sin 2\theta_{13} + \varepsilon^2$ $\varepsilon \cos(\Delta m_{31}^2 L/4E)$ ε	Modified ν_e flux Modified ν_μ flux
ε_{ee}^m $\varepsilon_{e\mu}^m$ $\varepsilon_{e\tau}^m$ $\varepsilon_{\mu\mu}^m$ $\varepsilon_{\mu\tau}^m$ $\varepsilon_{\tau\tau}^m$			$\varepsilon \sin 2\theta_{13}$ ε ε $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$	$\varepsilon \sin^2 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$ $\varepsilon \sin 2\theta_{13}$ $\varepsilon \cos 2\theta_{23}^a$ ε $\varepsilon \cos 2\theta_{23}^a$	

^aThe factor $\cos 2\theta_{23}$ cannot be derived from Fig. 3, but only from Eq. (35).

standard interaction, only ε_{ee}^s , $\varepsilon_{e\mu}^s$, $\varepsilon_{e\tau}^s$, ε_{ee}^d , $\varepsilon_{\mu e}^d$, and $\varepsilon_{\tau e}^d$ are relevant. Of these, ε_{ee}^s and ε_{ee}^d have an $\mathcal{O}(\varepsilon)$ effect which could even exceed standard oscillations if it were not for the near detector, where these parameters would induce a similar effect as in the far detector. Since the absolute reactor neutrino flux is not known precisely, the measurement relies on the *relative* counting rates in both detectors, so that the impact of ε_{ee}^s and ε_{ee}^d is canceled. The remaining NSI, $\varepsilon_{e\mu}^s$, $\varepsilon_{e\tau}^s$, $\varepsilon_{\mu e}^d$, and $\varepsilon_{\tau e}^d$, contribute to the oscillation probability at $\mathcal{O}(\varepsilon \sin 2\theta_{13})$ (or at $\mathcal{O}(\varepsilon \sin 2\theta_{13} + \varepsilon^2)$, if the constraint $\varepsilon_{e\alpha}^s = \varepsilon_{\alpha e}^{d*}$ from Eq. (16) is implemented). This can be comparable to the standard term, so that these NSI are expected to have a large impact on the far detector. They do not affect the near detector as long as only one of

them is present, but if Eq. (16) is taken into account, the near detector will receive an $\mathcal{O}(\varepsilon^2)$ contribution that can be important in some situations. All these considerations are nicely confirmed by Eq. (28).

For a superbeam experiment, Fig. 2 and Table II show that, as long as only one type of NSI is taken into account, $\varepsilon_{\mu e}^s$, $\varepsilon_{\mu\mu}^s$, $\varepsilon_{\mu\tau}^s$ can affect the production process, while ε_{ee}^d , $\varepsilon_{e\mu}^d$, $\varepsilon_{\mu e}^d$, $\varepsilon_{\mu\mu}^d$, $\varepsilon_{\tau e}^d$, and $\varepsilon_{\tau\mu}^d$ may be important in the detector. The propagation can be affected by all entries of ε^m . As for the reactor case, the suppression factors associated with these different processes can be understood from simple physical arguments, which are confirmed in a more rigorous way by Eqs. (30) and (34). Let us discuss the different types of NSI in more detail:

- (1) $\varepsilon_{e\mu}^d$ and $\varepsilon_{\tau\mu}^d$ affect only the disappearance channel and are therefore irrelevant for the measurement of θ_{13} (they may, however, lead to wrong results for the leading atmospheric parameters).
- (2) $\varepsilon_{\mu\mu}^d$ also affects the disappearance channel, but it can also lead to a modified ν_μ rate in the near detector, and therefore to wrong assumptions on the initial neutrino flux. This, in turn, could lead to a misinterpretation of the far detector appearance measurement, so that the θ_{13} measurement is influenced indirectly. The effect in the near detector is suppressed by ε , so it will affect the far detector analysis only at the subleading level of $\varepsilon \sin^2 2\theta_{13}$.
- (3) $\varepsilon_{\mu\mu}^s$, $\varepsilon_{\mu\tau}^s$, and ε_{ee}^d are relevant for the appearance channel, but the corresponding *amplitude* is suppressed by $\varepsilon \sin 2\theta_{13}$, so that in the oscillation *probability*, we would obtain a subdominant contribution of $\mathcal{O}(\varepsilon \sin^2 2\theta_{13})$ from the interference of the standard and nonstandard terms.
- (4) $\varepsilon_{\mu e}^s$, $\varepsilon_{\mu e}^d$, and $\varepsilon_{\tau e}^d$ have *amplitudes* of $\mathcal{O}(\varepsilon)$, i.e. they contribute to the appearance *probability* on the level of $\varepsilon \sin 2\theta_{13}$, which can be comparable to the leading contribution $\sim \sin^2 2\theta_{13}$. $\varepsilon_{\mu e}^d$, however, is suppressed by a factor of $\cos(\Delta m_{31}^2 L/4E)$, which is small at the first atmospheric maximum around which the beam is centered. Note also that the modified ν_e flux in the near detector that is expected in the presence of $\varepsilon_{\mu e}^s$ or $\varepsilon_{\mu e}^d$ can help to actually detect the NSI, although part of it may be misinterpreted as a systematical error on the intrinsic beam background.
- (5) Of the nonstandard matter effects, only $\varepsilon_{e\mu}^m$ and $\varepsilon_{e\tau}^m$ contribute at leading order to the appearance probability $P_{\nu_\mu^s \rightarrow \nu_e^d}^{\text{mat}}$. Of these, $\varepsilon_{e\mu}^m$ is already strongly constrained experimentally [47], and so is not expected to have a large impact on reactor and superbeam experiments. $\varepsilon_{e\tau}^m$, on the other hand, could contribute significantly to the superbeam appearance channel, in accordance with [8,30]. All other nonstandard matter effects are suppressed by an additional power of s_{13} , (or, more correctly, \tilde{s}_{13} , which is, however, still small since we are far from the MSW resonance).

It is interesting to observe that the sensitivity to ε_{ee}^m is very weak, although this type of interaction corresponds to a simple rescaling of the standard MSW potential. However, it is not a leading order effect, and therefore does not appear in our approximate formula, Eq. (33).

- (6) In $P_{\nu_\mu^s \rightarrow \nu_\mu^d}^{\text{mat}}$ the dominant matter effect is $\varepsilon_{\mu\tau}^m$, and since there is no θ_{13} suppression from the interference with the standard amplitude, this effect is even stronger than those in $P_{\nu_\mu^s \rightarrow \nu_e^d}^{\text{mat}}$. Note that, from Fig. 3, one might expect $\varepsilon_{\mu\mu}^m$ and $\varepsilon_{\tau\tau}^m$ to be of similar

strength as $\varepsilon_{\mu\tau}^m$, but when one performs the calculation, it turns out that an additional suppression factor $c_{2 \times 23}$ appears [cf. Eq. (35)].

- (7) The implementation of the constraints $\varepsilon_{e\alpha}^s = \varepsilon_{\alpha e}^{d*}$ [Eq. (16)] and $|\varepsilon_{\mu\alpha}^s| \geq |\varepsilon_{\alpha\mu}^d|$ [Eq. (17)] does not lead to any new effects, except for the appearance of an additional ε^2 term in the disappearance channel for $\varepsilon_{\mu e}^s = \varepsilon_{e\mu}^{d*}$.

Let us finally emphasize the crucial importance of the standard and nonstandard phases in the oscillation probabilities: The formulas from Secs. III A, III B, and III C reveal that unfavorable phase combinations may suppress nonstandard effects, even if the modulus of the corresponding ε parameter is large.

IV. SIMULATION OF REACTOR AND SUPERBEAM EXPERIMENTS

To fully assess the high-level consequences of nonstandard interactions for realistic reactor and superbeam experiments, we have performed numerical simulations using the GLOBES software [69,70]. We have considered the following scenarios:

- (1) T2K+Double Chooz. Our simulation of the T2K far detector, Super Kamiokande, is based on [71]. Most parameters are taken from the T2K letter of intent [48], and the systematical uncertainties are based on [72]. We include a separate 1.0 kt water Čerenkov near detector with similar properties as the far detector, and similar systematical uncertainties. To model the interplay of the two detectors, we introduce a common 10% uncertainty on the neutrino flux, and a common 20% error on the number of background events in the ν_e appearance channel. In the absence of nonstandard interactions, these correlated errors would cancel completely, since the total neutrino flux and the background contribution are effectively calibrated by the near detector, but if $\varepsilon^{s,d} \neq 0$, this calibration can be wrong, and there may be an observable effect. The neutrino interaction cross sections are taken from [60,73]. We assume 3 years of neutrino running and 3 years of antineutrino running, each with a beam power of 0.77 MW. The fiducial far detector mass is 22.5 kt, and the baseline is 295 km. We consider ν_e appearance events as well as the ν_μ disappearance signal. The background for the disappearance channel is made up of neutral current events, while for the appearance measurement, neutral current events, misidentified muons, and the intrinsic beam backgrounds can contribute. For the simulation of Double Chooz, we use the same parameters as in [53], and the cross sections for inverse beta decay are taken from [74]. As for T2K, we simulate the near and far detectors sepa-

rately, but take into account the appropriate correlations between systematical errors. In particular, we introduce a 2.8% flux normalization error, which is correlated between the near and far detectors, uncorrelated 0.6% fiducial mass errors for both detectors, uncorrelated 0.5% energy calibration uncertainties, and an 0.5% bin-to-bin uncorrelated error.

- (2) NO ν A+DC-200, where DC-200 refers to a reactor experiment similar to Double Chooz, but with a 200 t far detector [53]. Such a large reactor experiment has a considerable sensitivity not only to the total event rate, but also to distortions of the energy spectrum.

The simulation of the ν_e appearance signal in NO ν A is based on [50], while for the ν_μ disappearance channel, we follow [75]. We assume 3 years of neutrino running and 3 years of antineutrino running, with a beam power of 1.12 MW. The far detector mass is 25 kt, and the baseline is 812 km, with an average matter density of 2.8 g/cm³ along the trajectory, while the near detector has a mass of 0.0204 kt, and is located at 1 km from the target. Again, we introduce, in addition to the uncorrelated systematical errors from [50,75], a correlated 10% uncertainty on the total neutrino flux, and a correlated 20% error on the ν_e background.

The parameters and systematical errors of the DC-200 scenario are identical to those of Double Chooz.

Unless indicated otherwise, we calculate the respective event rates using the following “true” values for the oscillation parameters [76]:

$$\begin{aligned}\sin^2 2\theta_{12}^{\text{true}} &= 0.84, \\ \sin^2 2\theta_{23}^{\text{true}} &= 1.0, \\ \sin^2 2\theta_{13}^{\text{true}} &= 0.05, \\ \delta_{\text{CP}}^{\text{true}} &= 0.0, \\ (\Delta m_{21}^2)^{\text{true}} &= 7.9 \times 10^{-5} \text{ eV}^2, \\ (\Delta m_{31}^2)^{\text{true}} &= 2.6 \times 10^{-3} \text{ eV}^2,\end{aligned}\tag{36}$$

and assume a normal mass hierarchy. To analyze the simulated data, we follow the statistical procedure described in the appendix of [71], and define the following χ^2 function:¹

$$\chi^2 = \min_{\lambda} \sum_j^{\text{channel}} \sum_i^{\text{bin}} \frac{|N_{ij}(\lambda^{\text{true}}, \varepsilon^{\text{true}}) - N_{ij}(\lambda, \varepsilon = 0)|^2}{N_{ij}(\lambda^{\text{true}}, \varepsilon^{\text{true}})} + \text{Priors},\tag{37}$$

where N_{ij} denotes the number of events in the i -th energy

¹In the implementation of superbeam experiments, we assume the events to follow the Poisson distribution. However, for illustrative purposes, it is sufficient to consider the more compact approximative Gaussian expression.

bin for oscillation channel j , the vector $\lambda = (\theta_{12}, \theta_{13}, \theta_{23}, \delta_{\text{CP}}, \Delta m_{21}^2, \Delta m_{31}^2, \vec{b})$ contains the standard oscillation parameters and the systematical biases \vec{b} , and ε represents the nonstandard parameters. In the fit, we marginalize χ^2 over all standard oscillation parameters and over the systematical biases, but since we want to study how a standard-oscillation fit gets modified if there are nonstandard interactions, we keep the NSI parameters fixed at 0.² The prior terms implement external input from other experiments and have the form $(x - x^{\text{true}})^2 / \sigma_x^2$, where x stands for any oscillation parameter or systematical bias, and σ_x is the corresponding externally given uncertainty. We assume θ_{12} to be known to within 10%, and Δm_{21}^2 to within 5% from solar and reactor experiments [76]. When analyzing the reactor experiment alone, we additionally assume a 15% uncertainty on θ_{23} and a 5% error on Δm_{31}^2 . Beam experiments are themselves sensitive to θ_{23} and Δm_{31}^2 , so we omit these priors for them.

V. NSI-INDUCED OFFSETS AND DISCREPANCIES IN θ_{13} FITS

Using the simulation techniques discussed in the previous section, we can now determine the errors that are introduced when nonstandard interactions are present in reactor and superbeam experiments, but are not properly taken into account in the respective fits. Possible outcomes of such fits are shown in Fig. 4 for our two scenarios. As true parameter values, we have taken $\sin^2 2\theta_{13} = 0.05$ and $\delta_{\text{CP}} = \pi$, and the NSI contribution was assumed to be $\varepsilon_{e\tau}^m = 0.5e^{-i\pi/2}$ in the upper panel, and $\varepsilon_{e\tau}^s = \varepsilon_{\tau e}^d = 0.05$ [fulfilling Eq. (16)] in the lower panel. These NSI parameters are rather large, but still consistent with current bounds [31,47]. According to the discussion in Sec. III, only the superbeam experiment should be affected in the first case, while in the second case, there should be an impact on both experiments. The shaded areas show the 90% confidence regions for the reactor experiment, while the contours are for the superbeam. The data has been calculated under the assumption of a normal mass hierarchy, but the fit has been performed for both the normal mass ordering (solid contours) and for the inverted ordering (dashed contours). The vertical line and the diamonds represent the respective best fit values, while the star stands for the assumed true parameter values. We have assumed 2 degrees of freedom for the superbeam experiments, and 1 degree of freedom for the reactor setups, which are insensitive to δ_{CP} .

It is obvious from the plots that the standard oscillation fit to θ_{13} and δ_{CP} can be severely wrong if NSI are present. This observation is similar to the one made in [34] for a

²Of course, when computing confidence intervals for certain parameters, we have to keep these parameters fixed as well.

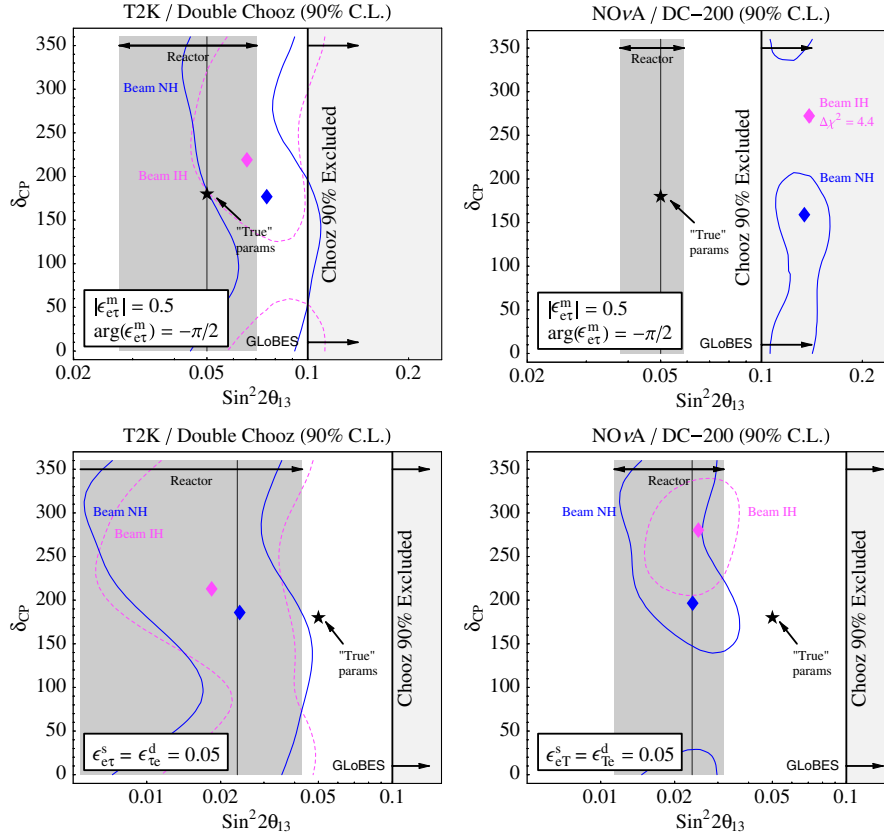


FIG. 4 (color online). Two examples for the errors that are introduced if nonstandard interactions are neglected when fitting θ_{13} and δ_{CP} to the data of reactor and superbeam experiments. In the upper plots, a discrepancy arises between the two experiments (the $\text{NO}\nu\text{A}$ fit is even above the Chooz bound), while in the lower plots, there is a common offset, leading to consistent results, but erroneously “ruling out” the true θ_{13} (indicated by the black star) at a high confidence level. The left-hand plots are for T2K and Double Chooz, and the right-hand ones are for $\text{NO}\nu\text{A}$ and DC-200. The gray shading represents the 90% confidence region from the reactor experiment, and the vertical black line shows the corresponding best fit value for θ_{13} . The 90% contours from the superbeam are shown as solid dark gray lines for a normal hierarchy fit, and as dashed light gray lines for an inverted hierarchy fit. The diamonds represent the corresponding best fit values. In interpreting the computed χ^2 values, we have assumed 2 degrees of freedom for the beam experiments, and 1 degree of freedom for the reactor setups.

neutrino factory. In the case shown in the upper plots of Fig. 4, the reactor experiment gives the correct best fit value, but the superbeam results conflict with this measurement. In the case of $\text{NO}\nu\text{A}$, we even obtain a fit value above the Chooz bound and a fake 90% hint to the mass hierarchy, indicated by the fact that, within the resolution of the plot, the 90% contour reduces to a single point. In the second case (lower plots), both experiment agree very well, but they erroneously seem to rule out the true θ_{13} .

Of course, the NSI scenarios analyzed in Fig. 4 were only two examples, and a more systematic analysis of nonstandard interactions in reactor and superbeam experiments is desirable. This is done in Figs. 5–7, where we show how the (standard oscillation) θ_{13} fits in T2K/Double Chooz, respectively, in $\text{NO}\nu\text{A}/\text{DC-200}$ may be distorted in the presence of nonstandard interactions. For each diagram, only one of the independent ε parameters was assumed to be nonzero, but we have ensured that

Eqs. (16) and (17) are fulfilled. In particular, we did not consider the hypothetical case $\varepsilon_{\mu\alpha}^s = 0$, $\varepsilon_{\alpha\mu}^d \neq 0$, but only $\varepsilon_{\mu\alpha}^s \neq 0$, $\varepsilon_{\alpha\mu}^d = 0$, and $\varepsilon_{\mu\alpha}^s = \varepsilon_{\alpha\mu}^d \neq 0$. Moreover we omit all entries of ε^m except $\varepsilon_{e\tau}^m$, because they are either strongly constrained already ($\varepsilon_{e\mu}^m$), or do not have any impact on the θ_{13} measurements (ε_{ee}^m , $\varepsilon_{\mu\mu}^m$, $\varepsilon_{\mu\tau}^m$, and $\varepsilon_{\tau\tau}^m$). The modulus of each parameter has been varied between 0 and its current upper bound, which is 0.1 for $\varepsilon_{\alpha\beta}^{s,d}$ from universality in charged lepton decays [31], and 0.7 for $\varepsilon_{e\tau}^m$ [47].³ The complex phases were allowed to vary between 0 and 2π . For each combination of $|\varepsilon|$ and $\arg(\varepsilon)$, we have then performed a fit assuming standard oscilla-

³Note that, according to the naive estimate from Eq. (7), such large values of $|\varepsilon|$ would correspond to $M_{\text{NSI}} \sim \mathcal{O}(100 \text{ GeV})$. In many models, such low new physics scales are already ruled out, but in our model-independent treatment, they are still viable.

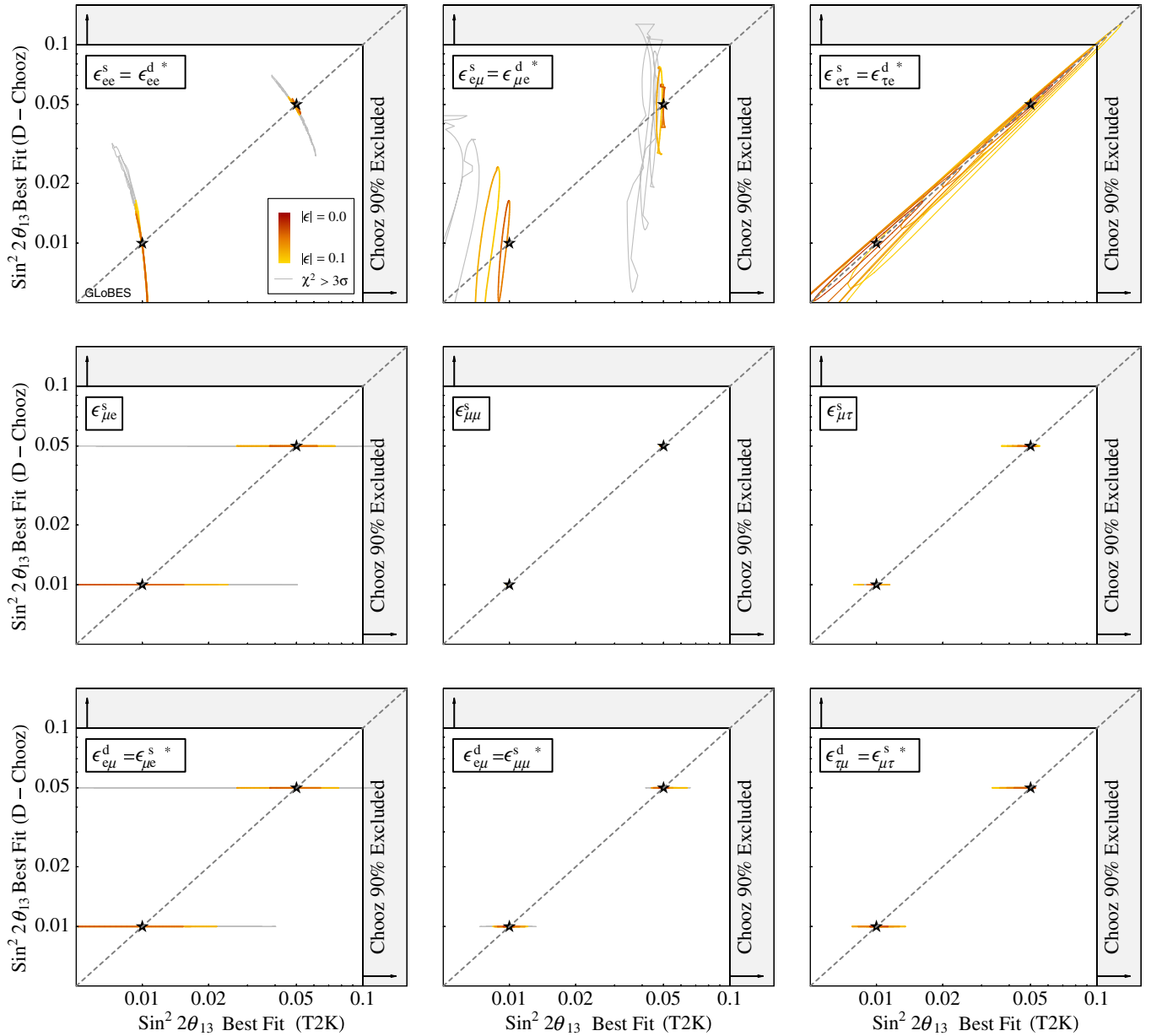


FIG. 5 (color online). Distortion of the θ_{13} fits in T2K and Double Chooz in the presence of $\varepsilon_{\alpha\beta}^s$ and $\varepsilon_{\beta\alpha}^d$. For each plot, the modulus of the corresponding ε parameter has been varied from 0 to 0.1, and its phase from 0 to 2π . For every such combination, we show the result of standard oscillation fits of θ_{13} . Connected lines represent contours of equal $|\varepsilon_{\alpha\beta}|$ and varying phase. Dark gray lines correspond to $|\varepsilon_{\alpha\beta}| = 0$, while medium gray lines correspond to $|\varepsilon_{\alpha\beta}| = 0.1$. Points giving a quality of fit worse than 3σ in at least one of the two experiments are plotted in light gray. The black stars indicate the assumed true $\sin^2 2\theta_{13}$.

tions, and the resulting best fit values for θ_{13} are shown in the plots. Points giving a good fit (better than 3σ in both experiments), are drawn as thick lines, with the hue indicating the respective value of $|\varepsilon|$. Dark gray corresponds to $|\varepsilon| = 0$, while medium gray corresponds to the upper bound of $|\varepsilon|$. Points giving a fit quality worse than 3σ are shown by thin light gray lines, and the information on $|\varepsilon|$ is omitted for them. All computations have been performed for two different true values, $\sin^2 2\theta_{13} = 0.01$ and $\sin^2 2\theta_{13} = 0.05$, as indicated by the black stars.

By comparing the plots with Table II, we find that our expectations for the impact of the different ε parameters from the discussion in Sec. III are confirmed. A particularly interesting situation arises for $\varepsilon_{\tau e}^d$, because this parameter has a sizeable effect in both the reactor experiment and the superbeam setup. It is especially dangerous because it induces a similar offset in both experiments, i.e. one would find perfectly consistent θ_{13} fits, which might, however, be far away from the true value.

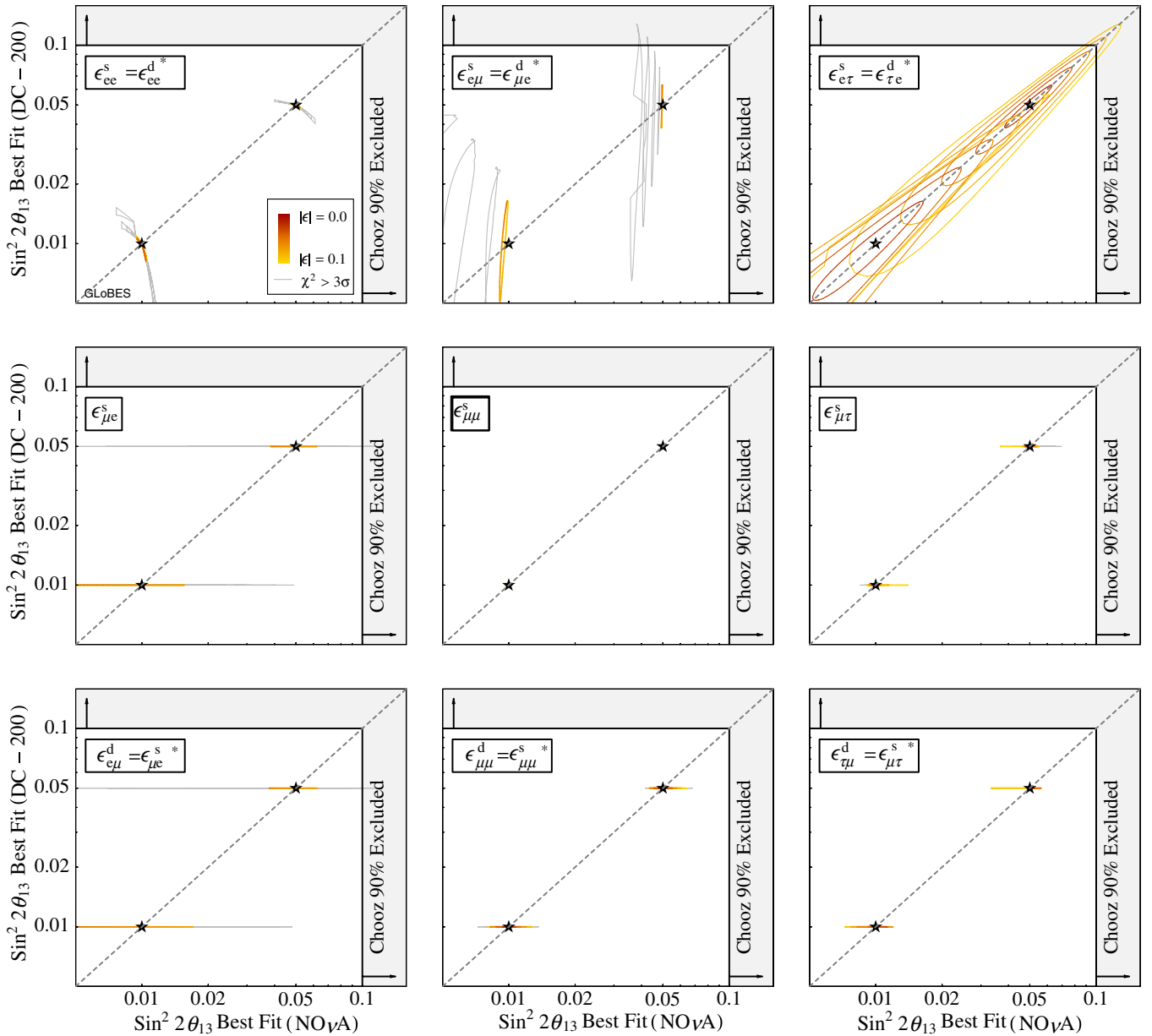


FIG. 6 (color online). Effect of $\varepsilon_{\alpha\beta}^s$ and $\varepsilon_{\beta\alpha}^d$ on the θ_{13} fits in NO ν A and DC-200. The shading is the same as in Fig. 5.

Other parameters may lead to fit points far from the diagonal, corresponding to seemingly conflicting fits. An interesting case is the $\varepsilon_{\mu e}^d$ term, for which the nonstandard interaction mimics a significantly modified ν_e flux in the near detector. This, in turn, leads to a miscalibration of the beam-intrinsic backgrounds, so that, at the far site, many of the actually oscillation-induced ν_e events will be mistaken as background. Thus, the fit value for θ_{13} becomes too small. However, we can also read off from the plot that, in this situation, the quality of the standard oscillation fit becomes so bad that the NSI effect can actually be detected. Note that the curves for large $|\varepsilon_{\mu e}^d|$ look slightly untidy, because for some parameter values, the smallest χ^2 is provided by the normal hierarchy fit,

while for others the inverted hierarchy fit is marginally better. Therefore, frequent “jumps” between these two solutions occur.

When interpreting Figs. 5 and 6, it is important to keep in mind that the error bars of the experiments considered here are rather large (cf. Fig. 4), so that even sizeable deviations from the diagonals will in most cases only create some tension, but no unambiguous contradiction between the beam and reactor fits.

Of the nonstandard matter effects, we expect from Table II that only $\varepsilon_{e\mu}^m$ and $\varepsilon_{e\tau}^m$ should have any effect on the θ_{13} fits. $\varepsilon_{e\mu}^m$ is already strongly constrained from charged lepton flavor violation experiments [47], but $\varepsilon_{e\tau}^m$ may still have a large impact. In fact, for extreme values of

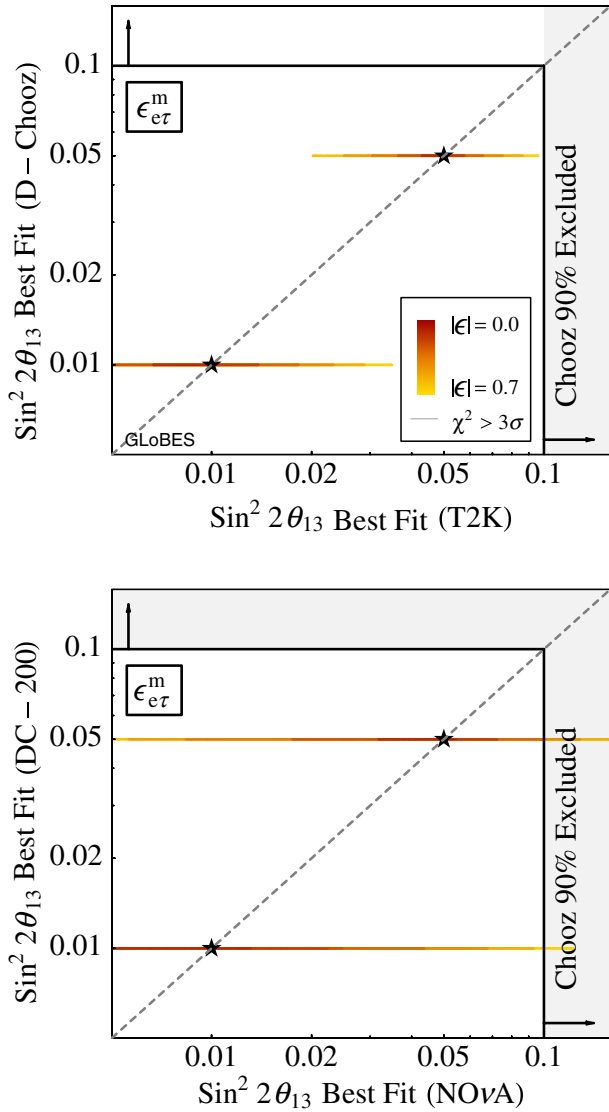


FIG. 7 (color online). Effect of $\epsilon_{e\tau}^m$ on the θ_{13} fits in T2K and Double Chooz, resp. in NO ν A and DC-200. We do not show plots for the other entries of ϵ^m , since these are either strongly constrained already ($\epsilon_{e\mu}^m$), or do not affect the θ_{13} measurement ($\epsilon_{ee}^m, \epsilon_{\mu\mu}^m, \epsilon_{\mu\tau}^m$, and $\epsilon_{\tau\tau}^m$). The shading is the same as in Fig. 5, but the scale is different since the bound on $\epsilon_{e\tau}^m$ is weaker than that for $\epsilon_{\alpha\beta}^{s,d}$ [31,47].

this parameter, there is even the possibility that NO ν A would erroneously report a θ_{13} value above the Chooz bound.

Let us emphasize that, in order to obtain reliable estimates for the impact of nonstandard interactions on reactor and superbeam experiments, it is crucial to take the information from the near detectors into account. To show this, we have also studied how Figs. 5 and 6 get modified if we use a simplified simulation, in which the near detector does not appear explicitly, but only through suitably small values for the systematical uncertainties. In doing so, we have

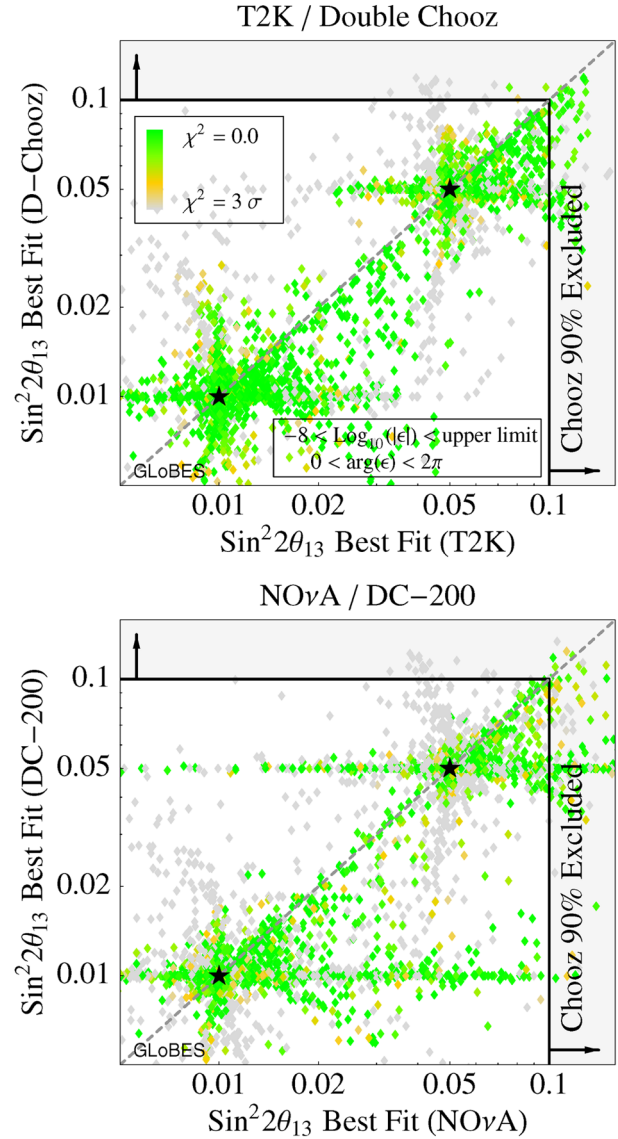


FIG. 8 (color online). Possible outcomes of standard three-flavor oscillation fits to reactor and superbeam data in the presence of nonstandard interactions. Each plot contains two datasets, one for $\sin^2 2\theta_{13}^{\text{true}} = 0.01$, and one for $\sin^2 2\theta_{13}^{\text{true}} = 0.05$ (indicated by the black stars). For each dataset, 5000 random combinations of ϵ parameters were chosen, with their moduli being distributed logarithmically between 10^{-8} and the respective upper bounds [31,47], and their phases varying linearly between 0 and 2π . Each of these random nonstandard scenarios was then fitted under the assumption of standard three-flavor oscillations. Dark gray points indicate a very good quality of this fit, while light gray points denote a fit quality worse than 3σ in at least one of the two experiments, i.e. an effective discovery of the nonstandard effect. The plots show that nonstandard interactions can induce ostensible discrepancies between reactor and superbeam data (off-diagonal points), or a common offset (close-to-diagonal points), which would lead to consistent, but wrong results. Note that some points lie even above the Chooz bound. A reactor fit above the Chooz bound indicates that the corresponding combination of NSI parameters and $\theta_{13}^{\text{true}}$ could already be ruled out using existing data.

again treated ε^s and ε^d as completely independent matrices, possibly violating Eqs. (16) and (17). Thus, the results are also applicable to setups where ε^s and ε^d are indeed unrelated. In accordance with our expectations from Table II, we have found:

- (1) For ε_{ee}^s and ε_{ee}^d , the effect on the reactor becomes stronger without the proper treatment of the near detector, because these terms no longer cancel then. Moreover, the discovery potential becomes worse, i.e. there will be fewer light gray segments in the plot.
- (2) For the superbeam, the discovery of $\varepsilon_{\mu e}^s$ and $\varepsilon_{\mu e}^d$ becomes also much harder without the near detector, because the clear signature of an apparently modified ν_e flux at the near site is no longer available. Moreover, for $\varepsilon_{\mu e}^d$, the strong impact of the NSI on the θ_{13} fit in the superbeam, which we have identified as a near detector effect in the above discussion, vanishes in the single-detector simulation.
- (3) The contours for $\varepsilon_{e\tau}^s = \varepsilon_{e\tau}^{d*}$ are deformed without the near detector because in this (unrealistic) situation, it is no longer possible to misinterpret the nonstandard effect as a reactor flux calibration error. Note that this misinterpretation is only due to the fact that $\varepsilon_{e\tau}^s$ and $\varepsilon_{e\tau}^{d*}$ are identical, since the near detector is only affected if both are present (cf. Table II). Otherwise, it would retain its capability to properly calibrate the reactor flux to its true value.

So far, we have only considered situations in which one nonstandard parameter is dominant, and all others are negligible. In realistic models, however, many parameters may be of the same order of magnitude. Since it is impossible to visualize the resulting high-dimensional parameter space, we resort to the scatter plots shown in Fig. 8. These plots were created by choosing a random value for each NSI parameter, and then performing a standard oscillation fit to the resulting experimental data. The moduli of the ε parameters were logarithmically distributed between 10^{-8} and their current upper limits, where we have assumed the model-independent bound from universality in charged lepton decays [31] for ε^s and ε^d , and the results of [47] for ε^m . The phases were distributed linearly between 0 and 2π .

We can see from Fig. 8 that there are again points which yield a clear discrepancy in the θ_{13} fits of the reactor and superbeam data, and others which correspond to a common offset of the fit value. The shading shows that for a considerable fraction of the parameter space, the nonstandard effect can actually be discovered. It is interesting to observe that there are some points for which the reactor fit lies above the Chooz bound. This indicates that already with the present data, some parts of the parameter space could be ruled out.

VI. DISCOVERY REACH FOR NONSTANDARD INTERACTIONS IN A COMBINED ANALYSIS OF REACTOR AND SUPERBEAM DATA

Let us now discuss the prospects of actually detecting the presence of nonstandard interactions in reactor and superbeam experiments. We define the *discovery reach* as the range of ε parameters for which the quality of a standard oscillation fit is below a given confidence level. In Figs. 9–12, we show numerical results for this quantity, which were obtained by performing standard oscillation fits to the combined data of *both* experiments.

The results can again be interpreted with the help of Table II and of the formulas derived in Sec. III. We see that for those nonstandard parameters which have a large impact on any of the observed oscillation channels, there is typically also a good discovery potential. For some parameters, it comes from the reactor measurement, for others, it is dominated by the superbeam. It is remarkable, however, that in the case $\varepsilon_{e\tau}^s = \varepsilon_{e\tau}^{d*}$, there is practically no discovery potential at all, because neither experiment can discover these parameters on its own, and there is also no significant discrepancy between them, but only a common offset in their θ_{13} fits.

It is interesting to observe that the good discovery reach for $\varepsilon_{\mu\tau}^s$ comes from the *disappearance* channel, as can be easily verified from the corresponding analytical formulas in Sec. III. Note that in those plots where $\varepsilon_{\mu\tau}^s = \varepsilon_{\tau\mu}^{d*}$ is assumed, there is no discovery potential because the corresponding NSI terms in Eq. (34) cancel.

The discovery reach depends strongly on the phases of the NSI coupling constants, $\phi_{\alpha\beta}^{s,d,m}$. To first order in s_{13} , all off-diagonal entries of the ε matrices (except the $\varepsilon_{\tau\mu}^s$ and $\varepsilon_{\mu\tau}^d$ contributions in the $\nu_\mu \rightarrow \nu_\mu$ disappearance channel) are accompanied by a combination of $\phi_{\alpha\beta}^{s,d,m}$ and δ_{CP} . To first order in $\Delta m_{21}^2/\Delta m_{31}^2$, they typically appear together with factors of $\cos\phi_{\alpha\beta}^{s,d}$ or $\sin\phi_{\alpha\beta}^{s,d}$. The diagonal components of the ε matrices usually have prefactors of $\cos\phi_{\alpha\alpha}^{s,d}$.

The plots do not exhibit any phase dependence in the discovery reach for $\varepsilon_{\mu e}^s$ and $\varepsilon_{\mu e}^d$ because the sensitivity to these parameters comes mainly from the modified ν_e flux in the near detector of the superbeam experiment. We have checked, that, in accordance with Eq. (30), the phase dependence would reappear if the near detector were omitted in the simulation.

Turning to nonstandard matter effects described by ε^m , it is clear that the discovery potential will be very limited, since already standard matter effects are small in T2K and NO ν A, and completely negligible in Double Chooz and DC-200. Therefore, we use a different scale for the horizontal axis in Figs. 11 and 12. However, for some entries of ε^m , the present bounds are very weak. In particular we have $\varepsilon_{ee}^m \lesssim 1.0$, $\varepsilon_{e\tau}^m \lesssim 0.7$, and $\varepsilon_{\tau\tau}^m \lesssim 1.4$ [47]. Figures 11 and 12 thus show that the bound on $\varepsilon_{e\tau}^m$ could be improved by NO ν A, but not by T2K. We should, however, keep in mind

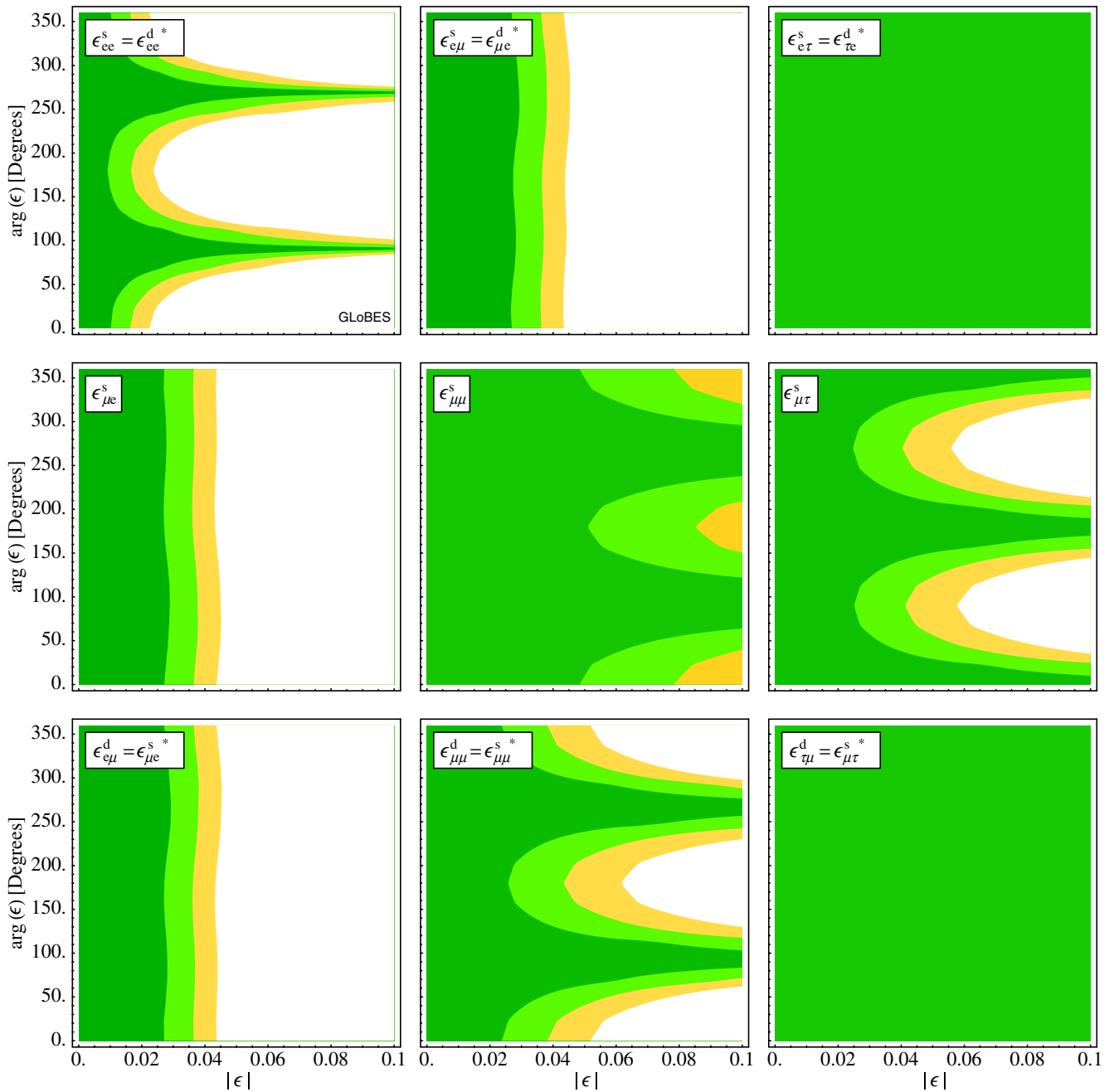


FIG. 9 (color online). Discovery reach for $\varepsilon_{\alpha\beta}^s$ and $\varepsilon_{\beta\alpha}^d$ in a combined analysis of T2K and Double Chooz. Contours for 1σ , 2σ , and 3σ are shown. A true value of $\sin^2 2\theta_{13}^{\text{true}} = 0.05$ was assumed, but we have checked that the results do not depend on $\sin^2 2\theta_{13}^{\text{true}}$.

that, according to Eq. (7), $|\varepsilon_{e\tau}^m| \sim 0.7$ corresponds to $M_{\text{NSI}} \sim 100$ GeV, and it is hard to imagine a model that could yield such a low NSI scale without violating present electroweak precision data. Both T2K and NO ν A have some sensitivity also to $\varepsilon_{e\mu}^m$ and $\varepsilon_{\mu\tau}^m$, but they cannot compete with the current bounds $\varepsilon_{e\mu}^m \lesssim 5 \cdot 10^{-4}$ and $\varepsilon_{\mu\tau}^m \lesssim 0.1$.

Note that, according to Eqs. (33) and (35), the sensitivity to $\varepsilon_{e\mu}^m$ and $\varepsilon_{e\tau}^m$ comes from the ν_e appearance channel,

while the sensitivity to $\varepsilon_{\mu\tau}^m$ has its origin in the disappearance channel.

Let us dwell for a moment on the interesting shape of the sensitivity contours for $\varepsilon_{e\tau}^m$ and $\varepsilon_{e\mu}^m$, which can only be understood by taking into account terms proportional to $|\varepsilon|^2$. Let us consider, for example, $\varepsilon_{e\mu}^m$. According to Eq. (33), the NSI contribution to the oscillation probability is, to first order in $|\varepsilon|$ and neglecting Δm_{21}^2 ,

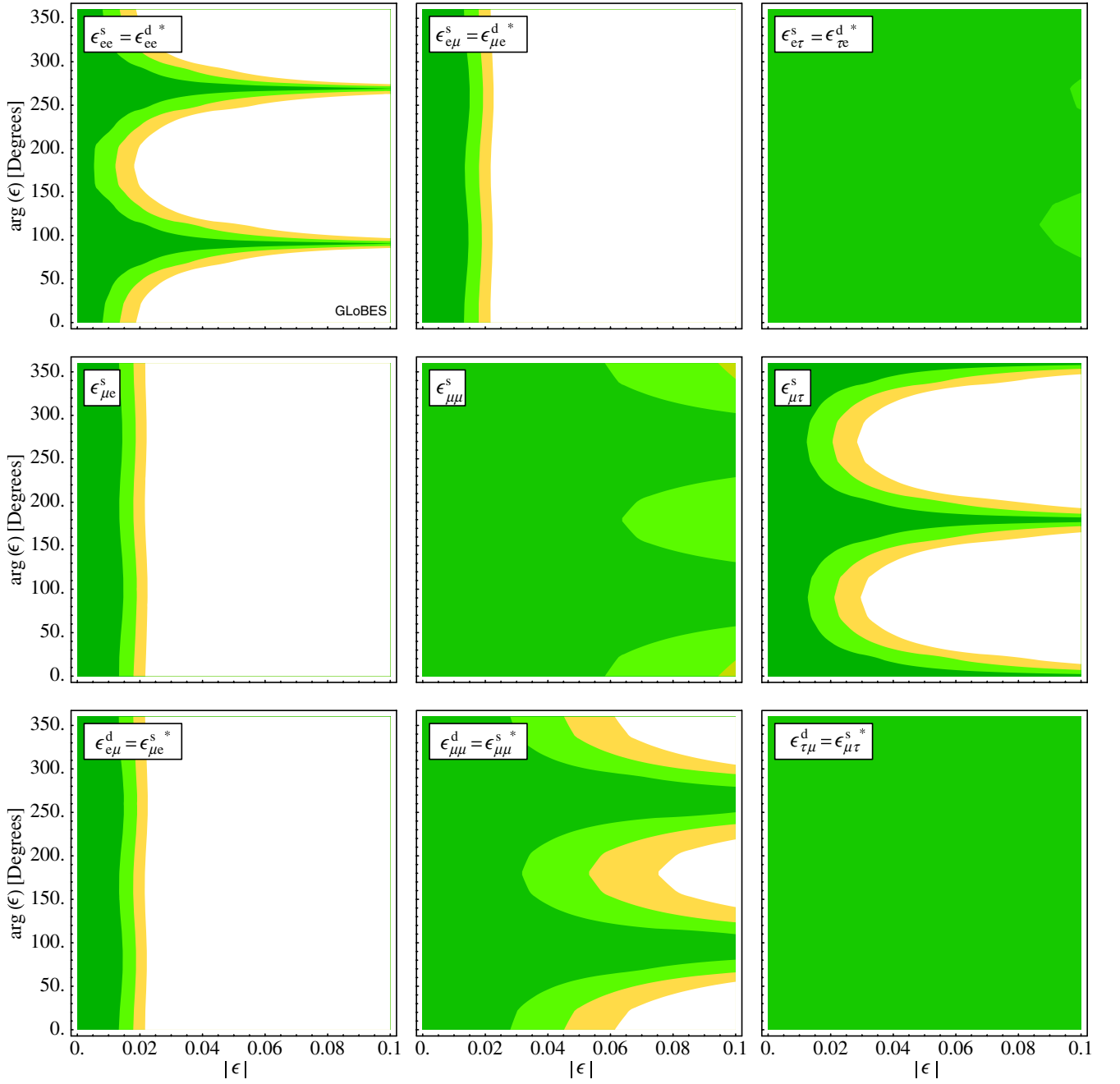


FIG. 10 (color online). Discovery reach for $\varepsilon_{\alpha\beta}^s$ and $\varepsilon_{\beta\alpha}^d$ in a combined analysis of NO ν A and DC-200. Contours for 1σ , 2σ , and 3σ are shown. A value of $\sin^2 2\theta_{13}^{\text{true}} = 0.05$ was assumed in the simulation, but we have checked that the results remain unchanged if we go to a different $\sin^2 2\theta_{13}^{\text{true}}$.

$$\begin{aligned}
& - 4|\epsilon_{e\mu}^m|s_{23}c_{23}^2\tilde{s}_{13}\cos(\phi_{e\mu}^m + \delta_{\text{CP}})\left[\sin^2\frac{a_{\text{CC}}L}{4E} - \sin^2\frac{\Delta m_{31}^2L}{4E} + \sin^2\frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E}\right] \\
& - 2|\epsilon_{e\mu}^m|s_{23}c_{23}^2\tilde{s}_{13}\sin(\phi_{e\mu}^m + \delta_{\text{CP}})\left[\sin\frac{a_{\text{CC}}L}{2E} - \sin\frac{\Delta m_{31}^2L}{2E} + \sin\frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{2E}\right] \\
& + 8|\epsilon_{e\mu}^m|s_{23}^3\tilde{s}_{13}\cos(\phi_{e\mu}^m + \delta_{\text{CP}})\frac{a_{\text{CC}}}{\Delta m_{31}^2 - a_{\text{CC}}}\sin^2\frac{(\Delta m_{31}^2 - a_{\text{CC}})L}{4E}. \tag{38}
\end{aligned}$$

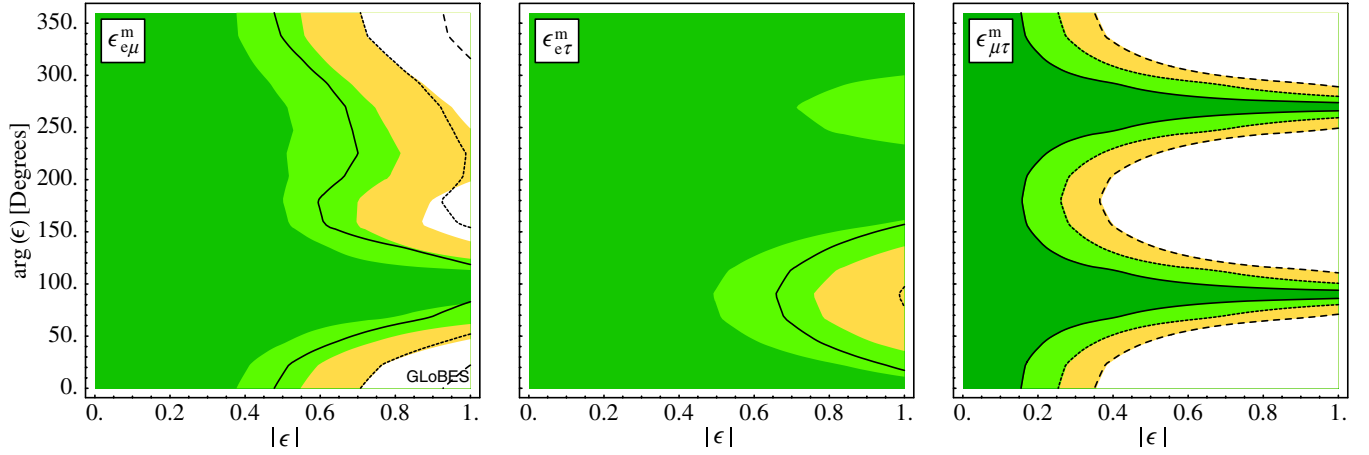


FIG. 11 (color online). Discovery reach for $\varepsilon_{\alpha\beta}^m$ in a combined analysis of T2K and Double Chooz. Since these experiments have essentially no sensitivity to ε_{ee}^m , $\varepsilon_{\mu\mu}^m$, and $\varepsilon_{\tau\tau}^m$, we show only the off-diagonal entries of ε^m . The shaded areas show the 1σ , 2σ , and 3σ confidence regions for $\sin^2 2\theta_{13} = 0.05$, while the black contours are for $\sin^2 2\theta_{13} = 0.01$. Note that the scaling of the horizontal axis is different from Figs. 9 and 10.

By carefully studying this expression, one finds that the energy dependence in the first and third terms of Eq. (38) is quite different from that of standard oscillations, which is proportional to $\sin^2(\Delta m_{31}^2 - a_{CC})L/4E$. Therefore, these terms will be easy to detect, while the second term, which modulates the spectrum in the same way as standard oscillations, can be absorbed into a modified θ_{13} fit, and will therefore be hard to detect. From the phase dependence of these terms, we expect that, for our choice of $\delta_{CP}^{\text{true}} = 0$, the discovery reach should be good for $\phi_{e\mu}^m \sim 0, \pi$, and poor for $\phi_{e\mu}^m \sim \frac{1}{2}\pi, \frac{3}{2}\pi$. The plots in Figs. 11 and 12 reveal that the discovery reach indeed shows this behavior, except for an unexpectedly good sensitivity at $\phi_{e\mu}^m = \frac{3}{2}\pi$. To understand this, we have to take into account the second order terms, which we have found to be

$$\begin{aligned}
 & 4|\varepsilon_{e\mu}^m|^2 c_{23}^4 \sin^2 \frac{a_{CC}L}{4E} \\
 & + 4|\varepsilon_{e\mu}^m|^2 s_{23}^4 \left(\frac{a_{CC}}{\Delta m_{31}^2 - a_{CC}} \right)^2 \sin^2 \frac{(\Delta m_{31}^2 - a_{CC})L}{4E} \\
 & + 2|\varepsilon_{e\mu}^m|^2 s_{23}^2 \frac{a_{CC}}{\Delta m_{31}^2 - a_{CC}} \cdot \cos \frac{\Delta m_{31}^2 L}{4E} \sin \frac{a_{CC}L}{4E} \\
 & \times \sin \frac{(\Delta m_{31}^2 - a_{CC})L}{4E}. \tag{39}
 \end{aligned}$$

The important observation is that the net effect of the second order terms is always positive, while for the first order terms, it is positive at $\phi_{e\mu}^m \approx \frac{3}{2}\pi$, and negative at

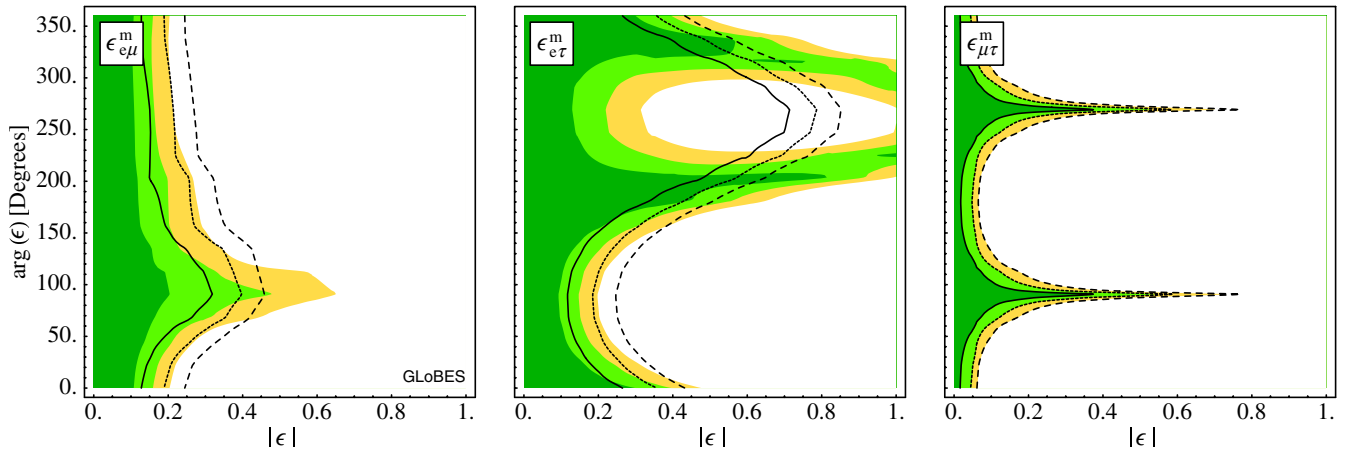


FIG. 12 (color online). Discovery reach for $\varepsilon_{\alpha\beta}^m$ in a combined analysis of NOνA and DC-200. Since these experiments have essentially no sensitivity to ε_{ee}^m , $\varepsilon_{\mu\mu}^m$, and $\varepsilon_{\tau\tau}^m$, we show only the off-diagonal entries of ε^m . The colored areas show the 1σ , 2σ , and 3σ confidence regions for $\sin^2 2\theta_{13} = 0.05$, while the black contours are for $\sin^2 2\theta_{13} = 0.01$. Note that the scaling of the horizontal axis is different from Figs. 9 and 10.

$\phi_{e\mu}^m \simeq \frac{1}{2}\pi$. In the first case, we would therefore need a much stronger deviation of the fitted θ_{13} from its true value in order to absorb the nonstandard term. This, however, is disfavored by the reactor measurement, so that the combined fit improves the discovery reach by a considerable amount at $\phi_{e\mu}^m \simeq \frac{3}{2}\pi$. We are here in the interesting situation that the combination of seemingly redundant data sets can be beneficial if there are deviations from standard three-flavor oscillations. For most other nonstandard parameters, the discovery reach is dominated by either the reactor or the superbeam.

VII. CONCLUSIONS

In this paper, we have studied the impact of nonstandard neutrino interactions on upcoming reactor and accelerator neutrino experiments. We have first classified the allowed NSI terms in the Lagrangian according to their Lorentz structure, and have found that many of them are irrelevant to reactor and superbeam setups. Those which can have an impact are mostly of the $(V - A)(V \pm A)$ type, but in superbeam experiments, also $(S + P)(S \pm P)$ type effects can be important. Since reactor and superbeam experiments are not able to distinguish different Lorentz structures, we have reparametrized the NSI coupling constants in order to greatly reduce the number of free parameters in the problem.

Using this reparametrization, we have then derived approximate analytic expressions for the nonstandard neutrino oscillation probabilities, both in vacuum and in matter of constant density. We have developed an intuitive understanding of the terms relevant to specific oscillation channels, and have classified them accordingly.

In the second part of our work, we have performed detailed numerical simulations using GLoBES. We have considered two scenarios: T2K combined with Double Chooz, and $\text{NO}\nu\text{A}$ combined with a 200 t reactor experiment, dubbed DC-200. Our simulations take into account parameter correlations, degeneracies, and systematical errors, and, in particular, we employ a realistic treatment of the near detectors. We have found that nonstandard interactions can have a sizeable impact on future reactor and superbeam experiments, if the coupling constants are close

to their current upper limits, and if complex phases do not conspire to cancel them. The biggest impact is on the θ_{13} measurement: If NSI are not properly taken into account in the fit, the results may be significantly wrong. There are scenarios in which a clear discrepancy between reactor and superbeam experiments shows up, but we can also have the situation that both fits sets seem to agree very well, but the derived θ_{13} value has a significant offset from the true value. It is even possible that the true θ_{13} is erroneously “ruled out” at 3σ . To detect this kind of problem, a third experiment, complementary to the other two, would be required. Thus, we see that the possibility of nonstandard effects should always be kept in mind when planning or analyzing upcoming experiments.

We have also studied the discovery potential for NSI in reactor and superbeam experiments, i.e. the range of nonstandard parameters, which can actually be detected by these experiments because the quality of a standard oscillation fit becomes poor. We have found that, depending on the complex phases, some NSI may be discovered if their coupling constants are not more than a factor of 5 smaller than the current upper bounds. The best discovery reach is obtained only if both reactor and superbeam experiments, and also the respective near detectors are considered in the analysis. In most cases, one of the experimental channels dominates the discovery reach, but there are also situations where only the discrepancy between the single-experiment fits indicates the presence of NSI. Our discussion thus shows that reactor and superbeam measurements, which might seem to be redundant in the standard three-flavor framework, turn out to be highly complementary once nonstandard effects are considered.

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