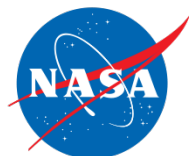


# Influence of Molecular Simulation Model Accuracy on the Interfacial Properties of an Ionic Liquid:

## *Overview of Recommended Practices*

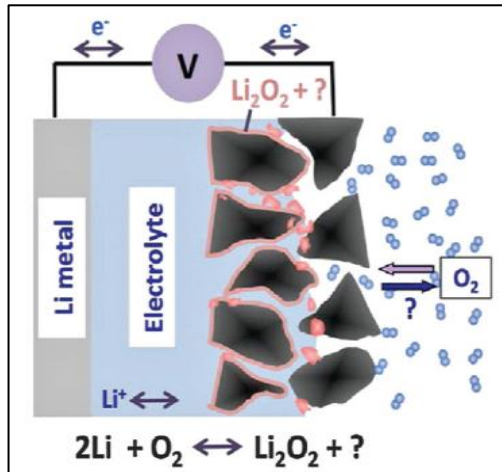
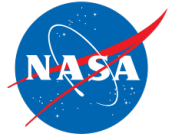


**Justin B. Haskins<sup>1</sup> and John W. Lawson<sup>2</sup>**

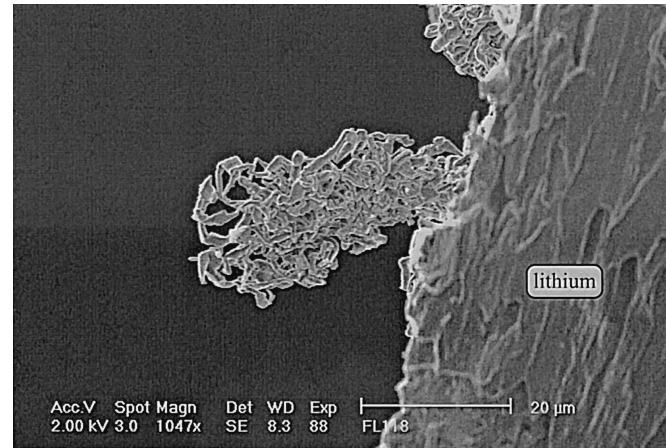
<sup>1</sup>AMA, Inc., NASA Ames Research Center

<sup>2</sup>NASA Ames Research Center

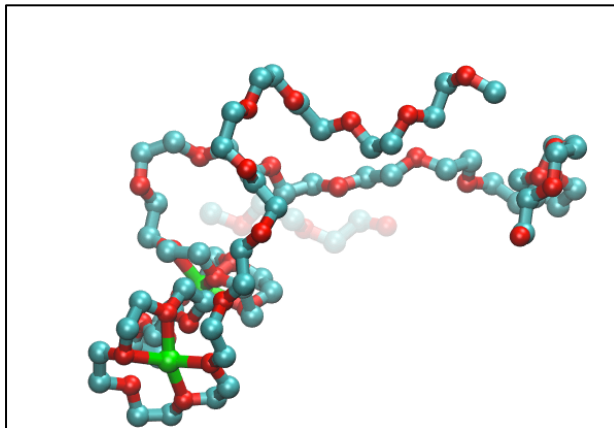
# Battery Research for Green Aviation at NASA



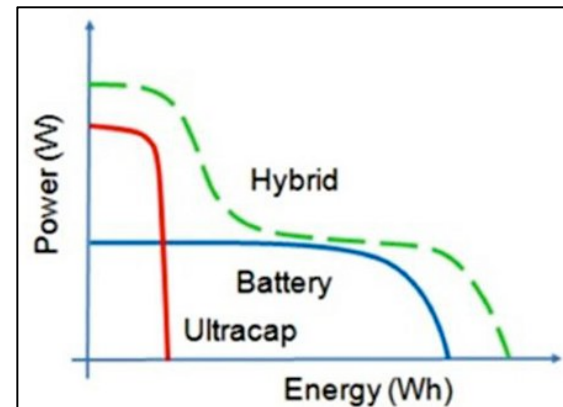
Li-Air Battery Chemistry



Electrolytes for Li-metal



Structural Electrolytes

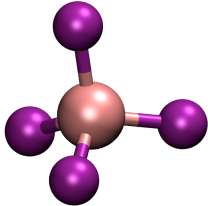


Hybrid Battery/Supercapacitors

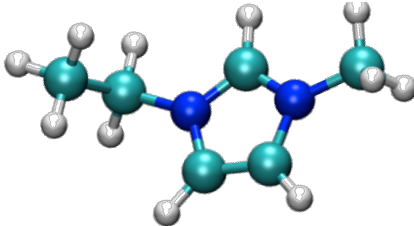
# Ionic liquids for Supercapacitors



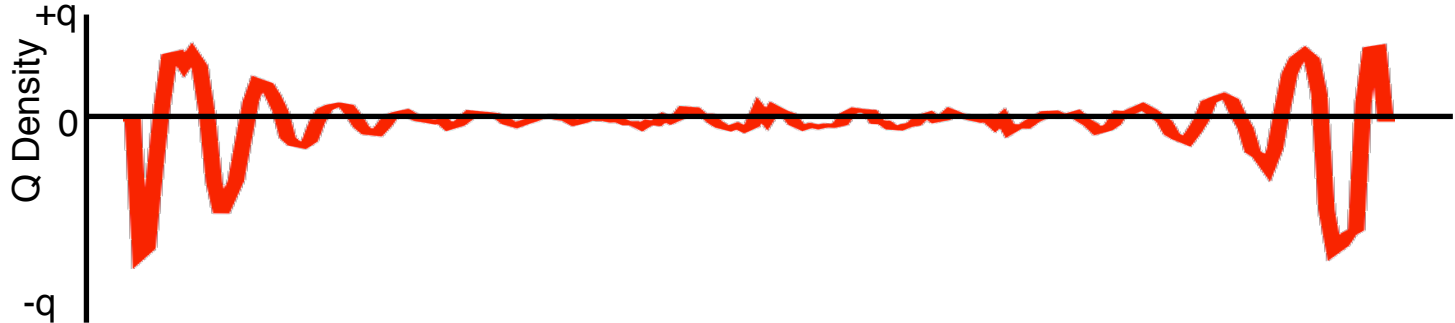
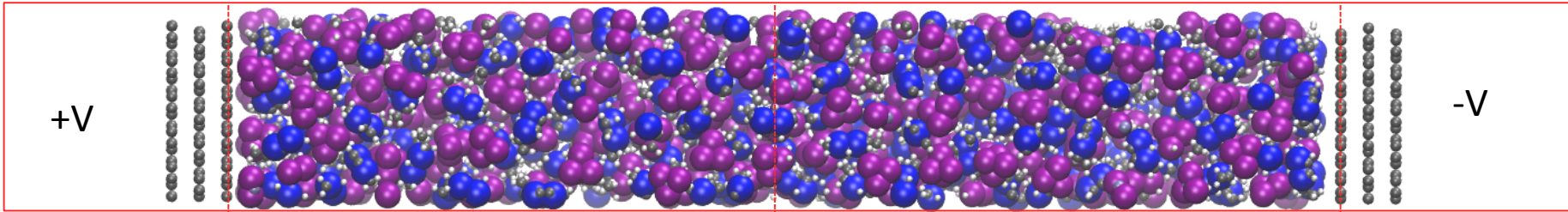
Boron Tetrafluoride ( $\text{BF}_4$ )



1-Ethly-3-Methyl-imidazolium (EMIM)



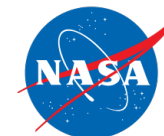
C (green)  
N (blue)  
F (purple)  
B (pink)  
H (white)



Model for classical molecular dynamics (MD) simulation of supercapacitors

# Challenges to the MD Simulation of Supercapacitors

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## 1. Electrostatic Summation:

Do we attain the parallel capacitor limit?

## 2. Differential Capacitance:

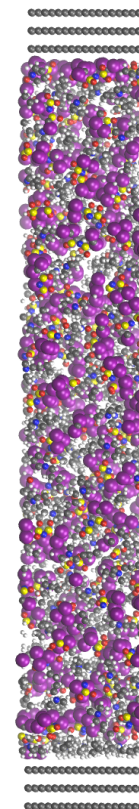
What is the most efficient way to compute capacitance?

## 3. Electrode Charging:

What is difference between smearing charge or setting potential?

## 4. Polarizable Force Field:

How sensitive is interfacial structure and capacitance to polarizability?



# Challenges to the MD Simulation of Supercapacitors

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## 1. Electrostatic Summation:

Do we attain the parallel capacitor limit?

## 2. Differential Capacitance:

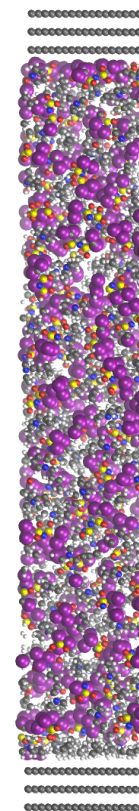
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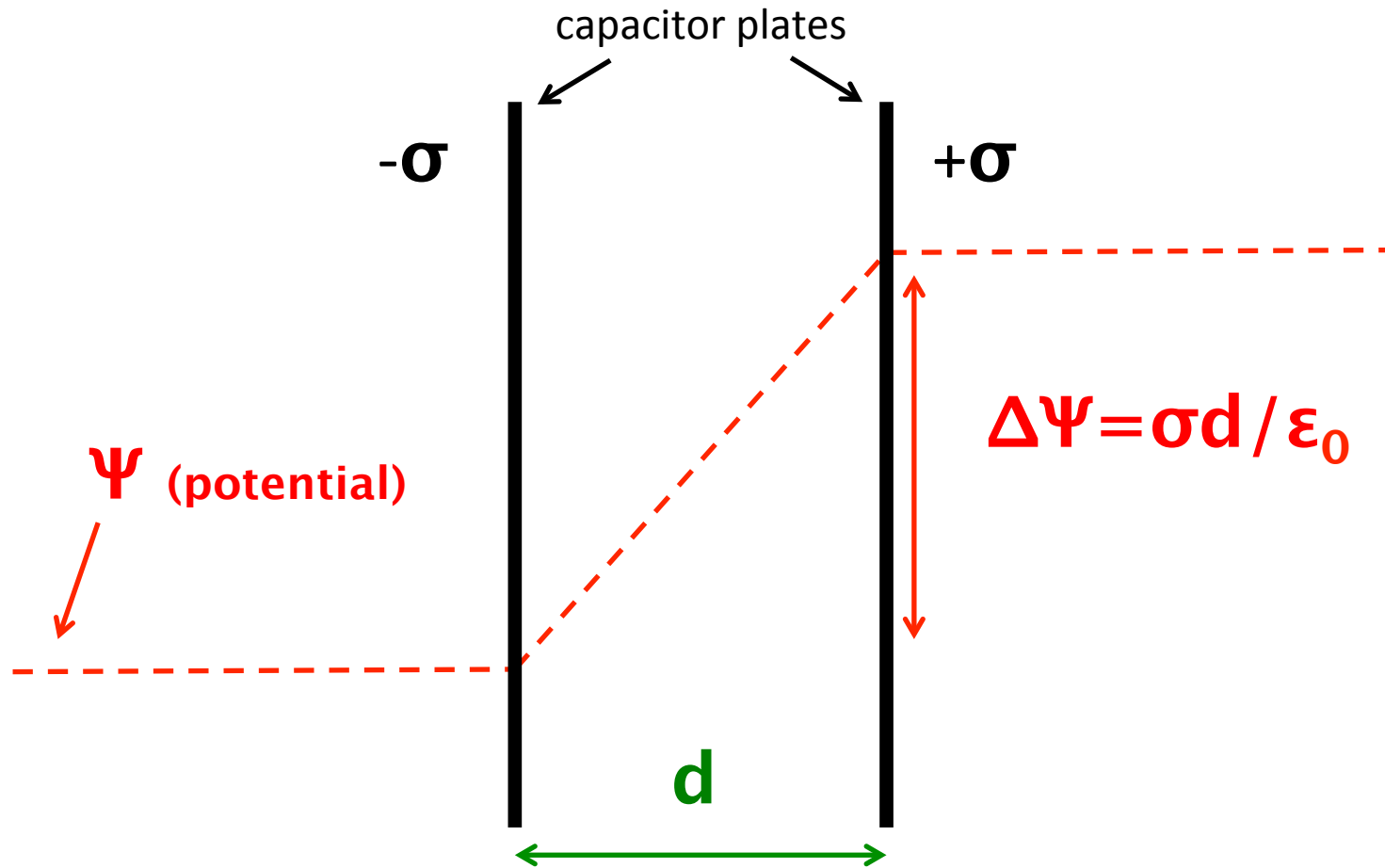
## 4. Polarizable Force Field:

How sensitive is interfacial structure and capacitance to polarizability?





# Parallel Plate Capacitor Model

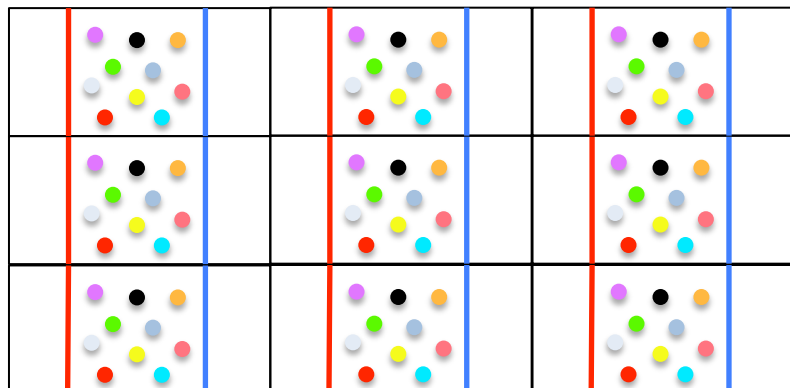


System should conform to the classical electrostatic parallel plate capacitor model

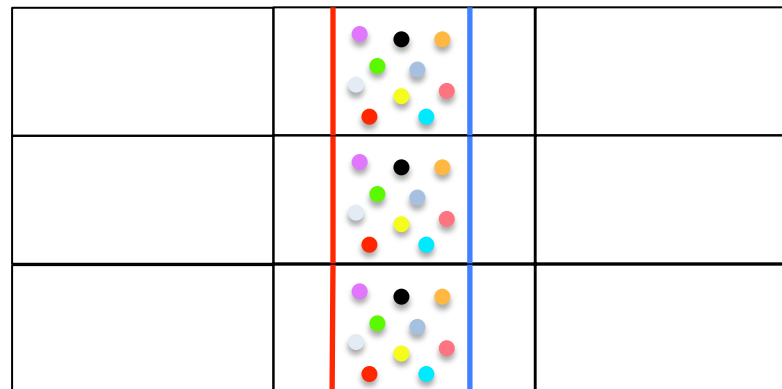


# Options for Electrostatic Summation

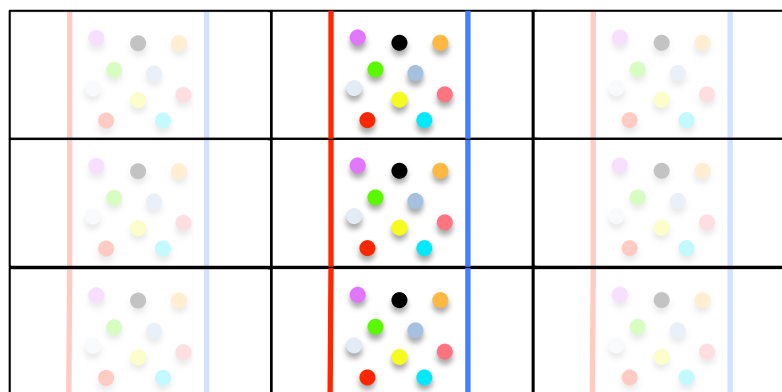
3D Summation



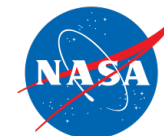
2D Summation



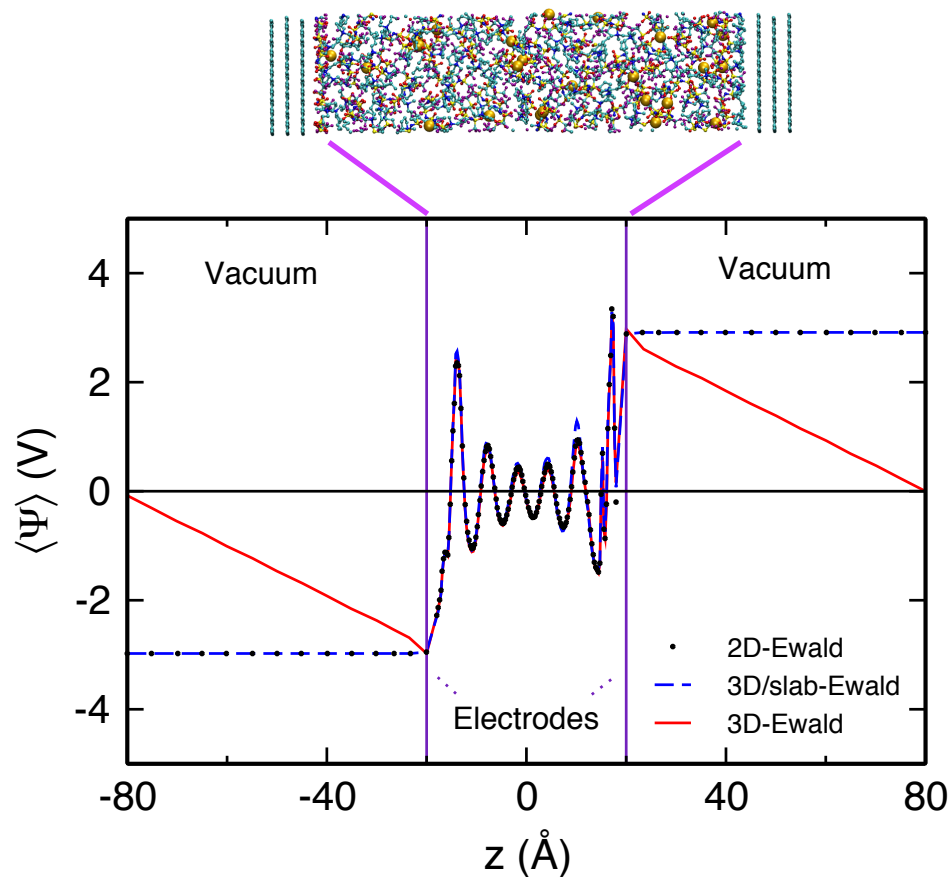
3D Summation + Slab Correction



Three primary options for electrostatic summation



# Average Electrostatic Potential



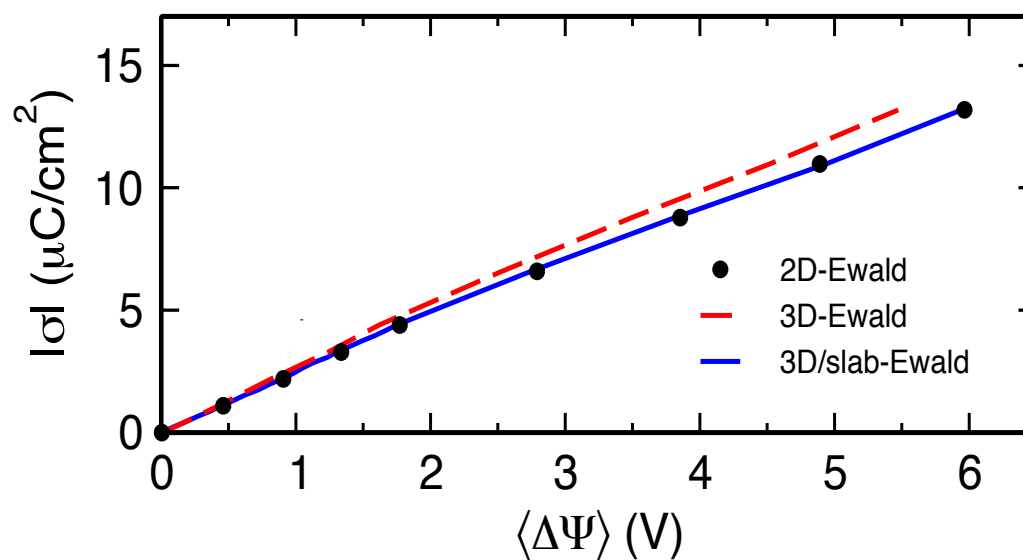
2D ~100x slower than 3D

3D/slab as accurate as 2D and fast as 3D





# Electrode Potential Versus Charge



Use of correct electrostatics prevents a 10-20 % error in capacitance

# Challenges to the MD Simulation of Supercapacitors

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## 1. Electrostatic Summation:

Do we attain the parallel capacitor limit?

## 2. Differential Capacitance:

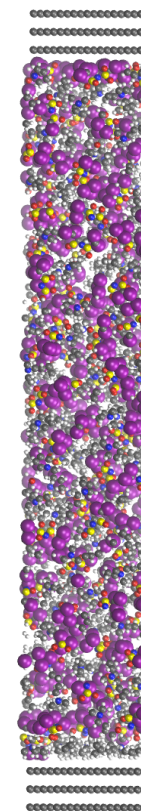
What is the most efficient way to compute capacitance?

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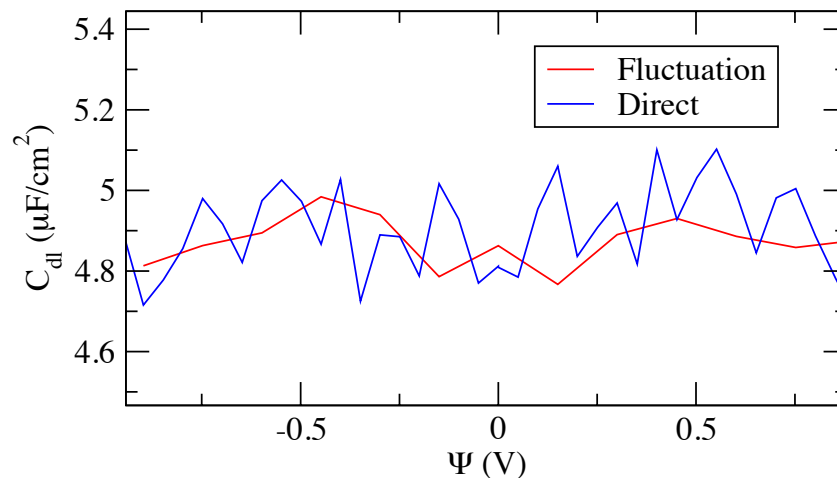


# Fluctuation Expression for Capacitance



Direct method

$$C_{dl} = \frac{\partial \langle \sigma \rangle}{\partial \langle \Psi \rangle}$$

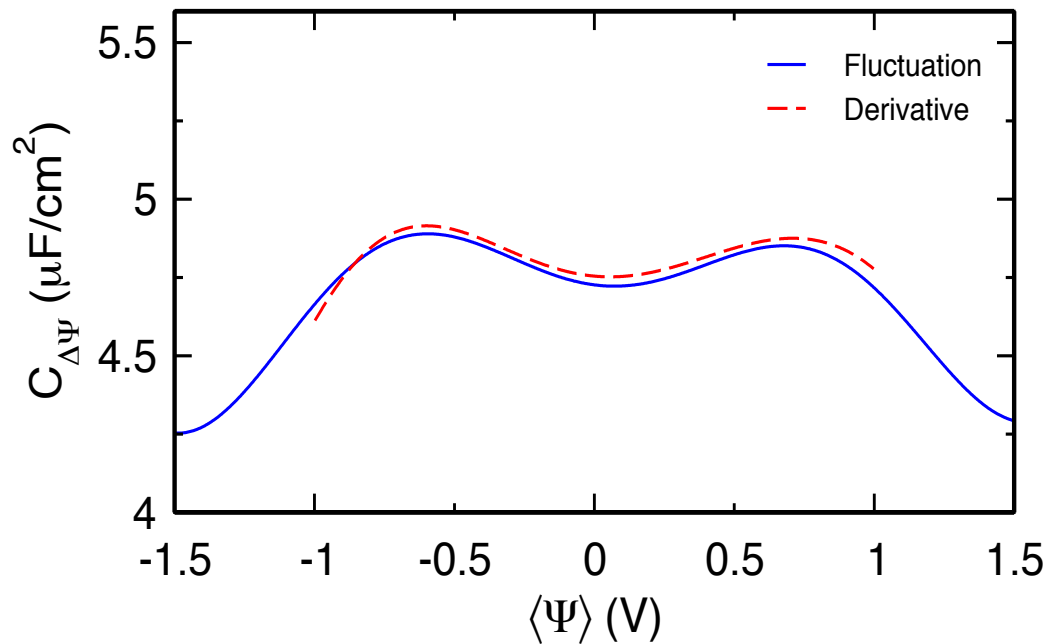


Fluctuation Expression (Newly Derived)

$$C_{\Delta\Psi} = \frac{\partial \langle \sigma \rangle}{\partial \langle \Psi \rangle} = \left[ \beta A \langle |\sigma| \delta \sigma \rangle + \left\langle \frac{\partial \sigma}{\partial \Delta \Psi} \right\rangle \right] \left[ \beta A \langle |\sigma| \delta \Psi \rangle + \left\langle \frac{\partial \Psi}{\partial \Delta \Psi} \right\rangle \right]^{-1}$$

Two approaches for computing capacitance

# Fluctuation Expression for Capacitance



Validated fluctuation formulas for capacitance

# Challenges to the MD Simulation of Supercapacitors

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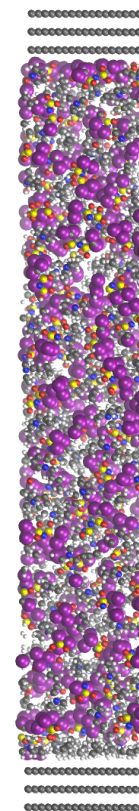
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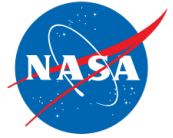
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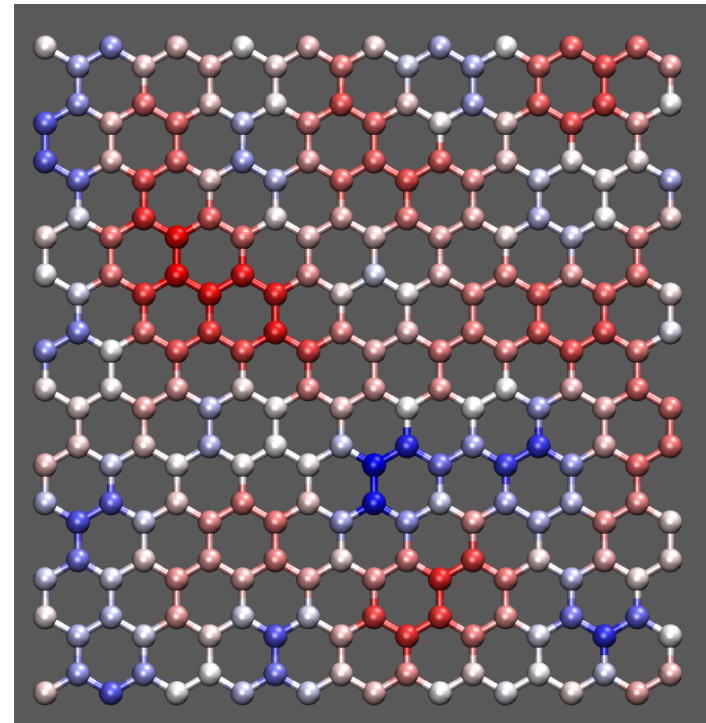
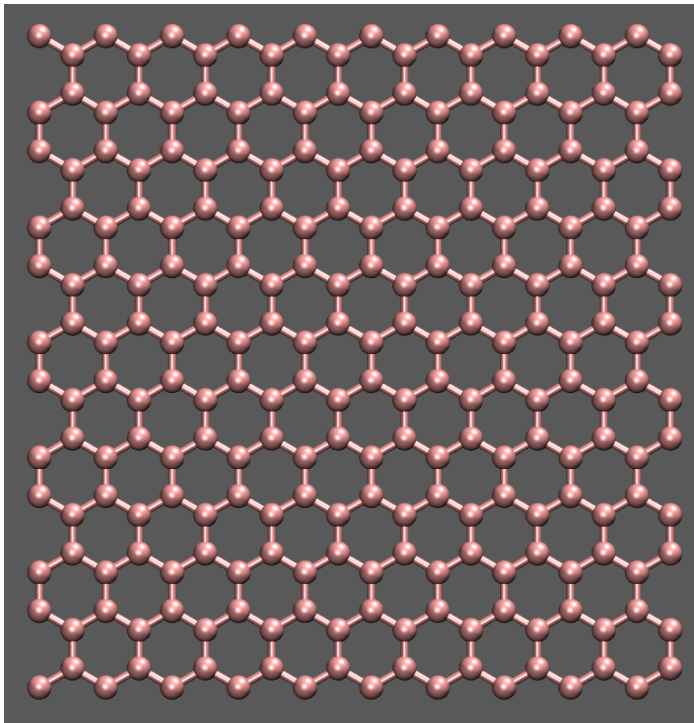
How sensitive is interfacial structure and capacitance to polarizability?



# Electrode Charging Techniques

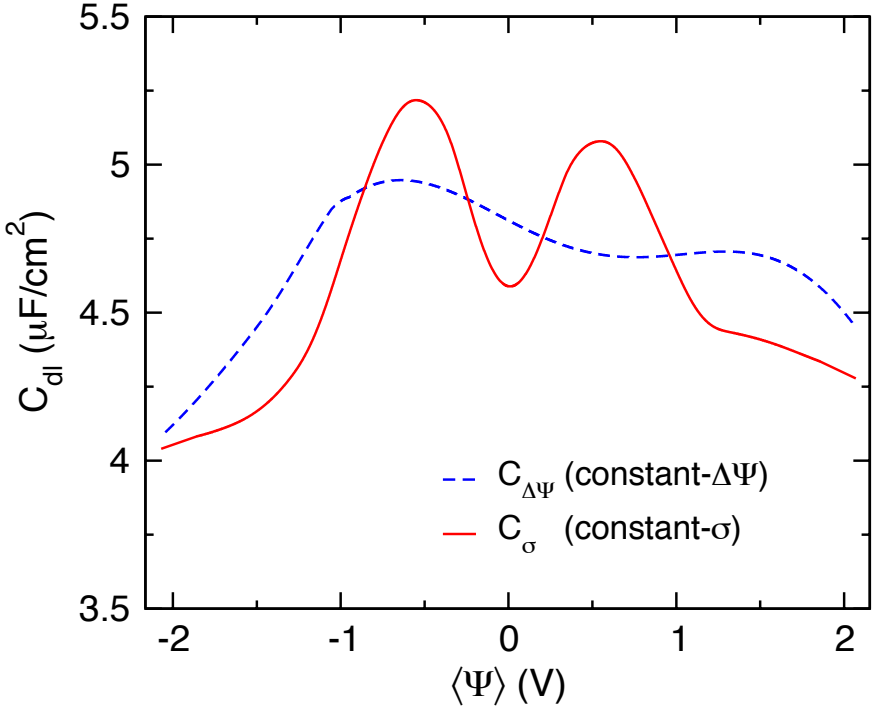
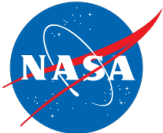


Anode: Constant-Charge      Red: Negative Q      Blue: Positive Q      Anode: Constant-Potential



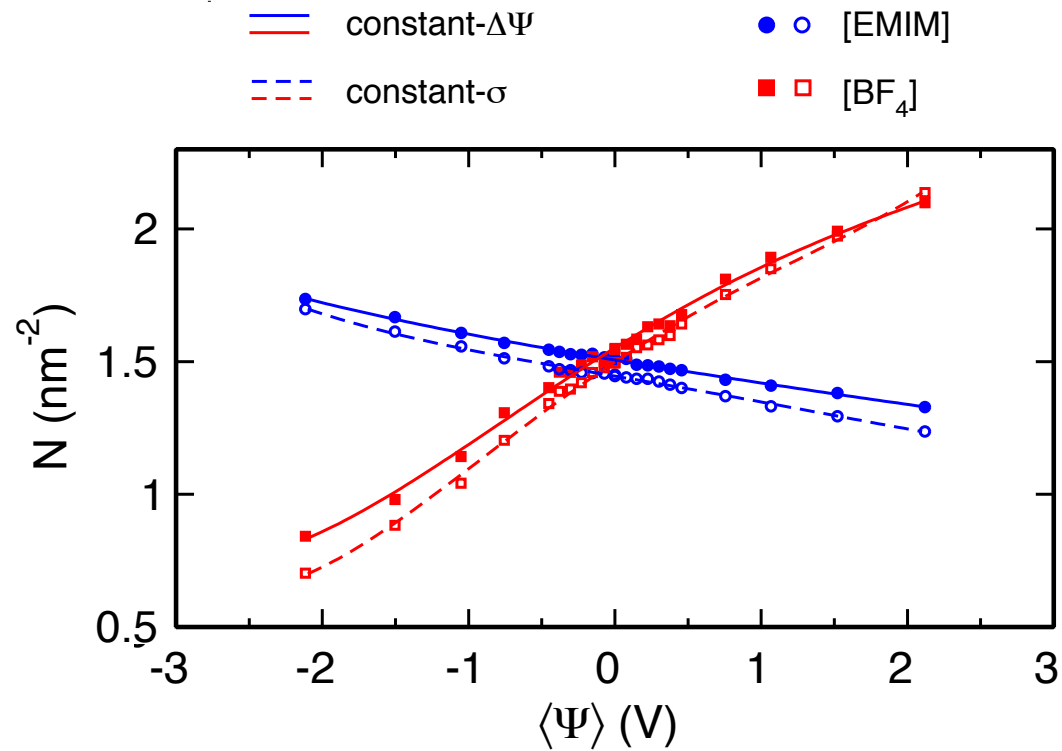
Constant-potential surface less homogeneous due to ion specific charge distribution

# Comparison of Capacitance



Constant-charge electrodes more akin to expectations from mean field theory

# Influence on Surface Layer Density



Constant-potential electrodes lead to denser ion surface layers



# Challenges to the MD Simulation of Supercapacitors

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## 1. Electrostatic Summation:

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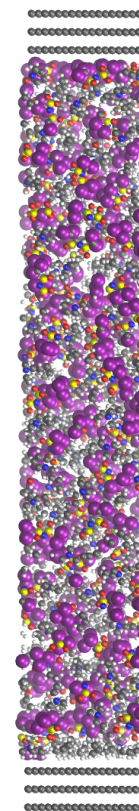
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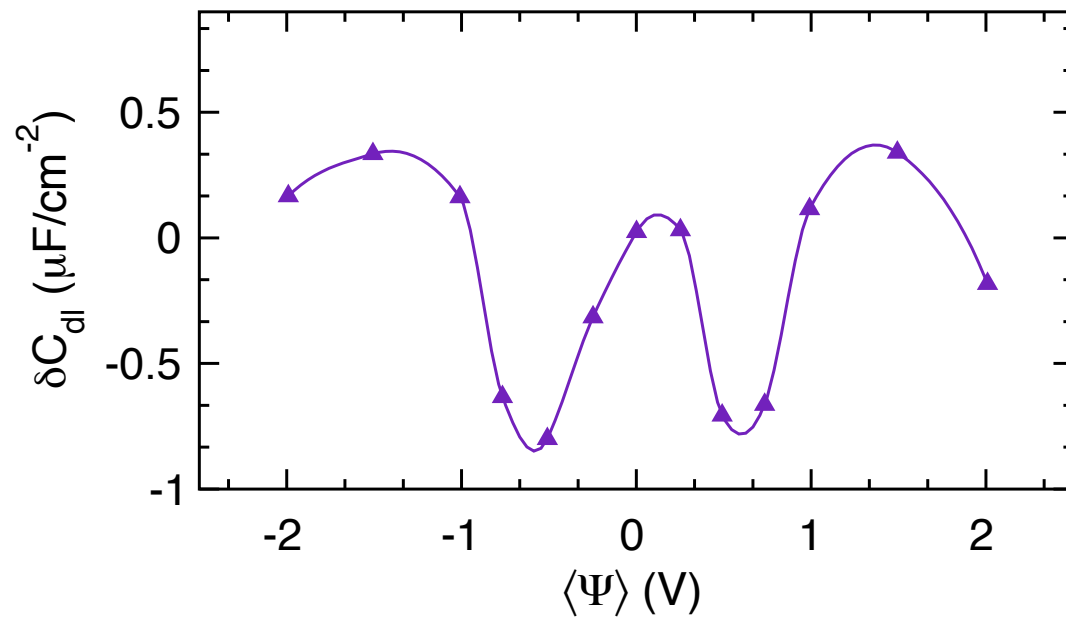
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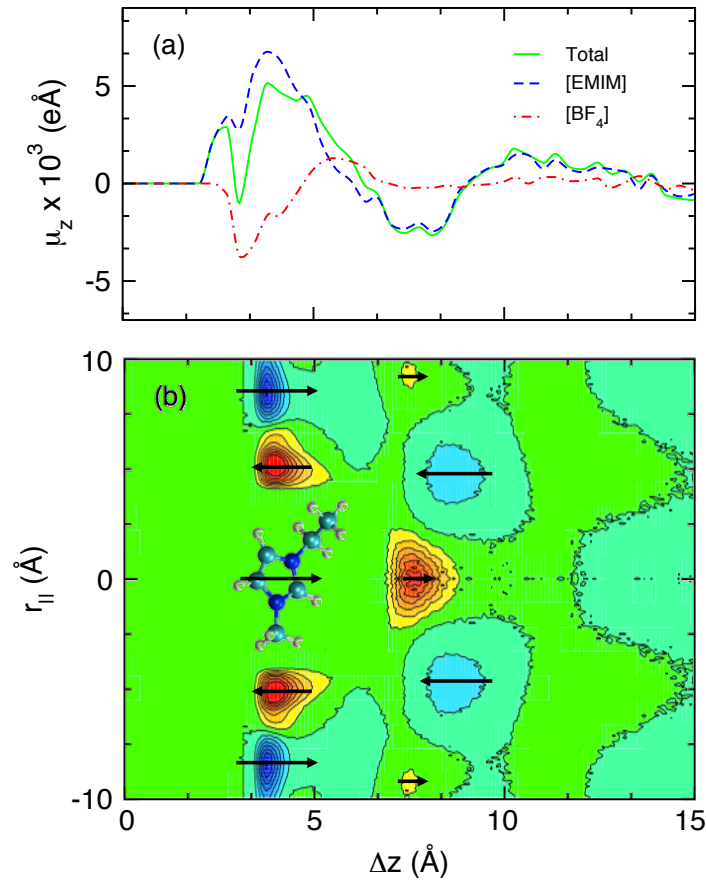


# Influence of Polarizable Force Field



Addition of polarization leads to a net decrease in capacitance and more ion mixing at the surface

# Inter-layer Correlation Effects



Inter-layer dipole correlation effects lead to resistance to EDL formation

Dipole effects missing from practically all simulations

## Conclusions

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- **Electrostatic summation performed cheaply and accurately**
- **Fluctuation formulas developed for capacitance**
- **Constant potential electrodes lead to more realistic capacitance profile**
- **Polarization effects lead to resistance to EDL formation**