Long-term behaviours of railway prestressed concrete sleepers due to shortening parameters
Li, Dan; Kaewunruen, Sakdirat; Robery, Peter; Remennikov, Alex

License: Creative Commons: Attribution (CC BY)

Document Version
Publisher's PDF, also known as Version of record

Citation for published version (Harvard):

Link to publication on Research at Birmingham portal

General rights
Unless a licence is specified above, all rights (including copyright and moral rights) in this document are retained by the authors and/or the copyright holders. The express permission of the copyright holder must be obtained for any use of this material other than for purposes permitted by law.

• Users may freely distribute the URL that is used to identify this publication.
• Users may download and/or print one copy of the publication from the University of Birmingham research portal for the purpose of private study or non-commercial research.
• Users may use extracts from the document in line with the concept of ‘fair dealing’ under the Copyright, Designs and Patents Act 1988 (?)
• Users may not further distribute the material nor use it for the purposes of commercial gain.

Where a licence is displayed above, please note the terms and conditions of the licence govern your use of this document.

Take down policy
While the University of Birmingham exercises care and attention in making items available there are rare occasions when an item has been uploaded in error or has been deemed to be commercially or otherwise sensitive.

If you believe that this is the case for this document, please contact UBIRA@lists.bham.ac.uk providing details and we will remove access to the work immediately and investigate.
LONG-TERM BEHAVIOURS OF RAILWAY PRESTRESSED CONCRETE SLEEPERS DUE TO SHORTENING PARAMETERS

Dan Li¹, Sakdirat Kaewunruen¹,², Peter Robery¹ and Alex M Remennikov³

¹ Department of Civil Engineering, the University of Birmingham, U.K.
² Birmingham Centre for Railway Research and Education, the University of Birmingham, U.K
³ School of Civil, Mining and Environmental Engineering, University of Wollongong, Australia

ABSTRACT

Long-term behaviours of railway prestressed concrete sleepers are critical parameters in determining durability and performance functions required for predictive maintenance management. The time-dependent behaviours vary largely due to their creep, shrinkage and elastic shortening responses. Many investigators in the past have proposed various material models to predict shortening effects but those were mostly applied to general reinforced concrete members. In contrast, prestressed concrete design has adopted those models for predicting the structural behaviour of prestressed concrete structures such as long span bridges, stadiums, silos and confined nuclear power plants, etc. Such the constitutive models have led to a concern of practitioners whether those existing predictive models could be realistically applied to prestressed concrete. Due to high initial elastic shortening in prestressed concrete, the creep and shrinkage effects should be critically re-evaluated in flexural members. This paper presents a comparative investigation using a variety of methods to evaluate shortening effects in railway prestressed concrete sleepers. Three common design codes have been considered, including European Standard EUROCODE2, American Standard ACI and Australian Standard AS3600-2009. The study results show that EUROCODE2 and AS3600 are very coherent and consistent. It also shows that ACI code will need to be revised to take into account various environmental factors. The insight of this study will help rail track engineers to improve predictive maintenance model of railway infrastructure and to minimise time spent on inspection activities, which are critical part of asset operations.

Keywords: railway, prestressed concrete, sleepers, long-term behaviour, shortening effects.

1. INTRODUCTION

Rail transport first appeared in 1820s which was critical to the Industrial Evolution and the development of economies. Nowadays, railway transportation system has become very important for both of passengers and freight transportation. It provides a highly enjoyable ride for passengers or freight. With railway technology developing dramatically, high-speed trains have been designed for long distance transportation. The speed of fastest train, Shanghai Maglev (China), is up to 430km/h. In addition, larger capacity for heavy-haul trains is required in freight transportation.
Therefore, the rail track structure must meet current design requirements for geometry, strength and load capacity to ensure safe and stable trip. Conventional or ballasted track can be divided into superstructure and substructure. The superstructure consists of rails, rail pads, sleepers, fastening system. The substructure includes ballast, sub-ballast and formation. Railway sleepers (or called ‘railroad ties’ in North America) are the main element of rail track structure. The main functions of railway sleepers are:

1. To support rail and maintain the track gauge.
2. To distribute loads to substructure.

Materials employed in sleepers can be timber, steel, concrete and any other engineered materials. Prestressed concrete sleepers are most commonly used type of sleeper around world (Taherinezhad, J. et al. 2013). Prestressed concrete sleepers have been developing for decades with long life cycle, low maintenance cost and good structural performance in comparison with reinforced concrete sleepers. Prestressed concrete sleepers are expected to withstand high dynamic loads and harsh environments. However, concrete structure, owing to its material property, is deforming with time which is risky from creep and shrinkage. Time-dependent behaviours can result in deformation, crack and loss of prestress to cause potential risks for trains using the sleepers. Therefore, prediction of time-dependent behaviours becomes essential when considering serviceability limit state (Byle, K. 1998, Razak, H. 1986, Taherinezhad, J. et al. 2013). This paper presents design considerations for estimating the long-term behaviour of prestressed concrete sleepers. In addition, three design (Eurocode 2, ACI and AS3600-2009) methods will be used to compare.

2. PREDICTING TIME-DEPENDENT BEHAVIOURS

2.1. Creep Prediction

The concrete under load that strain increases with time is due to creep. Therefore, creep can be defined as the increase in strain under the sustained stress and it can be several times as large as the initial strain (Bhatt, P. 2011). If the load is removed, the strain decreases immediately due to elastic recovery and a gradual incomplete recovery due to creep. This behaviour is shown in Figure 1. When creep is taken into account, its design effects are always evaluated under quasi-permanent combination of actions irrespective of the design situation considered, i.e. persistent, transient or accidental.
2.1.1. Eurocode 2

The total creep strain $\varepsilon_{cc}(\infty, t_0)$ of concrete due to the constant compressive stress of $\sigma_c$ applied at the concrete age of $t_0$ is given by:

$$\varepsilon_{cc}(\infty, t_0) = \varphi(\infty, t_0) \times \frac{\sigma_c}{E_c}$$

Where $(\infty, t_0)$ is the final creep coefficient, which the value of $\sigma_c$ does not exceed $0.45f_{ck}(t_0)$. $E_c$ is the tangent modulus.

$$\varphi(\infty, t_0) = \varphi_{RH} \times \frac{16.8}{\sqrt{f_{cm}}} \times \frac{1}{(0.1 + t_0^{0.2})}$$

$$\varphi_{RH} = 1 + \frac{1 - 0.01 \times RH}{0.1 + f_{cm}^{0.333}}, \quad f_{cm} \leq 35MPa$$

$$\varphi_{RH} = (1 + \frac{1 - 0.01 \times RH}{0.1 + f_{cm}^{0.333} - \alpha_1})\alpha_2, \quad f_{cm} > 35MPa$$

$$\alpha_1 = (\frac{35}{f_{cm}})^{0.7}, \quad \alpha_1 = (\frac{35}{f_{cm}})^{0.2} \quad f_{cm} = f_{ck} + 8MPa$$

$$t_0 = t_0,\alpha(\frac{9}{2 + t_0^{1.2}} + 1)^{\alpha} \geq 0.5,$$

$$\alpha = \{-1(S), 0(N), 1(R)\}$$
Where: RH = relative humidity in %, \( h_0 = 2A_c/u \) mm, \( A_c \) = cross sectional area, \( u \) = perimeter of the member in contact with the atmosphere, \( S, R \) and \( N \) refer to different classes of cement.

### 2.1.2. ACI

According to ACI 209-92, the predicted parameter is creep coefficient \( \varphi(t, t_0) \) and the equation is given by:

\[
\varphi(t, t_0) = \frac{(t - t_0) \psi}{d + (t - t_0) \psi} \varphi_u
\]

(6)

where \( \varphi(t, t_0) \) is creep coefficient at any time \( t \) when a load applied at age \( t_0 \).

\( d \) (days) and \( \psi \) are considered constants for a given member shape and size that define the time-ratio part. ACI-209R-92 recommends an average value of 10 and 0.60 for \( d \) and \( \psi \) respectively.

\( \varphi_u \) is the ultimate creep coefficient.

For the ultimate coefficient \( \varphi_u \), the average value is given:

\[
\varphi_u = 2.35
\]

(7)

According to ACI-209R-92, the creep coefficient \( \varphi_u \) needs to be modified by correction factors. Therefore, \( \varphi_u \) should be multiplied by six factors.

\[
\varphi_u = 2.35\gamma_c
\]

(7)

\[
\gamma_c = \gamma_{c,t0}\gamma_{c,RH}\gamma_{c,vs}\gamma_{c,s}\gamma_{c,\psi}\gamma_{c,\alpha}
\]

(8)

Where

\( \gamma_{c,t0} = \) loading age coefficient

\( \gamma_{c,RH} = \) ambient relative humidity coefficient

\( \gamma_{c,vs} = \) the volume to surface ratio of the concrete section coefficient

\( \gamma_{c,s} = \) slump coefficient

\( \gamma_{c,\psi} = \) fine aggregate coefficient

\( \gamma_{c,\alpha} = \) air content coefficient

### 2.1.3. Australian Standard 3600-2009

The creep coefficient at any time \( \varphi_{cc} \) can be determined by:

\[
\varphi_{cc} = k_2k_3k_4k_5\varphi_{cc,b}
\]

(9)
Where \( k_2 \) is the development of creep with time; \( k_3 \) is the factor which depends on the age at first loading \( \tau \) (in days); \( k_4 \) is the factor which accounts for the environment; and \( k_5 \) is the factor which accounts for the reduced influence of both relative and humidity and specimen size.

### 2.2. Shrinkage prediction

Bhatt, P (2011) stated that both of creep and shrinkage are influenced by the same parameters. Shrinkage is not an entirely reversible process like creep and it can be also influenced by relative humidity, surface exposed to atmosphere, compressive strength of concrete and types of cement.

#### 2.2.1. Eurocode 2

The total shrinkage strain \( \varepsilon_{cs} \) can be given by:

\[
\varepsilon_{cs} = \varepsilon_{ds} + \varepsilon_{as}
\]  

(10)

Where \( \varepsilon_{ds} \) is drying shrinkage strain; and \( \varepsilon_{as} \) is autogenous shrinkage strain.

#### 2.2.2. ACI

The shrinkage strain \( \varepsilon_{sh}(t, t_c) \) at age of concrete \( t \) (days), predicted from the start of drying at \( t_c \) can be calculated by:

\[
\varepsilon_{sh}(t) = \frac{(t - t_c)^\alpha}{f + (t - t_c)^\alpha} \varepsilon_{shu}
\]  

(11)

\[
\varepsilon_{shu} = 780 \times 10^{-6} \text{ mm/mm (in/in)}
\]

Where \( f \) (in days) and \( \alpha \) are considered constants for a given member shape and size that define the time-ratio factor

- \( \varepsilon_{shu} \) is ultimate shrinkage strain
- \( (t - t_c) \) is the time between end of curing and any time after curing

#### 2.2.3. Australian Standard 3600-2009

The total shrinkage strain \( \varepsilon_{cs} \) is shown below:

\[
\varepsilon_{cs} = \varepsilon_{csa} + \varepsilon_{csd}
\]  

(12)

Where \( \varepsilon_{csa} \) is autogenous shrinkage strain; \( \varepsilon_{csd} \) is drying shrinkage strain.

### 3. SLEEPER DETAILS

The effects of shortening and approximate deflections for estimating creep, shrinkage strain will be evaluated. The fundamental engineering properties of prestressed concrete sleeper used for
calculation are based on previous research by Remennikov et al. The results are generated for comparisons between Eurocode 2 (EC2) and Australian standard 3600-2009 (AS). Figure 2 shows the cross section at rail seat of the prestressed concrete sleepers. The parameters of prestressed concrete sleeper are shown below (Kaewunruen. S et al., 2011):

1. Sleeper length: 2700mm
2. Track gauge: 1600mm
3. Prestressing nominal force: 550kN

![Cross section of railway sleepers](image)

**Figure 2: Cross section of railway sleepers**

The case is estimated for 18250 days (50 years) in same conditions (uniform dimension of sleepers, 70% relative humidity, steam curing)

4. RESULTS AND DISCUSSIONS

4.1. Creep Shortening

To investigate creep shortening, the 7 cases have been analysed using different characteristic strength (20MPa, 25MPa, 32MPa, 40MPa, 55MPa, 65MPa, 80MPa), which are plotted in Figure 3. The data of creep shortening are calculated by EC2 and AS codes respectively. All the cases are estimated from 1 day up to 18250 days (50 years) in the same conditions (uniform dimension of sleepers, 70% relative humidity, steam curing etc.).

![Creep shortening in EC2 and AS](image)

**Figure 3: creep shortening**
4.2. Shrinkage Shortening

Figure 4 shows 7 cases of different strength of prestressed concrete sleepers on the shrinkage effect. The data of shrinkage shortening are calculated by EC2 and AS3600-2009 codes respectively.

![Figure 4: shrinkage shortening](image)

Based on the sensitive analysis, we found that long-term performance in prestressed concrete sleeper depends on various factors. According to obtained data, the shortening depends on strain, which means large strain leads to more shortening in prestressed concrete sleeper. Previous research had stated that the higher strength of concrete has less loss of prestress and concrete strength less than 25MPa was not suitable for use in prestressed concrete sleepers (Li, D et al., 2016). Figure 3 and Figure 4 indicate total long-term shortening (due to creep and shrinkage), which higher strength of concrete has less shortening. However, in initial period, higher strength has more shortening than lower strength concrete due to autogenous shrinkage. The ACI results haven’t shown on this paper because both of creep or shrinkage calculation doesn’t directly relate to concrete strength.

5. CONCLUSIONS

In practice, the use of the railway infrastructure system rapidly increased, which means time-dependent behaviour could have more significant influence for deformation of components. When shortening and deflection occur in prestressed concrete sleepers, the track gauge could change with shortening and deflections. It is hazard that train derails because of track gauge change. Furthermore, there are many other factors to affect prestressed concrete sleepers shortening and deflections like relative humidity, curing conditions, age at first loading, temperature, abrasion etc. In this paper, Eurocode 2 and AS3600-2009 are used in predicting creep and shrinkage shortening and deflection. Comparison between design codes provides the insight into long-term performance of prestressed concrete sleepers. This paper presents shortening and deflections due to creep and shrinkage. It will improve the rail maintenance and inspection criteria in order to establish appropriate sensible remote track condition monitor network in practice.
6. ACKNOWLEDGMENTS

The authors would also like to thank British Department of Transport (DfT) for Transport - Technology Research Innovations Grant Scheme, Project No. RCS15/0233; and the BRIDGE Grant (provided by University of Birmingham and the University of Illinois at Urbana Champaign). The last author is gratefully acknowledge the Japan Society for the Promotion of Science (JSPS) for his JSPS Invitation Research Fellowship (Long-term), Grant No L15701, at Track Dynamics Laboratory, Railway Technical Research Institute and at Concrete Laboratory, the University of Tokyo, Tokyo, Japan. The authors are sincerely grateful to European Commission for the financial sponsorship of the H2020-RISE Project No. 691135 “RISEN: Rail Infrastructure Systems Engineering Network,” which enables a global research network that tackles the grand challenge in railway infrastructure resilience and advanced sensing in extreme environments (www.risen2rail.eu). We would also like to acknowledge the support from European Cooperation in Science and Technology (EU-COST) Action: TU1404 Towards the next generation of standards for service life of cement-based materials and structures.

7. CITATIONS AND REFERENCES

American Concrete Institute (2005) Building code requirements for structural concrete (ACI 318-05) and commentary (ACI 318R-05): [an ACI standard]. 2nd edn. Farmington Hills, MI: American Concrete Institute.


Han, W.W and Lü, Y.G, (2016) Experimental research on prediction model of concrete shrinkage and creep, Journal of Central South University (Science and Technology) 2016, 47(10)


