

1 **Global Assessment of the SMAP Level-4 Surface and Root-Zone Soil Moisture Product**  
2 **Using Assimilation Diagnostics**  
3

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34 **Abstract**

35 The Soil Moisture Active Passive (SMAP) mission Level-4 Soil Moisture (L4\_SM) product  
36 provides 3-hourly, 9-km resolution, global estimates of surface (0-5 cm) and root-zone (0-100  
37 cm) soil moisture and related land surface variables from 31 March 2015 to present with ~2.5-  
38 day latency. The ensemble-based L4\_SM algorithm assimilates SMAP brightness temperature  
39 (Tb) observations into the Catchment land surface model. This study describes the spatially  
40 distributed L4\_SM analysis and assesses the observation-minus-forecast (O-F) Tb residuals and  
41 the soil moisture and temperature analysis increments. Owing to the climatological rescaling of  
42 the Tb observations prior to assimilation, the analysis is essentially unbiased, with global mean  
43 values of ~0.37 K for the O-F Tb residuals and practically zero for the soil moisture and  
44 temperature increments. There are, however, modest regional (absolute) biases in the O-F  
45 residuals (under ~3 K), the soil moisture increments (under ~0.01 m<sup>3</sup> m<sup>-3</sup>), and the surface soil  
46 temperature increments (under ~1 K). Typical instantaneous values are ~6 K for O-F residuals,  
47 ~0.01 (~0.003) m<sup>3</sup> m<sup>-3</sup> for surface (root-zone) soil moisture increments, and ~0.6 K for surface  
48 soil temperature increments. The O-F diagnostics indicate that the actual errors in the system are  
49 overestimated in deserts and densely vegetated regions and underestimated in agricultural  
50 regions and transition zones between dry and wet climates. The O-F auto-correlations suggest  
51 that the SMAP observations are used efficiently in western North America, the Sahel, and  
52 Australia, but not in many forested regions and the high northern latitudes. A case study in  
53 Australia demonstrates that assimilating SMAP observations successfully corrects short-term  
54 errors in the L4\_SM rainfall forcing.

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56 **1. Introduction**

57 Soil moisture plays an important role in the water, energy and carbon cycles (e.g., Seneviratne et  
58 al. 2010) and is considered an essential climate variable by the World Meteorological  
59 Organization (WMO 2006). The radiometer instrument onboard the NASA Soil Moisture Active  
60 Passive (SMAP) satellite mission (Entekhabi et al. 2010; Piepmeier et al. 2017) observes the L-  
61 band (1.4 GHz) microwave radiation emitted from the Earth's surface. Over land, the observed  
62 radiances (or brightness temperatures; or Tbs) are sensitive to the moisture in the top few  
63 centimeters of the soil, provided the overlying vegetation is not too dense (Jackson and  
64 Schmugge 1991; Entekhabi et al. 2014). This sensitivity is exploited in the SMAP Level-4 Soil  
65 Moisture (L4\_SM) algorithm to obtain estimates of surface (0-5 cm) and root-zone (0-100 cm)  
66 soil moisture (Reichle et al. 2014b, 2017b). Specifically, the ensemble-based L4\_SM algorithm  
67 assimilates the SMAP Tb observations into the NASA Catchment land surface model (Koster et  
68 al. 2000), and the resulting L4\_SM product consists of 3-hourly, 9-km resolution, global  
69 estimates of soil moisture and related land surface variables with complete coverage. These  
70 estimates are available from 31 March 2015 to present with a mean latency of ~2.5 days from the  
71 time of the SMAP observations.

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73 Reichle et al. (2017b) validated the L4\_SM soil moisture estimates against in situ measurements  
74 from SMAP core validation sites, which provide spatially averaged soil moisture measurements  
75 (at the grid-cell scale of the model and of the satellite estimates) for about a dozen distinct  
76 watersheds. They determined that the unbiased RMSE (ubRMSE, or standard deviation of the  
77 error) for L4\_SM surface (root-zone) soil moisture estimates is  $0.038 \text{ m}^3 \text{ m}^{-3}$  ( $0.030 \text{ m}^3 \text{ m}^{-3}$ ) at  
78 the 9-km scale and  $0.035 \text{ m}^3 \text{ m}^{-3}$  ( $0.026 \text{ m}^3 \text{ m}^{-3}$ ) at the 36-km scale. The L4\_SM product thus

79 meets its soil moisture accuracy requirement, which was specified prior to launch as an ubRMSE  
80 of  $0.04 \text{ m}^3 \text{ m}^{-3}$  or better (excluding regions of snow and ice, frozen ground, mountainous  
81 topography, open water, urban areas, and vegetation with water content greater than  $5 \text{ kg m}^{-2}$ ).  
82 Moreover, the L4\_SM estimates improve (significantly at the 5% level for surface soil moisture)  
83 over model-only estimates, which do not benefit from the assimilation of SMAP Tb observations  
84 and have a 9-km surface (root-zone) ubRMSE of  $0.042 \text{ m}^3 \text{ m}^{-3}$  ( $0.032 \text{ m}^3 \text{ m}^{-3}$ ) (Reichle et al.  
85 2017b). Furthermore, Reichle et al. (2017b) corroborated these results with other metrics,  
86 including time series correlations, and through validation against point-scale in situ  
87 measurements from ~400 sparse network sites, which represent a greater variety of climate and  
88 land cover conditions. Moreover, Crow et al. (2017) demonstrated for the south-central US that  
89 the assimilation-based L4\_SM soil moisture estimates have significantly improved utility for  
90 forecasting the streamflow response to future rainfall events (relative to that of soil moisture  
91 retrievals from L-band and higher-frequency Tb observations).

92  
93 Validation versus in situ measurements is an important step in the assessment of any data  
94 product that is based on satellite measurements and numerical modeling. For soil moisture,  
95 however, the available in situ measurements are limited to a relatively small number of locations  
96 (compared to the ~1.6 million land grid cells of the L4\_SM product) and do not fully represent  
97 the tremendous variety of land cover, soil, and climate conditions encountered across the global  
98 land area. It is therefore important to supplement the in situ validation of the L4\_SM product  
99 with additional assessments that provide a more global perspective. The key objective of the  
100 present paper is to offer this global evaluation perspective for the L4\_SM product. This is  
101 accomplished by investigating a variety of this product's data assimilation diagnostics, including

102 statistics of the observation-minus-forecast (O-F) Tb residuals, the observation-minus-analysis  
103 (O-A) Tb residuals, and the analysis-minus-forecast soil moisture differences (or increments).  
104 These diagnostics provide important information about the internal consistency of the  
105 assimilation system and the impact of the assimilated observations (Gelb 1974). Perhaps most  
106 importantly, the assimilation diagnostics are available wherever and whenever SMAP  
107 observations are assimilated and therefore have a much greater coverage in space and time than  
108 in situ soil moisture measurements.

109

110 There is a long history of using assimilation diagnostics to assess the performance of  
111 atmospheric assimilation systems (Hollingsworth and Lönnberg 1989; Daley 1992; Desroziers et  
112 al. 2005; Todling 2013). Assimilation diagnostics have also been used extensively in land data  
113 assimilation. For example, O-F residuals were used to assess whether the assumed error  
114 characteristics are consistent with actual errors (e.g., Reichle et al. 2002a; De Lannoy and  
115 Reichle 2016a,b), construct adaptive filtering approaches (Crow and Reichle 2008; Reichle et al.  
116 2008), tune the input error parameters (Crow and van den Berg 2010), and dynamically estimate  
117 and correct for bias (Draper et al. 2015). Furthermore, an investigation of the analysis  
118 increments demonstrated the progress made in revising the soil moisture analysis of the  
119 Integrated Forecasting System at the European Centre for Medium-Range Weather Forecasts  
120 (Drusch et al. 2009; de Rosnay et al. 2013).

121

122 This paper is organized as follows. Following a brief overview of the L4\_SM system and data  
123 product (section 2a), we describe the ensemble-based data assimilation algorithm (section 2b)  
124 and assimilation diagnostics (section 2c). Thereafter, our results address the global climatology

125 of the L4\_SM soil moisture estimates (section 3a) and illustrate the L4\_SM analysis with a case  
126 study in Australia (section 3b). Next, we investigate the observation counts (section 3c), the O-  
127 F Tb residuals (section 3d), and the soil moisture and temperature increments (section 3e). A  
128 summary and conclusions are provided in section 4.

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## 139 **2. L4\_SM Data Product and Algorithm**

140 A short overview of the Version 2 L4\_SM product and algorithm is provided in Reichle et al.  
141 (2017b). In this section, we briefly summarize the key aspects of the L4\_SM modeling system  
142 and data product following their text. Thereafter, we provide a more detailed discussion than  
143 Reichle et al. (2017b) of the L4\_SM analysis and assimilation diagnostics. This more detailed  
144 discussion is adapted from Reichle et al. (2014b) and De Lannoy and Reichle (2016a,b).

145

### 146 *a. Overview*

147 The L4\_SM algorithm, shown schematically in Figure 1 of Reichle et al. (2017b), is a  
148 customized version of the ensemble-based land data assimilation component of the Goddard  
149 Earth Observing System, version 5 (GEOS-5), modeling and assimilation system. This  
150 component is built around the Catchment land surface model (hereinafter “Catchment model”;  
151 Koster et al. 2000; Ducharne et al. 2000). Besides the surface meteorological forcing data (see  
152 below), the key drivers of the L4\_SM system are the 36-km resolution SMAP Level-1C Tb  
153 observations (Chan et al. 2016). The assimilated SMAP observations include horizontal-  
154 polarization (H-pol) and vertical-polarization (V-pol) Tbs from ascending and descending half-  
155 orbits (after first averaging over fore- and aft-looking Tbs). These observations are merged  
156 every three hours with the model estimates in a soil moisture and temperature analysis that uses a  
157 spatially distributed ensemble Kalman filter (EnKF; section 2b).

158

159 The Catchment model used in the L4\_SM algorithm includes an explicit treatment of the spatial  
160 variation of soil water and water table depth within each 9-km grid cell based on the statistics of  
161 the watershed topography. Furthermore, the snow pack is simulated in a three-layer snow model

162 component that tracks the evolution of the snow water equivalent, snow depth, and snow heat  
163 content (Stieglitz et al. 2001). The surface meteorological forcing data used in the L4\_SM  
164 algorithm are from the GEOS-5 operational forward-processing (FP) system at  $0.25^\circ \times 0.3125^\circ$   
165 (latitude  $\times$  longitude) resolution (Lucchesi 2013a). The GEOS-5 precipitation data are corrected  
166 using daily, gauge-based precipitation observations from the NOAA Climate Prediction Center  
167 Unified (CPCU) product (Reichle and Liu 2014; Reichle et al. 2017b). These precipitation  
168 corrections are applied globally except in Africa, where no corrections are applied, and in the  
169 high latitudes, where corrections are linearly tapered between  $42.5^\circ$  and  $62.5^\circ$  latitude (in both  
170 Hemispheres) and no corrections are applied poleward of  $62.5^\circ$  latitude. The Catchment model  
171 is supplemented with a zero-order “tau-omega” radiative transfer model (De Lannoy et al. 2013,  
172 2014) that converts the Catchment model soil moisture and temperature estimates into estimates  
173 of L-band Tbs, which are required for the radiance-based L4\_SM soil moisture analysis. See  
174 Reichle et al. (2017b) and references therein for details about the Catchment and radiative  
175 transfer model configuration, parameters, and forcing data.

176

177 The L4\_SM data are generated and distributed on the global, cylindrical, 9-km Equal-Area  
178 Scalable Earth, version 2 (EASEv2), grid (Brodzik et al. 2012). The L4\_SM outputs include soil  
179 moisture estimates for the “surface” (0-5 cm), “root-zone” (0-100 cm) and “profile” (0 cm to  
180 depth of bedrock) layers, along with a large number of related land surface variables, including  
181 surface (skin) temperature, soil temperature (in 6 layers down to  $\sim 13$  m depth), snow mass, land  
182 surface fluxes, surface meteorological forcing data, assimilation diagnostics, land model  
183 parameters, and error estimates for soil moisture and surface temperature (Reichle et al. 2015a).  
184 The L4\_SM surface (layer-1) soil temperature estimates are for the 0-10 cm layer except for



185 tropical (broadleaf evergreen) forests, where the surface soil temperature is for the 5-15 cm layer.  
186 The layer thickness associated with the overlying land skin temperature is thus negligible except  
187 for tropical forests, where the L4\_SM skin temperature represents the average temperature of the  
188 canopy and the 0-5 cm soil layer.

189

190 In this paper we use L4\_SM Version 2 data (Science Version ID: Vv2030) for the 2-year period  
191 from April 2015 to March 2017. Specifically, we use 3-hourly, instantaneous “forecast” and  
192 “analysis” soil moisture and temperature fields along with the corresponding Tb observations,  
193 forecasts, analysis, and error estimates from the “analysis update” files (Reichle et al. 2016a).  
194 We further use surface soil moisture, root-zone soil moisture, snow mass and precipitation  
195 estimates from the 3-hourly time-average “geophysical” files (Reichle et al. 2016b). Note that  
196 the latter files also provide many other land surface fields. Finally, time-invariant land model  
197 parameters (including soil porosity and wilting point) are available in the “land-model-constants”  
198 file (Reichle et al. 2016c). See Reichle et al. (2015a) for additional details about data product  
199 specifications.

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#### 202 *b. Assimilation algorithm*

203 The L4\_SM algorithm is built on the EnKF – a Monte-Carlo variant of the Kalman filter  
204 (Evensen 2003). The idea behind the EnKF is that a small ensemble of model trajectories  
205 captures the relevant parts of the model forecast error structure. Each member of the ensemble  
206 experiences perturbed instances of the surface meteorological forcing fields (representing errors  
207 in the forcing data) and/or randomly generated noise that is added to the model parameters and

208 prognostic variables (representing errors in model physics and parameters). The error covariance  
 209 matrices that are required for the filter update can then be diagnosed from the spread of the  
 210 ensemble at the update time. Its relative ease of implementation made the EnKF a popular  
 211 choice for land data assimilation (Reichle et al. 2002a,b; Andreadis and Lettenmaier 2006; Pan  
 212 and Wood 2006; Zhou et al. 2006; Durand and Margulis 2008; Hendricks Franssen et al. 2008;  
 213 Kumar et al. 2008; Lahoz and De Lannoy 2014; Carrera et al. 2015; Reichle et al. 2014a; Kurtz  
 214 et al. 2016).

215  
 216 The EnKF works sequentially by performing in turn a model forecast and a filter update. Its  
 217 implementation for the L4\_SM algorithm is shown schematically in Figure 1 of De Lannoy and  
 218 Reichle (2016b), except that – for the L4\_SM system discussed here – the model is on the 9-km  
 219 grid and the assimilated SMAP observations are only available for a single, 40° incidence angle.  
 220 Formally, the forecast step using the land surface model  $\mathbf{f}(\bullet)$  can be written as

221  
 222 
$$\mathbf{x}_t^{j-} = \mathbf{f}(\mathbf{x}_{t-1}^{j+}, \mathbf{w}_t^j), \tag{1}$$

223  
 224 where  $\mathbf{x}_t^{j-}$  and  $\mathbf{x}_{t-1}^{j+}$  are the forecast (denoted with  $-$ ) and analysis (denoted with  $+$ ) state vectors  
 225 at times  $t$  and  $t-1$ , respectively, of the  $j$ -th ensemble member. The model error (or perturbation  
 226 vector) is denoted with  $\mathbf{w}_t^j$ . Each ensemble member represents a particular realization of the  
 227 possible model trajectories with perturbations in model prognostic and forcing variables. The  
 228 EnKF state vector is at 9-km resolution and consists of the Catchment model prognostic  
 229 variables for soil moisture (surface excess, root-zone excess, and catchment deficit), skin

230 temperature, and surface (layer-1) soil heat content. The latter is the Catchment model  
 231 prognostic variable from which the surface soil temperature is diagnosed.

232

233 With the observations available at time  $t$ , the state vector of each ensemble member is updated to  
 234 new values. To this end, the filter update produces increments  $\Delta \mathbf{x}_t^j$  at time  $t$  that can be written  
 235 as

236

$$237 \quad \Delta \mathbf{x}_t^j = \mathbf{K}_t ( \mathbf{y}_t^j - \mathbf{h}(\mathbf{x}_t^{j-}) ), \quad (2)$$

238

239 where  $\mathbf{y}_t^j$  denotes the (suitably perturbed) vector of Tb observations (Burgers et al. 1998) and  
 240  $\mathbf{h}(\bullet)$  is the observation operator that converts the 9-km soil moisture and temperature state  
 241 estimates into model estimates of Tb at the coarser resolution of the SMAP observations. The  
 242 analyzed state vector is obtained as  $\mathbf{x}_t^{j+} = \mathbf{x}_t^{j-} + \Delta \mathbf{x}_t^j$ . As expressed in equation (2), the Kalman  
 243 gain matrix  $\mathbf{K}_t$  maps the coarser-resolution observational information, expressed in the O-F  
 244 residuals (i.e.,  $\mathbf{y}_t^j - \mathbf{h}(\mathbf{x}_t^{j-})$ ), onto the model state increments  $\Delta \mathbf{x}_t^j$  at 9-km resolution. The  
 245 Kalman gain is given by

246

$$247 \quad \mathbf{K}_t = \text{Cov}( \mathbf{x}_t^-, \mathbf{h}(\mathbf{x}_t^-) ) [ \text{Cov}( \mathbf{h}(\mathbf{x}_t^-), \mathbf{h}(\mathbf{x}_t^-) ) + \mathbf{R}_t ]^{-1}, \quad (3)$$

248

249 where the forecast error (cross-)covariances  $\text{Cov}(\bullet)$  are diagnosed from the ensemble, and  $\mathbf{R}_t$  is  
 250 the observation error covariance (including contributions from instrument errors and errors of  
 251 representativeness). Simply put, the Kalman gain represents the relative weights given to the  
 252 model forecast and the observations based on their respective uncertainties and based on the

253 modeled error correlations between different elements of the state vector and the corresponding  
254 Tbs. Finally, the EnKF state estimate is given by the ensemble mean, and the reduction of the  
255 uncertainty resulting from the analysis update is reflected in the reduction of the ensemble  
256 spread.

257  
258 The EnKF updates in the L4\_SM algorithm are spatially distributed in the sense that all  
259 observations within a radius of  $1.25^\circ$  impact the analysis at a given 9-km grid cell (De Lannoy et  
260 al. 2016b; their section 3.1). The weight of an O-F residual towards the soil moisture  
261 (temperature) increments at a given 9-km grid cell is proportional to the modeled error  
262 correlations between the Tb at the observation location and the soil moisture (temperature) at the  
263 location of the increment (equation 3). Since this error correlation typically decays with  
264 increasing distance of the observation from the location of the increment, its sample-based  
265 estimate becomes noisier with increasing distance, which is addressed through a distance-based  
266 covariance localization approach using a Gaspari-Cohn function (Gaspari and Cohn 1999; De  
267 Lannoy and Reichle 2016a) with the above-mentioned compact support radius of  $1.25^\circ$ . The  
268 L4\_SM system uses 24 ensemble members. The perturbation parameters for the model forcing  
269 and prognostic variables match those of De Lannoy and Reichle (2016a; their Table 2) except  
270 that the spatial correlation scale for the perturbations of the model prognostic variables is set to  
271  $0.3^\circ$  (instead of  $0.5^\circ$ ) in the L4\_SM system. The observation error standard deviation is set to 4  
272 K, which includes  $\sim 1.3$  K instrument error and  $\sim 3.8$  K representativeness error (that is, error in  
273 the radiative transfer model and remapping associated with the observation operator  $\mathbf{h}(\bullet)$ )  
274 (Reichle et al. 2017b).

275

276 The Kalman gain of equation (3) is optimal (in the sense of minimum estimation error variance)  
277 only if the dynamic system (equation 1) is linear, if its model and observation error  
278 characteristics satisfy certain assumptions (including white and uncorrelated noise), and if the  
279 input error parameters are correctly specified (Gelb 1974). In this case, the EnKF estimate is  
280 mathematically the best possible estimate of the true state given the observations, the model  
281 prediction, and the estimated errors of both. But the L4\_SM land model and observation  
282 operator are not linear (Koster et al. 2000; De Lannoy et al. 2013), and the L4\_SM error  
283 characteristics further violate the above-mentioned assumptions. The L4\_SM analysis is  
284 therefore not optimal. Nevertheless, as mentioned above, the analysis estimates have proven  
285 superior to model-only estimates when both are validated against in situ measurements (Reichle  
286 et al. 2017b).

287  
288 To address seasonally varying bias in the modeled Tbs, the observations ( $y_t^j$ ) and model forecast  
289 ( $\mathbf{h}(\mathbf{x}_t^-)$ ) of equation (2) are taken to be the anomalies of the SMAP and modeled Tbs from their  
290 respective long-term mean seasonal cycles. The seasonal cycle of the SMAP Tbs was estimated  
291 from SMOS (version-5) Tb observations for the period July 2010 to June 2014. The seasonal  
292 cycle of the modeled Tbs was estimated from a model-only simulation of the L4\_SM system for  
293 the same period. For details of this rescaling procedure, see section 3b and Figures 1 and 2 of  
294 (De Lannoy and Reichle 2016a) and section 2d of (Reichle et al. 2017b).

295  
296 *c. Assimilation diagnostics*

297 The L4\_SM system generates a variety of useful internal algorithm diagnostics that are available  
298 wherever and whenever SMAP observations are assimilated (see also Reichle et al. 2015b; their

299 Appendix B). Most importantly, the Tb forecasts generated by the model within the cycling  
300 assimilation system are repeatedly confronted with the assimilated observations as part of the  
301 analysis (equation 2). This routine evaluation of model estimates against the assimilated  
302 observations is primarily reflected in the ensemble mean O-F Tb residuals (i.e.,  $\mathbf{y}_t - \mathbf{h}(\mathbf{x}_t^-)$ ).

303  
304 In an optimally calibrated, linear system that satisfies the usual error assumptions (section 2b),  
305 the (ensemble mean) O-F residuals are a zero-mean, white noise sequence, thereby reflecting an  
306 unbiased analysis that extracts all of the information from the observations (Gelb 1974). As  
307 already mentioned above (section 2b), the L4\_SM analysis is not strictly optimal, but it is still  
308 interesting to know how close to optimal the system operates in any given region. When the  
309 lagged auto-correlations of the O-F residuals are small and consistent with white noise, the  
310 system is nearly optimal and has extracted most of the available information from the  
311 observations (Daley 1992). Conversely, when the lagged auto-correlations are not small, then  
312 the observations are not being used efficiently (Daley 1992). The sample auto-correlation  
313 estimates presented below are based on the asymptotically unbiased estimator (Jenkins and Watts  
314 1968; their equation 5.3.25). Four sets of sample auto-correlations were computed, separately  
315 for H-pol and V-pol O-F residuals from ascending and descending half-orbits, and then averaged  
316 across the four sets. Auto-correlations were computed at a given location only if a total of at  
317 least 80 lagged data pairs were available.

318  
319 Moreover, the standard deviation of the O-F residuals is a measure of the typical (absolute)  
320 difference between a model forecast Tb and the corresponding (rescaled) SMAP observation. In  
321 an optimally calibrated system, the covariance of the O-F residuals should thus equal the sum of

322 the covariances of the model forecast and observation errors (Reichle et al. 2002a; Desroziers et  
323 al. 2005), that is,

324

$$325 \quad \text{Cov}(\mathbf{y}_t - \mathbf{h}(\mathbf{x}_t^-)) = \text{Cov}(\mathbf{h}(\mathbf{x}_t^-), \mathbf{h}(\mathbf{x}_t^-)) + \mathbf{R}_t \quad (4)$$

326

327 In this expression, the left-hand-side represents the actual errors encountered in the system, and  
328 the right-hand-side represents the assumed errors. The latter are prescribed through the  
329 specification of the observation error covariance and through the specification of the model and  
330 forcing perturbations, which are key inputs to the ensemble-based L4\_SM assimilation algorithm  
331 (section 2b). Assuming that the off-diagonal elements of the O-F covariance (equation 4) are  
332 small, a useful assimilation diagnostic is the standard deviation of the *normalized* O-F residuals.  
333 This diagnostic is readily obtained from the published L4\_SM output by normalizing each O-F  
334 residual with its ensemble-diagnosed assumed error standard deviation, and then taking the time  
335 series standard deviation of these normalized O-F residuals. In an optimally calibrated system,  
336 this diagnostic ought to be unity. Values greater than one for this diagnostic indicate that the  
337 actual errors in the system are underestimated (that is, the actual errors are greater than the  
338 assumed errors). Similarly, values less than one indicate that the actual errors are overestimated  
339 (that is, the actual errors are less than the assumed errors). Note that the diagnostic only  
340 addresses the total error and does not distinguish between observation and forecast errors.

341

342 Another useful diagnostic is provided by the ensemble mean O-A Tb residuals (i.e.,  $\mathbf{y}_t - \mathbf{h}(\mathbf{x}_t^+)$ ),  
343 which are the differences between the (rescaled) SMAP Tb observations and the analyzed Tbs.  
344 (In the L4\_SM system, the latter are diagnosed from the analyzed soil moisture and temperature

345 fields.) As for the O-F residuals, the mean value for the O-A residuals should be zero in an  
346 optimally calibrated system. The standard deviation of the O-A residuals should be less than that  
347 of the O-F residuals, with the difference reflecting the reduction in the uncertainty of the  
348 estimated Tbs obtained through the analysis. Finally, the (time series) mean of the (ensemble  
349 mean) soil moisture and temperature increments ( $\Delta\mathbf{x}_t$ ) should be zero in an optimally calibrated  
350 system, and the standard deviation of the increments is a measure of a typical analysis-based  
351 adjustment to the model forecast.

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358 **3. Results**

359 Results are discussed in five subsections. First, we present global maps of L4\_SM soil moisture  
360 estimates (section 3a). Next, we briefly illustrate the impact of the SMAP observations in the  
361 L4\_SM analysis by investigating a particular rain event in Australia in May 2016 (section 3b).  
362 Finally, an assessment of the internal diagnostics of the L4\_SM assimilation system offers useful  
363 insights at the global scale into the quality of the L4\_SM product (section 3c-e). This evaluation  
364 focuses on the counts of the assimilated Tb observations, on the statistics of the O-F and O-A Tb  
365 residuals, and on the statistics of the soil moisture and temperature analysis increments. Some of  
366 the text in this section is adapted from two non-peer reviewed project reports (Reichle et al.  
367 2015b, 2016d) and has been updated to reflect the results obtained for the Version 2 L4\_SM  
368 product and the longer validation period used here.

369

370 *a. Global soil moisture*

371 We start with a discussion of global maps of time-averaged L4\_SM surface soil moisture (Figure  
372 1a) and root-zone soil moisture (Figure 1c) for the 2-year period from April 2015 to March 2017.  
373 The global patterns are as expected – arid regions such as the southwestern US, the Sahara  
374 desert, the Arabian Peninsula, southern Africa, and central Australia exhibit generally dry  
375 surface and root-zone soil moisture conditions, whereas the tropics (Amazon, central Africa, and  
376 Indonesia) and high-latitude regions show wetter conditions. One notable exception is that a  
377 portion of the Democratic Republic of Congo and adjacent areas appear unexpectedly dry. This  
378 is because over Africa, the Version 2 L4\_SM algorithm uses precipitation forcing directly from  
379 the GEOS-5 FP system, which has a known dry bias in central Africa similar to that of the

380 model-generated precipitation from the Modern-Era Retrospective Analysis for Research and  
381 Applications, version 2 (MERRA-2), reanalysis product (Reichle et al. 2017a; their Figure 3b).

382

383 Generally, the global patterns of absolute soil moisture values are dominated by soil parameters  
384 and climatological factors, which is reflected in the similar patterns of the long-term average  
385 surface and root-zone soil moisture maps. The influence of soil texture is noticeable in the  
386 coarse-scale patterns in the Sahara desert, where little is known about the spatial distribution of  
387 mineral soil fractions. In the land model, areas with high values of soil organic carbon  
388 (including, for example, the region along the southern edge of Hudson Bay and portions of  
389 Alaska) are assigned a high porosity value and show persistently wetter conditions than other  
390 areas.

391

392 The strong impact of climate on global soil moisture patterns is also reflected in the overall  
393 similarity between the time-averaged fields (Figure 1a and 1c) and the corresponding  
394 instantaneous fields for 1 June 2015 at 00:00 UTC, shown in Figure 1b and 1d, respectively, for  
395 surface and root-zone soil moisture. In the latter maps, however, some regions do exhibit strong  
396 differences in soil moisture conditions from the long-term average values. For example, the very  
397 wet conditions on 1 June 2015 in Texas, Oklahoma, and Kansas and extending into the US  
398 Midwest (Figure 1b and 1d) resulted from extreme rainfall events throughout May 2015.  
399 Another notable feature is the strong spatial contrast in dry and wet soil moisture conditions in  
400 western Australia on 1 June 2015. This contrast resulted from parts of the region having seen  
401 unseasonably high rainfall conditions in May 2015, with a few locations recording their wettest  
402 May on record, and with many locations recording their wettest May for over twenty years. In

403 contrast, the rest of Western Australia recorded rainfall that was below to very much below  
404 average (Bureau of Meteorology 2017). Also visible in Figure 1b and 1d are the dry conditions  
405 on 1 June 2015 in Spain, which in this year experienced its driest May on record, followed by an  
406 extraordinarily long, intense summer heat wave (Blunden and Arndt 2016).

407

408 The L4\_SM product also includes a large number of output fields that are not subject to formal  
409 validation requirements. Such “research” outputs include the surface meteorological forcing  
410 fields, land surface fluxes, soil temperature, and snow. Figure 2 illustrates two of these fields for  
411 24 January 2016, the surface soil temperature (at 12:00 UTC) and the snow mass (3-hour average  
412 for 12:00-15:00 UTC). Again, the global patterns are consistent with expectation. The hottest  
413 surface soil temperatures are in equatorial eastern Africa, where the local time is around 3pm and  
414 the diurnal cycle of the surface soil temperature is at or near its peak. The soil is frozen in large  
415 portions of the mid and high northern latitudes. The snow mass distribution is also consistent  
416 with expectation, with nearly continuous snow cover in the northern high latitudes and in the  
417 northern hemisphere high mountain ranges. Also visible is the snow accumulation from the  
418 severe blizzard that hit the eastern US on January 22-24, 2016 (Greybush et al. 2017). Snow is  
419 all but absent in the southern hemisphere in the middle of the austral summer. The L4\_SM snow  
420 mass estimates are, by construction, similar to those from MERRA-2, which were found to have  
421 reasonable skill when compared to independent data (Reichle et al. 2017c).

422

423 It should be noted that the L4\_SM temperature and snow fields are largely determined by the  
424 forcing data and the Catchment model physics. The L4\_SM temperature fields are also impacted  
425 by the SMAP observations (directly through the soil temperature increments, and indirectly

426 through the effect of soil moisture on the surface energy balance via the latent heat flux). But  
427 this impact is relatively minor (Reichle et al. 2017b; their Figure 6). In any case, though, the  
428 L4\_SM temperature and snow estimates are consistent with the L4\_SM soil moisture estimates  
429 and may be useful for studies that require land surface data beyond soil moisture. For example,  
430 the surface soil temperature and snow fields can be used to identify frozen or snow-covered  
431 conditions. Unlike the SMAP Level 2 and 3 retrieval products, the L4\_SM product does not  
432 provide binary flags to classify the conditions at the time for which the soil moisture estimates  
433 are valid. Rather, the L4\_SM product provides quantitative estimates of skin and soil  
434 temperatures, snow mass, precipitation, etc. (section 2a) that contain far more complete  
435 information than binary flags. Users can readily convert this quantitative information into binary  
436 flags should the need arise.

437

#### 438 *b. Illustration of the L4\_SM analysis*

439 A key element of the L4\_SM analysis update (section 2b) is the downscaling and inversion of the  
440 coarse-scale observational information of the assimilated Tbs into the modeled geophysical  
441 variables on the 9-km grid, a calculation that is based on modeled error characteristics, which  
442 vary dynamically and spatially. In this section we provide an example and illustration of a single  
443 analysis update.

444

445 Routine monitoring of the L4\_SM analysis diagnostics (section 2c) revealed a large spike in the  
446 (spatial) standard deviation of the H-pol and V-pol O-F Tb residuals on 8 May 2016 at 21:00  
447 UTC (see also section 3d). A closer investigation revealed that a major rain event occurred in  
448 the interior of Australia on this day (Figure 3a), according to observations from the Australian

449 Bureau of Meteorology (2017), and that this rain event was very poorly represented in the  
450 L4\_SM forcing data (Figure 3b). The L4\_SM system relies on the daily, global, 0.5°, gauge-  
451 based CPCU product (section 2a), which does not include many of the high-quality, local  
452 measurements available to the Bureau of Meteorology. As a consequence, the precipitation used  
453 in the L4\_SM system missed most of the rainfall that occurred in southeastern Queensland and  
454 northeastern South Australia. The L4\_SM precipitation further underestimated the rainfall in  
455 northern New South Wales. Therefore, the soil moisture in the model forecast for 21:00 UTC  
456 was too dry, and the model forecast Tb was too high compared to the SMAP observations,  
457 resulting in very large negative O-F Tb residuals (Figure 3c). Consequently, the L4\_SM analysis  
458 of the SMAP Tb observations resulted in substantial corrections (or increments) to the modeled  
459 surface soil moisture (Figure 3d), root-zone soil moisture (Figure 3e), and surface soil  
460 temperature (Figure 3f).

461  
462 The example in Figure 3 clearly illustrates the difficulties of modeling soil moisture at the global  
463 scale using standard meteorological forcing datasets and the benefits to this modeling of  
464 assimilating SMAP Tb observations. The quality of the global precipitation products that meet  
465 the L4\_SM latency requirement is uneven at best. The accuracy of the gauge-based CPCU  
466 product – the product selected for the L4\_SM system – in a given region obviously depends on  
467 the density of gauges in that region, and few gauges are available in the interior of Australia  
468 (Reichle et al. 2017a; their Figure 8e). Note also that over land, satellite-based precipitation  
469 products are not necessarily better on average than gauge-based products, and global combined  
470 satellite-gauge products are not available with the required latency (for L4\_SM operational  
471 production) and length of record (to calibrate the L4\_SM system). In this particular case, the

472 SMAP Tb observations are clearly inconsistent with the precipitation estimates from the CPCU  
473 product but are consistent with the more accurate regional precipitation measurements from the  
474 Australian Bureau of Meteorology. The analysis of SMAP Tb observations was able to correct  
475 short-term errors in the L4\_SM CPCU-based precipitation forcing and thereby improve the  
476 L4\_SM soil moisture estimates.

477

### 478 *c. Observation counts*

479 In this section we investigate the number of assimilated SMAP Tb observations. Figure 4 shows  
480 the total number of Tb observations that were assimilated during the assessment period (April  
481 2015 to March 2017). This count includes H-pol and V-pol observations from ascending and  
482 descending half-orbits (after first averaging over fore- and aft-looking Tbs). The average data  
483 count across the globe is ~804 for the 731-day period (excluding areas where observations were  
484 never assimilated, see below), which implies that one pair of H-pol and V-pol Tb observations  
485 was assimilated approximately every other day on average. Few or no SMAP Tbs were  
486 assimilated (1) in some mountainous areas, including portions of the Rocky Mountains and the  
487 Andes, (2) along coastlines and next to major rivers and lakes, including the Amazon, the Congo,  
488 and the Great Lakes, and (3) in regions with many small lakes, such as in northern Canada.  
489 Generally, SMAP Tb observations within 40 km of major water bodies and for grid cells with  
490 water fraction exceeding 5% are excluded because the L4\_SM model cannot predict the mixed  
491 (land and water) signal that is present in these observations and would thus yield an incompatible  
492 (land-only) Tb forecast. Despite the much shorter warm (unfrozen) season at high-latitudes, far  
493 northern areas exhibit relatively high counts of assimilated Tb observations because of SMAP's  
494 polar orbit, which results in more frequent revisit times there.

495

496 SMAP Tb observations were also never assimilated across large areas in eastern Europe and the  
497 southern half of continental Asia (Figure 4) because in this region L-band radio-frequency  
498 interference (RFI) is common (Oliva et al. 2012). To the extent possible, SMAP is equipped  
499 with a variety of hardware and software tools that detect and mitigate RFI, which allows SMAP  
500 to provide science-quality observations of the naturally emitted Tb with near-global coverage  
501 (Piepmeier et al. 2014, 2017). However, the L4\_SM algorithm also requires knowledge of the  
502 climatological seasonal cycle of the L-band Tb observations to address the bias in the  
503 corresponding Tb model forecasts (section 2b). This (seasonally varying) L-band climatology is  
504 derived from observations provided by the Soil Moisture Ocean Salinity (SMOS) mission. In the  
505 RFI-affected areas, SMOS does not provide Tb observations of sufficient quality and quantity to  
506 derive the climatology. The resulting spatial (and temporal) gaps in the climatology thus  
507 constrain the coverage of SMAP assimilation in Version 2 of the L4\_SM algorithm. (These gaps  
508 are largely closed in the recently released Version 3 L4\_SM system because its Tb rescaling  
509 parameters are based on SMOS and SMAP observations.) It is important to note, though, that  
510 the L4\_SM product provides soil moisture estimates everywhere, even if in some regions the  
511 L4\_SM estimates are not based on the assimilation of SMAP observations and thus rely solely  
512 on the information in the model and forcing data.

513

514 Next, Figure 5a shows a daily time series of the global observation counts for April 2015 to  
515 March 2017, again including H-pol and V-pol observations from ascending and descending half-  
516 orbits. The data counts clearly vary with season. They also vary with time of day (not shown);  
517 there are 8 analysis times per day (at 0z, 3z, ..., 18z, and 21z), and the counts vary according to

518 the amount of land surface area at those times having a local time close to 6am or 6pm, when  
519 SMAP crosses the Equator. Each day the L4\_SM analysis typically ingests between 40,000 and  
520 100,000 SMAP Tb observations (Figure 5a), with a mean of about 65,300 observations.  
521 Occasionally, few or no observations were assimilated (e.g., 13 May 2015, 16 Dec 2015, 1 May  
522 2016) because of short gaps in the SMAP observation record when the spacecraft was in safe  
523 mode.

524

#### 525 *d. Brightness temperature residuals*

526 In this section we investigate the O-F and O-A Tb residuals (section 2c). Figure 5b shows the  
527 daily time series of the spatially averaged O-F and O-A residuals. Global mean O-F values  
528 typically range from -2 K to 2 K, with a long-term average value of just 0.34 K. Typical mean  
529 O-A values are slightly smaller than mean O-F values and have a long-term average value of  
530 0.25 K. Overall, the relatively small mean O-F and O-A values suggest that the assimilation  
531 system is reasonably bias-free, at least in a global average sense.

532

533 Typical magnitudes of the O-F Tb residuals, indicated by the values of their daily (spatial)  
534 standard deviation, range between 4 K and 10 K (Figure 5c). The standard deviations of the O-A  
535 residuals range from 3 K to 6 K and are generally lower than those of the O-F residuals (Figure  
536 5c). The long-term average of 4.0 K for the O-A standard deviation, compared to 5.9 K for the  
537 O-F residuals, reflects the reduction in uncertainty obtained from the analysis. The values of the  
538 O-F spatial standard deviation show occasional spikes of around 8-10 K. Some of the spikes  
539 occur simply because few observations were assimilated on the days in question (Figure 5a).  
540 The 8 May 2016 spike, however, as well as several others (e.g., 1 January 2016, 2 Feb 2016, and



541 10 March 2016), can be traced back to extreme O-F values in the corresponding 21z analysis  
542 over Australia, which has very large negative O-F values reaching -90 K across a large region  
543 (e.g., Figure 3c). That is, these spikes correspond to major rain events in Australia during an  
544 unusually wet period, rain events that were missed in the CPCU-based precipitation forcing data  
545 used for L4\_SM (section 3b). This again highlights the potential for SMAP to provide valuable  
546 information about soil moisture and rainfall in areas where precipitation estimates are most  
547 impacted by errors.

548

549 Next, Figure 6 shows the global distributions of the time series mean and standard deviation of  
550 the O-F residuals. The time mean values of the O-F residuals are typically small and mostly  
551 range from -3 K to 3 K (Figure 6a). Overall, there is a positive bias of 0.37 K, with fewer areas  
552 exhibiting negative mean O-F values. The largest values of around 3 K are found in the Sahel  
553 and in central and southern Africa. Note that over Africa (and in the high latitudes), the L4\_SM  
554 precipitation forcing is not corrected to the gauge-based product (section 2a; Reichle and Liu  
555 2014). Consequently, the L4\_SM algorithm is somewhat biased where the climatology of the  
556 present forcing data (from the  $\sim 1/4^\circ$  GEOS-5.13 FP system; Lucchesi 2013a) is inconsistent with  
557 that of the historic forcing data (from the  $\sim 1/2^\circ$  GEOS-5.9 reprocessing “FP-IT” system; Lucchesi  
558 2013b), which was used to derive the Tb rescaling parameters in the pre-launch algorithm  
559 calibration (section 2b). Relatively high mean O-F values are also seen in the center of the  
560 United States, Argentina, Uruguay, Australia, and portions of Siberia, which indicates that the  
561 L4\_SM system would benefit from further calibration of the Tb rescaling parameters or,  
562 preferably, from reducing the bias in the modeling system.

563

564 The time series standard deviation of the O-F residuals ranges from a few Kelvin to around 15 K,  
565 with a global (spatial) average of about 6.0 K (Figure 6b). High values are found, for example,  
566 in central North America, the Sahel, central Asia, and Australia. These regions have sparse or  
567 modest vegetation cover and typically exhibit strong variability in soil moisture conditions. The  
568 O-F residuals are generally smallest in more densely vegetated regions, including the eastern  
569 United States, the Amazon basin, and tropical Africa. Small values are also found in the high-  
570 latitudes, including Alaska and Siberia, and in the Sahara desert. The spatially averaged time  
571 series standard deviation of the O-A residuals is 4.0 K (not shown), which again reflects the  
572 impact of the SMAP observations on the L4\_SM system. (Note that the spatio-temporal average  
573 statistics reported for Figure 5 are slightly different from those of Figure 6 because they are  
574 derived in different ways: by temporally averaging spatial statistics and by spatially averaging  
575 temporal statistics, respectively.)

576

577 Next, Figure 7 shows the standard deviation of the *normalized* O-F residuals, which measures the  
578 consistency between the assumed (modeled) errors and the actual errors in the observations and  
579 the model forecasts (section 2c). The global average of the metric is indeed 1.0 (Figure 7),  
580 which would suggest that, on average, the assumed errors are consistent with the actual errors.  
581 The metric, however, varies greatly across the globe. Typical values are either too low or too  
582 high. In densely vegetated regions (Amazon basin, eastern US, tropical Africa, Indonesia),  
583 deserts (Sahara, Arabian Peninsula), and the high northern latitudes, values range from 0.25 to  
584 0.5, and thus the actual errors there are considerably overestimated. In these regions, the total  
585 actual Tb errors (Figure 6b) are smaller than the assumed observation error standard deviation of  
586 4 K, suggesting that the error of representativeness (which dominates the assumed observation

587 error; section 2b) is too large. Conversely, in agricultural regions, including irrigated areas, and  
588 in transition zones between dry and wet climates (including central North America, portions of  
589 Brazil and Argentina, the Sahel, and India), values range from 1.5 to 4, meaning that the actual  
590 errors in these regions are considerably underestimated. Large values are also found in most of  
591 Australia, where errors in the precipitation forcing are particularly pronounced (section 3b) and  
592 presumably underestimated. In these regions, it is thus likely that the model forecast error is  
593 underestimated.

594

595 The standard deviation of the normalized O-F residuals (Figure 7) only evaluates the total error  
596 covariance (equation 4), whereas the Kalman gain (equation 3), and thus the weights given to the  
597 observations in the analysis, depend on the *relative* magnitude of the observation and model  
598 forecast errors. That is, the algorithm may well be using near-optimal weights even as the total  
599 error covariance is poorly specified. How efficiently the algorithm uses the observations is  
600 measured, at least for a linear system, by the lagged auto-correlation of the O-F residuals (section  
601 2c). The global average of this metric is shown in Figure 8a for lags from 1 day to 10 days. The  
602 auto-correlations are always positive, which is not consistent with the white noise characteristics  
603 expected from an optimal (linear) system.

604

605 The average number of data pairs that contribute to the auto-correlation estimate at a given  
606 location is shown in Figure 8b, along with the corresponding fraction of the global land area for  
607 which auto-correlation estimates were computed. These statistics vary with lag according to the  
608 characteristics of the SMAP orbit (Figure 8b). Statistics with at least 50% coverage are available  
609 for lags of 2, 3, 5, 6, 8 and 10 days. The maximum number of data pairs and coverage is

610 obtained for a lag of 8 days, which matches the exact repeat interval for the SMAP orbit. (Note  
611 that the number of data pairs and coverage is very similar for lags separated by 8 days, e.g., for  
612 lags of 2 and 10 days.)

613  
614 The spatial distributions of the auto-correlations for lags of 2, 3, 5, 6, 8 and 10 days are shown in  
615 Figure 9. Auto-correlation values that are within the 95% confidence intervals for white noise  
616 are shown in gray. When interpreting Figure 9, it is important to keep in mind that the width of  
617 the 95% confidence intervals, and thus the area showing significant auto-correlations, changes  
618 with lag partly because the number of data points changes with lag (Figure 8b) owing to the  
619 SMAP orbital characteristics. Notably, the 95% confidence intervals are smaller at 3-day lag  
620 than at 2-day lag, and they are smallest at 8-day lag. Across the lags shown in Figure 9, the auto-  
621 correlations are consistent with white noise (that is, not significantly different from zero at the  
622 5% level) in several regions, including most of western North America, the Sahel, southern  
623 Africa, and central Australia, suggesting that in these regions the L4\_SM algorithm makes  
624 efficient use of the observations.

625  
626 The auto-correlations are significant, however, for some lags across the eastern US, most of  
627 South America, central Africa, and in the northern high latitudes (Figure 9), suggesting that in  
628 these regions the SMAP observations are not used efficiently in the current version of the  
629 L4\_SM algorithm. A closer inspection of the results reveals that the regions with significant O-F  
630 auto-correlations (Figure 9) tend to have relatively small (typical) O-F values (Figure 6b) that are  
631 dominated by seasonally varying bias (not shown), resulting in high auto-correlation values.  
632 Somewhat fortuitously, many regions of sub-optimal algorithm performance thus largely

633 coincide with regions where SMAP Tb observations are not expected to have much influence on  
634 the L4\_SM estimates, including the forested regions of the eastern US and the tropics, where  
635 there is relatively little sensitivity of L-band Tbs to soil moisture.

636

637 Furthermore, the high auto-correlation at 8-day lag in Libya (Figure 9e) can be traced back to the  
638 6pm (ascending) SMAP overpass time and is probably related to errors caused by residual RFI in  
639 the 6pm (descending) SMOS observations used to derive the Tb rescaling parameters (section  
640 2b). Moreover, the high auto-correlation values at lags up to 8 days in the northern high latitudes  
641 and in the non-forested regions of Africa (Figure 9) may be related to seasonally varying bias  
642 caused by the above-mentioned inconsistencies between the current (GEOS-5 FP) and historic  
643 (GEOS-5 FP-IT) model forcing data. Finally, there is a relative maximum in the O-F auto-  
644 correlations at 8-day lag (Figures 8 and 9), which may reflect the periodicity in the spatial  
645 representativeness errors caused by the 8-day exact repeat interval of the SMAP viewing  
646 geometry. A similar connection between errors in gridded soil moisture retrieval products and  
647 orbit repeat cycles was tentatively established by Su et al. (2013) and Lei et al. (2017).

648

649 The auto-correlations reveal potential avenues for improving the L4\_SM algorithm, but it is  
650 important to keep in mind that the inferences offered above are uncertain. For example, serially  
651 correlated model or observation errors, if present, result in non-zero values of the lagged O-F  
652 auto-correlations, even if the weights assigned to the observations are nearly optimal, which  
653 compromises the use of the O-F auto-correlations as a diagnostic for optimality (Daley 1992;  
654 Crow and van den Berg 2010). In the L4\_SM system, errors in the parameters of the radiative  
655 transfer model (required for the observation operator) likely result in serially correlated

656 observation errors, and the ensemble perturbations approach likely results in serially correlated  
657 model errors. Moreover, the L4\_SM land surface model dynamics are non-linear. The O-F  
658 auto-correlations results must therefore be interpreted carefully.

659

660

661

662 *e. Soil moisture and temperature increments*

663 Finally, we evaluate the statistics of the soil moisture and temperature analysis increments  
664 (section 2c). Strictly speaking, the increments are in the space of the Catchment model  
665 prognostic variables that make up the EnKF state vector, including the “catchment deficit”,  
666 “root-zone excess”, “surface excess”, and “top-layer ground heat content” (section 2b; Reichle et  
667 al. 2017b). For the discussion below, the increments were expressed in the equivalent soil  
668 moisture and temperature terms.

669

670 Figure 10 shows the average number of increments that the L4\_SM algorithm generated per day  
671 during the assessment period (April 2015 to March 2017). The global mean is 0.70 (excluding  
672 areas where increments were never computed), which means that for a given location, there are  
673 approximately two increments applied every three days on average, either from an ascending or a  
674 descending overpass. The overall pattern of the increments count follows that of the count of the  
675 assimilated observations (Figure 4). The coverage of the increments, however, is somewhat  
676 greater than that of the observations due to the spatial interpolation and extrapolation of the  
677 observational information in the distributed analysis update of the L4\_SM algorithm. The figure  
678 also reveals the diamond patterns resulting from SMAP’s regular 8-day repeat orbit.

679

680 Next, Figure 11 shows the time mean values of the analysis increments for surface and root-zone  
681 soil moisture as well as for the surface (layer-1) soil temperature. In the long-term average, the  
682 increments for root-zone soil moisture and surface soil temperature vanish nearly everywhere.  
683 Only the increments in surface soil moisture exhibit a bias in some regions, including the US  
684 Great Plains, the Sahel, southern Africa, and Australia, with occasional values of around  $-0.01$   
685  $\text{m}^3 \text{m}^{-3}$ . These mean drying increments are a reflection of the warm bias in the O-F residuals  
686 (Figure 6a). Nevertheless, Figure 11 suggests that the analysis system is very nearly unbiased in  
687 the global mean sense.

688

689 Finally, Figure 12 shows the time series standard deviation of the increments in surface and root-  
690 zone soil moisture as well as surface soil temperature. This metric measures the typical  
691 magnitude of instantaneous increments. Typical increments in surface soil moisture (Figure 12a)  
692 are on the order of  $0.01$ - $0.02 \text{ m}^3 \text{m}^{-3}$  in the western US, central Mexico, southern Argentina, the  
693 Sahel, southern Africa, central Asia, and southern India. Typical increments are somewhat  
694 larger ( $0.02$ - $0.03 \text{ m}^3 \text{m}^{-3}$ ) in most of Australia and smaller ( $0.005 \text{ m}^3 \text{m}^{-3}$ ) in the eastern US,  
695 eastern Brazil, and the high northern latitudes. Over the tropical forests, surface soil moisture  
696 increments are generally negligible, reflecting the fact that in those areas the measured SMAP  
697 Tbs are mostly sensitive to the dense vegetation and are only marginally sensitive to soil  
698 moisture and soil temperature.

699

700 Typical increments in root-zone soil moisture (Figure 12b) show a global pattern that is very  
701 similar to that of the surface soil moisture increments, albeit with smaller magnitudes that again

702 reflect the weaker error correlations between the Tb observations and the deeper layer soil  
703 moisture. The magnitude of the average root-zone soil moisture increments rarely exceeds 0.01  
704  $\text{m}^3 \text{m}^{-3}$ , with a global average value of about 0.003  $\text{m}^3 \text{m}^{-3}$  (excluding areas where increments  
705 were never computed). Finally, typical increments for the surface soil temperature (Figure 12c)  
706 and the skin temperature (not shown) also exhibit a pattern similar to that of the surface soil  
707 moisture increments, with typical (absolute) surface soil temperature increments in dry regions  
708 ranging between 0.5 K and 1.5 K. The relatively small magnitude of the temperature increments  
709 reflects the fact that the L4\_SM Tb analysis has been calibrated primarily for updating the model  
710 soil moisture (De Lannoy and Reichle 2016a; Reichle et al. 2017b).

711

712



## 713 **5. Summary and Conclusions**

714 The SMAP L4\_SM algorithm assimilates SMAP Tb observations into the NASA Catchment  
715 model and thereby interpolates and extrapolates the information from the SMAP observations in  
716 time and in space by combining them with the model estimates, taking into consideration the  
717 relative uncertainties of each. The resulting L4\_SM data product represents this merged  
718 information and consists of global, 3-hourly, 9-km resolution estimates of surface and root-zone  
719 soil moisture conditions, along with a number of related land surface fields such as soil  
720 temperatures and snow mass. The L4\_SM product is available from 31 March 2015 to present,  
721 with a latency of 2-3 days from the time of observation.

722

723 The 2-year climatology of the L4\_SM surface and root-zone soil moisture estimates captures the  
724 expected global patterns of arid and humid regions (Figure 1). Moreover, we investigated the 8  
725 May 2016, 21:00 UTC analysis over Australia, which exhibited very large negative O-F Tb  
726 residuals, suggesting that the model forecast soil moisture was much too dry at the time in  
727 question (Figure 3). The reason for the lack of soil moisture prior to the analysis turned out to be  
728 a large underestimation in the rainfall used to force the model over the course of the preceding  
729 day. The assimilation of SMAP observations resulted in a considerable correction of the model  
730 forecast soil moisture towards wetter conditions, thereby compensating for the short-term deficit  
731 in the L4\_SM rainfall forcing. This case study clearly demonstrates that the assimilation of  
732 SMAP Tb observations can correct for such transient errors in the L4\_SM modeling system. The  
733 L4\_SM system is not designed, however, to correct for bias in the forcing data, such as the dry  
734 precipitation bias in the GEOS-5 forcing in central Africa (section 3a).

735

736 By validating the L4\_SM product against in situ measurements, Reichle et al. (2017b)  
737 demonstrated that the L4\_SM soil moisture estimates meet their accuracy requirement and are  
738 better than estimates from a model-only simulation that does not benefit from the assimilation of  
739 SMAP observations. The number of locations with suitable in situ measurements, however, is  
740 very limited. The present paper supplements the in situ validation results of Reichle et al.  
741 (2017b) with an evaluation of the internal diagnostics of the L4\_SM assimilation algorithm,  
742 which are available quasi-globally, wherever and whenever SMAP observations are assimilated.  
743 The assimilation diagnostics include the statistics of the observation counts, the O-F and O-A Tb  
744 residuals, and the soil moisture and temperature increments.

745

746 The Version 2 L4\_SM system assimilates between 40,000 and 100,000 SMAP Tb observations  
747 each day (Figure 5a), or about one pair of H-pol and V-pol Tb observations every other day, on  
748 average, over land where SMAP data are assimilated. SMAP observations are not assimilated  
749 over land that is permanently glaciated, close to open water or major rivers, or affected by RFI,  
750 where the necessary L-band climatology cannot be obtained from SMOS, including large  
751 portions of Europe, the Arabian Peninsula, and southern continental Asia (Figure 4). Because  
752 the impact of the assimilated SMAP Tb observations in the spatially distributed analysis update  
753 is non-local, soil moisture and temperature increments are applied over a somewhat larger area,  
754 which includes land close to major rivers and shorelines (Figure 10).

755

756 The instantaneous soil moisture and temperature analysis increments are within a reasonable  
757 range and, as expected, small over densely vegetated regions (Figure 12). The distributed  
758 filtering approach results in spatially smooth soil moisture increments (Figure 3). Moreover, the

759 time-average increments are well below  $0.01 \text{ m}^3 \text{ m}^{-3}$  for soil moisture and less than 1 K for  
760 surface soil temperature nearly everywhere (in terms of magnitude), suggesting that the L4\_SM  
761 system is reasonably unbiased (Figure 11). Similarly, the O-F Tb residuals exhibit only small  
762 (absolute) biases on the order of 1-3 K between the (rescaled) SMAP observations and the  
763 corresponding L4\_SM model forecasts (Figure 6a). This further indicates that the assimilation  
764 system is essentially unbiased owing to the rescaling of the Tb observations prior to assimilation.  
765 The spatially averaged time series standard deviation of the O-F Tb residuals is 5.9 K (Figure  
766 6b), which reduces to 4.0 K for the O-A residuals. This decrease reflects the reduction of the  
767 uncertainty following the assimilation of the SMAP observations. Averaged globally, the time  
768 series standard deviation of the normalized O-F residuals is close to unity (Figure 7), which  
769 would suggest that the magnitude of the assumed errors in the model and the observations  
770 approximately reflects that of the actual O-F errors.

771

772 The results, however, also reveal several limitations of the Version 2 L4\_SM data product and  
773 science algorithm calibration that will need to be addressed in future releases. Regionally, the  
774 time series standard deviation of the normalized O-F residuals deviates considerably from unity  
775 (Figure 7), which indicates that the L4\_SM assimilation algorithm either over- or underestimates  
776 the actual errors that are present in the system. This pattern is caused, at least in part, by the use  
777 of a spatially constant Tb observation error variance that does not capture the spatially variable  
778 representativeness errors associated with the radiative transfer model. Additionally, the spatially  
779 constant perturbation parameters do not account for spatially varying model error characteristics,  
780 including errors associated with the lack of irrigation in the modeling system.

781

782 Furthermore, non-zero and generally positive values of the lagged auto-correlations of the O-F  
783 residuals suggest that the SMAP Tb observations are not used efficiently in many forested  
784 regions (including the eastern US and the tropics), in most of the northern high latitudes, and in  
785 portions of South America and Africa (Figures 8 and 9). The lack of efficiency may be caused  
786 by seasonally varying bias, auto-correlated model and/or observation errors, and/or non-  
787 linearities in the land model and observation operator. In many of these regions, SMAP has only  
788 a small impact on the L4\_SM soil moisture estimates (that is, typically small O-F residuals and  
789 soil moisture increments), which is, at least for the forested regions, as expected. Finally, the  
790 adverse impact of RFI on the SMOS Tb observations in large portions of Europe, the Middle  
791 East, and East Asia made it impossible to calibrate the L4\_SM algorithm and assimilate SMAP  
792 observations in these regions in the Version 2 L4\_SM release (Figure 4).

793

794 Future improvements of the L4\_SM algorithm should focus on mitigating the over- and  
795 underestimation of the actual errors, which will likely require the specification of spatially  
796 variable inputs for the observation and model error characteristics. Additional revisions should  
797 focus on the structure and parameters of the Catchment model to reduce the bias in the L4\_SM  
798 soil moisture and temperature (Reichle et al. 2017b). This bias in the L4\_SM product is  
799 primarily driven by the bias in the Catchment model because the Tb rescaling yields, by  
800 construction, a reasonably unbiased L4\_SM analysis. Furthermore, the radiative transfer model  
801 and its parameters should be improved to reduce the Tb bias in the modeling system and thus  
802 minimize the need for Tb rescaling. These biases could be reduced prior to data assimilation  
803 (through model calibration) or dynamically within the assimilation system (through  
804 augmentation of the state vector).

805

806 Eliminating the seasonally varying bias in the modeled Tb and soil moisture, however, is  
807 difficult and likely requires a few more years of SMAP observations. In the meantime, the  
808 recently released Version 3 L4\_SM product employs improved Tb rescaling parameters that are  
809 based on (1) a longer period (and newer version) of SMOS observations where available and the  
810 shorter record of SMAP observations elsewhere (in particular, in regions where RFI prevents the  
811 use of SMOS data) and (2) a model Tb climatology constructed using retrospective surface  
812 meteorological forcing data that are more consistent with the forcing data used during the SMAP  
813 period. In this way, SMAP observations are now assimilated almost everywhere and with  
814 improved bias correction. In summary, the present paper and its companion (Reichle et al.  
815 2017b) demonstrate that the L4\_SM product is sufficiently mature and of adequate quality for  
816 distribution to and use by the larger science and application communities.

817

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825

826

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1037 **Figure Captions**

1038

1039 Fig. 1. (a) Two-year average (April 2015 to March 2017) L4\_SM surface soil moisture. (b)  
1040 Snapshot of L4\_SM surface soil moisture on 1 June 2015 at 00:00 UTC. (c) As in (a) but for  
1041 root-zone soil moisture. (d) As in (b) but for root-zone soil moisture.

1042

1043 Fig. 2. L4\_SM (a) surface soil temperature analysis for 24 January 2016, 12:00 UTC and (b)  
1044 snow mass for 24 January 2016, 12:00-15:00 UTC.

1045

1046 Fig. 3. Cumulative precipitation for 8 May 2016 (00:00 UTC to 00:00 UTC) indicated by (a)  
1047 measurements from the Australian Bureau of Meteorology (BoM) and (b) the L4\_SM  
1048 precipitation inputs. (c) O-F residuals for H-pol Tb on 8 May 2016, 21:00 UTC. Analysis  
1049 increments of (d) surface soil moisture, (e) root-zone soil moisture, and (f) surface soil  
1050 temperature on 8 May 2016, 21:00 UTC. Australian states and territories are labeled in (b).

1051

1052 Fig. 4. Number of SMAP Tb observations used in the L4\_SM algorithm during April 2015 to  
1053 March 2017. Data counts include H-pol and V-pol data from ascending and descending half-  
1054 orbits.

1055

1056

1057 Fig. 5. (a) Daily counts of SMAP Tb observations assimilated into L4\_SM during April 2015 to  
1058 March 2017, including H-pol and V-pol data from ascending and descending orbits. (b) Mean of  
1059 the corresponding O-F and O-A Tb residuals, where the mean values are computed separately for  
1060 each 3-hourly analysis by averaging across the global land domain (where SMAP observations  
1061 are assimilated) and then averaging the resulting values over the 8 analysis times for each day.  
1062 (c) As in (b) but for the standard deviation. Vertical grid lines indicate the first day of each  
1063 month.

1064

1065 Fig. 6. (a) Mean and (b) standard deviation of the O-F Tb residuals from the L4\_SM algorithm  
1066 for April 2015 to March 2017.

1067

1068 Fig. 7. Standard deviation of the *normalized* O-F Tb residuals from the L4\_SM algorithm for  
1069 April 2015 to March 2017.

1070

1071 Fig. 8. (a) Spatially averaged, lagged sample auto-correlation of the O-F Tb residuals. (b)  
1072 Average number of O-F data pairs at each grid cell (black; left axis) and fractional area coverage  
1073 (gray; right axis) contributing to the sample auto-correlation values.

1074

1075 Fig. 9. Sample auto-correlation of the O-F Tb residuals at (a) 2-day, (b) 3-day, (c) 5-day, (d) 6-  
1076 day, (e) 8-day, and (f) 10-day lag. Values that are not significantly different from zero (at the  
1077 5% level) are shown in gray.

1078

1079

1080 Fig. 10. Average number of increments per day generated by the L4\_SM algorithm during April  
1081 2015 to March 2017. The result applies equally to all elements of the control vector, including  
1082 the model prognostic variables related to surface soil moisture, root-zone soil moisture, skin  
1083 temperature, and surface (layer-1) soil temperature.

1084

1085 Fig. 11. Time series mean of the increments for (a) surface soil moisture, (b) root-zone soil  
1086 moisture, and (c) surface (layer-1) soil temperature from the L4\_SM algorithm for April 2015 to  
1087 March 2017.

1088

1089 Fig. 12. Same as Figure 10 but for time series standard deviation of the increments.

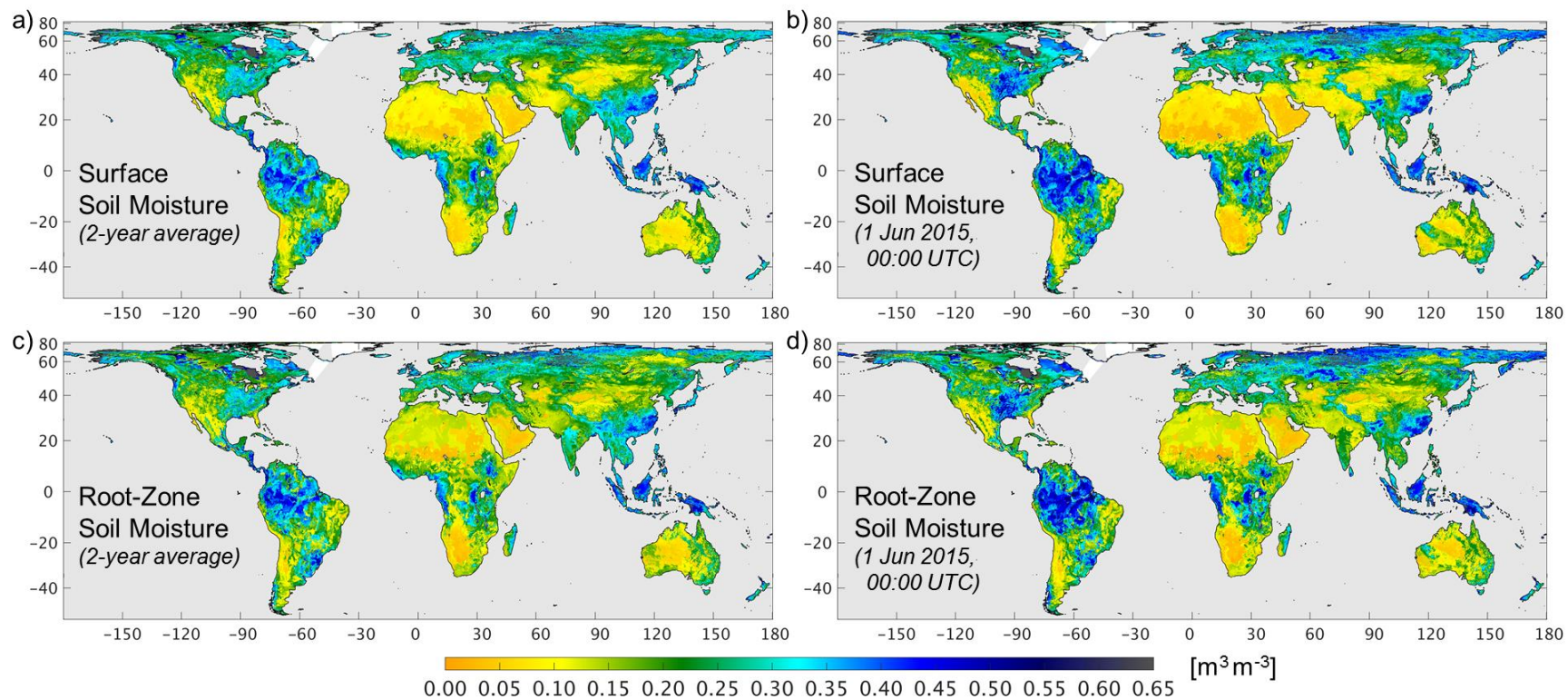
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1093 **Figures**

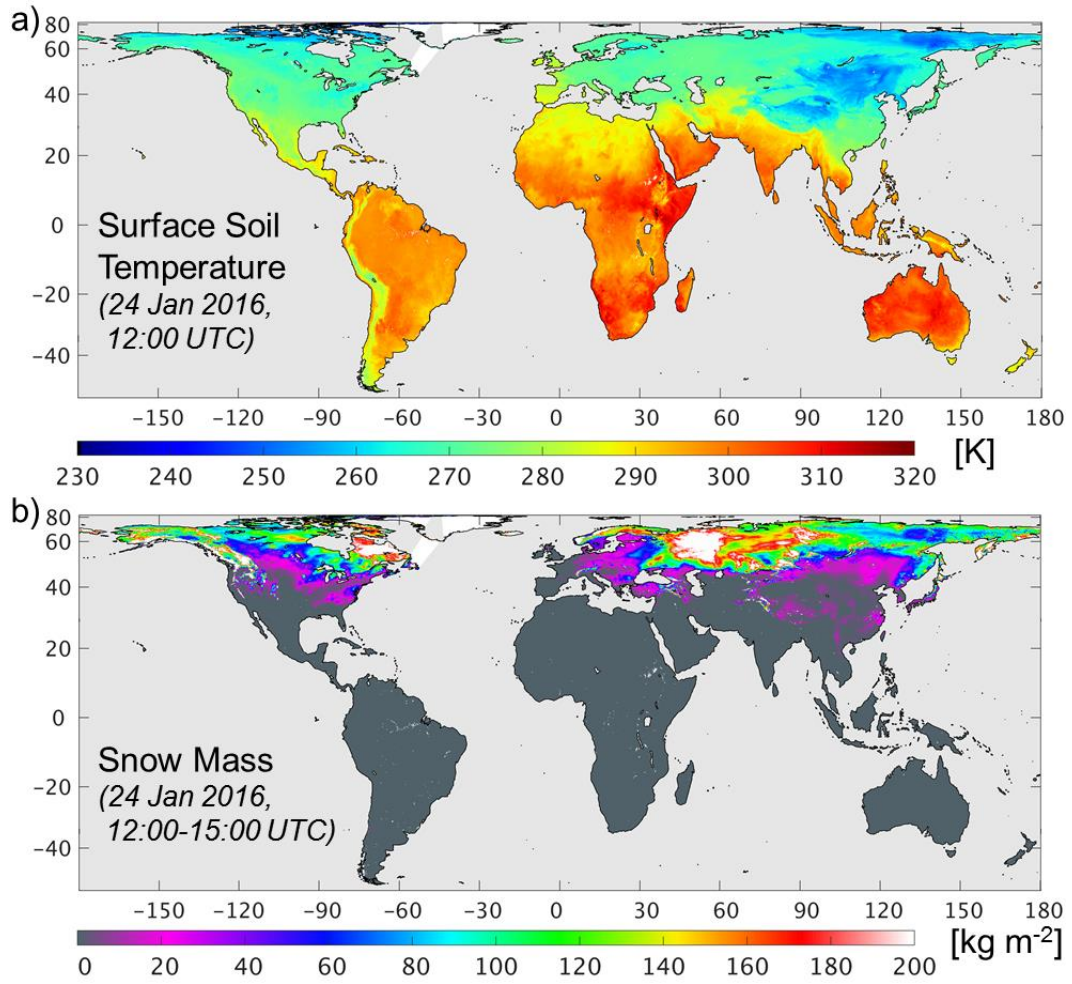
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1096 Fig. 1. (a) Two-year average (April 2015 to March 2017) L4\_SM surface soil moisture. (b) Snapshot of L4\_SM surface soil moisture

1097 on 1 June 2015 at 00:00 UTC. (c) As in (a) but for root-zone soil moisture. (d) As in (b) but for root-zone soil moisture.

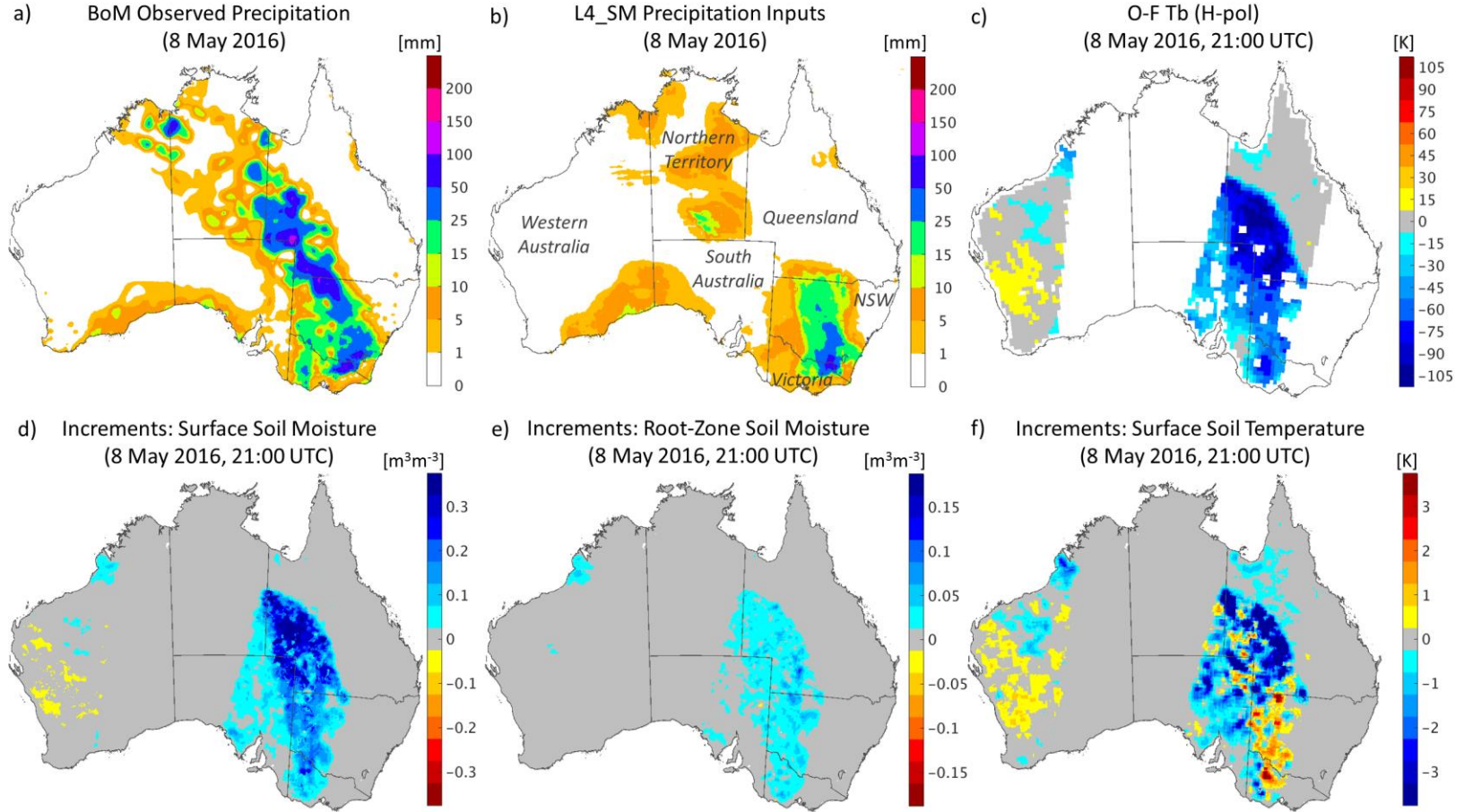


1098

1099 Fig. 2. L4\_SM (a) surface soil temperature analysis for 24 January 2016, 12:00 UTC and (b)

1100 snow mass for 24 January 2016, 12:00-15:00 UTC.

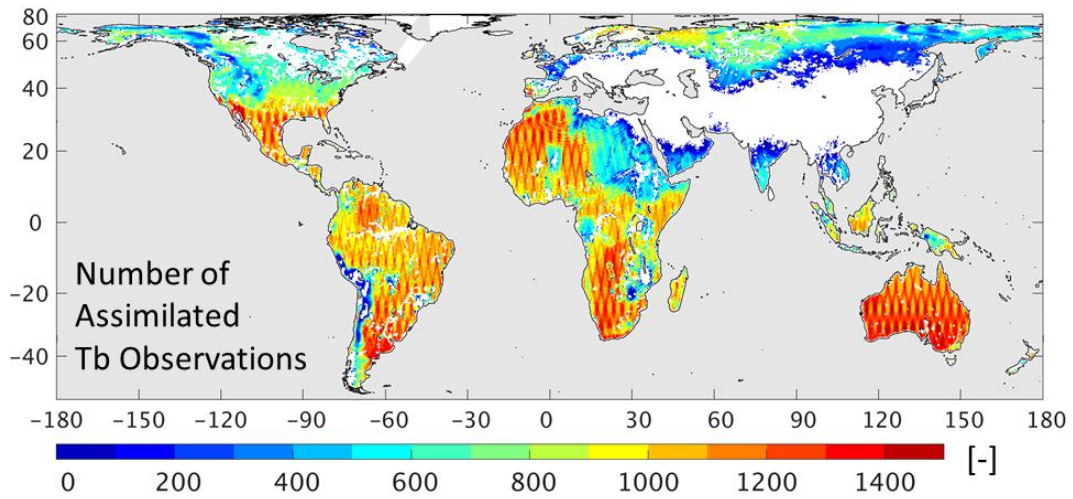
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1102

1103 Fig. 3. Cumulative precipitation for 8 May 2016 (00:00 UTC to 00:00 UTC) indicated by (a) measurements from the Australian  
 1104 Bureau of Meteorology (BoM) and (b) the L4\_SM precipitation inputs. (c) O-F residuals for H-pol Tb on 8 May 2016, 21:00 UTC.  
 1105 Analysis increments of (d) surface soil moisture, (e) root-zone soil moisture, and (f) surface soil temperature on 8 May 2016, 21:00  
 1106 UTC. Australian states and territories are labeled in (b).



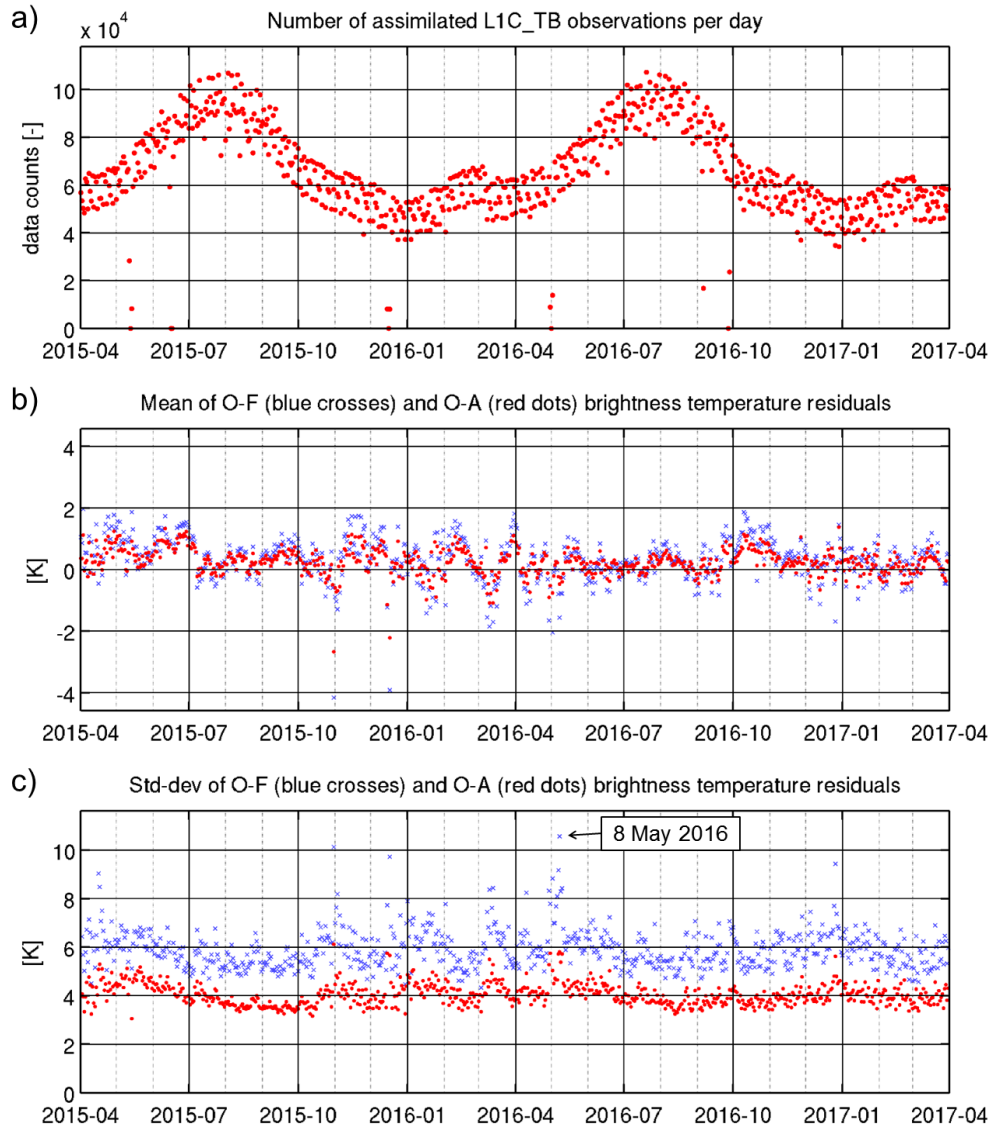


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1108 Fig. 4. Number of SMAP Tb observations used in the L4\_SM algorithm during April 2015 to  
 1109 March 2017. Data counts include H-pol and V-pol data from ascending and descending half-  
 1110 orbits.

1111

1112



1113

1114 Fig. 5. (a) Daily counts of SMAP Tb observations assimilated into L4\_SM during April 2015 to

1115 March 2017, including H-pol and V-pol data from ascending and descending orbits. (b) Mean of

1116 the corresponding O-F and O-A Tb residuals, where the mean values are computed separately for

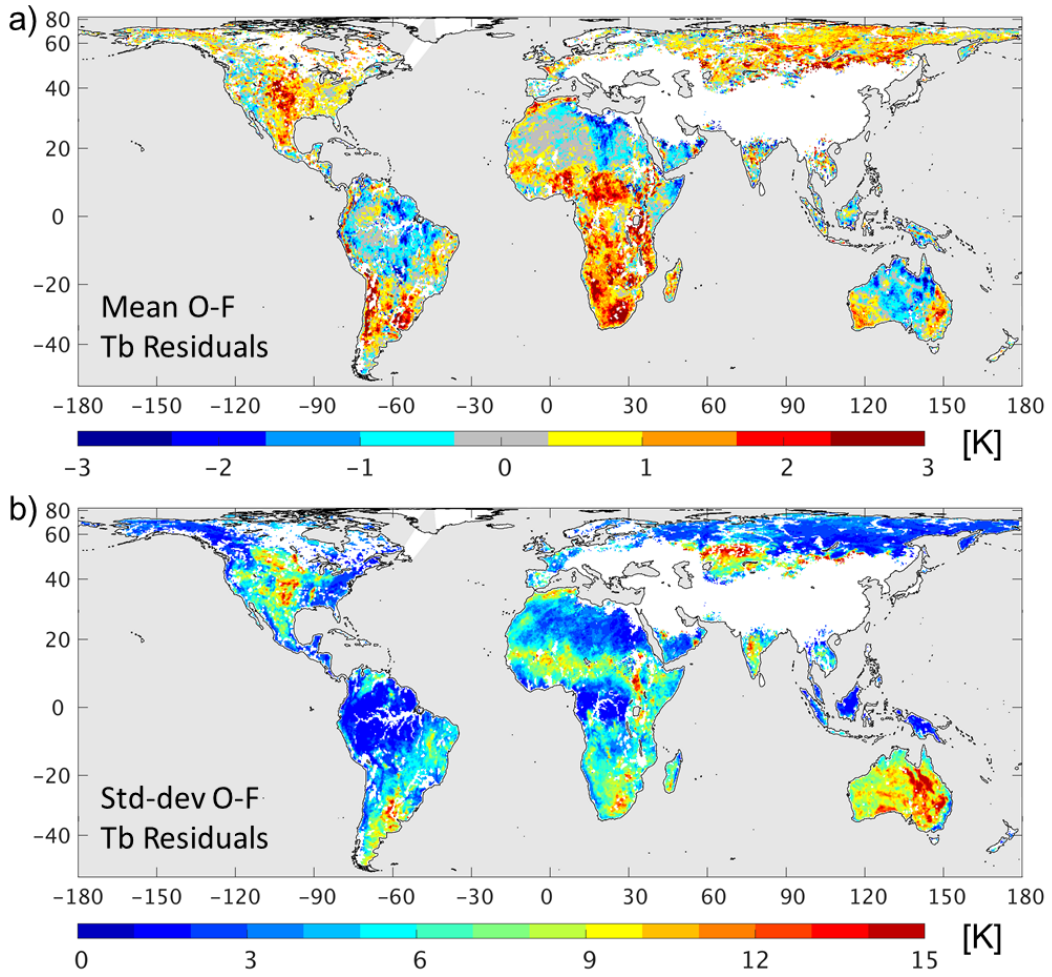
1117 each 3-hourly analysis by averaging across the global land domain (where SMAP observations

1118 are assimilated) and then averaging the resulting values over the 8 analysis times for each day.

1119 (c) As in (b) but for the standard deviation. Vertical grid lines indicate the first day of each

1120 month.





1121

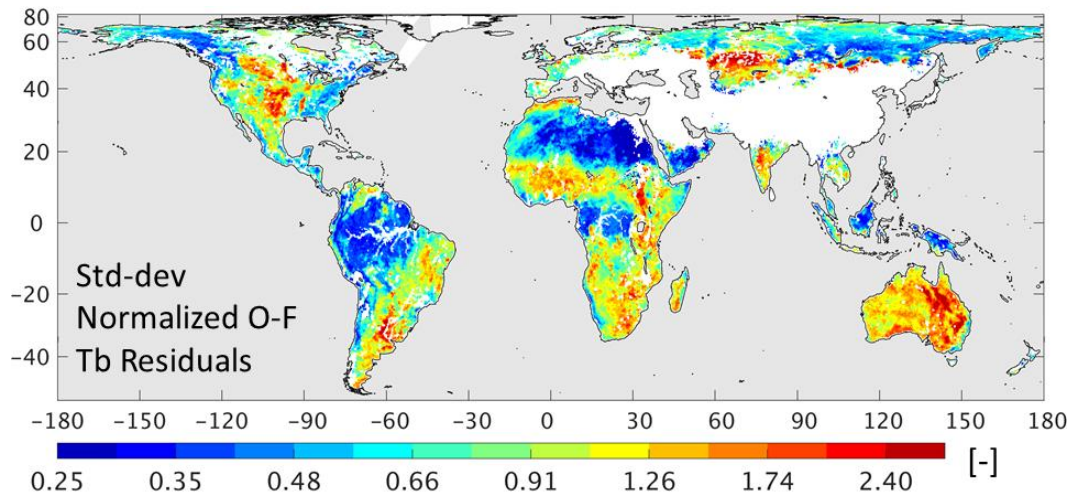
1122 Fig. 6. (a) Mean and (b) standard deviation of the O-F Tb residuals from the L4\_SM algorithm

1123 for April 2015 to March 2017.

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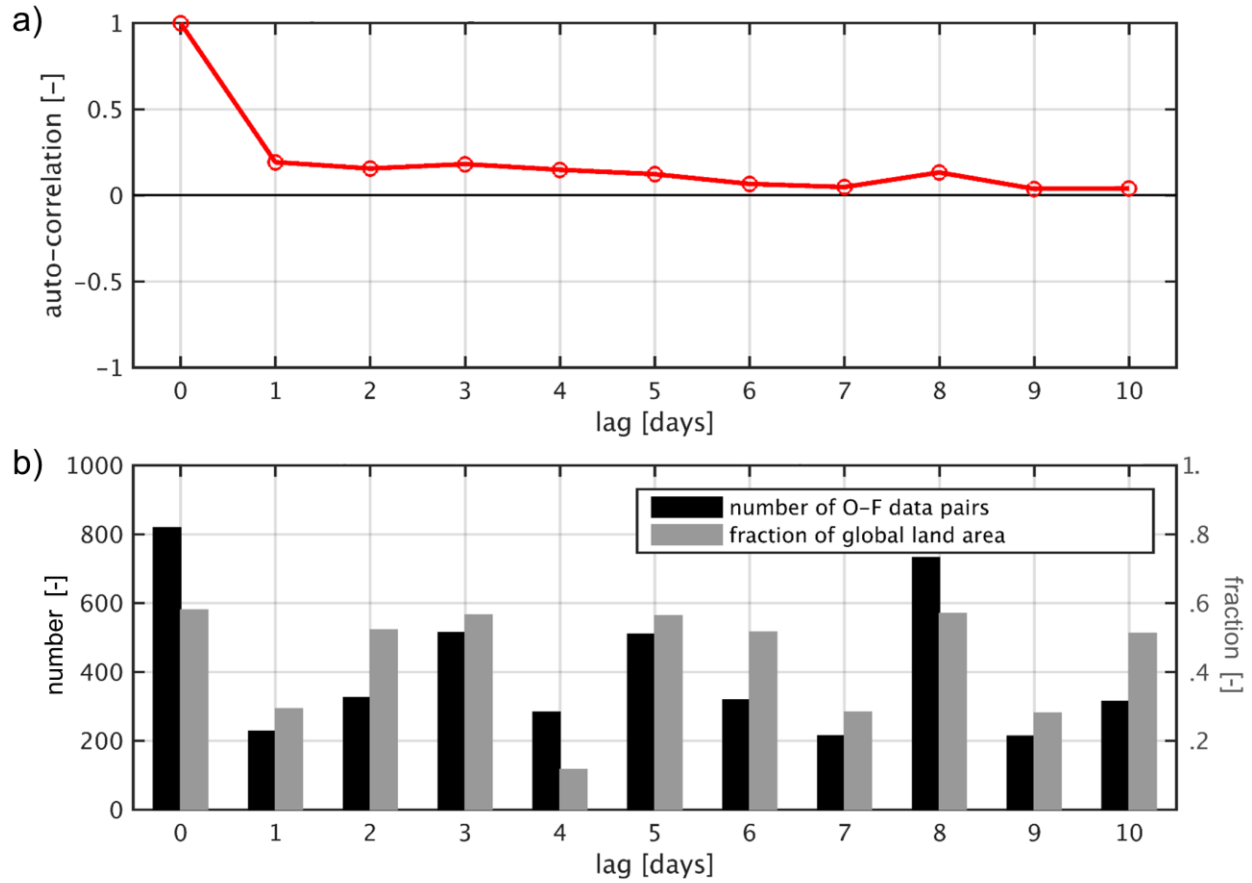
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1128 Fig. 7. Standard deviation of the *normalized* O-F Tb residuals from the L4\_SM algorithm for  
 1129 April 2015 to March 2017.

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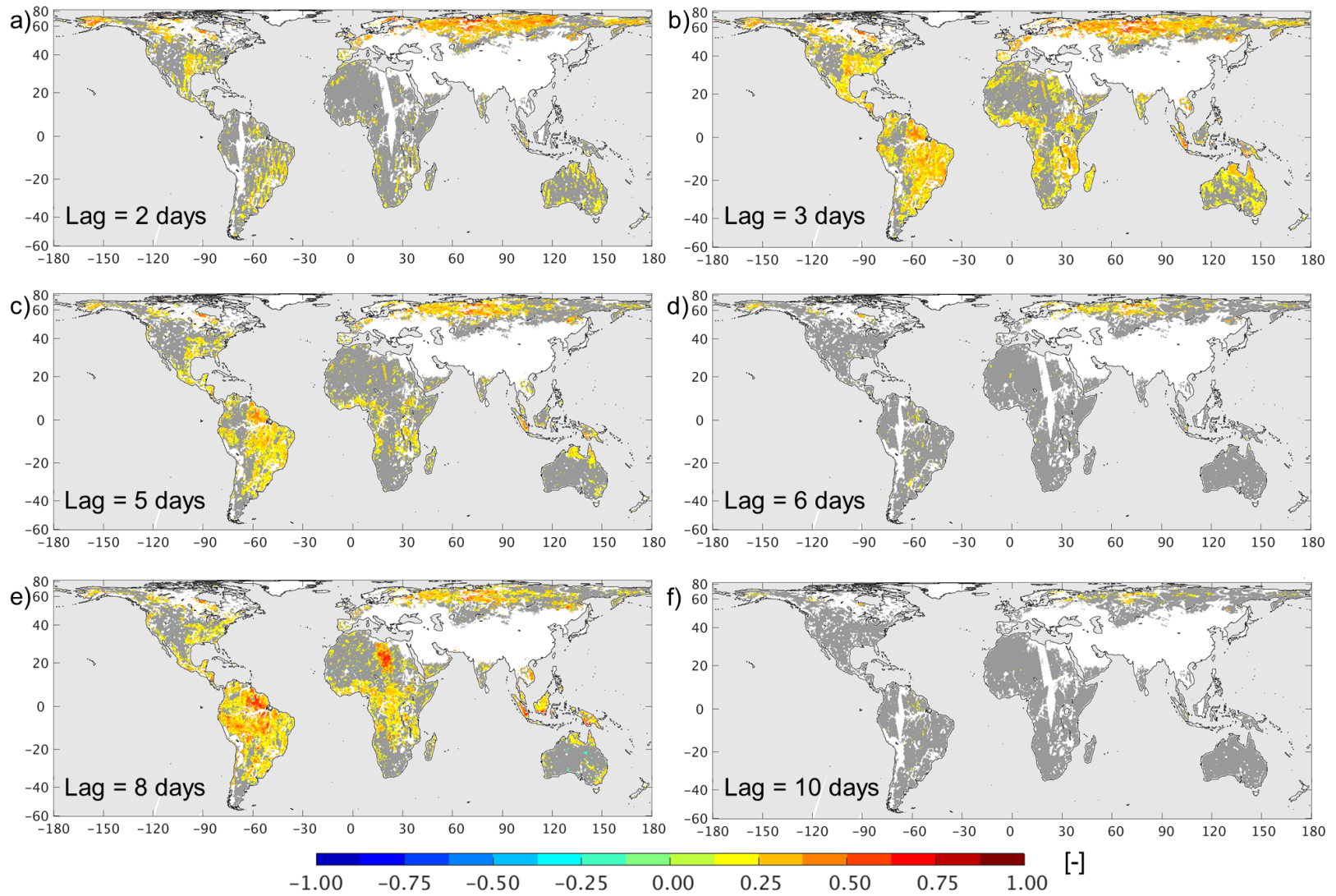


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1132 Fig. 8. (a) Spatially averaged, lagged sample auto-correlation of the O-F Tb residuals. (b)

1133 Average number of O-F data pairs at each grid cell (black; left axis) and fractional area coverage

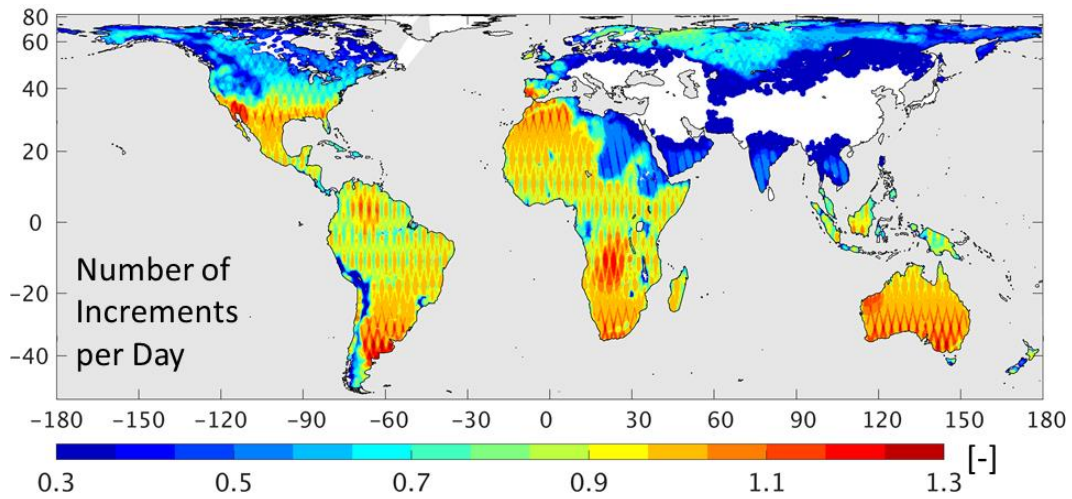
1134 (gray; right axis) contributing to the sample auto-correlation values.



1135

1136 Fig. 9. Sample auto-correlation of the O-F Tb residuals at (a) 2-day, (b) 3-day, (c) 5-day, (d) 6-day, (e) 8-day, and (f) 10-day lag.

1137 Values that are not significantly different from zero (at the 5% level) are shown in gray.



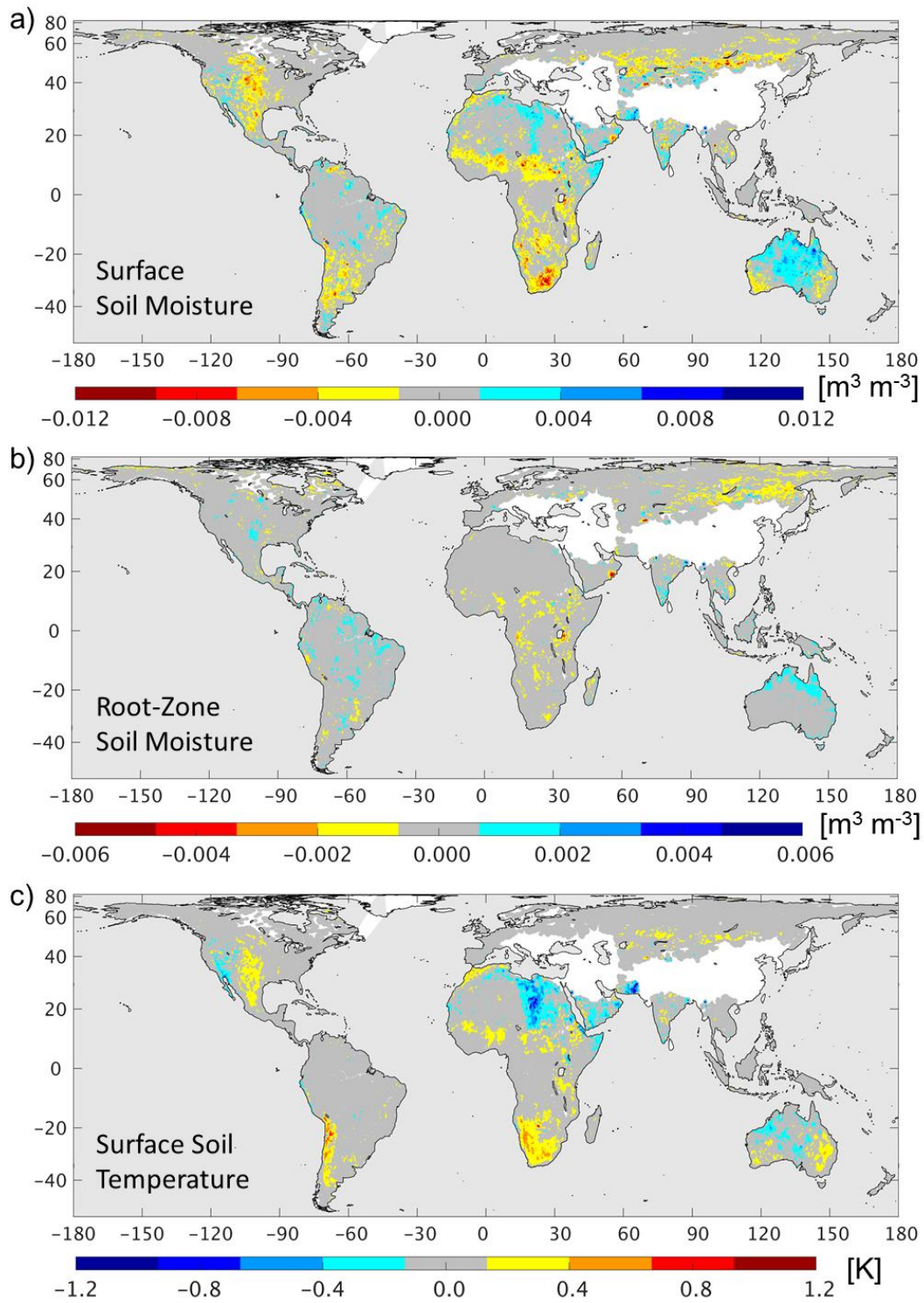
1138

1139 Fig. 10. Average number of increments per day generated by the L4\_SM algorithm during April  
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 1142 temperature, and surface (layer-1) soil temperature.

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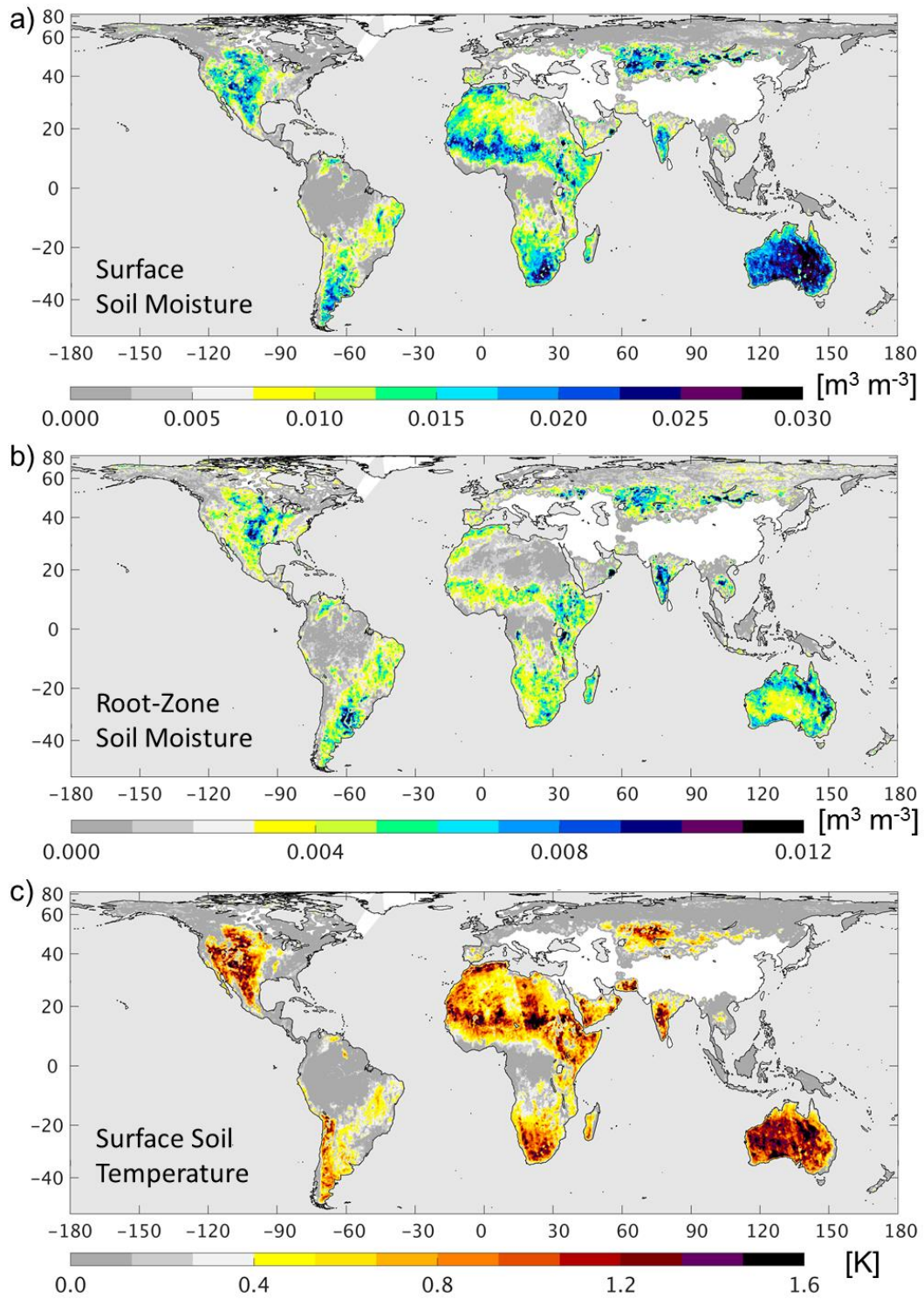
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Fig. 11. Time series mean of the increments for (a) surface soil moisture, (b) root-zone soil moisture, and (c) surface (layer-1) soil temperature from the L4\_SM algorithm for April 2015 to March 2017.



1149

1150 Fig. 12. Same as Figure 10 but for time series standard deviation of the increments.