



# Parallel Monotonic Basin Hopping for Low Thrust Trajectory Optimization

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**AIAA/AAS Space Flight Mechanics Meeting**  
**Kissimmee, Florida**  
**January 8-12, 2018**



- **What's the Problem?**
- **What is Monotonic Basin Hopping?**
- **What is Parallel Monotonic Basin Hopping?**
- **Small Example**
- **Medium Example**
- **Large Example**
- **Conclusion**



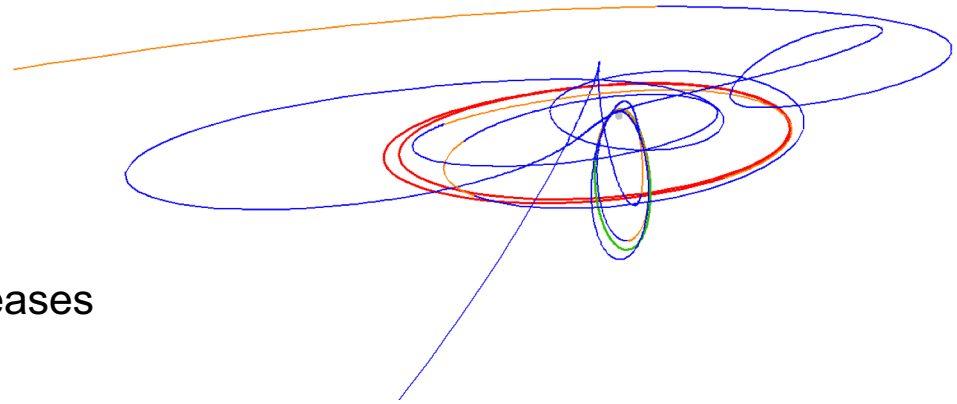
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# What's the Problem?



- **Low thrust trajectory optimization can be tricky:**

- Many locally optimal solutions
- Non-intuitive solutions
- Long integrated finite burns
- Full ephemeris models
- Tedious to design by hand
- This gets worse as complexity increases



- **Questions Arise:**

- Do I really have to locate a feasible solution "by hand"?
- Is there a more optimal solution nearby?
- Can this somehow be done while I'm out to lunch or home for the night?



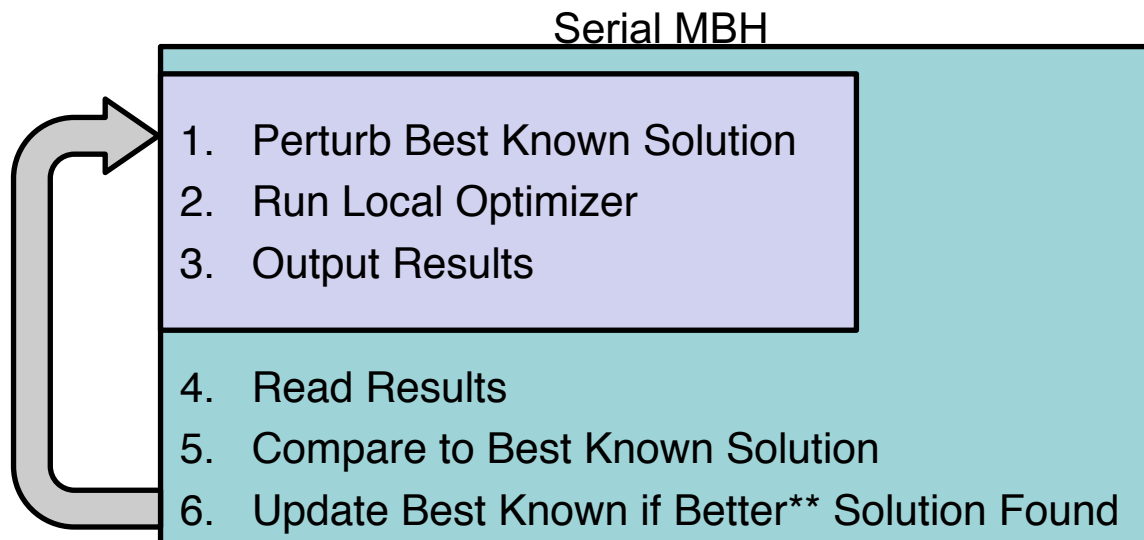


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# Serial Monotonic Basin Hopping (MBH)

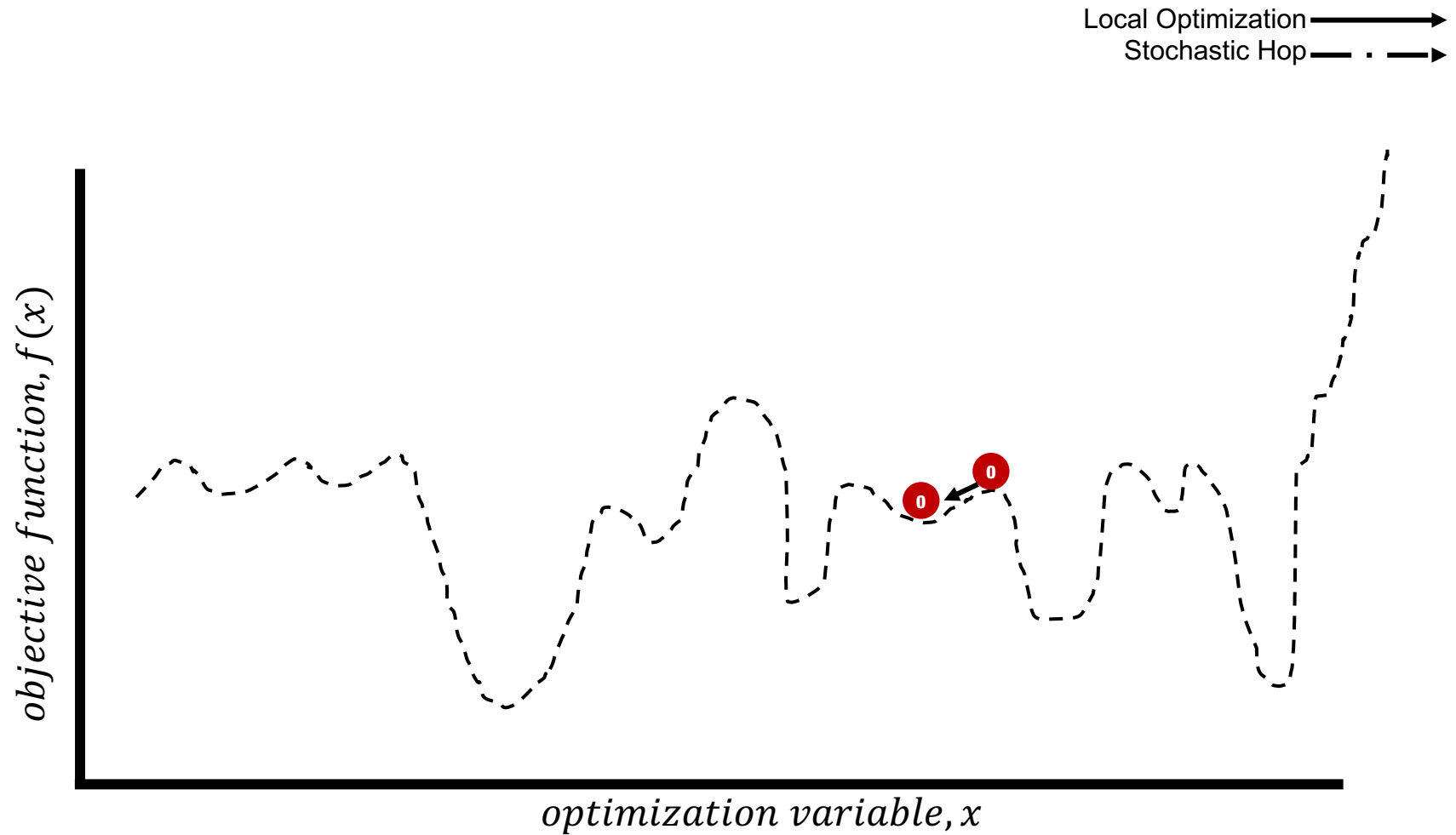


- **Stochastic Global Optimization Meta-algorithm**
- **Robust, Automated**
- **Notable example: Evolutionary Mission Trajectory Generator (EMTG)**

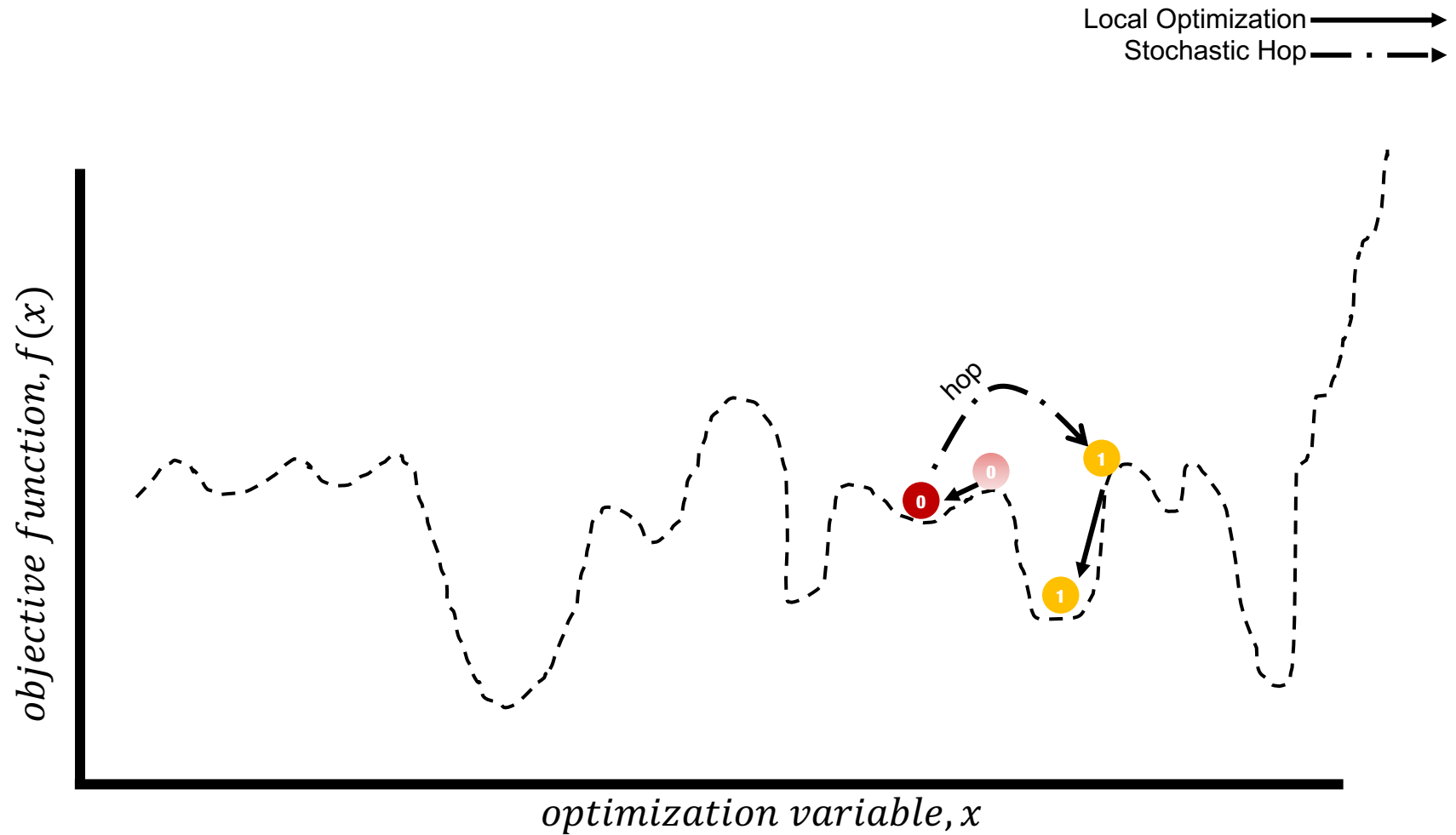


\*\*Better solution can be more optimal OR more feasible

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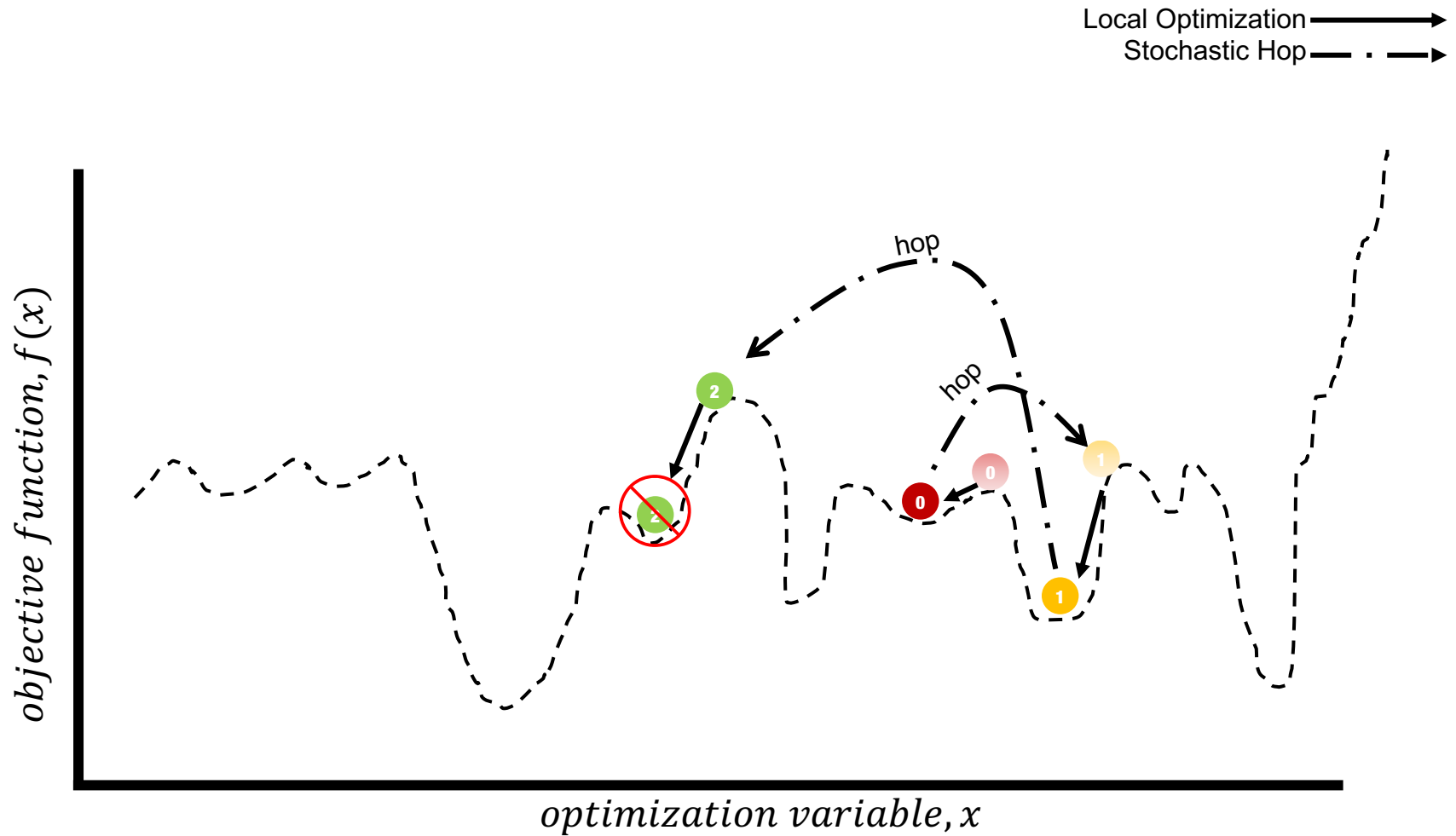


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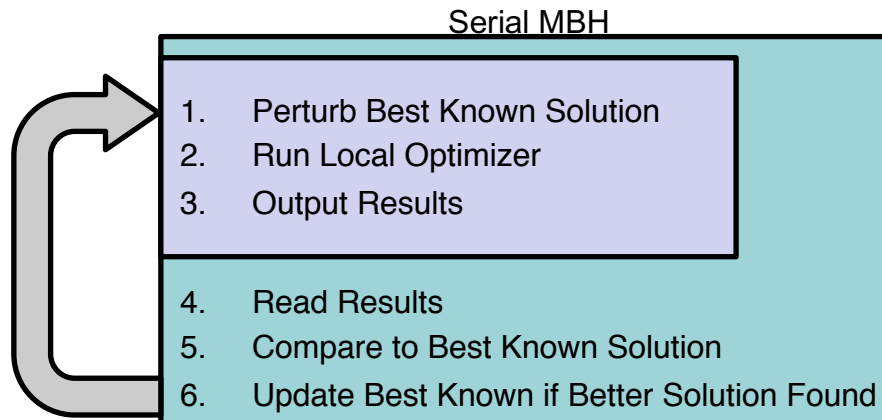
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2. Computation resources are relatively inexpensive

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- **Parallelizing Serial MBH**



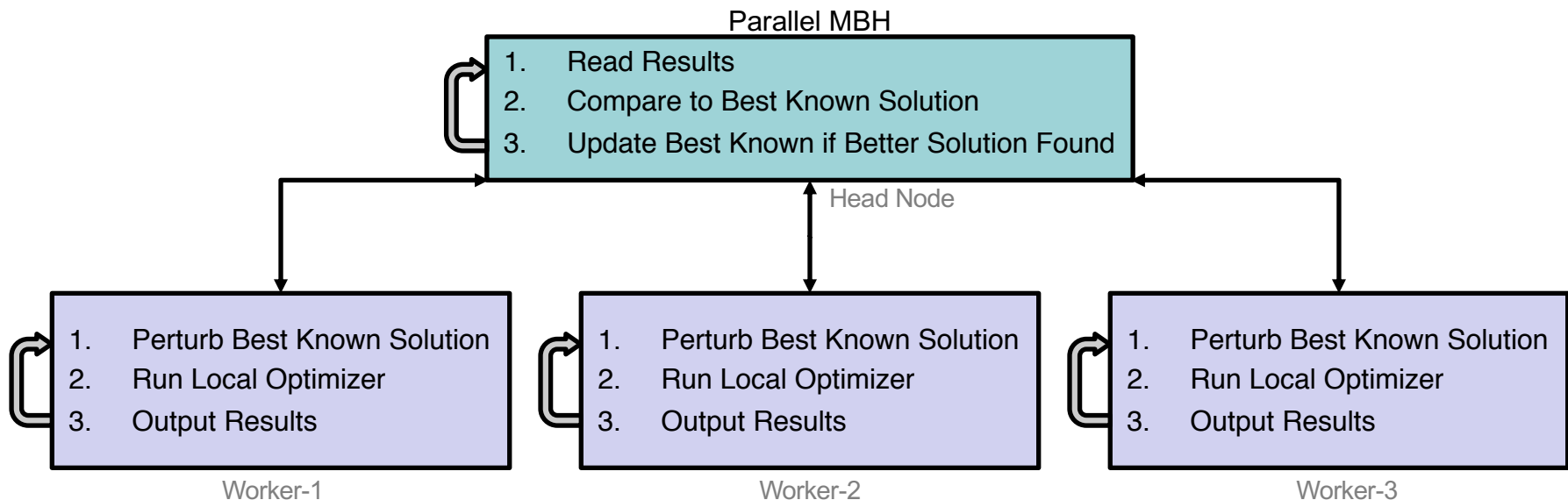
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- **Why Parallel MBH?**

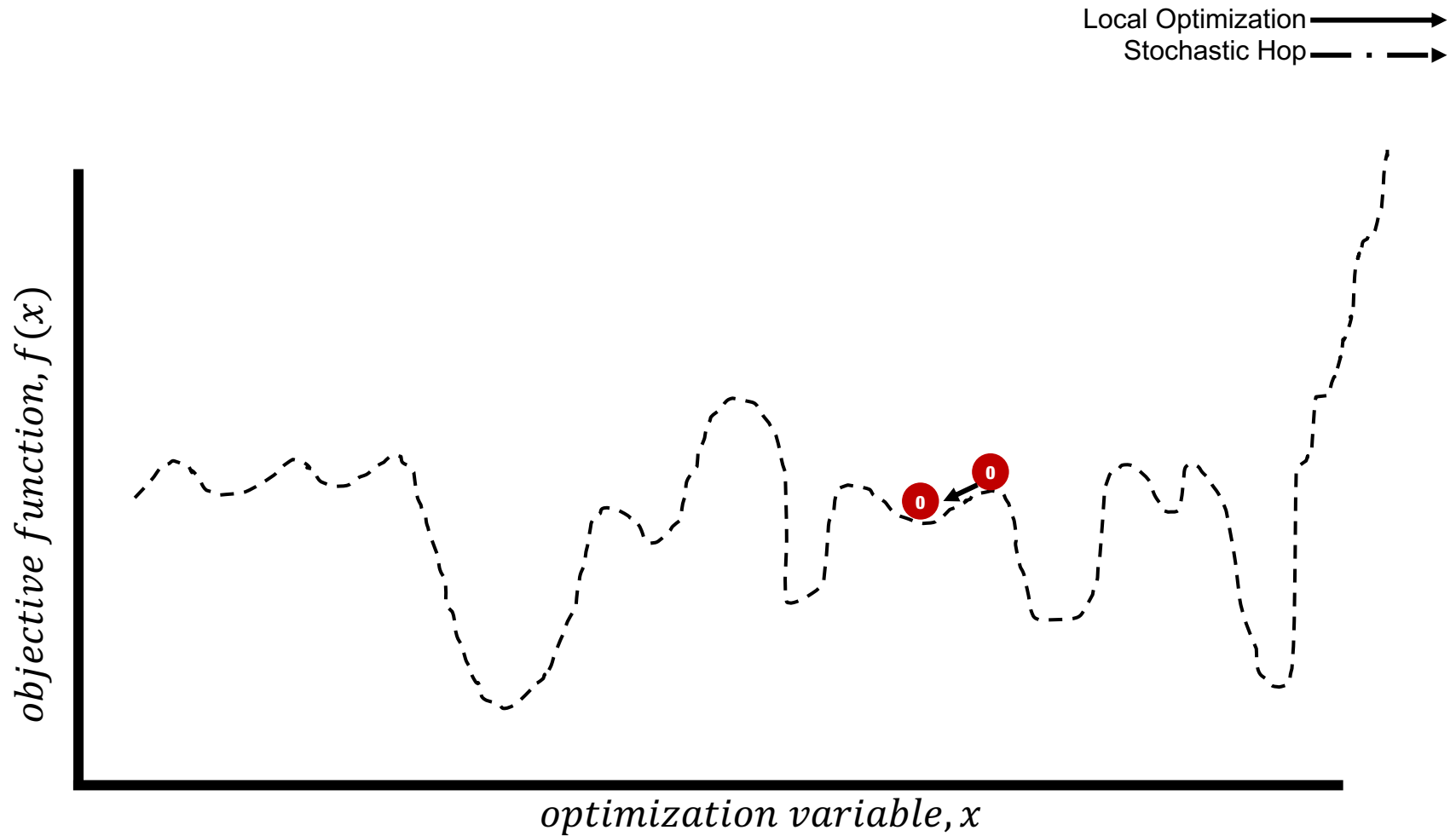
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- **Parallelizing Serial MBH**

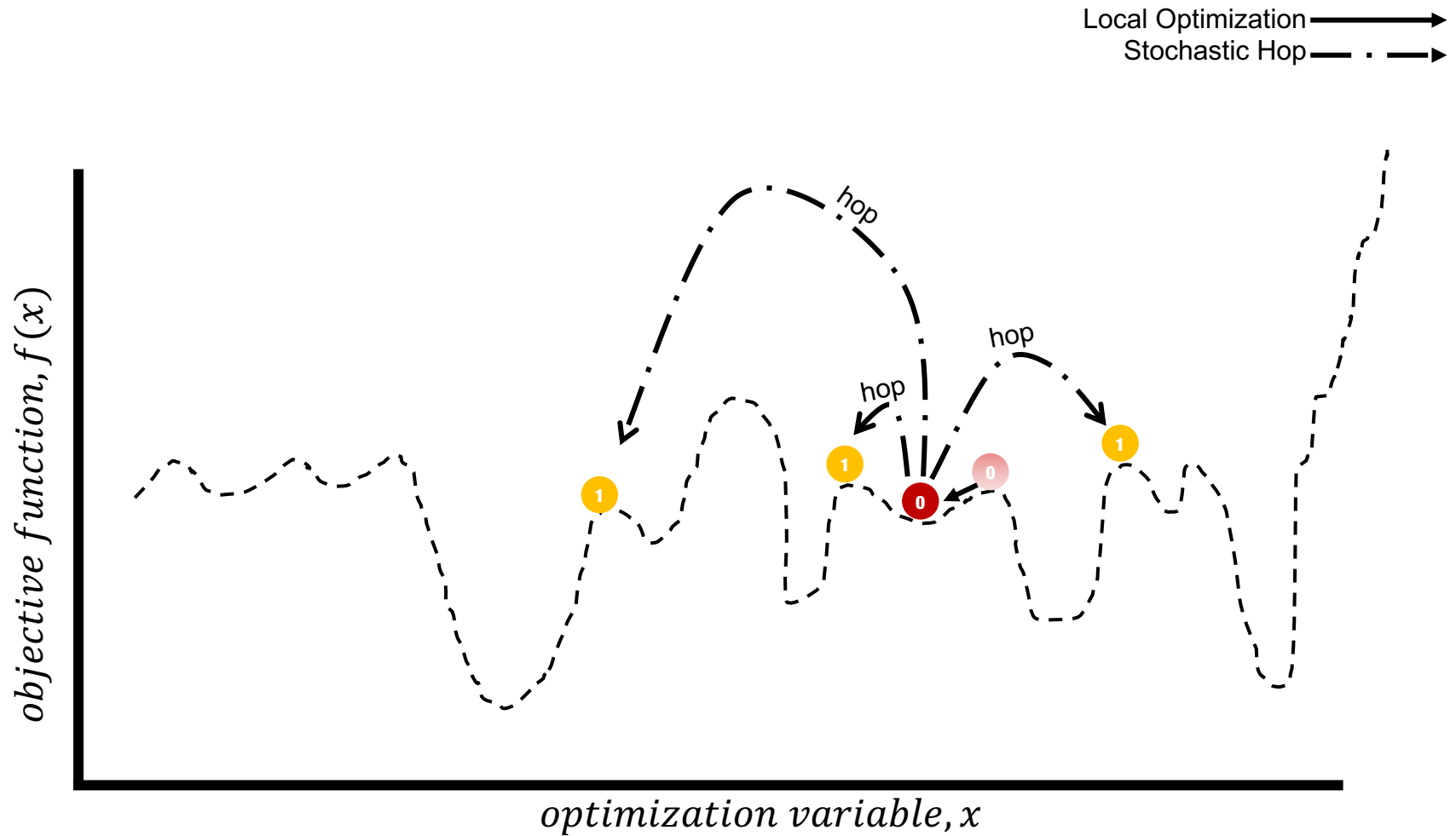




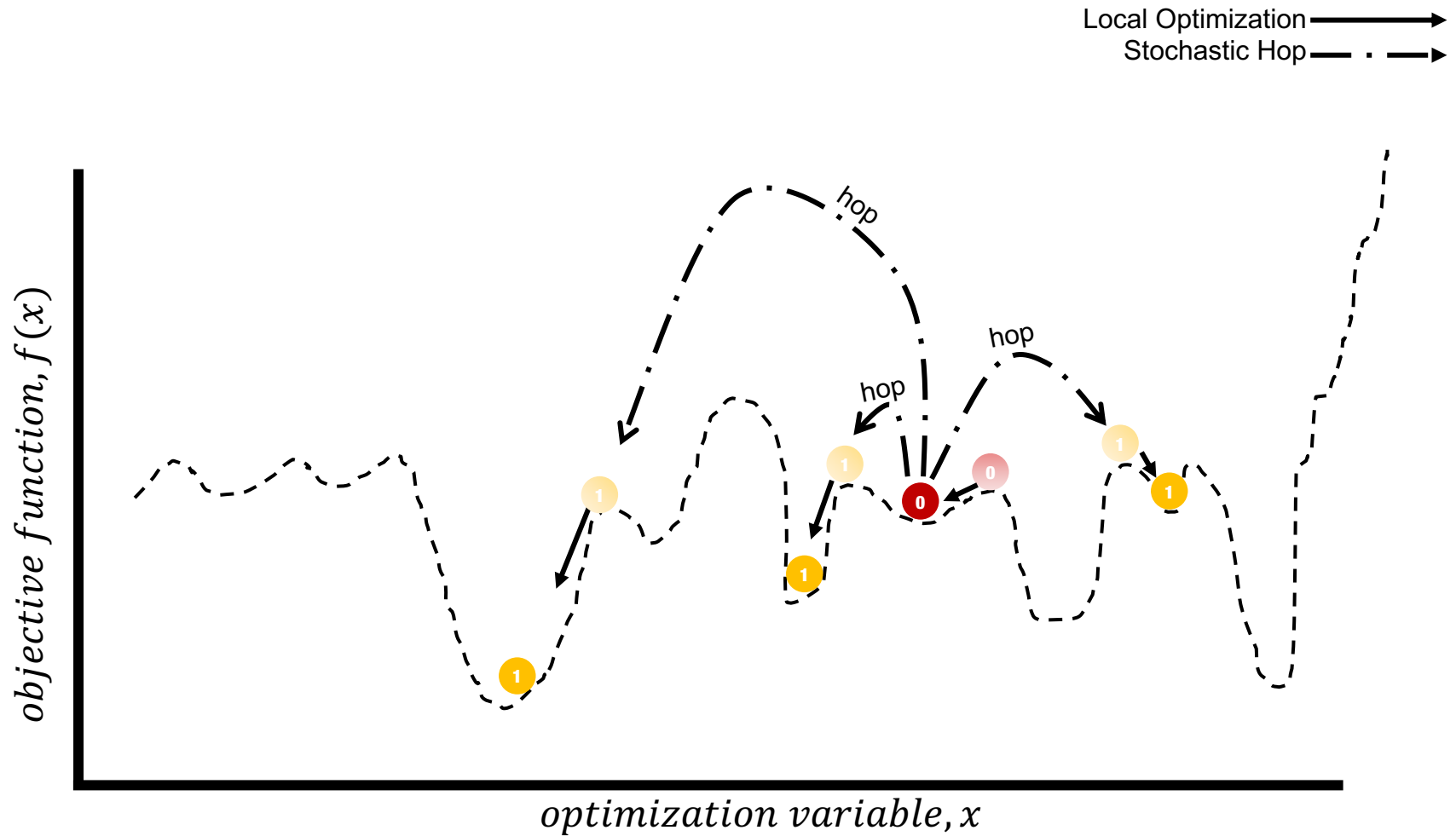
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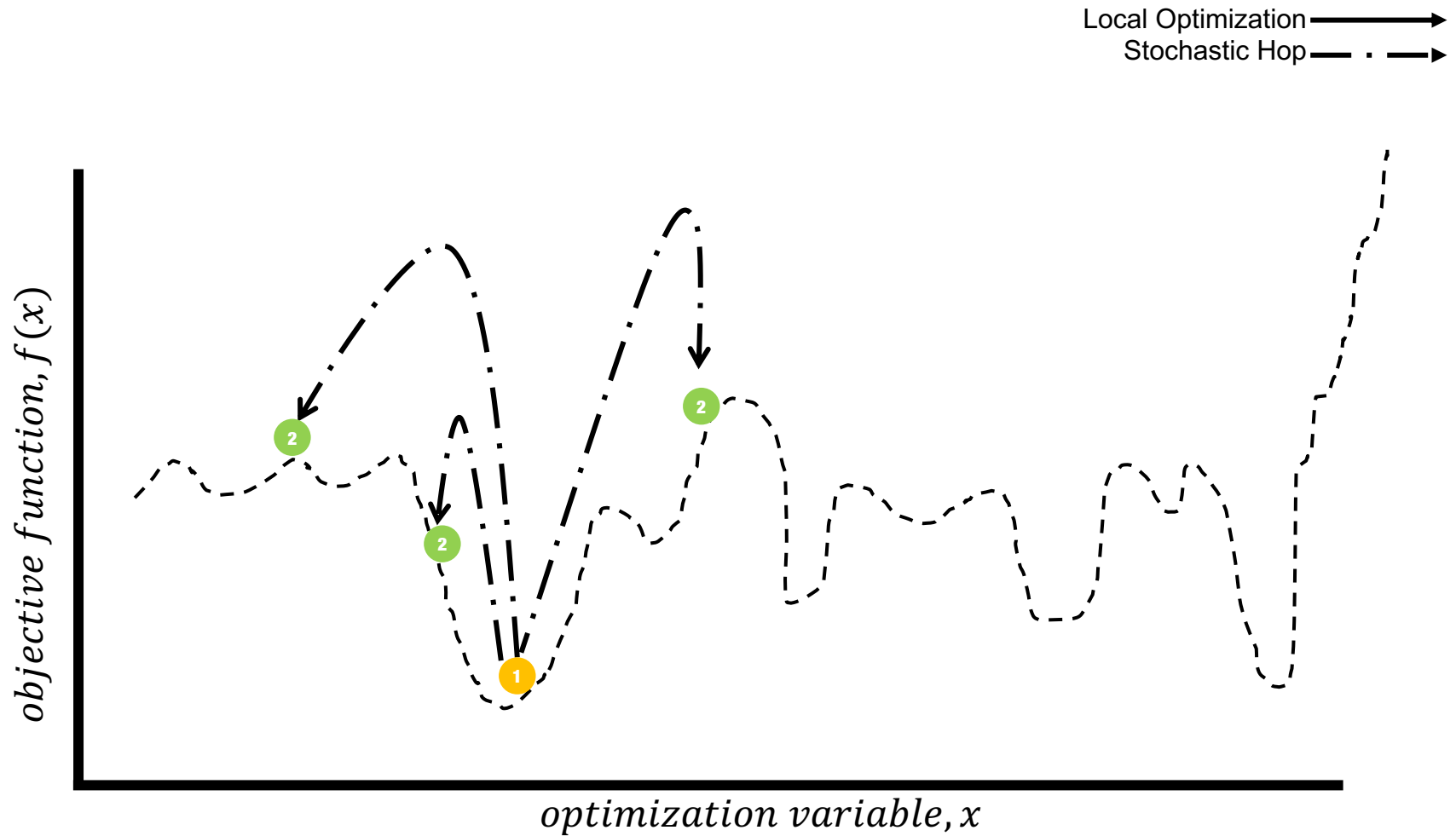
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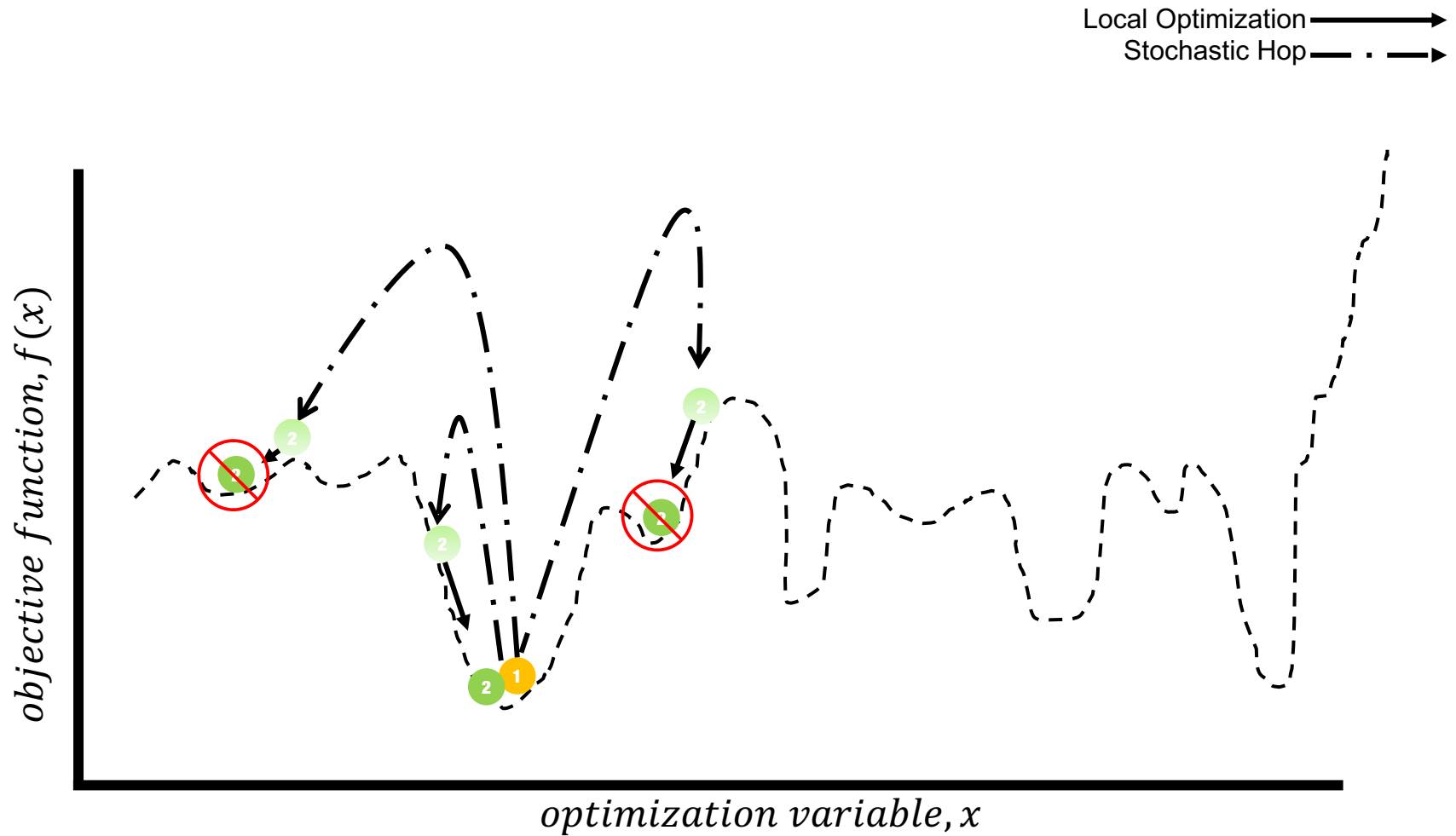
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- **MBH Scripts: Python**
  - Easy to interface with Copernicus
  - Easy to implement in parallel
  - Speed isn't important as most time is spent elsewhere
- **Mission Design Tool: Copernicus**
  - Developed at NASA Johnson Space Center
  - Primary mission design tool used at NASA GRC
  - Enables the formulation of arbitrarily complex trajectories
- **Local Optimization: SNOPT**
  - Built into Copernicus
  - Most of the computational time is spent here





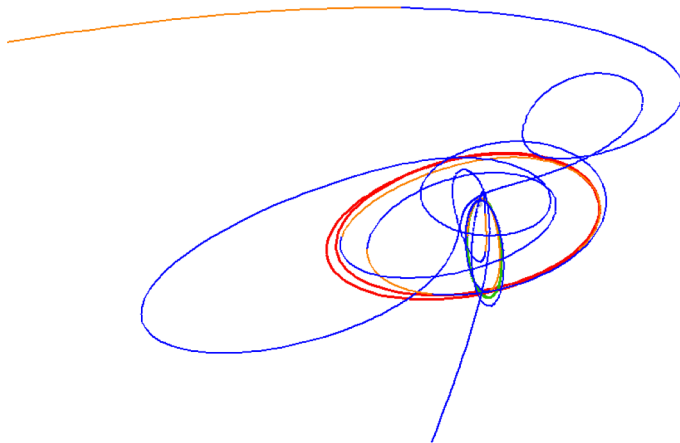
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# Small Example Problem

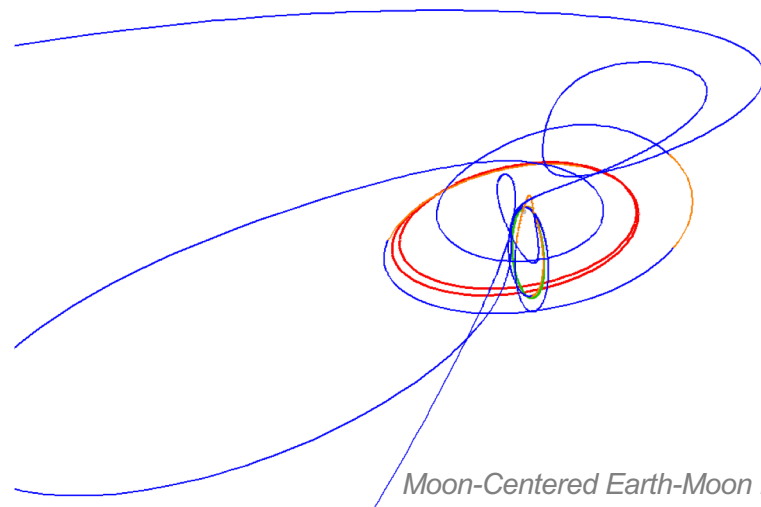


- **Low Thrust Solar Electric Propulsion Transfer**
- **Near Rectilinear Halo Orbit (NRHO) > Lunar Distant Retrograde Orbit**
- **Fully Integrated, Time Varying Finite Burns**
- **150-Day Duration**
- **Minimum Propellant Mass**
- **Serial MBH vs. 27-core PMBH (20 trials each)**

Initial Solution

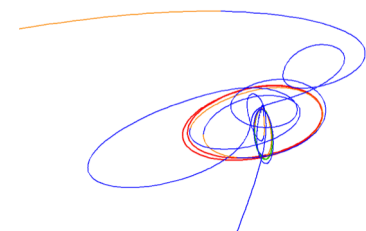
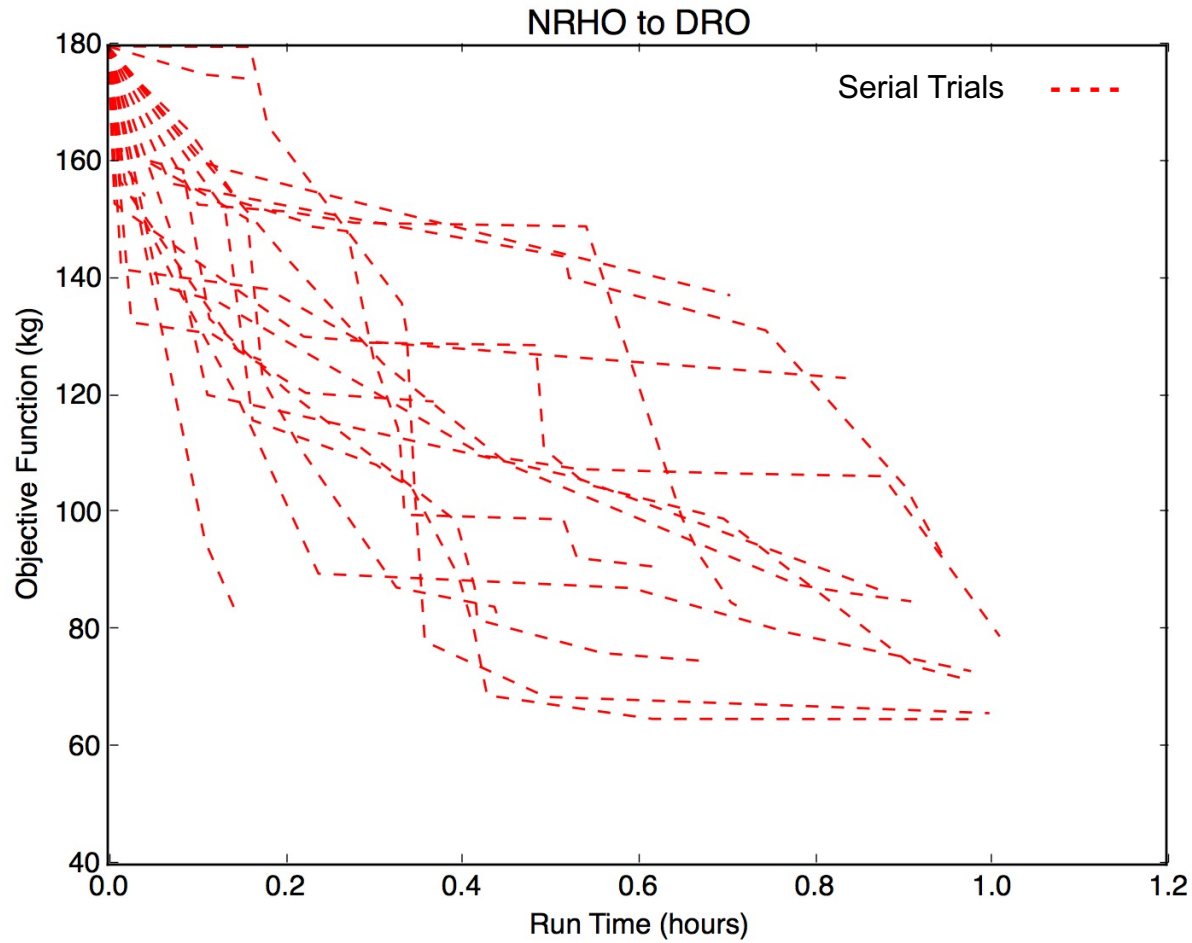


Final Solution

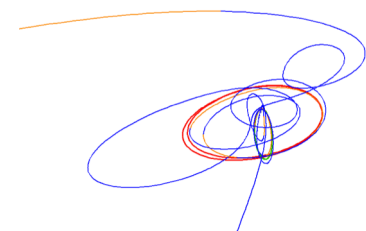
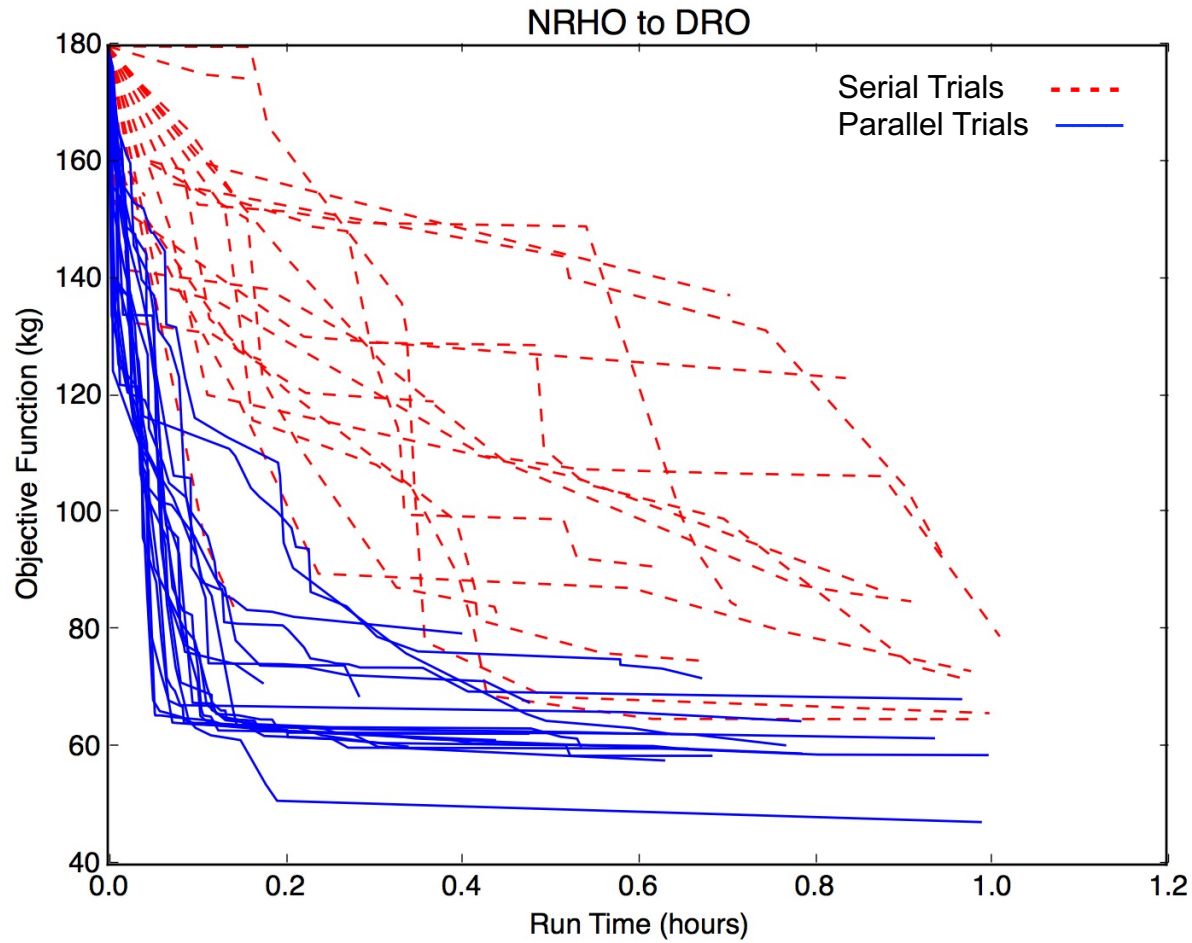


*Moon-Centered Earth-Moon Rotating Frame*

# Small Example Results



# Small Example Results





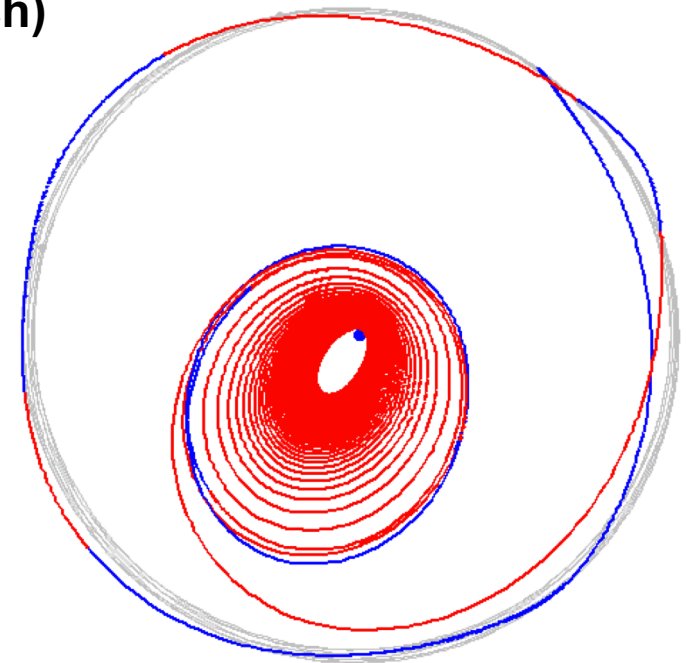


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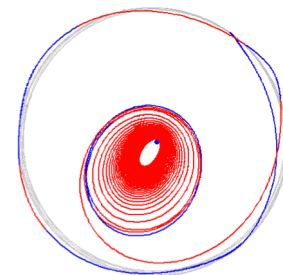
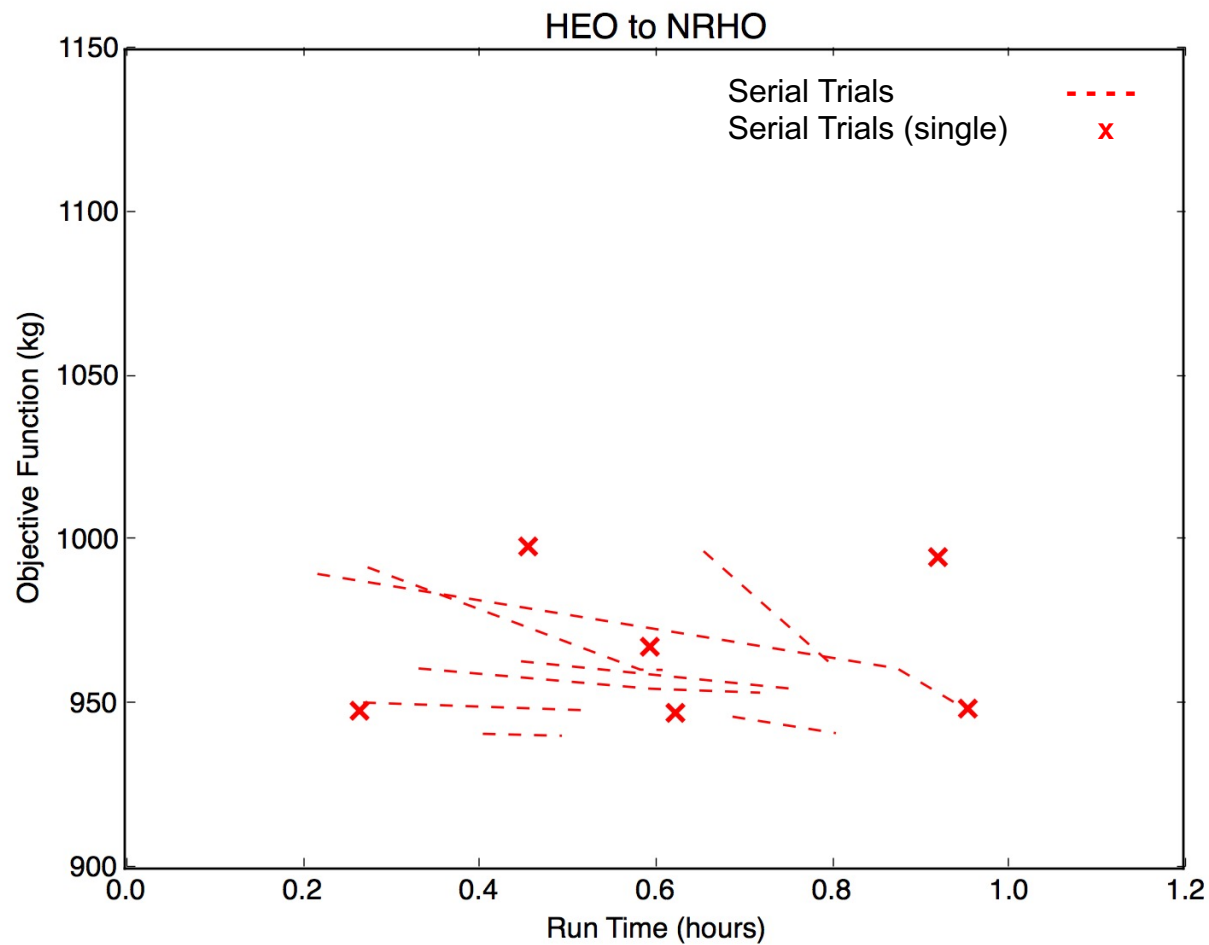
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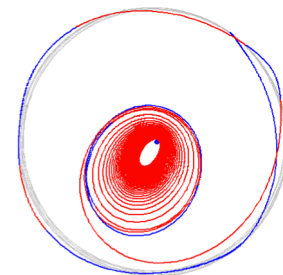
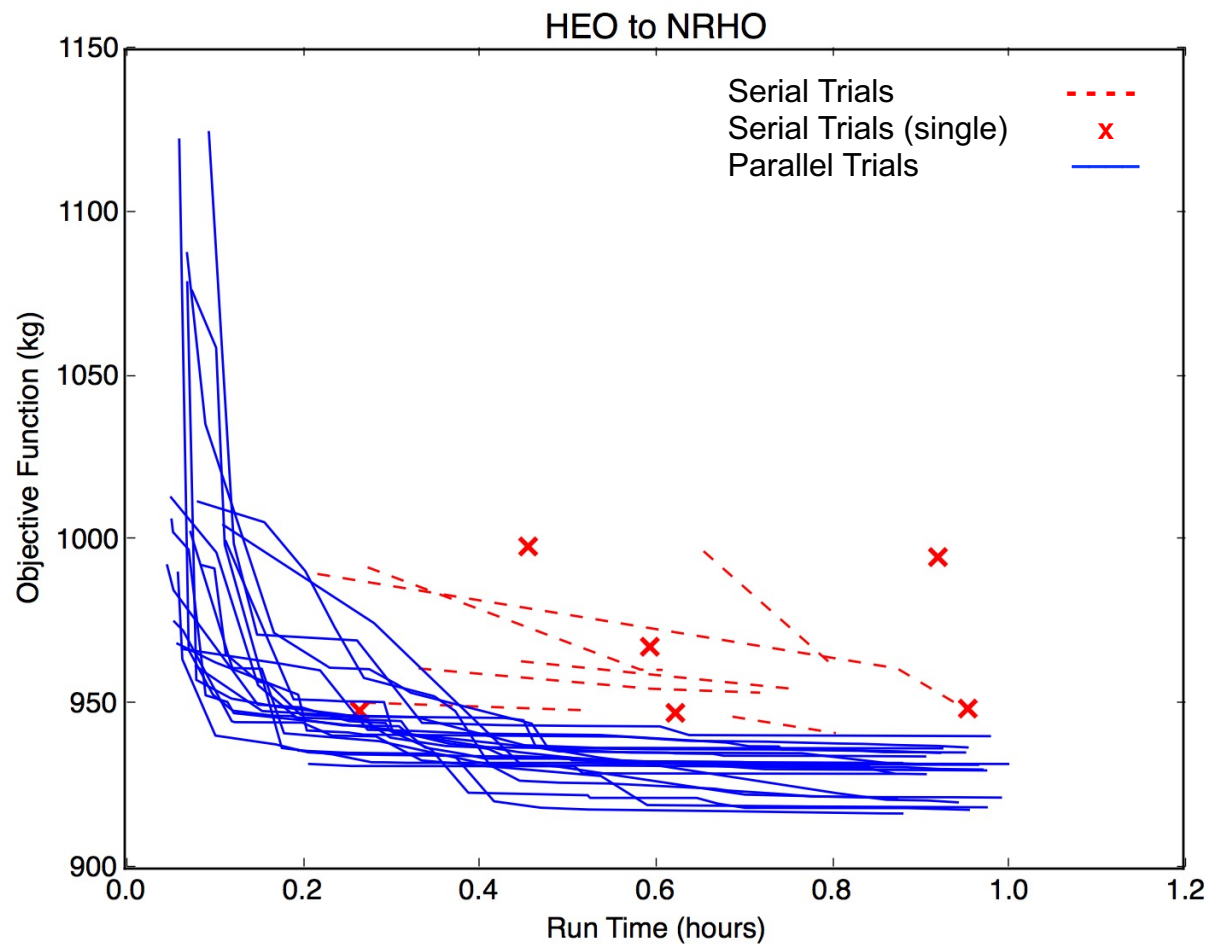
- **Low Thrust Solar Electric Propulsion Transfer**
- **High Earth Orbit > NRHO**
- **Fully Integrated, Time Varying Finite Burns**
- **100+ Day Low Thrust Spiral**
- **Minimum Propellant Mass**
- **Serial MBH vs. 27-core PMBH (20 trials each)**



# Medium Example Results



# Medium Example Results





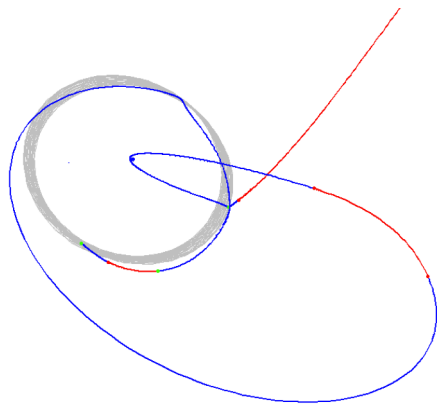
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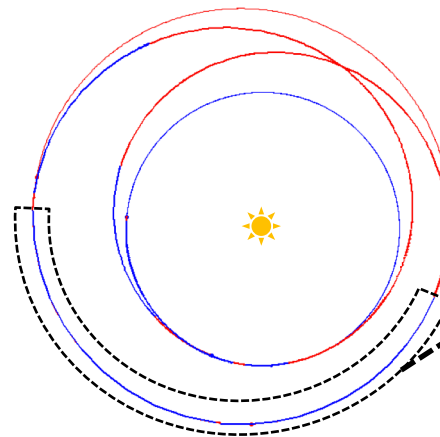
# Large Example Problem



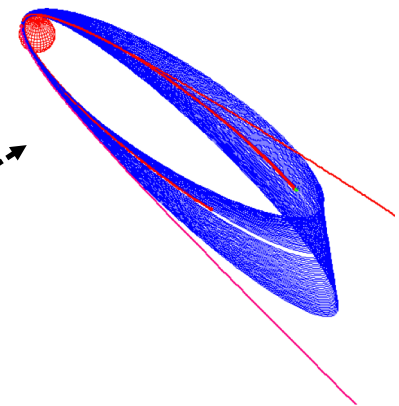
- **Hybrid (SEP + Chemical) Round Trip Mars Mission**
  - Chemical for Earth Departure, Mars Arrival, Mars Departure – SEP otherwise
- **NRHO > LGA Escape > High Mars Orbit > Earth**
- **Fully Integrated, Time Varying Finite Burns**
- **1100+ Day Mission Optimized End-to-End**
- **Minimum NRHO Departure Mass**
- **Serial MBH vs. 27-core PMBH (10 trials each)**



NRHO to LGA Escape

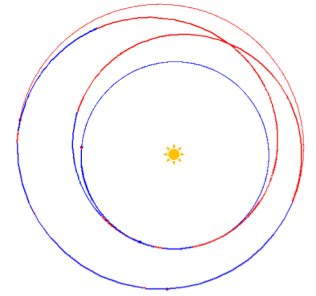
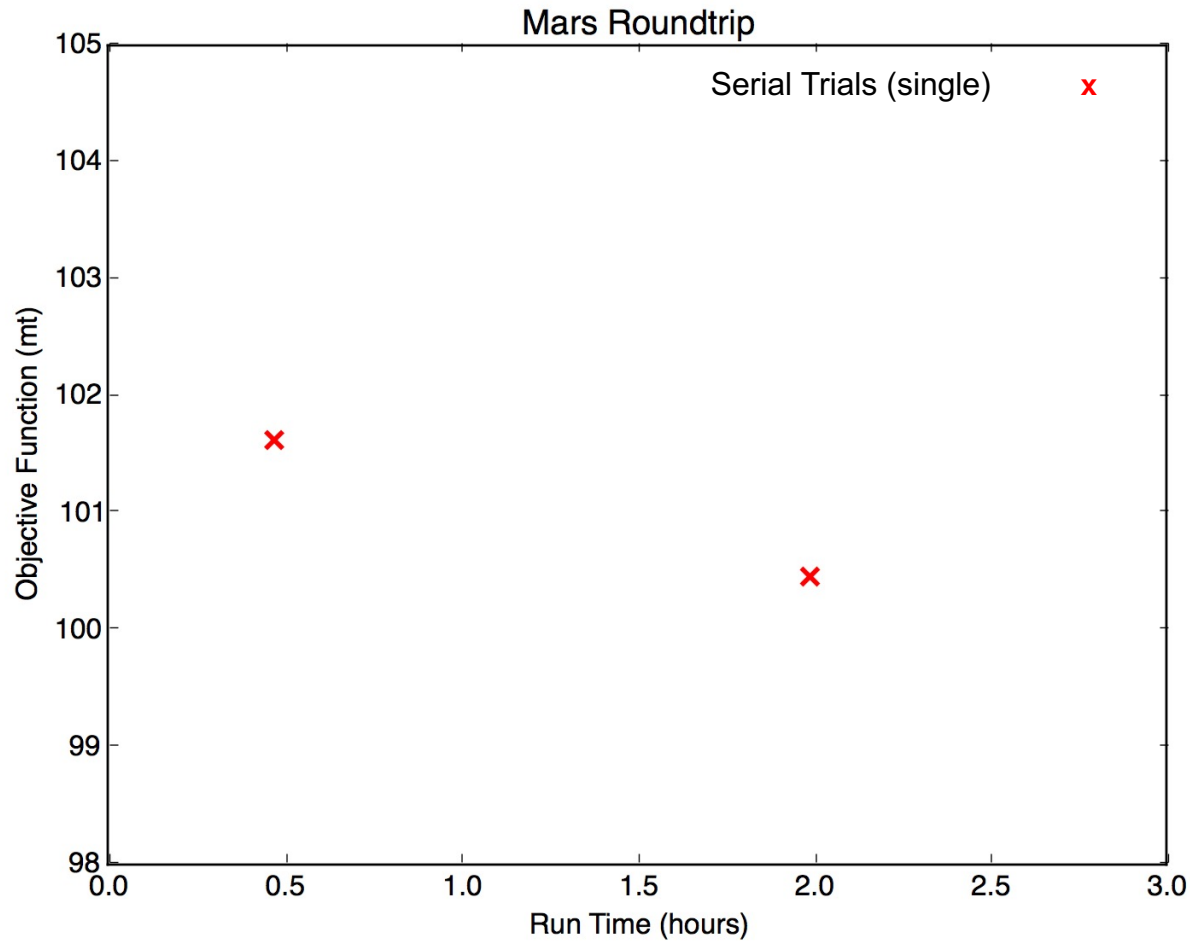


Roundtrip Earth-to-Mars

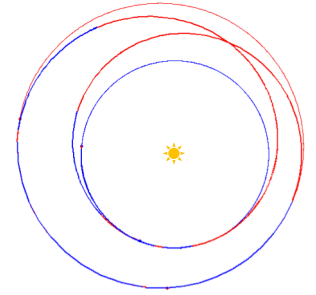
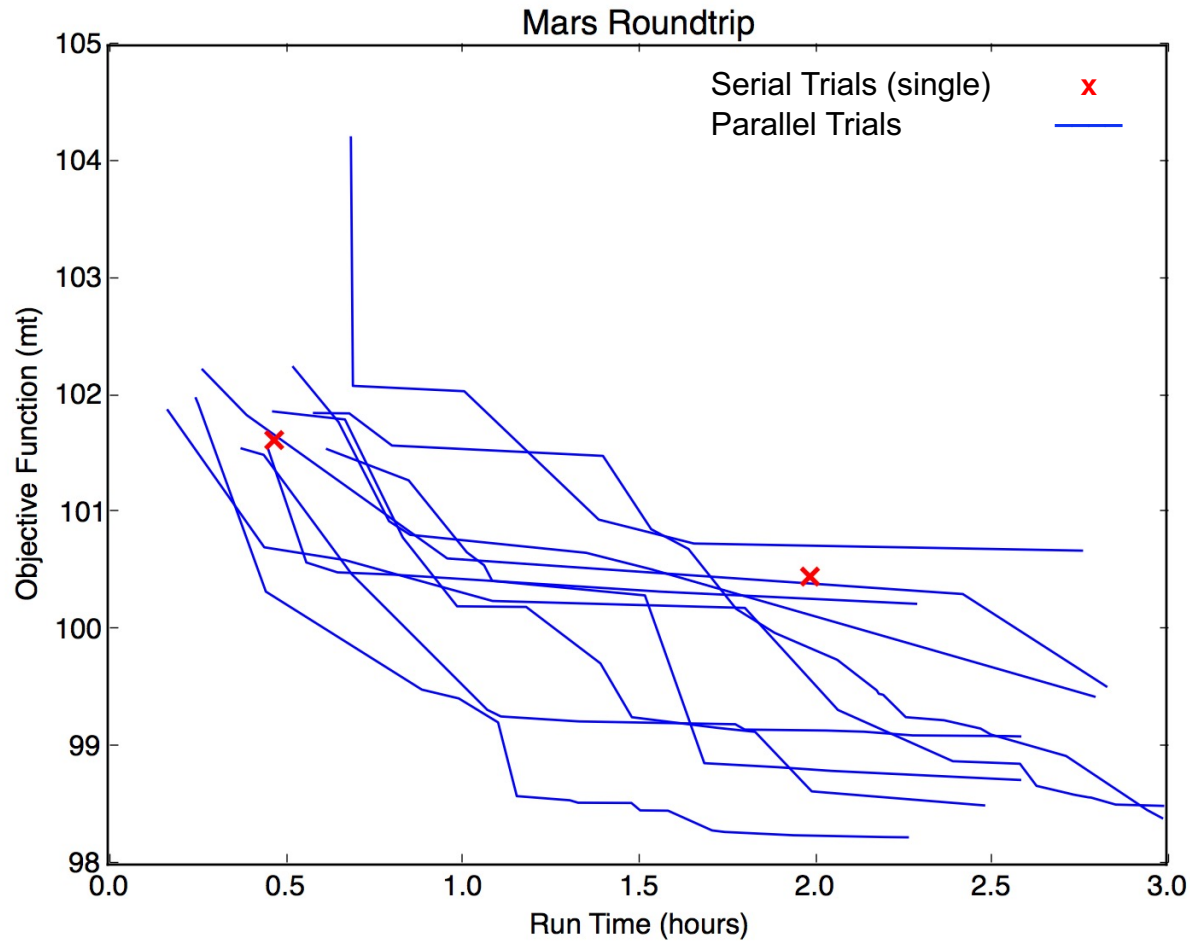


300-days at Mars

# Large Example Results



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1. PMBH can find feasible solutions faster & more reliably
2. PMBH can find more optimal solutions faster & more reliably
3. PMBH can solve problems that are impractical with serial MBH
4. **Questions Answered:**
  - Do I really have to locate a feasible solution "by hand"? **NO.**
  - Is there a more optimal solution nearby? **PROBABLY.**
  - Can this somehow be done while I'm out to lunch or home for the night? **YES.**

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