

# <span id="page-0-0"></span>Climates of Warm Earth-like Planets. II. Rotational "Goldilocks" Zones for Fractional Habitability and Silicate Weathering

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# **Abstract**

Planetary rotation rate has a significant effect on atmospheric circulation, where the strength of the Coriolis effect in part determines the efficiency of latitudinal heat transport, altering cloud distributions, surface temperatures, and precipitation patterns. In this study, we use the ROCKE-3D dynamic ocean general circulation model to study the effects of slow rotations and increased insolations on the "fractional habitability" and silicate weathering rate of an Earth-like world. Defining the fractional habitability  $f_h$  to be the percentage of a planet's surface that falls in the  $0 \leq T \leq 100$  °C temperature regime, we find a moderate increase in  $f_h$  with a 10% and 20% increase in insolation and a possible maximum in  $f_h$  at sidereal day lengths between 8 and 32 times that of the modern Earth. By tracking precipitation and runoff, we further determine that there is a rotational regime centered on a 4 day period in which the silicate weathering rate is maximized and is particularly strongly peaked at higher overall insolations. Because of weathering's integral role in the long-term carbonate–silicate cycle, we suggest that climate stability may be strongly affected by the anticipated rotational evolution of temperate terrestrial-type worlds and should be considered a major factor in their study. In light of our results, we argue that planetary rotation period is an important factor to consider when determining the habitability of terrestrial worlds.

Key words: atmospheric effects – methods: numerical – planets and satellites: atmospheres

## 1. Introduction

Modeling the atmospheres and surface environments of Earth-like worlds is a highly complex problem with potentially rich rewards in the field of exoplanetary science. Deepening our understanding and physical intuition of the forces governing a planet's climate not only allows us to speculate about the diversity of conditions and potential sustainability of life beyond our solar system, but also grants insight into the past, present, and future Earth.

The most complete method of climate modeling is the application of 3D general circulation models (GCMs). GCMs specialize in the diagnostics of atmospheric dynamics, with the ability to track wind velocities, changes in latent heat, differential albedos, and, in the case of the GCM used in this study (see below and Way et al. [2017](#page-7-0)), changes in oceanic energy transport and ground hydrology. Each GCM is unique in its capabilities and computational efficiency depending on the desired complexity of the model (see Eyring et al. [2016](#page-7-0) and references therein for information on recent climate model comparison efforts).

The rate at which a planet rotates about its axis has a significant impact on its atmospheric circulation. At the most fundamental level, the number and latitudinal extent of wind cells on a planet are determined, in part, by the strength of the Coriolis effect (Figure [1](#page-1-0)), which itself is determined by the planet's rotation period. Del Genio & Suozzo ([1987](#page-7-0)) used the Goddard Institute for Space Studies (GISS) Model 1 GCM to show that, for terrestrial bodies rotating more slowly than the Earth, the Hadley cell extends toward the poles and becomes the primary source of large-scale heat transport. This results in a more uniform temperature distribution across latitudes. The latitudinal extent of the Hadley cell also plays a significant role in large-scale precipitation patterns across a surface and is (for

example) responsible for arid desert regions occurring in northern Africa rather than in continental Europe here on Earth.

However, determining the precise origins and distributions of rocky planet rotations is a fundamental and challenging question in planetary and astronomical science. Because we can only observe the rotation rates of rocky planets in our own solar system, for now we must rely on theoretical predictions to estimate the ranges of possible rotation rates. For example, Miguel  $\&$  Brunini ([2010](#page-7-0)) suggest that the initial rotation periods of rocky planets range from 10 to 10,000 hr. Other work suggests that the upper limit of a planet's initial rotational velocity is bound by the magnitude of its surface gravity, i.e., the critical angular velocity of rotational stability (Kokubo & Ida [2007](#page-7-0)).

The rotation period of a planet at a given time is also dependent on its evolutionary path and frequency of encounters with exchanges in angular momentum, including star–planet and planet–moon tidal dissipation. For example, Barnes ([2017](#page-7-0)) shows that, for a moonless Earth with an initial rotation period of 3 days, stellar tides would cause its rotation to become synchronous within 4.5 Gyr. Evolution toward synchronized rotation due to tides is even swifter for potentially temperate planets around lower mass stars, with the spin-down rate following  $d\Omega/dt \propto M_{\star}^2/a^6$ , where a is the orbital semimajor<br>cysis (Coldraigh & Sotse 1066). For an Earth like planet in the axis (Goldreich & Soter [1966](#page-7-0)). For an Earth-like planet in the habitable zone of a Gliese 581-like M dwarf star, Heller et al. ([2011](#page-7-0)) show that the evolution timescale for equilibrium rotation is about 100 Myr. In light of these studies, the shape of the probability distribution of rocky planet rotation rates is debatable, although its range is most certainly wide. We do, however, expect a trend toward overall slower rotation rates with age due to star–planet tidal interactions.

Yang et al. ([2014](#page-7-0)) used the Community Atmosphere Model version 3.1 GCM (Collins et al. [2004](#page-7-0)) to show that clouds tend

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Figure 1. Illustration of the influence of the Coriolis effect on atmospheric circulation (arrows on the globe) for slowly rotating planets and more rapidly rotating planets. For reference, the wind cells on Earth are more similar to the diagram on the right.

to congregate around the substellar point of slowly rotating planets, thus increasing the planetary albedo and decreasing the surface temperature at that point, subsequently extending the inner habitable zone to smaller orbits. However, it is important to note that most of the Yang et al.  $(2014)$  $(2014)$  $(2014)$  study was conducted on an aquaplanet configuration, and because of the different heat capacities and albedos of land and ocean, we expect a significant land mass to have a nonzero effect on the overall climate.

In our study, we adopt the continental configuration of the Earth to study the effects of slow rotations and increased insolations on the climate of an Earth-like world using the Resolving Orbital and Climate Keys of Earth and Extraterrestrial Environments with Dynamics (ROCKE-3D) GCM developed by multiinstitutional collaboration at the GISS (Way et al. [2017](#page-7-0)). This model is further differentiated from those used in previous rotation studies in that ROCKE-3D uses a fully coupled dynamic ocean scheme rather than the static ocean model often adopted.

We investigate both the fractional habitability and silicate rock weathering of an Earth-like terrestrial world as key probes of short- and long-term climate states and stability. It is uncontroversial to state that the now-classical "zeroth-order" marker of habitability given by a global mean surface temperature (Kasting et al. [1993](#page-7-0); Kopparapu et al. [2013](#page-7-0)) is only a broad indicator of terrestrial planet environment; it is useful for a first pass evaluation of a system, but too basic for either predicting observable characteristics or potential for life. However, extending the parameterization of "habitability" to higher orders (e.g., details of atmospheric chemistry, hydrological features, orbit and rotation, planet composition and geophysics, and spatially resolved climate) quickly becomes cumbersome and uninformative in the absence of observable constraints on many variables. A variety of first-order or even second-order markers have been used to further refine habitability predictions (e.g., Spiegel et al. [2008](#page-7-0); Schulze-Makuch et al. [2011](#page-7-0)). In this study we perform a first-order analysis similar to that of Spiegel et al. ([2008](#page-7-0)) to evaluate the "habitability" of rocky worlds with rotation periods slower than that of modern Earth.

Furthermore, although the temperature range of  $0-100\degree C$  is not a strict set of boundaries for biochemistry and biological function (Rothschild & Mancinelli [2001](#page-7-0) and references therein), it does nonetheless encompass the temperature range over which known biochemistry takes place at high efficiency for modern Earth atmospheric surface pressures (Gillooly et al. [2001](#page-7-0);

Rothschild [2007](#page-7-0)). We also emphasize that because this temperature range is directly related to  $H_2O$  phase changes on a planet with an Earth-like atmospheric composition and surface gravity, it is centrally important to changes in surface albedo. These phase changes are also critical to the global climate state because of the contribution of latent heat to the overall energy transport in the atmosphere. In other words, in this present work we treat the term "habitability" as a convenient label, primarily for evaluating the physical and chemical environment of a rocky planet.

In Section 2 we describe the models used in this study and define the methods we use to determine the fractional habitability and silicate weathering rate from the model output. In Section [3](#page-3-0) we provide results on the behavior of surface temperature, fractional habitability, precipitation, and the silicate weathering rate for longer rotation periods. In Section [4](#page-5-0) we discuss the implications of these results, and present a brief conclusion in Section [5](#page-7-0).

# 2. Methods

# 2.1. GCM Model

The ROCKE-3D GCM was developed from the NASA GISS' preexisting ModelE2 GCM (Schmidt et al. [2014](#page-7-0)), whose publicly available model results for Earth climate studies continue to be utilized by the international community. ROCKE-3D was created for the purpose of extending the capabilities of ModelE2 toward modeling exoplanet atmospheres and rocky solar system planet atmospheres. For this study, we use ROCKE-3D's dynamic ocean capabilities, which are fully coupled to the model atmosphere. A brief description of the key elements of the models used in this study is below. For a more comprehensive description of ROCKE-3D, we refer the reader to Way et al.  $(2017)$  $(2017)$  $(2017)$ .

Each model planet in this study is one Earth radius in size and has a topography and a continental/oceanic distribution similar to those of the Earth. For dynamic simplicity, we set the eccentricity and obliquity of our model planets to zero. The surface resolution is  $4^{\circ}$  by  $5^{\circ}$  in latitude and longitude, respectively. For the fully coupled dynamic ocean, we use oceanic layers of varying thickness, with an overall depth of 1129.3 meters. The atmosphere spans nearly one bar of pressure from 984 to 0.139 mb over 40 vertical layers of varying thickness.

The dominant atmospheric constituent in each model is  $N_2$ , where  $CO_2$  and  $CH_4$  are included at 400 and 1.00 parts per million, respectively.  $H_2O$  is given a modern-Earth profile at model start, which changes depending on the atmospheric circulation, evaporation, and precipitation in each simulation. It should be noted that all runs have oxygen-free atmospheres, and no ecosystem models are implemented, i.e., vegetation and other biological sources are not included in these simulations.

ROCKE-3D uses the Suite of Community Radiative Transfer (SOCRATES) radiation scheme to solve the two-stream approximated radiative transfer equation (Edwards & Slingo [1996](#page-7-0); Edwards [1996](#page-7-0)). In this study we use the present-day Solar spectrum to weight the short-wave component of the planetary flux, although SOCRATES does have the capability to use a variety of stellar spectra. Land albedo is set to 0.2 at model start, although this can be changed by snow accumulation and soil wetness on the surface.

<span id="page-2-0"></span>To study the effects of rotation rate on the surface temperature of an Earth-like world, we analyze the results of nine simulation runs with rotations slower than (and equal to) that of present-day Earth. These rotations are  $t_{\text{rot}} = 1, 2, 4, 8$ , 16, 32, 64, 128, and 256 times the sidereal day length of present-day Earth. In solar days, these correspond to 1, 2, 4.03, 8.16, 16.7, 35.0, 76.6, 191, and 848 times the solar day length of present-day Earth. Additionally, we consider the effects of increasing the insolation S0 by 10% and 20% for each rotation period, where  $SO = 1365.3 \text{ W m}^{-2}$ , the insolation of modernday Earth. Specific insolations will be referenced using the nomenclature  $00t_{\text{rot}}$ X1.nS0, where 1.n indicates the insolation multiplier for  $n = 0, 1,$  or 2. For example, the simulation with a rotation period of 32 days and an insolation of 1.2S0 will be referenced as 032X1.2S0.

The GCM data presented in this study have been averaged over ten model years post hydrological and radiative equilibrium, which are reached within an order of  $10<sup>2</sup>$ simulated years. For a more in depth description of the simulations in this study, see Way et al.  $(2018)$  $(2018)$  $(2018)$ .

#### 2.2. Fractional Habitability

Here we define the "fractional habitability"  $f_h(t_{\text{rot}})$  as the fractional surface area that maintains a mean temperature between 0 and 100 °C at 984 mb of atmospheric pressure, averaged over at least one orbital period and diurnal cycle for a specific orbital period  $t_{\text{rot}}$ ,

$$
f_h(t_{\rm rot}) = \frac{1}{A_{\rm tot}} \sum_{i=1}^{n_{\theta}} \sum_{j=1}^{n_{\phi}} H(\theta_i, \phi_j, t_{\rm rot}) A_{i,j}
$$
 (1)

for total surface area  $A_{\text{tot}}$ , specific latitude grid  $\theta_i$  and longitude grid  $\phi_i$ , number of latitude and longitude grids  $n_\theta$  and  $n_\phi$ , respectively, and the area of the i, jth grid cell  $A_{i,j}$ , where we have adopted the "habitability function"  $H(\theta, \phi, t_{\text{rot}})$  from Spiegel et al. ([2008](#page-7-0)), defined to be

$$
H(\theta, \phi, t_{\text{rot}}) = \begin{cases} 1 & \text{if } 0 \leq T(\theta, \phi, t_{\text{rot}}) \, [^{\circ}\text{C}] \leq 100 \\ 0 & \text{else} \end{cases} \tag{2}
$$

We suggest that this is a useful first-order probe of climate state (habitability, see Section [1](#page-0-0)) for our simulations, for which seasonal variation is minimal. In a more general case where seasonal variation does occur, we would be motivated to consider both the surface area that is always capable of supporting liquid water and the surface area that can support liquid water for part of a single orbit, i.e., the seasonal fractional habitability, as is done in Spiegel et al. ([2008](#page-7-0)). Because our simulations are of planets with zero obliquity and zero orbital eccentricity, season variations are not present.

Instead,  $f_h(t_{\text{rot}})$  captures key aspects of simulation-tosimulation variations in cloud cover and albedo across the surface, as well as variations in heat transport. In other words,  $f<sub>h</sub>(t<sub>rot</sub>)$  contains more information about the state of a climate than the globally averaged mean temperature, yet it is sufficiently simple to allow us to build a meaningful physical intuition for the conditions of systems that have many sensitivities and underlying parameter dependencies.

## 2.3. The Silicate Weathering Rate

The carbonate–silicate (C–S) cycle plays an important role in the stabilization of the climate of water-bearing terrestrial

worlds. An element of this cycle is the silicate weathering process (e.g., Kasting et al.  $1993$ ), in which  $CO<sub>2</sub>$  is drawn from the atmosphere as carbonic acid in precipitation. When this acid contacts silicate rock, the silicates are chemically dissolved (with reaction rates dependent on temperature and acid concentrations) and the products are carried into the oceans via runoff. Eventually the products of silicate weathering, such as calcite  $(CaCO<sub>3</sub>)$ , sink to the ocean floor and become subducted into the mantle, where carbonate metamorphism eventually transforms them back into  $CO<sub>2</sub>$ , which may reenter the atmosphere diffusely or via volcanic outgassing. This process is commonly associated with the regulation of Earth's climate close to a state where surface liquid water is abundant (Walker et al. [1981;](#page-7-0) Berner et al. [1983](#page-7-0)). For example, a decrease in solar forcing would result in a drop in surface temperature and precipitation, leading to a buildup of atmospheric  $CO<sub>2</sub>$  and, therefore, an increased greenhouse effect, effectively rewarming the surface. If surface temperatures and precipitation patterns are significantly altered by planetary rotation rate, it is critical to our understanding of long-term exoplanetary climate stability to contemplate how the silicate weathering rate is impacted by rotation.

We adapt the method of Walker et al. ([1981](#page-7-0)) to model the total silicate weathering rate W from the ROCKE-3D output, normalized by the total weathering rate  $W_0$  of the  $001X1.0S0$ model, i.e., the 1 solar insolation, 1 day rotation period model,

$$
W/W_0 = \frac{\sum_{i,j} R_{i,j} \exp\left(\frac{T_{i,j}}{17.7}\right)}{\sum_{i,j} R_{0,i,j} \exp\left(\frac{T_{0,i,j}}{17.7}\right)}
$$
(3)

where  $R_{i,j}$  is the runoff of precipitation over bare soil on the surface and over soil underground in the  $i$ , jth cell, weighted by the fraction of soil in that cell.  $T_{i,j}$  is the soil temperature in the i, jth cell (in Kelvin) averaged across layers of soil with a total depth of 3.5 m, and weighted by the thickness of each soil layer and the area of the grid cell. The subscript "0" indicates the values from the 001X1.0S0 model.

Our representation of the relative weathering rate deviates from Equation (1) of Walker et al. ([1981](#page-7-0)) in a number of important ways. First, we exclude the expression for the dependence on the partial pressure of  $CO_2$  (i.e.,  $(P/P_0)^{0.3}$ ) because the abundances of  $CO<sub>2</sub>$  are fixed across all models of varying rotations and insolations, and we assume the partial pressures of  $CO<sub>2</sub>$  remain constant over the relatively short timescales of the simulation runs. Thus,  $(P/P_0)^{0.3}$  is simply equal to unity for all cases explored in this study.

The temperature scaling factor of 17.7 in the exponent of Equation (3) is chosen according to the following rationale. Walker et al. ([1981](#page-7-0)) used experimental results of the temperature dependence of the silicate weathering rate (Lagache [1965,](#page-7-0) [1976](#page-7-0)) together with conservative results from climatological models to get a scaling factor of 13.7 as an estimate of the dependence of runoff on temperature (Wetherald & Manabe [1975](#page-7-0); Manabe & Stouffer [1980a](#page-7-0); Manabe & Wetherald [1980b](#page-7-0)). This is the value used in many silicate weathering studies (e.g., Sleep & Zahnle [2001](#page-7-0); Rushby et al. [2018](#page-7-0)); however, because ROCKE-3D gives runoff as a diagnostic, our study does not require an estimate of the dependence on temperature as a proxy for runoff, and we, therefore, retain the temperature scaling factor of 17.7

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Figure 2. Mean global surface temperature in degrees Celsius for each model as a function of rotation period (in sidereal days), with insolations (in solar insolations S0) represented by lines of different color.

determined solely by the experimental results of Lagache ([1965](#page-7-0), [1976](#page-7-0)).

## 3. Results

#### 3.1. Fractional Habitability

As shown by Way et al. ([2018](#page-7-0)), the ROCKE-3D runs provide evidence that the average global surface temperature tends to decrease with increasingly long days (i.e., longer rotation periods) for runs with 10% and 20% increases in insolation (Figure 2). This trend is clearest in the 1.2S0 runs because of the increased insolation initiating a global climate state that contains fewer regions capable of switching between ice-covered and ice-free for all rotations. The relationship between average global surface temperature and rotation period is less consistent for the solar insolation models, although the 064X1.0S0, 128X1.0S0, and 256X1.0S0 rotation models remain at lower average surface temperatures than the more rapidly rotating model planets.

Figure 3 shows the total northward transport of dry static energy and latent heat for a sample of rotation periods at 1.0 solar insolation. While the transport changes direction at lower altitudes as expected for the Hadley cell, the net energy transport is indeed poleward. This illustrates that heat is more efficiently transported toward the poles for slower rotating planets, causing the more uniform distribution of surface temperature across latitudes seen in Figure [4.](#page-4-0) Because of the high thermal inertia of the model ocean, which reaches depths of nearly 1300 m, the oceans stay above their freezing point despite the tendency for land masses to slip below  $0^{\circ}C$ , especially for model planets with the longest day lengths where land masses cool significantly on the nightside.

The fraction of the surface that lies in the temperature range  $0 \leq T \leq 100$  °C for each rotation period and insolation can be seen in Figure [5](#page-4-0), and specific values of  $f<sub>h</sub>$  for each rotation and insolation are shown in Table [1](#page-4-0). We find moderate increases in fractional habitability  $f_h$  across all rotations for 10% and 20% increases in insolation, which follows intuitively from the increase in mean global surface temperature with insolation (Figure 2).



Figure 3. Total northward transport of energy as a sum of the dry static energy transport and latent heat transport in the solar insolation case for a different rotation period in each subfigure. From top to bottom, these rotation periods are  $1\times$ ,  $16\times$ , and  $256\times$  the sidereal day length of present Earth.

For the 1.0S0 insolation case, there is an intriguing rise and decline in fractional habitability as a function of rotation, with a defined peak of  $f_h(16) = 0.92$  at the 16 days rotation period model. This is an additional 12% of temperate surface area compared to the average value of  $\langle f_h \rangle = 0.80$  for 1.0S0 insolation. This peak in fractional habitability at intermediate rotation periods is due to the interplay between two dynamical regime changes: one between a quasi-geostrophic state and a quasi-barotropic state, and another in which diurnal heating contrasts begin to dominate.

In the transition from a quasi-geostrophic state to a quasibarotropic state, the Hadley cell extends to higher latitudes (Figure 3) and the poleward temperature gradient decreases (see Figure 9 in Way et al. [2018](#page-7-0)). This poleward extension of the relatively warm equatorial air effectively increases the surface area of "habitable" temperatures. This particular transition occurs when the Rossby radius of deformation approaches the size of the planet (Del Genio et al. [1993](#page-7-0);

<span id="page-4-0"></span>

surface temperature  $[°C]$ 

Figure 4. Surface temperatures for the 1.0S0 case (i.e., solar insolation) as a function of rotation shown on a Robinson projection of the globe. Rotation periods from left to right are  $1\times$ ,  $2\times$ ,  $4\times$ ,  $8\times$ ,  $16\times$ ,  $32\times$ ,  $64\times$ ,  $128\times$ , and  $256\times$  the sidereal day length of present Earth. Approximate continental configuration can be seen outlined in black. All red-colored regions are above freezing.



Figure 5. Fraction of the total surface area where the surface temperature  $T$  [°C] lies in the range  $0 \le T \le 100$  as a function of rotation period (longer days to the right) and insolation S0.

Table 1 Fraction of the Model's Surface Area Where the Surface Temperature  $T$  [ $^{\circ}$ C] Falls Into the Range  $0 \le T \le 100$ , i.e., "Fractional Habitability"

Rotation period [days]	Insolation [S0]		
	1.0	1.1	1.2
1	0.76	0.97	0.98
2	0.78	0.97	0.98
$\overline{4}$	0.80	0.97	0.98
8	0.81	0.92	0.98
16	0.92	0.98	0.98
32	0.87	0.96	0.99
64	0.78	0.88	0.94
128	0.74	0.82	0.87
256	0.71	0.75	0.82

Note. For reference, the Earth had a net fractional habitability of 0.85 according to temperatures measured in 2004 (Spiegel et al. [2008](#page-7-0)), although we reiterate that our models adopt a 0° obliquity and an eccentricity of 0, which should therefore not be directly compared to Earth values.

Edson et al. [2011](#page-7-0); Showman et al. [2013](#page-7-0)). For an Earth-sized planet, this occurs at a rotation period between 8 and 16 days (Del Genio & Suozzo [1987](#page-7-0)).

The second dynamical transition occurs when the dominant circulation switches from an equator-to-pole motion to a dayto-night motion as the length of the solar day grows approximately equal to the radiative relaxation timescale of the planet,

which for our Earth-like model is on the order of 1–2 months (Way et al. [2018](#page-7-0)). Therefore, the length of the solar day becomes longer than our models' radiative relaxation time in the 32 and 64 days rotation period interval, at which point the diurnal temperature contrast begins to increase significantly. As the average nightside temperature decreases with increasing rotation periods, the total area in which water can remain in liquid form at the surface is effectively diminished.

The rotation period at which the peak in fractional habitability occurs is, therefore, a result of the overlap of these dynamical transitions in the rotation period domain. In the 16–32 days interval, both the equator and poles are sufficiently warm, while the nightside does not yet grow too frigid.

A common trend for every insolation is the steep abatement in fractional habitability for rotation periods greater than 16 and 32 days. In addition to the increase in diurnal temperature contrast, we speculate that this occurs after the efficiency of the poleward transport of heat from the equator has been maximized and an increase of cloud coverage at the substellar point works to reflect more incoming radiation as rotation period increases. Because we are unable to track the exact location of the substellar point in these particular simulation runs, our speculation cannot be addressed until we obtain averages from finer time sampling of the models in future studies.

## 3.2. Precipitation and Silicate Weathering Rate

Surface temperatures rise with insolation, and precipitation increases correspondingly. For a 10% increase in insolation, the total precipitation summed over the planetary surface increases by an average of  $(4 \pm 3) \times 10^{14}$  kg day<sup>-1</sup> across all rotation models, while for a 20% increase in insolation, the total precipitation similarly increases by  $(6 \pm 3) \times 10^{14}$  kg day<sup>-1</sup> compared to the 001X1.0S0 model. At these increased insolations, the relationship between rotation rate and precipitation is not as consistent as the relationship between rotation rate and surface temperature, despite their correlation. As can be seen in Figure [6](#page-5-0), the four slowest rotating models (032X, 064X, 128X, and 256X) have the lowest total precipitation; however, the 001X model experiences less total precipitation than the succeeding rotation models (002X and 004X) despite having a higher average global temperature.

Another distinction of the more rapidly rotating models is the latitudinal extent of precipitation over land masses. At one solar insolation, the 001X, 002X, and 004X models show a noticeably greater amount of precipitation at higher latitudes than the models with increasingly long days (Figure [7](#page-6-0)). For

<span id="page-5-0"></span>

Figure 6. Total precipitation in kilograms per day<sup>-1</sup> weighted by grid area as a function of rotation period and insolation. Solid lines indicate precipitation over bare soil (i.e., land), while dashed lines indicate precipitation over the entire surface. Models with different insolations are indicated by color.

rotation periods >8 days, the bulk of the precipitation over land mass is concentrated within 50° in latitude about the equator.

Increased precipitation over land will correlate with an increase in underground runoff (and surface runoff, depending on the topography of the location of precipitation). For a given temperature, an increase in runoff directly correlates to an increase in the rate of silicate weathering (Equation ([3](#page-2-0))). This is reflected in Figure [8](#page-6-0), where the silicate weathering rate for a 10% and 20% increase in insolation increases by up to 8.5 times the rate of weathering of the 001X1.0S0 model.

As can also be seen in Figure [8](#page-6-0), there is a distinct growth and decline around a well-defined peak in the relative weathering rates across all insolations, which reaches a maximum around a rotation period of 4 days. Despite having more precipitation over land (Figure 6), the models with rotation periods greater than 32 days experience decreased weathering rates relative to the 001X1.0S0 model. This is due to a decrease in soil temperature with increasingly long days.

Because neither the average soil temperatures nor total runoffs display the same relation to rotation period as does the relative weathering rate (Figures [9](#page-6-0) and [10](#page-6-0)), it is apparent that weathering rates cannot be solely attributed to either the global average soil temperature or the amount of precipitation/runoff, but rather to a spatial conjunction of the two. For models with very long days, a soil depth greater than the current depth of 3.5 m may be needed to sufficiently capture diurnal soil temperatures.

#### 4. Discussion

For Earth-like planets with rotation periods of 1, 2, 4, 8, 16, 32, 64, 128, and 256 days, we find for a 10% and 20% increase in insolation that average global surface temperatures decrease for planets with longer days (as shown in Way et al. [2018](#page-7-0)). This drop in mean global surface temperature may be due to an increase in albedo from an increase in cloud cover at the substellar point, as has been observed in Way et al. ([2018](#page-7-0)) and in previous GCM studies of slowly rotating planets (e.g., Yang et al. [2014](#page-7-0)). In the near future we will continue to run these ROCKE-3D simulations to obtain subday averages in order to

track cloud distribution and evolution with changing rotation periods.

For all insolations we find that surface temperatures become more uniform in latitude with increasing day lengths. This is due, in part, to a weakening Coriolis force with longer rotation periods, which enables the Hadley cells to grow in latitudinal extent, transporting heat more efficiently from the equator to the poles. This result is in qualitative agreement with previous studies that used GCMs to observe the effect of rotation rate on terrestrial planet atmospheres (e.g., Williams & Holloway [1982](#page-7-0); Del Genio & Suozzo [1987;](#page-7-0) Showman et al. [2013;](#page-7-0) Kaspi & Showman [2015](#page-7-0) and references therein). Additionally, Way et al. ([2018](#page-7-0)) show by comparing ROCKE-3D simulations with a dynamic ocean (as used in this study) to ROCKE-3D simulations with a static ocean that the dynamic ocean significantly aids poleward heat transport and is responsible for a diminished ocean-ice fraction compared to the static ocean model.

Our results suggest that there may be a "rotational Goldilocks zone" in which the fractional habitability reaches a maximum at a critical rotation period (Section [2.2](#page-2-0), Figure [5](#page-4-0)). We speculate that this critical rotation period occurs at the transition between two rotational regimes: one in which the efficiency of poleward heat transport increases with slower rotations, effectively increasing the surface temperatures in the upper latitudes, and the other regime that encompasses even slower rotations, where the Hadley cell has extended to the poles and the nightside significantly cools with increasingly long nights, while cloud coverage (and therefore albedo) continues to grow about the substellar point, effectively decreasing the mean global surface temperature.

Our simulation results for the solar insolation case show a peak in fractional habitability at a rotation period of 16 days (Figure [5](#page-4-0)). Although there is no similar peak in the models with higher insolations, they do show a similar monotonic drop in fractional habitability with rotation periods beyond ∼16–32 days. If these results are supported with additional models with finer rotation and insolation sampling, this could suggest a potential "Goldilocks" zone for planetary rotation rate in addition to orbital range. Given the expectation that rotation rate evolves because of tides, this also suggests the possibility of peak fractional habitability at a predictable system age.

Across all insolations we also find that there is a peak in the rate of silicate weathering relative to the 001X1.0S0 model centered around a 4 day rotation period (Figure [8](#page-6-0)). While the simulations used here maintain a fixed atmospheric  $CO<sub>2</sub>$ abundance, we can nonetheless draw some conclusions about the potential evolution of weathering and climate states. The C–S cycle on the modern Earth operates with a weathering or sequestration rate of  $\sim$  7  $\times$  10<sup>12</sup> mols C yr<sup>-1</sup> (moles of carbon per year, e.g., Brantley & Koepenick [1995](#page-7-0); Rushby et al. [2018](#page-7-0)) and an estimated current mantle outgassing rate of  $\sim$ 3  $\times$  10<sup>12</sup> mols C yr<sup>-1</sup> (e.g., Zhang & Zindler [1993;](#page-7-0) Sleep & Zahnle [2001](#page-7-0)). Overall, together with other cycling pathways such as tectonic erosion and arc volcanism, it is estimated that the in-balance carbon fluxes in the Earth system operate at a level around  $10^{12} - 10^{13}$  mols yr<sup>-1</sup>. Given a present-day estimated atmospheric carbon content of  $\sim 1.8 \times 10^{14}$  mols, this implies that ∼1%–10% of the Earth's atmospheric carbon is undergoing cycling per year as part of the C–S balancing feedback loop. Therefore, there is considerable sensitivity on

<span id="page-6-0"></span>

Figure 7. Kilograms per day of precipitation over land averaged across longitudes as a function of rotation and insolation S0. Rotation periods are in present Earth sidereal days. Gray regions mark latitudes which have no land masses.



Figure 8. Total silicate weathering rate as a function of rotation and insolation relative to the weathering rate of the 1 day rotation 1.0 solar insolation case. The horizontal dashed line shows where the total weathering ratio between models is equal to 1.



Figure 9. Average global soil temperature in Celsius weighted by soil thickness as a function of rotation period in days and insolation S0.



**Figure 10.** Total runoff in kg day<sup>-1</sup> as a function of rotation period and insolation S0.

short timescales to any forcings that affect elements of the cycle.

Our results (Figure 8) suggest that weathering rates can peak by factors of ∼8 (for higher insolations) because of precipitation and temperature changes from rotational evolution. We stress that we do not track the full evolution of a single planet, i.e., we do not incorporate a C–S cycle in our models, but rather hold atmospheric  $CO<sub>2</sub>$  constant, and we do not evolve rotations within a model run. In a real system we might, for example, expect a coevolution of rotation-altered weathering with atmospheric  $CO<sub>2</sub>$  that leads to a progressive lowering of  $CO<sub>2</sub>$ and global temperatures that nonetheless remains in equilibrium at any given time because of the feedback cycle. However, this depends critically on the rate of rotational evolution. The overall climate state should adjust to day length changes on comparatively rapid timescales (e.g., centuries), whereas the C–S cycle is completed over  $\sim 10^8$  yr timescales (Sleep & Zahnle [2001](#page-7-0)).

There is a wide range of expected rotational evolution timescales for worlds in the nominal habitable zone of different stellar masses, ranging from very rapid tidal evolution toward synchronous or pseudo-synchronous rotation (e.g.,  $\langle 10^{7} \rangle$  yr for low-mass stars Goldreich & Soter [1966](#page-7-0); Kasting et al. [1993](#page-7-0)) to

<span id="page-7-0"></span>timescales commensurate with a system's present age (e.g.,  $10^9$  yr as for a moonless Earth (Barnes 2017)). For terrestrial-analog planets at the inner edge of the liquid water orbital range, with higher than solar insolation, it is therefore possible that weathering can evolve to draw down atmospheric  $CO<sub>2</sub>$  at rates far in excess of C–S equilibrium fluxes.

This could lead to climate plunging into a snowball state (Deitrick et al. 2018) at intermediate rotation rates to those of the modern Earth and synchronous or psuedosynchronous rotators. In extreme cases, a planet could remain snowballed until reaching its final slow rotation state. At this point, whether or not it will "recover" to a more temperate state will hinge on the geophysical gas flux and the still poorly understood properties of climate on very slowly rotating worlds (Kite et al. 2011).

In light of our results, it is intriguing to speculate on the role of rotation in the faint young Sun paradox (Sagan & Mullen 1972), given the expectation for shorter day lengths on the early Earth. An exploration of this speculation, however, would require a new suite of simulations for the early Earth, with the appropriate solar insolation, range of atmospheric abundances, and shorter rotation periods.

It is important to note that the exact relationship between the weathering rate and rotation is specific to a planet's land mass distribution. As we have shown, an Earth-like planet with a continental distribution similar to that of the Earth will experience an increased weathering rate for rotation periods <16 days as the Hadley cell and, therefore, location of rainfall expands to higher Northern latitudes where there is more land mass to be weathered. However, for a planet with a different continental distribution, the rotation period that maximizes the silicate weathering rate could very well be shifted. Nonetheless, our results support the suggestion of Rushby et al. (2018) to consider the relationships between the C–S cycle and fundamental planetary properties and the subsequent impact on long-term habitability.

# 5. Conclusion

In this study, we have used the GISS' ROCKE-3D general circulation model to examine how increases in insolation and planetary rotation period may affect a planet's "fractional habitability" and silicate weathering rate. In light of our results, we argue that the rotation period and length of a planet's day is an important factor to consider in the determination of the habitability of exoplanets.

We believe that our present GCM study is the first to investigate the role of planetary rotation period on the silicate weathering rate. We have shown that the irradiation and length of an Earth-like planet's day has a significant effect on its drawdown rate of atmospheric  $CO<sub>2</sub>$ .

For both fractional habitability and silicate weathering, we find evidence for peak-like behavior as a function of planetary day length. In terms of fractional habitability, we suggest that there may be a "Goldilocks" zone for planetary rotation rate in addition to orbital location. We also propose that a young terrestrial-type planet experiencing fast rotational evolution due to star–planet tides may pass through an epoch of significantly enhanced  $CO<sub>2</sub>$  draw down, potentially destabilizing its climate.

While it is extremely challenging to obtain observational constraints on rocky-exoplanet rotation rates, methods such as phase-curve photometry (e.g., Ford et al. 2001) might eventually yield results. We also suggest that a distinct climate state (such as low-temperature snowball states for water-rich worlds), combined with estimates of system age and tidal evolution, could itself conceivably provide clues to planetary spin.

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