Effects of Frequency Dependence of the External Quantum Efficiency of Perovskite Solar Cells

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Abstract

Perovskite solar cells are known to show very long response timescales, in the order of milliseconds to seconds. This generates considerable doubt over the validity of the measured external quantum efficiency and consequently the estimation of the short circuit current density. We observe a variation as high as 10% in the values of the EQE of perovskite solar cells for different optical chopper frequencies between 10 – 500 Hz, indicating a need to establish well-defined protocols of external quantum efficiency measurement. We also corroborate these values and obtain new insights regarding the working mechanisms of perovskite solar cells from intensity modulated photocurrent spectroscopy measurements, identifying the evolution of the external quantum efficiency over a range of frequencies, displaying a singular reduction at very low frequencies. This reduction in external quantum efficiency is ascribed to additional resistive contributions hindering charge extraction in the perovskite solar cell at short circuit conditions, which are delayed because of the concomitant large low-frequency capacitance.
The external quantum efficiency (EQE) is a central characterization tool to estimate the performance of a photovoltaic cell. It is defined as the ratio of number of collected electron-hole pairs to the number of photons impinging on the device.\textsuperscript{1} The EQE provides information on how efficiently the solar cell is able to absorb a photon, generate an electron-hole pair, separate and subsequently extract these carriers at respective selective contacts. It can also provide device parameters such as the short-circuit current ($J_{sc}$) and in some cases even the diffusion length, depending upon the dominant transport mechanism. An example being the diffusion-recombination model for dye sensitized solar cells\textsuperscript{2} which allows discerning transport from recombination time. Traditionally, the EQE is measured at short circuit (SC) by applying a monochromatic AC small perturbation in light intensity and measuring the response of the solar cell, subsequently scanned over the range of wavelengths of incoming light. The solar cell is kept under a DC biasing white light intensity that can range from 5 -100 mW·cm\textsuperscript{-2} during the measurement,\textsuperscript{3} although in most cases of collection efficiency measurements, the bias intensity is very low, between 5-10 mW·cm\textsuperscript{-2},\textsuperscript{4,5} whose main purpose is to provide a small background charge density to raise the conductivity of the solar cell from its minimal dark value.

The modulation frequency of the AC small perturbation in light intensity is determined by an optical chopper\textsuperscript{6} and is assumed to be much lower (a few hundred Hz)\textsuperscript{7-9} than the frequency associated with the processes of carrier generation, transport, recombination (lifetime) and charge storage mechanisms, and hence should not have an influence on the measured EQE. However, the validity of this assumption is not assured in the case of perovskite solar cells (PSCs). PSCs are known to show responses at very long timescales in the order of milliseconds to seconds, observed in both voltage and current evolution, which has been confirmed from a wide variety of experiments such as open-circuit voltage ($V_{oc}$) decay,\textsuperscript{10} stepped voltage scans\textsuperscript{11} and current decay from photoinduced charge extraction (PI-CE) measurements.\textsuperscript{12} This has also been observed in the EQE, which has been seen to evolve over timescales of minutes in both dark and light conditions,\textsuperscript{11,13} making the estimation of the $J_{sc}$ very difficult.\textsuperscript{14} Furthermore, a large capacitance of the order of mF cm\textsuperscript{-2} has been observed from impedance spectroscopy (IS) measurements at SC,\textsuperscript{15} similar in magnitude to that observed at open-circuit (OC) conditions,\textsuperscript{16} which is likely related to the aforementioned EQE evolution. Therefore, a clarification regarding the nature of EQE evolution in perovskites and its contributing factors is required to better understand its operation and limiting mechanisms at SC and ascertain the validity of the EQE obtained at a given state of the perovskite solar cell.

We first provide a general definition of the EQE as obtained from standard experimental practices. Let $j_e$ be the extracted photocurrent density while the maximal current density $j_\Phi = q \Phi$ is defined from $\Phi$, the input photon flux at a given wavelength $\lambda$, and $q$ the elementary charge. The steady state EQE, $\text{EQE}_{PV-SS}$, is

$$\text{EQE}_{PV-SS} = \frac{j_e}{j_\Phi}$$

The overhead bars indicate conditions of steady state. A traditional experimental
method termed the differential spectral response method, EQE_{PV-DIFF}, involves the measurement of the photocurrent at SC upon application of a small low frequency AC perturbation of monochromatic light (using an optical chopper) to the sample, which is illuminated by a DC bias white-light intensity. Under an applied small perturbation of light intensity $j_\phi = j_e + J_\phi$, we can write

$$E_{QE_{PV-DIFF}} = \frac{j_e}{j_\phi} \approx \frac{d j_e}{d j_\phi}$$

Equation 2 is an approximation because it assumes an infinitely slow (zero frequency) perturbation, while realistic measurements involve frequencies in the range of a few hundred Hz imparted by the optical chopper.

For the sake of generality, a power-law relationship can describe the most common dependences of collected current on photon flux as:

$$j_e(\lambda) = k j_\phi^n(\lambda)$$

where $n$ accounts for a power-law exponent and $k$ is a proportionality constant. This is because we are normally interested in the variation of EQE over several decades of photon flux from which $n$ is readily derived. Thus we have

$$E_{QE_{PV-DIFF}} = n k j_\phi^{-n-1}$$

We also corroborate the EQE_{PV-DIFF} values with IMPS measurements, which involve the measurement of modulated extracted photocurrent versus modulated input photon current density. The transfer function of IMPS is given by

$$Q(\omega) = \frac{j_e(\omega)}{j_\phi(\omega)}$$

Because of the modulated character of both input and output signals, one can expect in-phase and out-of-phase components of the transfer function, similarly to that occurring when measuring impedance spectroscopy. This implies the complex (real and imaginary) form of the IMPS measurement so that $Q = Q' + iQ''$, whose low-frequency limit is purely real and it is given by

$$Q(0) = \frac{d j_e}{d j_\phi}$$

which corresponds to the definition in Equation 2 provided that $\omega = 0$. Therefore, the EQE_{PV-DIFF} value ideally approximates the low frequency limit of the IMPS transfer function. We note that the measurement of EQE_{PV-DIFF} from direct measurements (differential spectral response method) and from IMPS measurements are identical in the sense that they are both small perturbation methods, the only difference being that the AC perturbation in direct measurements is generated using an optical chopper with the incident light beam, whereas the AC light perturbation in IMPS is generated by driving an AC current through the light source using a potentiostat. In both cases, it is ensured
that the light perturbation acting on the solar cells is the same in the full range of light intensities and frequencies. The other difference is in their application, since IMPS is usually considered as a frequency-resolved method to obtain kinetic information. However, from the point of view of EQE analysis, we can use both approaches in combination.

The above mentioned definitions are summarized in Table 1. By comparing Equations 1 and 4, we can see that the values of EQE obtained from small-perturbation methods and steady-state methods converge only if the relationship between extracted photocurrent and input photon flux is linear.

**Table 1** Definition of external quantum efficiency according to the measurement procedure. In the differential spectral response method, the output is a function of the optical chopper frequency, as indicated.

<table>
<thead>
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<th>EQEPV-SS</th>
<th>Steady state measurement</th>
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<td>EQEPV-DIFF</td>
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We now proceed to identify the trends of EQE evolution with input photon current density in perovskite solar cells and to clarify the above described methods of EQE measurement. Figure SI1a and SI1b show the J-V curve of the perovskite solar cell tested and its corresponding maximum photocurrent. In addition to measuring EQEPV-DIFF directly, we also obtain the value indirectly using the following methods. The first method involves determination of EQEPV-SS from steady state measurements of extracted photocurrent density for a given input photon current density. We then obtain EQEPV-DIFF from the slope of the data obtained from the steady state measurements, as shown in Equation 2. The second method involves measurement of IMPS spectra and extracting the EQEPV-DIFF value, which corresponds to the low-frequency limit of the transfer function, as shown in Equation 6. Both EQEPV-SS and IMPS measurements were carried out using a blue light (470 nm) source in order to avoid effects relating to absorption losses (see Figure SI2 for absorption spectrum).
Figure 1 (a) Evolution of extracted photocurrent versus input photon current density from steady state measurements (the inset shows the low intensity region) (b) IMPS spectra for different DC bias blue light intensities expressed as current density as shown in legend. (c) Evolution of EQE as defined from small perturbation methods (EQEPV-DIFF), obtained from steady state measurements (red) and IMPS (orange), and steady state method (green) (EQEPV-SS). (d) log-log plot of data in (a) to obtain the exponent $n$ in Equation 3. All measurements carried out with monochromatic radiation of wavelength 470 nm.

Figure 1a shows the evolution of steady state extracted photocurrent versus photon current density, from which the values of EQEPV-SS and EQEPV-DIFF are calculated, shown in Figure 1c. While EQEPV-SS values show a gradual rise to reach a constant value, the EQEPV-DIFF values are almost constant through the entire range of photon current densities. It can be seen that the values of EQEPV-DIFF and EQEPV-SS converge to similar values only
at high photon current densities. Since EQE measurements are usually carried out at low light intensities (and hence photon current densities), it is clear that the values of EQE will be quite different depending on the employed measuring method. Figure 1b shows the corresponding IMPS spectra of the perovskite solar cell obtained at different photon current densities. The spectra typically show two arcs in the upper quadrant, corresponding to high and intermediate frequencies, followed by a low-frequency arc in the lower quadrant, whose origins are discussed later on. For now, we observe that the low frequency limit of the IMPS spectra matches quite nicely with the values of EQEPV-DIFF obtained from the slope of the steady state measurements as seen in Figure 1c.

As mentioned earlier, the divergence in values of EQEPV-DIFF and EQESS depend on the exponential factor $n$ in Equation 1. This factor is obtained from a log-log plot of $j_e$ versus $j_0$, shown in Figure 1d. We can clearly distinguish two regimes of behavior. The first regime occurs at low photon current densities, where the relationship is highly non-linear with $n = 2.8$, while at higher photon current densities, the evolution is almost linear with $n = 1.1$. Therefore, the values of EQEPV-DIFF and EQESS collapse only at higher photon current densities. The existence of these regimes can be attributed to the strong photoconductive behavior in perovskites. At high light intensity, a linear behavior is observed as expected, but the low conductivity values near dark conditions$^{18,19}$ reduces charge collection and photocurrent values, so that the strong non-linear dependence at low light intensities (in Fig. 1e) is likely influenced by collection efficiency issues.

We now proceed to clarify the validity of Equation 2 for perovskite solar cells by measuring the effect of the optical chopper frequency on the EQEPV-DIFF values. The EQEPV-DIFF was measured with and without DC white light bias at five different optical chopper frequencies of 500, 400, 286, 110 and 14 Hz. Figure 2a and 2b shows the variation in EQEPV-DIFF without and with a 10 mW·cm$^{-2}$ DC white light bias at a given frequency of the optical chopper with respect to the values at 500 Hz, which is used as reference. We observe that the EQEPV-DIFF increases upon lowering the optical chopper frequency in both cases, with a maximum increment of 8-10% in EQEPV-DIFF from 500 Hz to 110 Hz. At lower frequencies (14 Hz) the EQEPV-DIFF drops. This strong frequency dependence describing a response peak is also reflected in the IMPS spectra of Figure 2c that shows high frequency and intermediate arcs in the first quadrant followed by a low frequency arc in the fourth quadrant. The evolution of the real part of the IMPS transfer function is shown in Figure 2d. It shows a maxima at high frequency ($\sim$10$^4$ Hz) and another at low frequency ($\sim$1Hz), with very little evolution in between. After the second maxima, it then drops sharply for very low frequencies. It is then evident that both techniques (EQEPV-DIFF and IMPS) exhibit similar evolution with the perturbation frequency. This is because EQEPV-DIFF and $Q'$, the real part of IMPS, provides information on the effective extracted photocurrent at a given perturbation frequency.
Figure 2 Variation in $\text{EQE}_{\text{PV-DIFF}}$ at (a) 0 DC white light bias and (b) 10 mW·cm$^{-2}$ DC white light bias for different optical chopper frequencies with respect to spectra measured at 500 Hz. (c) IMPS spectra measured at 33 mA·cm$^{-2}$ DC blue light bias and (d) Evolution of real part of IMPS transfer function versus frequency at 470 nm.

In general, the value of $\text{EQE}_{\text{PV-DIFF}}$ obtained from direct measurements is in fact the real part of the IMPS transfer function at the given optical chopper frequency, as mentioned earlier. For the simplest model of a solar cell, consisting of a recombination resistance ($R_{\text{rec}}$) and a chemical capacitance ($C_\mu$) coupled in parallel with a current source, and a series resistance ($R_s$), the IMPS response is an arc in the upper quadrant and the real part of the IMPS transfer function is a frequency-dependent process, containing the ratio between the frequency $\omega$ associated to the time constant $\tau = R_s C_\mu$ and the applied frequency (see SI for derivation). In this case,
\[ Q'(\omega) = \frac{Q(0)}{1 + Q(0)^2 (\omega/\omega_c)^2} \]  

(7)

where the low frequency intercept has the value

\[ Q(0) = \left(1 + \frac{R_s}{R_{rec}}\right)^{-1} \]  

(8)

This can be understood by observing the equivalent circuit of the simple solar cell model at SC shown in Figure 3a, with a current source corresponding to photogenerated carriers in parallel to both the recombination resistor and the chemical capacitor. The IMPS response can be viewed similar to an RC attenuator, where the capacitor controls the frequency-dependent response of the extracted photocurrent through the series resistance. Therefore, the IMPS arc is the attenuation of the total photocurrent through the equipotential lines in the circuit. At higher frequencies, the capacitor acts as a short circuit and reduces the flow of current through the series resistance, while at low frequencies, the capacitor behaves as a blocking element and the total current through the series resistance is determined simply by the ratio of magnitudes of the series resistance and the recombination resistance. Therefore, the real part of the IMPS transfer function and hence the EQE_{PV-DIFF} has a maximum at zero frequency corresponding to Equation 8 and reduces with increasing frequency for the simple solar cell model. This leads to the important fact that the EQE_{PV-DIFF} can be frequency independent only when the frequency associated with the time constant \( \tau = R_s C_\mu \) is much larger than the optical chopper frequency employed.
Figure 3 IMPS response at SC and corresponding equivalent circuit for (a) basic solar cell model and (b) perovskite solar cell.

In perovskite solar cells, the IMPS spectra in Figure 1b deviate from the previous simple model, with the observation of a distinctive low frequency arc in the lower quadrant. The high frequency arc can be attributed, as explained earlier, to the time constant formed by the series resistance and a high frequency capacitor, as shown in the equivalent circuit of Figure 3b, which corresponds to that commonly used to analyze impedance spectroscopy responses. The high-frequency capacitance is well established to be the bulk dielectric capacitance of the perovskite. The IMPS low-frequency arc is related to the components in the equivalent circuit as far as the generation of carriers is located exclusively across the high frequency resistor, as calculated using standard electrical network analysis. This creates a delay in the extracted photocurrent through the low-frequency capacitance with respect to the photogenerated current, leading to a response in the lower quadrant. At the low-frequency limit, the separated localization of the current source forces the resistor to act identically as an extra series resistor, which can be seen simply as the basic solar cell model with a net series resistance of \( R_{\text{net}} = R_s + R_{lf} \). This reduces the value of EQE as can be seen from Equation 8, which causes the arc in the fourth quadrant to evolve towards lower EQE values at lower frequencies. Therefore, the evolution of the magnitude of the low-frequency resistor with light intensity is crucial to determine the achievable low frequency EQE values.

In summary, some years back, the drift of efficiencies of perovskite solar cells by hysteresis effects could be identified. An ensuring point to a reliable measurement of performance is to calculate the expected photocurrent from independent EQE measurement. But here, we show that the latter effect can produce a disparity of results. To clarify the question, we provided formal definitions of the EQE for solar cells as can be obtained from steady state measurements or from small perturbation methods. The obtained values can vary strongly from each other depending on the linearity of the relationship between the extracted photocurrent and the input photon flux. The extremely slow response in timescale of seconds of perovskite solar cells at short circuit is inevitably reflected in small perturbation EQE measurements, where variations as high as 10% can be obtained with optical chopper frequencies in the range of 10-500 Hz. Through IMPS measurements, we shed light on the frequency-dependent evolution of the external quantum efficiency, which reaches a maximum at intermediate frequencies followed by a reduction at low frequencies. This low frequency effect is ascribed to the differences in charge generation within the perovskite solar cell. Due to the singular evolution of the
EQE, it is imperative to establish protocols and to provide detailed information regarding the method of measurement. Measurements with several optical chopper frequencies, stated explicitly, are recommended to avoid erroneous estimation of the true EQE.

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