



University of Groningen

Infrared Light Curves of Near-Earth Objects

Hora, Joseph L.; Siraj, Amir; Mommert, Michael; McNeill, Andrew; Trilling, David E.; Gustafsson, Annika; Smith, Howard A.; Fazio, Giovanni G.; Chesley, Steven; Emery, Joshua P.

Published in: The Astrophysical Journal Supplement Series

DOI: 10.3847/1538-4365/aadcf5

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version Publisher's PDF, also known as Version of record

Publication date: 2018

Link to publication in University of Groningen/UMCG research database

Citation for published version (APA): Hora, J. L., Siraj, A., Mommert, M., McNeill, A., Trilling, D. E., Gustafsson, A., ... Mueller, M. (2018). Infrared Light Curves of Near-Earth Objects. The Astrophysical Journal Supplement Series, 238(2), [22]. https://doi.org/10.3847/1538-4365/aadcf5

Copyright

Other than for strictly personal use, it is not permitted to download or to forward/distribute the text or part of it without the consent of the author(s) and/or copyright holder(s), unless the work is under an open content license (like Creative Commons).

Take-down policy

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.

Downloaded from the University of Groningen/UMCG research database (Pure): http://www.rug.nl/research/portal. For technical reasons the number of authors shown on this cover page is limited to 10 maximum.



Infrared Light Curves of Near-Earth Objects

Joseph L. Hora¹, Amir Siraj², Michael Mommert^{3,4}, Andrew McNeill⁴, David E. Trilling⁴, Annika Gustafsson⁴, Howard A. Smith¹, Giovanni G. Fazio¹, Steven Chesley⁵, Joshua P. Emery⁶, Alan Harris⁷, and Michael Mueller^{8,9}

Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, MS-65, Cambridge, MA 02138, USA; jhora@cfa.harvard.edu

Harvard University, Cambridge, MA 02138, USA

³ Lowell Observatory, 1400 W Mars Hill Road, Flagstaff, AZ 86001, USA

⁴ Department of Physics and Astronomy, P.O. Box 6010, Northern Arizona University, Flagstaff, AZ 86011, USA

⁵ Jet Propulsion Laboratory, California Institute of Technology, 4800 Oak Grove Drive, Pasadena, CA 91109, USA

⁶ Department of Earth & Planetary Science, University of Tennessee, 306 EPS Building, 1412 Circle Drive, Knoxville, TN 37996, USA

German Aerospace Center (DLR), Institute of Planetary Research, Rutherfordstrasse 2, D-12489, Berlin, Germany

⁸ Kapteyn Astronomical Institute, Rijksuniversiteit Groningen, P.O. Box 800, 9700AV Groningen, The Netherlands

SRON, Netherlands Institute for Space Research, P.O. Box 800, 9700AV Groningen, The Netherlands

Received 2018 May 4; revised 2018 August 20; accepted 2018 August 22; published 2018 October 4

Abstract

We present light curves and derive periods and amplitudes for a subset of 38 near-Earth objects (NEOs) observed at 4.5 μ m with the IRAC camera on the the *Spitzer Space Telescope*, many of them having no previously reported rotation periods. This subset was chosen from about 1800 IRAC NEO observations as having obvious periodicity and significant amplitude. For objects where the period observed did not sample the full rotational period, we derived lower limits to these parameters based on sinusoidal fits. Light curve durations ranged from 42 to 544 minutes, with derived periods from 16 to 270 minutes. We discuss the effects of light curve variations on the thermal modeling used to derive diameters and albedos from *Spitzer* photometry. We find that both diameters and albedos derived from the light curve maxima and minima agree with our previously published results, even for extreme objects, showing the conservative nature of the thermal model uncertainties. We also evaluate the NEO rotation rates, sizes, and their cohesive strengths.

Key words: infrared: planetary systems - minor planets, asteroids: general - surveys

Supporting material: extended figure

1. Introduction

Near-Earth Objects (NEOs) are small solar system bodies whose orbits bring them close to the Earth's orbit. NEOs are compositional and dynamical tracers from elsewhere in the solar system. The study of NEOs allows us to probe environmental conditions throughout the solar system and the history of our planetary system, and provides a template for analyzing the evolution of planetary disks around other stars. NEOs are the parent bodies of meteorites, one of our key sources of detailed knowledge about the development of the solar system, thus so studies of NEOs are essential for understanding the origins and evolution of our solar system and other stellar systems.

As of 2018 June there are over 18,000 known NEOs. Roughly 2000 new NEOs are being discovered each year, primarily by the Catalina Sky Survey (Leonard et al. 2017) and Pan-STARRS (Vereš et al. 2015), and the rate will significantly increase when LSST begins operations (Vereš & Chesley 2017). However, little is known about most NEOs after their discovery, beyond their orbits and optical magnitudes. The sizes of objects that pass close to Earth can be measured with radar, using, for example, the Arecibo or Goldstone facilities. Over 750 NEOs have been observed, ¹⁰ at a rate of \sim 75–100 objects per year over the past three years. This rate cannot be easily scaled up, however, and is not keeping pace with the rate of new NEO discoveries. Optical or near-IR spectra of NEOs can determine the surface properties and allow their taxonomic classification (Bus 1999; Bus & Binzel 2002a, 2002b; DeMeo et al. 2009). However, currently less than 2% of the NEOs in the JPL Small-Body Database¹¹ have assigned taxonomic types. Small NEOs are especially difficult to characterize: for example, Perna et al. (2018) recently conducted a 30-night GTO program at the NTT and obtained the spectra of 147 NEOs, focusing on smaller (<300 m) objects. With 24 usable nights, they were able to observe ~ 6 objects per night on this moderately sized telescope. It would take a major effort using large telescopes to increase the fraction of spectrally classified objects.

The IRAC instrument (Fazio et al. 2004) on the Spitzer Space Telescope (Werner et al. 2004) is a powerful NEO characterization system. NEOs typically have daytime temperatures ~ 250 K, hence their thermal emission at 4.5 μ m is almost always significantly larger than their reflected light at that wavelength. We can therefore use a thermal model using the optical and IR fluxes to derive NEO properties, including diameters and albedos (see Trilling et al. 2010, 2016). Measuring the size distribution, albedos, and compositions for a large fraction of all known NEOs will allow us to understand the scientific, exploration, and civil-defense-related properties of the NEO population.

After an initial pilot study to verify our observing techniques and analysis methods with the Spitzer data (Trilling et al. 2008), our team has conducted three major surveys of NEOs with Spitzer/IRAC in the Warm/Beyond Mission phases: the ExploreNEOs program (Trilling et al. 2010), the NEOSurvey (Trilling et al. 2016), and the NEOLegacy Survey (Trilling et al. 2017). As of 2018 March, Spitzer has completed

¹⁰ https://echo.jpl.nasa.gov/asteroids/index.html

¹¹ https://ssd.jpl.nasa.gov/sbdb_query.cgi

a total of over 1800 NEO observations, with an expected total of over 2100 observations by the time that the NEOLegacy program has completed in early 2019. Our initial NEO survey results are summarized in Trilling et al. (2010, 2016) and Harris et al. (2011). Since then we have examined the albedo distribution and related them to taxonomic classifications (Thomas et al. 2011), performed a physical characterization of NEOs in our sample (Thomas et al. 2014), and examined the physical properties of subsets of the sample, including low- $\Delta \nu \text{NEOs}$ (Mueller et al. 2011) and dormant short-period comets(Mommert et al. 2015). We examined individual objects more closely, such as in our discovery of cometary activity associated with the NEO Don Quixote (Mommert et al. 2014c). We have also performed additional observations on specific NEOs of interest, including the small (<10 m) NEOs 2009 BD (Mommert et al. 2014b) and 2011 MD (Mommert et al. 2014a), and the Hayabusa-2 mission target 162173 Ryugu (Müller et al. 2017). One part of our Spitzer observations of 162173 Ryugu consisted of repeated integrations during its full period to obtain an IR light curve to help to constrain the object's shape and size. This led us to conclude that we could perhaps extract similar light curves for objects in the survey programs, which were designed only to obtain a single flux measurement from the mosaic image averaging over all of the exposures in the observation. We found that our predicted NEO fluxes were fairly conservative in many cases, and that we could detect most of the NEOs in the individual IRAC exposures.

The Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010) has similarly used infrared observations to characterize a large sample of main-belt asteroids and NEOs. This Explorer-class mission obtained images in four broad infrared bands at 3.4, 4.6, 12, and 22 μ m. WISE conducted its four-band survey of the sky starting in 2010 January, and after the cryogen was depleted later that year, it continued to operate with its 3.4 and 4.6 μ m bands until 2011 February. The spacecraft was reactivated in 2013 December as NEOWISE (Mainzer et al. 2014) and has since been conducting a sky survey in the 3.4 and 4.6 μ m bands to focus on NEO discovery and characterization, using a thermal modeling technique similar to what we have employed with Spitzer as described above. Over its lifetime, NEOWISE has observed over 860 NEOs¹² and published their estimated diameters and albedos (e.g., Masiero et al. 2017). The WISE data can also be used to derive the light curves of asteroids (e.g., Sonnett et al. 2015). However, the cadence is quite different; the WISE survey typically provides repeated observations separated by 3 hr over a 1.5 day period, making it useful for sampling periodicities on the order of 1–2 days. The Spitzer data sample cadences from a few minutes to hours, making them ideal for small and fastrotating NEOs, and complementary to the data that WISE provides. Also, since Spitzer has a larger primary mirror, and it can direct the observatory to follow the apparent motion of the NEO, we can integrate for longer periods on each NEO, therefore providing more sensitivity and allowing us to detect objects at the level of a few μ Jy.

In this paper we present the results from an analysis of a sample of the available *Spitzer* light curve data. Section 2 describes the observations and the reduction techniques. Section 3 describes the analysis techniques used to derive the periods and amplitudes of the light curves and presents those

results. Section 3.3 discusses the effects of rotation-induced brightness variability on the thermal modeling results.

2. Observations and Data Reduction

2.1. The Spitzer NEOSurvey Programs

Observations were obtained with *Spitzer*/IRAC in the ExploreNEOs program (*Spitzer* Program IDs 60012, 61010, 61011, 61012, 61013), the NEOSurvey (Program ID 11002), and the NEOLegacy Survey (Program ID 13006). The observations were conducted in a similar manner for these three large survey programs, taking frames while tracking the NEO motion and dithering during the observations to eliminate instrument systematics such as bad pixels or array location-dependent scattered light effects. In ExploreNEOs, we used the "Moving Cluster" target mode with custom offsets to perform the dithers, alternating between the 3.6 and 4.5 μ m fields of view. For the other programs, we used the "Moving Single" target mode and used a large cycling dither pattern with the source in the 4.5 μ m field of view only.

In order to provide the required scheduling flexibility of the observations, we specified an observing window during which a fixed set of integrations would provide adequate signal-tonoise for the object in the total integration time. This was typically chosen to be near the time when the NEO would have its peak flux as seen by Spitzer, in order to minimize the time necessary to detect the source. The frame time was set to keep the NEO below saturation levels on the IRAC detectors based on the maximum expected NEO flux, and ranged from 12 to 100 s. When the uncertainty in the NEO flux was such that we could possibly be close to saturation in the long frames, we used the High Dynamic Range option, which adds little additional overhead but protects against an unexpectedly bright NEO saturating the detectors. We also required a minimum apparent motion of the source relative to the background during the observation, to make it possible to separate the NEO from background objects and isolate the NEO flux. For ones with slow apparent motions from Spitzer, we increased the number of frames, or added a second epoch of observations to ensure adequate motion to enable successful background subtraction and photometry of the object.

The total exposure time was chosen such that the source would be detected at a 10σ level in the final mosaic after combining all observations. To assess and schedule each potential target, we predicted the reflected+emitted flux density at 4.5 μ m as a function of time. Our flux predictions are based on the solar system absolute optical magnitude H, as reported by *Horizons*.¹³ *H* magnitudes for NEOs are of notoriously low quality and tend to be skewed bright (Ivezić et al. 2002; Romanishin & Tegler 2005; Vereš et al. 2015). We assume an H offset (ΔH) of [+0.6, +0.3, 0.0] mag for (faint, nominal, bright) fluxes, respectively, so that the observations will achieve or exceed the required signal-to-noise ratio. We predicted thermal fluxes using the Near-Earth Asteroid Thermal Model(NEATM, Harris 1998, see Section 3.3). We assume albedos (p_V) of [0.4, 0.2, 0.05] for (low, nominal, high) thermal fluxes. The nominal η value (the infrared beaming parameter) was determined from the solar phase angle using the linear relation given by Wolters et al. (2008), which is generally in agreement with the newer results of Mainzer et al. (2011b) and

¹² https://neowise.ipac.caltech.edu/

¹³ Giorgini et al. (1996); https://ssd.jpl.nasa.gov/?horizons.

Trilling et al. (2016); 0.3 was (added, subtracted) for (low, high) fluxes to capture the scatter in the empirical relationship derived in Wolters et al. (2008). The resulting NEATM fluxes were convolved with the IRAC passbands (Hora et al. 2008) to yield "color-corrected" in-band fluxes. Optical fluxes were calculated from $H + \Delta H$ together with the observing geometry and the solar flux at IRAC wavelengths. Asteroids were assumed to be 1.6 times more reflective at IRAC wavelengths than in the V band (Trilling et al. 2008; Harris et al. 2011; Mainzer et al. 2011b); color-corrections for the 5800 K reflected component are negligible. After removing all dates where an NEO's bright predicted flux could saturate the detector, we identified a 5 day window centered on the peak brightness during the observing cycle and used it as the timing constraint for the AOR. Our experiences with these programs have shown that a window of this size allows good scheduling flexibility while enabling us to use the shortest possible integration times.

There are some slight differences between the observing modes in the survey programs. In the ExploreNEOs program, we obtained near-simultaneous data for 575 sources in the 3.6 and 4.5 μ m channels by alternating between the two bands during the observation period. However, we found that the 3.6 μ m data were not a significant constraint in the NEATM fitting process, since the flux in that band is an unknown mix of reflected light and thermal emission. In addition, most NEOs are significantly fainter at 3.6 μ m than at 4.5 μ m, and therefore the sensitivity in that band was driving the total integration time requirements. We therefore observed only in the 4.5 μ m band in the NEOSurvey and NEOLegacy programs, reducing the required integration time for each NEO and allowing us to observe many more sources in the time awarded. Another change that was done in the NEOLegacy program was to set our minimum total observation time to \sim 30 minutes, in order to ensure we have sufficient frames for background subtraction and elimination of systematic effects. The maximum time for objects in the survey was chosen to be \sim 3 hr, to keep our total time request within the range allowed by the Spitzer program and maximize the number of objects we could characterize. Our group maintains a webpage¹⁴ where we provide the IRAC photometry and the results of the NEATM fitting for each object shortly after it is observed.

2.2. Light Curve Extraction

Extracting light curves from the *Spitzer* NEOSurvey was performed in several steps. Mosaics of the *Spitzer* data for each object were constructed using the IRACproc software (Schuster et al. 2006) which is based on the mopex mosaicking software (Makovoz et al. 2006) distributed by the *Spitzer* Science Center (SSC).¹⁵ We downloaded the Basic Calibrated Data (BCD) frames for each observation from the *Spitzer* Heritage Archive,¹⁶ which has data from the latest pipeline version for all IRAC observations. For each object, a mosaic was made of the background field by masking the NEO from each BCD and making a mosaic in the non-moving frame. Since the observations were obtained by tracking at the nonsidereal NEO rate, the background objects are more or less trailed in the image, depending on the NEO's apparent rate of

motion and the frame time being used. The mosaicking process removes any array artifacts and cosmic ray and other transient effects and creates a clean image of the field that the NEO was moving through. This background mosaic was then subtracted from each individual BCD image. This process removes most of the flux from the field objects, but the cosmic rays, hot or dead pixels, and other array artifacts remain in the BCD image. Also, the subtraction is incomplete near the core of bright stars and often artifacts are present in those locations. However, usually the fields are not very crowded with bright stars and the NEO falls on regions free from these effects for most of the observation. Aperture photometry on each BCD is then performed with the phot task in IRAF. An aperture radius of 6 pixels (7".32) was used, with a sky background annulus of 6 pixels separated from the aperture by 6 pixels. The zero-point magnitude for the photometry was determined from IRAC observations of calibration stars that we downloaded, reduced, and extracted in the same way (except without the background field subtraction). We also construct a mosaic from the BCDs in the moving reference frame of the NEO and perform photometry on that image, and we get excellent agreement between the fluxes derived from the BCD and the mosaic photometry. For some BCDs, the photometry process fails to generate valid results. For example, if the source happened to fall on a group of dead pixels, or there was a cosmic-ray event that affected the region near the NEO, the phot task would fail to produce photometry, or give invalid results. If the source is faint and close to the sensitivity limit of the IRAC frames, there can be photometry dropouts when the source becomes too faint to photometer during certain parts of the light curve. However, in most cases, 95%–100% of the BCDs yield valid photometry in this step.

After collecting the BCD photometry, two additional steps are performed to clean the light curve data. First, a check of the source positions is made in the extracted data. During these relatively short observations, the path of the NEO on the plane of the sky can be approximated by a linear, or in some cases a quadratic, function. The position of the source as a function of time is fit with a linear function in both R.A. and decl., and the deviation from the fit is calculated for each data point. For a few cases where a long light curve was obtained, this was switched to a quadratic function when it was apparent the linear fit was not sufficient. We then compare each point to the position predicted by the fitted function, and reject those data points with deviations greater than about 1 pixel (1.2). This approach rejects points that were affected by cosmic rays or other array artifacts that caused the source position and photometry to be affected.

The second step is to determine the noise level in the light curve and exclude photometry that exceeds a cutoff value, in order to reject photometry affected by cosmic rays or other effects like incomplete background subtraction. Since the source is likely variable, we must separate out the measurement noise from the source variation. The noise depends not only on the instrumental parameters such as integration time but also on the details of the background field and subtraction process. We therefore estimate the noise in the photometry by calculating for each data point the standard deviation, including the two points immediately preceding and following it (5 points in total). This is determined for points 3 through N-2 in the light curve, and the median of these values is taken to be the estimate of the measurement noise. We also determine the median value

¹⁴ http://nearearthobjects.nau.edu/spitzerneos.html

¹⁵ http://ssc.spitzer.caltech.edu/

¹⁶ http://sha.ipac.caltech.edu/applications/Spitzer/SHA/

of the nearest five light curve points, and calculate the difference between the data point and this local median value. If it differs by more than $3\times$ the noise estimate, then it is rejected from the light curve. This process is fairly robust and works well in most cases, but it assumes that the source is slowly changing during the course of five frames. Also, in some cases there are larger gaps in the light curve that can cause issues with this method. In these cases, we adjusted the noise estimate value slightly to allow more points to be declared valid. In most cases, >90% of the light curve points pass all of these checks and appear in the light curve. Plots of our sample of light curves showing periodicity are shown in Figures 1–3.

3. Results and Discussion

3.1. Period and Amplitude Derivation

We visually analyzed the set of light curves we reduced to search for apparent periodicities. We identified 38 NEOs that had obvious periodicity with a significant amplitude, and where the *Spitzer* data apparently covered a large fraction of the rotational period, or the light curve appeared close to sinusoidal but the observation time did not fully cover one period. These are shown in Figures 1–3, and analyzed in the sections below.

3.1.1. Lomb-Scargle (LS) Periodograms

We analyzed the NEOs with light curves that appeared to sample more than half of a rotational period using the Lomb-Scargle (LS) algorithm (Lomb 1976; Scargle 1982), as implemented by the NASA Exoplanet Science Institute Periodogram service.¹⁷ The rotational period of the NEO was then assumed to be double the period value of the highest peak of the periodogram for the 4.5 μ m flux density data of each light curve that is reported in Table 1.

We estimated the 1σ uncertainty for the rotational period reported by generating simulated data for each light curve and running the LS analysis to derive periods for them. The simulated data were constructed as follows: for each measured light curve, a smoothed curve was calculated using a running average of five data points. Then, noise was added to the smoothed curve using a normal distribution with the same standard deviation estimated for the measurement. We then performed the same LS analysis for these simulated light curves and derived periods. We calculated the standard deviation of the period estimates for the simulated data, which we report as the error estimate of the period in Table 1. The 1σ uncertainty value is contingent on the assumption that the highest peak in the LS analysis indeed represents the true period. A low value for the 1σ uncertainty signals high confidence in the precision of the period reported for the highest peak, but if the LS peak does not represent the true period, then the error would be much higher.

For each of these objects, the 4.5 μ m flux density data were processed through a simple moving mean algorithm with a sample width of 6 observations. We then used the maximum and minimum values of the processed flux density data to calculate the amplitude, in magnitudes, for each object's rotation. We used the associated photometric uncertainties to calculate the 1 σ uncertainty for each amplitude. These values are reported in Table 1.

To obtain a lower limit on the rotation period for the NEOs with light curves that indicated a long sinusoidal rotation period relative to the observation window, as well as to corroborate the period estimates for six of the NEOs analyzed with the periodogram that exhibited sinusoidal variation, we fit a sinusoidal function to the 4.5 μ m flux density data for each object using a nonlinear least-squares method, with all data points equally weighted. The periods reported in the table are the extrapolated rotational periods of the NEO, assuming that the full rotational light curve is a bimodal sine function with the fitted period. The uncertainties were estimated by simulating data sets with the sine function determined from the observations of each object, sampled at the same time intervals as the observation but with simulated flux data with random errors having the same σ as the observation. The estimated error was then taken to be the standard deviation of each parameter from the fits to the simulated data. Periods and amplitudes, and their respective 1σ uncertainties, are reported in Table 3. The fitted sine curves are plotted with the data in Figure 3.

3.2. Discussion of the Period-fitting Results

The NEOs listed in Table 1 (1990 MF, 1990 UA, 1998 FF14, 1999 JE1, 2003 EO16, 2005 HC3, 2009 WD106, 2011 XA3, and 2005 XC) were found to have fully sampled periods, assuming a bimodal light curve. While there is a high likelihood that the period estimates resulting from these well-sampled light curves are accurate, they should still be treated as lower bounds due to the possibility of multimodal distributions, combined with photometric uncertainties that can make two independent light curve peaks indistinguishable from one another.

The NEOs 2002 PM6 and 2011 WS2 had, at most, 25%–30% of their rotational period sampled. 2000 SH8, 2002 CA10, 2004 JR, 2005 XY, 2008 SD85, 2009 CS1, 1999 VT25, 2005HN3, and 2011 SM68 had, at most, 35%–50% of their rotational period sampled. Their periods were estimated by fitting a sine function to the data as described in Section 3.1.2, assuming they have symmetrical bimodal rotation curves. However, these period estimates should be treated strictly as lower bounds, as it is very possible that these objects have multimodal light curves that were not well-sampled.

Six of the NEOs with sinusoidal fits had light curves indicating total sampling near or greater than half a rotational period (2000 OM, 2003 XE, 2008 GV3, 2008 JM20, 2011GM44, and 2013 CW32). These objects had, at most, a median of 0.6 sampled rotation periods. Thus, we analyzed these objects with the periodogram method in addition to the sinusoidal fitting one. The periodogram-based period estimates are all within 3σ of the sinusoidal fit estimates, indicating consistency between the two methods.

Four of the NEOs in our sample have previously measured rotational periods: 2005 LG8, 2008 UE7, 2011 XA3, and 2015 XC. We compare our measurements to the previous results for each object in Section 3.4.

We converted the rotational periods and estimates in Tables 1-3 to spin frequencies and in Figure 4 we plot the frequency versus diameter of the new measurements compared to the NEOs listed in the light curve database (LCDB; Warner et al. 2009, updated 2018 March 7). The red points are for our

^{3.1.2.} Sine Fits

¹⁷ https://exoplanetarchive.ipac.caltech.edu/cgi-bin/Pgram/nph-pgram



Figure 1. Light curves and phase plots from the reduced and cleaned *Spitzer* light curves for the objects where the light curve duration is longer than the derived rotational period. On the left are the light curves for the duration of the observation. The horizontal axis gives the time in minutes relative to the first point in the light curve. The plots on the right show the folded light curves, assuming the periods listed in Table 1. The derived period (in minutes) is shown below the object name. (An extended version of this figure is available.)



Figure 2. Spitzer light curves that cover less than one rotation period. The horizontal axis gives the time in minutes relative to the first point in the light curve. The extrapolated lower limits to the rotation periods are given in Table 2.

measurements from Table 1, where the observations covered more than one rotational period, and the blue points are for the NEOs in Tables 2 and 3, where we have derived lower limits. For the objects that had previous observations, we used those published rotational periods in this figure instead of the lower limits we derived. The *Spitzer* measurements are within the same range as previous NEO spin frequencies and diameters. One point that is slightly discrepant is that of 1990 MF, which lies at D = 0.519 km, Freq = 26.5 rev/day, above the "spin barrier" at ~10 rev/day in this range of diameters. As seen in Figure 1, the amplitude of the *Spitzer* light curve for this object is low compared to the noise, and possibly the full light curve was not sampled and the period is longer than that derived, which would move the point down in the diagram.

3.3. Impact of Light Curve Variations on the Thermal Modeling

We investigated the impact of the detected light curve variations during our *Spitzer* observations on thermal modeling results. The default NEOSurvey thermal model (Trilling et al. 2016) uses an adaptation of the Near-Earth Asteroid Thermal



Figure 3. Plots of *Spitzer* light curves where less than one rotational period was observed, fit with sine functions. The blue line is the sine fit to the data, with the parameters given in Table 3.



Model (NEATM, Harris 1998) to derive diameter and geometric albedo estimates of the target in combination with a Monte Carlo model to derive realistic uncertainties on these parameters. The model uses *Spitzer*-measured thermal flux densities and combines them with optical data in the form of the target's absolute magnitude to model the surface temperature distribution on a spherical model asteroid. Target diameter and geometric albedo are found in a least-squares fit of the modeled spectral energy distribution to the observed one. The NEATM uses a variable "beaming parameter" η , which accounts for surface roughness, thermal inertia, and other effects in a zeroth order approximation. Being reliant on single-band *Spitzer* IRAC 4.5 μ m data, η is drawn from a measured distribution of such values (see Trilling et al. 2016, for details).

In this analysis, we re-derived diameters and albedos for the targets listed in Table 1 using a hypothetical nominal IRAC 4.5 μ m flux density for the target equal to the maximum and the minimum of the measured light curves. This simulates a hypothetical case in which we observed the target exactly during the light curve maximum or minimum, and allows us to investigate the impact on the thermal modeling results. We restricted ourselves to the targets listed in Table 1, which cover a wide range of light curve amplitudes. We compared the

thermal modeling diameters and geometric albedos with the previously derived uncertainty ranges of both parameters.¹⁸

Our analysis shows that both diameters and albedos derived from the light curve maximum and minimum agree with the previously derived and published see footnote 18 results at the 1σ -level in most cases, but on the 3σ -level in all cases. Even for objects like 2015 XC and 2001 DF47, which have large thermal flux density light curves, the simulated cases are well within the reported uncertainties. This proves the conservative nature of the thermal model uncertainties provided by the model described in Trilling et al. (2016). Note that this analysis does not account for light curve effects in the optical counterpart—this effect will be studied in a future work (A. Gustafsson et al. 2018, in preparation).

3.4. Notes on Individual NEOs

1990 UA: This is an object with no previously reported rotation period. The *Spitzer* 4.5 μ m light curve shows a distribution with three peaks over 315 minutes of observation. The Lomb–Scargle algorithm reports a period of 93.680 minutes, which is a solution that judges all of the peaks

¹⁸ See http://nearearthobjects.nau.edu/spitzerneos.html.

Object	AORID	UTC Start Time ^a (YYYY MM DD hh:mm:ss)	HMJD Start Time ^a (days)	Light Curve Duration (minutes)	Rotation Period (minutes)	Amplitude (mag)
1990 MF	52514560	2016 Feb 27 07:39:32	57445.3197069	105.0	54.4 ± 5.2	0.069 ± 0.012
1990 UA	42169088	2011 Jul 08 17:20:53	55750.7229074	315.8	180.1 ± 1.9^{b}	0.216 ± 0.008
1998 FF14	61788672	2016 Dec 27 16:27:21	57749.6862440	139.8	111.8 ± 4.2	0.271 ± 0.047
1999 JE1	42163456	2011 Jul 23 02:34:22	55765.1077800	544.3	394 ± 11.6	0.136 ± 0.015
2003 EO16	42164480	2011 Jun 16 09:11:35	55728.3836200	417.9	350.6 ± 3.4	0.135 ± 0.010
2005 HC3	52392192	2016 Apr 08 16:22:38	57486.6829712	178.5	144.2 ± 2.8	0.422 ± 0.046
2009 WD106	52496128	2015 Apr 10 16:43:14	57122.6972784	167.4	150.2 ± 7.8	0.299 ± 0.020
2011 SD173	52501760	2015 May 26 08:34:56	57168.3581743	163.6	137.0 ± 0.4	0.892 ± 0.022
2011 XA3	61855488	2017 Apr 17 09:50:19	57860.4105209	108.6	43.4 ± 0.6	0.648 ± 0.133
2015 XC	61809152	2017 Mar 14 18:31:52	57826.7727121	93.9	16.25 ± 0.05	1.566 ± 0.066

 Table 1

 Periodogram Fits of Full NEO Light Curves

Notes. Columns, from left to right: asteroid designations, Spitzer Astronomical Observation Request identifier, observation start time in UT, observation start time in heliocentric MJD, the observation duration, derived rotation period, and light curve amplitude (mag).

^a Time at the midpoint of the first frame of the observation.

^b The Plavchan algorithm was used to calculate this period; see Section 3.4.

symmetrically, which does not appear likely to be the case. The middle peak in the curve is noticeably narrower than the other two, which seems to be of similar width and height. Applying the Plavchan algorithm (Plavchan et al. 2008), we found that the highest peak at a period smaller than the light curve length gives a rotational period of 184.534 minutes. The phase plot for this solution is the one shown in Figure 1. Further observations of 1990 UA are necessary to unambiguously determine its rotation period.

2005 LG8. Light curve data for 2005 LG8 were obtained by Waszczak et al. (2015), who determined a period of 4.630 ± 0.0019 hr with an amplitude of 0.62 mag, although there is a note in the JPL Small Bodies Database that states "Result based on less than full coverage, so that the period may be wrong by 30 percent or so." Our derived period in Table 3 (3.62 hr) is near the full *Spitzer* sampling time, and there is some indication that the peaks of the light curves are not adequately sampled (see Figure 3), so it appears that the extrapolated period from the *Spitzer* data alone underestimates the period. We have performed a sine fit to the *Spitzer* data, constraining the fit to a 4.63 hr period, which also shown in Figure 3. The χ^2 value for this fit is ~10% higher than the unconstrained fit, but the data appear consistent with the curve for the longer period as reported by Waszczak et al. (2015).

2008 JM20. The length of time sampled for this object was just slightly longer than one full period, and this seemed to give the LS fitting some issues, with the best fit being about 120 minutes, which is greater than the length of time sampled. We again used the Plavchan algorithm for this object, which gave a rotational period of 208.8 ± 18.4 minutes, consistent with the period determined from the sine fitting.

2008 UE7. Ye et al. (2009) reported a light curve period of 3.25146 ± 0.00001 hr (195.0876 minutes) based on optical photometry obtained in 2008 December. The amplitude was ~ 0.2 mag, similar to the *Spitzer* value. The optical light curve is double-peaked, so it appears that the *Spitzer* data set covered less than half of the period. Therefore, the *Spitzer*-derived lower limit of 174.4 minutes is less than that derived from the optical data.

2011 SD173. The Spitzer light curve for 2011 SD173 has a high amplitude and a non-symmetric double-peaked

shape with a cusp-like feature at the minimum, indicating an irregular shape.

2011 WS2. Our thermal modeling based on the Spitzer observations (see Section 3.3) gives a diameter of $1.24^{+0.75}_{-0.34}$ km and an albedo of $0.104^{+0.099}_{-0.063}$ for this NEO. This is in agreement with previous results from WISE observations, which gave a diameter of 1.434 ± 0.056 km (Mainzer et al. 2011a).

2011 XA3. Urakawa et al. (2014) previously measured the period of this object to be 43.8 ± 0.4 minutes. This compares well to the value we derived of 45.2 ± 5.0 . The *Spitzer* period was not the highest peak reported by the LS algorithm; the highest periodogram peak was at 21.7 ± 0.3 minutes, or roughly half of the value in the table. That period solution is for the case of each peak in the light curve being at the same phase. However, the appearance of the light curve indicated that there are alternating peaks of different magnitudes; therefore this solution was chosen as being more likely. This was done before comparing to previous measurements.

Urakawa et al. (2014) determined that the diameter of 2011 XA3 is 255 ± 97 m if it is S-complex, and 166 ± 63 m if it is V-type, based on the albedo assumptions for S-complexes and V-types from Pravec et al. (2012) and Usui et al. (2013). Our estimate of the diameter of 2011 XA3, based on NEATM modeling using this *Spitzer* 4.5 μ m observation, is 163^{+56}_{-29} m, implying the object is more likely to be V-type than S-complex.

2015 XC:. This NEO was observed on 2015 December 02 by Carbognani & Buzzi (2016), who reported a period of 0.2767 ± 0.0001 hr (16.602 ± 0.006 minutes) and an amplitude of 0.39 mag in the *R* band. Further observations and an analysis by Pravec revealed that this NEO is likely a tumbler with a complex shape (Warner 2016). They found periods of P1 = 0.181099 hr and P2 = 0.27998 hr, the second period being roughly consistent with the value of 16.25 ± 0.05 minutes (0.2708 ± 0.001 hr) that we report here. We find the amplitude at 4.5 μ m of 1.566 ± 0.066 mag is higher than that seen in the optical measurements, where the maximum is ~0.64 mag. Our *Spitzer* light curve shows nonsinusoidal structure and amplitude that varies by a factor of 4 in flux, confirming the earlier indications that this object has a complex shape.

 Table 2

 Periodogram Fits of Partial NEO Light Curves

Object	AORID	UTC Start Time ^a (YYYY MM DD hh:mm:ss)	HMJD Start Time ^a (days)	Light Curve Duration (minutes)	Lower Limit to Rotation Period (minutes)	Amplitude (mag)
1991 BN	52457216	2015 Feb 28 01:55:51	57081.0810333	108.9	114.6 ± 8.4	0.218 ± 0.040
1996 FS1	52366592	2015 May 19 06:24:06	57161.2621636	108.8	163.2 ± 1.7	0.404 ± 0.015
2000 OM	44166656	2011 Aug 28 20:20:08	55801.8479200	152.7	190.2 ± 7.4	0.354 ± 0.049
2001 DF47	61870080	2016 Oct 25 21:58:09	57686.9159586	139.7	158.8 ± 4.8	1.208 ± 0.261
2003 BO1	52507648	2015 Jun 23 19:09:23	57196.7987658	182.3	187.4 ± 6.4	0.363 ± 0.063
2003 XE	52498944	2015 Apr 26 03:01:09	57138.1263838	108.7	203.8 ± 5.4	0.709 ± 0.047
2008 GV3	52410112	2016 Jan 16 12:07:41	57403.5059145	108.7	172.2 ± 7.2	0.231 ± 0.022
2008 JM20	58815488	2016 Aug 03 03:53:54	57603.1630151	108.7	208.8 ± 18.8^{b}	0.187 ± 0.020
2008 UE7	52413184	2015 Jul 16 18:52:07	57219.7867809	106.7	174.4 ± 10.6	0.270 ± 0.024
2008 UF7	52413440	2015 Feb 01 06:39:26	57054.2779595	156.5	166.1 ± 1.8	0.514 ± 0.053
2011 GM44	52424704	2015 Jul 02 06:21:57	57205.2658287	106.8	155.8 ± 4.2	0.277 ± 0.015
2013 CW32	61845504	2017 May 13 05:50:42	57886.2441315	42.6	79.2 ± 2.6	0.224 ± 0.030

Notes. Columns: asteroid designations, *Spitzer* Astronomical Observation Request identifier, observation start time in UT, observation start time in heliocentric MJD, the observation duration, derived rotation period, and light curve amplitude (mag). The periods and amplitudes should be treated as lower limits.

^a Time at the midpoint of the first frame of the observation.

^b The Plavchan algorithm was used to calculate this period; see Section 3.4.

4. Cohesive Strength

The minimum cohesive strength has been determined for only a small sample of NEOs to date. The elongation and rotation period of most objects require a minimum cohesive strength of 0 Pa. As a lower limit, this is not informative. For these objects, light curves alone are not enough to determine whether they are strengthless rubble piles or have some significant internal strength. Instead, we look at objects with high amplitudes or very short rotation periods that require nonzero minimum strengths. The minimum cohesive strength has been studied for fast-rotating objects (Polishook et al. 2017) and highly elongated objects (McNeill et al. 2018) but the overall sample size remains small. A survey like the work presented in this paper serves to increase this population as we will incidentally identify high amplitude and fast-rotating objects without the need for a targeted study.

Of the observed objects we find two with D > 200 m and 4.5 μ m light curves showing rotation periods shorter than the spin barrier at P = 2.2 hr. If these bodies are rubble piles they should undergo rotational fission at their current spin rate. Instead we must assume that they have some internal cohesive strength or are monolithic in nature. Therefore, we calculate the cohesive strength required using a simplified Drucker–Prager model (Holsapple 2004).

The Drucker–Prager failure criterion models the threedimensional stresses within geological material at the point of critical rotation. The three orthogonal shear stresses on a body in the xyz axes are dependent on the shape, density, and rotational properties of the body (Holsapple 2007):

$$\sigma_x = (\rho\omega^2 - 2\pi\rho^2 GA_x)\frac{a^2}{5},\tag{1}$$

$$\sigma_{\rm y} = (\rho\omega^2 - 2\pi\rho^2 GA_{\rm y})\frac{b^2}{5},\qquad(2)$$

$$\sigma_z = (-2\pi\rho^2 GA_z)\frac{c^2}{5},\tag{3}$$

where ρ is the bulk density of the asteroid, ω is its rotational frequency, G is the gravitational constant, and a, b, c are the

lengths of the semi-axes of the ellipsoidal body, from largest to smallest. These three A_i functions are dimensionless parameters dependent on the axis ratios of the body:

$$A_x = \frac{c}{a} \frac{b}{a} \int_0^\infty \frac{1}{(u+1)^{3/2} \left(u + \frac{b^2}{a}\right)^{1/2} \left(u + \frac{c^2}{a}\right)^{1/2}} du, \quad (4)$$

$$A_{y} = \frac{c}{a} \frac{b}{a} \int_{0}^{\infty} \frac{1}{(u+1)^{1/2} \left(u + \frac{b^{2}}{a}\right)^{3/2} \left(u + \frac{c^{2}}{a}\right)^{1/2}} du, \quad (5)$$

$$A_{z} = \frac{c}{a} \frac{b}{a} \int_{0}^{\infty} \frac{1}{(u+1)^{1/2} \left(u + \frac{b^{2}}{a}\right)^{1/2} \left(u + \frac{c^{2}}{a}\right)^{3/2}} du.$$
 (6)

The Drucker–Prager failure criterion is the point at which the object will rotationally fission and is given by

$$\frac{1}{6}[(\sigma_x - \sigma_y)^2 + (\sigma_y - \sigma_z)^2 + (\sigma_z - \sigma_x)^2]$$

$$\leq [k - s(\sigma_x + \sigma_y + \sigma_z)]^2, \qquad (7)$$

where *k* represents the cohesive strength within the body and *s* is a slope parameter dependent on the angle of friction, ϕ :

$$s = \frac{2\sin\phi}{\sqrt{3}\left(3 - \sin\phi\right)}.$$
(8)

For these calculations we consider the value $\phi = 35^{\circ}$, corresponding to the average angle of friction from geological materials (Hirabayashi & Scheeres 2015).

1990 MF was measured to have a full rotation period of 54.4 ± 5.4 minutes, with a light curve amplitude $A = 0.069 \pm 0.012$ mag. Scattering effects and increased shadowing at high phase angles will result in light curve minima appearing fainter. This causes the apparent light curve amplitude to be increased, leading to a potential overestimation of the amplitude. We correct for this using the method of Zappala et al. (1990), using their derived correction coefficient for S-type asteroids, 0.03 magdeg^{-1} . This results in a corrected amplitude for this light curve of $A = 0.025 \pm 0.004$ mag. Using these parameters, its *Spitzer*-derived diameter $D = 519^{+227}_{-116}$ m, and assuming a

Object	AORID	UTC Start Time ^a (YYYY MM DD hh:mm:ss)	HMJD Start Time ^a (days)	Light Curve Duration (minutes)	Lower Limit to Rotation Period (minutes)	Amplitude (mag)
1999 VT25	52457728	2016 Mar 10 00:33:20	57457.0237318	162.0	329.6 ± 0.64	0.228 ± 0.002
2000 OM	44166656	2011 Aug 28 20:20:08	55801.8479200	152.7	185.6 ± 0.30	0.299 ± 0.001
2000 SH8	58817280	2016 Jun 08 12:37:52	57547.5268862	103.2	290.6 ± 0.12	0.182 ± 0.001
2002 CA10	52459008	2015 May 15 15:10:54	57157.6331529	182.1	495.0 ± 3.0	0.956 ± 0.021
2002 CZ46	52462336	2015 Jul 01 09:04:46	57204.3788919	182.2	399.0 ± 1.4	0.552 ± 0.005
2002 PM6	52454656	2015 Sep 26 22:30:04	57291.9381325	42.5	146.4 ± 1.4	0.200 ± 0.011
2003 XE	52498944	2015 Apr 26 03:01:09	57138.1263838	108.7	192.2 ± 4.6	0.323 ± 0.010
2004 JR	52387584	2015 Feb 27 08:23:03	57080.3499218	165.6	468.2 ± 4.6	0.221 ± 0.006
2005 HN3	52392448	2015 Jul 27 14:28:50	57230.6039391	180.1	363.2 ± 6.8	0.480 ± 0.033
2005 LG8	52481280	2015 May 11 09:25:07	57153.3930231	108.7	$217.0^{b} \pm 3.0$	1.027 ± 0.054
2005 XY	52396544	2015 Feb 07 11:18:06	57060.4714836	167.2	395.0 ± 7.6	0.588 ± 0.037
2006 GA1	52460800	2015 May 04 16:48:26	57146.7008871	108.6	251.8 ± 4.8	0.639 ± 0.065
2007 TB23	52406272	2015 Feb 25 04:27:32	57078.1863634	103.3	255.8 ± 1.1	1.046 ± 0.024
2008 GV3	52410112	2016 Jan 16 12:07:41	57403.5059145	108.7	172.2 ± 0.4	0.179 ± 0.002
2008 JM20	58815488	2016 Aug 03 03:53:54	57603.1630151	108.7	209.4 ± 0.08	0.184 ± 0.001
2008 SD85	61826048	2016 Dec 28 11:34:16	57750.4827190	145.3	417.0 ± 0.88	0.486 ± 0.004
2009 CS1	52414720	2015 Oct 25 00:54:58	57320.0387609	180.4	541.0 ± 2.4	0.565 ± 0.009
2011 GM44	52424704	2015 Jul 02 06:21:57	57205.2658287	106.8	155.0 ± 0.6	0.220 ± 0.002
2011 SM68	52428288	2015 Feb 01 09:52:09	57054.4117981	182.0	367.0 ± 11	0.995 ± 0.084
2011 WS2	52429568	2015 Feb 03 02:31:17	57056.1056369	106.8	392.0 ± 1.8	1.453 ± 0.020
2013 CW32	61845504	2017 May 13 05:50:42	57886.2441315	42.6	76.4 ± 0.26	0.184 ± 0.002
6344 P-L	61869824	2017 May 27 14:39:23	57900.6112606	145.1	373.0 ± 0.28	0.259 ± 0.001

 Table 3

 Sinusoidal Eits of Partial NEO Light Curve

Notes. Columns: asteroid designations, *Spitzer* Astronomical Observation Request identifier, observation start time in UT, observation start time in heliocentric MJD, the observation duration, derived rotation period, and light curve amplitude (mag). The periods and amplitudes should be treated as lower limits.

^a Time at the midpoint of the first frame of the observation.

^b Period is not consistent with prior measurements; see the discussion in Section 3.4.



Figure 4. Plot of the frequency vs. diameter of the NEOs. The black dots are measurements of NEOs from the LCDB (Warner et al. 2009). The red points show the *Spitzer* measurements for the cases where the light curve covered the full rotation period, and the blue dots show the extrapolated values for those where less than one rotational period was observed. The *Spitzer* values fall in the range of previously observed NEOs. The red point at (0.517, 26.47) that is above the "spin barrier" line at a frequency of ~10 d⁻¹ is 1990 MF, which is discussed in Section 4.

typical S-type asteroid bulk density of $\rho = 2500 \text{ kg m}^{-3}$, we find that a cohesive strength of 225_{-72}^{+225} Pa is required for this object to resist rotational fission. This is a higher value than has been calculated for most rubble-pile asteroids and is a comparable value to the relatively large cohesion required by 2000 GD65, as calculated by Polishook et al. (2016). Unlike the case of 2001 OE84, the cohesive strength is not so large

(of order 10^3 Pa) that it is explicable only in terms of a monolithic structure (Polishook et al. 2017).

1991 BN was determined to have a rotation period $P = 114.6 \pm 8.4$ minutes, just below the spin barrier. The corrected light curve amplitude of this object was $A = 0.132 \pm 0.020$ mag, which results in an estimate for the required cohesive strength of 7^{+5}_{-4} Pa.

These two objects were found in our relatively small sample of *Spitzer* NEOs analyzed to date. The remainder of the data set may yield many more objects for which we can put limits on the cohesive strength and learn more about the internal strengths of asteroids.

5. Conclusions

We have presented a sample of 38 NEO light curves obtained from data taken as part of the ExploreNEOs, NEOSurvey, and NEOLegacy Spitzer programs. We derived periods and amplitudes based on Lomb-Scargle or Plavchan fits for 10 objects where we appear to have complete sampling of the periods, and also present lower limits for another 28 objects based on sine fits to light curves shorter than or about equal to one period. Six light curves were fit with both periodogram and sine fits and found to have consistent periods. Enabled by the sensitivity and stability of Spitzer/IRAC, the NEO surveys have observed thousands of objects where light curves can be extracted and periods and amplitudes can be determined or constrained by the data. Because of Spitzer's current position in its orbit, it can observe NEOs that are not currently accessible with Earth-based observatories. With the 4.5 μ m data, we can also estimate the diameter and measure the

albedos of the NEOs using the same observations. By analyzing the full database as we have done for this small sample, we will be able to extract light curves for hundreds of NEOs and determine or set limits on their periods and amplitudes.

This work is based on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology under a contract with NASA. Support for this work was provided by NASA through an award issued by JPL/Caltech. This work is supported in part by NSF award 1229776. IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under a cooperative agreement with the National Science Foundation.

Software: IRAF, mopex (Makovoz et al. 2006), IRACproc (Schuster et al. 2006).

Facility: Spitzer/IRAC.

ORCID iDs

Joseph L. Hora https://orcid.org/0000-0002-5599-4650 Michael Mommert https://orcid.org/0000-0002-8132-778X David E. Trilling https://orcid.org/0000-0003-4580-3790 Giovanni G. Fazio https://orcid.org/0000-0002-0670-0708 Steven Chesley https://orcid.org/0000-0003-3240-6497 Alan Harris https://orcid.org/0000-0001-8548-8268 Michael Mueller https://orcid.org/0000-0003-3217-5385

References

- Bus, S. J. 1999, PhD thesis, Massachusetts Institute of Technology
- Bus, S. J., & Binzel, R. P. 2002a, Icar, 158, 146
- Bus, S. J., & Binzel, R. P. 2002b, Icar, 158, 106
- Carbognani, A., & Buzzi, L. 2016, MPBu, 43, 160
- DeMeo, F. E., Binzel, R. P., Slivan, S. M., & Bus, S. J. 2009, Icar, 202, 160
- Fazio, G. G., Hora, J. L., Allen, L. E., et al. 2004, ApJS, 154, 10
- Giorgini, J. D., Yeomans, D. K., Chamberlin, A. B., et al. 1996, BAAS, 28, 1158
- Harris, A. W. 1998, Icar, 131, 291
- Harris, A. W., Mommert, M., Hora, J. L., et al. 2011, AJ, 141, 75
- Hirabayashi, M., & Scheeres, D. J. 2015, ApJL, 798, L8
- Holsapple, K. A. 2004, Icar, 172, 272
- Holsapple, K. A. 2007, Icar, 187, 500

- Hora, J. L., Carey, S., Surace, J., et al. 2008, PASP, 120, 1233
- Ivezić, Ž, Lupton, R. H., Jurić, M., et al. 2002, AJ, 124, 2943
- Leonard, G. J., Christensen, E. J., Fuls, C., et al. 2017, AAS Meeting Abstracts, 49.117.07
- Lomb, N. R. 1976, Ap&SS, 39, 447
- Mainzer, A., Bauer, J., Cutri, R. M., et al. 2014, ApJ, 792, 30
- Mainzer, A., Grav, T., Bauer, J., et al. 2011a, ApJ, 743, 156
- Mainzer, A., Grav, T., Masiero, J., et al. 2011b, ApJ, 741, 90
- Makovoz, D., Roby, T., Khan, I., & Booth, H. 2006, Proc. SPIE, 6274, 62740C
- Masiero, J. R., Nugent, C., Mainzer, A. K., et al. 2017, AJ, 154, 168
- McNeill, A., Trilling, D. E., & Mommert, M. 2018, ApJL, 857, L1
- Mommert, M., Farnocchia, D., Hora, J. L., et al. 2014a, ApJL, 789, L22
- Mommert, M., Harris, A. W., Mueller, M., et al. 2015, AJ, 150, 106 Mommert, M., Hora, J. L., Farnocchia, D., et al. 2014b, ApJ, 786, 148
- Mommert, M., Hora, J. L., Harris, A. W., et al. 2014c, ApJ, 781, 25
- Mueller, M., Delbo', M., Hora, J. L., et al. 2011, AJ, 141, 109 Müller, T. G., Ďurech, J., Ishiguro, M., et al. 2017, A&A, 599, A103
- Perna, D., Barucci, M. A., Fulchignoni, M., et al. 2018, P&SS, 157, 82
- Plavchan, P., Jura, M., Kirkpatrick, J. D., Cutri, R. M., & Gallagher, S. C. 2008, ApJS, 175, 191
- Polishook, D., Moskovitz, N., Binzel, R. P., et al. 2016, Icar, 267, 243
- Polishook, D., Moskovitz, N., Thirouin, A., et al. 2017, Icar, 297, 126
- Pravec, P., Harris, A. W., Kušnirák, P., Galád, A., & Hornoch, K. 2012, Icar, 221. 365
- Romanishin, W., & Tegler, S. C. 2005, Icar, 179, 523
- Scargle, J. D. 1982, ApJ, 263, 835
- Schuster, M. T., Marengo, M., & Patten, B. M. 2006, Proc. SPIE, 6270, 627020
- Sonnett, S., Mainzer, A., Grav, T., Masiero, J., & Bauer, J. 2015, ApJ, 799, 191
- Thomas, C. A., Emery, J. P., Trilling, D. E., et al. 2014, Icar, 228, 217
- Thomas, C. A., Rivkin, A. S., Trilling, D. E., Enga, M.-t., & Grier, J. A. 2011, Icar, 212, 158
- Trilling, D. E., Hora, J. L., Mommert, M., et al. 2017, AAS/DPS Meeting Abstracts, 49, 110.06
- Trilling, D. E., Mommert, M., Hora, J., et al. 2016, AJ, 152, 172
- Trilling, D. E., Mueller, M., Hora, J. L., et al. 2008, ApJL, 683, L199
- Trilling, D. E., Mueller, M., Hora, J. L., et al. 2010, AJ, 140, 770 Urakawa, S., Ohtsuka, K., Abe, S., Ito, T., & Nakamura, T. 2014, AJ, 147, 121
- Usui, F., Kasuga, T., Hasegawa, S., et al. 2013, ApJ, 762, 56
- Vereš, P., & Chesley, S. R. 2017, AJ, 154, 12
- Vereš, P., Jedicke, R., Fitzsimmons, A., et al. 2015, Icar, 261, 34
- Warner, B. D. 2016, MPBu, 43, 143
- Warner, B. D., Harris, A. W., & Pravec, P. 2009, Icar, 202, 134
- Waszczak, A., Chang, C.-K., Ofek, E. O., et al. 2015, AJ, 150, 75
- Werner, M. W., Roellig, T. L., Low, F. J., et al. 2004, ApJS, 154, 1
- Wolters, S. D., Green, S. F., McBride, N., & Davies, J. K. 2008, Icar, 193. 535
- Wright, E. L., Eisenhardt, P. R. M., Mainzer, A. K., et al. 2010, AJ, 140, 1868
- Ye, Q., Shi, L., Xu, W., Lin, H.-C., & Zhang, J. 2009, MPBu, 36, 180
- Zappala, V., Cellino, A., Barucci, A. M., Fulchignoni, M., & Lupishko, D. F. 1990, A&A, 231, 548