

Invariant Imbedded T-Matrix Method for Axial Symmetric Hydrometeors with Extreme Aspect Ratios

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Introduction

One of the most fundamental and crucial quantities for accurate precipitation retrievals is the single-scattering property (SSP) of each individual hydrometeor in the precipitating volume. Thus, an important step in minimizing retrieval uncertainty is to ensure that the particles used for single-scattering calculations resemble those that occur in nature, allowing the SSPs to be computed precisely with numerical techniques.

Hydrometeors with rotational symmetry (axial symmetry) are most efficiently computed using the T-Matrix methods. For hydrometeors with a uniform dielectric, the Extended Boundary Condition Method (EBCM) is the most efficient. However, for mixed-phase hydrometeors with non-uniform dielectrics EBCM is not applicable. In these cases, we can use the Invariant Imbedded T-Matrix (IITM), which we developed for this purpose. It is also noted that hydrometeors with more extreme aspect ratios can be computed with IITM than EBCM and that such hydrometeors are found in precipitating systems. For hydrometeors without any rotational symmetry, however, volume integral methods like Discrete Dipole Approximation (DDA) and the Method of Moments (MoM) must be employed.

Hydrometeors SSPs Spherical No Symmetry Rotational Symmetry (non-uniform Symmetry (non-uniform) Multi-layered Non-Uniform Uniform DDA, MoM Dielectric Dielectric Lorenz-Mie Moderate Extreme IITM Aspect Ratios Aspect Ratios EBCM

Algorithm Flow-Chart for SSPs

Implementation

The IITM is typically an order of magnitude more computationally expensive than EBCM. To make IITM practical requires an efficient implementation that is optimized and takes advantage of parallelism in the IITM algorithm.

Algorithm Schematic

- Initialize with Separation of Variables (SOV).
- 2. Perform quadrature over spherical shell r_{k-1} --- Gauss-Legendre quadrature.
- 3. Using recursion relations to get the T-Matrix at rk, $T(r_k)$. --matrix inversion + linear algebra. Romberg integration used.



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wave truncation and the number of radial shells (δI)(δr), respectively.



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T-Matrix methods are computationally more efficient than Discrete Dipole Approximations (DDAs) for scattering targets that possess a high degree of symmetry. For the case of spheroids shown, it only takes a few minutes on 32 cores to compute the orientation averaged scattering properties. The reason for this is that the T-Matrix becomes sparse and structured, reducing the problem size significantly. Irregular particles incur a substantially larger cost as the maximum allowed angular momentum, L_{max}, increases, since the block diagonal structure is lost. Specifically, the computational cost for axial and no symmetry:

FLOPS

A further complication is that surface integrals carried out over the sphere become highly discontinuous for irregular particles. In this case, the "nice" properties of Gauss-Legendre quadrature are no longer true, and partitioning the integrals would require a numerical routine to find the boundaries.

An efficient C++ parallel IIITM code has been developed. This code accurately computes SSPs of non-uniform hydrometeors with rotational symmetry. The code parallelizes by taking advantage of the block structure induced by rotational symmetry about the z-axis by distributing blocks among MPI processes. Long double precisions was required to achieve satisfactory accuracy. This IITM code will allow the efficient computation of mixed-phase rotationally-symmetric hydrometeors necessary for modeling precipitating systems.

References

[1] Bi, L., P. Yang, G.W. Kattawar, and M.I. Mishchenko, 2013: Efficient implementation of the invariant imbedding T-matrix method and the separation of variables method applied to large nonspherical inhomogeneous particles. J. Quant. Spectrosc. Radiat. Transfer, 116, 169-183, doi:10.1016/j.jqsrt.2012.11.014

Acknowledgements

We would like to thank the NASA Center for Climate Simulation (NCCS) for partial support of this ongoing effort.

Contact Information

Irregular Hydrometeors

Axial symmetry	No symmetry
$\sim L_{\rm max}^4 \times \# shells$	$\sim L_{\rm max}^6 \times \# shells$

Conclusions

It is challenging to use T-Matrix Methods for irregular hydrometeors, and it is not clear that numerical precision and compute constraints will allow accurate SSPs to be computed using this method. Currently, DDA approaches are employed.

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