



# The equivalent translational stiffness of steel studs

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## ABSTRACT

The effect of the resilience of the steel studs on the sound insulation of steel stud cavity walls can be modelled as an equivalent translational stiffness in simple models for predicting the sound insulation of walls. Numerical calculations (Poblet-Puig *et al.*, 2009) have shown that this equivalent translational stiffness varies with frequency. Vigran (2010a) has derived a best-fit third order polynomial approximation to the logarithm of these numerical values as a function of the logarithm of the frequency for the most common type of steel stud. This paper uses an inverse experimental technique. It determines the values of the equivalent translational stiffness of steel studs which make Davy's (2010) sound insulation theory agree best with experimental sound insulation data from the National Research Council of Canada (NRCC) (Halliwell *et al.*, 1998) for 126 steel stud cavity walls with gypsum plasterboard on each side of the steel studs and sound absorbing material in the wall cavity. These values are approximately constant as a function of frequency up to 400 Hz. Above 400 Hz they increase approximately as a non-integer power of the frequency. The equivalent translational stiffness also depends on the mass per unit surface area of the cladding on each side of the steel studs and on the width of the steel studs. Above 400 Hz, this stiffness also depends on the stud spacing. The equivalent translational stiffness of steel studs determined in this paper and the best-fit approximation to that data are compared with that determined numerically by Poblet-Puig *et al.* (2009) and with Vigran's (2010a) best-fit approximation as a function of frequency. The best-fit approximation to the inversely experimentally determined values of equivalent translational stiffness are used with Davy's (2010) sound insulation prediction model to predict the sound insulation of steel stud cavity walls whose sound insulation has been determined experimentally by NRCC (Halliwell *et al.*, 1998) or CSTB (Guigou-Carter and Villot, 2006).

## INTRODUCTION

Heckl (1959a; b) derived formulae for the sound power radiated on one side of an infinite plate excited by a point force and the sound power per unit length radiated from one side of an infinite plate excited by an infinite line source. These formulae only apply below the critical frequency of the plate. He used these results to predict the improvement in sound insulation obtained by attaching a lightweight panel at a distance from heavyweight wall with point or line connections to the heavy weight wall and filling the resulting wall cavity with sound absorbing material. Heckl's theory and those theories based on it, ignore the mass of the connecting studs and assume that the behaviour of each stud is independent of the other studs.

Sharp (1973; 1978) and Sharp *et al.* (1980) applied Heckl's results to predict the sound insulation of lightweight cavity walls with rigid studs or rigid point connections. Gu and Wang (1983) modelled resilient steel studs as springs with an equivalent translational stiffness of 9 or 10 MPa. Davy (1990b; a) stated that Gu and Wang's formulae "are not obviously an extension of Sharp's formulae" and introduced an equivalent mechanical compliance (the inverse of equivalent mechanical stiffness) of  $1 \times 10^{-6}$  1/Pa into Fahy's (1985) version of Sharp's theory. Notice that Davy's value of equivalent mechanical stiffness is a factor of 9 or 10 less than

Gu and Wang's value. Because Fahy had not integrated over angle of incidence, Davy performed the integration.

The results mentioned above only apply below the critical frequency. Davy (1991) extended his theory to above the critical frequency. Both Sharp's and Davy's theories included empirical correction factors below the critical frequency. Davy (1993) replaced his empirical correction factor with the effects of resonant vibration in both panels. He also found and corrected an error in his theory above the critical frequency. Unfortunately this paper introduced an apparent asymmetry into the theory. Davy was able to explain that the apparent asymmetry in panel critical frequency was due to total internal reflection. If this total internal reflection is taken into account, the apparent asymmetry in panel critical frequency is removed. Heckl pointed out that there is still an asymmetry in panel total damping loss factors. However this asymmetry will only arise if the panels have identical critical frequencies and different total damping loss factors. The recommended approach in this case is to use the average total damping loss factor for both panels.

Vigran (2010b) gives a good summary of Sharp's method of modelling sound transmission due to rigid studs and point connections. Vigran extends Sharp's theory to above the critical frequency using a different approach to that of Davy.

Hongisto (2006) showed that Davy's theory agreed well with measurements on steel stud walls with sound absorption in

the cavity while Gu and Wang's theory did not. Unfortunately Davy's theory only agreed well because as Hongisto also showed Davy's theory for the sound transmission via a wall cavity with sound absorbing material produced results which were too high. It turned out that Davy's theoretical air borne results were approximately the same as the experimental steel stud structure borne results and thus produced excellent agreement. Davy (1998) modified his airborne theory by limiting the upper angle of integration to a maximum value of  $61^\circ$ . He also set the equivalent mechanical compliance of the steel studs to  $0 \text{ 1/Pa}$  and introduced "an empirical steel stud structure borne attenuation of 10 dB relative to wooden studs". In 2009, Davy (2009) recommended "a stud attenuation factor in the range from 0.02 to 0.2". He actually used a stud attenuation factor of 0.04 to compare his theory with experimental results. Davy (2010) used an equivalent mechanical compliance of  $1.6 \times 10^{-6} \text{ 1/Pa}$  for steel studs but limited the predicted steel stud transmission to be greater than a minimum value of 0.005.

Guigou-Carter *et al.* (1998) modelled the sound insulation of 10 mm plasterboard mounted by rigid or resilient line connections 50 mm from a heavyweight wall. The 50 mm cavity was filled with glass wool. Their resilient line connectors were assumed to have an equivalent translational stiffness of 10 MPa. Poblet-Puig *et al.* (2006) calculated the vibrational level difference between 9 mm and 13 mm gypsum plaster board wall leaves connected via steel studs and compared these differences with those calculated for a line connections with a range of equivalent translational stiffnesses or a range of equivalent rotational stiffness. Guigou-Carter and Villot (2006) used this information to calculate the sound insulation at low frequencies of two gypsum plaster board steel stud cavity walls with sound absorbing material in the wall cavity. At higher frequencies they modelled the steel studs as resilient point connections situated at the positions of the screws used to attach the gypsum plaster board to the steel studs.

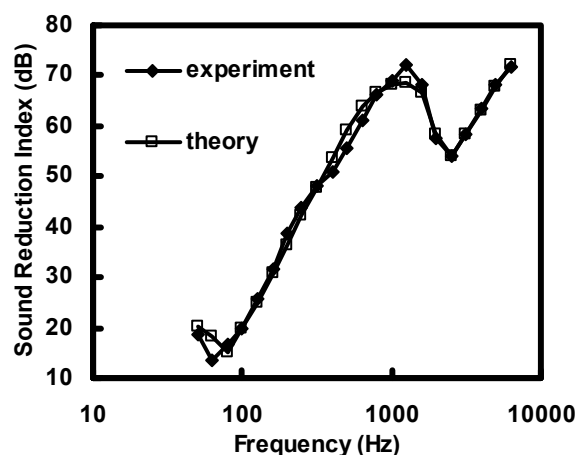
Research by Poblet-Puig (2008) and Poblet-Puig *et al.* (2009) has shown that a steel stud can be modelled as a translational spring with an equivalent translational stiffness which varies with frequency in the range from  $10^5$  to  $10^8 \text{ Pa}$ . The constant value of equivalent mechanical compliance used in Davy (2010) corresponds to an equivalent translational stiffness of  $6 \times 10^5 \text{ Pa}$  which lies towards the bottom end of the above range. The value of the minimum stud transmission used in Davy (2010) is -23 dB. This also lies in the 0 to -40 dB stud transmission range determined by Poblet-Puig *et al.* (2009) for a standard steel stud. Vigran (2010a) has derived a best-fit third order polynomial approximation to the logarithm of Poblet-Puig's numerical values as a function of the logarithm of the frequency for the most common type of steel stud.

## USE OF POBLET-PUIG'S STIFFNESS VALUES

Initially, the equivalent translational stiffness values of Poblet-Puig *et al.* (2009) for standard TC steel studs were used with Davy's (2010) theory to predict the average of nine experimental measurements by the NRCC (Halliwell *et al.*, 1998). These nine measurements were made on walls consisting of two layers of 16 mm gypsum plasterboard on each side of 90 mm steel studs at 406 mm spacing. There was sound absorbing material in the wall cavity. This type of wall construction is denoted as 16+16-90-406 in this paper. For walls where the thicknesses of gypsum plaster board on each side of the steel studs are different, the second leaf thicknesses are included in brackets. An example is 13+16(16+16)-90-406. Some of the walls only had one layer rather than two layers of gypsum plasterboard on one side or both sides of the steel studs. An example is 13-90-406.

Walls with fire rated and non fire rated gypsum plaster board (with slightly different masses per unit area) were grouped together, as were walls with different sound absorbing material in the cavity. The NRCC report gives the actual mass per unit area of the gypsum plaster board. Because of the combination of different densities of gypsum plaster board into the same group, gypsum plaster board is assumed to have a density of  $770 \text{ kg/m}^2$  in this paper and the nominal thickness of the gypsum plasterboard is used with this density to calculate the mass per unit area. The sound absorption coefficient of the cavity sound absorbing material is assumed to be 1. Note that Davy's (2009) theory limits the actual value of the sound absorbing material at low frequencies depending on the width of the cavity.

A single layer of gypsum plaster board is assumed to have a Young's modulus of 2.2 GPa. Because two layers of gypsum plaster board on one side of the steel studs are only fastened at points by the screws, they can slide relative to each other when being bent by the sound. The result is that the critical frequency of two equal thicknesses of gypsum plaster board is almost the same as that of a single thickness. In the theoretical results of this paper this result is achieved by assuming that two thicknesses behave as a single thickness of the same total thickness with a Young's modulus of approximately one quarter of one of the original single layers. In this paper two layers of gypsum plaster board are assumed to have a Young's modulus of 0.6 GPa. The Poisson's ratio of gypsum plaster board is assumed to be 0.3.



**Figure 1.** Comparison of the average of five NRCC experimental results with theoretical calculations for a 16-90-none type wall using Davy's (2010) theory.

Based on the comparison between Davy's (2010) theory and the average of 5 NRCC measurements on walls with 16 mm of gypsum plaster board on each side of 40 mm double steel studs, the in-situ damping loss factor of gypsum plaster board is assumed to be 0.03. There was a 10 mm gap between the 40 mm double steel studs giving a cavity width of 90 mm. The cavity was filled with sound absorbing material. This wall type is denoted 16-90-none in this paper and the comparison is shown in figure 1.

The comparison between theory and the average of the nine experimental results for the 16+16-90-406 type is shown in figure 2. It is apparent that the stud only and the combined theoretical results are much more irregular than the experimental or studless theoretical results. This is due to the irregularity of the numerically calculated equivalent translational stiffness. Nevertheless, the comparison was encouraging enough to proceed further.

### DERIVING COMPLIANCE FROM NRCC DATA

One way forward would have been to fit a smooth curve to the numerically calculated values of equivalent translational stiffness as has been done by Vigran (2010a). Instead the decision was made to determine the values of the equivalent translational compliance which would make Davy's (2010) theory agree with NRCC sound insulation measurements on steel stud walls (Halliwell *et al.*, 1998). The 126 steel stud walls were grouped into 28 different classes of wall. These types of wall were labelled as described at the start of the previous section. For each wall type and third octave band centre frequency, the value of equivalent translational compliance which made zero or minimised the difference between theory and experiment was determined if possible. Davy's (2010) theory does not use the stud borne transmission theory below the mass-air-mass resonance frequency because in that frequency range the air cavity rigidly couples the two wall leaves. Thus an equivalent translational compliance could not be determined for frequencies below the mass-air-mass resonance frequency. In some situations, the theoretical air borne sound insulation was less than the experimental sound insulation. In these situations, it was also not possible to determine a meaningful value of equivalent stud compliance.

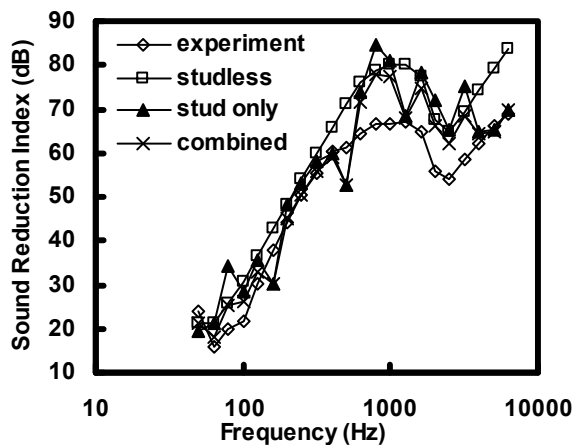


Figure 2. Comparison of the average of nine NRCC experimental results (Halliwell *et al.*, 1998) with theoretical calculations for a 16+16-90-406 type wall using Poblet-Puig *et al.*'s (2009) equivalent translational stiffness values for TC steel studs in Davy's (2010) theory.

Figure 3 shows the equivalent translational compliance determined using this method for a 16+16-90-406 type of wall. Examination of figure 3 suggests that the equivalent translational compliance is approximately constant up to about 400 Hz. Above 400 Hz, the relationship between the logarithm of the equivalent translational compliance and the logarithm of the frequency is approximately linear. In this frequency range, this linearity is very sensitive to the value of the critical frequency. The values of Young's modulus given above for both double and single layers of gypsum plaster board were determined by choosing the values which made the above relationship as linear as possible.

Also shown in figure 3 are the equivalent translational compliances derived for the average of eleven 13-90-406 type NRCC measurements. These results show more variability than those derived from the 16+16-90-406 type walls because

there is less difference between the theoretical studless sound insulation and the stud only sound insulation in this case. Since these are all greater than the compliances derived from the 16+16-90-406 type walls, it appears that the equivalent translational compliance depends on the properties of the gypsum plaster board leaves.

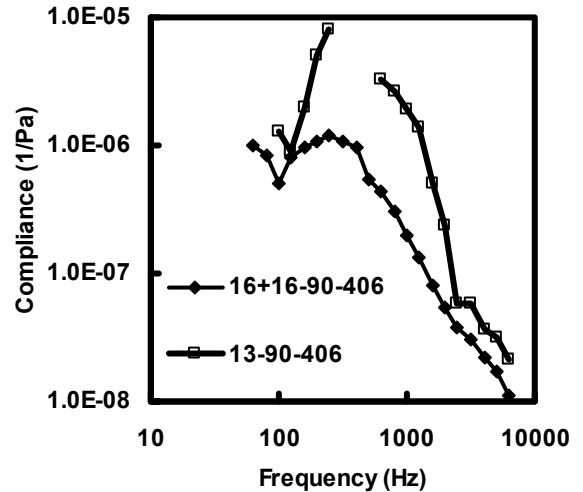


Figure 3. The equivalent translational compliance required to make Davy's (2010) theory agree with the average of nine 16+16-90-406 type and eleven 13-90-406 type NRCC experimental results (Halliwell *et al.*, 1998).

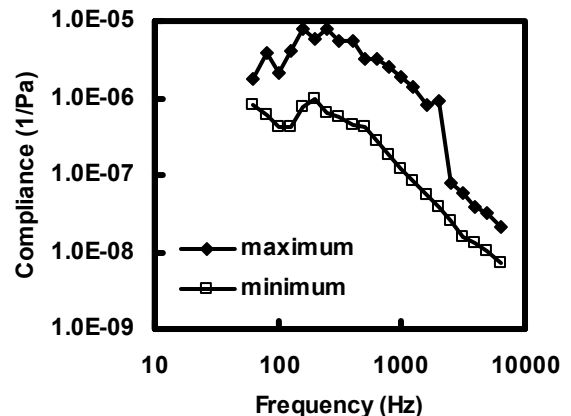


Figure 4. The maximum and minimum values of equivalent translational compliance of steel studs derived by making Davy's (2010) theory fit NRCC experimental data (Halliwell *et al.*, 1998).

### BEST FITTING TO COMPLIANCE VALUES

Figure 4 shows the maximum and minimum values of equivalent translation compliance derived by making Davy's (2010) theory fit the 28 different wall type averages of the 126 NRCC (Halliwell *et al.*, 1998) measurements on steel stud walls with sound absorbing material in their wall cavities. Because the equivalent translational compliance appears to decrease as a function of frequency above 400 or 500 Hz, a linear regression in the frequency range from 400 to 6300 Hz was conducted of the natural logarithm of the compliance  $C_M$  as a function of the natural logarithms of the frequency  $f$ , the reduced mass of the gypsum plasterboard wall leaves  $m_r$ , the steel stud spacing  $b$  and the steel stud (cavity) width  $d$ .

The reduced mass  $m_r$  is given by

$$m_r = \frac{m_1 m_2}{m_1 + m_2} \quad (1)$$

where  $m_i$  is the mass per unit area of the  $i$ th wall leaf. It was chosen because it appears in the equation for the normal incidence mass-air-mass resonance angular frequency  $\omega_0$ ,

$$\omega_0 = \sqrt{\frac{\rho_0 c^2}{dm_r}} \quad (2)$$

In this equation  $\rho_0$  is the ambient density of air,  $c$  is the speed of sound in air and  $d$  is the cavity (steel stud) width.

According to Davy (2010), the stud transmission ratio  $J$  is given by

$$J = \frac{2}{1 + \left(1 - \frac{4\omega^{3/2} m_1 m_2 c C_M}{G}\right)^2} \quad (3)$$

where

$$G = m_1 \omega_{c2}^{1/2} + m_2 \omega_{c1}^{1/2} \quad (4)$$

(Davy, 2009). The stud transmission ratio  $J$  is the ratio of the vibrational energy transmitted from wall leaf 1 to wall leaf 2 by a resilient stud with an equivalent translation compliance of  $C_M$  to that transmitted by a rigid stud ( $C_M = 0$ ).  $\omega_{ci}$  is the angular critical frequency of the  $i$ th wall leaf and  $\omega$  is the angular frequency of the sound.

Inserting equation (4) into equation (3) gives

$$J = \frac{2}{1 + \left(1 - \frac{4\omega^{3/2} m_1 m_2 c C_M}{m_1 \omega_{c2}^{1/2} + m_2 \omega_{c1}^{1/2}}\right)^2} \quad (5)$$

If  $\omega_{c1} = \omega_{c2} = \omega_c$ , then equation (5) becomes

$$J = \frac{2}{1 + \left(1 - \frac{4\omega^{3/2} m_r c C_M}{\omega_c^{1/2}}\right)^2} \quad (6)$$

The appearance of the reduced mass  $m_r$  in equation (6) is another reason for using it in the linear regression.

Using each side of the linear regression equation as the argument of the exponential function produces the following equation.

$$C_M = A f^{x_f} m_r^{x_m} b^{x_b} d^{x_d} \quad (7)$$

The linear regression produced the values and 95% confidence limits shown in table 1 for the constants in equation (7). Notice that at the 95% confidence level,  $A$  is statistically different from 1 and all four  $x$ 's are statistically different from 0.

Because the equivalent translational compliance appears to be approximately constant as a function of frequency below 400 or 500 Hz, a linear regression in the frequency range from 63 to 500 Hz was conducted of the natural logarithm of

the compliance  $C_M$  as a function of the natural logarithms of the same variables used in the previous linear regression. This linear regression produced the values and 95% confidence limits shown in table 2 for the constants in equation (7)

**Table 1.** Values and confidence limits for the constants in equation (7) in the frequency range from 400 to 6300 Hz.

Constant	Value	95% Upper Limit	95% Lower Limit
$A$	1.74	2.94	1.03
$x_f$	-1.81	-1.77	-1.84
$x_m$	-1.40	-1.29	-1.51
$x_b$	-0.75	-0.59	-0.92
$x_d$	0.28	0.43	0.13

**Table 2.** Values and confidence limits for the constants in equation (7) in the frequency range from 63 to 500 Hz.

Constant	Value	95% Upper Limit	95% Lower Limit
$A$	$8.5 \times 10^{-5}$	$3.1 \times 10^{-4}$	$2.3 \times 10^{-5}$
$x_f$	0.0134	0.133	-0.106
$x_m$	-1.09	-0.82	-1.35
$x_b$	-0.02	0.35	-0.40
$x_d$	0.81	1.19	0.42

At the 95% confidence level,  $A$  is statistically different from 1,  $x_m$  and  $x_d$  are statistically different from 0 and  $x_f$  and  $x_b$  are not statistically different from 0. The fact that  $x_f$  is not statistically different from zero confirms the visual observation that the equivalent translational compliance is not a function of frequency in the frequency range from 63 to 500 Hz.

Because  $x_f$  and  $x_b$  are not statistically different from 0, a new linear regression in the frequency range from 63 to 500 Hz was conducted of the natural logarithm of the compliance  $C_M$  as a function of the natural logarithms of the reduced mass of the gypsum plasterboard wall leaves  $m_r$  and the steel stud (cavity width)  $d$ . Using each side of this linear regression equation as the argument of the exponential function produces the following equation.

$$C_M = A m_r^{x_m} d^{x_d} \quad (8)$$

The linear regression produced the values and 95% confidence limits shown in table 3 for the constants in equation (8)

**Table 3.** Values and confidence limits for the constants in equation (8) in the frequency range from 63 to 500 Hz.

Constant	Value	95% Upper Limit	95% Lower Limit
$A$	$9.3 \times 10^{-5}$	$2.7 \times 10^{-4}$	$3.2 \times 10^{-5}$
$x_m$	-1.09	-0.83	-1.35
$x_d$	0.80	1.19	0.41

**Table 4.** Values and confidence limits for the constants in equation (7) in the frequency range from 2500 to 6300 Hz.

Constant	Value	95% Upper Limit	95% Lower Limit
$A$	0.0120	0.0196	0.0073
$x_f$	-1.37	-1.32	-1.43
$x_m$	-0.77	-0.71	-0.83
$x_b$	-0.58	-0.49	-0.66
$x_d$	0.22	0.30	0.15

Looking at figure 4, the values of equivalent translational compliance are much more tightly grouped in the frequency range from 2500 to 6300 Hz. Thus it is of interest to repeat the original linear regression restricted to this frequency range. The results are shown in table 4.

Given that the confidence intervals for  $x_f$  and  $x_m$  in table 1 are less than -1.5 and -1 respectively, while they are greater than -1.5 and -1 respectively in table 4, it is interesting to speculate that the true values of  $x_f$  and  $x_m$  in the high frequency range are -1.5 and -1 respectively. Also  $x_b$  in table 4 is not statistically significantly different from -0.5 and it is also interesting to speculate that the true value of  $x_b$  in the high frequency range is -0.5. These speculations lead to an interesting conclusion. They imply that for a constant value  $d$ , the equivalent translational compliance is given by

$$C_M = Bb^{-1/2}\omega^{-3/2}m_r^{-1} \quad (9)$$

in the high frequency range where  $B$  is a constant. Substituting equation (9) into equation (6) gives

$$J = \frac{2}{1 + \left(1 - \frac{4Bc}{b^{1/2}\omega_c^{1/2}}\right)^2} \quad (10)$$

This implies that for constant angular critical frequency  $\omega_c$ , constant stud spacing  $b$  and constant speed of sound  $c$ , the stud transmission ratio  $J$  is constant. This speculative result agrees with the assumption of a constant or a minimum stud transmission ratio made by Davy (1998; 2009; 2010).

If the magnitude of the second term in the brackets of equation (10) is much greater than one, equation (10) becomes

$$J = \frac{b\omega_c}{8B^2c^2} \quad (11)$$

Equation (29) of Davy (2010) gives the stud borne transmission coefficient  $\tau$  as

$$\tau = \frac{32\rho_0^2c^3HJ}{G^2b\omega^2} \quad (12)$$

where  $H$  is the  $D$  of equation (50) of Davy (2009).

Substituting equation (11) into equation (12) gives

$$\tau = \frac{4\rho_0^2c\omega_cH}{G^2B^2\omega^2} \quad (13)$$

Thus the speculative assumptions suggest that the stud borne sound insulation of a steel stud gypsum plaster board cavity wall with sound absorbing material in the wall cavity is independent of the stud spacing at medium and high frequencies. This is not the case at low frequencies where table 2 shows that the equivalent translational compliance is independent of the stud spacing and thus that equation (12) retains its inverse dependence on the stud spacing  $b$ .

Another conclusion to be drawn from an examination of tables 1 to 4 is that the equivalent translational compliance depends more strongly on the stud (cavity) width at low frequencies than at medium and high frequencies.

Some caution should be exercised with regard to the dependence on stud spacing and stud (cavity) width. Only two stud spacings (406 and 610 mm) were considered. All but two of the walls whose results were analysed had 65 or 90 mm stud widths. The other two had 150 mm stud widths. On the other hand the values analysed are the most common used in practice.

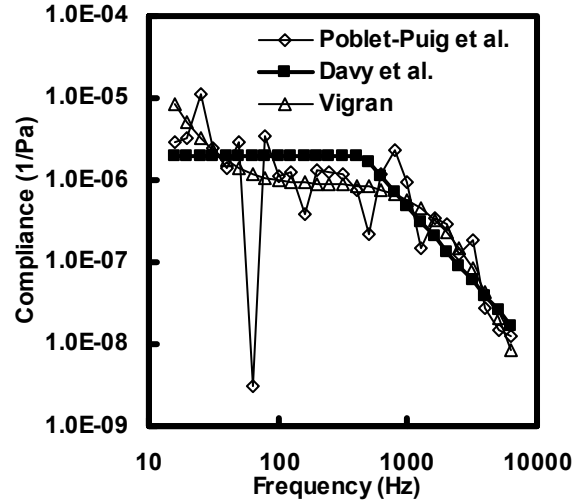


Figure 5. Comparison of the best fit equations of this paper (Davy *et al.*) and that of Vigran (2010a) for the equivalent translational compliance with the Poblet-Puig *et al.*'s (2009) data for 70 mm wide TC steel studs spaced at 600 mm with 13 mm gypsum plasterboard on each side.

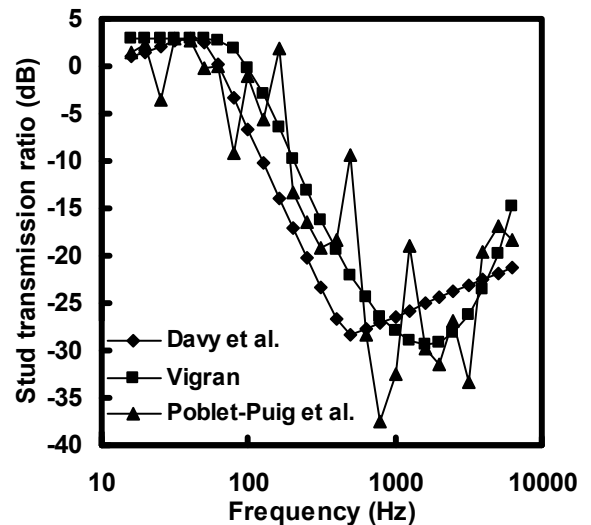


Figure 6. Comparison of stud transmission ratio (dB) calculated using equation (3) and the best fit equations for the equivalent translational compliance of this paper (Davy *et al.*), the best fit equation of Vigran (2010a) and Poblet-Puig *et al.*'s (2009) numerical data for 70 mm wide TC steel studs spaced at 600 mm with 13 mm gypsum plasterboard on each side.

In this paper the equivalent translational compliance  $C_M$  will be calculated as the minimum of equation (7) calculated using the constant values in table 1 and equation (8) using the constant values in table 3. The equivalent translational stiffness is calculated by inverting of the value of the equivalent translational compliance.

Define

$$x = \log_{10}(f). \tag{14}$$

Then Vigran’s (2010a) best fit third order polynomial approximation, to Poblet-Puig *et al.*’s (2009) numerically calculated equivalent translational stiffness data for TC steel studs, is given by the following equation.

$$-\log_{10}(C_M) = 0.6286x^3 - 4.4051x^2 + 10.3323x - 7.0722 \tag{15}$$

Figure 5 compares the best fit equations of this paper (Davy *et al.*) and that of Vigran with the Poblet-Puig *et al.* data for 70 mm wide TC steel studs spaced at 600 mm with 13 mm gypsum plasterboard on each side. The equivalent translation compliance of  $1.6 \times 10^{-6}$  1/Pa recommended by Davy (2010) is in rough agreement with the low frequency value of this paper of  $1.9 \times 10^{-6}$  1/Pa shown in figure 5.

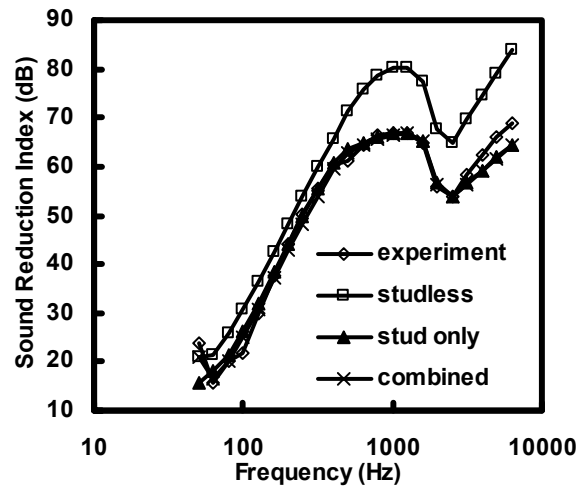
**USE OF THE BEST FIT EQUATIONS**

Figure 6 shows the comparison of the stud transmission ratio *J* (dB) calculated using equation (3) and the best fit equations for the equivalent translational compliance of this paper (Davy *et al.*), the best fit equation of Vigran (2010a) and Poblet-Puig *et al.*’s (2009) numerical values for 70 mm wide TC steel studs spaced at 600 mm with 13 mm gypsum plasterboard on each side. The minimum value of the stud transmission ratio of -23 dB recommended by Davy (2010) is in rough agreement with the high frequency results of this paper shown in figure 6.

**Table 5.** The mean, standard deviation, maximum and minimum of sound insulation theory (Davy, 2010) minus experiment (Halliwell *et al.*, 1998) for the third octave frequency bands from 50 to 6300 Hz for different wall types.

Wall Type	mean (dB)	std dev (dB)	max (dB)	min (dB)
13-65-406	-0.2	3.2	6.9	-4.0
13-65-610	0.8	2.5	5.7	-2.5
13-90-406	0.0	2.7	5.0	-4.0
13-90-610	-0.2	2.4	5.7	-4.6
13-150-610	-2.6	3.6	4.7	-6.1
16-65-406	0.6	2.7	6.9	-4.2
16-65-610	0.8	2.6	7.0	-3.9
16-90-406	0.3	2.2	4.7	-2.9
16-90-610	0.0	2.5	6.0	-3.2
16-150-610	-0.5	2.4	3.1	-5.9
13(13+13)-65-406	0.8	2.5	6.0	-3.8
13(13+13)-65-610	-0.2	2.3	6.5	-3.5
13(13+13)-90-406	0.8	1.9	5.1	-1.7
13(13+13)-90-610	0.1	2.4	5.7	-4.1
16(16+13)-65-610	-0.2	2.4	6.2	-3.8
16(16+16)-65-406	0.1	2.6	5.3	-5.4
16(16+16)-65-610	0.5	2.3	6.0	-3.2
16(16+16)-90-406	0.4	1.6	3.7	-2.0
16(16+16)-90-610	0.4	1.7	3.6	-2.2
13+13-65-406	-0.2	2.3	5.1	-4.0
13+13-65-610	-0.3	2.6	5.0	-4.8
13+13-90-406	0.1	1.4	3.8	-2.9
13+13-90-610	0.1	2.8	5.9	-4.4
13+16(16+16)-90-406	-0.2	2.1	4.0	-3.9
16+16-65-406	-1.3	2.5	4.3	-6.4
16+16-65-610	-0.6	2.0	3.9	-4.1
16+16-90-406	-0.8	1.8	3.1	-4.5
16+16-90-610	-0.5	2.4	3.4	-4.6
Overall	-0.1	2.4	7.0	-6.4
16-90-none	0.2	1.9	4.6	-3.2

Table 5 shows the mean, standard deviation, maximum and minimum of sound insulation theory (Davy, 2010) minus experiment (Halliwell *et al.*, 1998) for the third octave frequency bands from 50 to 6300 Hz for the 28 different wall types using the best fit equations derived in this paper for equivalent translational compliance. The overall row in table 5 shows the average value of the mean differences, the root mean square of the standard deviations of the differences, the maximum of the maximum differences and the minimum of the minimum differences. For comparison, the last row of table 5 shows the values for the 16-90-none wall type whose theoretical and experimental results are graphed in figure 1. This last wall type is without studs which bridge the wall cavity. The overall standard deviation of 2.4 dB is not excessively greater than the 1.9 dB standard deviation of the 16-90-none wall type without bridging studs.

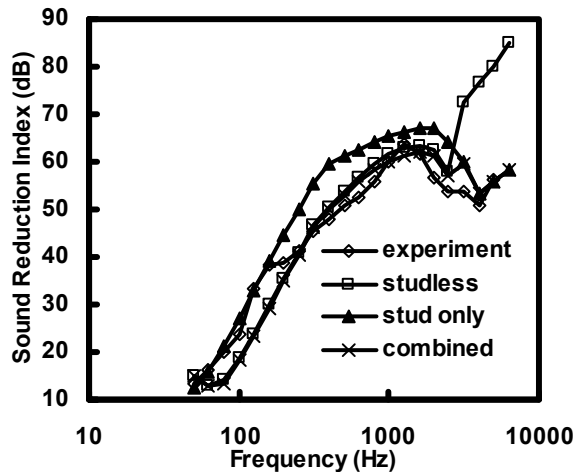


**Figure 7.** Comparison of the average of nine NRCC experimental results (Halliwell *et al.*, 1998) with theoretical calculations for a 16+16-90-406 type wall using the equivalent translational compliance best fit equations for steel studs in Davy’s (2010) theory.

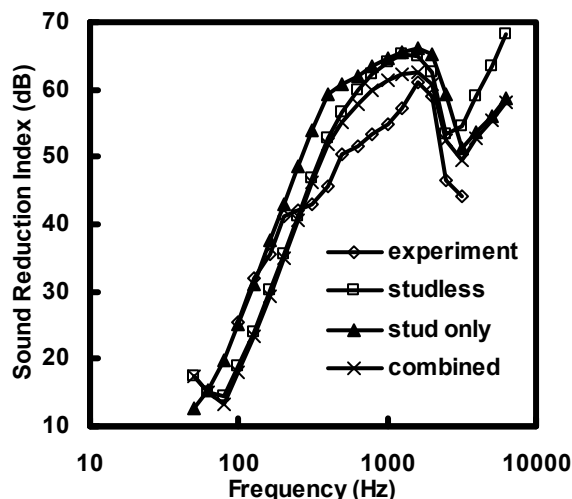
Figure 7 shows the comparison of the average of nine NRCC experimental results (Halliwell *et al.*, 1998) with theoretical calculations for a 16+16-90-406 type wall using the equivalent translational compliance best fit equations for steel studs in Davy’s (2010) theory. This figure should be compared with figure 2. From Table 5, it can be seen that the mean, standard deviation, maximum and minimum of the combined theory minus experiment for figure 7 are -0.8, 1.8, 3.1 and -4.5 dB respectively. The equivalent numbers for figure 2 are 3.0, 5.7, 11.2 and -8.4 dB. Thus it can be seen from both these sets of numbers and the figures that the best fit equations derived in this paper perform better overall than the numerical calculations of Poblet-Puig *et al.* (2009). This is thought to be due the very complicated vibrational situation that the numerical calculations of Poblet-Puig *et al.* (2009) are attempting to analyse from first principles. Nevertheless, the calculations of Poblet-Puig *et al.* (2009) are very important because they provide a first principles theoretical explanation of why steel studs behave vibrationally in the way that they do.

Of course, the real test of the best fit equations derived in this paper is how they perform when used to predict experimental sound insulation data other than that from which they were derived and when they are used with theories other than Davy’s (2010) theory. As a first step in this direction, CSTB measurements (Guigou-Carter and Villot, 2006) are compared with Davy’s (2010) theory using the best fit equations derived in this paper.

Figure 8 shows a comparison of CSTB experimental results (Guigou-Carter and Villot, 2006) with theoretical calculations for a 9(13)-175-600 type wall using the equivalent translational compliance best fit equations for steel studs in Davy's (2010) theory. The mean, standard deviation, maximum and minimum of the combined theory minus experiment are -0.6, 4.4, 6.0 and -9.8 dB respectively.



**Figure 8.** Comparison of CSTB experimental results (Guigou-Carter and Villot, 2006) with theoretical calculations for a 9(13)-175-600 type wall using the equivalent translational compliance best fit equations for steel studs in Davy's (2010) theory.



**Figure 9.** Comparison of CSTB experimental results (Guigou-Carter and Villot, 2006) with theoretical calculations for a 13-125-600 type wall using the equivalent translational compliance best fit equations for steel studs in Davy's (2010) theory.

Figure 9 shows a comparison of CSTB experimental results (Guigou-Carter and Villot, 2006) with theoretical calculations for a 13-125-600 type wall using the equivalent translational compliance best fit equations for steel studs in Davy's (2010) theory. The mean, standard deviation, maximum and minimum of the combined theory minus experiment are 1.4, 5.6, 6.5 and -8.7 dB respectively.

From 50 to 160 Hz in figure 8 and from 100 to 200 Hz in figure 9, the experimental curve is in reasonable agreement

with the stud only curve. Over most of these two frequency ranges, the studless curve and hence the combined curve are less than the experimental curve. Thus although the airborne sound insulation is under predicted by Davy's (2010) theory in these frequency ranges for reasons which are not clear at this stage, the stud borne sound insulation predictions appear to be in good agreement with the experimental results in these frequency ranges. At most of the higher frequencies the experimental results are less than the predicted results and the differences are larger in figure 9.

At first sight, it appears that there may be some systematic difference between these two CSTB results and the 126 NRCC results. However it should be borne in mind that the 175 mm cavity width of figure 8 is larger than any of the 126 NRCC cavity widths and that the 125 mm cavity width of figure 9 is larger than all but 2 of the 126 NRCC cavity widths.

It should also be noted that Guigou-Carter and Villot (2006) modelled the experimental results in figures 8 and 9 as point connections due to the screws above about 100 or 150 Hz. However the NRCC walls also used screws to attach the gypsum plaster board to the steel studs. Clearly more comparisons between Davy's (2010) theory, other theories and experiment are needed.

## CONCLUSIONS

This paper has derived empirical best fit formulae for the equivalent translational compliance of standard steel studs by making Davy's (2010) sound insulation theory agree with the experimental measurements of the National Research Council of Canada (NRCC) on 126 different gypsum plaster board steel stud walls with sound absorbing material in their wall cavities. The values of the equivalent translational stiffness of standard steel studs are easily obtained by inverting the calculated values of equivalent translational compliance.

The equivalent translational compliance or stiffness depends on the masses per unit area of gypsum plaster board fastened to each side of the steel studs and the width of the steel studs (which is also the cavity width). Above 400 or 500 Hz, it also depends on the frequency and the spacing between the steel studs.

The values of equivalent translational compliance derived in this paper and the stud velocity transmission ratios derived from them are in rough agreement with values proposed previously by Davy.

When used with Davy's (2010) sound insulation theory, the empirical best fit formulae for equivalent translational stud compliance are reasonably successful at predicting the NRCC experimental sound insulation results from which the empirical best fit formulae were derived. They are less successful when predicting two CSTB experiment sound insulation results. Thus more comparisons between experimental sound insulation results, Davy's (2010) sound insulation theory and other sound insulation theories using the empirical best equations derived in this paper are needed. Other theories of sound insulation with which the empirical best fit equations of this paper could be used include those of Craik and Smith (2000a; b), Wang *et al.* (2005), Legault and Atalla (2009; 2010), Poblet-Puig (2008) and Vigran (2010b; a).

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