Investigation of Thermopower Waves based Energy Sources

A thesis submitted in fulfilment of the requirements for the degree of Doctor of Philosophy

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Declaration

I certify that except where due acknowledgement has been made, the work is that of the author alone; the work has not been submitted previously, in whole or in part, to qualify for any other academic award; the content of this thesis is the result of work which has been carried out since the official commencement date of the approved research program; any editorial work, paid or unpaid, carried out by a third party is acknowledged; and, ethics procedures and guidelines have been followed.

Sumeet Walia Aug, 2013

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Abstract

Miniaturisation of energy sources is critical for the development of the next generation electronic devices. However, reduction in dimensions of none of the commonly used energy generation technologies including batteries, fuel cells, heat engines and supercapacitors have resulted in efficient and reliable energy sources with high specific powers (power-to-mass ratio). Recently, the new concept of energy generation based on thermopower waves has shown promise for miniaturization. In such sources, exothermic chemical reactions of a reactive fuel are coupled to charge carriers of a thermoelectric (TE) material in its affinity, resulting in an intense thermal wave that self-propagates along the surface of the TE materials. This wave simultaneously entrains charge carriers, resulting in a large current. If the TE material also has a high Seebeck coefficient, a large output voltage and subsequently large specific power output are obtained. As the thermal wave results in a power output, it is called a thermopower wave.

This PhD research aimed at creating thermopower wave based energy sources with large enough output voltages and specific powers viable for driving electronic circuits. Before the commencement of this research, only one type of thermopower wave system based on multi walled carbon nanotube (MWNT) TE cores had been reported. Although the MWNT based thermopower wave system generated specific powers as large as 7 kW/kg, the voltage and oscillation amplitudes generated using that system was too low (in the order of 20-50 mV) for any practical application. The author of this thesis identified that the low Seebeck coefficient of MWNTs (-80μ V/K) was the main reason for such small output voltages. Therefore, to achieve the aims of this PhD research program, the PhD candidate developed a set of innovative research goals as follows: (1) exploring potential core TE materials that exhibit a high Seebeck coefficient (*S*), electrical conductivity (σ) and moderate thermal conductivity (κ), (2) designing thermopower wave systems by incorporating such core TE materials to generate high amplitude oscillatory voltages, while maintaining a high specific power, and (3) understanding the influence of thermal conductivity of the core material and the substrate on the behaviour of thermopower waves. In order to realize the aforementioned goals, the author comprehensively reviewed the TE properties of conventional TE materials such as bismuth telluride (Bi₂Te₃), antimony telluride (Sb₂Te₃) as well as TE transition metal oxides (TMOs). Additionally, the author reviewed strategies that can be used for tuning the *S*, σ and κ of the selected materials. Based on the literature review, the author chose the appropriate core TE materials to develop thermopower wave devices in the thin film geometry. As such, the author implemented his research in four distinct stages such that the work in the earlier stages could provide the platform for the subsequent work.

In the first stage, the author demonstrated thermopower wave systems based on thin films of Bi_2Te_3 . Bi_2Te_3 was implemented due to its high $S (\sim -200 \,\mu\text{V/K})$ and $\sigma (10^5 \,\text{S/m})$. As Bi_2Te_3 exhibits a low κ , the author devised a novel strategy by placing it on thermally conductive alumina (Al₂O₃) substrate to compensate for this deficiency. The Bi_2Te_3 based thermopower wave sources generated voltages and oscillations higher (at least 150 %) than MWNT based thermopower wave sources, while maintaining a high specific power in the order of 1 kW/kg. A comprehensive theoretical analysis of the system was carried out and the influence of substrate thermal conductivity was studied by concurrently developing thermopower wave devices based on terracotta substrates that exhibit extremely low thermal conductivity compared to Al₂O₃.

In the second stage, the author implemented a novel combination of p-type Sb_2Te_3 and n-type Bi_2Te_3 as the core TE materials with complimentary semiconducting properties, to show the generation of voltage signals with alternating polarities. For the first time, the phenomenon of thermopower waves was demonstrated using a p-type TE core material (Sb_2Te_3 in this case), in which the majority charge carriers are holes.

Due to fundamental deficiencies of Bi_2Te_3 and Sb_2Te_3 , thermopower wave systems based on them could not generate voltages exceeding 200 mV. To make thermopower wave systems practically applicable, larger output voltages are desired, while maintaining a large specific power. As a result, the author searched for alternatives. A thorough literature review revealed that TMOs can potentially solve this problem as some of them can offer a high *S* and σ as well as moderate thermal conductivity κ simultaneously.

As such, in the third stage, the author implemented zinc oxide (ZnO), which is a TE TMO, for the first time as the core material in thermopower wave sources. It was shown that both $S (\sim -500 \,\mu\text{V/K} \text{ at } 300 \,^{\circ}\text{C})$ and $\sigma (\sim 4 \times 10^3 \,\text{S/m}$ at 300 $^{\circ}\text{C})$ of ZnO increased at elevated temperatures. By incorporating ZnO as the core TE material, the PhD candidate obtained voltages and oscillation amplitudes at least 200 % higher than any previously demonstrated thermopower wave systems (in the order of > 500mV), while maintaining a high specific power (~ 0.5 kW/kg).

In the final stage, in order to exceed voltages larger than 1 V, the PhD candidate identified that manganese dioxide (MnO₂), which is another TE TMO, can exhibit exceptionally large *S* and moderate σ at elevated temperatures. As a result, the author implemented MnO₂ as the core TE material. It was shown that the *S* of MnO₂ increased dramatically with temperature, exhibiting a peak value of approximately –1900 μ V/K at 350 °C. Consequently, voltages large enough (~1.8 V) to drive small electronic circuits were obtained, while maintaining high specific powers in the order of 1 kW/kg. The author also provided novel fundamental insights to explain the increase in Seebeck coefficient of such TE TMOs at elevated temperatures.

In summary, the author believes that this PhD thesis provides the readers with an in-depth analysis of thermopower wave sources based on thin films of conventional TE materials including p-type Sb_2Te_3 and n-type Bi_2Te_3 as well as TE TMOs. The author also believes that this study has contributed significantly towards establishing thermopower wave sources as a viable miniaturised energy generation technology.

List of symbols

S	Seebeck coefficient
σ	electrical conductivity
κ	thermal conductivity
κ_{phonon}	phonon thermal conductivity
<i>K</i> electron	electron electrical conductivity
C_{ν}	electronic specific heat per volume
v	electron velocity
Vs	velocity of sound
L_{ph}	phonon mean free path
L	Lorenz number
k_B	Boltzmann constant
h	Planck constant
τ	electron relaxation time
d_w	diameter of wire
а	cross sectional width
n	carrier concentration
е	electronic charge
μ	electron mobility
m^*	carrier effective mass
F_i	Fermi energy
Т	temperature
Λ	electron mean free path
c _p	specific heat
ρ	density of fuel
W	concentration of fuel
Q	heat of reaction
А	pre-exponential rate constant

- *c* wave propagation velocity
- E activation energy
- R universal gas constant
- S/V surface to volume ratio

List of abbreviations

AFM	atomic force microscopy
ALD	atomic layer deposition
ac	alternating current
dc	direct current
CVD	chemical vapour deposition
DOS	density of states
DFT	density functional theory
2DEG	two-dimensional electron gas
EBE	electron beam evaporation
GPR	gas phase reaction
LPR	liquid phase reaction
LED	light emitting diode
MBE	molecular beam epitaxy
MOCVD	metal organic chemical vapour deposition
PLD	pulsed laser deposition
QDSL	quantum dot superlattice
RF	radio frequency
RTA	relaxation time approximation
SEM	scanning electron microscopy
SNW	segmented nanowire
SSR	solid state reaction
SPS	spark plasma sintering
TE	thermoelectric
TMOs	transition metal oxides
TPF	thermoelectric power factor
VDWE	Van der Waals epitaxy
XRD	x-ray diffraction

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Chapter 1

Introduction

1.1 Motivation

Miniaturisation of energy sources, while maintaining or enhancing their energy discharge capabilities is one of the greatest technological challenges of our time. Researchers envision micro/nano scale systems whose realization is hampered by the lack of sufficiently small power sources. Such miniaturised power sources are extremely vital for future micro/nanoscale advanced electronics, telecommunications systems as well as implantable bio-devices. These future systems include cardioverter-defibrillators the size of apple seeds, implanted unobtrusively in a heart patient to automatically control heart arrhythmias. Also, such small scale energy generation systems could possibly apply localized high energies to muscles or attack cancerous cells *in vivo* with localized pulses of large energies [1]. Another possible application for these puny powerhouses is in "smart dust"— sensors that float in the air, collecting information about temperature, airborne pollutants, and other characteristics [1, 2].

Commonly used energy generation systems include batteries, fuel cells, supercapacitors and heat engines. However, all of them have failed to be miniaturised while maintaining their specific energy (energy to mass ratio) and specific powers (power to mass ratio).

Although there have been recent advances in designing thin films based 3-D Li-ion micro/nano batteries [3], their specific energies and powers are still low (0.4 kWh/kg and 0.3 kW/kg, respectively at 10-15 μ m thickness) [4-6]. A reduction in size of such sources gives rise to problems such as ionic flow disruption around electrodes as well as electrical shorts that hamper their ability to perform effectively [7]. Additionally, microlithography

processes have proved cumbersome and expensive to transfer to batteries [8]. Although, a few newer technologies such as small stacked micro fuel cells (~ 200 μ m thick) [9], may become promising sources to power future micro/nano scale systems, but despite many years of research and innovation, fuel cells of this size are yet to produce sufficiently large specific powers. Fuel cells designed to work with microscale systems exhibit specific powers less than 0.1 kW/kg [1, 10] [11].

Energy can also be stored and released at high rates using technologies such as supercapacitors. It has been shown that that they can exhibit a specific power as high as 10 kW/kg [12-14]. The major disadvantage of supercapacitors is their high self-discharge rate. This renders them impractical for long-term energy storage as they have to be charged frequently in order to maintain the stored energy.

Energy can also be generated using systems such as heat engines. However, they don't typically scale to the sizes needed for the next generation of technologies, either. To date, scaled-down heat engines with dimensions of the order of 1 mm can only sustain specific powers of only around 0.1 W/kg which is a minute fraction of the 0.2 kW/kg that average lithium-ion batteries achieve [1, 15].

Thus, none of the aforementioned technologies have so far enabled reliable miniaturized power sources with high specific power. It seems that a mere miniaturization of the current energy sources cannot simply solve the problem. Therefore, new technologies at small dimensions can possibly be the answer.

MIT's Strano Laboratory, first demonstrated a new approach to energy storage and power generation. Their experimental system generated power in a way that has no macroscopic analogy. In their work, they developed aligned arrays of multiwalled carbon nanotubes (MWNTs) wrapped in a several-nm-thick cyclotrimethylene-trinitramine (TNA) annular coating (Figure 1.1) [16-18]. By coating the MWNTs with a reactive fuel (TNA in their case)

and ignition at one end sets off a combustion wave along the nanotube was generated. This combustion wave created a strong electric current along their propagation direction and was called a 'thermopower wave' because it transmitted energy from one place to another, by coupling with the nanotube's electrical carriers, setting them in motion along the conducting nanotube. The moving heat source swept the coupled electrical carriers along, an effect which was called electron entrainment. The carriers all moved together in a single direction, creating an electrical current that is extremely large relative to the mass of the system. The propagation of the charge carriers was governed by the thermoelectric (TE) effect—the voltage that results from a temperature differential across a material. The specific power generated by the MWNT based thermopower wave system exceeded the best lithium-ion batteries currently available by as much as 3-4 times [1]. It was also demonstrated that the highest specific powers (~7 kW/kg) were obtained from the thermopower devices with the smallest masses (0.01-0.1 mg) [18].

Thermopower wave generators are remarkable in other ways. For instance, before the ignition, the chemical energy is stored in the chemical bonds of the fuel indefinitely. Therefore, such sources do not suffer from any self-discharge. They also have simple designs (Figure 1.1), which can take advantage of standard industrial micro- and nanofabrication technologies. Another feature of thermopower wave sources, is their ability to generate an oscillatory voltage signal, unlike energy sources such as batteries, fuel cells, supercapacitors and heat engines that are capable of producing only direct current (dc) power [16].

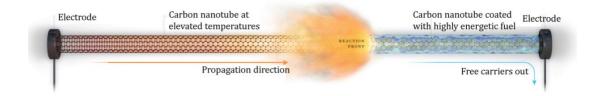


Figure 1.1: Schematic representation of a MWNT based thermopower wave system (not to scale). (Reproduced with permission from Ref [1].)

Although the aforementioned results were encouraging, there is much to be investigated before thermopower wave generators could be developed into a commercially viable power source. The main limitation of the MWNT based thermopower wave sources is the low voltage (generally 30-50 mV) and small oscillation amplitudes (10-15 mV) generated, although voltages as large as 200 mV were reported [17]. Such voltages aren't enough for most applications. Therefore, as with any energy generation system, the main challenge is to maximize the output power from thermopower wave systems. This can be potentially achieved by increasing the output voltage (by using materials with high Seebeck coefficient (S)) and boost the current by decreasing the internal resistance of the core TE materials. Therefore, an ideal TE material for thermopower wave systems should exhibit a high Seebeck coefficient (S) and high electrical conductivity (σ). Contrary to conventional TEs, thermopower wave sources benefit from a moderate to high thermal conductivity (κ) as it facilitates the sustained propagation of the reaction. Hence, thermopower wave sources based on materials exhibiting the aforementioned properties need to be investigated in order to achieve high output voltages enabling such sources to be used as micro/nano energy sources.

1.2 Objectives

The research work for this PhD thesis was based on developing thermopower wave systems in thin film geometries using different core TE materials that exhibit high *S* and σ and moderate to high κ , so that output voltages large enough for practical applications could be obtained.

In order to solve the challenges of this PhD thesis, the author made informed choices regarding the incorporation of a variety of materials as TE cores in thermopower wave sources. He studied conventional TE materials including bismuth telluride (Bi_2Te_3) and

antimony telluride (Sb₂Te₃) whose TE properties have been widely examined. The PhD candidate then extended his studies to TE transition metal oxides (TMOs) such as zinc oxide (ZnO) and manganese dioxide (MnO₂), which have been much less investigated for their TE properties. The author of this thesis focussed his attention on developing thermopower wave devices based on thin films of the aforementioned materials. The author chose to develop thermopower wave devices in thin film geometries due to its distinct advantages. Thin films allow the deposition of different layers with varying TE and thermal conductivity properties in order to control the propagation of the thermopower waves. Additionally, it allows the alteration of the surface roughness which can be used to increase the amount of solid fuel that can be placed over the TE layer. The compatibility of thin films with current microchips standards, which are all lithographically obtained in two dimensions (2D) is an added advantage.

Bi₂Te₃ and Sb₂Te₃ are the most commonly used TE materials. In order to increase the output voltage from thermopower wave sources, Bi₂Te₃ and Sb₂Te₃, with respective absolute Seebeck coefficients of ~200 μ V/K and 160 μ V/K, could be used instead of carbon nanotubes (CNTs) that exhibit an absolute *S* of only 80 μ V/K [17, 19, 20]. Advantageously, both Bi₂Te₃ and Sb₂Te₃ also have high electrical conductivities of the order of 10⁴–10⁵ S/m [21-23]. This combination of their high Seebeck coefficient and electrical conductivity made these two materials potential candidates for applications in thermopower wave generators. Bi₂Te₃ and Sb₂Te₃ do not exhibit high thermal conductivities that are required for the successful self-propagation of thermopower waves. As a result, the PhD candidate designed a viable system for the propagation of thermopower waves by placing Bi₂Te₃ and Sb₂Te₃ and Sb₂Te₃ and Sb₂Te₃ and Sb₂Te₃ and substrates such as alumina (Al₂O₃) to compensate for this deficiency. The role of the highly thermally conducting alumina substrate is to provide a pathway for the thermal conduction across the sample thereby assisting the self-propagation of the thermopower waves.

The incorporation of Bi₂Te₃ and Sb₂Te₃ by the PhD candidate was a critical choice as both these materials exhibit complementary semiconducting properties (Bi₂Te₃ is n-type while Sb₂Te₃ is a p-type TE material). The work conducted by Strano *et al.* at MIT was based only on n-type MWNTs in which electrons were the majority carriers [18], and it was not clear whether the same phenomenon can be observed for p-type core. By demonstrating thermopower wave devices based on n and p-type materials the author showed that the same phenomenon also extended to hole dominant semiconducting TE materials. Additionally, it was shown that a combination of such n and p-type materials resulted in output voltage signals with alternating polarities.

The next approach by the PhD candidate was to investigate TE TMOs such as ZnO and MnO₂. These materials turned out to be potential candidates, as they demonstrated an ideal combination of the required characteristics (a high *S*, σ and moderate κ) at elevated temperatures. Contrary to Bi₂Te₃ and Sb₂Te₃, such TE TMOs are non-toxic and abundant in nature. Additionally, TMOs are stable at extremes of temperatures which is a desirable feature for the high temperature thermopower wave reaction. As such, they can lead to the development of low cost and safe functional thermopower wave systems.

ZnO a n-type semiconducting oxide was an outstanding candidate as the core TE material for thermopower based energy sources as it exhibited a high Seebeck coefficient (~ -200μ V/K at room temperature) which increased by ~150% at 300 °C which is the temperature regime in which the thermopower wave systems operate. Its high electrical conductivity at such elevated temperatures (of the order of 10^3 S/m), moderate thermal conductivity (15 W/m.K) and good chemical stability were also desirable features for implementation in thermopower wave sources [24-26].

MnO₂ was another TE TMO that was applied as the core material in thermopower wave sources due to its exceptionally high Seebeck coefficient, especially at elevated temperatures (-1900μ V/K at 300 °C). Similar to ZnO, its electrical conductivity was also enhanced as the

temperature increased, thereby resulting in a high thermoelectric power factor (TPF- defined as $S^2\sigma$) of the order of 10³ µW/m.K² [27-29].

In the thermopower wave sources developed by the author of this thesis, the temperature gradient was achieved by the combustion of a reactive fuel. The author used nitrocellulose $[C_6H_8(NO_2)_2O_5]$ as the highly reactive solid fuel due to its large enthalpy of reaction $(4.75 \times 10^6 \text{ J/kg})$ which helped in achieving a high temperature gradient. Although TNA exhibits a much higher enthalpy compared to nitrocellulose, there are legal restrictions on its use in Australia, therefore it could not be procured for the author's experiments.

Throughout his PhD, the author focussed on increasing the output voltages obtained from thermopower wave sources, while mainitaing a high specific power. The gaps were highlighted by the PhD candidate and as such the primary objectives of this PhD work were targeted towards those gaps as follows:

- The author of this thesis generated new knowledge by preparing a comprehensive text reviewing the TE properties of conventional TE materials such as Bi₂Te₃ and Sb₂Te₃ as well as TMOs in pure, doped and non-stoichiometric forms. The developed literature was especially important as there is no comprenesive review on the properties of TE TMOs. Based on this analysis, the author made informed choices regarding the core TE materials to be implemented in thermopower wave sources developed during his PhD research.
- 2. The author of this thesis first demonstrated thermopower wave systems in a thin film geometry using Bi₂Te₃, a conventional TE material. This was the first demonstration of thermopower wave generation in a thin film geometry using core TE materials other than MWNTs. Theoretical modelling was also carried out in order to assess and predict the behaviour of thermopower waves. The author also examined the influence of various parameters such as the thermal conductivity and the wave propagation velocities on the behaviour of the thermopower waves. It was shown that these systems are able to produce

higher voltage and oscillation amplitudes than previously demonstrated thermopower wave systems using MWNT cores

- 3. For the first time, the author provided a comparison of thermopower wave systems based on two complementary core TE materials (p-type Sb₂Te₃ and n-type Bi₂Te₃). By implementing a combination of such p and n type core TE materials, an output voltage with alternating polarities can was obtained.
- 4. For the first time, the author demonstrated the incorporation of TMOs as the core TE materials in thermopower wave sources. TE TMOs such as ZnO and MnO₂ were used due to their high S, σ and moderate κ resulting in the generation of very high oscillatory output voltages compared to any previously developed thermopower wave system. Additionally, the author also provided a fundamental insight into the enhancement of Seebeck coefficient with increasing temperature in such TE TMOs.
- 5. Furthermore, the author also used the experimental results to assess the influence of the thermal conductivity of the core TE materials and the substrates to assess its impact on the wave propagation velocities and the oscillatory behaviour of the voltage signals.

1.3 Thesis organisation

This thesis is primarily dedicated to developing thin film based thermopower wave sources using different core TE materials to maximise the voltage output, while maintaining a high specific power. The major sections of this thesis are as follows:

In Chapter 2, the author will provide the literature review of this thesis. The chapter will discuss the theory governing the key TE parameters of *S*, σ and κ for bulk and low dimensional TE materials. The author will then overview the strategies that are implemented to tune the aforementioned key TE parameters. A detailed discussion of the TE properties of Bi₂Te₃, Sb₂Te₃ and TMOs in pure and doped states will be presented.

In Chapter 3, the author will demonstrate his work on Bi_2Te_3 based thermopower wave sources. In this chapter the author will show thermopower wave generation by coupling the exothermic chemical reaction of nitrocellulose to charge carriers in Bi_2Te_3 films supported by alumina (Al₂O₃) or terracotta (baked natural polysilicate) substrates. Al₂O₃ and terracotta were used as substrates because of their contrasting thermal conductivities which helped to assess the effect of thermal properties of the system on the thermopower waves. It will be shown that devices based on Bi_2Te_3/Al_2O_3 generated self-propagating thermopower waves, which resulted in larger voltages and oscillatory amplitudes (~ 150 %) than the MWNTbased thermopower wave systems. The author will also provide a theoretical analysis to describe the behaviour of thermopower waves for nitrocellulose/Bi₂Te₃/substrate system.

In Chapter 4, the author will present a detailed comparison of thermopower wave sources based on TE cores with complementary semiconducting properties (p-type Sb_2Te_3 and n-type Bi_2Te_3). Such a contrast ensured that the voltage output from these thermopower wave sources, with identical characteristics (one based on Bi_2Te_3 and the other based on Sb_2Te_3), produced both positive and negative polarities. The combination of these two resulted in an alternating signal, which is required for practical applications.

In Chapter 5, the author will present the implementation of a TE TMO (ZnO in this case) as the core TE material in thin film thermopower wave sources for the first time. ZnO based thermopower devices were capable of generating significantly larger voltages and oscillation amplitudes than any previously reported systems (>200%). The Seebeck coefficients and the electrical conductivities of the ZnO films at elevated temperatures will also be discussed to assess the behaviour of the system.

In Chapter 6, the author will cover his work on the development of MnO_2 thin films' based thermopower wave sources which resulted in exceptionally high output voltages (~1.8 V). New insights into the fundamentals of the enhancement of Seebeck coefficient in TE TMOs such as ZnO, MnO_2 at elevated temperatures will be presented by the author. A full analysis of the system by characterizing the device before and after the thermopower wave propagation and also its Seebeck coefficient, electrical conductiviy, output voltage profile, specific power and thermopower wave propagation velocities will also be included.

Finally, in Chapter 7, the author will present concluding remarks and suggest possible future works.

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Chapter 2

Literature review

2.1 Introduction

In the previous chapter, the author highlighted the importance of developing thermopower wave sources as an alternative energy generation technology. Prior to the research conducted by the author of this thesis, only one thermopower wave system that was based on multi walled carbon nanotube (MWNT) thermoelectric (TE) cores had been reported [1]. It was highlighted that the output voltages and oscillation amplitudes from thermopower wave sources needed to increase to establish it as a viable technology. The author chose to develop thermopower wave devices in thin film geometries and highlighted its advantages in the previous chapter. The author also explained that in order to achieve higher voltages with larger oscillations while maintaining a high specific powers, core thermoelectric (TE) materials with high Seebeck coefficients (*S*), electrical conductivities (σ) and moderate thermal conductivities (κ) are required.

In this chapter, the author will review the TE properties of bismuth telluride (Bi₂Te₃), antimony telluride (Sb₂Te₃) which are conventional TE materials and various transition metal oxides (TMOs) in their intrinsic, various stoichiometry and doped forms. The theory governing the key TE parameters of κ , σ and *S* for the aforementioned materials in bulk and low dimensional form will be discussed, along with effects of morphological tuning and stoichiometric changes on these parameters. The author of this thesis prepared this important review in order to highlight the key considerations that are required to successfully develop thermopower wave systems for this PhD research and choose the most suitable core TE materials to incorporate in the thermopower wave devices.

This chapter also includes an extended review on the techniques that are implemented to tune the key TE parameters of the materials. A comprehensive text covering the TE properties of TMOs does not exist in literature. As such, a major portion of the contents of this review was submitted to the Journal Progress in Materials Science.

The author will organise this chapter into 3 major categories. These include the theory governing the key TE parameters (S, σ and κ) for bulk and low dimensional Bi₂Te₃, Sb₂Te₃ and TMOs, strategies to tune their TE parameters and a review of their TE properties.

2.2 Basic principles of thermoelectricity

The fundamental factors that govern TE properties are thermal conductivity (κ), electrical conductivity (σ) and Seebeck coefficient (S). The performance of TE materials is generally assessed by the figures of merit (ZT) defined as $S^2\sigma/\kappa$, and the thermoelectric power factor (TPF) defined as $S^2\sigma$. In this section, we present an overview of the main equations governing the aforementioned TE parameters for bulk three dimensional (3D) and low dimensional (2D, 1D and 0D) structures.

2.2.1 Thermal conductivity

Thermal conductivity is the ability of a material to conduct heat. The main contributors to the thermal conductivity are phonons and charge carriers (electrons and holes). The overall thermal conductivity (κ_{total}) of a material is defined as [2, 3]:

$$\kappa_{total} = \kappa_{phonon} + \kappa_{electron} \tag{1}$$

where, κ_{phonon} is the lattice thermal conductivity due to acoustic phonons travelling through the crystal lattice and $\kappa_{electron}$ is the electronic thermal conductivity due to charge carriers. Phonons and charge carriers can undergo scattering due to other phonons, lattice defects, impurities, electrons, grain boundaries and interfaces [4]. Such scattering then results in changes of thermal conductivity. The fundamentals of κ_{phonon} and $\kappa_{electron}$ for bulk as well as low dimensional materials are discussed next.

2.2.1.1 Bulk (3D) materials

For semiconducting and insulating TE materials, acoustic phonons are the major contributors to $\kappa_{total.}$ However, for highly doped and non-stoichiometric TE materials the electronic thermal conductivity also plays an important role. For bulk materials, the kinetic theory of gases defines the κ_{phonon} and $\kappa_{electron}$ as:

$$\kappa_{phonon} = \frac{1}{3} \upsilon_s C_{\upsilon} L_{ph} \tag{2a}$$

$$\kappa_{electron} = \frac{1}{3} c_{\nu} \upsilon \Lambda = L \sigma T \tag{2b}$$

where v_s is the velocity of sound, C_v is the heat capacity at constant volume, L_{ph} is the phonon mean free path, c_v is the electronic specific heat per volume, v is the electron velocity that can be assumed to be the Fermi velocity v_F , Λ is the electron mean free path, L is the Lorenz number (2.45×10⁻⁸ V².K²), σ is the electrical conductivity, and T is the temperature in Kelvin.

 C_{v} and v_{s} are typically temperature independent for T > 300K; hence at high temperatures, κ_{phonon} primarily depends on L_{ph} and can be largely attributed to phonon-phonon scattering [5].

On the other hand, $\kappa_{electron}$ depends on the electron mean free path. The Wiedemann-Franz law as shown in Eq. 2b states that $\kappa_{electron}$ is directly proportional to σ and T, so that any variation in $\kappa_{electron}$ affects σ . Hence, the only TE parameter that is independent of the electronic band structure is κ_{phonon} .

In semiconducting materials, phonons are the majority contributors to κ_{total} , making it possible to tune their κ_{total} with a negligible effect on σ . A comprehensive theoretical analysis of κ has been provided elsewhere [3]. In order to improve the performance of TE materials for conventional applications such as cooling and energy scavenging, a reduction in κ_{phonon} is desirable. In theory, the minimum κ_{phonon} is achieved when the mean free path of the phonons is no more than the interatomic spacing of the constituent atoms [6]. Limiting L_{ph} by confining phonons can help achieve this goal. Such a confinement can be obtained by creating low dimensional materials, which are described next.

2.2.1.2 2D materials

A two-dimensional (2D) quantum well structure consists of a very thin layer of material that is nanometers thick in one dimension and semi-infinitely large in the other two dimensions. 2D quantum well structures are likely to reduce the κ_{total} of TE materials compared to their bulk counterparts because phonons mainly scatter at the interfaces, while the motion of the electrons can be confined parallel to the layers. $\kappa_{electron2D}$ is a strong function of the thickness of layers (*W*). For 2D quantum well structures, $\kappa_{phonon2D}$ and $\kappa_{electron2D}$ along the *x*-axis (Figure 2.1 (a)) have been defined as [7, 8]:

$$\kappa_{phonon2D} = \frac{k_B}{2\pi^2 v} \left(\frac{k_B}{h}\right)^3 T^3 \int_0^{\theta/T} \frac{\tau_c \xi^4 e^{\xi}}{(e^{\xi} - 1)^2} d\xi$$
(3a)

$$\kappa_{electron2D} = \frac{\tau h^2}{4\pi W} \left(\frac{2k_B T}{h^2}\right)^2 \left(\frac{m_y}{m_x}\right)^{1/2} k_B \left(3F_2 - 4\frac{F_1^2}{F_0}\right)$$
(3b)

where, k_B is the Boltzmann constant, h is the Planck constant, e is the electron charge, $m_{x,y,z}$ are the three components of the effective mass, θ is the Debye temperature, $\xi = h\omega/k_BT$ ($h\omega$ being the phonon energy), T is the absolute temperature, τ is the electron relaxation time and is defined as $\tau = \mu_x m_x/e$ where μ_x is the mobility along the *x*-axis (Figure 2.1 (a)), v is the velocity of sound, F_i are the Fermi-Dirac functions and τ_c is the combined phonon relaxation time due to all resistive processes (which include boundary scattering, mass difference scattering, scattering at dislocations and Umklapp scattering processes), which is governed by the Matthiessen's rule (see ref. [8] for details). According to Eq. 3a, the theoretical value of $\kappa_{phonon2D}$ is strongly influenced by the phonon-phonon energy, its relaxation time τ_c , which is a function of the quantum well dimension and temperature.

 $\kappa_{electron2D}$ depends only on two effective mass components of the electrons as shown in Eq.3b. This is because, unlike phonons, electrons can only move in a 2D motion parallel to the layers due to the quantum confinement. Additionally, a stronger confinement (by decreasing *W*) is expected to increase $\kappa_{electron2D}$. However, the result of reducing *W* is generally a decrease in the overall thermal conductivity. This is especially useful in engineering ZT when both Seebeck coefficient and electrical conductivity of the material remain constant. 2D Bi₂Te₃ and Sb₂Te₃ have also been shown to exhibit enhanced TPFs and ZTs [9, 10]. There are also practical examples of employing 2D TMOs such as TiO₂, cobalt oxides and manganese oxides [11] with increased ZTs and will be discussed in their relevant sections. The application of 2D TE materials with increased ZT values [11] has been demonstrated in energy scavenging at elevated temperatures that will also be discussed later.

2.2.1.3 1D materials

Hicks *et al.* developed a theoretical model and predicted that materials in 1D form (such as quantum wires, nanobelts and nanorods) can result in further reduction of $\kappa_{electron}$, compared to bulk and 2D structures [12]. The thermal conductivity of phonons in 1D structures were theoretically modelled by Zou and Balandin [13]. The equations describing κ_{phonon} and $\kappa_{electron}$ for 1D structures are [12, 13]:

$$\kappa_{phonon1D} = \frac{k_B}{2\pi^2 v} \left(\frac{k_B}{h}\right)^3 T^3 \int_0^{\theta/T} \frac{\tau_c \xi^4 e^{\xi}}{(e^{\xi} - 1)^2} d\xi \times \left[1 - \frac{24}{\pi} G(\eta(\xi), p)\right] d\xi \tag{4a}$$

$$\kappa_{electron1D} = \frac{2\tau}{\pi a^2} \left(\frac{2k_B T}{h^2}\right)^{1/2} (m_{\chi})^{-1/2} k_B^2 T \left(\frac{5}{2} F_{3/2} - \frac{9F_{1/2}^2}{2F_{-1/2}}\right)$$
(4b)

where, *a* is the width of a 1D structure with a square cross section, m_x is the effective mass component in the *x* direction (Figure 2.1 (b)), *v* is the phonon group velocity, *T* is the temperature, θ is the Debye temperature, $\xi = h\omega/k_BT$ ($h\omega$ being the phonon energy), Λ is the phonon mean free path ($\Lambda(\xi) = v(\xi)\tau_c(\xi)$), η is the ratio between the wire width and Λ ($\eta(\xi) = a\pi/\Lambda(\xi)$), *p* is a parameter which characterizes the interface roughness and its effect on the phonon scattering. The value of *p* represents the probability of a phonon undergoing diffusive scattering (refer to [13] for additional details). Other parameters have been defined in Eq. 3a & 3b. The theoretical ZT calculations using Eqs.4a and 4b for a 1D structure show that it strongly depends on its width. For widths smaller than the thermal de Broglie wavelength of the carriers, the ZT increases significantly with decreasing the width of the 1D structure. 1D structures of Bi_2Te_3 and Sb_2Te_3 have been shown to alter their thermal conductivities [10, 14-20]. TMOs such as ZnO and TiO₂ have also been extensively synthesised in 1D morphologies (nanorods, nanoribons and nanotubes) [21, 22] and the thermal conductivity of such materials are strongly affected by such morphological manipulations [21].

2.2.1.4 0D materials

Unlike 2D or 1D structures, the carriers in 0D structures such as quantum dots are confined in all directions. The transport mechanism in 0D structures is thus different from others, in the sense that unconventional conduction behaviour such as tunnelling is required to maintain its electronic conductivity. Therefore, 0D structures such as quantum dot superlattices (QDSLs) and segmented nanowires (SNWs) were proposed to provide a conduction pathway. As the name suggests, such segmented structures consist of a series of interwoven quantum dots of two different materials (Figure 2.1 (c)). The electronic transport along the wire axis occurs by tunnelling between adjacent quantum dots. Furthermore, due to the wire boundaries and interfaces between the quantum dots, the phonon conduction along the wire axis is impeded, resulting in a reduced lattice thermal conductivity.

The lattice thermal conductivity for 0D structures ($\kappa_{phonon0D}$) such as QDSLs and SNWs comprising of two different materials *A* and *B* is defined as [23, 24]:

$$\frac{L}{\kappa_{phonon0D}} = \frac{L_A}{\kappa_{phononA}} + \frac{L_B}{\kappa_{phononB}} + 4\left(\frac{1}{C_A v_A t_{AB}} + \frac{1}{C_B v_B t_{BA}}\right)\left(1 - \frac{t_{AB} + t_{BA}}{2}\right)$$
(5)
$$+ \frac{3}{d_w}\left(\frac{L_A}{C_A v_A \propto_A} + \frac{L_B}{C_B v_B \propto_B}\right)$$

where, $C_{A,B}$ is the heat capacity, $v_{A,B}$ is the sound velocity of the nanodot material, $L_{A,B}$ is the length of the material's segment, t_{AB} and t_{BA} are the average transmissivity of phonons from quantum dot A to B and vice versa, $\alpha_{A,B}$ is the geometric factor that depends on the aspect ratio (L_A/d_w or L_B/d_w) of the quantum dots in which d_w is the diameter of the wire. The first two terms in Eq.5 account for the intrinsic phonon scattering events, while the third and fourth terms account for the contribution of the segment interface and the wire boundary scattering processes to the $\kappa_{phonon0D}$. It is evident that the segment length, the choice of materials *A* and *B*, as well as the aspect ratio of the quantum dots play a vital role in determining $\kappa_{phonon0D}$ and hence, the design of the QDSL or SNW structure is the most important factor governing the thermal properties. In order to quantify the electronic contribution of the thermal conductivity ($\kappa_{electron0D}$) in a QDSL or SNW structure, the Kroenig-Penney model is used. This model determines the dispersion relation $E_{n,m}(k)$ for the electrons that move along the axis in the n,m sub-band of the wire experiencing a square periodic potential [25], where *k* is a 1D wave vector that describes the energies of these electrons in the square potential [24]. The electronic band structure of each sub-band is highly dependent on the segment length (L_A or L_B), the potential barrier height and the transport effective masses [24].

The constant relaxation time approximation is used for calculating the following fundamental integrals for the conduction band [23]:

$$K_{(\alpha)} = \frac{4\tau}{\pi^2 h^2 d_w^2} \sum_{n,m} \int \frac{1}{g_{n,m}(E)} (E_{n,m} - E_F)^\alpha \left(-\frac{\delta f}{\delta E}\right) dE$$
(6a)

$$g_{n,m}(E) = \frac{2}{\pi} \left(\frac{\delta E_{n,m}}{\delta \kappa}\right)^{-1}$$
(6b)

where, α =0,1 or 2, τ is the relaxation time of the carriers, E_F is the Fermi energy, f(E) is the Fermi-dirac distribution function and $g_{n,m}(E)$ is the density of states of the *n*,*m* sub-band, which is defined in Eq. 6b. The electronic component of the lattice thermal conductivity in 0D structures ($\kappa_{electron0D}$) is defined as [23]:

$$\kappa_{electron0D} = \frac{1}{T} \left(K_{(2)} - \frac{K_{(1)}^2}{K_{(0)}} \right)^{1/2}$$
(7)

From Eq. 6a, b & 7, it is clear that $\kappa_{electron0D}$ is strongly dependent on the diameter of the SNWs, as well as the carrier relaxation time. However, as discussed before, the electronic contribution towards the thermal conductivity in semiconducting TE materials is generally much lower, compared to the phonon contribution at small diameters. The superlattice

interfaces in 0D structures such as SNWs are expected to enhance the phonon scattering to further suppress the thermal conductivity compared to the bulk form [26].

The above discussion shows that a reduction in the dimensionality of the system can result in a reduced lattice thermal conductivity, due to the phonon mean free paths being limited by the nanostructuring, and consequently increased phonon scattering. This can potentially enhance the efficiency of TE materials for energy scavenging applications, while can increase the performance of temperature sensors, which are based on such structures.

2.2.2 Electrical conductivity

The electrical conductivity of TE materials in bulk and low dimensional form has been extensively studied [27-30]. It has been shown that quantum confinement of charge carriers alters the electronic density of states (DOS). Various nanostructuring and doping techniques can be employed to alter the carrier concentrations by adjusting the bandgap and surface energy in such TE materials [27]. In this section, we will discuss the theoretical equations that govern the electrical conductivity of TE materials in bulk and low dimensional forms.

2.2.2.1 Bulk (3D) materials

For bulk TMOs, the electrical conductivity can be defined in a simplistic form as follows [2, 25]:

$$\sigma = n(E)e\mu(E) = n(E)e^2 \frac{\tau(E)}{m^*}$$
(8)

where, n(E) is the density of carriers which is a function of the density of states g(E), e is the electronic charge, $\mu(E)$ is the differential carrier mobility, $\tau(E)$ is the relaxation time and m^* is the carrier effective mass.

The m^* of many TE materials such as Bi₂Te₃, Sb₂Te₃ and TE TMOs TiO₂ and layered cobalt oxides is relatively large [2, 31, 32]. Additionally, they also suffer due to short relaxation times [33-35]. As a result, the charge carrier mobilities of many TE materials can be relatively small. The carrier concentrations of bulk TE materials, which is affected by the thermionic effect, depend on their bandgap and temperature. As a result, the carrier mobilities and concentrations in TE materials can be tuned using various doping and nanostructuring techniques.

2.2.2.2 2D materials

The electrical conductivity of TE materials can be enhanced by fabricating quantum well structures, which result in the quantum confinement of carriers. For a 2D quantum well structure discussed previously in section 2.2.1.2, Hicks *et al.* defined the electrical conductivity (σ_{2D}) as [7]:

$$\sigma_{2D} = \frac{1}{2\pi W} \left(m_x^* m_y^* \right)^{1/2} F_0 e \mu_x \left(\frac{2k_B T}{h^2} \right)$$
(9)

where, *W* is the quantum well width, m_x^* and m_y^* are the effective mass components in the *x* and *y* direction (in the plane of the 2D material) respectively, F_0 is the Fermi energy, *e* is the electron charge, μ_x is the mobility, *T* is the temperature, k_B is the Boltzmann constant and *h* is the Planck's constant. In such structures the electrons are confined only to a 2D motion that is parallel to the layers. Eq.9 shows that a reduction in *W* enhances σ_{2D} . In TMOs, the Fermi level can be adjusted using various doping techniques and methods that control stoichiometry. The Fermi level of TE materials is a strong function of morphology and the temperature [36]. As expected, enhanced electrical conductivities have been demonstrated in 2D morphologies of Bi₂Te₃, Sb₂Te₃ [10] and TMOs such as MoO₃, CoO₂ and ZnO nanobelts [37] [38] [39].

2.2.2.3 1D materials

In morphologies such as one-dimensional nanorods, nanotubes or nanobelts of TE materials, σ is predicted to increase by reducing the cross sectional area of the structure. Such enhancement is mainly due to increased charge carrier mobilities *via* changes in DOS [40, 41]. σ in such 1D structures is defined as [12]:

$$\sigma_{1D} = \frac{1}{\pi a^2} (m_x^*)^{1/2} F_{-1/2} e \mu_x \left(\frac{2k_B T}{h^2}\right)^{1/2} \tag{10}$$

where, *a* is the width of a 1D structure with a square cross section, m_x^* is the effective mass component in the *x* direction. Other parameters have been defined in Eq. 9. Additionally, σ can be tuned by changing the Fermi levels, which result in the carrier concentration change as well [42] [43].

Conventional TE materials such as Bi_2Te_3 , Sb_2Te_3 and TMOs such as TiO_2 and ZnO are widely synthesised in various 1D morphologies [14-22]. As predicted, σ in such quasi-1D structures is shown to increase compared to the bulk forms [42]. The carrier concentrations in such structures can be adjusted by the use of suitable dopants [42, 44]. There are many good review articles that cover the topic of electrical conductivity in various 1D TE structures [42, 45].

2.2.2.4 0D materials

QDSL or SNW structures, described in section 2.2.1.4, allow for electrical conduction through mechanisms such as tunnelling or hopping. Well-separated discrete energy states of the segments alter the fundamental properties such as DOS and bandgap energy in an alternating manner along the 1D wire [46, 47]. At the same time, the 0D characteristics, and in particular the electrical conductivity, of each quantum dot is maintained by the energy differential of the conduction or valence bands between the two constituent materials that form the wire [24]. The electrical conductivity for such 0D structures is defined as [23, 24]:

$$\sigma_{0D} = e^2 K_{(0)} \tag{11}$$

 $K_{(\alpha)}$ is defined in Eq. 6a. It can be seen from Eq.11 that the σ_{0D} is a strong function of the diameter as well as the electronic DOS. An enhanced σ is expected in QDSL and SNW structures with reducing diameters. This is mainly because of the increased carrier relaxation times in such low dimensional structures [47].

2.2.3 Seebeck coefficient

The Seebeck coefficient is the magnitude of the induced voltage divided by the temperature gradient across a material. The Seebeck effect is caused by charge-carrier diffusion and phonon drag. TE materials such as Bi_2Te_3 , Sb_2Te_3 and TE TMOs such as TiO_2 , ZnO, CoO and MnO₂ exhibit large Seebeck coefficients. Such a high *S* usually arises from high effective masses (m^*) due to electronic correlations [48] or from electron–electron interactions [49]. An enhancement in the *S* can be achieved by altering the DOS through nanostructuring techniques. The theory governing the *S* of bulk and low dimensional TE materials is presented in this section.

2.2.3.1 Bulk (3D) materials

For semiconducting TE materials in bulk form, the simplified Seebeck coefficient can be estimated by the following expression [2]:

$$S_{bulk} = \frac{8m^* \pi^2 k_B^2}{3eh^2} T\left(\frac{\pi}{3n}\right)^{2/3}$$
(12)

where, *n* is the carrier concentration, m^* is the carrier effective mass, *e* is the electronic charge, *T* is the temperature, *h* is Planck's constant and k_B is the Boltzmann constant.

Eq.12 shows that a higher m^* results in larger Seebeck coefficients. Bi₂Te₃, Sb₂Te₃ and TMOs usually exhibit high effective carrier masses, which explain the high *S* values observed in these materials. From Eq. 12 it is also predicted that in an increase in *T* also enhances *S*. Enhanced *S* has been observed in Bi₂Te₃, Sb₂Te₃ and many TMOs such as ZnO and MnO₂ at elevated temperatures [50, 51] and will be discussed in their relevant sections.

2.2.3.2 2D materials

2D quantum well structures can result in enhanced *S* of TE TMOs materials due to changes in the Fermi energy of the carriers as well as the electronic DOS. For a 2D quantum well structure, the Seebeck coefficient is defined as [7]:

$$S_{2D} = -\frac{k_B}{e} \left(\frac{2F_1}{F_0} - \chi_{2D}^* \right)$$
(13a)

$$\chi_{2D}^* = \frac{1}{k_B T} \left(E_F - \frac{\pi^2 k_B^2 T^2}{12E_F} - \frac{h^2 \pi^2}{2m_z^* W^2} \right)$$
(13b)

where, k_B is the Boltzmann constant, e is the electron charge, E_F is the Fermi energy, T is the temperature, m_Z^* is the component of the effective mass, W is the quantum well width and F_i are Fermi-Dirac functions. χ^*_{2D} is the reduced chemical potential for quasi-2D structures.

The decrease in *W* of the quantum well is predicted to result in an enhanced *S* as can be seen from Eq. 13a & b. Additionally, the electron filtering (i.e. only high energy electrons can pass while others are scattered) [52] in such low-dimensional heterostructures is expected to decouple the *S* and σ , allowing fairly independent control over these properties. The phenomenon of electron filtering is explained in more detail elsewhere [47, 53]. Enhanced *S* has been demonstrated in 2D structures of Bi₂Te₃ and Sb₂Te₃ [9, 10]. In 2D TMOs, an increase in *S* has also been experimentally observed. Ohta *et al.* demonstrated dramatic increases in *S* (up to ~ 5 times) for 2D electron gas (2DEG) systems based on doped TiO₂ which will be discussed in detail in Section 2.4.3.3 [54, 55]. 2D layered cobalt oxides and rhodium oxide also show higher *S* compared to their bulk forms [56, 57].

2.2.3.3 1D materials

Bi₂Te₃. Sb₂Te₃ and TMOs are widely synthesised in various 1D morphologies [20, 22, 58-60]. Size reduction to a single dimension is expected to enhance *S* due to the altered DOS. The *S* for a 1D structure is defined as [12]:

$$S_{1D} = -\frac{k_B}{e} \left(\frac{3F_{1/2}}{F_{-1/2}} - \eta \right)$$
(14)

where, F_i is the Fermi Dirac function, e is the electronic charge, k_B is the Boltzmann constant and $\eta = \zeta / k_B T$ is the reduced chemical potential, in which ζ is the chemical potential relative to the lowest bound state. In a 1D structure, S is influenced by the Fermi level of the carriers (Eq.14), which in turn is strongly influenced by the width of the 1D structure (see ref.[12] for details). Hence, an enhancement of *S* is predicted with decreasing width of the 1D structure. *S* is also a function of the energy derivative of the electronic DOS [61]. As the dimensionality decreases, an increase in Seebeck coefficient is expected because of changes in the DOS due to quantum confinement [7, 8, 12, 62]. As predicted, the *S* of 1D structures of Bi₂Te₃, Sb₂Te₃ and TE TMOs such as ZnO nanowires is shown to increase due to quantum confinement [14-20, 45].

2.2.3.4 0D materials

QDSL and SNW structures as described in section 2.2.1.4 exhibit sharper DOS compared to higher dimensional structures, due to the superlattice-like structure along the wire axis (Figure 2.1 (c)). An electronic structure with sharp maxima in the DOS like this is predicted to be the best for TE materials [46, 63]. Due to their unique electronic band structure and sharp density of states, an enhancement of *S* is expected in QDSLs and SNWs [46].

The Seebeck coefficient of a segmented nanowire is defined as [23, 24]:

$$S_{0D} = -\frac{1}{eT} \left(\frac{K_{(1)}}{K_{(0)}} \right)$$
(15)

From Eq. 6 a, b and 15 it is obvious that a sharp maximum in the electronic DOS (Figure 2.1 (d)) will result in a strong increase in the Seebeck coefficient. As the diameter is decreased, the size quantisation effects prevail, resulting in an enhanced *S*. Experimentally, QDSLs and SNWs of materials such as Bi_2Te_3 , PbTe have been shown to enhance *S* [23, 64-70] [46]. The increase of *S* in such 0D TMO structures is expected to be pronounced. Even though metal oxide based SNWs have been synthesized [42, 71], there are no reports investigating their Seebeck coefficients. This presents a vast potential for future work in the field of TE TMOs.

From the discussion in this section, it is evident that reducing the dimensionality of TE materials offers opportunities to tune the key TE parameters of κ , σ and S independently.

There has been a continuous development in the synthesis techniques of TE materials in various morphologies. This allows flexibility in their fabrication which can be carried out at both large and small scales using liquid and gas phase deposition techniques, allowing tuning of their TE properties at low dimensions to engineer TE materials with high TPFs and figures of merit. Recent review articles comprehensively discuss the latest developments in the synthesis of nanostructures of TE materials [70, 72].

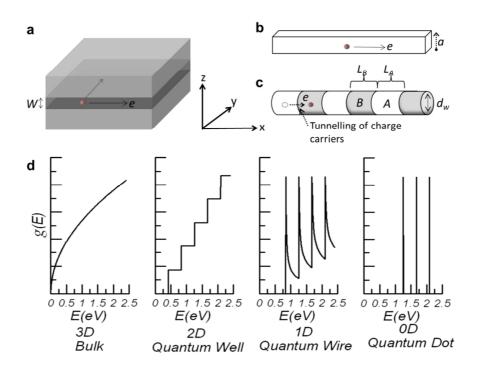


Figure 2.1: (a) A 2D quantum well structure with width W, (b) 1D conductor (nanowire) with a square cross section of width a, (c) a segmented nanowire superlattice of diameter d_w comprising of quantum dots (0D) of alternating materials A and B, with respective segment lengths L_A and L_B . (d) Energy dependence of the electronic DOS in 3D, 2D, 1D and 0D materials. ((c), (d) Reproduced with permission from [24] and [25].)

2.3 Strategies to tune and alter TE parameters

The performance of TE materials is assessed on the basis of the application. Applications of TE materials can be classified into four major categories: (1) cooling and refrigeration, (2) energy scavenging from heat, (3) sensors and (4) thermopower wave sources. For cooling, refrigeration, and energy scavenging, a high TPF along with a low κ is desirable [73, 74]. Sensors generally require high *S* and low κ , while σ can be either high or low depending on

the type of sensor. Thermopower wave sources require a high TPF and benefit from a high κ [1, 50, 75, 76]. Hence, the tuning of the key TE parameters depends on the application.

Furthermore, a fundamental understanding of the carrier transport processes contributing to the TE effect is required. There are however, many complexities in determining the key quantities in electron and phonon transport both theoretically and experimentally [77-79]. Tuning of transport properties of TE materials, such as reducing electronic thermal conductivity [80] or reducing the bipolar effect [81, 82], is possible. In their recent review papers, Minnich *et al.* [79] and Zebarjadi *et al.* [77] have extensively covered the challenges and strategies for improving our understanding of carrier transport processes.

In this section, the techniques that are commonly used to alter the materials' key TE parameters are briefly discussed.

2.3.1 Optimization using stoichiometry and doping technique

The incorporation of dopants and altering of stoichiometry are widely employed for adjusting the TE parameters of of materials such as Bi₂Te₃ and Sb₂Te₃ and TMOs [83-87]. The type of application plays a crucial role in determining the correct technique in this regard [88]. For cooling, refrigeration, heat scavenging and sensing applications, methods that reduce κ_{phonon} are generally desirable. Crystal disorder in the unit cell can be created by doping or altering stoichiometry of the materials' crystal lattice [30]. Such manipulations change the vibrational properties of the crystal and influence κ_{phonon} [2] or by introducing additional scattering sites for phonons, thereby limiting κ_{phonon} [19, 89-92]. $\kappa_{electron}$ is also affected by changing the stoichiometry and doping level in TE materials. $\kappa_{electron}$ depends on the electrical conductivity of the material (Eq. 2b) and is also a function of the Fermi level and charge carrier concentration, which are directly affected by changes of stoichiometry or incorporation of dopants [3]. In many refrigeration and heat scavenging applications, high electrical conductivity is desired, which generally directly increases $\kappa_{electron}$. However, this is not desirable as it enhances the exchange of heat between two sides. Hence, doping,

compositing and processes altering the oxygen deficiency can be implemented to achieve the desired thermal conductivity. Conversely, in thermopower wave sources, high TPF and κ are desirable. This can be achieved by the use of metallic dopants. Such dopants result in enhanced TPFs in Bi₂Te₃, Sb₂Te₃ and TMOs such as ZnO and CoO₂, which will be discussed in details in section 2.4 [93-105] [106].

After incorporating dopants and altering the stoichiometry, the most challenging issue is the determination of electronic band structures [77]. Theoretical methods such as density functional theory (DFT) can help; however, underestimation of the band gap by DFT calculations generally results in inaccuracy of theoretical predictions of the Seebeck coefficient and the bipolar effect [77]. Many methods have been developed to address this issue, such as the dynamical mean-field theory (DMFT) [107] [108].

The calculation of electron mobility and carrier lifetime is even more challenging. First principles calculations can only be performed on limited supercell sizes and the inclusion of long range potentials is difficult [77]. More importantly, inelastic scattering mechanisms at the elevated operating temperatures renders relaxation time approximations (RTA) calculated from first-principles and DFT mostly invalid [109, 110]. The details of carrier lifetimes in many TE materials are still relatively unknown. Hence, an improved fundamental understanding of the mechanisms governing the formation, stability, and properties of interfaces is required [52].

2.3.2 Substructuring

In engineering TE materials, it is generally desirable to decouple κ_{phonon} and $\kappa_{electron}$. For many refrigeration and heat scavenging applications it is desired to adjust κ_{phonon} without affecting σ (hence $\kappa_{electron}$). Substructuring (or segmentation) approaches are suggested to be efficient for such manipulations. Substructuring relies on a periodic arrangement of layers with different electron and phonon transport characteristics, resulting in a complex material structure with distinct regions providing particular functionalities (Figure 2.2). For many refrigeration and heat scavenging applications, an ideal TE material would comprise a high mobility semiconductor region entwined with a phonon scattering region that houses disordered structures (dopants and lack of stoichiometry), without affecting the carrier mobilities of the other region [2]. A detailed discussion on the substructuring approach is provided in another review [2]. TE materials occurring as natural superlattices can provide an independent control of transport properties, providing an excellent platform to engineer high performance TE materials. TMOs such as the doped cobalt oxide systems are a classic example of the benefits of substructuring approach, which will be discussed in detail later [111]. Another advantage of TMOs is that they can be fabricated in a variety of well-studied structures and a large number of synthesis techniques to fabricate them in different morphologies and structures have been well-established, making the substructuring approach highly attractive in order to tune their TE parameters according to the desired application.

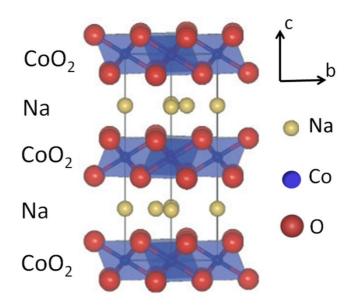


Figure 2.2: Schematic depiction of the substructuring approach in doped cobalt oxide, comprising of ordered CoO_2 layers that are separated by disordered layers (of Na dopant) to achieve a good electrical conductivity and poor phonon conductivity. (Reproduced with permission from [38].)

2.3.3 Nanostructuring

As discussed earlier, the S, σ and κ for conventional 3D crystalline TE materials are interrelated and cannot be controlled independently. Any increase in σ results in an enhanced $\kappa_{electron}$ (Eq. 2b). Additionally, a change in the Fermi level and carrier concentration affects both $\kappa_{electron}$ and κ_{phonon} .

At the nanometer scale, there are significant changes to the electronics of TE materials (see section 2.2), which allow for alternative techniques to control the *S*, σ and κ in a relatively independent manner. In nanostructured materials, quantum confinement effects [47] and surface properties become much more important, and result in properties that are changed from those of the bulk forms. The quantum confinement of carriers in nanostructured TE materials is predicted to enhance both their TPF and ZT (see section 2.2) [62]. Additionally, it is well known that nanostructuring of TE materials alters their Fermi level and carrier concentration [27]. Nanostructures also introduce additional scattering mechanisms. If the spacing between the nanoparticles is larger than the electron mean free path (MFP), they will act as an additional source of electron scattering in the host material. If however, the spacing is smaller than the electron MFP, the scattering mechanisms will become much more complex since the leakage of the electron wave into the nanoparticles is no longer negligible [77, 112]. The nanostructuring technique has resulted in enhanced TPFs and ZTs in Bi₂Te₃, Sb₂Te₃ and TMOs such as TiO₂, ZnO, cobalates and manganates which will be discussed in detail in Section 2.4 [54] [101] [113, 114].

In addition to the electronics of TE materials, their phonon propagation properties and as a result κ_{phonon} can be tuned *via* nanostructuring (see section 2.2.1), resulting in enhanced phonon scattering and altered phonon mean free paths [114]. If the dimensions of semiconducting TE materials are smaller than the mean free path of the phonons, but larger than the mean free path of the charge carriers, a reduction in κ_{phonon} can be obtained due to boundary scatterings, without affecting σ . Dressalhaus *et al.* have reviewed the latest developments in nanostructured TE materials such as Bi₂Te₃ and Sb₂Te₃ based materials [70], while Koumoto *et al.* have reviewed the progress in the development of nanostructured TE TMOs [11].

Nanostructuring can be implemented to decrease the lattice thermal conductivity by introducing many interfaces with spacing smaller than the phonon mean free path. Although reducing lattice thermal conductivity through alloying and/or nanostructuring techniques has been the most effective way to improve performance of TE materials for conventional applications, details of phonon transport mechanisms are still not very well understood [79]. Even in bulk form, theoretical and experimental determination of quantities such as phonon mean free path is still a challenge [79]. Phonon transport models based on Callaway model of thermal conductivity [115] usually require adjusting various fitting parameters causing inconsistency in the models fundamental predictions such as phonon's wavelength and mean free path. Calculations of the thermal conductivity and phonon mean free path in TE materials using combined density functional theory (DFT) [116, 117] and molecular dynamics (MD) [118-120] simulations on the other hand are difficult and computationally costly because of the extremely complex crystal structure of alloys and misfit layered oxides. Moreover, the introduction of many interfaces in the material *via* nanostructuring adds more complexity to the problem.

The problem is even more complex in case of electron transport. In case of heavily doped complex TE materials, the standard analysis based on the Boltzmann equation with the assumption that the mean free path is much larger than the de Broglie wavelength leads to inaccurate results [79, 121]. Nanostructuring further complicates the problem as the interfaces introduce complex scattering mechanisms that should be accounted for in theoretical analysis [122]. Therefore, modeling the transport phenomena in bulk and nanostructured TE materials would require more powerful tools such as the non-equilibrium Green's functions with the inclusion of electron wave effects [79].

2.3.4 Compositing

It is suggested that composites can be useful in controlling TE parameters of Bi_2Te_3 , Sb_2Te_3 and TMOs, as they can be designed to show high density of the interfaces [123], that can be used for adjusting both phonon and electron scattering. An excellent review article discussing the impact of the bulk composite engineering approaches on *S*, σ and κ can be seen in ref. [79]. Composites of materials such as Bi₂Te₃, Sb₂Te₃ and TMOs have resulted in enhanced TPFs, which will be discussed later in the relevant sections [10, 124] [101, 125-129].

2.4 Bi₂Te₃, Sb₂Te₃ and TMOs- TE properties

In this section, the TE properties of Bi_2Te_3 , Sb_2Te_3 and TMOs will be discussed. An overview of their crystal structures and their TE properties in pure and doped states will be presented. Additionally, different synthesis methods of these TE materials will be illustrated. For further information regarding the structures, properties and synthesis of Bi_2Te_3 , Sb_2Te_3 and TMOs, the readers can refer to comprehensive text books in this field [130-132].

2.4.1 Bi₂Te₃

2.4.1.1 Crystal structure

 Bi_2Te_3 is a n-type semiconducting material with a bandgap of ~ 0.20 eV [133]. A detailed description of its electronic band structure exists elsewhere [134, 135]. It exhibits a rhombohedral crystal structure [136] comprising of 5 atoms in a unit cell [137, 138] and is stable up to temperatures of ~ 525 K [82]. The TE properties of Bi_2Te_3 in a pure and doped form have been widely investigated and are discussed next.

2.4.1.2 TE properties of pure Bi₂Te₃

Bi₂Te₃ is the most widely used TE material at room temperature. In a pure bulk form, it exhibits *S* of approximately –190 μ V/K and a high σ of the order of 10⁵ S/m [139]. Its thermal conductivity is ~ 1 W/m.K [18]. Its TPF and ZT is of the order of 10³ μ W/m.K² and 0.4, respectively, at 298 K (room temperature). Theoretical models suggest that a reduction in dimensionality can result in enhanced TPFs due to significant changes in the density of states (section 2.2) [7, 12]. The TE properties of low dimensional morphologies of Bi₂Te₃ such as nanotubes, nanowires and nanosheets have been extensively investigated [14-19]. As predicted, such nanostructures show enhanced TPFs and ZTs of the order of $2.4 \times 10^3 \,\mu$ W/m.K² and 0.96 respectively mainly on account of enhanced *S* and smaller κ [140-142].

Such high TPFs makes Bi_2Te_3 an attractive candidate for thermopower wave sources. Their low thermal conductivities can be compensated by placing them on thermally conductive substrates such as alumina (Al₂O₃).

2.4.1.3 TE properties of doped and composite Bi₂Te₃

The doping and compositing techniques are commonly utilised to alter *S*, σ and κ of Bi₂Te₃ in order to enhance the TPFs and ZTs. The incorporation of dopants provides additional scattering sites for phonons, thereby suppressing the phonon thermal conductivity. Doped Bi₂Te₃ has been shown to exhibit TPFs and ZTs of the order of $5\times10^3 \,\mu$ W/m.K² and 1 respectively [83-86]. The compositing strategy has also been widely employed to adjust the TE parameters of Bi₂Te₃ [82, 128, 143]. Many Bi₂Te₃ composites and superlattice structures have been studied and ZTs as high as 2.4 have been observed for its superlattice with Sb₂Te₃ [10, 124]. Composites of Bi₂Te₃ in low dimensional morphologies such as nanowires and nanotubes have also been reported [144, 145]. Such structures have been shown to consistently exhibit ZTs higher than one [69, 70, 146, 147]. A review article covers the most recent advances in the development of low dimensional TE Bi₂Te₃ [70].

2.4.1.4 Methods of synthesis

Various liquid and vapour phase techniques have been shown to synthesise Bi_2Te_3 in a variety of morphologies. Commonly used liquid phase techniques include hydrothermal [144] and electrochemical methods such as electrodeposition [139, 148].

Vapour phases techniques such as RF magnetron sputtering [149], pulsed laser deposition (PLD) [150], thermal evaporation [151], metal organic chemical vapour deposition (MOCVD) [152], flash evaporation [153] are also used to synthesise Bi₂Te₃.

2.4.2 Sb₂Te₃

2.4.2.1 Crystal structure

 Sb_2Te_3 is a p-type semiconductor with a bandgap of ~ 0.28 eV [20]. Similar to Bi_2Te_3 , it exhibits a rhombohedral crystal structure with 5 atoms in a unit cell [138]. A detailed description of its electronic band structure is provided elsewhere [135]. Sb_2Te_3 is stable up to temperatures of ~ 550 K. The TE properties of pure and doped Sb_2Te_3 are discussed next.

2.4.2.2 TE properties of pure Sb₂Te₃

Sb₂Te₃ is a widely studied TE material. In a pure bulk form, it exhibits *S*, σ and κ of 180 µV/K, 10⁴ S/m and 2.5 W/m.K respectively [154] [155]. The TPF of bulk Sb₂Te₃ has been reported to be of the order of 10² µW/m.K² [155]. The TE properties of Sb₂Te₃ has also been investigated for a variety of low dimensional morphologies such as nanowires[20] and nanosheets [156]. As predicted (section 2.2), such nanostructures show enhanced TPFs and ZTs of the order of 10³ µW/m.K² and 0.58 respectively at 420 K [156]. Such an increase is mainly attributed to increased *S* (~210 µV/K) and lower κ (~0.76 W/m.K) achieved as a result of quantum confinement. Such high TPFs make Sb₂Te₃ a plausible candidate for implementation as the core TE material in thermopower wave sources. Additionally, such a p-type semiconducting material can be used to demonstrate thermopower wave system based on such a p-type material has never been developed so far and will be demonstrated by the author of the thesis in chapter 4 of this thesis.

2.4.2.3 TE properties of doped and composite Sb₂Te₃

The doping technique is widely used to alter the TE properties of Sb_2Te_3 . The incorporation of dopants can be used to tune the key TE parameters of Sb_2Te_3 in a manner described in section 2.3.1. Several reports on doped Sb_2Te_3 and its TE properties exist in literature [86, 157-162]. Such doped Sb_2Te_3 has been shown to demonstrate TPFs and ZTs of the order of $10^3 \mu$ W/m.K² and 0.6 respectively. Compositing of Sb_2Te_3 has also been demonstrated to alter its key TE parameters [82, 124, 163]. Several Sb_2Te_3 composites have been shown to exhibit high ZTs [125-128]. The maximum ZT has been reported to be 1.56 at 300 K for $Bi_{0.52}Sb_{1.48}Te_3$ [145]. As previously mentioned, low dimensional structures such as Bi_2Te_3/Sb_2Te_3 superlattices have been shown to exhibit large ZTs of up to 2.4 [10] [152].

2.4.2.4 Methods of synthesis

Many liquid and vapour phase techniques have been shown to fabricate different morphologies of Sb₂Te₃. Liquid phase techniques such as hydrothermal [164, 165] and electrochemical methods such as electrodeposition [166] [157] have been shown to synthesise thin films, nanoplates and nanobelts of Sb₂Te₃. Vapour phase techniques such as RF magnetron sputtering [167], ALD [168], MOCVD [169], PLD [170] and flash evaporation [153] have also been shown to synthesise different morphologies of Sb₂Te₃. Vapour phase methods are generally employed to prepare Sb₂Te₃ in doped forms as well as composites as they allow an accurate control over deposition conditions, parameters, dopant concentrations and crystallinity.

2.4.3 Titanium oxides – TiO_x

2.4.3.1 Crystal structure

TiO₂ is one of the most investigated metal oxides for a wide variety of photocatalytic, TE, solar cell, biosensing and gas sensing applications. TiO₂ has a bandgap of ~3.2 eV in its intrinsic form [171]. The most common polymorphs of TiO₂ are anatase, rutile and brookite. Rutile and anatase exhibit a tetragonal structure, while brookite is orthorhombic [172]. The transformation with increasing temperature usually follows the sequence: anatase \rightarrow brookite \rightarrow rutile. Generally in between room temperature and 598 K anatase is the dominant polymorph. Above 625 K, the anatase transforms to brookite [173]. Heating of titania in the temperature range of 873 to 1275 K leads to an alteration of phase stabilities, and it transforms almost completely to rutile. Many reviews on the various crystal structures, size and temperature dependence of the different polymorphs as well as different morphologies of stoichiometric and non-stoichiometric TiO_x exists [172-174].

2.4.3.2 TE properties of stoichiometric TiO₂

TiO₂ can be synthesised in many different morphologies such as spheroidal nanocrystallites, nanoparticles, nanotubes, nanosheets, nanofibers and epitaxial thin films [175]. The room temperature *S* of crystalline TiO₂ is reported to be approximately -600μ V/K, while σ of the order of 10^3 S/m is observed, resulting in a TPF of 360 μ W/m.K². The κ at room temperature is ~ 5.8 W/m.K and is reduced with increasing temperature (~ 2.8 W/m.K at 1073 K) [176]. Owing to a moderate σ and high κ , the ZT in pure TiO₂ is low (< 0.025) [176, 177]. However, non-stoichiometric TiO_(2-x) has been demonstrated to be promising for TE applications at both cryogenic [178] and elevated temperatures [177]. The TE properties of reduced, oxidized and doped TiO₂ are discussed next.

2.4.3.3 TE properties of non-stoichiometric, doped and composite TiO_x

Non-stoichiometric TiO_x can show fascinating TE properties both at elevated and cryogenic temperatures. Tsuyomoto *et al.* have shown that TiO_x (x=1.94) with an orthorhombic crystal structure, exhibits a peak S of $-518 \,\mu\text{V/K}$ and σ of 2×10^3 S/m at ~350 K. They demonstrated that both S and σ increase with temperature, resulting in a TPF of ~540 μ W/m.K² at 343 K [179]. Interestingly, single crystal rutile TiO_2 reduced to $TiO_{(2-x)}$ via annealing in H₂ at elevated temperatures as high as 1050 K shows exceptionally high TPFs at cryogenic temperatures. TiO_(2-x) generates enlarged phonon scattering by the defect planes, resulting in low thermal conductivities (0.83 W/m.K). Figure 2.3 (a,b) depict that $TiO_{(2-x)}$ can exhibit an extraordinary S of up to -60,000 μ V/K, with TPF and ZT of ~ 1.7×10⁴ μ W/m.K² and 0.1, respectively, at temperatures in the range of 10 K [178]. Another study showed that nonstoichiometric TiO_(2-x) with a rutile crystalline structure, formed after annealing and reduction in a carbon environment at 1373 K, demonstrates a TPF of 100 µW/m.K² at temperatures of up to 550 K [177]. Obviously, the introduction of oxygen vacancies in the TiO₂ crystal result in enhanced σ due to an increase in carrier concentration (Eq. 8). In contrast, a prolonged oxidation of TiO₂ at elevated temperatures, results in lower σ and S $(-600 \text{ to } +150 \,\mu\text{V/K})$ and therefore low TPFs and ZTs (<0.1). Additionally, a transition

from n-type to p-type is also observed in the oxidation process, at temperatures around 1300 K [180].

In addition to the change of stoichiometry, the doping technique is usually employed to tune the TE properties in TiO₂. As discussed in section 2.3.1, metallic dopants are useful as they result in enhanced electrical conductivities. Additionally, the doping process creates crystal disorder, which reduces the lattice thermal conductivities. It has been shown that Na doped titanate nanotubes (DTNTs) with a composition such as $Na_{2-x}H_xTi_3O_7$ result in TPFs ranging between 174 - 280 µW/m.K², and a peak ZT of 0.3, at elevated temperatures (745-1032 K) [181]. 2% Nb doped, anatase, n-type TiO₂ epitaxial films show a TPF and ZT of 250 µW/m.K² and 0.25, respectively, at 900 K [182]. Similar observations have also been made by Sheppard *et al.* at elevated temperatures [183, 184].

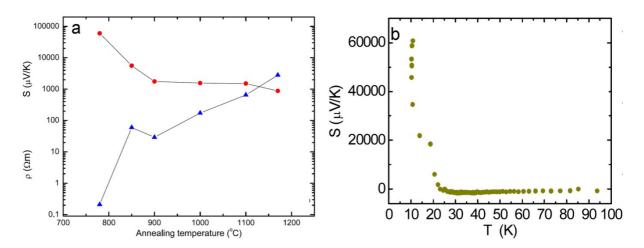


Figure 2.3: (a) Seebeck coefficient (red) and electrical resistivity (blue) of reduced single crystal rutile TiO_x as a function of annealing temperature and (b) Seebeck coefficient as a function of temperature for a sample annealed in H₂ at 1053 K. (Reproduced with permission from [178].)

A TiO₂ composite commonly investigated for its excellent TE properties is strontium titanate (SrTiO₃), also known as STO [55, 185, 186]. STO is a perovskite type oxide that exists in an isotropic cubic crystal structure at temperatures above 100 K. Additionally, it shows a strong structural tolerance to substitutional doping. Due to its *d*-band nature, the effective mass of carriers is quite large in STO, resulting in a high *S* (Eq.12). Additionally, STO exhibits a very high melting point (~2350 K), suggesting its stability at high temperatures [11].

In its pure form, STO is essentially an insulator; however, it can be tuned to be semiconducting or metallic by substitutional doping with La³⁺ or Nb⁵⁺[55]. The highest TPF and ZT for La and Nb doped STO single crystal has been reported to be 3600 μ W/m.K² and 0.1, respectively at room temperature, while the corresponding values at 1000 K, are 865 μ W/m.K² and 0.27, respectively (Figure 2.4 (a-e)) [187] [185, 186] [188]. A number of studies on the TE properties of La and Nb doped STO thin films exist [182] [188] [189]. The ZT values are limited primarily due to its high κ (~11.0-3.2 W/m.K in the temperatures of 300-1000 K respectively) [11]. This high κ value can be ascribed to the perovskite type structure of STO, which even in the presence of dopant cations as point defects, lacks effective phonon scattering centers.

Muta *et al.* suggested that a Ca²⁺ substitution at Sr²⁺ sites may result in reduced κ , as it is established that such substitutions result in the introduction of defects that usually lower κ [190]. However, Yamamoto *et al.* have reported that such an approach results in a dramatic reduction of the TPF, which indicates that any further improvement in ZT is almost impossible to achieve in a conventional 3D bulk state of STO [191].

A reduction in the STO dimensionality is a strategy that is predicted to enhance TE properties by offering independent control of the key TE parameters (section 2.2). The fabrication of a two-dimensional electron gas (2DEG) can be useful as it results in a 2D quantum confinement of carriers. Ohta *et al.* utilized a high density 2DEG, which is confined within a layer of STO that has a thickness of a unit cell (0.3905 nm) [54]. Such 2DEG is realized in SrTiO₃/SrTi_{0.8}Nb_{0.2}O₃ superlattices and TiO₂/SrTiO₃ heterointerfaces. It was shown that in an optimised state, a 2DEG exhibits a massive TPF of $1.0 \times 10^5 \,\mu$ W/m.K². The resultant ZT at room temperature was approximately 2.4 even if a κ value of a bulk single crystal STO is used (12 W/m.K). A recently published review article discusses new developments in STO based thermoelectrics in detail [89].

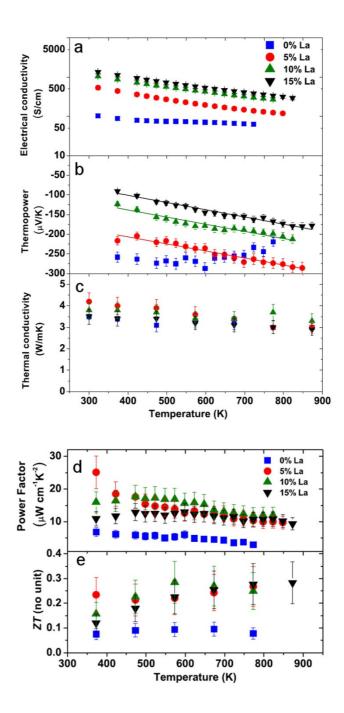


Figure 2.4: (a) Electrical conductivity, (b) Seebeck coefficient, (c) thermal conductivity, (d) TPF and (e) ZT *vs* temperature for different concentrations of La dopant in STO thin films. (Reproduced with permission from [188].)

2.4.3.4 Methods of synthesis

Many different vapour chemical based methods have been used for forming TE TiO_2 materials. Chemical synthesis which involves sol gel hydrolysis, electrochemical methods such as anodization of Ti and hydrothermal synthesis have been commonly used for

producing doped or non-stoichiometric TiO_2 , as the concentration of dopants and metal/oxygen ratios can be readily controlled in such methods [175][192] [181].

Vapour deposition techniques including sputtering and pulsed laser deposition (PLD) have also been commonly used for forming highly crystalline TiO₂ with predetermined concentrations of dopants [182]. STO thin films doped with both La and oxygen vacancies have been shown to be synthesized using the PLD technique [188] [193]. PLD can also be used in forming 2DEG STO crystals comprised of superlattices of insulating/ Nb-doped layers of STO to achieve very high TPF of $1.0 \times 10^5 \,\mu$ W/m.K² [54, 55].

2.4.4 Manganese oxides – MnO_x

2.4.4.1 Crystal structure

MnO₂, the most common form of manganese oxide, is a small bandgap (~ 1.3 eV), n-type semiconductor and is widely used for electrodes in supercapacitors, electrochemical batteries and microbial fuel cells [194] and as a catalytic material [195]. It exists in a number of structural forms [196, 197]. The most common polymorphs are the α -MnO₂ (psilomelane - monoclinic structure) and β -MnO₂ (pyrolusite - rutile structure) [194]. Other forms known as δ -, γ - and λ -MnO₂ also exist, and differ in the way in which the MnO₆ octahedra are linked [192, 198, 199]. A detailed study of various crystal phases of MnO₂ is presented elsewhere [197].

2.4.4.2 TE properties of stoichiometric MnO₂

 β -MnO₂ has been reported to be promising for TE applications at elevated temperatures [51, 196]. Although, the semiconducting properties of α -, β - and γ -MnO₂ have been studied in detail [200], their TE properties have not been widely investigated, and only a limited number of studies exist. It has been reported that bulk and thin film β -MnO₂ exhibit *S* of approximately –300 μ V/K and σ of 10³ S/m, resulting in a TPF of 90 μ W/m.K² [201]. Recently, Song *et al.* reported extremely high Seebeck coefficients in β -MnO₂ nanopowder [196]. The *S* and σ of the MnO₂ thin films have been shown to increase dramatically with temperature [51]. A Seebeck coefficient of approximately –1900 μ V/K at a temperature of

623 K has been demonstrated. The σ of the thin films at such elevated temperatures is ~10³ S/m, resulting in a TPF of 3600 μ W/m.K². The κ for MnO₂ is reported to be approximately 4 W/m.K [51].

Although the TPF of MnO_2 is high, its ZT is still low. As suggested in section 2.3.3, nanostructuring can be used to tune the TE properties of a material. MnO_2 nanostructures such as nanorods and nanowires have been synthesized *via* various methods [51, 196].

2.4.4.3 TE properties of non-stoichiometric, doped and composite MnO_x

Doping and compositing are good strategies that can be used for increasing TE performance of MnO_x by introducing defects in the crystal structure, thereby impeding the lattice thermal conduction. Polycrystalline, bi-layered LaSr₂Mn_{2-x}Co_xO₇ (x<0.2) has been reported to exhibit extremely low TPFs [202]. However, the most commonly reported manganate stoichiometry for TE applications is the perovskite type $CaMnO_3$. It exhibits an orthorhombic symmetry in which each Mn atom is surrounded by six Mn neighbours. It occurs in two antiferromagnetic crystal phases: the A-type and G-type, out of which the G-type phase is more stable. The G-type phase exhibits an indirect bandgap of 0.7 eV, which accounts for its perfect semiconducting behavior [203]. The mixed valent, perovskite electron doped manganite $CaMnO_3$ has been shown to be a promising n-type TE material, especially at high temperatures [19]. This perovskite system exhibits S of $-350 \,\mu\text{V/K}$ and σ of 50 S/m, resulting in a TPF of 6.1 μ W/m.K², which is very low for TE applications. However, the electrical conductivity of such an oxide can be enhanced by introducing suitable dopants [11]. The manganate may be doped on either site. The most commonly used dopant is ytterbium (Y) on the calcium site and niobium (Nb) on the manganese site. The Y doping is particularly beneficial as it results in a lower κ and has been shown to be the most effective dopant [19, 89-91].

A peak TPF of 300 μ W/m.K² has been reported in CaMn_{0.96}Nb_{0.4}O₃ at 1000 K. The highest reported value of ZT is 0.2 at 1000 K for the stoichiometry Ca_{1-x}R_xMnO₃, which is much less than the desired value of at least 1, to make it practically applicable in TE modules [204].

Unfortunately, it has been predicted, using the dynamical mean field theory, that ZT>1 in electron doped CaMnO₃ is rather unlikely to be achieved [19].

Koumoto *et al.* used a nanostructuring approach in an effort to enhance the TE performance as predicted in section 2.3.3 [11]. They showed that $Ca_{0.9}Yb_{0.1}MnO_3$ nanoparticles synthesised using gas phase reaction (GPR) show a higher TPF and ZT compared to those synthesised using solid state reaction (SSR) or liquid phase reaction (LPR). This is because GPR generally results in smaller and impurity-free particles due to the nature of the reaction medium. The highest value of the TPF was 190 μ W/m.K² at 973 K, for the GPR synthesised nanoparticles, mainly due to lower electrical resistivity. The maximum ZT value was 0.13 at 1073 K for particles synthesised using the GPR, which was approximately 1.5 times higher compared to the one's synthesised using SSR at the same temperature [11]. In this case, there was no significant enhancement in the TPF and ZT after nanostructuring.

2.4.4.4 Methods of synthesis

Similar to other metal oxides, various liquid and gas phase synthesis techniques have been used for forming MnO₂. Electrochemical techniques such as anodization and electrodeposition are some of the commonly used liquid phase methods [205-208]. Chemical techniques such as the sol-gel and hydrothermal are also used to prepare crystalline α and β -MnO₂ [209-211]. Vapour phase techniques such as PLD, atomic layer deposition (ALD) and molecular beam epitaxy (MBE) have also been used to synthesise MnO₂ thin films [212-214].

2.4.5 Tungsten oxides – WO_x

2.4.5.1 Crystal structure

Tungsten oxides (WO_x) are widely studied for sensing, chromic and photocatalytic properties [58] and WO_3 is the most commonly investigated stoichiometry of WO_x . WO_3 is an n-type TMO with a perovskite-like structure. It is well known for its various properties in a non-stoichiometric form, as its lattice can support a significant concentration of oxygen vacancies [58, 215]. Crystals of WO_3 are formed by the corner and edge sharing of WO_6 octahedra.

Such corner sharing results in the following crystal phases: monoclinic I (γ), monoclinic II (ε), triclinic (δ), orthorhombic (β), tetragonal (α) and cubic (although cubic is not a commonly observed phase) [58]. Under different temperature conditions, bulk WO₃ follows the following sequence: monoclinic II (ε -WO₃, < 230 K) \rightarrow triclinic (δ -WO₃, 230 to 290 K) \rightarrow monoclinic I (γ -WO₃, 290 K to 603 K) \rightarrow orthorhombic (β -WO₃, 603 K to 1013 K) \rightarrow tetragonal (α -WO₃, > 1013 K) [216, 217]. At room temperature, γ -WO₃ is the most stable crystal phase [58]. The bandgap of WO₃ ranges between 2.6-3.25 eV depending on the crystal phase and size [58]. Tungsten oxide, which is synthesised or manipulated in liquid media, is very commonly found in hydrated form (γ H₂O.WO₃).

2.4.5.2 TE properties of stoichiometric WO₃

There are only a few studies that have examined the TE properties of stoichiometric WO₃ and WO₃ hydrates [218, 219]. WO₃ exhibits σ ranging between 10–10⁻² S/m depending on the stoichiometry [220]. Additionally, σ is also influenced by the grain size, film thickness and dopants. Hence, the electrical properties are strongly dependent on the synthesis techniques and conditions [221]. It has been shown that the *S* of WO₃ hydrates is highly temperature dependent and generally increases linearly with temperatures between sub-zero to 323 K. Beyond 373 K, *S* decreases exponentially and it also gradually loses the water content at higher temperatures. A peak *S* with an absolute value of 480 μ V/K is observed at 363 K [218]. Due to a low σ , the TPF is poor.

Hutchins *et al.* investigated the TE properties of α -WO₃ films of different thicknesses (100-500 nm) [222]. The *S* of the n-type WO₃ thin films varies with temperature (Figure 2.5 (a)), with the magnitude decreasing with increasing the film thickness, attaining a maximum absolute value of ~ 780 µV/K at a temperature of 350 K. Figure 2.5 (b) shows that σ of a 100 nm thick α -WO₃ film increases exponentially with temperature. The peak TPF of the α -WO₃ films was reported to be of the order of 1 µW/m.K² [222]. Additionally, Patil *et al.* demonstrated *S* of 600 µV/K in stoichiometric WO₃ films at a temperature of 473 K [219]. The κ of stoichiometric WO₃ thin films is 1.63 W/m.K [223]. Undoped WO₃ films thus exhibit a maximum TPF of ~ 4 μ W/m.K², which is rather too low to be considered for many TE applications except possibly in sensors for measuring temperatures.

2.4.5.3 TE properties of non-stoichiometric and doped WOx

Non-stoichiometric tungsten oxides have not shown any improvement in TE performance compared to the stoichiometric counterparts owing to the poor σ [224]. However, using other TMOs for doping WO₃ appears to be an effective approach to manipulate its TE properties. Recently, the TE properties of ZnO doped WO₃ ceramics were investigated [215]. The introduction of ZnO was shown to result in an increased σ , by approximately two orders of magnitude, while causing only a slight drop in *S*. A ZnO doping concentration of 0.5 % was found to be optimal, resulting in a maximum TPF of 1.34 μ W/m.K² at 973 K, which is similar to the values reported in stoichiometric WO₃ and at least four orders of magnitude higher than that of non-stoichiometric WO₃ [225]. The variation of TPF with temperature for different levels of ZnO doping is shown in Figure 2.5 (c). Aluminium oxide (Al₂O₃) doping has also been shown to enhance σ of WO₃ by a factor of 10⁴ [220]. Elevated σ was also observed by adding Co₃O₄, MnO₂, LiO₂ and TiO₂ dopants [226].

To make WO_3 a viable TE TMO, nanostructured WO_3 needs to be investigated for its TE properties. Although, WO_3 nanostructures are widely synthesised and reported for other applications, a detailed investigation of their TE properties has not been carried out.

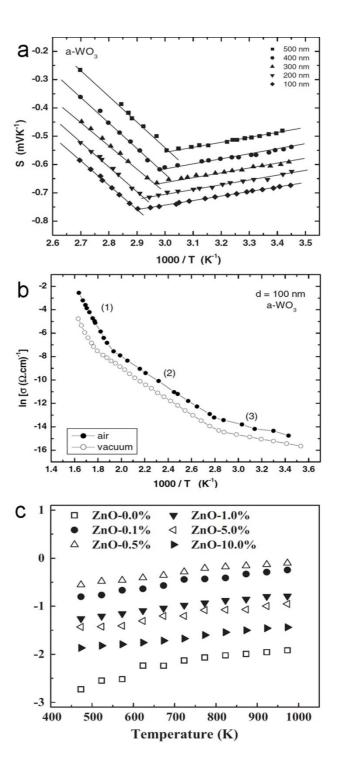


Figure 2.5: (a) Seebeck coefficient, (b) electrical conductivity variation with temperature for α -WO₃ films and (c) TPF obtained for varying ZnO doping concentrations in WO₃ ceramics. (Reproduced with permission from (a), (b) [222] and (c) [215].)

2.4.5.4 Methods of synthesis

Many liquid and vapour phase synthesis methods have been used to synthesise WO₃. Due to a high dependence of σ on the stoichiometry, the parameters of synthesis techniques play important roles in determining the TE properties of WO₃. The commonly used liquid phase techniques to synthesise crystalline WO_3 are sol-gel, hydrothermal synthesis and electrochemical techniques such as anodization and electrodeposition [227-229] [58, 230, 231]. The most common vapour phase techniques include RF sputtering, PLD, electron beam evaporation and thermal evaporation [58, 232, 233]. A detailed review of synthesis techniques for various WO_3 is presented elsewhere [58].

2.4.6 Zinc oxides – ZnO

2.4.6.1 Crystal structure

ZnO is the most widely investigated TMO for a wide variety of photovoltaic, sensing, optoelectronic, piezoelectric and TE applications [39, 234-237]. ZnO is a direct bandgap binary n-type semiconductor with a bandgap of 3.3 eV at room temperature and substantial ionic character residing at the borderline between a covalent and an ionic semiconductor [238]. It can show either a hexagonal wurtzite, cubic zinc-blende (which are both tetrahedral) or rarely rocksalt structure (which is formed at very high pressures) [39] [238]. In wurtzite structure, every Zn atom is surrounded by four oxygen atoms. In zinc-blende structure, each oxygen atom is surrounded by four Zn atoms in a similar fashion. At ambient temperatures and pressure wurtzite is the stable polymorph and a stable zinc-blende structure is generally obtained when ZnO is grown on cubic substrates [238].

2.4.6.2 TE properties of stoichiometric ZnO

ZnO is considered as a promising high temperature TE material and can be synthesised in a variety of morphologies such as poly- and single crystal ceramics, epitaxial thin films, nanorods, nanobelts, nanorings, hierarchical nanostructures [39].

At ambient temperatures, pure ZnO shows a TPF of ~800 μ W/m.K². However, it also exhibits a high κ (~40 W/m.K). The κ of ZnO reduces at higher temperatures (~5 W/m.K at 1000 K). This has been attributed to increased phonon scattering possibly as a result of large and substantially anisotropic thermal expansion of ZnO [239]. Another study showed that sputtered ZnO thin films can exhibit TPFs as high as $1.0 \times 10^3 \mu$ W/m.K² [50].

Although it is possible to reach low κ 's of 2-3 W/m.K at room temperature for nanograined ZnO ceramics [240], these structures exhibit highly reduced σ and therefore, neither TPF or ZTs improves. It has been postulated that the defects at grain boundaries are the major contributor to the drop in σ [240]. Overall, samples with larger grain sizes have been shown to exhibit higher σ .

As expected, nanostructuring approaches for bulk doped and undoped ZnO have also been shown to reduce κ [101, 240]. A large number of studies on TE properties of pure and doped ZnO have been conducted on polycrystalline ceramics [94-96, 98-100, 102, 103, 241-252]. TE properties of ZnO thin films [253-255] as well as nanostructures [97, 101, 104, 256, 257] have also been targeted in a number of studies. Commonly, nanostructuring results in a significant increase in *S*. As temperature increases, both *S* and σ are enhanced, resulting in higher TPFs and ZTs.

Of more interest however, are the TE properties of doped and co-doped ZnO, where the TPF and ZT can reach values as high as 1500 μ W/m.K² and 0.65 respectively, making ZnO a viable candidate for a variety of TE applications.

2.4.6.3 TE properties of non-stoichiometric and doped ZnO

For heat scavenging applications, ZnO is commonly doped by n-type dopants such as Al, Ge, Ni and Ti to achieve improved TE properties. Al is the most common dopant for ZnO [93-104]. Generally, Al doping increases the carrier mobility and reduces the phonon mean free path in the crystal lattice of ZnO, resulting in higher σ and lower κ . ZT has been shown to increase to as high as 0.30 at 1273 K for Al concentrations of ~0.02 and a high TPF of 1500 μ W/m.K² has been achieved at such elevated temperatures [93] Beneficial effects of Al doping can also be described in terms of its contribution to the high *c*-axis compression of the ZnO lattice leading to the increase in effective mass (m^*), resulting in enhanced *S* (Eq. 12) [99].

The dependence of TE properties of Al-doped ZnO (AZO), on the grain structure and secondary phases is further highlighted in a study by Jood *et al* [101]. Bulk pellets, obtained

by cold-pressing and sintering the nanocrystals that comprise of ZnO nanograins with $ZnAl_2O_4$ nanoprecipitates, were shown to reduce κ to very low values (1.5 W/m K at 300 K). These nanocomposites also showed high σ and *S*, resulting in a significantly high TPF and ZT of 900 μ W/m.K² and 0.44 respectively, at 1000 K.

There are also reports of co-doping ZnO with Al and other n-type dopants. Co-doping of Fe, Ni and Sm metals with AZO has not shown significant improvement in TE properties, with the highest TPF and ZT of $675 \,\mu$ W/m.K² and 0.126 respectively, for Ni-co-doped AZO at 1073 K [103]. On the other hand, co-doping of AZO with Ga resulted in significant improvement in ZT. Ga co-doping seemed to increase the solubility of Al in ZnO and strongly reduce the κ value at 2 mol% of Ga. Also, much larger TPFs than those of AZO have been observed in co-doped samples (Figure 2.6). The ZT value Zn_{0.96}Al_{0.02}Ga_{0.02}O reached a maximum of 0.47 at 1000K and 0.65 at 1247 K, a significant enhancement over conventional AZO [98].

A study on co-doped $Zn_{0.97}Al_{0.03-y}Ti_yO$ has shown an enhancement in both σ and *S*, resulting in TPFs as high as $3.8 \times 10^2 \,\mu$ W/m.K² for $Zn_{0.97}Al_{0.02}Ti_{0.01}O$ at 1073 K [96]. κ and ZT values of these samples have however not been reported. Ga doping has also been reported to improve TE properties of ZnO resulting in ZT values close to the best Al-doped ZnO ceramics [252].

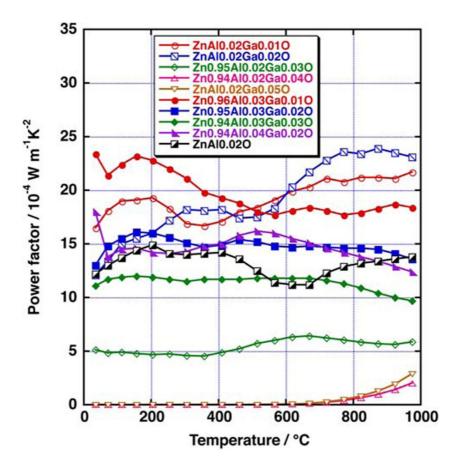


Figure 2.6: Temperature dependence of TPF of $Zn_{1-x-y}Al_xGa_yO$ ceramics. (Reproduced with permission from [98].)

2.4.6.4 Methods of synthesis

ZnO is widely synthesised using various liquid and vapour phase fabrication techniques. It can be synthesised in many different morphologies such as nanowires, nanospikes, nanopillars, nanorods and nanobelts. Over the years, liquid phase fabrication techniques such as hydrolysis, spray pyrolysis, sol-gel and hydrothermal synthesis have been employed to prepare ZnO for various applications [258-260] [261]. Other liquid phase methods to synthesise highly crystalline ZnO nanostructures include electrochemical techniques such as anodization and electrodeposition [262, 263].

Vapour deposition techniques such as RF/DC sputtering, ALD and MBE as well as chemical vapour deposition (CVD) technique and metal organic chemical vapour deposition (MOCVD) have been used to synthesise pure as well as doped ZnO thin films [264-267].

Other techniques such as spark plasma sintering (SPS) and PLD have also been widely used to synthesise densified ZnO in a powdered form [170][268, 269].

2.4.7 Copper oxides – Cu₂O and CuO

2.4.7.1 Crystal structure

Copper oxide occurs in two common phases: cuprous oxide (Cu₂O) and cupric oxide (CuO). Cu₂O (copper (I) oxide) has been commonly used for application in solar cells, catalysts, and sensors [270]. It exhibits a cubic crystal structure with a forbidden direct bandgap of ~1.9-2.2 eV, making it very challenging to study quantum confinement effects or modify its properties [271, 272]. Cu₂O has also been shown to depart from stoichiometry towards excess oxygen, leading to a p-type semiconducting nature and has been one of the most studied materials in semiconducting physics [273]. On the other hand, CuO (copper (II) oxide) belongs to the monoclinic crystal system with a direct bandgap of 1.2-1.5 eV and has been studied for photoconductive applications and is also the basis for several high temperature superconductors [271, 274]. In CuO, each Cu atom is coordinated by 4 oxygen atoms in an approximately square planar configuration. In a pure state and good stoichiometry, CuO behaves almost like an electrical insulator. However, non-stoichiometry leads to important semiconducting characteristics [275].

2.4.7.2 TE properties of stoichiometric copper oxides

A limited number of studies have been carried out on the TE properties of copper oxides in the 1990s. Jeong *et al.* examined the *S* and σ in uniaxially pressed CuO powder, which was subsequently sintered at different temperatures [276]. The CuO sample sintered at 1273 K in air, showed a peak *S* of ~650 µV/K between 400 to 500 K. Beyond 500 K, the *S* dropped rapidly. The corresponding σ as seen from Figure 2.7 (a) was approximately 1 S/m, resulting in a TPF of 0.42 µW/m.K² [276].

It has been shown that single crystal Cu₂O exhibits a high *S* at elevated temperatures (~1050 μ V/K at 923 K) [273]. On the other hand, the *S* of CuO thin films has been shown to change with varying film thicknesses (340 nm to 620 nm) and exhibits a maximum value of

~ 500 μ V/K for ~600 nm thick films (Figure 2.7 (b)) [275]. However, none of these works reported electrical or thermal conductivities. The full TE properties of intrinsic copper oxides are yet to be investigated.

2.4.7.3 TE properties of non-stoichiometric, doped and composite copper oxides

The doping technique has been shown to result in significant effect on the TE properties of copper oxides. Koffyberg *et al.* have demonstrated the TE effect in polycrystalline samples of Li doped CuO [277]. They have shown an average p-type S of 770 μ V/K and σ of 6.25 S/m, resulting in a TPF of 3.7 μ W/m.K²[277].

It seems that the most commonly investigated copper oxide composite for its TE properties is La_2CuO_4 . It exhibits a simple layered structure comprising of 2D CuO₂ planes in a unit cell and is the parent compound for high temperature superconductivity, which is related to the excess oxygen content and the structural change as a result of phase transition [278]. This layered structure makes the anisotropy of conduction very strong. Due to the anisotropic nature of their electrical conduction, such composites are potential TE materials. A detailed overview of its crystal phases is provided elsewhere [279].

For enhancing the TE properties of La₂CuO₄ metallic dopants can be incorporated. In this regard, TE properties of La_{2-x}R_xCuO₄ polycrystalline ceramics, where R can be Pr, Y or Nb have been investigated [280]. In this study, it has been shown that the choice of dopants plays a crucial role in determining the TE properties. Figure 2.7 (c) shows the variation of the TPF of La_{2-x}R_xCuO₄ with temperature for different dopants. As can be seen, with increasing temperature the TPFs of all composites decrease, eventually becoming stable above 700 K [280]. Samples show *S* ranging between 200 to 620 μ V/K. Amongst them La_{1.98}Y_{0.02}CuO₄ ceramics exhibit a high TPF of 10³ μ W/m.K². The maximum ZT was reported to be 0.17 at 330 K, which is around 3 times higher than pure La₂CuO₄ [280].

Studies on TE properties of n-type RE_2CuO_4 oxides, where RE is a rare earth element such as neodymium, samarium or gadolinium, have shown TPFs and ZTs of the order of μ W/m.K² and 0.005, respectively, at 950 K [281]. The electrical resistivities of such composites show a negative temperature dependence and is at least a magnitude higher than many conventional TE materials. Such RE₂CuO₄ type oxides exhibit a high κ of ~30 W/m.K at 300 K, which drops to ~ 8 W/m.K at 950 K [281], and can potentially be suitable for thermopower wave applications.

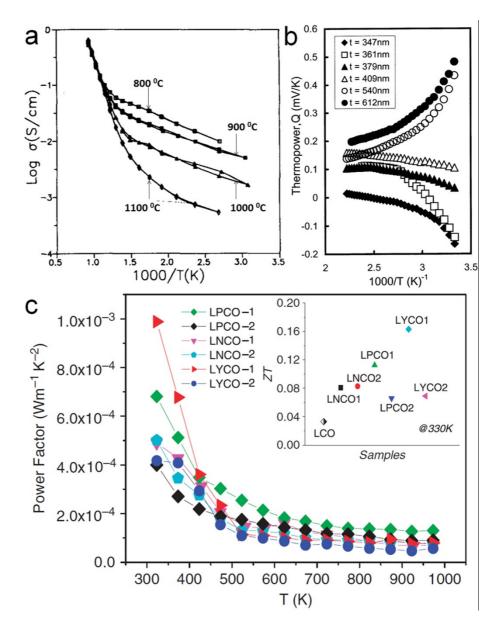


Figure 2.7: (a) Electrical conductivity variation of CuO sintered at different temperatures, (b) Seebeck coefficient variation with temperature for CuO films of different thicknesses and (c) Temperature dependence of TPF for various La_2CuO_4 ceramics, (inset shows ZT values at 330 K) [LNCO (Nb doped La_2CuO_4), LPCO (Pr doped La_2CuO_4), LYCO (Y doped La_2CuO_4)]. (Reproduced with permission from (a) [276], (b) [280] and (c) [275].)

2.4.7.4 Methods of synthesis

Many liquid and vapour phase methods are used for synthesising Cu₂O and CuO. Liquid phase techniques of for the sol-gel [282], hydrothermal [283] and spray pyrolysis [284] have been used for the synthesis of copper oxides. Other liquid phase techniques commonly employed to prepare high purity copper oxides include electrochemical methods such as anodization and electrodeposition [285, 286]. The chemical synthesis methods, especially hydrothermal are much desired for many applications as they are low cost, offer morphology control and facilitate low temperature synthesis and are therefore viable for large scale production [283]. Additionally, they result in a departure from stoichiometry when it is needed due to the introduction of point defects and impurities in the crystal lattice. Vapour phase techniques such as RF sputtering, PLD, various evaporation approaches and MBE have been demonstrated to synthesise crystalline copper oxide thin films at different oxygen contents [274]. Additionally, the CVD technique has also been utilized to synthesise copper oxides [287].

In most copper oxide synthesis methods a mixture of phases like Cu, Cu_2O and CuO is obtained. Post-deposition annealing or deposition at high temperature is usually needed to achieve the desired phase.

2.4.8 Vanadium oxides

2.4.8.1 Crystal structure

Vanadium oxide exists in many phases that include VO, VO₂, V₂O₃ or V₂O₅. However, only V₂O₅ demonstrates TE properties and shows highly anisotropic n-type electrical conduction [288]. It has a direct bandgap of ~2.4 eV and is a promising electrode material for energy storage systems such as Li-ion batteries [289-292] and possesses a high ionic storage capacity because of its layered structure [293]. Over the years, it has also been intensely investigated for its electrochromic properties [294, 295]. Unlike other configurations of vanadium oxide that have been known to exhibit multiple crystal phases, V_2O_5 exists only as an orthorhombic crystal, which is fundamentally comprised of VO₅ pyramids that form alternating double chains along the *b*-axis [296]. A detailed overview of the crystal structures of all phases of vanadium oxide is provided elsewhere [296].

2.4.8.2 TE properties of stoichiometric V₂O₅

Kounavis *et al.* have demonstrated that V_2O_5 gels exhibit a room temperature TPF of 0.3 μ W/m.K²[297]. V_2O_5 films synthesised by sol-gel method exhibit *S* of ~ -200 μ V/K, but have very high resistances of the order of 10³ to 10⁴ Ω [293]. Hence, it is evident that the σ of V_2O_5 films requires significant enhancement for practical refrigeration and energy scavenging applications.

2.4.8.3 TE properties of nanostructured, doped and composite V₂O₅

Bahgat *et al.* have synthesized highly oriented nanocrystalline, hydrated vanadium pentoxide, (V₂O₅.*n*H₂O) films of 200 nm thickness. The *S* and σ of such films have been shown to increase with temperature, resulting in a peak TPF of 101.25 μ W/m.K² at 480 K (Figure 2.8 (a,b)) [298].

Iwanaga *et al.* have studied the TE properties of V_2O_5 thin films and reported that the introduction of metallic dopants (Na in this case) can improve the TPF values dramatically. This is primarily due to an increase in σ by a factor of up to ~ 10⁴. At the same time, the *S* reduces to almost half its value. The direct measurements of TPF have shown an enhanced

TPF of 10 μ W/m.K² (compared to ~10⁻² μ W/m.K² for pure V₂O₅ films) for 35 % Na doping [299].

Liu *et al.* have shown that polyethylene oxide (PEO) intercalated layered V₂O₅ xerogel nanocomposites result in low TPFs [300]. PbO and ZnO based vandates have also been shown to exhibit *S* of up to -400 μ V/K at room temperature [301]. However, σ in such composites is low, so they can possibly be used only in temperature sensors.

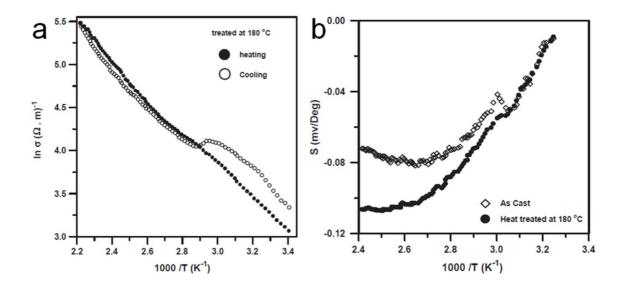


Figure 2.8: Temperature dependence of (a) electrical conductivity, (b) Seebeck coefficient for the ascast and heat treated films during heating and cooling cycles of hydrated V_2O_5 . (Reproduced with permission from [298].)

2.4.8.4 Methods of synthesis

 V_2O_5 films can be synthesised using various liquid and vapour phase techniques [302]. Commonly used liquid phase methods for the synthesis of V_2O_5 thin films are the sol-gel and the hydrothermal synthesis technique in which hydrated forms are obtained. The sol-gel synthesised hydrated nanocrystalline V_2O_5 has been shown to exhibit the highest TPF [298]. A melt quench technique has also been employed to dope various concentrations of Na⁺ ions into sol-gel solutions and subsequently, thin films of Na intercalated V_2O_5 can be prepared [297, 299]. Hydrothermal synthesis is often utilized to synthesise V_2O_5 nanostructures such as nanotubes and nanowires [303, 304]. Other liquid phase methods include the electrodeposition and anodization techniques which have also been shown to synthesise V_2O_5 nanostructures [305-307].

Vapour phase techniques such as RF sputtering [308], ALD [309] and PLD [310] have also been shown to deposit crystalline V_2O_5 thin films of various phases. Additionally, the CVD method has also been demonstrated to form highly crystalline V_2O_5 thin films [311]. However, there are few reports on the TE properties of V_2O_5 prepared using vapour deposition techniques.

2.4.9 Cobalt oxides

2.4.9.1 Crystal structure

Cobalt oxide based materials have received great attention for their application in gas sensing, heterogeneous catalysts, intercalation compounds for energy storages, electrochromic devices and more recently as TE materials [312, 313]. Cobalt oxides are generally found in two stable oxide compounds: Co_3O_4 and CoO. Co_3O_4 is the more stable of these two. Both Co_3O_4 and CoO exhibit a cubic lattice. Co_3O_4 is a spinel with the presence of both Co^{2+} and Co^{3+} ions in its lattice. Co_3O_4 exhibits a bandgap in the range of 1.4-1.8 eV, while CoO has a higher energy bandgap of 2.2-2.8 eV. Both Co_3O_4 and CoO are usually non-stoichiometric with excess oxygen, leading to p-type semiconducting behaviours [313].

2.4.9.2 TE properties of stoichiometric cobalt oxides

So far, the TE properties of pure cobalt oxides have not been investigated widely, mainly due to the fact that high resistivities result in a poor TE performance for many energy scavenging applications. It has been shown that in a bulk form CoO exhibits a TPF of ~ 80μ W/m.K² at 1000 K [314]. However, the use of various approaches suggested in section 2.3 such as the addition of metallic dopants, substructuring, and reducing the dimensionality have made doped cobalt oxides the best TMOs for various TE applications.

2.4.9.3 TE properties of non-stoichiometric, doped, composite and nanostructured cobalt oxides

Rare-earth cobalt oxides (RECoO₃) with perovskite crystal structures have been studied for their TE properties for energy scavenging and cooling properties and have shown relatively large figure of merits around the room temperature [92]. Their high-temperature performance is however limited.

P-type cobalt oxide composites are among the TE metal oxides with the largest ZT values reported to date. The most promising cobaltite composites for such TE applications are Na_xCoO_2 and $Ca_3Co_4O_9$ [89]. The high ZT values are associated with their crystal structures, which consist of CoO_2^- planes composed of edge-sharing CoO_6 octahedra, and other structural components between these layers. Na_xCoO_2 exhibits a weak monoclininc distortion with respect to the hexagonal unit cell caused by the ordering of a layer of sodium ions in between CoO_2 planes, while $Ca_3Co_4O_9$ comprises of a distorted rock-salt type layer of Ca_2CoO_3 , which lowers thermal conductivity by shortening the phonon mean free path (Eq. 2a), and is located between two CdI_2 type CoO_2 layers that are mainly responsible for providing the path for electrical conduction. Hence, these composites are a classic example of substructuring, which is predicted to enhance TE performance (section 2.3.3).

Terasaki *et al.* are the pioneers of layered cobalt oxide base TE materials. They were the first group to demonstrate large TPFs of the order of $5 \times 10^3 \ \mu\text{W/m.K}^2$ (compared to $4 \times 10^3 \ \mu\text{W/m.K}^2$ for Bi₂Te₃) and ZT as high as 0.75 in NaCo₂O₄ single crystals at room temperature [111]. Figure 2.9 (a,b) show the variation of resistivity and *S* with temperature for the NaCo₂O₄ single crystals [111]. Subsequent studies have shown that polycrystalline Na_xCoO₂ exhibits TPF as high as $1.4 \times 10^3 \ \mu\text{W/m.K}^2$ for x = 0.85 at room temperature [315, 316]. For Na_xCoO₂, silver (Ag) doping results in the enhancement of ZT [89]. Other metallic dopants such as Cu [105] and Zn [106] have also been shown to increase the TPFs, while Sr doping results in the improvement of ZT [317]. Polycrystalline Na_xCoO₂ typically shows a peak ZT of ~0.11. However, recently, two-dimensional (2D) and stacked Na_xCoO₂ nanostructures prepared by exfoliation/restacking method were reported to exhibit enhanced

TE properties for energy scavenging applications, as expected from the discussion in section 2.2 [318, 319]. The enhancement was attributed to the reduction of in-plane and cross-plane thermal conductivities in the super-lattice like structures, resulting in enhanced TPFs and ZTs of approximately 500 μ W/m.K² and 0.4, respectively.

On the other hand, undoped Ca₃Co₄O₉ exhibits σ , *S*, κ , TPF and ZT of 10⁴ S/m, 150 μ V/K, 2 W/m.K, 225 μ W/m.K² and 0.3, respectively, at elevated temperatures as large as 1000 K. Although, the room temperature TPFs performance of Ca₃Co₄O₉ is inferior to Na_xCoO₂, it is more commonly used in various TE applications due to its superior stability to compositional changes and better performance at high temperatures [89].

Similar to Na_xCoO₂, the addition of Ag as a dopant [320, 321] or a second phase composite [320, 322, 323] has been shown to improve TE properties of Ca₃Co₄O₉. A Ca_{2.7}Ag_{0.3}Co₄O₉/Ag-10 wt% composite showed an enhanced ZT of 0.5 at 1000 K. Bismuth (Bi) doping has also resulted in enhanced TPFs and reduced κ . However, the ZT of Bi-doped samples, is not as high as those of Ag doped oxides. Ca_{2.75}Gd_{0.25}Co₄O₉ ceramics have also been shown to exhibit TPF and ZT of 480 μ W/m.K² and 0.23 respectively, at 923 K (Figure 2.9 (c)) [324]. It is seen that the Ca_{2.75}Gd_{0.25}Co₄O₉ ceramics synthesised using the SPS method exhibit slightly higher TPFs and ZTs compared to hot press (HP) synthesised samples (Figure 2.9 (c)). There are also reports on the doping of Ca₃Co₄O₉ with transition metals [325, 326] such as copper and nickel. Gallium addition has been demonstrated to improve TPFs and ZTs [327]. Doping with lanthanum and lanthanide elements has also been studied but the TE enhancements have not been as impressive [89].

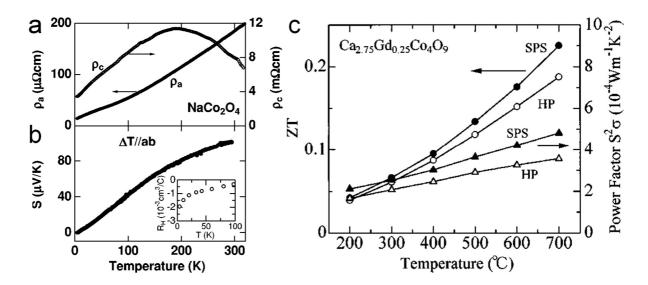


Figure 2.9: (a) Resistivity and (b) Seebeck coefficient variations with temperature for NaCo₂O₄ single crystals in plane (ρ_a) and out of plane (ρ_c) and (c) comparison of ZT and TPF for SPS and hot pressed (HP) synthesised Ca_{2.75}Gd_{0.25}Co₄O₉ samples. (Reproduced with permission from (a), (b) [111] and (c) [324].)

2.4.9.4 Methods of synthesis

Cobalt oxide can be synthesised using various liquid and vapour phase methods. Epitaxial thin films are generally preferred as they result in highly oriented structures [186, 328, 329]. Liquid phase techniques such as spray pyrolysis, sol-gel and hydrothermal have been employed to fabricate cobalt oxide thin films as well as nanostructures in various morphologies such as nanorods, hierarchical nanocolumns, nanocubes, nanowires and nanorods [312, 330-332]. Although, other liquid phase methods such as electrodeposition have also been employed [333]. An excellent review article summarises various liquid phase synthesis techniques for fabricating cobalt oxide nanostructures [332].

Vapour phase methods that include MBE, PLD and EBE have conventionally been used for the growth of epitaxial $Ca_3Co_4O_9$ films. For Na_xCo_2 films however, the volatility of sodium ions poses difficulties in controlling stoichiometry. The CVD synthesis technique has been shown to be advantageous since it allows accurate tailoring of system composition, structure, morphology *via* suitable choice of a precursor compounds and deposition conditions [312].

2.4.10 Rhodium oxides – RhO_x

2.4.10.1 Crystal structure

Rhodium oxides are generally found in two crystal oxide compounds: RhO₂ and Rh₂O₃. RhO₂ exhibits a tetragonal rutile structure, which transforms into corundum type α -Rh₂O₃ after annealing above 1000 K [334]. Heating above such temperatures results in a transformation to orthorhombic type β -Rh₂O₃ [335]. Rhodium oxides have been investigated primarily for applications in catalytic chemistry, electrochromisms and as a conductive transparent oxide [336-338]. Additionally, misfit-layered rhodium oxides with two-dimensional CdI₂-type crystal structures, analogous to that of cobalt oxides, are among the best candidates for forming p-type TE materials [57]. As in the case for cobalt oxides, their superior thermopower properties originate from CdI₂-type layers, which favour low spin state of Rh³⁺/ Rh⁴⁺ with degeneracies of spin and orbital as the key factors [339]. The CdI₂-type layer has a hexagonal symmetry, while the misfit layer is generally a square lattice. However, a layered Bi-Sr-Rh-O system with fluorite-type misfit layers with a trigonal symmetry has also been reported to exhibit similar TE properties [57].

2.4.10.2 TE properties of stoichiometric RhO_x

There are no reports of stoichiometric RhO_x being employed in TE systems. What follows is a brief overview of the studies on rhodium oxide based metal oxide systems that are among the best p-type TE TMOs.

2.4.10.3 TE properties of non-stoichiometric, composite and doped RhO_x

Okada *et al.* initially reported the first synthesized misfit-layered rhodium based metal oxide in polycrystalline form [340]. Samples of $(Bi_{1-x}Pb_x)_{1.8}Sr_2Rh_{1.6}O_y$ (*x*=0, 0.1, 0.2) and $Bi_{1.8}Ba_2Rh_{1.9}O_y$ were investigated for their TE properties, with the most promising results being 125 μ V/K, 213 S/m and 3.3 μ W/m.K² for *S*, σ and TPF, respectively, at room temperature (see Figure 2.10 (a-c)). In another study, polycrystalline samples of Co and Rh mixed solutions $Bi_{1.7}Ba_2(Co_{1-z}Rh_z)O_y$ with hexagonal (Co, Rh)O₂ layers have been synthesized in an effort to further alter the TE properties by decreasing κ [341]. Although κ was reduced in the solid solution, the σ also dropped due to the distortions made by different ionic size elements in (Co, Rh)O₂ layers and therefore, TE performance did not improve.

Kobayashi *et al.* have synthesized rhodium oxide based single crystals in Br-Sr-Rh-O systems with alternately stacked conductive RhO_x and insulating in (Bi_{0.75}Sr_{0.25})O_{1.5} fluorite-type layers [57]. Interestingly, the misfit layer showed a trigonal symmetry with a rhombohedral unit cell, rather than the square-lattice usually observed in other oxides. Room temperature *S* of up to 63 μ V/K and σ of 6.25×10⁴ S/m were obtained for Bi_{0.78}Sr_{0.4}RhO_{3+y} crystals. The TPF of such a composite was estimated to be 248 μ W/m.K², which is comparable to the values for cobalt oxide based systems [57]. Additionally, single crystals of Ba_{1.2}Rh₈O₁₆ have been shown to exhibit κ and ZT values of 3 W/m.K and 0.02 at 200 K, respectively [342].

A recent first principle investigation of layered K_xRhO_2 composites based on ab-initio calculations and Boltzmann transport theory has suggested that the material system has the potential for exceptionally remarkable TE properties [343]. Calculations found large Seebeck coefficients in the temperature range of 0 to 700 K for hydrated phase of K_xRhO_2 . Moreover a peak value of ZT = 0.3 is predicted for $K_{7/8}RhO_2$ at 100 K, which is higher than Na_xCoO_2 systems. Even at room temperature, TPFs higher than Na_xCoO_2 are predicted [343].

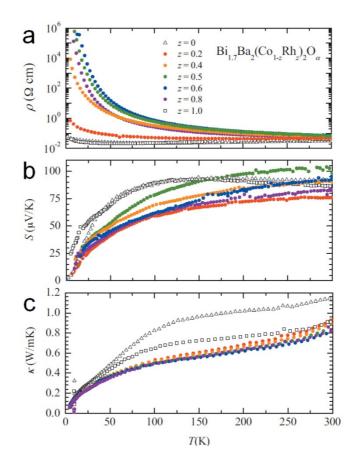


Figure 2.10: Temperature (*T*) dependence of (a) resistivity (ρ), (b) Seebeck coefficient (*S*), and (c) thermal conductivity (κ) for Bi_{1.7}Ba₂(Co_{1-z}Rh_z)O_y of varying rhodium concentration (*z*) (Reproduced with permission from [341].)

2.4.10.4 Methods of synthesis

Many liquid and vapour phase techniques are employed to synthesise rhodium oxides. Amongst the liquid phase synthesis techniques, sol-gel and hydrothermal are the most commonly used methods to synthesise Rh_2O_3 in various morphologies [344-346]. Vapour phase techniques such as RF sputtering, electron beam evaporation (EBE) and the CVD method are used for preparing crystalline rhodium oxide thin films [347]. Misfit, layered rhodium oxide composites such as $(Bi_{1-x}Pb_x)_{1.8}Sr_2Rh_{1.6}O_y$ are synthesised using the SSR technique [340, 341]. It should be considered that RhO_2 is insoluble even in hot aqua regia, hence solution based synthesis techniques are not employed for forming RhO_2 . SSR is therefore commonly utilized [348].

2.4.11 Molybdenum oxides – MoO_x

2.4.11.1 Crystal structure

The most common stoichiometries of MoO_x are MoO_2 and MoO_3 . However, MoO_3 is the most widely investigated stoichiometry of MoO_x for a variety of applications such as gas sensing, photochromic devices, light emitting diodes (LEDs), batteries and organic solar cells [292, 349-356]. The most common crystal phases of MoO_3 are the thermodynamically stable α -MoO₃ and the metastable β -MoO₃ [357-360]. Bulk α -MoO₃ exhibits an indirect bandgap of ~3 eV and has an orthorhombic crystal structure, that comprises of dual layered planar crystals of distorted MoO_6 octahedra that are held together by weak van der Waals forces. β -MoO₃ on the other hand comprises of MoO_6 octahedra that share corners in all the three dimensions, resulting in a monoclinic 3D structure [356, 361]. At temperatures above 620 K, the β phase transforms into the more stable, layered α -MoO₃ phase [357, 358].

2.4.11.2 TE properties of stoichiometric MoO_x

There is no literature that reports the TE properties of stoichiometric molybdenum oxides, primarily due to their low σ . However, incorporation of various dopants and implementation of MoO_x composites have been shown to result in high TPFs.

2.4.11.3 TE properties of non-stoichiometric, doped and composite MoO_x

Non-stoichiometric and doped molybdenum oxides have been shown to exhibit high TPFs. Xu *et al.* investigated the TE properties of highly reduced molybdenum oxides (RMo₈O₁₄) where R=La, Ce, Nd and Sm. Figure 2.11 (a) shows the TPFs of the four composites at different temperatures. It is seen that NdMo₈O₁₈ exhibits a peak TPF and ZT of 177 μ W/m.K² and 0.1, respectively, at 1000 K. The κ of the composite has been reported to be 3.19 W/m.K at 322 K, which drops to 2 W/m.K at 1164 K [362, 363]. It is evident that the TPF is certainly large enough to make these molybdenum oxide composites promising for high temperature energy scavenging applications.

It has also been shown that the use of composites can result in enhanced TE performance as suggested in section 2.3.4. A study reports that the TPFs of polyaniline (a typical conductive

polymer) molybdenum trioxide (PANI/MoO₃) composites, is high. A maximum TPF of $\sim 10^2 \,\mu\text{W/m.K}^2$ was observed for 10 wt% of MoO₃ (Figure 2.11 (b)) [364].

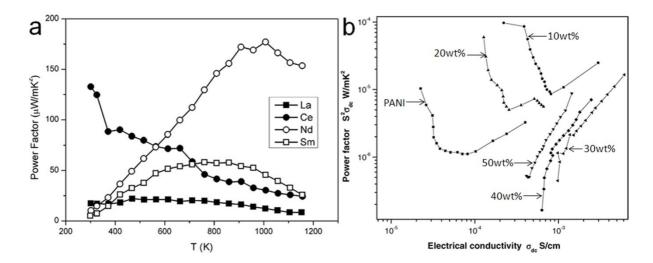


Figure 2.11: (a) Temperature dependence of TPF of RMo_8O_{14} (R:La, Ce, Nd, Sm) pellets, and (b) electrical conductivity *vs* TPF of PANI/MoO₃ composites *vs* MoO₃ concentration in the composite. (Reproduced with permission from (a) [363] and (b) [364].)

2.4.11.4 Methods of synthesis

Similar to other TMOs, MoO₃ can be synthesised using many different liquid and vapour phase techniques. The commonly used liquid phase techniques include sol-gel, hydrothermal, and electrodeposition [358]. Vapour phase techniques such as thermal evaporation, electron beam epitaxy, PLD, RF/DC sputtering, MBE and van der Waal epitaxy (VDWE) have been used for synthesising MoO₃ in various thin film and nanostructured forms. Amongst these, MBE and VDWE have been shown to synthesise ordered, layered MoO₃ structures. Additionally, CVD techniques are also employed to synthesise crystalline MoO₃. A detailed overview of the synthesis techniques to produce various morphologies of MoO₃ is provided elsewhere [356].

2.4.12 Other transition metal oxides and their TE properties

In this section, we will discuss other TMOs, whose TE properties have not been widely investigated. Most of these TMOs are wide bandgap materials, resulting in extremely poor electrical conductivities. However, a few oxides such as iron oxide, cadmium oxide, nickel oxide and doped zirconium oxide exhibit promising TE properties for various applications.

In this section, we provide a brief overview of the small number of reports on the TE properties of the remaining TMOs in their stoichiometric and/or doped states.

2.4.12.1 Iron oxides

There are many known stable iron oxide stoichiometries available. Amongst them, Fe_2O_3 is the iron oxide compound that has been studied for its TE properties. An analysis of a limited number of reports suggests that Fe_2O_3 can potentially be a promising TMO for TE applications at high temperatures as it exhibits high TPFs at room as well as elevated temperatures

Fe₂O₃ thin films have been shown to exhibit peak *S* of 1650 μ V/K in the temperature range of 270-290 K. A peak σ of 5.5×10³ S/m has been reported in the same temperature range, resulting in a high TPF of 1.5×10⁴ μ W/m.K² [365]. Li- doped α -Fe₂O₃ has been reported to exhibit a TPF of 5.5×10³ μ W/m.K² at temperature over 800 K for which a κ of 4 W/m.K has been reported [366]. Fe₂O₃-NiO composites have also been shown to exhibit high TPFs at elevated temperatures (900 μ W/m.K² at 823 K) [367]. Nanostructuring technique has been predicted to enhance TE performance (section 2.3.3). Although, 1D electronic quantum confinement has been demonstrated in α -Fe₂O₃ nanorods, they have not been examined for their TE properties [368].

2.4.12.2 Chromium oxides

There exists many crystalline phases of chromium oxides however, Cr_2O_3 is the most stable bulk form of this TMO [369], with a few recent reports on its TE properties [365, 370].

 Cr_2O_3 thin films have been shown to exhibit *S* of 3500-4500 µV/K at room temperature. However, we wish to add that such dramatically high *S* has not been confirmed by any other study so far. A σ of 5.8×10³ S/m has been reported for stoichiometric Cr_2O_3 [365]. Another study demonstrates a TPF of 3.5 µW/m.K² at a temperature of 1300 K in Cr_2O_3 [370]. The effect of TiO₂ addition to Cr_2O_3 on its TE properties has also been investigated. A 2 %

TiO₂ addition results in a slightly improved TPF of 5.6 μ W/m.K² [371].

The TE properties of chromium oxide compounds such as $CuCrO_2$ have also been studied. A maximum TPF and ZT of 236 μ W/m.K² and 0.1 at 1100 K has been obtained [372]. $CrO_{0.1}N_{0.9}$ polycrystalline samples have also been reported to show a TPF of 80 μ W/m.K² at 300 K [373].

The above discussion shows that sufficiently large TPFs have been demonstrated for Cr_2O_3 and its compounds. However, further studies are required to establish chromium oxide as a viable TE TMO for many applications.

2.4.12.3 Scandium oxides

Scandium oxide is a wide band gap (6 eV) insulating material, and is therefore not useful for TE conversion applications [171]. Doping can slightly improve electrical conduction; however, it is still insufficient for any meaningful TE energy scavenging applications. Cu doped scandium oxide epitaxial thin films exhibit *S* and σ of 40 µV/K and 110 S/m, respectively, at room temperature, resulting in extremely low TPF of 0.18 µW/m.K² [374].

2.4.12.4 Zirconium oxides

Zirconium oxides are stable at extremely high temperatures and are generally used as ionic conductors at such temperatures. As such these oxides are frequently used in oxygen sensors and fuel cell membranes [375]. ZrO_2 is the most common crystal phase of zirconium oxides which is found in three phases: a cubic phase with a fluorite structure that occurs at temperatures >2850 K and transforms into a tetragonal phase at 2650 K, which on further cooling transforms to a monoclinic phase [376]. It exhibits a wide bandgap of 5 eV [171].

Pure ZrO₂ does not exhibit good TE properties due to its poor σ . However, ZrO₂/CoSb₃ nanocomposites show a peak S of 140 μ V/K at 700 K for 5 % ZrO₂ and a corresponding σ and κ of 3.75×10⁴ S/m and 2.75 W/m.K, respectively [129]. The resulting TPF and ZT is approximately 735 μ W/m.K² and 0.2, respectively. Therefore, it is obvious that the incorporation of ZrO₂ can potentially be a good approach for obtaining enhanced TE properties for energy scavenging at elevated temperatures.

2.4.12.5 Cadmium oxides

Cadmium oxide is an n-type semiconductor, which exhibits a cubic rocksalt type crystal structure with a direct bandgap of ~2.1 eV at room temperature [377]. A study of highly crystalline CdO thin films have revealed high σ of the order of 10⁵ S/m and a peak *S* of – 90 μ V/K, resulting in a high TPF of ~800 μ W/m.K² [378]. Another study has demonstrated a TPF of 100 μ W/m.K² at 700 K [379]. Other studies on pure as well as doped CdO have revealed similar order of magnitude TPFs [380-382]. Therefore, it is evident that CdO can potentially be a viable n-type TE TMO at elevated temperatures.

2.4.12.6 Nickel oxides

Nickel oxide is a p-type semiconductor that exhibits a cubic rocksalt type crystal structure with a rather large bandgap of 3.6-4.0 eV. Although the σ of stoichiometric NiO is extremely low, Ni²⁺ vacancies are easily formed in undoped NiO, resulting in dramatic improvements in σ [383].

In the past, a few studies have examined TE properties of NiO [384, 385]. One such study has reported *S*, σ of 101 μ V/K and 10⁻² S/m respectively, at room temperature. The TPF is extremely low primarily due to poor electrical conductivity [385].

The use of metallic dopants such as Li and Na has been shown to result in enhanced TE properties [386][387]. Li doped NiO exhibits TPFs of the order of $10^2 \,\mu\text{W/m.K}^2$ at temperatures exceeding 1000 K, suggesting its suitability as a promising metal oxide for energy scavenging and thermopower wave sources [386].

2.4.12.7 Iridium oxides

IrO₂ is the most stable phase of iridium oxides and exhibits a TiO₂ like rutile crystal structure. The TE properties of pure IrO₂ have not been examined. However, Ca-Ir-O composites have been investigated for their TE properties by Keawprak *et al.* [388-390]. They reported low TPFs and ZTs (~35 μ W/m.K² and 0.01, respectively).

2.4.12.8 Other TMOs

Other transition metals such as Nb, La, Ac Y, Ta, Re, Hf, Ag and Te are usually employed as dopants in other TE TMOs for tuning their various TE properties in order to achieve higher TPFs and ZTs. However, reports on their stoichiometric TMOs are rare and yet to be fully investigated.

2.5 Summary

In this chapter, the author presented the TE properties of Bi_2Te_3 , Sb_2Te_3 as the conventional TE materials and a variety of TE TMOs. In addition, he presented the theory governing the key TE parameters (*S*, σ and κ) and strategies to alter these parameters *via* stoichiometric, dimensional and morphological changes. A major portion of this chapter was submitted for publication consideration in Journal of Progress in Materials Science.

Based on the analysis conducted in this chapter, the author made an informed choice of core TE materials for the thin film thermopower wave devices. These comprised of Bi_2Te_3 and Sb_2Te_3 as the conventional TE materials and zinc oxide (ZnO), manganese dioxide (MnO₂) as TE transition metal oxides TMOs that can provide advantageous properties to the thermopower wave systems. Bi_2Te_3 and Sb_2Te_3 were chosen at the first stage as they exhibit high Seebeck coefficient and electrical conductivities. However, in order to compensate for their low thermal conductivity, the author devised a successful strategy by placed them on thermally conductive Al_2O_3 substrates. The author then chose ZnO and MnO_2 for the development of thermopower wave systems. These two TE TMOs show exceptionally large Seebeck coefficients, high electrical conductivities and moderate thermal conductivities at elevated temperatures. A detailed description of thermopower wave systems based on the aforementioned core TE materials will be provided in Chapters 3, 4, 5 and 6.

In the next chapter, the author will demonstrate thermopower wave sources in a thin film geometry for the first time using Bi_2Te_3 as the core TE material. The exothermic

chemical reactions from a solid fuel will be coupled to charge carriers in Bi_2Te_3 layers to generate voltages and oscillations amplitudes higher than previously demonstrated MWNT based thermopower wave sources, while maintaining a high specific power.

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Chapter 3

Oscillatory Thermopower Wave Sources based on Bi₂Te₃

3.1 Introduction

In chapter 1, it was highlighted that prior to the commencement of the author's PhD candidature, only one thermopower wave system that incorporated multi-walled carbon nanotubes (MWNTs) as the thermoelectric (TE) cores had been reported (by Strano group at MIT) [1]. However, the main limitation of that work was that their system generated low voltages (generally 30-50 mV) and oscillation amplitudes. This highlighted the need for investigating other core thermoelectric (TE) materials that exhibit high Seebeck coefficients (*S*), electrical conductivities (σ) and moderate thermal conductivities (κ) so that the output voltages from such sources could be increased, while maintaining a high specific power. In order to identify the potential core TE materials that exhibit the aforementioned properties, the author reviewed the TE properties of conventional TE materials such as bismuth telluride (Bi₂Te₃), antimony telluride (Sb₂Te₃) and TE transition metal oxides (TMOs) in the previous chapter. Based on the analysis carried out in chapter 2, the author of this thesis identified Bi₂Te₃ as one of the potential candidates due to its high *S* (~ -200μ V/K) and σ (10⁵ S/m).

In this chapter, the author will demonstrate thin film thermopower wave generation systems based on n-type Bi_2Te_3 as the core TE material. As a moderate to high thermal conductivity is essential to sustain the self-propagation of the thermopower waves, the author will compensate for the low κ of Bi_2Te_3 by depositing it on thermally conductive alumina (Al₂O₃) substrates. Subsequently, highly exothermic chemical reaction of a solid fuel (nitrocellulose) will be coupled to charge carriers in the Bi_2Te_3 layers to generate self-propagating thermopower waves which entrain charge carriers of Bi_2Te_3 to generate voltage and power.

The author will conduct a comprehensive theoretical analysis of the Bi_2Te_3 based thermopower wave system by adapting the theory of combustion waves to assess and predict the behaviour of the thermopower waves in thin film geometries. A thorough analysis of the system will be carried out by characterizing the Bi_2Te_3 films before and after the thermopower wave propagation. The influence of the mass of fuel on the voltage and power generated will be studied. Terracotta substrates, which exhibit contrastingly low thermal conductivity compared to Al_2O_3 will also be used to study the role of the substrate thermal conductivity on the behaviour of thermopower waves. Additionally, the influence of the Bi_2Te_3 film thickness on the output voltage will also be investigated by the author. The work in this chapter was published as a full article in the journal Advanced Functional Materials.

3.2 Experimental

3.2.1 Synthesis of Bi₂Te₃ films

RF magnetron sputtering was used to deposit Bi_2Te_3 films. High purity (99%) Bi_2Te_3 sputtering target (Vin Karola Instruments) was used in the process [2]. The sputtering process was started after the chamber was pumped down to 2×10^{-5} torr. Al_2O_3 and terracotta, with dimensions in the order of 5 to 25 mm, were used as substrates after being adequately cleaned using acetone, isopropanol and distilled water successively, and dried using a high pressure air gun. The choice of substrates was based on their contrasting thermal conductivities. Al_2O_3 has a thermal conductivity of over 20 W/m.K while terracotta has a thermal conductivity of approximately 1 W/m.K [3, 4]. This difference enabled the author to test the performance of the system for two extremely different thermal conductivities and compare the results with our theoretical model which is described in section 3.3 of this chapter. The substrates were kept at 100 °C during the sputtering process. RF sputtering power of 100 W was used throughout the deposition process. The sputtering process was carried out under an atmosphere of 100% Argon (Ar). A sputtering time of 90 min resulted in 5 μ m Bi₂Te₃ layer. Adhesive conductive

silver (Ag) paste (42469, Alfa Aesar) was used to make electrical contacts between the copper tape electrodes and the Bi_2Te_3 samples. Their resistance ranged from 2 Ω to 10 Ω .

3.2.2 Preparation of the fuel

Nitrocellulose $[C_6H_8 (NO_2)_2O_5]$ was used as the fuel due to its large enthalpy of reaction. Nitrocellulose was prepared by dissolving millipore nitrocellulose membranes (N8645, Sigma Aldrich) in acetonitrile (15g/L). This solution was dropped onto the Bi₂Te₃ film using a pipette and left to dry in ambient air. The acetonitrile evaporated, leaving a layer of adhesive nitrocellulose coating. Sodium azide (NaN₃) (14314, Alfa Aesar) in aqueous solution (50mg/mL) was then added on top of the nitrocellulose layer using a pipette to serve as a primary igniter. The total thickness of the fuel layers was approximately 240 µm. A schematic representation of a fuel/Bi₂Te₃/substrate thermopower wave device is shown in Figure 3.1.

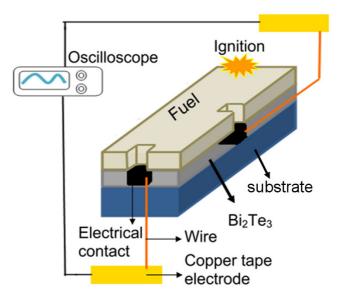


Figure 3.1: Schematic representation of a fuel/Bi₂Te₃/substrate system (not to scale).

3.2.3 Characterization of the Bi₂Te₃ film surface

Scanning electron microscopy was conducted using the FEI Nova Nano SEM to investigate the structure of the Bi_2Te_3 films to assess their porosity. Figures 3.2 (a,b) show SEM images of the Bi_2Te_3 film for two different thicknesses (5 and 10 μ m) on

 Al_2O_3 substrates. Figures 3.2 (c,d) show their cross-sectional view. The images show clearly that the Bi_2Te_3 film is not smooth but consists of layers made of nano sized flakes of irregular shape and size.

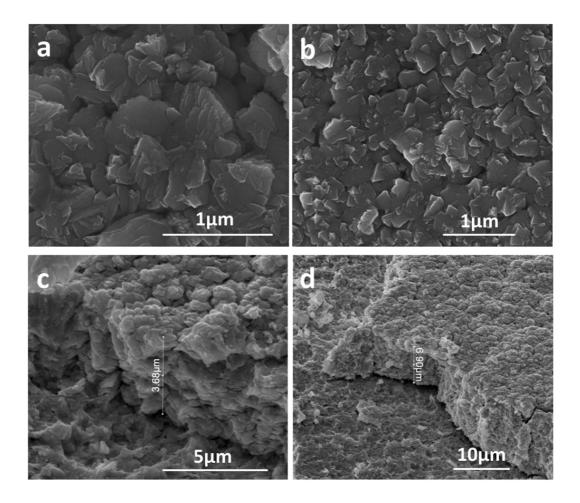


Figure 3.2: SEM image of Bi₂Te₃ film (a) 5 µm thick on Al₂O₃, (b) 10 µm thick on Al₂O₃. Crosssectional SEM images of (c) 5 µm Bi₂Te₃ film on Al₂O₃ substrate and (d) a 10 µm Bi₂Te₃ film on Al₂O₃ substrate, The samples in (c,d) were tilted at an angle of 45° when the SEM images were taken. Hence, the thickness of the Bi₂Te₃ films in (c) & (d) are $3.68\sqrt{2} = 5.2$ µm and $6.9\sqrt{2} = 9.8$ µm, respectively.

An AMBIOS Technology (XP-2 SERIES) profiler was used in order to further investigate the morphology of the Bi_2Te_3 surface. Figures 3.3 (a,b) show the surface profile of the 5 and 10 µm Bi_2Te_3 films, respectively, as well as the surface profile of the Al_2O_3 substrate. The standard deviation of approximately 0.6 and 0.7 µm was obtained for Bi_2Te_3 surface roughness for 5 and 10 µm films, respectively, indicating their almost similar porous natures. Obviously, a greater porosity enables more fuel to be placed on the surface of the film, resulting in a sustained reaction propagation. Additionally, porosity is also important to increase the thermal conductivity between the fuel and the TE films.

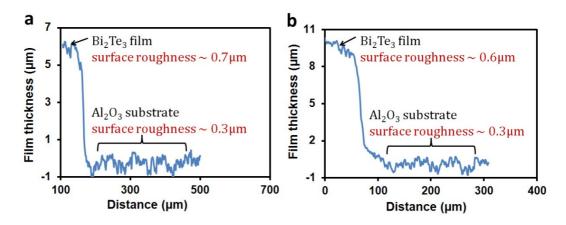


Figure 3.3: Surface profile of (a) 5 μ m Bi₂Te₃ film on Al₂O₃ substrate, and (b) surface profile of 10 μ m Bi₂Te₃ film on Al₂O₃ substrate.

In order to observe the crystalline structure of Bi_2Te_3 , and the effect of nitrocellulose on the crystallinity of the sample, x-ray diffraction (XRD) was carried out using a Bruker D8 DISCOVER microdiffractometer fitted with a GADDS (General Area Detector Diffraction System). Data was collected at room temperature using CuK α radiation (λ = 1.54178 Å) with a potential of 40 kV and a current of 40 mA, and filtered with a graphite monochromator in the parallel mode (175 mm collimator with 0.5 mm pinholes). The effect of NaN₃ could not be investigated using XRD due to its low reaction threshold. The XRD data (Figures 3.4 (a,b)) show that the crystallinity of Bi₂Te₃ changes slightly with a change in film thickness. The XRD pattern of Bi2Te3 also reveals its polycrystalline nature [5]. Deposition of nitrocellulose on the Bi₂Te₃ film also influences the XRD pattern. The Bi₂Te₃ peak at around 18.1° 20 ((006) plane for rhombohedral Bi₂Te₃- ICDD No. [1-75-0921]) is no longer exhibited in the Bi₂Te₃ samples with nitrocellulose (Figures 3.4 (c,d)). The disappearance of this peak may be due to incoherent scattering and adsorption effects. It is possible, that on coating the Bi₂Te₃ sample with the nitrocellulose surface was effectively masked, inhibiting the penetration of x-rays to, and collection of scattering data from, the lower Bi₂Te₃ surface. This effect is

particularly acute for the relatively low intensity (006) Bi_2Te_3 peak, which occurs in the same region as the principal XRD reflections for nitrocellulose (ICDD No. [03-0114]). This argument is confirmed further by XRD data from samples following consumption of the nitrocellulose, where the (006) peak reappears (Figure 3.4 (e)).

The effect of adding nitrocellulose on the 18.1° 2θ peak is slightly different for the 5 and 10 µm Bi₂Te₃ films. This observation may be due to slightly different porosities of the two Bi₂Te₃ thicknesses, resulting in different behaviour of incoherent scattering and adsorption effects.

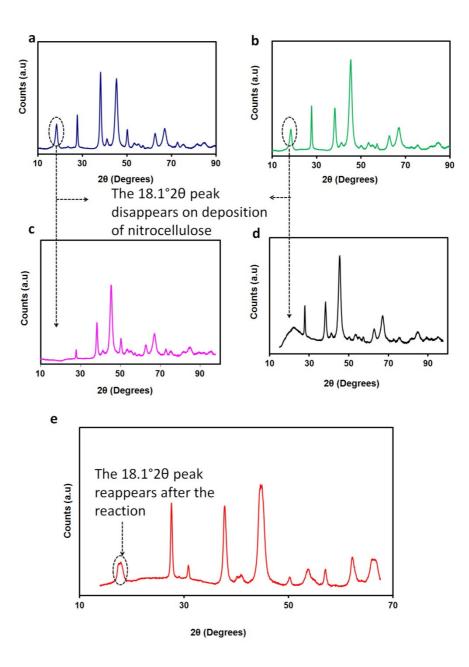


Figure 3.4: XRD pattern of: (a) $5 \mu m$ thick Bi_2Te_3 film, (b) $10 \mu m$ thick Bi_2Te_3 film, (c) $5 \mu m$ thick Bi_2Te_3 film after depositing a layer of nitrocellulose, and (d) $10 \mu m$ thick Bi_2Te_3 film after depositing a layer of nitrocellulose and (e) the Bi_2Te_3 film after the reaction (note: traces of oxidized Bi_2Te_3 (ICDD No. [24-0154]) and carbon are also present in the after the reaction XRD pattern. The oxidation of Bi_2Te_3 may be the reason for the emergence of the $31^{\circ} 2\theta$ that appears in (e) after the consumption of nitrocellulose.

3.2.4 Thermal conduction of AI_2O_3 and terracotta substrates

In order to show the difference in thermal conductivities of the Al_2O_3 and terracotta substrates, both were heated at one end for the same duration using a custom-made blowtorch and the temperature profile was obtained at the other end to see how fast thermal conduction occurs through the substrate.

As seen from Figure 3.5, the temperature for Al_2O_3 rises rapidly to about 130 °C in about 40 sec. The terracotta substrate however reaches a maximum temperature of around 40 °C and takes about twice the time taken by Al_2O_3 to reach peak temperature. It should be noted that the temperature continues to rise even after the heat source is withdrawn. This is because heat takes time to travel from one end to the other and finally dissipates, depending on the thermal conductivity of the material. Therefore, the peak temperature is obtained a few seconds after the heat source is turned off. However we can see that terracotta takes approximately 60 seconds longer than Al_2O_3 to reach its peak temperature. A similar observation is made in the cooling durations of the two substrates. While Al_2O_3 cools down to room temperature in about 150 seconds from the point of its peak temperature, terracotta takes approximately 240 seconds to cool down to room temperature. These observations clearly demonstrate that the thermal conduction through terracotta is significantly slower than Al_2O_3 .

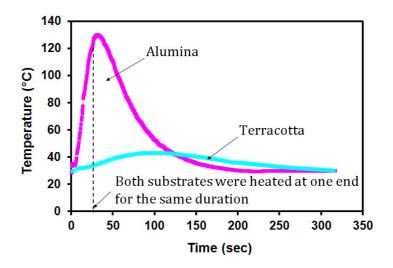


Figure 3.5: Difference in the thermal conduction rate of Al₂O₃ and terracotta substrates.

3.2.5 Calculation of Specific Power

In order to obtain the specific power, the masses of the fuel (nitrocellulose & sodium azide) and Bi₂Te₃ films were considered. The relationship between mass, density and volume was used for calculating the mass of the Bi₂Te₃ as: $m = \rho \times V$ where, *m* is the mass in grams (g), ρ is the density in g/cm³ and *V* is the volume in cm³. For Bi₂Te₃ ρ =7.7 g/cm³ [6] and V depends on the dimensions of the sample and is calculated using the formula $V = l \times w \times h$, where l is the length, w is the width and h is the thickness of the Bi₂Te₃ film in cm, respectively.

For fuels, nitrocellulose and NaN₃ in our case, we knew the concentration of the two in their respective solutions. As mentioned in Section 3.2.2, 15g/L nitrocellulose and 20g/L NaN₃ were used by drop casting. Hence, we know the amount of solution for each fuel and therefore the corresponding mass for each sample, depending on the volume of the liquid placed on the Bi₂Te₃ films. The sum of the masses of the Bi₂Te₃ film and the fuels gives the total mass of the materials used. The corresponding power from the sample is then scaled to per kg of the materials to obtain the specific power of the sample in kW/kg.

3.3 Theory of Thermopower Wave oscillations

In order to assess the behaviour of the thermopower waves the author adapted the theory of combustion waves to describe coupled thermal waves in fuel/ Bi₂Te₃/ Al₂O₃ or fuel/ Bi₂Te₃/ terracotta systems. The Bi₂Te₃ layer is comparatively thin (5 or 10 μ m compared to 100 μ m Al₂O₃ substrate), so the main path for thermal conduction is through the substrate. Additionally, our experimental systems are much longer than they are wide. As a result, one-dimensional approximations for both the fuel/Al₂O₃ system and the fuel/terracotta system are considered in the calculations. It means that fuel either exchanges heat with a thermally conductive substrate of alumina with κ =20 W.m⁻¹.K⁻¹ or much less thermally conductive substrate of terracotta with κ =1 W/m.K (see Figure 3.5).

The theoretical approach is of particular importance as it can be used to predict the behaviour of the system, the velocity of the wave front and the possibility of oscillations. It is assumed that the solid fuel combustion is exothermic, oxygen is supplied in excess, and governed by Arrhenius kinetics with volumetric heat loss, the dimensional equations for the conservation of heat and mass are [7]:

$$\rho c_{p} \frac{\partial T}{\partial t} = k \frac{\partial^{2} T}{\partial x^{2}} + \rho Q A w e^{-E/RT} - \frac{hS}{V} (T - T_{a})$$
(1)

$$\rho \frac{\partial w}{\partial t} = -\rho A w e^{-\mathbf{E}/\mathbf{R}T} \tag{2}$$

where *T* and *w* denote the temperature and the concentration of the fuel, respectively; *x* and *t* describe space and time variables, ρ is the density of the fuel (kg/m³), c_p is the specific heat of the fuel (J/kg.K), k is the thermal conductivity of the fuel (J/s.m.K), Q is the heat of reaction (J/kg), A is the pre-exponential rate constant (/s), E is the activation energy (J/mol), R is the universal gas constant (8.314 J/mol.K). Heat is transferred from the fuel layer to the Bi₂Te₃/substrate layer and to the surroundings. As we are using a one-dimensional averaged model, the term $\frac{hS}{V}(T - T_a)$ models both the transfer to Bi₂Te₃/substrate and the Newtonian cooling to the ambient surrounding, which is at a temperature T_a [7]. In the latter case, S/V is the surface-area-to-volume ratio of the fuel (/m) and h is the heat transfer coefficient from the fuel to the quiescent surroundings (J/s.m².K¹) [7] which is typically quite small. The term $\rho QAwe^{-E/RT}$ in Equation (1) accounts for the exponential decomposition reaction of the fuel.

As a first step towards analysing the combustion, the model presented by Mercer *et al.*[7] is applied. Defining the non-dimensional temperature to be $u = \frac{RT}{E}$ and re-scaling space

and time co-ordinates by $\sqrt{\frac{\rho QAR}{kE}}$ and $\frac{QAR}{c_pE}$, respectively, leads to the non-dimensional

version of the governing equations:

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + w e^{-1/u} - \ell(u - u_a)$$
(1a)

$$\frac{\partial w}{\partial t} = -\beta w e^{-1/u} \tag{2a}$$

where we define $\beta = \frac{Ec_p}{QR}$, a parameter related to the properties of the fuel, and the non-

dimensional volumetric heat transfer, $\ell = \frac{hSE}{VR\rho QA}$.

Depending on the value of system parameters, thermopower waves with or without oscillations can be predicted [8, 9]. For simplification in the theoretical analysis, we start with a one-dimensional space model and transform it to a non-dimensional system to predict the occurrence of oscillatory combustion linked to the heat losses.

The determination of all the necessary parameter values is the key to being able to apply the model to a real system. The solution of the model presented by Mercer *et al.*, [7] assumes that the ambient temperature is absolute zero ($u_a=0$). Ambient temperatures are typically very small compared to the reaction temperature and hence this assumption has little effect on the overall behaviour of the solutions to this model.

For the fuel (which is a combination of nitrocellulose and sodium azide in our case) the values parameters are as follows: S/V=1/240 / μ m , ρ = 1600 kg/m³, c_p =1596 J/kg.K, Q = 4.75 ×10⁶ J/kg, E = 1.26× 10⁵ J/mol, A = 10⁵ /s and h=2 × 10⁻³ J/s.m².K. In all cases the β value is 5.09 for the nitrocellulose fuel layer. Two extreme conditions are now considered for the substrate:

3.3.1 A thermally conductive substrate (x=20 W/m.K)

This system is similar to the schematic, which is shown in Figure 3.1. The fuel is deposited on Al_2O_3 (with a thin layer of Bi_2Te_3 in between) with a thermal conductivity

of approximately 20 W/m.K. This results in the non- dimensional heat loss parameter ℓ = 1.7 ×10⁻⁴. The oscillation period is directly related to β and ℓ . For β = 5.09 the critical heat loss value for the onset of oscillations can be estimated from Figure 3.6 as being smaller than ℓ/β = 0.000035. Furthermore, the model predicts that there would be a time of approximately 0.05 seconds between peaks in the oscillating signal. In this case an oscillatory behaviour is predicted hence, the slower and faster propagation speeds are strongly dependent on very fine scale details of the solution to the model; the slower one being of the order of 0.002m/sec and the faster one, an order of magnitude higher.

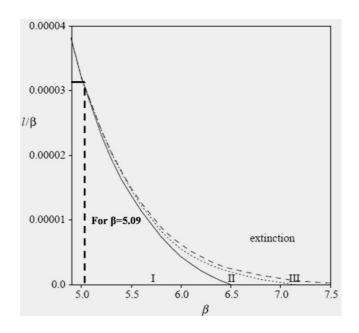


Figure 3.6: Region in the parameter (β , ℓ / β) space where combustion waves and extinction occurs.

Due to the oscillatory behaviour, a two dimensional model will better account for the various paths of heat conduction to provide accurate velocity predictions in this case.

3.3.2 A substrate with a low thermal conductivity (x=1 W/m.K)

This system is similar to the schematic which is shown in Figure 3.1. The fuel is deposited on terracotta (with a thin layer of Bi_2Te_3 in between) with a thermal conductivity of approximately 1 W/m.K. The change in thermal conductivity of the substrate effects the heat loss parameter. In case of terracotta the heat loss parameter is

obtained as $\ell = 2 \times 10^{-5}$ which according to Figure 3.6 predicts that oscillations will cease to exist.

Next, the model proposed by McIntosh *et al.* is applied to predict the reaction propagation velocity for the fuel/terracotta system [11]. The equation is as follows:

$$c - \frac{\ell}{c} = \frac{1}{c} e^{-\beta} (e^{-\beta} (e^{-\beta}))$$
(3)

where c is the wave speed in m/sec. Using Equation (3), it is estimated that the reaction average propagation velocity is approximately 0.007m/sec. The velocity measured in the author's experiments for the fuel/terracotta system was about 0.009m/sec so the simulation agrees reasonably well with our measurements. Hence, the mathematical model is able to reasonably predict the oscillation period and the reaction propagation velocity.

3.4 Results and discussion

A schematic of a Bi_2Te_3 based thermopower device is shown in Figure 3.1. Ignition is initiated at one end of this system using a custom-made blow torch with a fine tip and the resulting reaction wave self-propagates to the other end. We show that such self-propagating thermal waves result in either oscillating or non-oscillating wave front velocities [12].

For the self-propagation of an exothermic reaction, heat must be generated through the reaction faster than it is removed by thermal diffusion [13]. Hence, nitrocellulose $[C_6H_8 (NO_2)_2O_5]$ is used as the fuel due to its large enthalpy of reaction. Sodium azide (NaN_3) in aqueous solution (50mg/mL) is then added to serve as a primary igniter to lower activation energy (40kJ/mol for NaN₃, compared to 110 – 150 kJ/mol for nitrocellulose) [14, 15]. Samples with low nitrocellulose and/or NaN₃ weights showed no sustained reaction under any conditions. The Bi₂Te₃ layer generally survived the thermopower

wave propagation and remained intact after the reaction, which is proved by the optical observation and X-ray diffraction (XRD) pattern, shown in Figure 3.3 (e).

Several samples using different masses of the fuel and two different thicknesses of Bi_2Te_3 (5 µm and 10 µm) were prepared and tested. A high speed camera tracked the propagation of the reaction front. Figure 3.7 depicts the propagation of one such reaction along a fuel/ Bi_2Te_3/Al_2O_3 sample at different times.

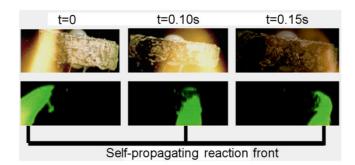


Figure 3.7: Images of the self-propagating reaction front using a high speed camera. Ignition occurs at the left corner and the wave self-propagates across the surface to the other end. The length of the sample is ~14 mm. The propagation of the combustion wave was filmed using a high speed video camera (Phantom v4.3, Vision Research Inc.) with a 105 mm f/2.8 Micro-Nikkor lens at 1000 frames per second with an exposure time of 25 μ s for each frame.

The accelerated reaction wave drives a simultaneous wave of electrons. This wave of electrons results in oscillatory, followed by non-oscillatory, voltage output. An oscilloscope (Agilent MSO7014) was used for voltage acquisition from the thermopower experiments. The voltage signal was positive for waves emanating from the negative electrode (Figure 3.8 (a)). This observation can be attributed to the negative Seebeck coefficient of Bi₂Te₃ (-287μ V/K). The voltage signal is of the same duration as the corresponding reaction wave, thereby enabling the calculation of the reaction propagation velocity for the sample.

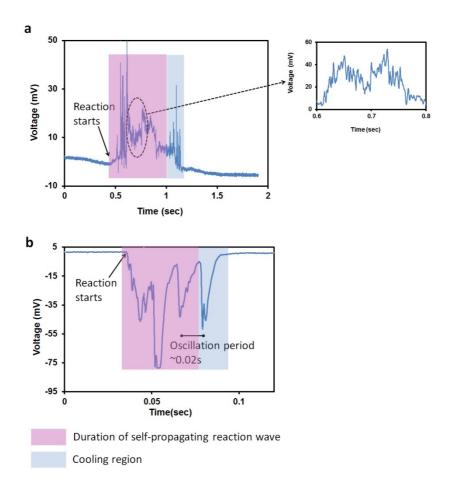


Figure 3.8: Thermopower voltage signals in reaction and cooling zones. The voltage signal is divided into two phases: the initial oscillation phase indicates reaction time and the smooth phase reflects the cooling time. The voltage returns to zero after the temperature across the sample reaches equilibrium. (a) Negative voltage generation with clear oscillating regions. (b) Positive voltage generation with oscillating zones after reversing the measurement system electrodes.

The chemically driven thermopower waves with high propagation velocities have a constant polarity depending on the direction of the reaction. This suggests that the wave passes through the system faster than the cooling time of the region it left behind, resulting in a highly efficient direction of energy [1].

3.4.1 System based on a thermally conducting substrate (Al₂O₃)

The average wave front propagation velocity is in the order of 0.01 to 0.9 m/sec with the median of 0.4 m/sec for Al_2O_3 substrate and it was mostly oscillatory, particularly for large velocity reactions. Very wide ranges of velocity were also observed by Strano *et al.* [1] The oscillatory nature of the system based on thermally conductive Al_2O_3 (20 W/m.K) was discussed in section 3.3.1 of this chapter and clearly observed in experimentally obtained

output signals. Sustained reaction waves specifically along the direction of the Bi₂Te₃ layer (Figure 3.7) were observed at velocities up to 10 orders of magnitude larger than the bulk combustion rate of nitrocellulose (20 - 70 mm/sec) under atmospheric conditions [1, 16]. The high speed videos of the reaction waves also show that in some cases combustion behind the main wavefront may be interrupted till the arrival of the next transverse wave. The reason for the emergence of the transverse wave may be due to the combustion wave being spatially unstable [17]. This interrupted combustion pattern may also be responsible for the large oscillations seen in the voltage. Figures 3.8 (a,b) show the voltage measurements across two samples of the fuel/ Bi₂Te₃/Al₂O₃ system (the measurement system electrodes were connected in reverse for Figure 3.8 (b). The voltage profiles in Figure 3.8 can be classified into two phases: an initial reaction phase and a cooling phase [12]. The high speed videos show that the oscillation region corresponds to the period when the reaction waves are propagating. The reaction phase consists of a region of rising voltage as the wavefront spreads radially across the sample until all the combustion fuel is consumed. This is followed by a region of exponential decay [12]. Large temperature gradients result in voltages with peak magnitudes in the range of 40 to 150 mV and oscillations with peak-to-peak amplitude of up to 140 mV. The peak power obtained from these devices is as large as 10 mW. By comparing Figures 3.8 (a,b) it can be seen that after swapping the electrodes of the measurement system the voltage polarity was also reversed. This implies that the polarity of the reaction depends on the Seebeck coefficient of Bi₂Te₃ and the direction of the reaction.

The shape and magnitude of the voltage signals varied through different samples. Figures 3.9 (a,b) show the respective velocity profiles of two starkly different voltage signals shown in Figures 3.9 (c,d). The velocity profiles for the corresponding voltage profiles are obtained from the high speed videos. The profiles illustrate that the reaction velocities also exhibit an oscillatory behaviour. Additionally, it seems that the voltage oscillations are correlated with the velocity profiles. Further work is required to accurately establish the relation between the

velocity and voltage oscillations. The shape of the velocity profiles again proves that the propagation of the combustion wave is not linear and is highly oscillatory.

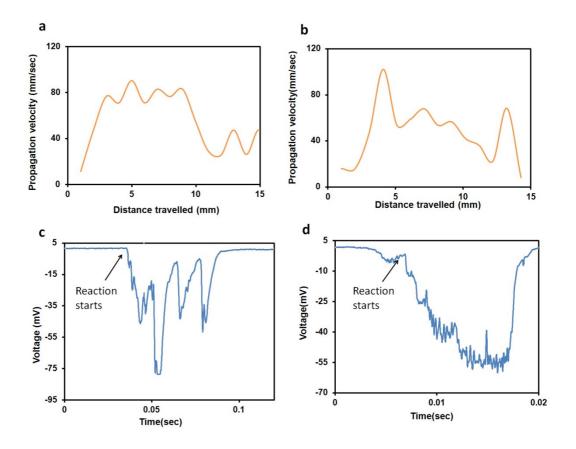


Figure 3.9: Velocity profiles (a,b) along with the corresponding voltage signals (c, d). Reaction velocity also exhibits an oscillatory behaviour. The oscillations in voltage seem to follow the velocity oscillations in general. The velocity profiles are extracted from the high speed videos. The x axis of the velocity graphs show the distance travelled by the self-propagating wavefront from the point of ignition. Velocity of this wavefront is obtained at different points during the course of its propagation. Velocity oscillations in the reaction wave may be responsible for the significant oscillations in the voltage signal. The reaction time corresponds to the duration of the voltage signal.

The magnitude of the voltage depends on the sample mass, particularly the amount of fuel. Larger mass results in a higher peak value of the voltage signal as well as higher output power, as shown in Figures 3.10 (a,b) Analysis of the voltage and power vs mass data indicates an optimal mass range, where both the voltage and power obtained are maximized, about 24 – 27 mg. The data indicate that a very low mass of fuel cannot supply enough heat to sustain exothermic reaction waves. On the other hand, too much fuel may provide more heat energy but the non-reacted regions require a large amount of

energy, and consequently the propagation may not be sustained. As a result, we may expect that there is an optimal mass range to promote sustained reaction propagation, which is also suggested by Strano *et al* [1].

As can be seen in Figure 3.10 (c) both generated voltages for samples with Bi_2Te_3 films of 5 and 10 µm thicknesses have fairly similar patterns. The voltages produced for 10 µm sample were slightly larger than the 5 µm samples due to their higher sheet resistance. Additionally, there was no obvious relation between the propagation velocity and magnitude of voltage produced, as can be seen in Figure 3.10 (d).

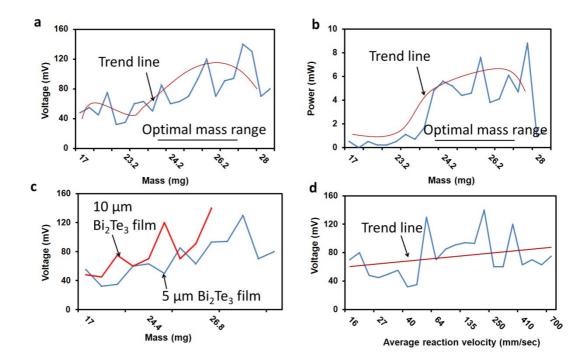


Figure 3.10: (a) Variation of peak voltage with mass of (fuel & Bi_2Te_3). The trend line indicates that peak voltage increases with the mass of the materials. (b) Power plotted as a function of system mass. The optimal mass range corresponds to the one for peak voltage. (c) Variation of peak voltage with mass for two different thicknesses of the Bi_2Te_3 film. (d) Voltage as a function of the propagation velocity.

However, very thick Bi_2Te_3 films (>30 µm) effectively reduced the thermal conductivity effect of the Al_2O_3 substrate, and hence, oscillations ceased. This was both predicted by our theoretical model and shown by experiments. For these systems, the oscillation almost stopped and the produced voltage was relatively low. The cross-sectional SEM of thick Bi_2Te_3 film (thickness >30 µm) sample and the corresponding voltage signal are shown in Figures 3.11 (a) and 3.11 (b), respectively.

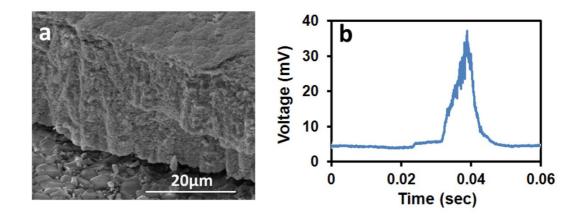


Figure 3.11: (a) Cross-sectional SEM image of Bi_2Te_3 film with thickness of >30 µm on Al_2O_3 substrate and (b) the corresponding thermopower voltage signal. It can be seen that the magnitude of voltage has been reduced compared to thinner Bi_2Te_3 films and there is nearly no oscillations.

3.4.2 System based on substrate with low thermal conductivity (terracotta)

The thermal conductivity of the substrate determines the oscillatory behaviour and the wave front velocity. Due to the low thermal conductivity of terracotta, which is of the order of 1 W/m.K, no oscillation was predicted as per section 3.3.2 of this chapter. In addition, the theoretical calculations also suggested that the propagation velocity would be reduced dramatically. Confirming these predictions, the wave propagation velocity for the fuel/Bi₂Te₃/terracotta system was consistently measured to be lower, on average approximately ~0.01 m/sec (30-40 times less than the Bi₂Te₃/Al₂O₃ films on average). Figure 3.12 is an example output signal of a fuel/Bi₂Te₃/terracotta system, which illustrates the voltage generated peaks of 7 mV with no oscillations. The difference in propagation velocities using the two substrates closely follows the difference in thermal conductivities of the two substrates. The thermal conductivity of Al₂O₃ is 20 times that of terracotta, and we consequently observe significant difference in wave front propagation velocities in the order of 30-40. This further proves that thermal conduction from the fuel layer to the substrate drives reaction wave propagation.

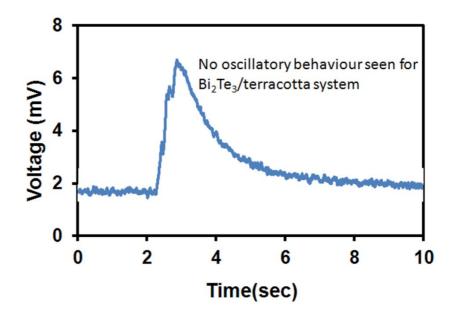


Figure 3.12: Voltage signal obtained using a Bi_2Te_3 layer on a terracotta substrate (low thermal conductivity). It shows that the oscillations cease to exist if the effective thermal conductivity is low. This observation is in line with the prediction made by the author's theoretical model. Furthermore, it also shows that the thermal conductivity of the substrate plays an important part in determining whether oscillations occur.

3.5 Summary

In this chapter, the author demonstrated a thin film thermopower wave system based on Bi_2Te_3 as the core TE material. It was shown that the generation of directionally dependant thermopower waves using a fuel/ Bi_2Te_3/Al_2O_3 system resulted in oscillatory voltages as high as 150 mV and powers up to 10 mW. At the same time a high specific power in the order of 1 kW/kg was maintained. This can be ascribed to the high *S* of Bi_2Te_3 (~ -200 μ V/K) and high electrical conductivities of the order of 10⁵ S/m.

A full analysis of the system was carried out and it was observed that when using the thermally conductive substrate of alumina, the output showed strong oscillatory behaviour, while there were no oscillations seen when terracotta substrates with a low thermal conductivity were used. This behaviour was described well by the theoretical model using the heat transfer equations with suitable boundary conditions. It was also shown using characterization techniques such as XRD that the Bi₂Te₃ films remained intact at the end of the thermopower wave propagation.

Furthermore, it was demonstrated that the mass of the fuel played an important role in determining the magnitude of the output voltage. A higher fuel mass generally resulted in larger output voltages. However, it was observed that the amount of fuel exhibited an optimal mass range in which the output voltages were maximised.

This work conducted by the author of this thesis is of utmost importance as it demonstrates thermopower wave systems in a thin film geometry for the first time. The use of thin films is important as it will enable the incorporation and testing of a wide variety of core TE materials in order to increase the output voltage and specific power outputs from such sources. By developing thermopower wave sources based on Bi₂Te₃, a common TE material, output voltages higher than MWNT based thermopower sources (>150%) were generated while maintaining large specific power. This is an important step towards the realisation of thermopower waves systems as a new category of micro power sources.

In the next chapter, the author will use a novel combination of two commonly used TE materials with complimentary semiconducting properties (p-type Sb_2Te_3 and n-type Bi_2Te_3) in order to generate voltage signals with alternating polarities. A detailed comparison of p-type Sb_2Te_3 and n-type Bi_2Te_3 based thermopower wave sources will be presented.

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Chapter 4

Comparison of p-type Sb₂Te₃ and n-type Bi₂Te₃ based Thermopower Wave Sources

4.1 Introduction

In the previous chapter, the author demonstrated thin film thermopower wave devices based on thermoelectric (TE) cores of n-type bismuth telluride (Bi₂Te₃) for the first time. Voltages and oscillation amplitudes larger (>150%) than previously developed thermopower wave system based on (MWNTs) were demonstrated, while maintaining a high specific powers in the order of 1 kW/kg. However, as discussed in chapter 1, voltage signals with alternating polarities are highly desirable for practical applications. This could potentially be achieved by implementing a combination of p and n-type TE core materials. However, it was not known whether the phenomenon of thermopower waves extends to p-type materials which have holes as the majority charge. Subsequently, based on the analysis presented in chapter 2, the author chose to develop thermopower wave sources based on a novel combination of p-type antimony telluride (Sb₂Te₃) and n-type Bi₂Te₃. Sb₂Te₃, a conventional TE material was chosen as the complimentary core TE material due to its high Seebeck coefficient (~180 μ V/K) and electrical conductivity (10⁴ S/m).

In this chapter, the author will demonstrate thermopower wave sources by incorporating p-type Sb_2Te_3 and n-type Bi_2Te_3 as the core TE materials. In order to compensate for the low thermal conductivity of Sb_2Te_3 and Bi_2Te_3 , the author will place them on thermally conductive alumina (Al₂O₃) substrates. Subsequently, highly exothermic chemical reaction of a solid fuel (nitrocellulose) will be coupled to charge carriers in Sb_2Te_3 and Bi_2Te_3 layers to generate self-propagating thermopower waves which entrain holes and

electrons in Sb₂Te₃ and Bi₂Te₃ respectively, to generate voltage and power. The theory of combustion waves will be adapted to understand the behaviour of thermopower waves in the Sb₂Te₃ and Bi₂Te₃ based thermopower wave devices. The author will present detailed characterizations of the Sb₂Te₃ and Bi₂Te₃ films before and after thermopower wave propagation. The role of thermal conductivity of the substrates on the behaviour of thermopower waves will be assessed by depositing Sb₂Te₃ and Bi₂Te₃ on terracotta (baked natural polysilicate) which exhibits a contrastingly low thermal conductivity compared to Al₂O₃. The influence of the mass of fuel on the voltage and power generated will be studied. A detailed comparison of the output voltages, specific powers, oscillatory behaviours and thermopower wave propagation velocities for Sb₂Te₃ and Bi₂Te₃ based thermopower wave devices will also be presented in this chapter. The outcome of this work was published as a full article in the journal Energy & Environmental Science.

4.2 Experimental

4.2.1 Deposition of Sb₂Te₃ and Bi₂Te₃ films

The Sb₂Te₃ and Bi₂Te₃ films were deposited on Al₂O₃ and terracotta substrates using RF magnetron sputtering, under identical deposition conditions. High purity (99%) Sb₂Te₃ and Bi₂Te₃ targets (Vin Karola Instruments) were used for sputtering. The chamber was pumped down to a pressure of 2×10^{-5} Torr before starting the sputtering process. Al₂O₃ and dimensions of terracotta substrates with linear 12-15 mm (L) \times 4-6 mm (W) \times 100 μ m (H) were utilised after being cleaned using acetone, isopropyl alcohol, and distilled water. The substrates were held at a constant temperature of 100 °C throughout the sputtering process, in which a power of 100 W and an argon atmosphere with 10 mTorr process pressure were used. Sputtering time of 90 mins resulted in a 6 μ m thick Sb₂Te₃ and 5 μ m Bi₂Te₃ films, repectively. Electrical contacts between the copper tape electrodes and the thermoelectric layer were made using adhesive conductive silver paste (42469, Alfa Aesar). The resistance between the

electrodes for Sb_2Te_3 films and Bi_2Te_3 films ranged from 6-12 Ω and 2-10 Ω , respectively [1].

4.2.2 Preparation of fuel

The fuel used for the exothermic reaction was a combination of nitrocellulose $(C_6H_8(NO_2)_2O_5)$ and sodium azide (NaN_3) . Nitrocellulose was used due to its large enthalpy of reaction $(4.75 \times 10^6 \text{ J/kg})$. It was prepared by dissolving millipore nitrocellulose membranes (N8645, Sigma Aldrich) in acetonitrile (15g/L). This solution was then dropcast on the Bi₂Te₃ and Sb₂Te₃ films using a pipette and left to dry. The acetonitrile evaporated leaving an adhesive and solid nitrocellulose layer deposited on top of the thermoelectric materials. NaN₃ was used to serve as a primary igniter due to its low activation energy (40 kJ/mol for NaN₃ compared to 110-150 kJ/mol for nitrocellulose) [2, 3]. NaN₃ (14314, Alfa Aesar) in aqueous solution (50 mg/mL) was then added on top of the nitrocellulose layer using a pipette. The total thickness of the fuel layer was ~240 µm.

4.2.3 Characterization of Sb₂Te₃ and Bi₂Te₃ films

Figures 4.1 (a,b) show scanning electron micrographs (SEM) of Sb₂Te₃ and Bi₂Te₃ films, respectively. The images clearly show the difference between the structures of the two films with Bi_2Te_3 exhibiting a more irregular structure compared to Sb₂Te₃. This confirms the polycrystalline nature of Bi_2Te_3 [1]. The SEM images also show that Bi_2Te_3 films are more porous than Sb₂Te₃, when deposited on Al₂O₃ substrates under identical conditions.

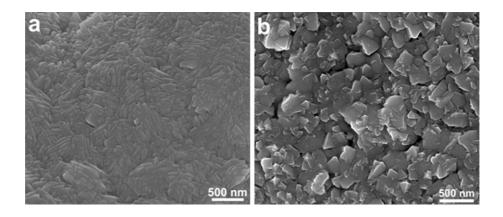


Figure 4.1: The SEM images of: (a) Sb₂Te₃ film on Al₂O₃ (b) Bi₂Te₃ film on Al₂O₃.

A surface profilometer (Ambios Technology XP-2) was used to further investigate the morphology of the Sb₂Te₃ and Bi₂Te₃ surfaces and that of the substrate (Figure 4.2 (a,b)). The average surface roughness of Sb₂Te₃ and Bi₂Te₃ was determined to be 0.4 and 0.7 μ m, respectively. This indicates that the Bi₂Te₃ films are more porous; thereby, confirming the earlier observation made from the micrograph in Figure 4.1 (b). A greater porosity enables more fuel to be placed on the surface of the films. Additionally, a higher porosity is also important to facilitate increased thermal conduction between the fuel and thermoelectric films [1], resulting in a more sustained reaction propagation.

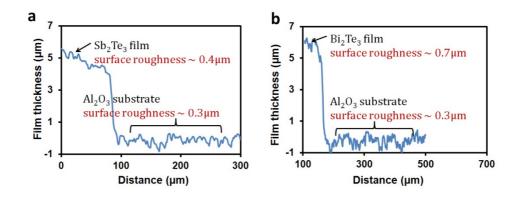


Figure 4.2: (a) surface profile of a 6 μ m Sb₂Te₃ film on Al₂O₃ substrate, (b) surface profile of 6 μ m Bi₂Te₃ film on Al₂O₃ substrate.

X-ray diffraction (XRD) measurements were carried out on the Sb_2Te_3 and Bi_2Te_3 samples in order to assess the crystallinity of the films. The XRD was conducted using a Bruker D8 DISCOVER microdiffractometer fitted with a GADDS (General Area Detector Diffraction System). The XRD pattern for Sb_2Te_3 (Figure 4.3 (a), 1] shows three well defined peaks, which indicate its crystalline structure. In case of Bi_2Te_3 , the XRD pattern reveals a more polycrystalline structure (Figure 4.3 (b), 1] [4]. On addition of nitrocellulose different effects on the XRD patterns of Sb₂Te₃ and Bi₂Te₃ are observed (Figure 4.3 (c), 2 and Figure 4.3 (d), 2]. For Bi_2Te_3 the peak at 18.1 2θ (006) plane for rhombohedral Bi₂Te₃ - ICDD No. [1-75-0921]) is no longer exhibited in the samples with nitrocellulose (Figure 4.3 (d), 1). Possibly incoherent scattering and adsorption effects may be responsible for the disappearance of this peak. It is also probable that the nitrocellulose coating on both the Sb₂Te₃ and Bi₂Te₃ samples effectively masks the surface, thus inhibiting the penetration of X-rays to, and collection of scattering data from this particular peak. This effect is particularly acute for the relatively low intensity (006) Bi_2Te_3 peak, which lies in the same region as the principal XRD reflections for nitrocellulose (ICDD No. [03-0114]) [1]. Sb₂Te₃ on the other hand does not show any significant diffraction peaks in this region. Thus, the masking effect caused by the nitrocellulose layer only results in a general decrease in diffraction intensity across its entire diffraction pattern. The XRD patterns of the samples following consumption of the nitrocellulose are also shown (Figure 4.3 (c), 3 and Figure 4.3 (d), 3], and will be discussed later.

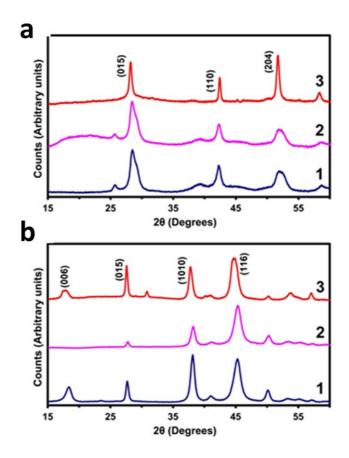


Figure 4.3: (a) 1. The XRD pattern of Sb_2Te_3 before thermopower wave propagation, 2. after adding nitrocellulose and 3. after thermopower wave propagation (b) 1. The XRD pattern of Bi_2Te_3 before thermopower wave propagation, 2. after adding nitrocellulose and 3. after thermopower wave propagation.

4.2.4 Comparison of thermal conduction rate of Sb₂Te₃ and Bi₂Te₃

In order to show the difference in the thermal conduction rates of Sb₂Te₃ and Bi₂Te₃, the measurement set up Figure 4.4 (a) is used. The Sb₂Te₃/Al₂O₃ and Bi₂Te₃/Al₂O₃ samples of ~ 12 mm length were used for the measurement and the thickness of both Sb₂Te₃ and Bi₂Te₃ films were equal to 6 µm. A heater with a sharp tip was used as the heating source and was positioned at one end on the sample. The temperature profile was acquired at the opposite end using a TENMA 727730 thermocouple. The heat source was kept in place until the temperature at the other end reached a constant value (approximately 200 s) in equilibrium with the ambient. Figure 4.4 (b) shows the temperature profile for the two samples. It shows that the temperature rises to approximately 47 °C for both samples. However, the rate of rise is approximately 2.2 times higher for the Al₂O₃/Sb₂Te₃ sample which is analogous to the

ratio of the thermal conductivities of Sb_2Te_3 and Bi_2Te_3 . Therefore, the rate of heat conduction in Sb_2Te_3 is ~2.5 times faster than that in Bi_2Te_3 .

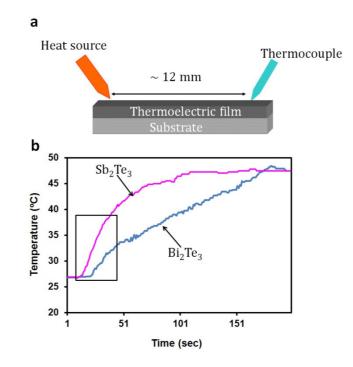


Figure 4.4: (a) Measurement set up, (b) Difference in thermal conduction of Sb₂Te₃ and Bi₂Te₃ films.

4.2.5 Electrical conductivities of Sb₂Te₃ and Bi₂Te₃ films

In order to compare the electrical conductivities of the two films four point probe measurements were carried out on Sb₂Te₃ and Bi₂Te₃. The resistivity can be calculated using the equation $\rho = R_{Sh} \times t$ in which ρ is the resistivity of the film in Ω .m, R_{Sh} is the sheet resistance of the film in Ω/\Box and t is the thickness of the film in m.

4.2.5.1 Sb₂Te₃ film

The four point probe showed that the sheet resistance of the Sb₂Te₃ film was 3.103 Ω/\Box for the Sb₂Te₃ film of approximately 6µm. Therefore the resistivity of the film was calculated to be 1.86 × 10⁻⁵ Ω .m. Inverse of the resistivity gives the conductivity. Thus, the electrical conductivity of the Sb₂Te₃ film was found to be 5.3 × 10⁴ S/m.

4.2.5.2 Bi₂Te₃ film

A similar approach was used to calculate the electrical conductivity of the Bi₂Te₃ film. The sheet resistance of the Bi₂Te₃ film was found to be 1.75 Ω/\Box . Therefore the electrical conductivity of the film was calculated to be 1.1×10^5 S/m. The above measurements show that the electrical conductivity of Bi₂Te₃ is an order of magnitude higher than Sb₂Te₃. The values obtained are also comparable with the literature values of 10⁴ and 10⁵ S/m for Sb₂Te₃ and Bi₂Te₃ films respectively [5-7].

4.2.6 Calculation of Specific Power

In order to obtain the specific power, the masses of the fuel (nitrocellulose & sodium azide) and thermoelectric films were considered. The relationship between mass, density and volume was used for calculating the mass of the Sb₂Te₃ and Bi₂Te₃ films as: $m = \rho \times V$, where, *m* is the mass in grams (g), ρ is the density in g/cm³ and *V* is the volume in cm³.

 ρ =6.5 g/cm³ and 7.7 g/cm³ for Sb₂Te₃ and Bi₂Te₃ respectively [8, 9]. and *V* depends on the dimensions of the sample and is calculated using the formula, $V = l \times w \times h$ where *l* is the length, *w* is the width and *h* is the thickness of the thermoelecteric film in cm, respectively.

For fuels, nitrocellulose and NaN₃ in our case, we knew the concentration of the two in their respective solutions. As mentioned in section 4.2.2, 15g/L nitrocellulose and 20g/L NaN₃ were used by drop casting. Hence, we know the amount of solution for each fuel and therefore the corresponding mass for each sample, depending on the volume of the liquid placed on the thermoelectric films. The sum of the masses of the thermoelectric film and the fuels gives the total mass of the materials used. The corresponding power from the sample is then scaled to per kg of the materials to obtain the specific power of the sample in kW/kg.

4.3 Results and Discussion

4.3.1 Comparison of Sb₂Te₃ and Bi₂Te₃ based thermopower devices

4.3.1.1 Thermopower devices based on Al₂O₃ substrate

Figure 4.5 shows the schematic of the set-up used for the thermopower experiments. Ignition takes place at one end of this system and the reaction self-propagates to the other end.

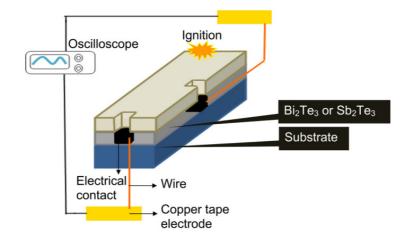


Figure 4.5: Schematic of the fuel/thermoelectric material/substrate thermopower wave generation system. Ignition at one end of the fuel (combination of nitrocellulose and sodium azide) layer results in a self-propagating exothermic reaction. (not to scale)

A custom-made blow torch with a localized flame tip is used to initiate the reaction. Samples with low mass of nitrocellulose or NaN₃ (masses below 15 mg per 75 mm²) showed no sustained wavefront propagation in any direction. Several samples using different mass of the fuels were prepared and tested. For both Bi_2Te_3 and Sb_2Te_3 systems identical masses were used to ensure statistical comparison. Ignition at one end of the system, shown in Figure 4.5, results in an accelerated self-propagating reaction wave that drives a simultaneous wave of free carriers. This wave of carriers results in a flow of current and voltage across the devices. The voltage signal exhibited a positive polarity for waves initiating at the positive electrode for p-type Sb_2Te_3 and the opposite polarity for the n-type Bi_2Te_3 . The duration of the output signal corresponds to the reaction time, thus enabling us to calculate the reaction propagation velocity. Even in oscillatory mode, the thermopower waves always exhibit a constant polarity during the reaction, depending on the direction of wavefront propagation. This suggests that the wave passes through the system faster than the cooling time of its posterior region [1, 10].

The thermal conductivity of Al_2O_3 is much higher than Bi_2Te_3 and Sb_2Te_3 . Both Bi_2Te_3 and Sb_2Te_3 films are comparatively thin (<10 µm compared to the ~100 µm thick Al_2O_3 substrate). Thus we can assume that the Al_2O_3 substrate will dominate the thermal conduction process [1].

Figures 4.6 (a,b) show typical voltage measurements across the fuel/Sb₂Te₃/Al₂O₃ and the fuel/ Bi_2Te_3/Al_2O_3 systems, respectively. The voltage profiles of Figures 4.6 (a,b) can be divided into an initial reaction phase followed by a cooling down phase. The reaction phase consists of a rising voltage and continues until all the combustion fuel is consumed. This is followed by a region of exponential decay [11]. The voltage generated depends on the sample mass, especially the amount of fuel used (which is a combination of nitrocellulose and sodium azide). Sb₂Te₃-based devices generated voltages as large as 200 mV with oscillations in the range of 10-40 mV. On the other hand, Bi₂Te₃ devices generated voltages as large as 140 mV with larger oscillations generally within the range of 40-140 mV. The Bi₂Te₃-based devices occasionally showed voltages as high as 300-400 mV; however, due to lack of consistency these results are not included. Figures 4.6 (a,b) also show the difference in the oscillation amplitudes of the Sb₂Te₃ and Bi_2Te_3 devices. The reason for the difference in oscillatory behaviour can be attributed to the larger thermal conductivity of Sb₂Te₃ (2.5 times that of Bi₂Te₃). Oscillation amplitude difference between the two devices corresponds to the difference in thermal conductivities of the two materials. A larger effective thermal conductivity means that the reaction will propagate faster, potentially affecting the oscillation amplitude. Previously, we have theoretically demonstrated that a change in thermal conductivity affects the rate of heat loss and hence the oscillations [1].

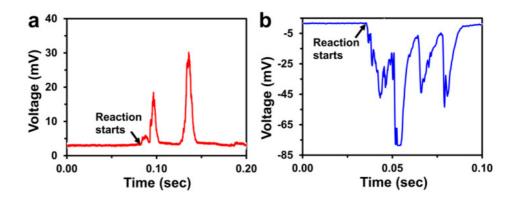


Figure 4.6: Comparison of oscillations between Sb₂Te₃ and Bi₂Te₃ based thermopower devices. (a) Oscillatory thermopower voltage signal for Sb₂Te₃ device using Al₂O₃ substrate.(b) Oscillatory thermopower voltage signal for Bi₂Te₃ device using Al₂O₃ substrate. We can see that Bi₂Te₃ based devices exhibit amplitudes approximately 3 times larger than that of Sb₂Te₃ based devices. The difference is similar to the variation in the thermal conductivities of Bi₂Te₃ and Sb₂Te₃.

For simplification in our theoretical analysis, we started with a one-dimensional space model and transformed it to a non-dimensional system to predict the occurrence of oscillatory combustion linked to the heat losses. As a first step towards analysing the combustion, we applied the model presented by Mercer *et al.*[12] Assuming that the solid fuel combustion is exothermic, oxygen is supplied in excess, and governed by Arrhenius kinetics with volumetric heat loss and defining the non-dimensional temperature u to be:

$$u = \frac{RT}{E} \tag{1}$$

The non-dimensional equations for the conservation of heat and mass are:

$$\frac{\partial u}{\partial t} = \frac{\partial^2 u}{\partial x^2} + w e^{-1/u} - \ell(u - u_a)$$
(2)

$$\frac{\partial w}{\partial t} = -\beta w e^{-1/u} \tag{3}$$

in which T and w denote the temperature and concentration of the fuel, respectively, and

x and t are the defined space and time variables. We define as $\beta = \frac{Ec_p}{QR}$, a parameter

related to the properties of the fuel, and the non-dimensional volumetric heat transfer,

$$\ell = \frac{hSE}{VR\rho QA}$$
 where, $\frac{S}{V}$ is the surface-area-to-volume ratio of the fuel (/m) and and h is

the heat transfer coefficient from the fuel to the quiescent surroundings (J/s.m².K), ρ is the density of the fuel (kg/m³), c_p is the specific heat of the fuel (J/kg.K), Q is the heat of reaction (J/kg), A is the pre-exponential rate constant (/s), E is the activation energy (J/mol), R is the universal gas constant (8.314 J/mol.K). The heat transfer coefficient h is an estimate for all the losses in the averaged model that we have used. For the purpose of gaining an understanding of the process, we estimated the heat losses to the substrate and the environment and lumped them together in h. Heat is transferred from the fuel layer to the $(Bi_2Te_3 \text{ or } Sb_2Te_3)$ thermoelectric/substrate layer and to the surroundings. Depending on the value of system parameters, we can predict the oscillatory behaviour of the thermopower waves. The determination of all the necessary parameter values is the key to being able to apply the model to a real system. The solution of the model presented by Mercer *et al.* [12], assumes that the ambient temperature is absolute zero ($u_a=0$). Ambient temperatures are very small relative to the reaction temperature, and hence, this inference has little effect on the overall behaviour of the solutions to this model. For the fuel, the value of the parameters is as follows: S/V=1/240 / μ m, ρ = 1600 kg/m³, c_p =1596 J/kg.K, $Q = 4.75 \times 10^6 \text{ J/kg}, E = 1.26 \times 10^5 \text{ J/mol}, A = 10^5 \text{ /s and } h=2 \times 10^{-3} \text{ J/s.m}^2$.K. In all cases the β value is 5.09 for the nitrocellulose fuel layer. The oscillation period is directly related to β and ℓ . For β = 5.09, the critical heat loss value for the onset of oscillations can be estimated as being smaller than $\ell/\beta = 0.000035$ (Figure 4.7). The change in thermal conductivity affects the heat loss parameter. The higher thermal conductivity of Sb₂Te₃ compared to Bi₂Te₃ will enhance heat transfer (section 4.2.4). Hence, faster combustion velocities are predicted for Sb₂Te₃-based devices and that the system would be closer to the parameter values where oscillations in the combustion occur. However, as the model is based on a one-dimensional average over all the layers, the resultant changes predicted dramatic as observed are not as in the

experiments. Abrahamson *et al.* [11, 13] have employed a similar averaged onedimensional model. They have solved their model numerically (rather than use the asymptotic results that we have) with a set of estimated parameter values and found corresponding results to those reported in this work, albeit for carbon nanotube guided thermopower waves, which are on a smaller scale than our experiments.

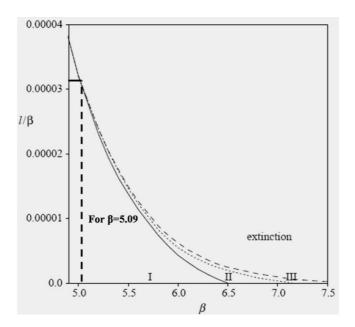


Figure 4.7: Region in the parameter (β , ℓ / β) space where combustion waves and extinction occurs.

The analysis of voltage and power as a function of mass shows an optimal mass range for both Sb₂Te₃ and Bi₂Te₃ based devices. A very low amount of fuel does not generate enough heat to sustain the propagation of the exothermic reaction. Too much fuel, on the other hand may provide more heat energy, but the unreacted accumulated fuel mass renders the reaction unsustainable [1]. As a result, we observed an optimal mass range (22-26 mg for ~75 mm² samples) that sustained the wavefront propagation. Almost both type devices exhibited well-matched trends in terms of the relation between voltage and mass (Figure 4.8 (a)). Comparison of peak power vs. mass for the two different materials is shown in Figure 4.8(b). The peak power was determined using the equation: $P = \frac{V^2}{R}$ in which P is the peak power in watts, V is the peak output voltage in volts and R the resistance in Ω .

The resistance of the Sb₂Te₃ films ranged from 6-12 Ω , while Bi₂Te₃ films resistances were between 2-10 Ω . The difference between the resistances can be attributed to the larger electrical conductivity of Bi₂Te₃ (section 4.2.5). Hence, we expect the power output from Bi₂Te₃-based devices to be higher. Experimental observations show that the peak power generated by Sb₂Te₃-based devices is ~6 mW, while Bi₂Te₃-based devices on an average generate 67% larger power with the peak value of ~10 mW. The resistance of the thermoelectric films remains almost the same even after the end of the reactions. The resistance dependence on temperature is defined by the following equation:

$$R(T) = R_o \left[1 + \alpha \left(T - T_o \right) \right] \tag{4}$$

where *T* is the temperature, T_0 is the reference temperature, R_o is the resistance at T_o and α is the temperature coefficient of resistivity of the material. Since, Sb₂Te₃ and Bi₂Te₃ are semiconductors they exhibit negative temperature coefficient of resistivity [14, 15]. Hence, it is expected that the resistance actually decreases during the reaction propagation in our case.

Additionally, the XRD pattern of the samples after the thermopower wave propagation, confirm that the structures of Sb₂Te₃ and Bi₂Te₃ remain unchanged (Figure 4.3 (a), 3 and Figure 4.3 (b), 3), as the peaks remain dominantly unaltered. The average wavefront propagation velocity for Sb₂Te₃-based devices was approximately 0.7 m/s compared to ~0.3 m/s average propagation velocity for Bi₂Te₃-based devices. Propagation velocities for Sb₂Te₃-based devices were generally 2-2.5 times higher than the velocity for Bi₂Te₃-based devices (Figure 4.8(c)), which nicely corresponds to the difference in the thermal conductivities of the two thermoelectric materials. A higher thermal conductivity of the

thermoelectric material provides an extra path for heat conduction (*i.e.* the surface of the Sb_2Te_3 film) in addition to the path provided by the thermally conductive Al_2O_3 substrate. This will consequently cause the wave to travel faster on Sb_2Te_3 , as the thermal wave generated from the exothermic reaction travels approximately 2.5 times faster than on Bi_2Te_3 (section 4.2.4).

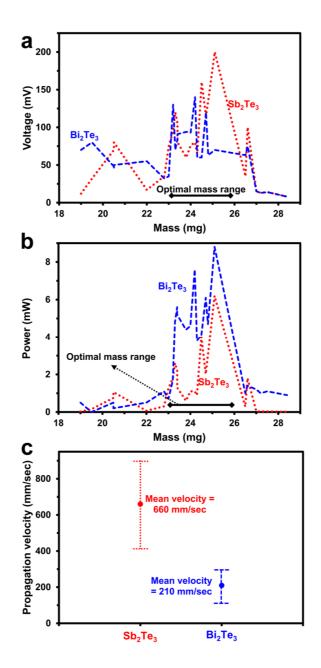


Figure 4.8: (a) Comparison of voltage generated as a function of mass (of fuel and thermoelectric material) for Sb_2Te_3 and Bi_2Te_3 based thermopower devices. (b) Power as a function of mass. (c) Comparison of the reaction propagation velocity for Sb_2Te_3 and Bi_2Te_3 based devices.

4.3.1.2 Thermopower devices based on terracotta substrate

The oscillatory behaviour and wave front velocities strongly depend on the thermal conductivity of the substrate. Terracotta has an identical thermal conductivity to Bi_2Te_3 . However, thermal conductivity of Sb_2Te_3 is 2.5 times higher. Consequently, we expect the rate of heat conduction for Sb_2Te_3 -based devices to be approximately 2.5 times faster than Bi_2Te_3 -based thermopower devices (section 4.2.4).

Figures 4.9 (a,b) show the voltage signals obtained for Sb_2Te_3 /terracotta and Bi_2Te_3 /terracotta systems, respectively. In line with our expectation, we can see that the reaction propagation for the Sb_2Te_3 /terracotta device is ~3 times faster than the Bi_2Te_3 /terracotta device. This endorses our explanation that the reaction propagation velocity depends on the thermal conductivity of the material (see section 4.2.4). The voltages generated by both devices are comparatively low. The reason is that a high thermal conductivity is essential for a sustained thermopower wave propagation and to maintain a high reaction temperature [1].

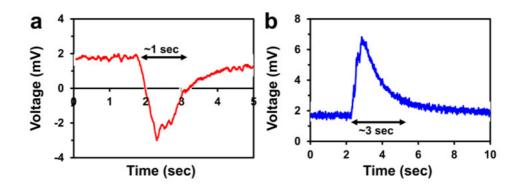


Figure 4.9: Comparison of thermopower voltage signals on terracotta substrates for: (a) Sb_2Te_3 films, (b) Bi_2Te_3 films.

4.4 Summary

In this chapter, the author demonstrated a thermopower wave system based on a novel combination of two complementary thermoelectric materials; p-type Sb_2Te_3 and n-type Bi_2Te_3 . A highly thermally conductive substrate of Al_2O_3 accelerated the thermopower waves, which entrained free electrical carriers (holes in Sb_2Te_3 and electrons in Bi_2Te_3) to

produce oscillatory voltages with alternating polarities, while maintaining high specific powers (0.6 kW/kg and 1 kW/kg for Sb_2Te_3 and Bi_2Te_3 based devices respectively).

A full analysis of the system was conducted and it was observed that the thermally conductive substrate of alumina resulted in oscillatory output signals , while there were no oscillations seen when terracotta substrates with a low thermal conductivity were used. This behaviour was also described by developing a theoretical model using the heat transfer equations with suitable boundary conditions. Furthermore, it was observed that the amount of fuel exhibited an optimal mass range in which the output voltages were maximised. A detailed comparison of Sb₂Te₃ and Bi₂Te₃ based thermopower wave systems revealed that devices based on Bi₂Te₃ generated higher specific powers (~67%) mainly owing to the larger electrical conductivity of Bi₂Te₃. It was also shown that the Sb₂Te₃ and Bi₂Te₃ films survived the thermopower wave reaction largely intact.

This work conducted by the author is extremely important as it demonstrates thermopower wave propagation using a p-type (hole dominant electrical conduction) core TE material for the first time. It also shows that output voltage signals with alternating polarities could be obtained using a combination of p and n-type core TE materials. This is an important milestone towards making practically useful thermopower wave systems.

However, in order to establish thermopower wave sources as a viable energy generation technology, even larger output voltages and oscillation amplitudes than demonstrated in this work are required, while maintaining a high specific power. As a result, the author conducted a comprehensive study on the TE properties of transition metal oxides (TMOs) as presented in chapter 2. Based on the analysis, ZnO, which is a TE TMO was identified as an outstanding potential core TE material due to its high Seebeck coefficient, electrical conductivity and moderate thermal conductivity at elevated temperatures.

In the next chapter, the author will demonstrate thermopower wave systems by incorporating thin films of ZnO as the core TE material for the first time.

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Chapter 5

ZnO based Thermopower Wave Sources

5.1 Introduction

In the previous chapter, the author demonstrated thermopower wave systems based on a novel combination of two conventional thermoelectric (TE) materials with complementary semiconducting properties (p-type Sb₂Te₃ and n-type Bi₂Te₃). Oscillatory voltages with alternating polarities were obtained while maintaining a high specific power of at least 0.6 kW/kg. However, there are still some fundamental deficiencies regarding thermopower wave systems based on Bi₂Te₃ and Sb₂Te₃. The maximum voltages obtained were in the order of only 200 mV. To make such systems practically applicable, larger output voltages while maintaining high specific powers are desired. Additionally, materials such as Bi₂Te₃ and Sb₂Te₃ pose a health hazard and are rare earth. As a result, the author decided to search for alternatives. In chapter 2, the author showed that transition metal oxides (TMOs) can potentially solve these problems. They are generally non-toxic, naturally abundant and a wealth of information about their synthesis is available. Furthermore, some of them can offer a high Seebeck coefficient (*S*) and electrical conductivity (σ) as well as moderate thermal conductivity (κ) simultaneously.

As presented in chapter 2, ZnO which is a n-type semiconducting transition metal oxide (TMO) is an outstanding candidate as the core TE material for thermopower based energy sources as it exhibits a high Seebeck coefficient which increases with temperature, a high electrical conductivity at elevated temperatures, moderate thermal conductivity and good chemical stability, all of which are highly desirable features.

In this chapter, the author will incorporate thin films of ZnO, a common TE TMO as the core material in thermopower wave sources. Exothermic chemical reactions from a reactive fuel (nitrocellulose) will be coupled to charge carriers in the ZnO film to generate voltage and power. In order to gain a complete understanding of the system, the author will conduct a full analysis by characterizing the ZnO films before and after the thermopower wave reaction. The thermopower wave propagation velocities will also be assessed with respect to the thermal conductivity of the core TE material. The outcome of this work was published as a communication in the journal Chemical Communications.

5.2 Experimental

5.2.1 Deposition of ZnO films

The ZnO films were deposited using RF magnetron sputtering. High purity (99%) ZnO sputtering target (Vin Karola Instruments) was used in the process. The sputtering process was started after the chamber was pumped down to 2×10^{-5} torr. Previous works carried out on RF sputtered ZnO films shows that their resistivity can vary up to 8 orders of magnitude depending on the sputtering power and the substrate temperature [1-3]. Consequently, in this work the author used a high sputtering power (160 W) and no substrate heating in order to synthesise crystalline and electrically conductive ZnO thin films (~1.2 μ m). The sputtering process was carried out under an atmosphere of 100% Argon (Ar). Al_2O_3 substrates were used after being adequately cleaned using acetone, isopropanol and distilled water successively, and dried using a high pressure nitrogen gun. Adhesive conductive silver (Ag) paste (42469, Alfa Aesar) was used to make electrical contacts between the copper tape electrodes and the ZnO samples. Nitrocellulose $[C_6H_8(NO_2)_2O_5]$ was used as the fuel, due to its large enthalpy of reaction $(4.75 \times 10^6 \text{ J kg}^{-1})$ [4]. Sodium azide (NaN₃) in aqueous solution (50 mg/mL) was then added to serve as a primary igniter to lower activation energy (40 kJ/mol for NaN₃, compared to 110–150 kJ/mol for nitrocellulose. Nitrocellulose $[C_6H_8 (NO_2)_2O_5]$ was used as the fuel due to its large enthalpy of reaction. Nitrocellulose was prepared by

dissolving millipore nitrocellulose membranes (N8645, Sigma Aldrich) in acetonitrile (15g/L). This solution was drop-cast onto the ZnO film and dried at 50° C. The acetonitrile evaporated, leaving a layer of adhesive nitrocellulose coating. Sodium azide (NaN₃) (14314, Alfa Aesar) in aqueous solution (50mg/mL) was then added on top of the nitrocellulose layer using a pipette to serve as a primary igniter.

5.2.2 SEM and AFM analysis of the ZnO film surface

Scanning electron microscopy (SEM) was conducted using the FEI Nova Nano SEM to investigate the structure of the ZnO films. The SEM image (Figure 5.1(a)) shows that the ZnO film is composed of crystals of varying sizes (250 nm to 1 μ m).

Atomic force microscopy (AFM) was carried out on the ZnO films using a AFM-Bruker D3100 in order to assess their surface roughness. The ZnO films exhibit a root mean squared roughness of ~250 nm indicating strong porous nature of the films. A higher porosity is important for an increased thermal conduction between the fuel layer and the ZnO surface thereby resulting in a more sustained reaction propagation. Figure 5.1 (b,c) shows the 2D and 3D profiles of the ZnO film surface sample, respectively.

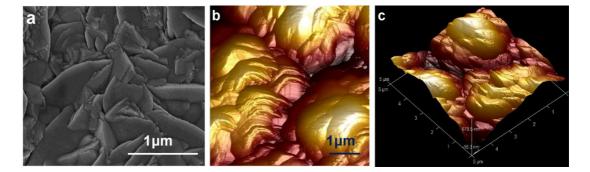


Figure 5.1: (a) SEM micrograph of ZnO film, (b) 2D AFM image of the ZnO film surface (b) 3D AFM profile of the ZnO film surface.

5.2.3 Effect of annealing on the ZnO thin film

The author has previously shown that in a thin film thermopower system configuration, incorporating nitrocellulose as the fuel, the reaction temperature remains under 300 °C (chapters 2 & 3).To emulate the effect of surface heating on ZnO film during the

thermopower propagation reaction, a ZnO/Al₂O₃ sample was annealed at 300 °C for 1 min in a vacuum furnace. Its thermal conduction behaviour was compared with the non-annealed sample. Additionally, its crystal structure was also examined after annealing. In order to make the thermal conductivity comparison, one end of the sample with ZnO film was rested on a heater at 40 °C and the temperature was recorded at the opposite end. Figure 5.2 shows the results after 150 seconds of measurements. The slope of the rise in temperature with time highlights the rate at which heat is transferred from one end to the other. The slope of the temperature rise was calculated to be 0.28 °C /s before annealing while it decreased slightly to 0.22 °C/s after annealing. This directly translates into less than 25% decrease in thermal conductivity. As a result, the thermal conductivity shows a small reduction in value after annealing.

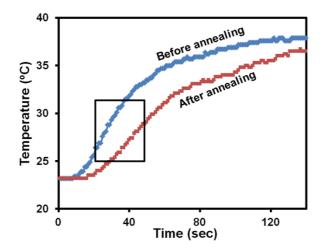


Figure 5.2: Change in thermal conduction of the ZnO films before and after annealing at 300 °C.

Figure 5.3 (a, b) show the Raman spectra and XRD patterns of the ZnO films before and after annealing, respectively. The Raman spectra were recorded with a system incorporating an Ocean Optics QE 6500 spectrometer, and a 532 nm 40 mW laser as the excitation source. XRD was carried out using a Bruker D8 DISCOVER microdiffractometer fitted with a GADDS (General Area Detector Diffraction System). Data was collected at room temperature using CuK α radiation ($\lambda = 1.54178$ Å) with a potential of 40 kV and a current of 20 mA, and filtered with a graphite monochromator

in the parallel mode (175 mm collimator with 0.5 mm pinholes).

The XRD shows that the relative intensity of the dominant (002) to the (101) peak increases slightly (approximately 7%) after annealing [5]. This indicates the *c* axis directional orientation of the ZnO enhanced marginally after annealing. Additionally, the Raman spectra also does not identify any significant change as a result of annealing. This shows that the ZnO films are expected to be stable after the thermopower wave reaction.

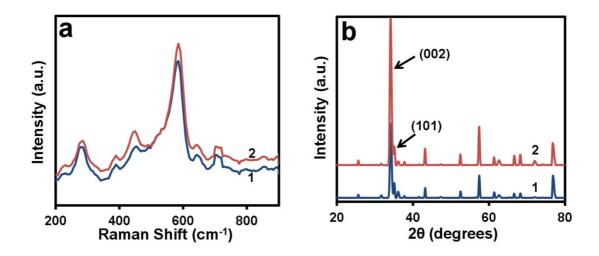


Figure 5.3: (a) Raman peaks of ZnO films 1. before and 2. after thermal annealing at 300 °C, (b) XRD pattern of 1.ZnO film before and 2. after annealing.

5.2.4 Calculation of specific power

In order to obtain the specific power, the masses of the fuel (nitrocellulose & sodium azide) and thermoelectric films were considered. The relationship between mass, density and volume was used for calculating the mass of the ZnO films as: $m = \rho \times V$, where, m is the mass in grams (g), ρ is the density in g/cm³ and V is the volume in cm³.

 ρ =5.6 g/cm³ for ZnO and V depends on the dimensions of the sample and is calculated using the formula, $V = l \times w \times h$ where l is the length, w is the width and h is the thickness of the thermoelectric film in cm, respectively. For fuels, nitrocellulose and NaN₃ in our case, we knew the concentration of the two in their respective solutions. As mentioned in the main manuscript, 15g/L nitrocellulose and 20g/L NaN₃ were used by drop casting. Hence, we know the amount of solution for each fuel and therefore the corresponding mass for each sample, depending on the volume of the liquid placed on the thermoelectric films. The sum of the masses of the thermoelectric film and the fuels gives the total mass of the materials used. The corresponding power from the sample is

obtained using the equation: $P = \frac{V^2}{R}$ in which P is the peak power in watts, V is the peak output voltage in volts and R the resistance in Ω . The output power is then scaled to per kg of the materials to obtain the specific power of the sample in kW/kg.

5.3 Results and Discussion

5.3.1 Output voltage and power

A schematic of the fuel/ ZnO/Al_2O_3 is shown in Figure 5.4.

Ignition was initiated at one end using a blow torch with a fine tip resulting in selfpropagating reaction waves that travels at a rapid pace to the opposite end. This accelerated reaction wave entrains a simultaneous wave of electrical carriers resulting in an oscillatory voltage output.

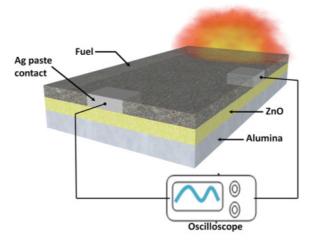


Figure 5.4: Schematic of a fuel/ZnO/Al₂O₃ thermopower wave generation system (not to scale). The optical photos of the samples before and after the reaction are shown in Figure 5.5 (a). A typical thermopower voltage signal obtained across a sample of the fuel/

 ZnO/Al_2O_3 system is shown in Figure 5.5 (b). The voltage profile exhibits two distinct regions: an initial phase during the wave propagation and a cooling down phase until the temperature across the ZnO film reaches equilibrium. The initial reaction phase is a region of rising voltage as the wavefront spreads across the sample until all the combustion fuel is consumed. This is followed by a region of exponential decay. The moving temperature gradient results in voltages with peak magnitudes of up to 500 mV and oscillations with peak-to-peak amplitude of up to 400 mV. The power and specific power obtained from these devices can be as large as 1 mW and 0.5 kW/kg respectively. The author previously (chapter 2 & 3) adapted the theory of combustion waves to describe coupled thermal waves in fuel/Bi₂Te₃/Al₂O₃ and fuel/Sb₂Te₃/Al₂O₃ systems [6, 7]. Using the model presented by Mercer *et al.* and McIntosh *et al.* the author was able to predict the oscillatory behaviour and the propagation velocity of the thermopower waves [8, 9]. The theoretical analysis concluded that the oscillatory behaviour and wave front velocities strongly depend on the thermal conductivity. A change in thermal conductivity affects the heat loss parameters of the system. It was demonstrated that a higher thermal conductivity enhances the heat transfer through the thermoelectric core, resulting in a proportional increase in combustion velocities. Consequently, Sb₂Te₃ based systems exhibited combustion velocities that were almost 2.5 times faster than the Bi₂Te₃ based devices reflecting the difference in the thermal conductivities of the two materials [7]. Hence, based on the aforementioned analysis it is expected that a higher thermal conductivity of ZnO (~15.0 W/m.K) compared to Bi2Te3 (1.0 W/m.K) and Sb2Te3

(2.5 W W/m.K) would result in a faster wave velocity and larger oscillations. The author assessed the velocity of the waves in this system by using the duration in which the output voltage exists. As demonstrated previously by the author, the duration of the voltage signal corresponds to the reaction wave propagation time which enables the calculation of the linear propagation velocity of the thermopower waves [6, 7]. A high thermal conductivity of the ZnO thermoelectric material provides an extra path for heat conduction (i.e. the surface of the ZnO film) in addition to the path provided by the

thermally conductive Al_2O_3 substrate. As a result, it was expected that the rate of heat conduction for ZnO-based devices would be approximately 15 times faster than Bi_2Te_3 based thermopower devices. Propagation velocities for the ZnO based devices were measured to range between 12–35 m/sec (Figure 5.5 (c)) which was generally 15–25 times higher than the velocities for Sb_2Te_3 (1.2 m/sec) and Bi_2Te_3 (0.4 m/sec) based devices demonstrated in the author's previous work (chapter 3 and 4) [6, 7]. This difference nicely corresponds to the variation in the thermal conductivities of these materials and is in excellent agreement with theoretical expectations.

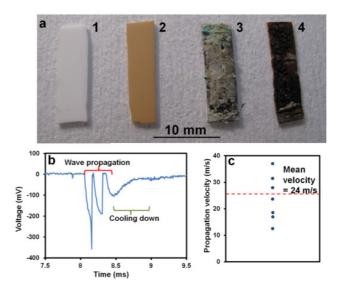


Figure 5.5: (a) Photo of the 1. Al_2O_3 substrate, 2. ZnO deposited on Al_2O_3 substrate, 3. fuel/ZnO/Al_2O_3 sample and 4. Sample after thermopower wave propagation. (b) Oscillatory thermopower voltage signal obtained using the fuel/ZnO/Al_2O_3 device. (c) Reaction propagation velocities for the fuel/ZnO/Al_2O_3 thermopower systems.

5.3.2 Seebeck coefficient and resistance profiles

The author has already shown that in a thin film thermopower system configuration, incorporating nitrocellulose as the fuel, the reaction temperature remains under 300 °C (chapters 2 & 3) [6, 7]. As a result, an estimation of the Seebeck coefficient and resistance of the ZnO films was required within this range to understand the behaviour of the ZnO based thermopower devices.

The experimental set up to measure the Seebeck coefficient is shown in Figure 5.6 (a). The temperature difference was attained using two Peltier modules. The sample was placed such

that one edge rested on the hot side of one Peltier module while the other edge rested on the cold side of the other module. Micromanipulator probes were then used to measure the voltage generated as a result of the temperature difference. An infrared camera (FLIR Systems, Thermo Vision A320, Sweden) with a lateral resolution of ~ 600 μ m was interfaced with ThermaCAM Researcher software to accurately measure the temperature at the two ends of the sample. The temperature gradient between the two ends of the sample was in the range of 10-20 °C. Measurements were made up to a temperature of 350 °C with an uncertainty of ± 2%. The uncertainty in the measured Seebeck coefficient values is < ± 5%. A hot plate was used to elevate the temperature of the sample to the required level whereas the Peltier modules were used to create a temperature difference.

Kim *et al.* have shown that the Seebeck coefficient of ZnO increases with temperature. In their work, it has been demonstrated that the Seebeck coefficient of ZnO is approximately $-300 \,\mu$ V/K at 85 °C [10]. In the author's measurements the Seebeck coefficient of the ZnO films was measured to be approximately $-360 \,\mu$ V/K. (Figure 5.6 (b)) At 300 °C the Seebeck coefficient is expected to be approximately $-500 \,\mu$ V/K based on linear extrapolation (Figure 5.6 (b)) [10]. Figure 5.6 (b) also shows a comparison of the measured Seebeck coefficient at different temperatures with the literature values. The Seebeck coefficient obtained at 85 °C was approximately $-360 \,\mu$ V/K. It shows that the measurement values are comparable to those obtained by Kim *et al.*[10] The increase in *S* (Δ V/ Δ T) was observed to be non-linear with Δ V/ Δ T tending to increase at higher temperatures. A detailed explanation of such temperature dependant behaviour of *S* has been provided on Pg. 162 of the thesis.

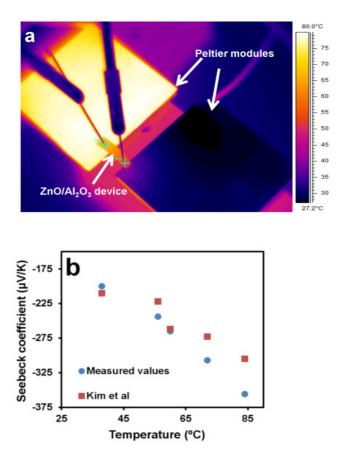


Figure 5.6: (a) Measurement set up used to calculate the Seebeck coefficient. The above image has been obtained using an infrared camera , (b) Measured and literature values of the Seebeck coefficient at different temperatures.

It has been reported that ZnO exhibits a negative temperature coefficient of resistance at temperatures up to 350 °C [11, 12]. The author measured ZnO film resistance at temperatures of up to 300 °C as shown in Figure 5.7, which is in close agreement with the value of the temperature coefficient of resistance suggested in the work of Caillaud *et al.* (approximately -3.5×10^{-3} /°C) [12]. At 300 °C the resistance was reduced to approximately 250 Ω . This is not an ideal internal impedance for a power source, however it resulted in the maximum current of the order of 2 mA in a short circuit load condition.

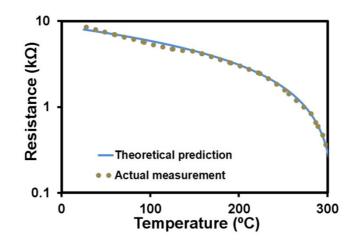


Figure 5.7: Change of resistance of ZnO film with temperature.

5.3.3 ZnO film structure before and after thermopower wave propagation

Figure 5.8(a), 1 illustrates the Raman spectra (indicated as '1') of the as-grown ZnO structure. The peaks observed at around 436 and 576 cm⁻¹ correspond to the E_2 (high) and the dominant A_1 (LO) modes, respectively. The E_2 (high) is a characteristic mode of the ZnO hexagonal wurtzite type lattice [13]. In a wurtzite ZnO crystal there are 4 atoms per unit cell and a total of 12 phonon modes. These include one longitudinal-acoustic (LA), two transverse-acoustic (TA), three longitudinal-optical (LO) and six transverse-optical (TO) branches. The A_1 and E_1 branches are both Raman and infrared active while the two non-polar E_2 branches are Raman active only. For lattice vibrations with A_1 symmetries the atoms move parallel to the *c* axis while the high frequency E_2 mode involves the vibrations of the oxygen atoms. If the incident light is normal to the surface and only, A_1 (LO) and E_2 modes are observed, it implies that the film is highly oriented. The E_2 (high) is a characteristic mode of the ZnO hexagonal wurtzite type lattice [13].

The Raman peaks after the deposition of nitrocellulose (spectrum '2' in Figure 5.8 (a)) shows the presence of strong C–H and NO₂ bonds [14]. After the thermopower wave propagation the C–H and NO₂ bonds disappear, while carbon peaks appear on the Raman spectra (spectrum '3' in Figure 5.8 (a)). The exothermic reaction causes the C–H bonds

to decompose, while carbon is left behind as the residual product.

The X-ray diffraction (XRD) pattern Figure 5.8 (b) reveals that the ZnO films are highly crystalline with a strong *c*-directional (002) preferred orientation. Addition of nitrocellulose results in an acute reduction in intensity of the $25.3^{\circ} 2\theta \text{ Al}_2\text{O}_3$ substrate peak. This is because the $25.3^{\circ} 2\theta \text{ Al}_2\text{O}_3$ substrate peak lies in the same region as the principal XRD reflections for nitrocellulose (ICDD No. 03-0114). A general decrease in diffrraction intensity due to the nitrocellulose coating inhibiting X-ray peneration is observed [7]. The XRD pattern following thermopower wave propagation shows strong ZnO peaks (Figure 5.8 (b)) verifying that ZnO remained largely intact at the end of the process.

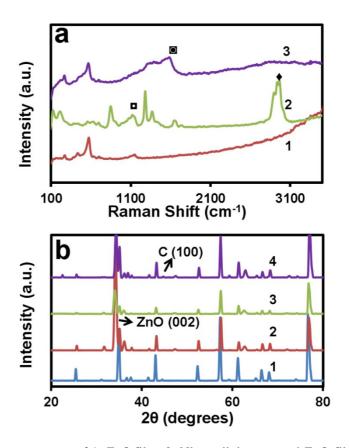


Figure 5.8: (a) Raman spectra of 1. ZnO film, 2. Nitrocellulose coated ZnO film (\square peak denotes strong NO₂ bonds, \blacklozenge denotes strong C-H bonds), 3. After the reaction (\square peak denotes carbon), (b) XRD pattern of 1. Al₂O₃ substrate, 2. ZnO before thermopower wave propagation, 3. after adding nitrocellulose and 4. after thermopower wave propagation.

5.4 Summary

In this chapter, the author demonstrated thermopower wave sources based on ZnO, a TE TMO for the first time. It was shown that the incorporation of ZnO as the core TE material resulted in oscillatory output voltages as large as 500 mV, which was at least 200 % larger than previously demonstrated thermopower wave sources based on MWNTs, Bi₂Te₃ and Sb₂Te₃. At the same time a high specific power in the order of 0.5 kW/kg was maintained. The generation of large voltages was due to the high *S* of ZnO at elevated temperatures (-500μ V/K at 300 °C). At the same time the resistance of the ZnO films also dropped with increasing temperature (from ~8 kΩ at room temperature to 250 Ω at 300 °C).

A full analysis of the system was also carried out by characterizing the ZnO films before and after the thermopower wave propagation. It was shown that the ZnO films survived the thermopower wave propagation largely intact.

This work conducted by the author is of utmost importance as it is the first thermopower wave system based on a TMO. By demonstrating the generation of high amplitude alternating voltages (up to 500 mV), this work conducted by the author shows significantly larger voltages and oscillations than previously demonstrated thermopower wave systems. This work also highlights that the incorporation of TMOs in thermopower wave sources will potentially allow their application as a new class of micro-power sources.

After the development of ZnO based thermopower wave sources, the author reviewed other TE TMOs in an effort to identify materials that can result in increasing the output voltages from thermopower wave sources even further. Based on the analysis, MnO_2 appeared to be an outstanding candidate as a core TE material, as it exhibited an extremely high Seebeck coefficient and moderate electrical conductivity at elevated temperatures. In the next chapter, the author will demonstrate thermopower wave sources based on thin films of TE MnO_2 to

show the generation of voltages higher than any thermopower wave system demonstrated previously.

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Chapter 6

MnO₂ based Thermopower Wave Sources with Exceptionally large Output Voltages

6.1 Introduction

In the previous chapter, the author of this thesis demonstrated thermopower wave sources by incorporating thin film thermoelectric (TE) cores of ZnO, which is a transition metal oxide (TMO), for the first time. The implementation of a TE TMO turned out to be a great approach and output voltages (as large as ~500 mV) and oscillatory amplitudes that were at least 200% higher than previously reported thermopower wave systems based on MWNT, Bi₂Te₃ and Sb₂Te₃ were obtained, while maintaining a high specific power in the order of 0.5 kW/kg. It was also shown that the Seebeck coefficient (S) and the electrical conductivity (σ) of the ZnO films increased with temperature underlining its suitability as a core TE material for thermopower wave sources. However, in order to establish thermopower wave sources as a viable energy generation technology, voltages more than 1.2 V, exceeding those of small batteries, are desirable. The results obtained by incorporating ZnO as the core TE material demonstrated the potential of employing TE TMOs in thermopower wave sources. Subsequently, the author comprehensively investigated TMOs other than ZnO and selected manganese dioxide (MnO₂) as the potential candidate. As presented in chapter 2, MnO₂ exhibits an exceptionally high Seebeck coefficient. MnO_2 is also an n-type semiconductor with an electrical conductivity that increases at elevated temperatures, thereby resulting in a high thermoelectric power factor (TPF-' $S^2\sigma$ '). A high TPF is vital to increase the output voltage and power from thermopower wave sources and the choice of MnO₂ as the core TE material was based on this highly desirable characteristic of MnO₂.

In this chapter, the author will demonstrate thermopower wave sources based on thin films of TE MnO_2 , as the core material. Exothermic chemical reactions from a solid fuel (nitrocellulose) will be coupled to charge carriers of the MnO_2 layers to generate voltage and power. The author will also present a full analysis of the system by characterizing the Seebeck coefficient and the electrical resistivity of the MnO_2 based thermopower wave devices before and after the thermopower wave reaction. The influence of the thermal conductivity of the core TE material on the reaction propagation velocities will be assessed and a comparison with previously demonstrated thin film thermopower wave sources will be carried out. The work in this chapter was published as a full article in the Journal of Physical Chemistry C.

6.2 Experimental details

6.2.1 Synthesis of MnO₂ thin films

MnO₂ films were prepared using ball-milled MnO₂ powder (42250, Alfa Aesar). The MnO₂ powder was ball-milled for 20 h at 500 rpm with a ball-to-powder mass ratio of 10:1 in order to reduce the size of the crystals. This MnO₂ nanopowder was then mixed with acetone (25 mg/mL) and the solution was subsequently drop-casted on to alumina substrates and dried in ambient conditions. Alumina with a thickness of ~100 μ m was used as the substrate as it exhibits high thermal conductivity and can assist in the propagation of the thermopower waves [1-3]. The as fabricated samples were then annealed in air at 400 °C for 4 h in a MTI V1200X furnace to improve the crystallinity, adhesion and consequently the electrical conductivity of the films. Scanning electron microscopy (SEM) was conducted using the FEI Nova Nano SEM to investigate the structure of the MnO₂ films. Figure 6.1 (a, b) shows the SEM images of the MnO₂ surface before and after the annealing process.

Annealing results in an improvement in the crystallization state of the film by lowering the number of grain boundary barriers, thereby facilitating the mobility of charge carriers resulting in a reduced resistivity [4].

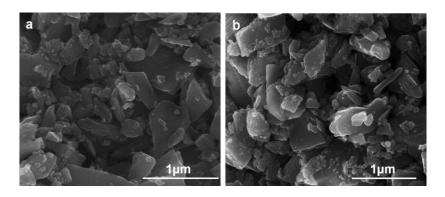


Figure 6.1: SEM images of the MnO₂ film surfaces: (a) before annealing and (b) after annealing.

6.2.2 Effect of ball-milling

SEM micrographs (Figure 6.2 (a,b)) show that the as-purchased powder is composed of crystals of dimensions in the order of 4-6 μ m. Ball milling was used to increase the surface-to-volume ratio (thereby increasing the possibility of the phonon exchange between the fuel and MnO₂). Following ball milling the MnO₂ powder comprised of crystals ranging from 400-700 nm in size, as suggested by Song *et al.* [6] The SEM micrographs also illustrate the highly porous nature of the films. BET analysis of the MnO₂ films (carried out using an ASAP 2000 Surface Area Analyser) revealed an average pore diameter of ~ 12 nm further confirming the porous nature of the MnO₂ films.

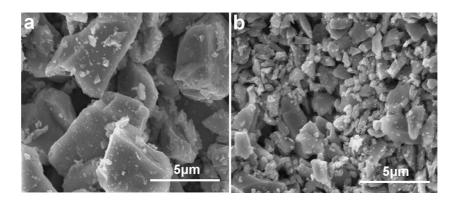


Figure 6.2: SEM micrograph of the (a) MnO₂ film before ball milling, (b) after ball milling. However, no enhancement in Seebeck coefficients was observed as a result of ball-milling

which was in contrast with the claim made by Song *et al.* [6] (Figure 6.3). Figure 6.3 shows that the Seebeck coefficient values for the MnO_2 films synthesised using ball-milled and non ball-milled powder were quite similar. The experimental set-up used to measure the Seebeck coefficient was identical to the one described in section 5.3.2 of chapter 5.

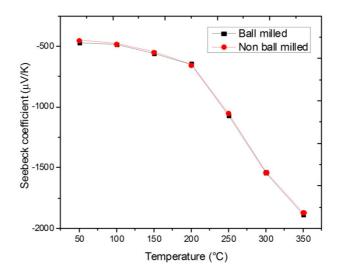


Figure 6.3: Seebeck coefficient vs temperature for MnO_2 films synthesised using ball-milled and nonball milled MnO_2 powder.

6.2.3 Preparation of the fuel

Nitrocellulose $[C_6H_8(NO_2)_2O_5]$ was used as the fuel, due to its large enthalpy of reaction $(4.75 \times 10^6 \text{ J/kg})$. Sodium azide (NaN_3) in aqueous solution (50 mg/mL) was then added to serve as a primary ignition source to lower activation energy $(40 \text{ kJ/mol for NaN}_3, \text{ compared to } 110-150 \text{ kJ/mol for nitrocellulose})$.

6.2.4 Device schematic and voltage measurement set up

A pictorial representation of a MnO_2 based thermopower wave device is shown in Figure 6.4 (a). Electrical contacts between the copper tape electrodes and the TE layer were made using an adhesive conductive silver paste (42469, Alfa Aesar). The MnO_2 films (2-2.5 µm thick) were subsequently coated with ~ 220-260 µm thick solid fuel layer (nitrocellulose & sodium azide in this case) and integrated with electrodes to complete the system.

An Agilent MSO7014 oscilloscope (set at an input impedance of 1 M Ω) was used for acquiring the output voltage signals from the thermopower wave devices. A load resistance of 1 k Ω was also added in parallel to the input of the oscilloscope in order to ensure that power is generated. A schematic of the measurement set up is shown in Figure 6.4 (b).

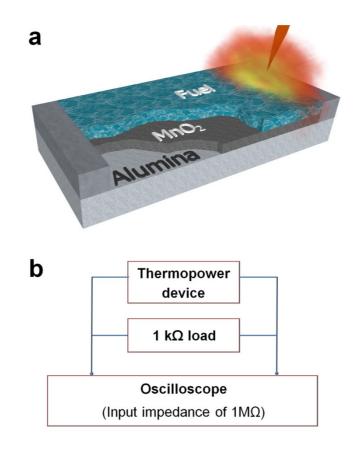


Figure 6.4: Schematic of (a) a thermopower wave generation device (not to scale) and (b) the measurement set up for a fuel/ MnO_2/Al_2O_3 thermopower wave device.

6.2.5 Calculation of specific power

In order to obtain the specific power, the masses of the fuel (nitrocellulose & sodium azide) and thermoelectric films were considered. The relationship between mass, density and volume was used for calculating the mass of the MnO₂ films as: $m = \rho \times V$, where, m is the mass in grams (g), ρ is the density in g/cm³ and V is the volume in cm³.

For MnO₂, ρ =5.026 g/cm³ and V depends on the dimensions of the sample and is calculated using the formula $V = l \times w \times h$, where l is the length, w is the width and h is the thickness of the TE film in cm, respectively. For fuels, nitrocellulose and NaN₃, the concentration in their respective solutions is known. As mentioned in the experimental section, 15g/L nitrocellulose and 20g/L NaN₃ were used by drop casting. Hence, we know the amount of solution for each fuel and therefore the corresponding mass for each sample, depending on the volume of the liquid placed on the thermoelectric films. The sum of the masses of the thermoelectric film (~ 0.60 mg) and the fuels (~3.2 mg) gives the total mass of the materials used. The corresponding power from the sample is obtained using the equation: $P = \frac{V^2}{R}$, in which P is the peak power in watts, V is the peak output voltage in volts and R is the load resistance in Ω . The output power is then scaled to per kg of the materials to obtain the specific power of the sample in kW/kg.

6.3 Results and Discussion

6.3.1 Output voltage and power

A schematic of the fuel/ MnO_2/Al_2O_3 system is shown in Figure 6.4 (a). A fine tip blowtorch was employed to initiate the reaction at one end. This resulted in a self-propagating reaction wave that travels rapidly to the other end, simultaneously entraining electrical carriers along its path, resulting in an output signal. A typical thermopower voltage signal of the fuel/MnO₂/Al₂O₃ system is shown in Figure 6.5 (a). The voltage signal was positive for waves emanating from the negative electrode. This can be ascribed to the n-type semiconducting nature of MnO₂. Additionally, the polarity of the voltage signal depends on the direction of the thermopower wave propagation. The voltage profiles can be divided into two distinct regions (Figure 6.5 (a)). An initial phase during the thermopower wave propagation, which lasts until the combustion fuel is consumed followed by a decaying phase which is the cooling down region. During the initial phase the moving temperature gradient across the surface of MnO_2 results in a voltage output, while in the decay phase the voltage drops back to zero as the temperature reaches equilibrium with the room temperature environment. This thermal wave propagation results in peak voltages as large as $1.8 \text{ V} \pm 5\%$ and fluctuations of the order of 400 mV $\pm 5\%$ in the output voltage signal (Figure 6.5 (a)). A peak output power as large as $3.24 \text{ mW} \pm 10\%$ was also observed.

The specific power obtained from the MnO_2 -based thermopower wave devices was of the order of ~1.0 kW/kg ± 15%. Voltage and power outputs obtained from seven MnO_2 -based thermopower devices are shown in Figure 6.5 (b).

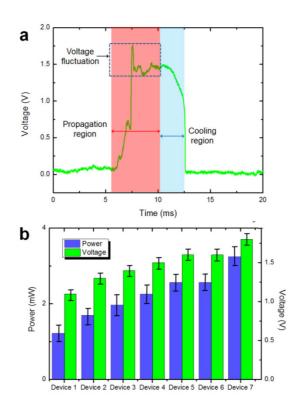


Figure 6.5: (a) A thermopower voltage signal obtained using the fuel/ MnO_2/Al_2O_3 device. (b) Power and voltage outputs obtained from the fuel/ MnO_2/Al_2O_3 thermopower devices.

The reaction temperature remains in the region of 300-400 °C similar to the author's previous experiments [1-3]. There is a large variation in the output voltage and consequently power. This is due to the chaotic nature of thermopower waves. This chaotic behaviour is an intrinsic part of the thermopower wave propagation front, which is described by the equations governing the system and have been discussed by the author in Chapters 1 and 2. This produces disordered changes in the temperature of the areas near the wavefronts. As both internal resistivity and Seebeck coefficient change with temperature (Figure 6.6), variation in the output values of thermopower wave devices is inherently large even for those devices with very similar fabrication parameters. As such, this chaotic behaviour can be observed in the output voltage profiles (Figure 6.5 (a)).

6.3.2 Resistivity and Seebeck coefficient profiles before and after the reaction

To understand the performance of the system, the resistivity and Seebeck coefficient of MnO_2 films were characterized as a function of temperature. These two parameters are sufficient to assess and predict the output of the system as the power, voltage and current generated are directly dependent on these two properties.

An accurate value of the resistance is required in order to calculate the output power from the devices as well as the internal resistivity of the source. The author measured the MnO₂ film resistance at temperatures as large as 300 °C. The resistivity profile of the MnO₂ films as a function of temperature is shown in Figure 6.6. From these results the thermal coefficient of resistance is estimated to be equal to -2.85×10^{-3} /°C, which is a negative value for the n-type MnO₂. At room temperature the resistivity of the film was 0.43 Ω .cm ± 8% which was reduced to 0.1 Ω .cm ± 8% at 300 °C. In order to evaluate the stability of the film, the resistivity profile was also obtained after the thermopower wave propagation (Figure 6.7 (a)). The resistivity profile after the reaction followed a similar trend as the one before the reaction. It can be seen that the resistivity of the film slightly increased after the reaction. Such an increase in resistivity is ascribed to a slight damage (the surface was chipped at a few locations) to the MnO₂ films. However, it proves that the MnO₂ films remain fairly stable after the thermopower wave propagation.

The Seebeck coefficient of the MnO₂ films was also measured for temperatures up to 350 °C (Figure 6.6). The room temperature Seebeck coefficient was measured to be $-460 \ \mu\text{V/K} \pm 5\%$. Interestingly, the Seebeck coefficient shows a significant increase in magnitude at elevated temperatures, attaining a value of $-1900 \ \mu\text{V/K} \pm 5\%$ at 350 °C. It is expected that the absolute value of Seebeck coefficient increases even further up to a temperature of approximately 500 °C, after which MnO₂ starts transforming into Mn₂O₃ [7]. The Seebeck coefficient profile of the film after the thermopower wave propagation was very similar to the one before the reaction (Figure 6.7 (b)).

The aforementioned measurements also followed the trend reported by Klose *et al.* and Khan *et al.* [8, 9] Furthermore, such behaviour explains the generation of such high output voltages in the MnO_2 based thermopower wave systems developed by the author.

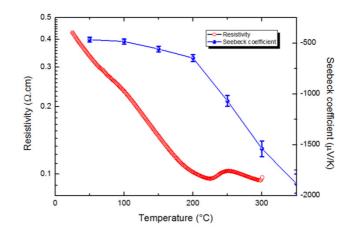


Figure 6.6: Changes of resistivity and Seebeck coefficient of the MnO₂ film with temperature.

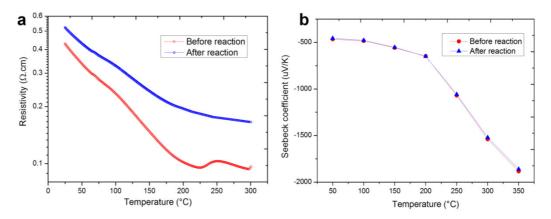


Figure 6.7: (a) Resistivity profiles of the MnO_2 films before and after thermopower wave propagation, (b) Seebeck coefficient profiles before and after thermopower wave propagation.

In order to explain the observation of enhanced Seebeck coefficient (*S*) with an increase in temperature, the following expression can be used to describe *S* for semiconducting materials (which is also a good approximation for several μ m thick films made of micro/nanostructured grains) [10]:

$$S = \frac{8m^*\pi^2 k_B^2}{3eh^2} T\left(\frac{\pi}{3n}\right)^{2/3}$$
(1)

where, *n* is the carrier concentration, m^* is the carrier effective mass, *e* is the electronic charge, *T* is the temperature, *h* is Planck's constant and k_B is the Boltzmann constant.

From Eq. 1, it is predicted that in general an increase in temperature linearly enhances S. Eq.1 also shows that a higher m^* results in larger Seebeck coefficients. Additionally, the equation shows that, any decrease in carrier concentration can also enhances S.

The author has previously shown that the Seebeck coefficient of ZnO rises significantly with increasing temperature [1]. The calculations demonstrate that room temperature carrier concentration of our ZnO film (considering a typical carrier mobility of ~1 cm²/V.s for ZnO thin films [11]) is ~10¹⁹ /cm³, while ZnO electron effective mass is relatively high (0.28) [12]. Obviously, the carrier concentration of ZnO increases with temperature due to the thermionic effect [13]. However, the influence of temperature on *S* is more dominant than the carrier concentration for temperatures smaller than 350 °C, after which *S* starts falling [14]. Hence, an overall enhancement of Seebeck coefficient is observed at the temperatures in which ZnO based thermopower wave systems operate.

The author proposes that the enhanced *S* at elevated temperatures for MnO₂ can also be similarly described. To date, there are no reliable studies regarding the effective mass of electrons in MnO₂ films. Although, the reported very low electron mobility for MnO₂ $(0.1 \text{ cm}^2/\text{V.s<})$ should be partially as a result of a relatively high electron effective mass [15]. In the MnO₂ films synthesised by the author, the carrier concentration is in the order of n = $\sim 10^{18}$ /cm³ for the upper limit of mobility of approximately 0.1 cm²/V.s (calculated from $n=\sigma/e\mu$ where μ is the mobility and σ is the electrical conductivity), which is an order of magnitude smaller than that of the ZnO film based thermopower wave system in our previous work [1]. As such for MnO₂, the effect of electron concentration should take effect and dominate at temperatures higher than 600 °C and the absolute value of its Seebeck coefficient should increase with temperature linearly up to those temperatures. Increase in Seebeck coefficients with temperature has been demonstrated in other transition metal oxides such as TiO_2 and WO_3 [16, 17], but such dramatically high values, which are observed for MnO_2 , have not been reported for those transition metal oxides at elevated temperatures.

6.3.3 XRD of MnO₂ films before and after the reaction

The author also observed that the MnO_2 films are very stable both before and after the reaction. XRD was carried out using a Bruker D8 DISCOVER microdiffractometer fitted with a GADDS (General Area Detector Diffraction System). Data was collected at room temperature using CuK α radiation ($\lambda = 1.54178$ Å) with a potential of 40 kV and a current of 20 mA, and filtered with a graphite monochromator in the parallel mode (175 mm collimator with 0.5 mm pinholes). The X-ray diffraction (XRD) patterns shown in Figure 6.8 reveal the presence of the signature MnO₂ peaks (ICCD 01-072-1984), showing that the films are highly crystalline and exhibit a rutile crystal structure [18]. The XRD pattern after the wave propagation (Figure 6.8) shows the principal MnO₂ peaks which proves that the MnO₂ films remain largely intact after the reaction. Additionally, the XRD peaks after the reaction do not show any presence of Mn₂O₃ suggesting that the reaction temperature remained under 500 °C.

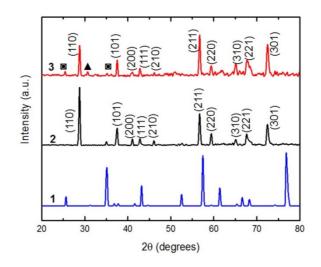


Figure 6.8: XRD pattern of 1. Al_2O_3 substrate , 2. MnO_2 before thermopower wave propagation, and 3. after thermopower wave propagation. The symbols **and** denote the XRD peaks of the Al_2O_3 substrate and sodium azide (NaN₃) respectively.

6.3.4 Comparison of thermal conduction rates and thermopower wave propagation velocities for different core TE materials

The author previously developed a model for the thermopower wave propagation by adapting the theory of combustion waves as described by McIntosh *et al.* and Mercer *et al.* [19, 20] This model demonstrated that the thermal conductivity of the core material affects the propagation velocity as well as the chaotic behaviour of the thermopower waves. Furthermore, it showed that a higher thermal conductivity facilitates the transfer of heat through the thermoelectric core, resulting in a proportional increase in combustion velocities [1-3]. The thermal conductivity of MnO₂ is 4.0 W/m.K compared to previously investigated core thermoelectric materials such as Bi₂Te₃ (1.0 W/m.K), Sb₂Te₃ (2.5 W/m.K) and ZnO (15.0 W/m.K) [21-26]. Based on the theoretical model, it is expected that the propagation velocity for the MnO₂ devices would be higher than Bi₂Te₃, Sb₂Te₃ and lower than ZnO based devices.

In order to experimentally demonstrate the difference between the thermal conduction behaviour of different thermoelectric core materials; Bi_2Te_3 , Sb_2Te_3 , MnO_2 and ZnO films on Al_2O_3 substrates with identical dimensions were heated using a micro heater at one end. Figure 6.9 (a) shows the measurement set up.

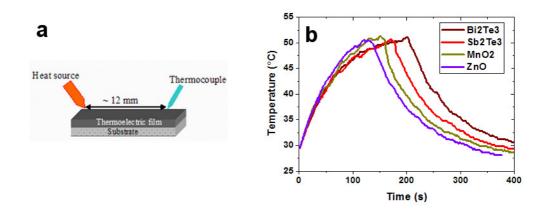


Figure 6.9: (a) Measurement set up to compare the thermal conduction rates of different thermoelectric films, (b) Difference between thermal conduction rates of Bi_2Te_3 , Sb_2Te_3 , MnO_2 and ZnO.

A heater with a sharp tip was used as the heating source and was positioned at one end on the sample. The temperature profile was acquired at the opposite end using a TENMA 727730

thermocouple. The heat source was withdrawn as soon as the temperature at the opposite end reached 50 °C. Figure 6.9 (b) shows the temperature profile for the samples. A faster approach to 50 °C indicates a higher rate of thermal conduction and therefore a higher thermal conductivity. Figure 6.9 (b) shows that Bi_2Te_3 sample takes 197 s to reach 50 °C while Sb_2Te_3 , MnO_2 and ZnO take 168, 150 and 126 s, respectively. Hence, it can be concluded that Bi_2Te_3 exhibits the lowest thermal conductivity followed by Sb_2Te_3 , MnO_2 and ZnO in ascending order.

The velocity of the thermopower waves was assessed experimentally to test the influence of thermal conductivity on the wave propagation velocities. The duration of the output signal corresponds to the time of the wave propagation which enables the author to calculate the linear propagation velocity of the wave. The author has previously shown that the average combustion velocities for Bi_2Te_3 , Sb_2Te_3 and ZnO based thermopower devices are 0.2, 0.7 and 23.0 m/sec, respectively with an error of ±10% [1-3]. Figure 6.10 shows that the average combustion velocity for the MnO₂-based devices is 3.9 m/sec. Due to the chaotic nature of the thermopower waves, the propagation velocities exhibit a wide range for all thermopower wave systems as shown in Figure 6.10 [1-3]. The difference in the propagation velocities corresponds well to the variation in the thermal conductivities of the core thermoelectric materials and is in excellent agreement with the theoretical expectations.

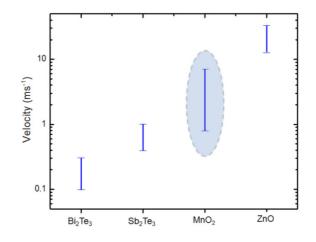


Figure 6.10: Reaction propagation velocities for thermopower systems based on different core thermoelectric materials.

6.4 Summary

In this chapter, the author demonstrated thermopower wave propagation using MnO_2 as the core TE material. The MnO_2 based thermopower wave devices resulted in extremely large output voltages of up to 1.8 V, which was at least 300% higher than any previously demonstrated thermopower wave system. At the same time, a high specific power in the order of ~1 kW/kg was maintained. The achievement of such large output voltages and specific power was primarily due to the large *S* exhibited by MnO_2 at elevated temperatures (-1900 μ V/K at 350 °C) in which thermopower wave systems with nitrocellulose as the reactive fuel operate. Its electrical resistivity also dropped significantly with an increase in temperature (0.43 Ω .cm at room temperature to 0.1 Ω .cm at 300 °C). Consequently, a high TPF in the order of ~10³ μ W/m.K² was achieved at elevated temperatures.

The author also provided important fundamental insights to explain the observation of enhanced Seebeck coefficients with increasing temperatures in TMOs such as ZnO and MnO₂. A full analysis of the system by characterizing the device before and after the thermopower wave reaction was conducted and it was shown that the MnO₂ films survived the thermopower wave propagation largely intact and retained their large TPFs. It was also shown that the thermopower wave propagation velocities were strongly influenced by the thermal conductivity of the core TE material.

This work conducted by the author is very important as it is the first demonstration of voltages that are high enough to power small electronic circuits. Furthermore, this work conducted by the author underscores the crucial role that TMOs can play to make thermopower wave sources a viable future energy generation technology.

In the next chapter the author will present a summary of his PhD thesis and discusses future work related to his PhD research project.

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Chapter 7

Conclusions and future works

7.1 Concluding remarks

The author's vision for this PhD involved developing thermopower wave sources to obtain output voltages, large enough for being employed in practical applications, while maintaining a high specific power. The author's vision was realised by developing thermopower wave sources in thin film geometries. The implementation of thermoelectric (TE) thin films for the propagation of thermopower waves turned out to be a crucial step as the author was able to employ a variety of core TE materials ranging from conventional TE materials such as Bi₂Te₃ and Sb₂Te₃ to TE transition metal oxide (TMOs) such as ZnO and MnO₂ to generate large magnitude voltages oscillatory, both oscillatory and non-oscillatory, while maintaining high specific powers.

In the course of conducting this research the author studied many reports on conventional TE materials such as Bi₂Te₃, Sb₂Te₃ and various TE TMOs. However, a comprehensive review on the TE properties of TMOs was lacking. As a result, the author prepared a comprehensive review article that provided the readers with a detailed description of TE properties of various TMOs in bulk and low dimensional morphologies as well as potential TE applications that they offer. Various tuning strategies to alter their TE properties via changes in morphology and stoichiometry were also discussed. The article highlighted the need to investigate many TMOs as viable TE materials, a research area where information is lacking. It was also noticed that prior to the author's research, only one thermopower wave system that was based on MWNTs had been reported (by Strano group at MIT). That system generated low voltages and oscillation amplitudes and it was obvious that the output voltages and oscillation amplitudes from thermopower wave sources needed to increase significantly to make it a viable technology. This highlighted the need for investigating other core TE

materials that exhibit high Seebeck coefficients, electrical conductivities and moderate thermal conductivities. It was also highlighted that thermopower wave propagation had not been demonstrated using p-type core materials which exhibit hole dominant electrical conduction. The review conducted by the author identified the potential of conventional TE materials such as Bi₂Te₃, Sb₂Te₃ and TE TMOs as possible candidates for being used as the core materials in thermopower wave sources due to their high TPFs. As such, the author's research was organised and conducted so as to target the identified research deficiencies.

In the first stage he demonstrated thermopower wave devices based on thin films of n-type Bi₂Te₃. Bi₂Te₃ was chosen due to its high S and σ . However, as its thermal conductivity was low, the author designed a viable system by depositing Bi_2Te_3 on the thermally conductive substrate of Al₂O₃ to compensate for this deficiency. This was the first demonstration of thermopower wave devices based on thin films. Subsequently, in the second stage the author developed thermopower wave devices based on p-type Sb₂Te₃ and n-type Bi₂Te₃ thin films to generate voltages with alternating polarities. This was the first demonstration of thermopower wave propagation using a p-type TE core material. In the third stage, the author for the first time implemented ZnO, a TE TMO as the core material in thermopower wave sources owing to its high TPF at elevated temperatures in which thermopower wave systems operate. The ZnO based thermopower wave system resulted in high voltage and oscillations amplitudes (>200%) compared to any previous thermopower wave system. Finally, in the fourth stage, prompted by the excellent results obtained by incorporating ZnO, the author implemented MnO₂, another TMO as the core TE material in thermopower wave sources to obtain significantly larger voltage (~1.8 V) and oscillations amplitudes than any previously developed thermopower wave system.

The major findings of each stage of this PhD research project are summarised as follows:

7.1.1 Stage 1

- In the first stage, the author demonstrated thermopower wave systems in a thin film geometry for the first time. n-type Bi₂Te₃ was incorporated as the core TE layer and exothermic chemical reactions from a solid fuel (nitrocellulose) were coupled to charge carriers of the Bi₂Te₃ layer to generate self-propagating thermopower waves. Bi₂Te₃ was used due to its high *S* and σ . However, the author compensated for its low κ by placing it on a thermally conductive substrate of Al₂O₃. Output voltages and oscillation amplitudes at least 150% higher than the previously reported MWNT based thermopower wave systems were achieved, while maintaining a high specific power of the order of 1 kW/kg.
- In addition to employing a thermally conductive substrate of Al₂O₃, the author also deposited Bi₂Te₃ on a substrate with extremely low thermal conductivity (terracotta). This was important in order to observe the effect of substrate thermal conductivity on the behaviour of thermopower waves and it was shown that a moderate to high thermal conductivity is an important requirement for generating oscillatory voltage signals of high magnitude.
- The author adapted the theory of combustion waves to theoretically analyse the fuel/Bi₂Te₃/Al₂O₃ and fuel/Bi₂Te₃/terracotta systems. Using a 1D approximation, the author estimated the thermopower wave propagation velocities and voltage oscillation frequencies. These estimations were also experimentally confirmed with an acceptable degree of accuracy.
- The author also examined the effect of the fuel mass and wave propagation velocities on the output voltage. It was observed that there was an optimal mass range of the fuel for which output voltages were maximised.
- The author employed the XRD technique to show that the Bi₂Te₃ films remained intact even after the thermopower wave propagation. This is an important observation as it can allow for developing reusable thermopower wave devices in the future.
- To the best of the author's knowledge, this was the first demonstration of thermopower

wave systems in a thin film geometry with highly oscillatory voltage signals and high specific power. The development of thin film thermopower wave systems is of utmost importance due to several advantages that thin films offer. Thin films allow the synthesis of different layers of varying TE properties that can be used for manipulating the propagation of the thermopower waves. Additionally, it allows for altering of the surface roughness which can be employed to increase the amount of solid fuel that can be placed over the TE layer. These advantages will certainly lead to the investigation of a wide variety and combination of TE cores for thermopower wave devices.

7.1.2 Stage 2

- In this stage the author developed thermopower wave devices based on a novel combination of two TE materials with complimentary semiconducting properties. The author employed p-type Sb₂Te₃ and n-type Bi₂Te₃ thin films as the TE cores. This unique combination of p and n-type materials with high *S* and σ resulted in output voltage signals with alternating polarities and higher magnitudes than MWNT based thermopower wave systems (at least 100 % higher in general). At the same time the devices generated a high specific power (0.6-1 kW/kg). Such oscillatory voltages along with high specific powers are highly desirable for practical applications.
- Thin films of the Sb₂Te₃ and Bi₂Te₃ were deposited on substrates with contrasting thermal conductivities (thermally conducting Al₂O₃ and thermally insulating terracotta) in order to assess the influence of the substrate thermal conductivity on the output voltages and the thermopower wave propagation velocities. It was observed that the substrate's thermal conductivity played a crucial role in the propagation of thermopower waves. Devices based on low thermal conductivity substrate of terracotta generated very low voltages with no oscillations.
- The author conducted a theoretical analysis of the Sb₂Te₃ and Bi₂Te₃ based thermopower wave devices to assess and predict the behaviour of thermopower waves. Using the theoretical model, the author was able to predict the oscillation frequencies

and thermopower wave propagation velocities with an acceptable accuracy.

- The author compared the performance of the thermopower wave sources based on the two p and n-type TE materials, and experimentally assessed the influence of thermal conductivity of the substrate and the core TE material on the propagation velocity and the output voltages. It was shown that the specific power obtained from Bi₂Te₃ based devices was higher, primarily due to the higher electrical conductivity of Bi₂Te₃. It was also shown that the difference in thermopower wave propagation velocities correspond to the difference in the thermal conductivities of the core TE materials, when deposited on identical substrates.
- Characterization techniques such as XRD were employed to assess the structure of the Sb₂Te₃ and Bi₂Te₃ films before and after the thermopower wave propagation. They showed that the films survived the reaction and remained largely intact.
- For the first time, the author showed that the phenomenon of thermopower waves was not just limited to n-type materials, but extended to p-type TE materials as well. This work is of utmost importance as it opens the opportunity of investigating other p-type materials, especially p-type TE TMOs as the core TE materials in thermopower wave sources. Additionally, this work shows that by using a combination of p and n-type materials also has the potential to generate ac voltage signals from such sources.

7.1.3 Stage 3

- In this stage, the author incorporated ZnO, a TE TMO, as the core material in thermopower wave devices for the first time. The author showed that the Seebeck coefficient and electrical conductivity of the ZnO thin films was enhanced in the temperature regimes in which thermopower wave systems operate, resulting in a high TPF. This made ZnO an outstanding choice as a core TE material in thermopower wave sources
- It was shown that ZnO based thermopower wave sources generated output voltages and oscillations at least 200% higher, while maintaining a high specific power (~0.5 kW/kg)

than any previously demonstrated thermopower wave system.

- Characterization techniques such as Raman spectroscopy and XRD were used to assess the structure of the ZnO film before and after thermopower wave propagation. It revealed that the ZnO films remained intact after the completion of the reaction.
- This was the first implementation of a TE TMO as the core material for thermopower wave sources. It also showed that TE TMOs were attractive candidates for thermopower wave sources due to their highly desirable properties (high *S*, *σ* and moderate *κ*). The success of this work formed the basis of further work conducted by the author by employing another TE TMO as described in stage 4.

7.1.4 Stage 4

- In this stage, the author implemented MnO_2 which is another TE TMO, as the core material in thermopower wave sources. The Seebeck coefficient and electrical conductivity of the MnO_2 thin films was assessed at elevated temperatures of up to $350 \,^{\circ}$ C. It was observed that both *S* and σ were dramatically enhanced at such elevated temperatures in which thermopower wave systems operate. The author also provided new fundamental insights into the observation of enhanced Seebeck coefficient with temperature. As expected, MnO_2 based thermopower wave systems generated voltages as high as 1.8 V, while maintaining high specific powers of the order of 1 kW/kg.
- Characterisation techniques such as SEM, BET and AFM were carried out to assess the surface roughness and porosity of the MnO₂ films. XRD was also carried out and revealed that the MnO₂ surface remained intact after the thermopower wave propagation.
- The Seebeck coefficient and electrical resistivity profiles were also obtained after the reaction to show that the MnO₂ films still retained their structure and properties after the reaction. Such behaviour is an important feature for the development of reusable thermopower wave devices in the future.
- The influence of thermal conductivity of the core TE material on the reaction

propagation velocities was assessed and a comparison with previously demonstrated thin film thermopower wave sources was conducted to prove that reaction propagation velocities are strongly influenced by the thermal conductivity of the core TE materials.

• This work is highly significant due to the generation of output voltages as high as 1.8 V, while maintaining a high specific power of the order of 1 kW/kg. Such voltages are enough to power small electronic circuits. It further highlighted the important role TMOs can play in making thermopower wave sources a viable energy generation technology in the future.

In conclusion, this research project has successfully brought new ideas and knowledge to the field of thermopower wave sources as well as the thermoelectric field in general. As such, the outcomes of this PhD research have been published in prestigious peer reviewed scientific journals. A complete list of publications by the author since the beginning of his PhD research project, are as follows:

7.2 Journal publications:

The work conducted by the author of this thesis during his PhD candidature has resulted in eight journal papers (five as the first author) in prestigious journals such as Advanced Functional Materials, Energy & Environmental Science, Chemical Communications, Journal of Physical Chemistry C and Advanced Materials. The list of author's scientific papers is presented below:

- S. Walia, R. Weber, K. Latham, P. Petersen, J. T. Abrahamson, M. S. Strano and K. Kalantar-zadeh, "Oscillatory Thermopower Waves Based on Bi₂Te₃ Films," *Advanced Functional Materials*, vol. 21, pp. 2072-2079, 2011.
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7.3 Conference publications:

In addition to the journal papers, the author of this thesis has had the opportunity to attend prestigious conferences such as the Materials Research Society meeting in San Francisco, USA and the International Conference on Nanoscience and Nanotechnology (ICONN) held in Perth, Australia to present the outcomes of his PhD research. Additionally, it resulted in the following publication in the proceedings of the ICONN conference: S. Walia, Sriram, M. Bhaskaran, S. Balendhran, S. Zhuiykov, and K. Kalantar-zadeh, "A combination of silicon and multi-walled carbon nanotubes with controllable thermoelectric parameters", in Brendan Griffin, Lorenzo Faraone, Mariusz Martyniuk (ed.) *Proceedings of the APMC 10 / ICONN 2012 / ACMM 22, Perth, Australia, 5-9 February 2012* 151, 2012.

7.4 Recommendations for future works

Significant strides have been made in the development of thermopower waves' based energy sources as part of this PhD project, however the author feels that there still exists numerous opportunities for continuing research in alignment with those presented in this thesis, and recommends the following as future work:

- The evolution of thin film thermopower wave devices allow for investigation of more TE core materials, especially TMOs. The high TPFs of many TMOs at elevated temperatures makes them attractive materials for thermopower wave sources. Modification strategies based on reducing dimensions of TE TMOs have already resulted in enhanced TPFs through engineering of their density of states. Enhanced TPFs can certainly be achieved by nanostructuring, substructuring, compositing, doping and changing the stoichiometry of TMOs. Considering that significant enhancements in TPF can be obtained in TMOs, the author of this thesis suggests that achieving output voltages as high as 10 V in thermopower wave sources based on TMOs is possible.
- Another future prospect for the development of viable thermopower wave systems would be the integration of liquid and gaseous fuels. As the thin films of the TE cores easily survive the thermopower wave propagation, the use of liquid and gaseous fuels will provide the opportunity to develop reusable/re-fuellable thermopower wave systems. Additionally, it will also provide the opportunity of using many highly intense fuels in gas and liquid phases, which can result in larger temperature gradients, producing higher output voltages.

- The physics of thermopower waves still needs to be fully understood. In this context, the development of a 3D theoretical model for thermopower wave systems is certainly an important proposition for future work. Such a model will allow researchers to accurately assess the influence of every parameter of the fuel, core TE material and the substrate on the behaviour of thermopower waves. This knowledge has the potential for the development of thermopower wave sources in which the frequency of the output voltage oscillations can be controlled.
- The efficiency of thermopower wave systems is still very low. This is mainly because a large portion of the heat generated from the exothermic chemical reaction of the fuel is dissipated to the ambient surroundings. Methods to minimise this heat dissipation need to be explored to increase the efficiency of thermopower wave systems.