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1 **STRENGTH ASSESMENT OF AL-HUMIC AND AL-KAOLIN**
2 **AGGREGATES BY INTRUSIVE AND NON-INTRUSIVE METHODS**
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33 **Abstract:**

34 Resistance to breakage is a critical property of aggregates generated in water and wastewater
35 treatment processes. After flocculation, aggregates should ideally keep their physical
36 characteristics (i.e. size and morphology), to result in the best performance possible by individual
37 separation processes. The integrity of aggregates after flocculation depends upon their capacity to
38 resist shear forces while transported through canals, passages, apertures, orifices and other
39 hydraulic units. In this study, the strength of Al-Humic and Al-Kaolin aggregates was
40 investigated using two macroscopic measurement techniques, based on both intrusive and non-
41 intrusive methods, using image analysis and light scattering based equipment. Each technique
42 generates different information which was used for obtaining three floc strength indicators,
43 namely, strength factor (SF), local stress from the hydrodynamic disturbance (σ) and the force
44 coefficient (γ) for two different study waters. The results showed an increasing trend for the SF of
45 both Al-Humic and Al-Kaolin aggregates, ranging from 29.7% to 78.6% and from 33.3% to
46 85.2%, respectively, in response to the increase of applied shear forces during flocculation (from
47 20 to 120 s^{-1}). This indicates that aggregates formed at higher shear rates are more resistant to
48 breakage than those formed at lower rates. In these conditions, σ values were observed to range
49 from 0.07 to 0.44 N/m^2 and from 0.08 to 0.47 N/m^2 for Al-Humic and Al-Kaolin, respectively.
50 Additionally, it was found that for all studied conditions, the resistance of aggregates to shear
51 forces was nearly the same for Al-Humic and Al-Kaolin aggregates, formed from destabilized
52 particles using sweep coagulation. These results suggest that aggregate strength may be mainly
53 controlled by the coagulant, emphasizing the importance of the coagulant selection in water
54 treatment. In addition, the use of both intrusive and non-intrusive techniques helped to confirm
55 and expand previous experiments recently reported in literature.

56

57 **Keywords:** Aggregates, floc resistance, image analysis, flocculation.

58 **1. Introduction**

59 Most solid-liquid separation processes work by increasing the size of the particulate matter,
60 leading to the formation of aggregates or flocs. The performance of solids removal is dependent
61 on the physical characteristics of the aggregates that need to be compatible with the separation
62 method used (Yukselen and Gregory, 2004). Among these characteristics, the floc strength,
63 which is an expression of resistance to breakage, is crucial for effective particle separation in
64 clarification units, such as sedimentation tanks, dissolved air flotation units and membrane
65 filtration (Jarvis *et al.*,2005).

66 It is well-documented that, solid-liquid processes are negatively affected by the breakage of flocs,
67 as only limited regrowth of broken flocs can occur, thus leading to low removal efficiency in
68 sedimentation units (Yukselen and Gregory, 2002, 2004; Yu *et al.*, 2010b, 2011, 2015). The floc
69 strength is also linked to problems in treatment plants with rapid sand filtration, in which the
70 small resistance of the aggregates to the hydrodynamic variations has a damaging impact on the
71 filter media, shortening their operational life and resulting in pollutant trespassing (Moruzzi and
72 Silva, 2018). Therefore, water treatment plants should ideally be designed to minimize floc
73 breakage; however, despite the recommendations, it is difficult to precisely determine how much
74 stress a previously formed floc can take without breaking.

75 When the shear rate is larger than floc strength, the flocs either break into approximately equal
76 size fragments, or under some circumstances, erosion of small particles from the flocs' surface
77 may occur. In turbulent flow, the breakage type depends on the size of the flocs in relation to the
78 micro-scale of turbulence (Mühle, 1993). Because of floc breakage, some regions of the floc
79 surface may become inactive and incapable of forming new bonds of attachment to other flocs,
80 thus reducing the flocculation efficiency (Yu *et al.*, 2011). The fact that broken flocs do not fully
81 regrow when the original low shear rate is restored means that the binding between particles is
82 weaker (Yu *et al.*, 2010b).

83 It is well acknowledged that the floc strength is dependent on the bonds between aggregate
84 component particles (Parker *et al.*, 1972, Bache *et al.*, 1997). This includes the strength and
85 number of individual bonds within the floc. However, recent studies (e.g. Yu *et al.*, 2015) have
86 shown that kaolin particles incorporated within hydroxide flocs appear to have no influence on
87 floc properties, including floc strength and size. Younker and Walsh (2016) demonstrated that the

88 addition of adsorbents to metallic salt flocs did not increase or reduce floc strength. Conversely,
89 kaolin flocs formed by ferric coagulants were found to be larger and stronger than those formed
90 by alum coagulants (Zhong *et al.*, 2011). Bridging flocculation by long-chain polymers can
91 generate very resistant flocs, while the destabilization of particles by low dosages of inorganic
92 salts results in fairly weak flocs (Yukselen and Gregory, 2004; Wang *et al.*, 2009; Yu *et al.*,
93 2015).

94 Humic acids have been widely used as natural organic matter to investigate floc properties after
95 flocculation. It has been shown that humic flocs growth is not determined by the flocs' size
96 distribution (Yu *et al.*, 2010b, 2012), but by some of their properties, including floc strength,
97 which is mostly dependent on the surface activity of flocs, and coagulant species formed from
98 Alum and Iron hydrolysis (Wang *et al.*, 2009).

99 Moruzzi and Silva (2018) carried out experiments on Al-Humic and Al-Kaolin aggregates and
100 showed that flocs formed from sweep coagulation mechanism, by different particulate matter and
101 the same coagulant have similar regrowth patterns, indicating similar binding between particles
102 for Al-Humic and Al-Kaolin, as presented by Yu *et al.* (2010b). On the basis of these findings, it
103 is speculated that Al-Humic flocs strength might have similar resistance to shear forces as Al-
104 Kaolin flocs. In this case, the resistance of the flocs to shear rate could be attributed to the used
105 coagulant, corroborating with results presented by Yu *et al.* (2015).

106 For determining aggregate proprieties, such as size and floc strength, monitoring techniques
107 should be applied during flocculation. Intrusive techniques, such as those based on light
108 scattering, have been conventionally used for monitoring aggregates during flocculation
109 (Yukselen and Gregory, 2002; 2004; Yu *et al.*, 2011). However, these techniques require taking
110 frequent samples from the water into measurements chambers, a process that may cause some
111 damage to aggregates due to their fragile nature. In some cases, flocs damage may be minimized
112 by limiting the average gradient velocity during the sample extraction, controlling inner tube size
113 and flow through tube, as presented by Gregory (1981) and Yu *et al.* (2010b). Recently,
114 however, flocculation monitoring by non-intrusive image analysis has shown promising results
115 (Li *et al.*, 2007; Moruzzi *et al.*, 2017; Moruzzi and Silva, 2018) and has allowed the
116 determination of floc strength, among other floc characteristics.

117 In practice, the strength of the floc is often determined in an empirical way, usually by
118 establishing a relationship between the floc size and the applied shear rate (François, 1987; Jarvis
119 *et al.*, 2005, Li *et al.*, 2007). This empirical approach was firstly suggested by Parker *et al.*
120 (1972), and it has been used extensively in theoretical and experimental research to evaluate
121 maximum floc size under a given turbulent intensity (e.g. Bache, 1989; 2004 and Li *et al.*, 2006;
122 2007).

123 There are two fundamental approaches to measuring the strength of the floc *i.e.* a macroscopic
124 approach, which measures the system energy required for breakage of flocs, and a microscopic
125 approach, which measures the interparticle forces within individual flocs (Jarvis *et al.*, 2005). In
126 the microscopic approach, the strength can be measured by applying a shear stress or a normal
127 stress to a floc individually. On the other hand, macroscopic techniques perform an indirect
128 evaluation of the floc resistance by means of analysing the energy dissipation, or the mean
129 velocity gradient (G), applied to maximum- or average-sized flocs. This approach originated from
130 the empirical relationship between the applied hydrodynamic shear rate and the resulted floc size
131 (Jarvis *et al.*, 2005).

132 This work aims to investigate the floc strength for both Al-Kaolin and Al-Humic aggregates by
133 means of macroscopic indicators, and to demonstrate the insignificant effect of the particulate
134 matter within the flocs on their properties, namely size and strength. For the first time, image
135 analysis is applied concomitantly with photometric dispersion to obtain the strength factor (SF),
136 local stress from the hydrodynamic disturbance (σ) and the force coefficient (γ). The combined
137 application permits the comparison and establishment of correlations between the data obtained
138 from two different techniques (intrusive and non-intrusive). This is the first time image and
139 photometric dispersion of Al-Humic acid flocs is measured by this technique and the results from
140 the two complementary methods is used to understand the factors affecting floc strength.

141 **2. Materials and Methods**

142 *2.1 Study Waters*

143 Two water samples were prepared from stock suspension of kaolin and from stock solution of
144 humic acid. For sample one, hereafter referred to as type 1, a humic acid solution prepared from
145 lyophilised natural organic matter (*Aldrich Chemical*) with concentration of 30 mg/L was used to
146 obtain 50 units of Platinum-Cobalt Scale - PtCo at 455 nm, as the initial condition (Moruzzi and

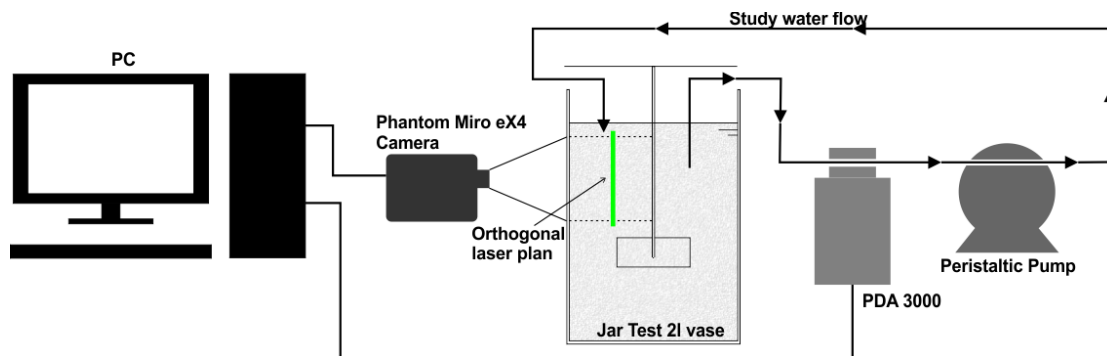
147 Silva, 2018). For the second sample (type 2), a kaolin suspension was prepared from a
148 commercial kaolin (Sigma-Aldrich) to obtain 25 units of turbidity scale as Nephelometric
149 Turbidity Units - NTU (Moruzzi *et. al*, 2017 and Yukselen and Gregory, 2004).

150 Coagulation was performed by dosing alum $[\text{Al}_2(\text{SO}_4)_3 \cdot 18\text{H}_2\text{O}]$ using sweep-coagulation
151 mechanism, following recommendations by Oliveira *et al.* (2015). So, dosages of 10 and 30
152 $\text{mgAl}^{+3}/\text{l}$ at pH of 7.5 and 4.5 were applied for Al-Kaolin and Al-Humic aggregates formation,
153 respectively. Sodium hydroxide (NaOH) 1 mM was used as a buffer during coagulation to control
154 pH. All tests were performed at room temperature (20 ± 2 °C).

155 *2.2 Flocculation and strength tests*

156 Jar tests were performed for flocculation and breakage experiments (*Ethik Technology Model*
157 *218/6 LDB*). The method applied consists of an intrusive and non-intrusive image-based
158 acquisition method and photometric dispersion analyser (PDA), similar to that used by Yu *et al.*
159 (2015). Here, however, both image and photometric dispersion were applied at the same time to
160 obtain strength indices, thus permitting comparison and correlation of results. A simplified
161 schematic of the experimental apparatus, including Jar Test, the image-based system and light-
162 scattering monitoring equipment, is shown in Figure 1.

163 A mean velocity gradient of 800 s^{-1} was applied for 10 seconds to ensure a rapid mixing, and also
164 for flocs breakage in all light scattering tests, based on preliminary tests (Oliveira *et al.*, 2015).
165 This standard shear rate was chosen for taking a central position in the typical shear range of
166 predominant erosion breakage as proposed by Mikkelsen and Keiding (2002), and the duration
167 was sufficient for the coagulant transportation (Yukselen and Gregory, 2004). For flocculation,
168 the following velocity gradients (G) were applied: 20, 30, 40, 50, 60, 80, 100 and 120 s^{-1} . For the
169 trials involving PDA measurements, G values were kept constant during the first 25 minutes, and
170 after this period, G was set to 800 s^{-1} for 10 seconds to induce breakage of flocs. This short period
171 of time was chosen to simulate the water passage in gates and orifices that normally occur after
172 flocculation.



173

174 Figure 1. A simplified schematic of the experimental apparatus.

175

176 2.3 Image Analysis

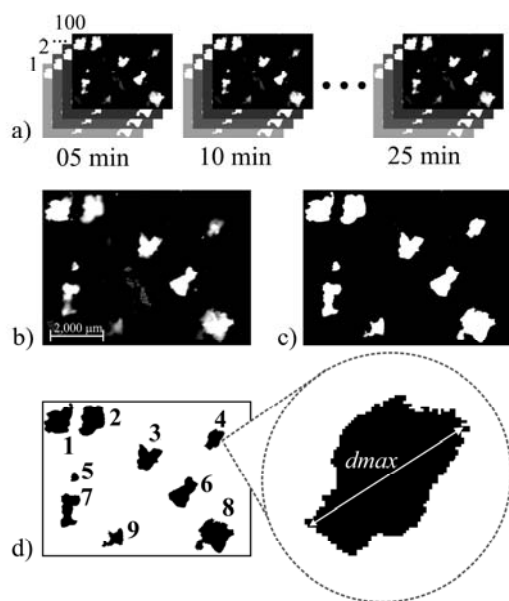
177 The image analysis applied here was strictly used to obtain aggregates size, which in turn was
 178 used for floc strength indicator calculations, namely local stress from the hydrodynamic
 179 disturbance (σ) and the force coefficient (γ), as presented in Section 2.6. Images were captured in
 180 2^8 bit monochromatic mode (*i.e.* 256 grey scale) using a *Vision Research Miro EX4* camera
 181 together with a set of lenses, and 840 pixel x 640 pixel of image resolution, to obtain a pixel size
 182 of 10 μm . A laser sheet of 20,000 mW and wavelength of 520 nm provided the lighting as
 183 described by Oliveira *et al.* (2015) and Moruzzi *et al.* (2017).

184 Samples were obtained at 5-minute intervals (from 5 to 25 minutes) to assess floc size at a given
 185 flocculation time (T) of interest, *i.e.* those usually applied in drinking water treatment plants.
 186 Each image package was taken over a short duration of 10 seconds with a frequency of 10 Hz
 187 (Figure 2-a) to precisely describe the system situation at that given time of interest. This sample
 188 time and frequency was sufficient to capture a reliable picture of the floc characteristics at the
 189 required flocculation time along with a statically representative number of flocs within the 10
 190 seconds sampling time.

191 The image processing software *Image-Pro-Plus*® (IPP) was used to develop the images, *i.e.*
 192 conversion from 2^8 to 2^1 bits, enhancement and measurement (Figures 2-b to 2-d). Only
 193 aggregate sizes longer than 100 μm (≥ 10 pixels) were monitored for image precision, as
 194 recommended by Chakraborti *et al.* (2003).

195 In total, 197,207 aggregates were measured from 7,200 frames (average of 27 aggregates/frame)
 196 for Al-Humic water, and 141,609 aggregates were measured from 6,800 frames (average of 21

197 aggregates/frame) for Al-Kaolin water. In these sample sizes, floc size errors were lower than
 198 4.0% and 4.6% at 95% of confidence interval for an infinite population of Al-Humic and Al-
 199 Kaolin aggregates, respectively. Figure 2 illustrates the different steps involved in the image
 200 processing procedure applied here, from acquisition to image processing and size measurement.



201

202 Figure 2. An example of image conversion enhancement and measurement: (a) Image acquisition
 203 using on 10 Hz during 10 seconds for each flocculation time (T), resulting in a pack of 100 frames
 204 per $G \times T$; (b) Floccs in grey scale (2^8 bits); (c) Image after threshold with black and white pixels
 205 only (2^1 bits); (d) Counting and measuring floccs by IPP 7.0 software®.

206 2.4 Light Scattering

207 The light scattering approach applied was strictly used to obtain the flocculation index (FI),
 208 which will be better explained in the following sections. Light scattering analysis was performed
 209 using a *Photometric Dispersion Analyser* (PDA), and the obtained results were used for
 210 calculating the strength factor, which will be introduced and presented in Section 2.6. In PDA
 211 equipment, samples flow through a 3-mm-diameter tube where the intensity of a narrow beam of
 212 light is monitored by a sensitive photodetector following Yukselen and Gregory (2004) and
 213 Moruzzi *et al.* (2017). Although intrusive technologies can cause some damage to floccs, in PDA
 214 this can be minimised by controlling the average gradient velocity during sample extraction.
 215 Here, the flow rate through the sampling tube was controlled to enforce laminar flow regime

216 (Reynolds number ≤ 80) and shear rates lower than 50 s^{-1} , as shown by Gregory (1981);
217 conditions where damage is considered insignificant, as also shown by Yu *et al.*, 2010b. Further,
218 the water samples were circulated by means of a peristaltic pump located after the PDA
219 instrument to avoid the effects of possible floc breakage in the pinch part of the pump (Figure 1),
220 as performed by Li *et al.* (2007).

221 The *PDA 3000* measures the average transmitted light intensity (dc value) and the root mean
222 square (rms) value of the fluctuating component. The ratio (rms/dc) provides a measure of the
223 balance of particle aggregation (Gregory, 1984; Gregory and Nelson, 1986; Yukselen and
224 Gregory, 2004; Yu *et al.*, 2010b), hereafter referred to as flocculation index (*FI*). Up to a limited
225 size, the *FI* value is strongly correlated with floc size and always increases as flocs grow larger,
226 but the *FI* value can become uncertain when flocs are larger than $250 \mu\text{m}$ and absolute floc size
227 cannot be taken from *FI* signals (Yu *et al.*, 2010a; Yu *et al.*, 2010b and 2011). Also, larger
228 aggregates have a predominant influence on the ratio value (Gregory, 1984), thus affecting *FI*
229 signals. Therefore, the PDA shows qualitative changes in flocs, as reported by Gregory and
230 Nelson (1986), but the instrument is unable to give an absolute particle size. Further, the *FI*
231 signals vary with both particle size and particle number and it is not possible to know the precise
232 contribution of each of these components in the *FI* signal. Yu *et al.* (2015) have shown that flocs
233 with similar size can have very different *FI* values, confirming the idea that *FI* does not give an
234 absolute indication of size for hydroxide flocs. However, the generated signal can be used as an
235 indicator of aggregation, as shown by Gregory (1985), and also as a measure of floc strength as
236 shown by Li *et al.* (2007), Gregory (2009) and Yu *et al.* (2010b). More details are given in the
237 following sections.

238

239 2.5 Floc size and *FI* determination

240 The macroscopic techniques used for the study of the floc strength were developed based on the
241 relationship between the applied hydrodynamic shear rate and the resulting floc size. According
242 to Gregory (2003), floc size and *FI* can be both used as floc strength indicators for a given shear
243 rate. In order to obtain the floc strength indicators, which are related directly to the size limit
244 reached by the floc, two different sources of information were utilized: one from the image
245 analysis and another from the PDA.

246 For image analysis, the average diameter (d) of aggregates was determined from the average of
247 the longest length of the aggregates (d_{max}) in the selected times of interest, following Li *et al.*
248 (2007):

$$249 \quad d = \frac{1}{n} \sum_{i=1}^n d_{imax} \quad (1)$$

250 where d is the average of d_{max} (μm), d_{max} is the longest length (μm), as shown in Figure 2, and n
251 is the number of counted aggregates in a sample varying from $i = 1, 2 \dots, n$.

252
253 The d values obtained from Equation 1 represents the average of d_{max} , measured for each one of
254 the eight investigated flocculation times (T), *i.e.* 5, 10, 15, 20, 25, 30, 35 or 40 minutes. It is
255 important to emphasize that, flocculation kinetics were not the focus of this paper, but rather the
256 floc strength assessment at given flocculation times of interest, where the dynamic equilibrium
257 between flocs breakage and aggregation could be indirectly observed by the floc size. Therefore,
258 the d value represents the balance between flocs aggregation and breakage at a given time of
259 flocculation, and its average size tends to a stable value, *i.e.* a limiting size, for a given shear rate
260 as the steady state regime is reached. When little variation is observed in floc size, the average
261 size of d remains oscillating slightly around a maximum value, which is referred to as the plateau.

262 The plateau was determined from the incremental variation of the average diameter (d) during
263 flocculation. This variation tends to a narrow range because of the dynamic steady state. The
264 incremental variation can be determined by:

$$265 \quad \Delta d_i = \left| \frac{(d_i - d_{i-1})}{d_i} \right| \quad (2)$$

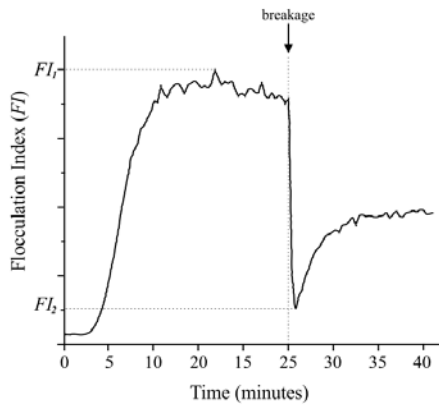
266 where Δd_i is the incremental variation of average diameter between the time interval $t_i - t_{i-1}$, with i
267 = 1, 2, ..., n.

268 The typical value of the diameter in the plateau was then determined from the average of
269 diameters within $\Delta d \leq 10\%$. Hypothesis tests were also performed to confirm the plateau with
270 significance of 0.05.

271 The analysis based on light scattering was done through the *FI* signal generated from the PDA.

272 The maximum value observed in the stationary flocculation phase was adopted once the plateau

273 was reached at that time interval. For FI_2 , the value adopted was the minimum point at the instant
 274 of the induced rupture, following Li *et al.* (2007). Here, the rupture shear rate of 800 s^{-1} was
 275 applied for 10 seconds, at the flocculation time of 25 minutes. Figure 3 schematically shows how
 276 FI_1 and FI_2 are determined from the FI signal.



277

278 Figure 3. Schematic representation of the FI signal, with indication of the values of FI_1 , FI_2 and
 279 induced breakage by applying velocity gradient of 800 s^{-1} at 25 minutes (adapted from Li *et al.*,
 280 2007).

281

282 2.6 Floc strength indicators

283 As mentioned in previous sections, the floc strength indicators presented here were determined
 284 using both image analysis and PDA. For the image analysis method, d values were taken, whilst
 285 for PDA only FI signals were used.

286 Floc strength coefficient (γ)

287 The floc strength coefficient (γ) was obtained from image analysis using Equation 3 that
 288 describes the stable size determined from image analysis as a function of the mean velocity
 289 gradient applied to the system during flocculation, firstly suggested by Parker *et al.* (1972):

$$290 \quad d = C \cdot G^{-\gamma} \quad (3)$$

291 where C is the multiplicative constant ($\mu\text{m/s}$), G is the average velocity gradient (s^{-1}), and γ is
 292 the floc strength coefficient (dimensionless), obtained from stable floc size.

293 The floc strength coefficient (γ) can be calculated using mean, median and longest length of flocs
 294 with nearly the same results, as reported by Leentvaar and Rebhun (1983). For the results

295 presented here, d values were calculated using the longest length of flocs obtained during
296 flocculation from different shear rates according to Equation 1.

297 The $\ln-\ln$ plot of Equation 3 against the average gradient velocity **applied during flocculation**
298 results in a line, which its slope is indicative of floc strength. The inverse relationship of
299 proportionality indicates that the higher the value of γ , the more prone the floc is to breakage
300 under increasing shear rates, resulting in smaller aggregates (Li *et al.*, 2007). Therefore, the value
301 of γ is considered as an indicator of its strength. This concept was proposed by Parker *et al.*
302 (1972) and is adopted in the study of Li *et al.* (2007). Here, the floc strength coefficient (γ) was
303 determined from the slope of linear best fit to the $\ln-\ln$ plot of Equation 3, using experimental
304 data for the study waters. It is worth noting that the value of C can also be used as a floc strength
305 indicator, but only within the same experimental conditions, as its value depends upon the
306 method used for particle size measurements and the choice of the characteristic value of d (Jarvis
307 *et al.*, 2005).

308 *Strength factor (SF)*

309 The strength factor (SF) has been previously used by several researchers (*e.g.* Li *et al.*, 2007; Yu
310 *et al.*, 2010b and 2015; Su *et al.*, 2017) to compare the breakage and the strength of flocs in
311 different shear rate conditions for Al-Kaolin aggregates. The results of these studies indicate that
312 this parameter can be effectively used as a floc strength index. SF is calculated based on FI
313 signals only and used to characterize the aggregate size maintenance capacity, following
314 Yukselen and Gregory (2002):

$$315 \quad SF (\%) = \frac{FI_2}{FI_1} 100 \quad (4)$$

316 where FI_1 is the maximum FI value before breakage, and FI_2 is the FI value right after the
317 breakage period, as shown in Figure 3. In this study, FI_1 was calculated from different shear rates
318 and FI_2 was always determined after applying a shear rate of 800 s^{-1} , as described in Section 2.5.

319 High values of the SF indicate that flocs are better able to withstand shear rates, and therefore, the
320 higher the value of SF , the stronger the flocs can be considered for a given rupture shear rate
321 (Jarvis *et al.*, 2005). It is important to note that SF is not constant, the shear rate applied during

322 the breakage strongly affects FI_2 (Yu *et al.*, 2010b), and so, SF can only be compared for similar
323 **induced** rupture conditions. Here, the average velocity gradient of 800 s^{-1} was applied for rupture.

324 *Hydrodynamic disturbance (σ)*

325 In addition to the above-mentioned empirical methods for obtaining a force coefficient, Bache *et*
326 *al.* (1997) proposed a theoretical method where the mean force applied per unit area of the
327 system, σ (N/m^2), could be determined by:

$$328 \quad \sigma = \frac{4\sqrt{3}}{3} \frac{\rho_w \mathcal{E}^{3/4} d}{\nu^{1/4}} \quad (5)$$

329 where ρ_w is the density of the water (kg/m^3), \mathcal{E} is the local energy dissipation rate per unit mass
330 (m^2/s^3), d is the average of the longest length of aggregates at a given time, measured by image
331 analysis (m) and ν is the kinematic viscosity (m^2/s) at room temperature of $20 \pm 2^\circ\text{C}$.

332 Parameter \mathcal{E} is usually replaced by $\bar{\mathcal{E}}$ (Equation 6), which is the average rate of dissipation of the
333 local energy per unit mass and is directly proportional to G , a parameter easily administered
334 during the experiment:

$$335 \quad \bar{\mathcal{E}} = \nu G^2 \quad (6)$$

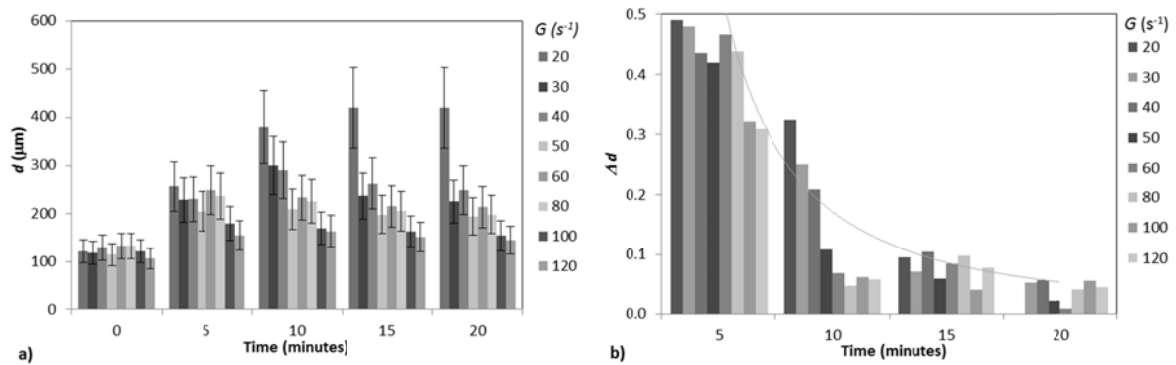
336 where ν is the kinematic viscosity (m^2/s).

337 **3. Results and Discussion**

338 *3.1 Image analysis*

339 Figure 4, as an example, presents the time evolution of d and Δd obtained from Equations 1 and
340 2, respectively, for various velocity gradients (G) applied to study water type 2. For d evolution
341 (Figure 4-a), aggregates have grown for time intervals between 5 and 10 minutes and for G from
342 20 to 40 s^{-1} . After 10 minutes of flocculation, only G of 20 s^{-1} has resulted in aggregates
343 increment for d . Consequently, the incremental variation of floc size (Figure 4-b) is observed to
344 be smaller than 10% for the majority of the analysed velocity gradients during the flocculation at
345 times 10-15 and 15- 20 minutes (except for G of 20, 30 and 40 s^{-1}), indicating the establishment
346 of steady-state conditions. Thus, d was obtained by averaging d during the period 15-20 minutes,
347 when significant stability was observed, *i.e.* when the stable size of d was reached. For these time
348 intervals, test of hypothesis has shown that there is no significant difference between the two

351 water types for p-value of 0.05, *i.e.* for both Al-Humic and Al-Kaolin the average diameter did
 352 not change for time intervals from 15 to 20 minutes, making it possible to confirm the plateau.



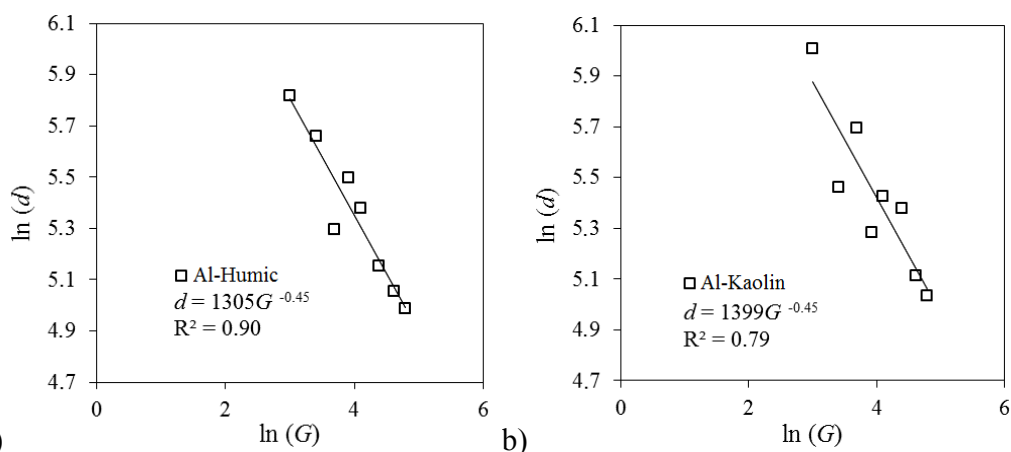
357 a) b)
 358 Figure 4. Time evolution of (a) d and (b) Δd during flocculation time (for discrete intervals of 5,
 359 10, 15 and 20 minutes) for water type 2. Fluctuation bars in (a), represent standard derivations
 360 and the decay curve in (b), represents the overall trend of Δd during time. Time zero in Fig. 4-a
 361 shows flocs size measurements in the very beginning of flocculation and those results were used
 362 as d_{i-1} for Δd calculation in time of 5 minutes, as Equation 2.

365 Figure 5 shows the relationship between $\ln(d)$, calculated by Equation 1, and $\ln(G)$, where the
 366 slope of the trend line, as described by Equation 3, indicates the floc strength coefficient γ . Once
 367 γ value remains constant, any variant characteristic of d (*i.e.* mean, median or maximum length)
 368 can be used for comparing results among different studies (Jarvis *et al.*, 2005). A decreasing
 369 tendency of the stable size d in response to the increase of G was observed at a rate near 0.45 for
 370 the two study waters, which is in the range of 0.44 to 0.63 reported by other researchers (*e.g.*
 371 Bache and Rasool, 2001; Francois, 1987; Li *et al.*, 2007) when using alum as coagulant for Al-
 372 Humic and Al-Kaolin flocs.

373 The obtained γ value for the two study waters indicates that Al-Humic and Al-Kaolin flocs are
 374 similarly able to resist shear rates, as the steepness of the $\ln-\ln$ plot slopes are nearly the same for
 375 both waters (0.45). The analysis of C from Equation 3 is not commonly used for floc strength
 376 evaluation, as it depends upon which characteristic of d has been used, and wide variation
 377 between different studies has been reported, *e.g.* from $\ln C$ of 7.1 to 9.4 according to Bache *et al.*
 378 (1999) and Bache and Rasool (2001), respectively. However, C can be also used to compare floc
 379 strength within specific experimental system (Jarvis *et al.*, 2005). Results presented here have
 380 shown C values of 1305 ($\ln C$ of 7.17) and of 1399 ($\ln C$ of 7.24) for Al-Humic and Al-Kaolin,

373 respectively, thus reinforcing that Al-Humic and Al-Kaolin have nearly the same ability to resist
 374 applied shear forces. These results are in agreement with the finding by Yu *et al.* (2015) who
 375 found that the nature of primary particles has no influence on floc strength when sweep
 376 coagulation mechanism is applied and once flocs rapidly grow and incorporate most particles
 377 within the hydroxide precipitate. Also, the use of a non-intrusive technique, such as the image
 378 analysis system here applied, permits to confirm the previous findings by Yu *et al.* (2015), once it
 379 is not influenced by possible interferences caused by samples extraction and light scattering, as
 380 presented by Gregory (2009) and Yu *et al.* (2015).

381 The analysis of strength coefficient (γ) can also be related to turbulent shear patterns due to eddy
 382 size, as proposed by Biggs and Lant (2000) and Bache (2004), resulting in different floc breakage
 383 modes during flocculation. Based on the analysis of the dominant mode of floc degradation
 384 presented by Parker (1972) and François (1987), the results presented here for γ (Figure 5)
 385 indicate that the flocs are more prone to breakage due to a dominant effect of fragmentation, as
 386 the result of the viscous energy dissipation, once the floc strength coefficient γ was around the
 387 theoretical value of 0.5. This is an indication that small eddies (*i.e.* the turbulence micro-scale) is
 388 of a similar order of magnitude to the flocs sizes (Mühle, 1993; Jarvis *et al.*, 2005). However,
 389 fragmentation and erosion are expected to occur at the same time, as large flocs in an aggregated
 390 system may be larger than the micro-scale whilst smaller flocs may be smaller than micro-scale
 391 (Biggs and Lant, 2000).

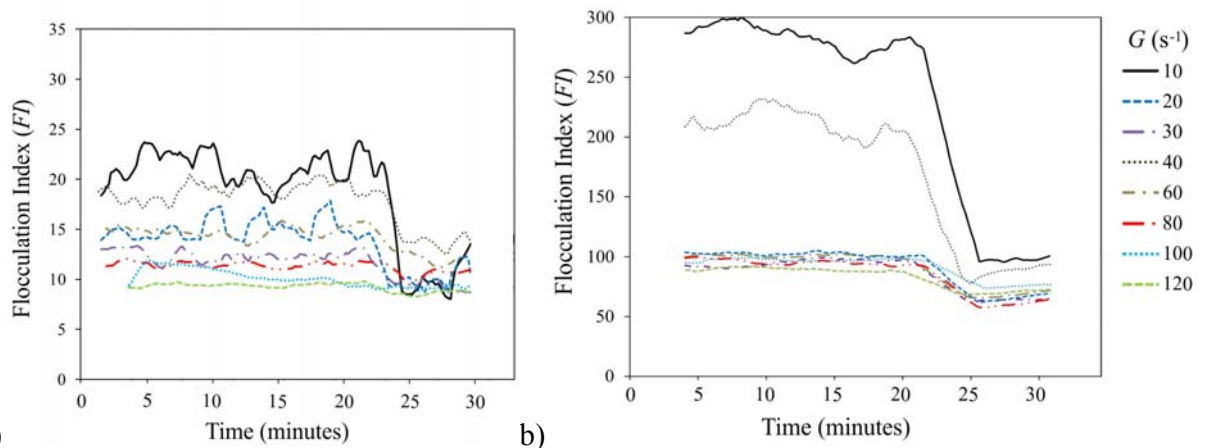


392 a) 393 Figure 5. Relationship between $\ln d$ versus $\ln G$ during flocculation: (a) water type 1 – Al-Humic
 394 and (b) water type 2 – Al-Kaolin. $\ln d$ was obtained by averaging d during the period 15-20
 395 minutes, where $\Delta d < 10\%$ was observed.

396 3.2 Light scattering

397 Figure 6 shows the temporal evolution of the FI signal (obtained by PDA) in the tests carried out.
398 It is clearly observed that in the flocculation [0-20 minutes] and regrowth [25-40 minutes] phases,
399 the floc size tend towards a stabilized plateau. The sharp drop of FI at 25 minutes was the point
400 where the induced breakage occurred. The difference in the signal scale between the two study
401 waters is caused by the different light scattering properties, *e.g.* floc density and scattering cross-
402 section, which are also dependent on both particle concentration (in terms of volume, mostly) and
403 type (Gregory, 2009). This difference has important implications for the monitoring of floc size
404 by light scattering methods as also observed by Yu *et al.* (2015). Similar fluctuation on FI values
405 were observed by Gregory (2009), while studying optical proprieties of flocs using PDA for
406 different waters. The author concluded that scattering cross-section is expected to be different
407 when different concentration of impurities, as clay, are within flocs and so FI signals vary.
408 However, the results obtained by Gregory (2009) have shown that curves are rather similar in
409 shape, showing the same relative increase in FI during floc formation. Therefore, although
410 scattering proprieties can limit direct comparisons of FI values among different waters, it is not
411 expected to affect the strength factor (SF) given by Equation 4, once it is determined as a ratio for
412 the same water, *i.e.* subjected to the same scattering properties.

413



414

415 Figure 6. Time evolution of FI for different velocity gradients, G before and after induced
416 breakage using 800 s^{-1} at time 25 minutes. (a) water type 1 for Al-Humic acid and (b) water type
417 2 for Al-Kaolin.

418

419 *3.3 Combined analyses of image and photometric dispersion methods*

420 Both analyses of image and photometric dispersion methods permitted to compare and correlate
421 data obtained from two different techniques *i.e.* intrusive and non-intrusive methods. Tables 1
422 and 2 present a comparison between the stable size and the floc strength for eight different
423 velocity gradients (G). The floc strength indicators presented are local stress (σ) and the force
424 factor (SF).

425 It is observed that, for each of the studied waters, SF , σ and d were strongly correlated with the
426 parameter G , resulting in Pearson correlation coefficient of 0.95, 0.99 and -0.89 for Al-Humic
427 and of 0.90, 0.99 and -0.80 for Al-Kaolin, respectively. Results found here corroborate well with
428 Li *et al.* (2007), who found that flocs formed at higher shear intensities have a small size and are
429 more resistant to breakage than those formed from lower ones. Floc resistance is determined by
430 both hydraulic shear rates and the strength of flocs bonds, which withstand shear forces during
431 floc formation (Jarvis *et al.*, 2005; Gregory, 2009). During floc formation in high shear rates, the
432 weak bonds might be broken, promoting a kind of selection, which results in floc fragments with
433 strong bonds. Therefore, with the higher shear rates, only the strongest bonds, which are more
434 likely to resist to the abrupt G variations, are maintained (Li *et al.*, 2007). This fact was shown by
435 the increase in SF value from 29.7% for G of 20 s^{-1} to 78.6% for G of 120 s^{-1} in water type 1 and
436 33.3% for G of 20 s^{-1} to 85.2% for G of 120 s^{-1} in water type 2.

437 Results in Tables 1 and 2 also suggested that the effect of G on SF might be more relevant for G
438 from 20 to 40 s^{-1} , and that d values can also decrease dramatically with the increase of G ,
439 indicating there might be a limit above which floc strength is slightly affected by shear rate, but it
440 can strongly affect floc formation.

441 Results obtained from the two other strength indices used here seem to agree with the strength
442 coefficient (γ) analysis. The values of σ were nearly the same for water types 1 and 2, ranging
443 from 0.08 to 0.47 and from 0.07 to 0.44, respectively, with Pearson correlation coefficient (r)
444 between waters near to 1 ($r = 0.97$). These results are in agreement with previous work done by
445 Bache *et al.* (1999) who found Al-Humic flocs strength in the range of 0.08 to 0.42 N/m^2 , and
446 close to the study by Li *et al.* (2007), who found Al-Kaolin flocs strength in the range of 0.01 to

447 0.24 N/m². Moreover, ANOVA test for σ variation with G indicates that floc strength is not
 448 different between Al-Humic and Al-Kaolin for 0.05 of significance (p-value over 0.05), but it
 449 depends on G and d only.

450 Regarding the strength factor (SF), results also have shown slight differences between aggregates
 451 formed from Al-Humic and Al-Kaolin. Again, the ANOVA test for SF with G indicates that floc
 452 strength is not different between Al-Humic and Al-Kaolin for 0.05 of significance, but it depends
 453 on G and d only.

454 Despite the fact that the intrinsic characteristics of flocs formed from Al-Kaolin and Al-Humic,
 455 namely, the scattering cross-section, altered FI measurements it seems that it did not affect floc
 456 strength measurements by SF , as it is in agreement with the other two strength indicators.
 457 Therefore, it is not expected that optical proprieties affect physical proprieties measurements,
 458 such as resistance, and so the FI signal has been used by many researchers as an aggregation
 459 indicator and as well as an indirect measurement of floc strength, *e.g.* Li *et al.* (2007), Yu *et al.*
 460 (2010b and 2011), Su *et al.* (2017).

461

G	SF	σ	d
(s ⁻¹)	(%)	N/m ²	μm
20	36.73	0.07	337
30	56.82	0.11	287
40	55.56	0.12	200
50	69.70	0.20	245
60	69.34	0.23	217
80	83.33	0.29	173
100	83.33	0.36	157
120	95.00	0.44	146

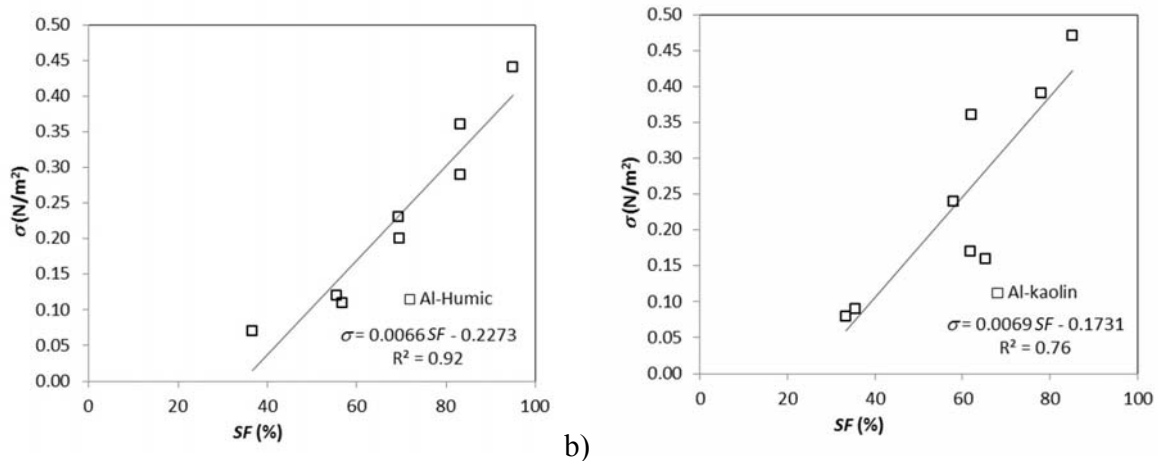
Table 1. Shear rates (G), strength indexes (SF and σ) and stable size (d) for water type 1 (Al-Humic acid) during flocculation.

G	SF	σ	d
(s ⁻¹)	(%)	N/m ²	μm
20	33.33	0.08	407
30	35.56	0.09	236
40	61.82	0.17	298
50	65.42	0.16	197
60	58.00	0.24	228
80	62.00	0.36	217
100	78.00	0.39	167
120	85.23	0.47	154

Table 2. Shear rates (G), strength indexes (SF and σ) and stable size (d) for water type 2 (Al-Kaolin) during flocculation.

462 Figure 7 shows the relationship of the strength factor (SF), obtained from PDA, with the
 463 parameter σ , which was calculated from image analysis data. It is observed that for both water

464 types, relatively high regression coefficients are obtained between SF and σ (R^2 of 0.92 and 0.76
 465 for Al-Humic and Al-Kaolin, respectively) and a similar slope (close to 0.0070) is found for
 466 σ/SF . It is apparent that the values of both mentioned parameters enhance with increase in G ,
 467 which are in agreement with results presented by Li *et al.* (2007) and Jarvis *et al.* (2005). Further,
 468 Pearson correlation coefficient between SF and σ resulted in 0.96 and in 0.87 for Al-Humic and
 469 Al-Kaolin, respectively. **These strong correlations have confirmed that the macroscopic approach**
 470 **represented by SF is consistent with the theoretical method for different types of water, despite of**
 471 **the different methods used and the variations of FI signals.**



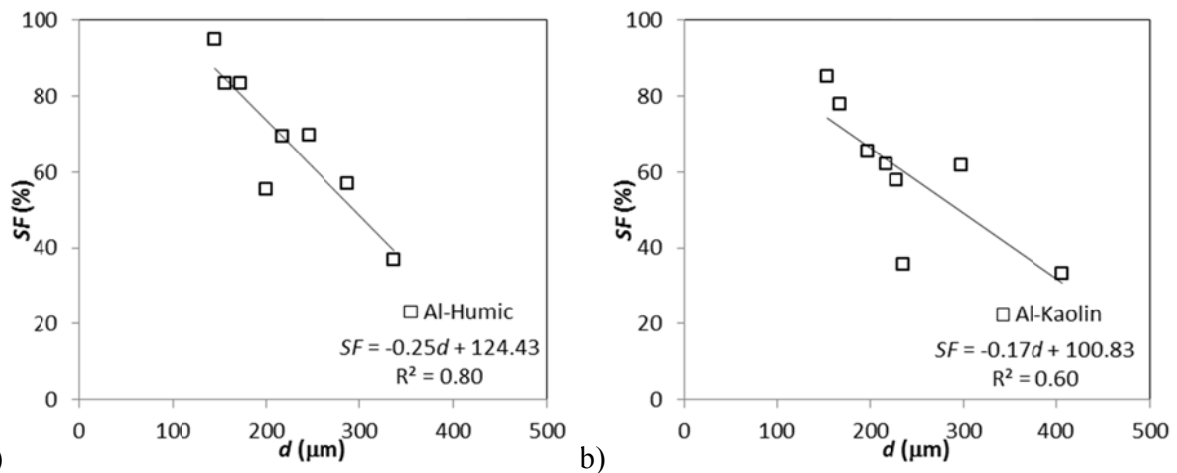
472 a) b)
 473 Figure 7. Relationship between SF and σ for (a) water type 1 for Al-Humic acid and (b) water
 474 type 2 for Al-Kaolin.

475 Figure 8 shows the relationship between SF and d , *i.e.* the specific relationship between the
 476 strength force indicator obtained from PDA and values of average floc length, monitored by
 477 image analysis. The strength factor (SF) behaved nearly the same as d varied for Al-Humic and
 478 Al-Kaolin flocs, with smaller flocs resulting in higher resistant to G variations. These results are
 479 in agreement with the other strength indicator reported here (Table 1 and 2).

480 Moreover, despite of the differences between the two methods (PDA and image analysis), results
 481 indicate that the parameter d , derived from the non-intrusive image analysis, and SF , obtained
 482 from the PDA signal, behaved in similar way, with R^2 values near to 0.80 for Al-Humic and 0.60
 483 for Al-Kaolin.

484 The lower R^2 value for Al-Kaolin is believed to be attributed to the different scattering area, as
 485 previously discussed. However, this does not explain why SF for Al-Humic and Al-Kaolin

493 behaved with no significant difference (p-value over 0.05), when exposed to rupture shear rate of
 494 800 s^{-1} . A possible explanation is that flocs formed from sweep coagulation mechanism are
 495 bigger than those formed from charge neutralization and their physical properties are likely
 496 determined by coagulant only, as pointed out by Yu *et al.* (2015). Besides, floc characteristic size
 497 was calculated based on the average of longest length, and so, it is expected that large flocs are
 498 more prone to breakage by fragmentation when exposed to micro-scale dissipating eddies, thus
 499 resulting in similar strength for Al-Humic and Al-Kaolin aggregates.



494 a) Figure 8. Relationship between SF and d : (a) water type 1 – Al-Humic and (b) water type 2 – Al-
 496 Kaolin.
 497

497 4. Conclusions

405 Floc size and strength play an important role in separation processes used in water and
 406 wastewater treatment, and the influence of different primary particles on the floc strength is still
 407 poorly understood. The evidence that aggregates resistance is invariable with particles when
 408 sweep coagulation is applied needs to be further investigated. Here, two aggregates formed by
 409 Al-Humic and Al-Kaolin during flocculation were investigated using two techniques, namely
 410 intrusive photometric dispersion analyser and non-intrusive image system. Both techniques were
 411 applied to determine three floc strength indexes: the strength factors (SF), the local stress (σ) and
 412 floc strength coefficient (γ). The main conclusions of this work are:

506

- 508 1. For Al-Humic and Al-Kaolin flocs, the strength factors (SF) and the local stress (σ) have
 509 a positive variation in response to the increase of G because the high shear forces select

508 the strongest bonds within the aggregates. This means that higher G produces more
509 resistant aggregates, however the size dependence for an individual separation process
510 efficiency must be considered.

511 2. The comparison between the aggregates strength for Al-Humic acid and Al-Kaolin using
512 floc strength coefficient (γ) indicates that both aggregates have nearly the same resistance,
513 possible due to the precipitate hydroxide of alum mostly influencing floc size and
514 strength. This finding reinforces the perspective that particles within a floc may have
515 slight, or even no influence, on the floc strength when sweep coagulation is applied.

516 3. The intrusive photometric dispersion analyser and non-intrusive image-based system used
517 in this study produced well correlated parameters, with a similar behaviour. However, the
518 non-intrusive image method proved to be more reliable, as images are not influenced by
519 the optical characteristics of the flocs.

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