

Methodological Advances for Detecting Physiological Synchrony During Dyadic Interactions

Michael P. McAssey,^{1,2} Jonathan Helm,² Fushing Hsieh,² David A. Sbarra,³ and Emilio Ferrer²

¹Vrije Universiteit, Amsterdam, The Netherlands, ²University of California, Davis, USA, ³University of Arizona, Tucson, Arizona, USA

Abstract. A defining feature of many physiological systems is their synchrony and reciprocal influence. An important challenge, however, is how to measure such features. This paper presents two new approaches for identifying synchrony between the physiological signals of individuals in dyads. The approaches are adaptations of two recently-developed techniques, depending on the nature of the physiological time series. For respiration and thoracic impedance, signals that are measured continuously, we use Empirical Mode Decomposition to extract the low-frequency components of a nonstationary signal, which carry the signal's trend. We then compute the maximum cross-correlation between the trends of two signals within consecutive overlapping time windows of fixed width throughout each of a number of experimental tasks, and identify the proportion of large values of this measure occurring during each task. For heart rate, which is output discretely, we use a structural linear model that takes into account heteroscedastic measurement error on both series. The results of this study indicate that these methods are effective in detecting synchrony between physiological measures and can be used to examine emotional coherence in dyadic interactions.

Keywords: time series analysis, dyadic interactions, dynamical systems, psychophysiology

The synchronization of oscillatory systems – or coupled oscillations – is widely studied in the biological and physical sciences (e.g., Mirolo & Strogatz, 1990; Pikovsky, Rosenblum, & Kurths, 2001; Weishenbush, Nishioka, Ishikawa, & Arakawa, 1992), with also multiple applications in the social sciences, economics, and medicine (e.g., Quian Quiroga, Kraskov, Kreuz, & Grassberger, 2002). The synchrony of these oscillations can provide information about the system not available from separate univariate analyses. Consider, for example, the investigation of several electroencephalographic signals measured simultaneously from an individual's scalp during a particular task. Each signal could be analyzed separately, and those with the most activity would indicate an area of relative activation. However, various signals can show simultaneous activation, revealing communication between different areas of the brain during the task (Engel & Singer, 2001; Fries, 2005). Furthermore, different types of such coherence – or synchrony – may be evident for different mental processes, as is the case with epileptic seizures (Quian Quiroga et al., 2002). Thus, the study of synchrony and oscillatory systems can provide a valuable means of studying psychophysiological processes, as well as possible changes in those processes as a function of different stimuli and conditions.

In the current study we propose the application of two recently-developed methodologies for examining the relations between two time series. The first technique is the

Empirical Mode Decomposition (EMD), an algorithm for filtering continuous time series data. The second method is the structural heteroscedastic measurement-error (SHME) model, which is adapted here for detecting linear associations between two discrete time series. We apply these techniques to physiological data from individuals in couples that participated in a laboratory-based social interaction task.

The paper is organized as follows. First, we provide a brief review of some of the common synchronization measures and their rationale in the context of emotional processes in dyadic interactions. Second, we describe the EMD and SHME methods, with details about each of the required steps for their implementation. Third, we illustrate the application of the proposed methods with an application. The paper ends with a discussion of the potential of these models in psychophysiological research.

Synchronization Measures

Synchronization measures have become an important tool for exploring the associations between time series. Multiple methods now exist to identify and characterize synchronization, including indices of linear interdependence, such as cross-correlation, coherence, and event-related coherence, as well as more recent measures of nonlinear interdependence,

73 such as mutual information (Kramer et al., 2004). In
74 econometric research, for example, one of the most common
75 methods to assess whether two series share a pattern in their
76 long-term fluctuations is co-integration (Engle & Granger,
77 1987; Granger, 1981). In psychological research, perhaps the
78 most standard method to assess synchronization consists of
79 cross-correlations (e.g., Gottman, 1990; Mauss, Levenson,
80 McCarter, Wilhelm, & Gross, 2005). This method can be
81 useful to examine concurrent and lagged relations between
82 two time series, either through the entire series or through
83 windows of interest (e.g., Boker, Rotondo, & King, 2002).

84 Synchronization of Emotion 85 in Dyadic Interactions

86 Human and animal research suggests that psychophysiological
87 linkages between two conspecifics are an inherent element
88 of social bonding and attachment (Coan, 2008; Coan,
89 Schaefer, & Davidson, 2006; Feldman, 2007; Gottman,
90 Swanson, & Swanson, 2002; Guastello, Pincus,
91 & Gunderson, 2006; Hofer, 1984, 1994; Sbarra & Hazan,
92 2008). The study of dyadic interactions indicates that emo-
93 tional exchanges between the two members of a couple can
94 be highly interdependent (Cowan & Cowan, 2000; Ferrer &
95 Nesselroade, 2003; Ferrer & Widaman, 2008; Song &
96 Ferrer, 2009; Thompson & Bolger, 1999). This research
97 shows, for example, that the adoption of one individual's
98 emotion state by another promotes relationship longevity
99 (Hatfield, Cacioppo, & Rapson, 1994), that the length of
100 the relationship between romantic and non-romantic partners
101 corresponds to the level of emotional coherence that the pair
102 maintains (Anderson, Keltner, & John, 2003), and that the
103 facial expression and emotional tone exhibited by romantic
104 partners are a strong predictor of relationship dissolution
105 (Levenson & Gottman, 1985).

106 Research in dyadic interactions using psychophysiological
107 signals is scarcer. In a classic study of couples, Levenson
108 and Gottman (1983) found that, during a conversation of
109 disagreement, distressed couples showed significantly
110 higher levels of synchrony between the partners' autonomic
111 response signals than non-distressed couples. Moreover, this
112 synchrony was predictive of marital satisfaction in the same
113 couples. This study notwithstanding, the relative absence of
114 research on psychophysiological synchrony in couples is
115 conspicuous, largely because most theories of human attach-
116 ment and emotion regulation suggest that the emotional
117 experiences of one member of a couple are highly related
118 – if not dependent upon – the experiences of his or her part-
119 ner (cf. Sbarra & Hazan, 2008). In our view, a large part of
120 the discrepancy is methodological; theoretical developments
121 in this area greatly outpace methodological innovations. In
122 order to fully understand dyadic emotion regulation and
123 psychophysiological synchrony in couples, the field needs
124 accessible methods that can capture and adequately

represent the complexity in interdependent emotional regu- 125
latory systems (Cole, Martin, & Dennis, 2004). 126

Synchrony Between Continuous Variables: Trend Extraction Using EMD

127 The EMD (Huang et al., 1998) is an algorithm developed to 129
130 filter continuous data into any number of intrinsic mode 130
131 functions (IMFs), each representing a particular frequency 131
132 component of the original data. EMD works so that the 132
133 highest-frequency components are separated out of the origi- 133
134 nal time series until either no further frequency components 134
135 can be detected within the residual series or a preset maxi- 135
136 mum number of IMFs has been extracted. These IMFs must 136
137 satisfy two conditions. First, in each IMF, the total number 137
138 of extrema and the total number of zero crossings must be 138
139 the same or differ by 1. Second, at every point in the 139
140 IMF, the mean value of the envelopes defined by the local 140
141 maxima and the local minima must equal zero. These con- 141
142 ditions are necessary for the purpose of defining the concept 142
143 of instantaneous frequency in a meaningful way. The IMFs 143
144 are extracted from a time series one by one beginning with 144
145 the highest intrinsic frequency using an iterative process 145
146 called sifting. The goal of this process is the empirical iden- 146
147 tification of intrinsic oscillatory modes in the data based on 147
148 their instantaneous frequencies. The time lapse between suc- 148
149 cessive extrema defines this time scale. 149

150 In the sifting process, the local maxima of the original 150
151 time series are identified and connected by a cubic spline 151
152 to form a curved upper envelope for the series. A lower 152
153 envelope for the time series is formed in a similar way. In 153
154 forming the cubic spline, adjustments at the signal bound- 154
155 aries must be implemented to eliminate boundary effects. 155
156 The mean of the upper and lower envelopes is then com- 156
157 puted and subtracted from the original time series to form 157
158 a new series. If this new series satisfies the two IMF condi- 158
159 tions, it is taken as the first IMF. Otherwise, the process is 159
160 repeated on the new series, and so on, until the IMF condi- 160
161 tions are satisfied. Once the first IMF is identified, it is sub- 161
162 tracted from the original data and the residual becomes the 162
163 starting point for finding the next IMF. The procedure stops 163
164 when the residual signal fails to yield any suitable IMF can- 164
165 didates, or a preset maximum number of IMFs is extracted.¹ 165

166 The input to the EMD is *any* continuous time series. 166
167 A strong advantage of this nonparametric method is that it 167
168 does not require a stationary time series in order to accom- 168
169 plish its task. The output from the EMD consists of a resid- 169
170 ual signal and a set of n IMFs in decreasing-frequency order. 170
171 The first few IMFs cumulatively carry high-frequency com- 171
172 ponents of the original time series, which are here consid- 172
173 ered to carry extraneous information riding on the actual 173
174 signal of interest, which oscillates at a lower frequency. 174
175 These components could be caused by associated processes, 175
176 or by concurrent phenomena in the environment, or by 176
177 imperfections in the recording instruments. Summing the 177

¹ Kim and Oh (2009) have developed an *R* package called EMD that implements this procedure very efficiently. The *R* code used in these analyses is provided in the appendix.

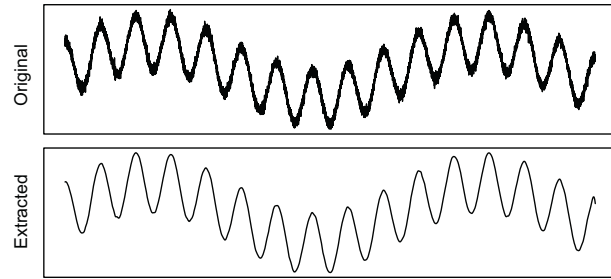


Figure 1. Original signal (top) consisting of high-frequency oscillations riding on a low-frequency signal of interest, and the low-frequency signal of interest (bottom) created by summing the last three IMFs and the residual.

178
179
180
181
182
183
184
185
186
187
188
189
190
191
192
193
194
195
196
197
198
199
200
201
202
203
204
205
206
207
208
209
210
211
212
213
214
215
216
217
218
219
220
221

residual and the last k IMFs together thus produces a time series that captures the information in which we are interested, while discarding extraneous information. Hence we refer to the resulting time series as the signal of interest.

An important goal here is determining which value of k to use. The idea is to find a sufficient number of low-frequency IMFs to capture the signal that we wish to study, with some tolerance for capturing extraneous information embedded in medium-frequency IMFs. A Fast-Fourier Transform (FFT) could be used to detect the most powerful frequencies within each IMF. Then only those IMFs whose dominant frequencies are below a desired threshold are selected. However, use of the FFT is contrary to the EMD approach, since it assumes global frequencies in the signal, while EMD is devised to identify local frequencies that are not necessarily global. A better approach uses the Hilbert-Huang Transform (HHT) applied to the IMFs (Huang, 2005; Huang et al., 1998). This transform provides the amplitude and instantaneous frequency at each time point for each IMF. The energy contained in a single IMF is the sum of the squared amplitudes. Dividing this sum by the total energy of all IMFs enables us to compute the percentage of the total energy contributed by each IMF. We then select the last k IMFs such that the percentage of the total energy contributed by their combination exceeds some chosen threshold, say 90%. Adding these to the residual produces the signal of interest. See Kim, Paek, and Oh (2008) and Wu and Huang (2004) for related applications of the HHT. Regardless of the method employed, it is informative to compare the plot of the extracted signal with that of the original signal in every case to determine whether the extracted signal appears to capture the desired trend of the original while removing sufficient extraneous information. Such a comparison may convince one to include more or fewer IMFs. For a simple example, Figure 1 shows (top panel) an obvious low-frequency sinusoidal signal with high-frequency noise. The signal of interest (bottom panel) is completely captured by adding the residual and the last three IMFs, whose combined energy is 99% of the total, while the extraneous information (the noise) is completely removed.

Once the signals of interest are extracted, the synchrony between them can then be assessed using cross-correlations. These steps are illustrated with empirical data in subsequent sections.

Synchrony Between Discrete Variables: Slope Estimation Using a SHME Model

222
223

The SHME model is a technique to detect linear associations between discrete time series. This approach is particularly suited for capturing the relationship between two time series when the variability within each time series is not constant. The first step in the application of the SHME model consists of transforming the raw signal. For example, if the observed time series consists of electrocardiogram (EKG) data (as in the current empirical application), the raw signal is transformed into a heart rate in the form of, say, beats per minute. This can be accomplished in various ways, as is illustrated in subsequent sections.

224
225
226
227
228
229
230
231
232
233
234

Once the data are transformed, each of two time series is partitioned into n segments of some specified width, where n depends on the duration of the task. The choice of the segment width is a function of both detailed information and precision. Denote these segments I_1, \dots, I_n . Consider, for example, a selected time of 5 s (5,000 ms) for the segments. Each segment I_i will consist of m_i distinct heart rate values $x_{j,i}, j = 1, \dots, m_i$, for one of the series (e.g., one person's signal), each of which lasts for k_j milliseconds, and p_i distinct heart rate values $y_{j,i}, j = 1, \dots, p_i$ for the other series (e.g., the other person's signal), each of which lasts for l_j milliseconds. Hence $5000 = k_1 + \dots + k_{m_i} = l_1 + \dots + l_{p_i}$ for $i = 1, \dots, n$. For each segment I_i , the weighted mean heart rates are then computed as

235
236
237
238
239
240
241
242
243
244
245
246
247
248

$$u_i = \frac{1}{5000} \sum_{j=1}^{m_i} k_j x_{j,i} \quad \text{and} \quad v_i = \frac{1}{5000} \sum_{j=1}^{p_i} l_j y_{j,i} \quad 250$$

for each series, respectively. Because the model requires the independence of $u_1, \dots, u_n, v_1, \dots, v_n$, we assume that the average heart rates in segments I_1, \dots, I_n are mutually independent for each subject.

251
252
253
254

Similarly, the weighted variance of the mean heart rate for each segment is approximated as

255
256

$$\sigma_i^2 \approx s_i^2 \sum_{j=1}^{m_i} \left(\frac{k_j}{5000} \right)^2 \quad \text{and} \quad \tau_i^2 \approx t_i^2 \sum_{j=1}^{p_i} \left(\frac{l_j}{5000} \right)^2, \quad 258$$

where s_i^2 and t_i^2 are the sample variances for each time series over I_i , respectively. Since these $2n$ variances are potentially different across the two series (e.g., as in two individuals in a couple), any method for estimating the linear association between $u = (u_1, \dots, u_n)$ and $v = (v_1, \dots, v_n)$ must account for heteroscedastic measurement error on each variable.

259
260
261
262
263
264
265

The SHME model with equation error assumes that

266

$$u_i = x_i + \varepsilon_i, \quad v_i = \mu_i + v_i, \quad \text{and} \quad \mu_i = \alpha + \beta_{y_i} + \gamma_i, \quad 268$$

where the independent measurement errors are $\varepsilon_i \sim \mathcal{N}(0, \sigma_\varepsilon^2)$ and $v_i \sim \mathcal{N}(0, \tau_i^2)$, and the equation error is $\gamma_i \sim \mathcal{N}(0, \sigma^2)$. The normality of the model errors is well justified, since the observations u_i and v_i are defined as the weighted average of independent random variables. Moreover, this model assumes that all error terms are mutually independent.

269
270
271
272
273
274
275

276 Under a structural model, both χ_i and μ_i are assumed to be
 277 random with unspecified but finite first and second moments.
 278 Note that the symmetry of this model would allow one to
 279 switch μ_i and χ_i in the latter model equation above, so that
 280 there is no implication of directionality. Techniques for
 281 estimating the slope β in this setting are available in the liter-
 282 ature (e.g., Cheng & Riu, 2006; Kulathinal, Kuulasmaa, &
 283 Gasbarra, 2002; McAssey & Hsieh, 2010; Patriota, Bolfarine,
 284 & de Castro, 2009). When the measurement-error variance is
 285 small, as in the application here, the method of moments
 286 (Patriota et al., 2009) provides an efficient estimate of the
 287 slope that is simple to compute. This approach will be used
 288 to estimate β and test whether it is significantly nonzero in
 289 the empirical application.

290 To this end, let

$$S_{uu} = \sum_{i=1}^n \frac{(u_i - \bar{u})^2}{n-1}, S_{uv} = \sum_{i=1}^n \frac{(u_i - \bar{u})(v_i - \bar{v})}{n-1},$$

$$S_{vv} = \sum_{i=1}^n \frac{(v_i - \bar{v})^2}{n-1}, \sigma_n^* = \sum_{i=1}^n \frac{\sigma_i^2}{n}, \tau_n^* = \sum_{i=1}^n \frac{\tau_i^2}{n},$$

$$\sigma_n^{**} = \sum_{i=1}^n \frac{\sigma_i^4}{n}, \text{ and } (\sigma\tau)_n^* = \sum_{i=1}^n \frac{\sigma_i^2 \tau_i^2}{n}.$$

292

293 Moreover, let $\sigma_\chi^2 = Var(\chi)$, $\sigma^* = \lim_{n \rightarrow \infty} \sigma_n^*$, $\sigma^{**} =$
 294 $\lim_{n \rightarrow \infty} \sigma_n^{**}$, $\tau^* = \lim_{n \rightarrow \infty} \tau_n^*$, and $(\sigma\tau)^* = \lim_{n \rightarrow \infty} (\sigma\tau)_n^*$.
 295 Then, having established that the distribution of
 296 $\sqrt{n}(\hat{\beta} - \beta)$ converges to $\mathcal{N}(0, \omega)$, the slope estimate $\hat{\beta}$
 297 and its asymptotic variance ω under this model are

$$\hat{\beta} = \frac{S_{uv}}{(S_{uu} - \sigma_n^*)} \text{ and } \omega = \frac{2\beta^2(\sigma^{**} - \sigma_\chi^4) + \pi}{\sigma_\chi^4},$$

299

300

where,

302

$$\pi = \beta^2 \sigma_\chi^2 \sigma^* + \sigma^2 \sigma_\chi^2 + (\sigma\tau)^* + \sigma^2 \sigma^* + \sigma_\chi^2 \tau^* + 2\beta^2 \sigma_\chi^4.$$

303

304

305

Thus $Var(\hat{\beta}) \approx \omega/n$ for n large. Substituting the
 parameter estimates given in Patriota et al. (2009) and sim-
 plifying, the estimated variance of $\hat{\beta}$ is

$$\widehat{Var}(\hat{\beta}) = \frac{2S_{uv}^2 [\sigma_n^{**} - (S_{uu} - \sigma_n^*)^2]}{n(S_{uu} - \sigma_n^*)^4} + \frac{S_{uv}^2 + S_{uu}S_{vv} + (\sigma\tau)_n^* - \sigma_n^* \tau_n^*}{n(S_{uu} - \sigma_n^*)^2}$$

307

308

The hypothesis $H_0: \beta = 0$ will be rejected when the ratio

309

310

311

$\hat{\beta} / \sqrt{\widehat{Var}(\hat{\beta})}$ deviates significantly from zero with respect to
 the standard normal. This procedure is illustrated with
 empirical data in subsequent sections.

312

Empirical Illustration

313

Measures and Procedures

314

315

The data in this study are from four couples who completed
 psychophysiological measurements as part of a study of dya-

Table 1. Individual- and dyad-level characteristics of the four couples

Variable	Couple	Male	Female
Attachment-related avoidance (1–7 Likert scale)	1	2.33	3.67
	2	2.61	1.39
	3	3.56	2.06
	4	1.56	1.06
Attachment-related anxiety (1–7 Likert scale)	1	2.78	3.72
	2	3.22	1.94
	3	2.78	4.39
	4	2.61	2.06
Relationship satisfaction (1–7 Likert scale)	1	6.17	6.67
	2	6.00	6.83
	3	6.83	6.17
	4	6.50	6.83
Relationship status	1		Exclusively dating
	2		Exclusively dating
	3		Exclusively dating
	4		Married
Relationship length (months)	1		41
	2		53
	3		08
	4		71

dic interactions (see Ferrer & Widaman, 2008 for details of the study). All four couples were heterosexual with ages across all participants ranging from 26 to 32 years. The first three couples defined their relationship as “exclusively dating” and the fourth coupled as “married.” Table 1 presents information about characteristics of the individuals in the couples.

Physiological measures were collected through the MP150 physiological data collection system (BIOPAC systems) and AcqKnowledge. Stimuli were administered in a computer monitor using E-prime (Psychology Software Tools, Inc.). Three autonomic response variables were recorded from each individual within the dyad simultaneously throughout the experiment. Respiration was recorded using an elastic belt that was attached to each of the participants. The belt was placed on each subject’s chest at the point of highest extension during inhalation and exhalation. The center of the belt contained a device that recorded the level of stretch within the belt at any moment, with greater stretch indicating inhalation and lower stretch indicating exhalation. Level of stretch within the belt was measured continuously at a rate of 1,000 Hz.

Thoracic impedance was measured using four spot electrodes placed at the well of the neck, back of the neck, center of the chest, and center of the back. This configuration is known formally as the Qu et al. configuration (Qu, Zhang, Webster, & Thompkins, 1986). Each spot electrode came prepared with Ag/AgCl paste, and had an adhesive collar to ensure both good conductivity as well as stationarity of the electrode during the experiment. Level of impedance was measured continuously at a rate of 1,000 Hz.

346 An EKG was recorded using a lead II configuration, with
 347 spot electrodes on the left and right torso (bipolar leads),
 348 as well as the right collarbone (unipolar lead). All spot elec-
 349 trodes came prepared with Ag/AgCl paste and also had an
 350 adhesive collar. The EKG was measured continuously at a
 351 rate of 1,000 Hz. All signals were recorded via the BIOPAC
 352 150 and sent online to an external computer for processing
 353 and analyses. The raw signals were exported to text files and
 354 processed using the software package *R* (*R* Development
 355 Core Team, 2009) for analysis.

356 Participants visited a laboratory for the physiological
 357 assessment in couples. They were instructed about the
 358 experiment and completed three tasks. During the first task
 359 (Baseline task) participants were seated in comfortable arm-
 360 chairs and instructed to relax and refrain from making bodily
 361 movements or gestures for a period of 5 min. Sleep masks
 362 were placed over the participants' eyes and the overhead
 363 lights were turned off in order to induce an environment
 364 of relaxation. The purpose of this first task was to gain a
 365 baseline signal for each individual. During the second task
 366 (Gazing task), participants were asked to gaze into one
 367 another's eyes without talking or touching each other for
 368 3 min. The purpose of this task was to engage the partici-
 369 pants into an interaction that would elicit physiological arou-
 370 sal. During the third task (In-sync task), they were instructed
 371 to try to become in-sync with each other for 3 min. The term
 372 in-sync was described to the participants as being analogous
 373 to becoming one individual, and therefore their goal would
 374 be to match their partner's physiology. They were instructed
 375 not to speak or attempt physical contact during this task, but
 376 no further clarification was provided as to what constitutes
 377 being in-sync or how to accomplish this. After the comple-
 378 tion of the three tasks, the participants were debriefed and
 379 paid for their participation. To our knowledge, none of the
 380 couples knew any of the other couples. We never had more
 381 than one couple in the laboratory at any time. All aspects of
 382 this project were approved by the correspondent Institutional
 383 Review Board for the Protection of Human Subjects.

384 Application of EMD to Respiration 385 and Impedance

386 The EMD was applied to two continuous signals, respiration
 387 and thoracic impedance. The respiration signal is a measure-
 388 ment of the expansion and contraction of the rib cage as the
 389 subject breathes, and thus oscillates about a fairly constant
 390 value at a varying frequency. The impedance measures the
 391 cyclical changes in cardiopulmonary output and thus is cor-
 392 related with heartbeat and respiration. Figure 2 displays the
 393 raw impedance signal for one individual (i.e., male) in
 394 Couple 3 during the first minute of the gazing task. As
 395 depicted in the figure, this time series includes considerable
 396 high-frequency oscillations riding on the underlying trend of
 397 interest.

398 The EMD of this impedance series produced 10 IMFs
 399 (displayed in Figure 3). Of these, only the last two IMFs
 400 were selected and added to the residual, to obtain a smoother
 401 signal. Figure 4 depicts this resulting smooth signal. Preced-

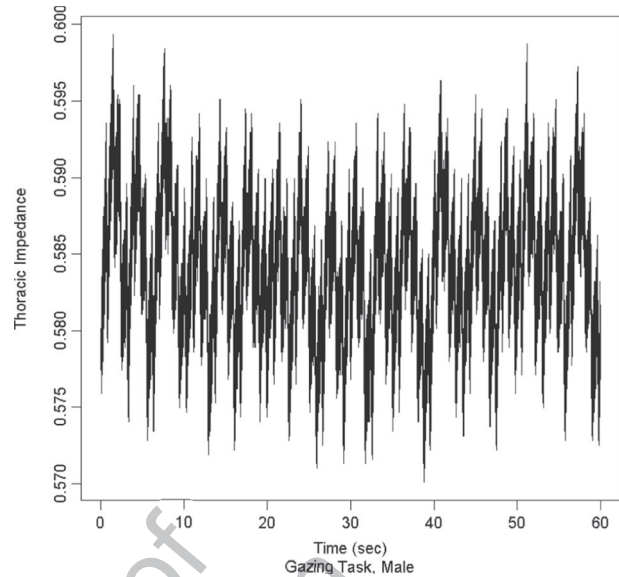


Figure 2. Male's impedance signal during gazing task for Couple 3.

ing IMFs could be added to obtain more detail, but at the
 cost of including unnecessary information. Figure 5 displays
 the resulting impedance signals of interest for both members
 of each couple during the first minute of the baseline task.

After removing the lower-frequency IMFs from each
 individual's time series across the three tasks, time segments
 of synchrony were detected between the signals of interest
 for the two individuals in each of the couples. For this, each
 pair of signals was examined using a sliding window of a
 fixed 6-s width, which moved in 2-s increments from the
 beginning to the end of each 3- to 5-min task. This choice
 of the window width and the increment size is arbitrary;
 other choices result in equivalent outputs but with different
 details. However, the 6-s width was deemed reasonable to
 capture two or three cycles of the signals, and thereby estab-
 lish a basis for detecting an occasion of synchrony between
 them. The 2-s increments allow the detection of changes in
 the synchrony on a moment-to-moment level.

At each point, the cross-correlation was then computed
 between the signals over a range of lags, and the maximum
 computed value was selected as a measure of synchrony dur-
 ing that moment. The default lag range in *R* was used, which
 is $\pm \lfloor 10 \log_{10}(3000) \rfloor = \pm 34$. This measure is referred to as
 the instantaneous coupling (IC) strength. Figure 6 displays
 the IC series for the third couple during the baseline task with
 respect to their respiration (solid line) and their impedance
 (dashed line). Note that the two series are highly correlated,
 as one would expect. Moreover, there appear to be many
 occasions during this task when the couple's physiological
 responses appear to be highly synchronized in both variables.
 The same phenomenon is found for the other couples.

For each of the three tasks in the experiment, the propor-
 tion $\hat{\pi}$ of IC values that exceeded a given threshold was then
 computed. Thresholds of .6 for the respiration and .5
 for the impedance were chosen, as these values provided

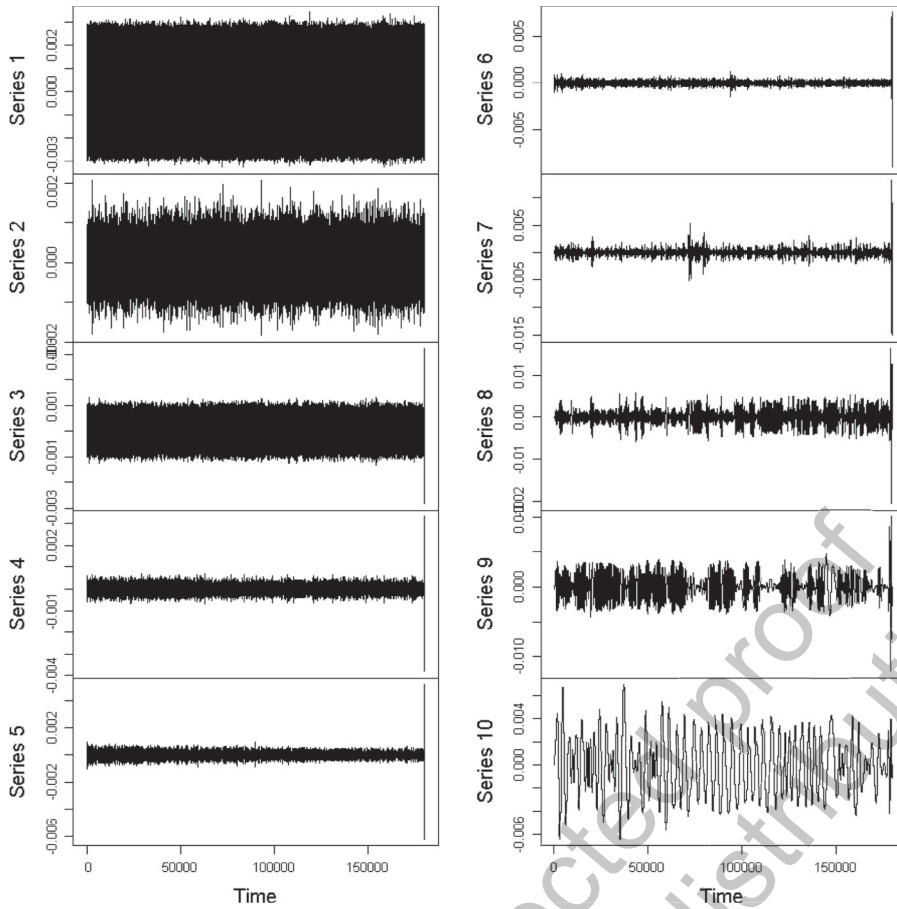


Figure 3. IMFs produced by EMD of male's impedance signal during gazing task.

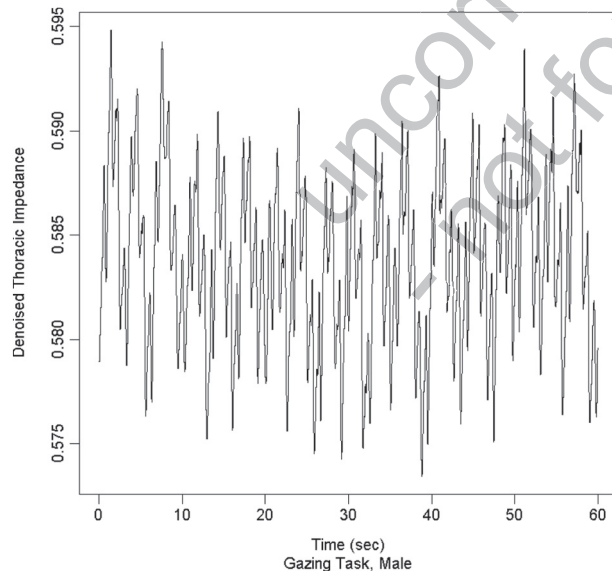


Figure 4. Male's impedance signal during gazing task, after higher-frequency IMFs are removed.

a routine hypothesis test was conducted to determine whether any subsequent proportion was significantly higher than the baseline proportion. If so, it was considered as evidence of synchronization between the individuals' physiological signals. Note that changing the threshold would not only alter the baseline proportion correspondingly, but it would also change the proportion for the second and third tasks by the same amount, so that the comparison of these proportions with the baseline proportion would not change. Table 2 displays the results of these analyses for respiration and impedance, for each of the four couples.

For respiration, the results indicate a significant increase in synchrony from baseline between the partners' signals during the in-sync task for all four couples. During the gazing task, such increase in synchrony was only evident for the first couple. With regard to impedance, the significant increase in synchrony between the partners was perceptible during the gazing task for three of the couples, and such amplification was also true for two couples during the in-sync task.

Application of SHME to Heart Rate

In the first step, the raw EKG signal during each task was transformed into a heart rate. For this, the duration of each peak-to-peak interval of the EKG waveform

a reasonable baseline proportion (i.e., not too small). Finally, the proportions above the threshold for the second and third tasks were compared with that from the baseline, and

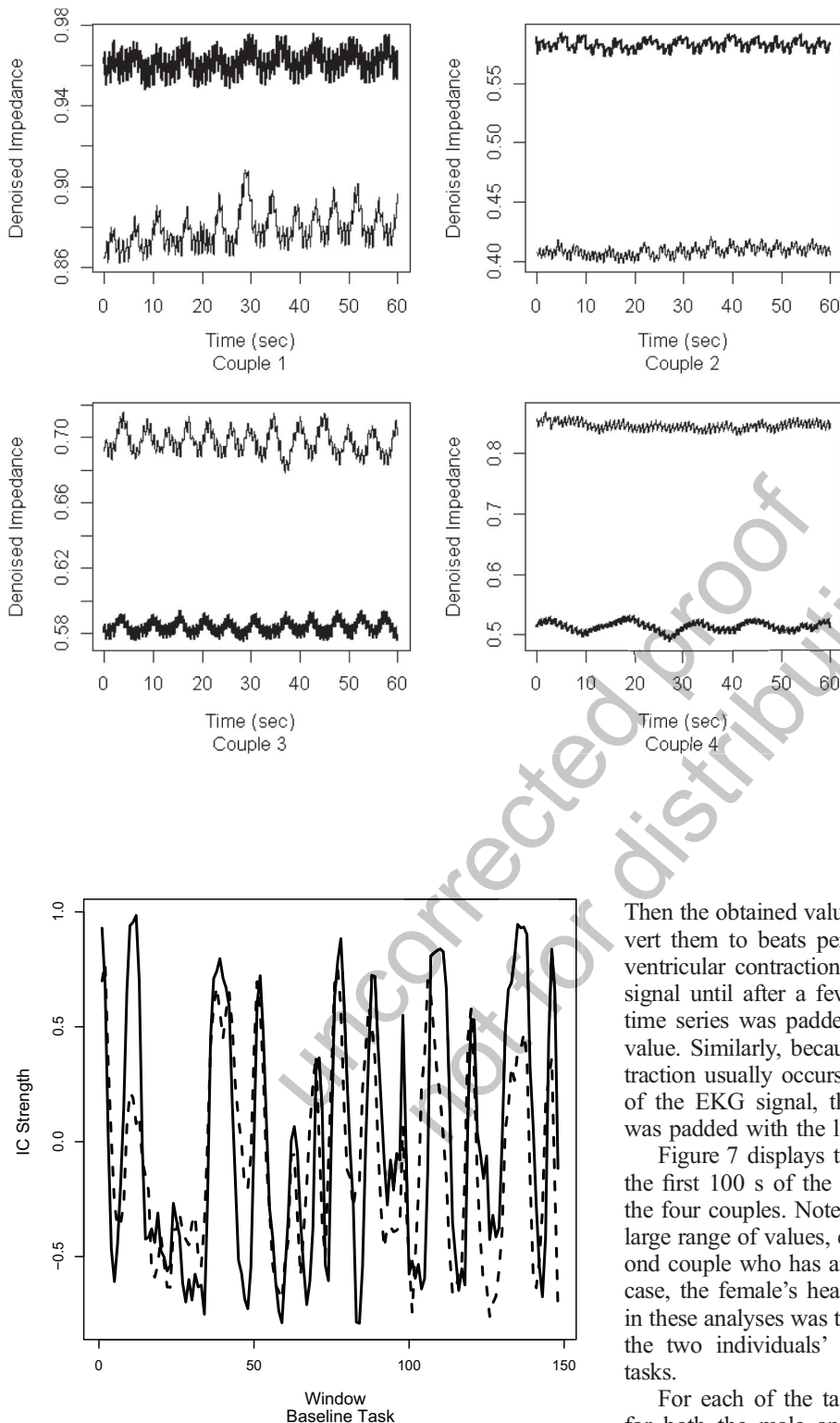


Figure 6. IC strength for Couple 3 during baseline task, with respect to respiration (solid line) and impedance (dashed line).

463
464

(in milliseconds) was determined, and its reciprocal was used to compute the heart rate (in beats per millisecond).

Figure 5. Impedance for the male (dark) and the female (light) during the baseline task for each couple, after higher-frequency IMFs are removed.

Then the obtained values were multiplied by 60,000 to convert them to beats per minute. Because the first recorded ventricular contraction usually does not occur in the EKG signal until after a few milliseconds, the beginning of the time series was padded with the first computed heart rate value. Similarly, because the last recorded ventricular contraction usually occurs a few milliseconds prior to the end of the EKG signal, the end of the heart rate time series was padded with the last computed value.

Figure 7 displays the resulting heart rate signals during the first 100 s of the baseline task for both individuals in the four couples. Note that each heart rate oscillates over a large range of values, except for that of the male in the second couple who has an almost constant heartbeat. In every case, the female's heart tends to beat faster. The objective in these analyses was to identify linear associations between the two individuals' heart rates across the experimental tasks.

For each of the tasks, the 5-min heart rate time series for both the male and female were partitioned into $n = 60$ five-second segments, following the procedure described in previous sections. The SHME model was then applied to the EKG generated data, separately for each of the four couples. The results from these analyses are presented in Table 3. These results indicate that, during the gazing task, the first couple showed a significant linear association between their heart rates. During the in-sync

465
466
467
468
469
470
471
472
473
474
475
476
477
478
479
480
481
482
483
484
485
486
487
488
489
490
491

Table 2. Significant increase in relative frequency of strong instantaneous coupling across tasks

Couple	Task	Respiration $\hat{\pi}$	p value	Impedance $\hat{\pi}$	p value
1	Baseline	.149	–	.020	–
	Gazing	.239	.048*	.102	.008**
	In-sync	.886	.000***	.011	.709
2	Baseline	.068	–	.007	–
	Gazing	.125	.080	.045	.048*
	In-sync	.659	.000***	.364	.000***
3	Baseline	.236	–	.122	–
	Gazing	.125	.988	.045	.986
	In-sync	.818	.000***	.375	.000***
4	Baseline	.216	–	.027	–
	Gazing	.114	.984	.148	.001***
	In-sync	.841	.000***	.000	.979

Note. .05 < * < .01 < ** < .001 < ***.

492 task, such synchrony between the partners' heart rates was
 493 evident for three couples. As expected, no synchrony was
 494 perceptible during the baseline task for any couple. We
 495 also present in Figure 8 a scatterplot of the heart rates
 496 for the first couple during each of the three tasks, along
 497 with the fitted line bearing the estimated slope. As can
 498 be seen, the lines accurately convey the linear trajectory
 499 of each association when such an association exists.

Cross-Validation Analysis

500 To confirm the discovery of synchrony in heart rate, respira-
 501 tion, and thoracic impedance within each of the four couples
 502 in our analyses, we applied the same methods to two mis-
 503 matched couples. For this, the male from one randomly
 504 selected couple was paired with the female from another
 505 randomly selected couple as one dyad, and this process was
 506

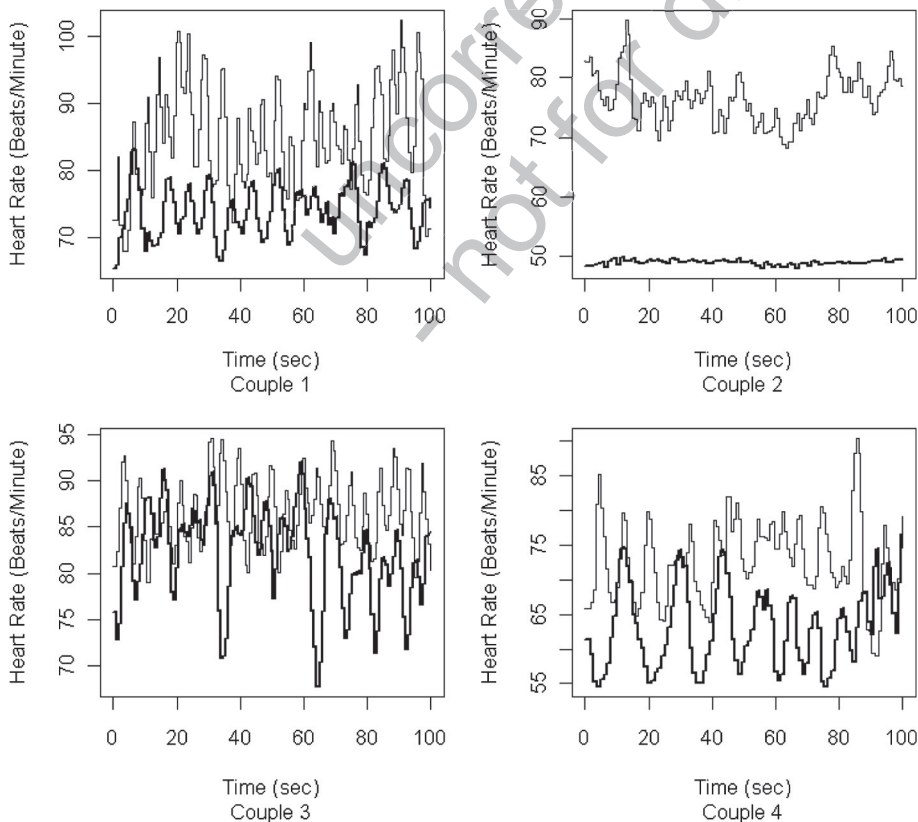


Figure 7. Heart rates for the male (dark) and the female (light) during the baseline task for each couple.

Table 3. Slope estimates for association between heart rates using the SHME model across tasks

Couple	Task	$\hat{\beta}$	$\sqrt{\widehat{Var}(\hat{\beta})}$	<i>p</i> value
1	Baseline	0.003	.274	.993
	Gazing	1.071	.212	.000***
	In-sync	1.344	.626	.032*
2	Baseline	0.358	.703	.610
	Gazing	0.504	.436	.248
	In-sync	0.579	.473	.221
3	Baseline	-0.089	.079	.254
	Gazing	0.171	.099	.083
	In-sync	0.369	.149	.013**
4	Baseline	-0.142	.185	.445
	Gazing	-0.227	.961	.813
	In-sync	0.497	.239	.037*

Note. .05 < * < .01 < ** < .001 < ***.

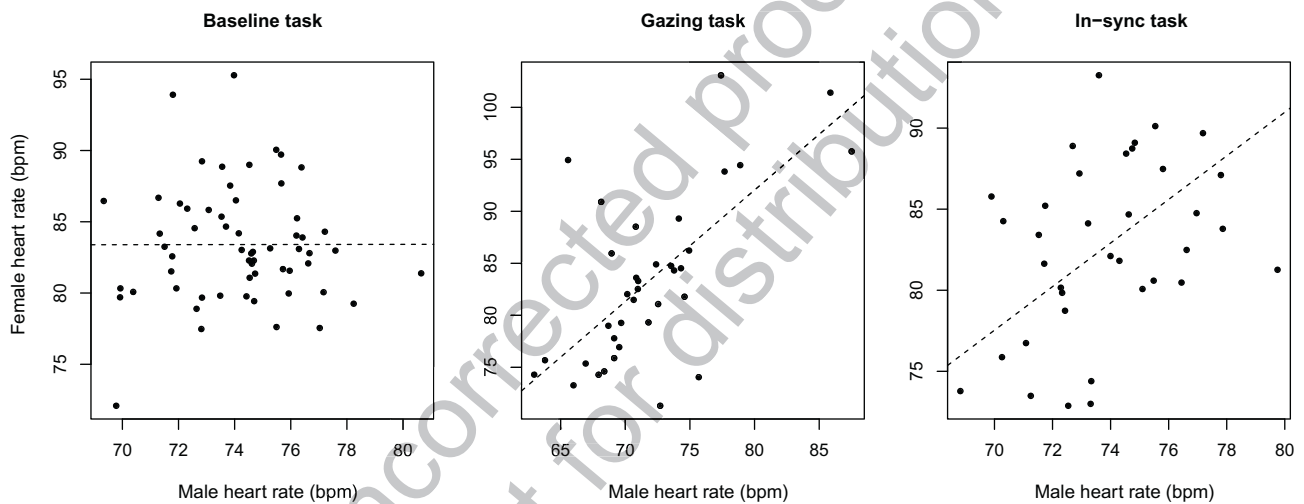


Figure 8. Scatterplots of the heart rates for the first couple during each task, with the corresponding best-fit lines.

Table 4. Measures of synchrony between heart rates, respiration, and thoracic impedance for mismatched couples across tasks

Mismatched couple	Task	$\hat{\beta}$	$\sqrt{\widehat{Var}(\hat{\beta})}$	<i>p</i> value	
1	Baseline	-11.525	12.356	.823	
	Gazing	0.250	0.206	.117	
	In-sync	-54.825	482.732	.545	
2	Baseline	0.000	0.001	.500	
	Gazing	0.023	0.022	.151	
	In-sync	0.000	0.021	.500	
Mismatched couple	Task	Respiration $\hat{\pi}$	<i>p</i> value	Impedance $\hat{\pi}$	<i>p</i> value
1	Baseline	.095	-	.041	-
	Gazing	.091	.538	.011	.930
	In-sync	.148	.118	.080	.119
2	Baseline	.230	-	.108	-
	Gazing	.091	.999	.045	.968
	In-sync	.216	.598	.114	.448

507 repeated to form a second dyad. Then the analytic procedures
508 used in the empirical analyses were implemented to detect syn-
509 chrony in heart rate, respiration, and thoracic impedance of the
510 two mismatched dyads, across the three tasks. Table 4 reports
511 the results from these cross-validation analyses. None of the
512 coefficients in these analyses reached significance for any mea-
513 sure or task (i.e., all *p* values exceeding .1), indicating no syn-
514 chrony for any of the mismatched dyads.

515 Discussion

516 Summary of Results

517 We presented in this paper two techniques for assessing syn-
518 chrony between psychophysiological time series. For respira-
519 tion and thoracic impedance, which are continuously
520 oscillating signals, we used the EMD algorithm to filter the
521 data and extract smooth versions of the time series. We
522 applied a moving window to measure the maximum cross-
523 correlation between the signals of the two individuals in
524 the couple within the window over a lag range, and to deter-
525 mine when this coupling exceeded a chosen threshold. The
526 relative frequency of high coupling values during the base-
527 line was then compared with those during the gazing and
528 in-sync tasks. Synchronization in respiration or impedance
529 was inferred when the proportion of coupling occurrences
530 increased significantly from the baseline to the experimental
531 tasks. Our findings indicate an increase in synchrony in res-
532 piration between the partners of all four couples during the
533 in-sync task, relative to the baseline. Such an increase was
534 only perceptible for one couple during the gazing task. The
535 findings for thoracic impedance show an increase in syn-
536 chrony, also relative to the baseline, during the gazing (for
537 three couples) and the in-sync (for two couples) tasks.

538 For heart rate, which is measured at discrete intervals, we
539 applied the SHME model with equation error to identify
540 synchrony between the partners' signals. Using this
541 approach, we estimated the slope representing the linear
542 association between the heart rates of the two individuals
543 in the couple during each of the three tasks. This slope
544 was taken as an indicator of synchronization between the
545 two partners' heart rates. Our findings indicate the presence
546 of synchrony between the signals of three couples during the
547 in-sync task, of one couple during the gazing task, and no
548 synchrony at all during the baseline task. Importantly,
549 cross-validation analyses provided no evidence for syn-
550 chrony when different members of a couple were randomly
551 paired, thus providing evidence for the discriminative valid-
552 ity of these synchrony detection approaches.

553 Synchronization of the physiological signals was
554 regarded as a reflection of emotional coherence between
555 the two individuals in the couples. For example, during
556 the in-sync task, participants might have concentrated on
557 matching each other's breathing – as a way to mirror their
558 partners' physiological state – thus resulting in an increase
559 in synchrony for respiration. This effect might have carried
560 over to the impedance (e.g., Ernst, Litvack, Lozano,
561 Cacioppo, & Bertson, 1999). Similarly, matching each

562 other's breathing could have resulted in an increase of the
563 coupling between the partners' heart rates. The synchrony
564 during the gazing task can also be regarded as emotional
565 coherence between the partners. In particular, this task was
566 designed to elicit physiological arousal in the participants.
567 Synchrony between the signals can then be indicative of
568 physiological coregulation between both partners, perhaps
569 as a way to cope with such arousal and provide ease or,
570 more generally, showing an activation of emotional interac-
571 tion between two intimate partners (e.g., Hatfield et al.,
572 1994). Accordingly, the methods used in these analyses
573 appear to be useful to study emotional coregulation in dya-
574 dic interactions (cf. Sbarra & Hazan, 2008). Finally,
575 although we expect the use of individual- and dyad-level
576 characteristics (e.g., as reported in Table 1) to predict syn-
577 chrony of physiological responses (e.g., higher relationship
578 satisfaction is related to lower physiological concordance
579 (Levenson & Gottman, 1983)), our sample size is not large
580 enough to detect such associations reliably.

581 Methodological Considerations 582 and Future Directions

583 The two approaches for assessing synchrony described in
584 this report present a number of benefits. For example, the
585 EMD algorithm, as a tool to parse out unwanted high-fre-
586 quency oscillations from continuous data, has two important
587 advantages over other standard methods. First, it does not
588 rely on assumptions of stationarity, assumptions required
589 by methods such as the Fourier transform. Second, in the
590 decomposition of the original series via EMD, there is no
591 leakage of energy, which is common in techniques such as
592 the wavelet transform. Moreover, in many situations, heart
593 rate data are analyzed using methods for continuous signals.
594 The heart rate signal, however, constitutes a step function,
595 since it is constant on intervals between contractions. Hence,
596 analyzing this signal as a continuous measure is not appro-
597 priate. A smoothing method could be used to transform the
598 step function into a continuous signal, but making inferences
599 using an imputed signal is hard to justify statistically.

600 A fundamental hope for the proposed statistical methods
601 is that they can be used profitably to better understand dya-
602 dic emotion regulation and coregulation. Sbarra and Hazan
603 (2008, p. 157) recently outlined a series of analyses that
604 would be needed in order to develop a more complete
605 understanding of normative attachment in human beings.
606 In outlining these analyses, they wrote, "One feasible and
607 straightforward way of testing this hypothesis would be to
608 model the physiological functioning (e.g., indices of cardio-
609 vascular responses) of each person in a relationship as a
610 bivariate system in which changes in one person's physi-
611 ology (in response to any task demands) are dependent on, not
612 only their own prior physiological state, but their partner's
613 prior physiological state as well." The methods proposed
614 here are ideally suited to answer these kinds of questions.
615 Furthermore, many psychophysiological studies rely on col-
616 lapsing data across measurement and assessment periods.
617 This is a reasonable approach in order to create highly reli-
618 able, epoch-specific variables, but, at the same time, it is a

619 fundamentally limited way of studying process. When two
620 individuals interact, it is assumed that emotional synchroni-
621 zation is a continuous process that is best studied in a man-
622 ner that is as close to the raw data as possible. The EMD and
623 SHME approaches allow for this type of data analysis.

624 One obvious extension of these analyses is the use of
625 covariates to assess the extent to which psychophysiological
626 synchronization is related to couple-level or individual differ-
627 ence variables of interest. For example, when studying intact
628 couples, the approaches described here can be examined as a
629 function of marital satisfaction or attachment styles, with the
630 degree of synchronization evidenced across a study paradigm
631 serving as an outcome variable (e.g., do more highly satisfied
632 coupled evidence greater heart rate synchronization?) as well
633 as a predictor of future relationship outcomes. In dyadic
634 interaction tasks the approaches described here can be used
635 to determine if different experimental manipulations alter
636 the physiological synchronization or linkage between people.
637 For instance, Butler, Wilhelm, and Gross (2006) examined
638 respiratory sinus arrhythmia as an indicator of emotion regu-
639 lation during a social interaction task. In studies of this kind,
640 the EMD and SHME approaches can be used to determine
641 the extent to which physiological synchronization might differ
642 across the different instructed emotion regulation tasks.
643 These applications, of course, would require the inclusion
644 of more couples in the sample.

645 Finally, this paper focused on dyadic interactions and
646 examined the synchronization between two individuals with
647 regard to a given physiological signal (i.e., respiration,
648 impedance, or heart rate). Thus, this study investigated asso-
649 ciations between two time series. An important extension of
650 this work would involve the use of multivariate time series.
651 For example, a pertinent question here is how to identify syn-
652 chronization among multiple physiological signals and then
653 across the two members of a dyad. In particular, emotion
654 researchers would be interested in examining under which
655 conditions, and to what extent, such multivariate coherence
656 is most likely to emerge (e.g., Hsieh et al., 2011; McAssey,
657 Hsieh, & Ferrer, 2010). These possible extensions notwith-
658 standing, we hope that the methods proposed in this paper
659 illustrate some new possibilities for studying physiological
660 synchrony during dyadic interactions.

661 Acknowledgments

662 This work was supported in part by grants from the National
663 Science Foundation (BCS-05-27766 and BCS-08-27021)
664 and NIH-NINDS (R01 NS057146-01) to Emilio Ferrer.

665 References

666 Anderson, C., Keltner, D., & John, O. P. (2003). Emotional
667 convergence over people over time. *Journal of Personality*
668 *and Social Psychology, 84*, 1054–1068.
669 Q1 Boker, S. M., Rotondo, J. L., Xu, M., & King, K. (2002).
670 Windowed cross-correlation and peak picking for the anal-
671 ysis of variability in the association between behavioral time
672 series. *Psychological Methods, 7*, 338–355.

Butler, E. A., Wilhelm, F. H., & Gross, J. J. (2006). Respiratory
673 sinus arrhythmia, emotion, and emotion regulation during
674 social interaction. *Psychophysiology, 43*, 612–622.
675 Cheng, C.-L., & Riu, J. (2006). On estimating linear relationships
676 when both variables are subject to heteroscedastic measure-
677 ment errors. *Technometrics, 48*, 511–519.
678 Coan, J. A. (2008). Toward a neuroscience of attachment. In J.
679 Cassidy & P. R. Shaver (Eds.), *Handbook of attachment: Theory, research, and clinical applications* (2nd ed., pp.
680 241–265). New York, NY: Guildford.
681 Coan, J. A., Schaefer, H. S., & Davidson, R. J. (2006). Lending
682 a hand: Social regulation of the neural response to threat.
683 *Psychological Science, 17*, 1032–1039.
684 Cole, P. M., Martin, S. E., & Dennis, T. A. (2004). Emotion
685 regulation as a scientific construct: Methodological chal-
686 lenges and directions for child development research. *Child*
687 *Development, 75*, 317–333.
688 Cowan, C. P., & Cowan, P. A. (2000). *When partners become*
689 *parents: The big life change for couples*. Mahwah, NJ: Erlbaum.
690 Engel, A. K., & Singer, W. (2001). Temporal binding and the
691 neural correlates of sensory awareness. *Trends in cognitive*
692 *Sciences, 5*, 16–25.
693 Engle, R. F., & Granger, C. W. J. (1987). Co-integration and
694 error correction: Representation, estimation, and testing.
695 *Econometrica, 55*, 251–276.
696 Ernst, J. M., Litvack, D. A., Lozano, D. L., Cacioppo, J. T., &
697 Berntson, G. C. (1999). Impedance pneumography: Noise as
698 signal in impedance cardiography. *Psychophysiology, 36*,
699 333–338.
700 Feldman, R. (2007). Parent-infant synchrony: Biological foun-
701 dations and developmental outcomes. *Current Directions in*
702 *Psychological Science, 16*, 340–345.
703 Ferrer, E., & Nesselroade, J. R. (2003). Modeling affective
704 processes in dyadic relations via dynamic factor analysis.
705 *Emotion, 3*, 344–360.
706 Ferrer, E., & Widaman, K. F. (2008). Dynamic factor analysis of
707 dyadic affective processes with inter-group differences. In
708 N. A. Card, J. P. Selig, & T. D. Little (Eds.), *Modeling dyadic*
709 *and interdependent data in the developmental and behavioral*
710 *sciences* (pp. 107–137). Hillsdale, NJ: Psychology Press.
711 Fries, P. (2005). A mechanism for cognitive dynamics: Neuronal
712 communication through neuronal coherence. *Trends in*
713 *Cognitive Sciences, 9*, 474–480.
714 Granger, C. W. J. (1981). Some properties of time series data and
715 their use in econometric model specification. *Journal of*
716 *Econometrics, 16*, 121–130.
717 Gottman, J. M. (1990). Time-series analysis applied to physiolog-
718 ical data. In J. T. Cacioppo & L. G. Tassinary (Eds.), *Principles*
719 *of psychophysiology: Physical, social, and inferential elements*
720 (pp. 754–774). New York, NY: Cambridge University Press.
721 Gottman, J., Swanson, C., & Swanson, K. (2002). A general
722 systems theory of marriage: Nonlinear difference equation
723 modeling of marital interaction. *Personality and Social*
724 *Psychology Review, 6*, 326–340.
725 Guastello, S. J., Pincus, D., & Gunderson, P. R. (2006). Elec-
726 trodermal arousal between participants in a conversation:
727 Nonlinear dynamics and linkage effects. *Nonlinear Dynam-*
728 *ics, Psychology, and Life Sciences, 10*, 365–399.
729 Hatfield, E., Cacioppo, J. T., & Rapson, R. L. (1994). *Emotional*
730 *contagion: Cambridge studies in emotion and social inter-*
731 *action*. Cambridge, UK: Cambridge University Press.
732 Hofer, M. A. (1984). Relationships as regulators: A psychobi-
733 ological perspective on bereavement. *Psychosomatic Medi-*
734 *cine, 46*, 183–197.
735 Hofer, M. A. (1994). Hidden regulators in attachment, separa-
736 tion, and loss. In N. A. Fox (Ed.), *The development of*
737 *emotion regulation: Biological and behavioral consider-*
738 *ations. Monographs of the Society for Research in Child*
739 *Development* (Vol. 59, pp. 250–283).
740
741

- 742 Hsieh, F., Ferrer, E., Chen, S., Mauss, I. B., Oliver, J., & Gross,
743 J. L. (2011). A network approach for evaluating coherence in
744 multivariate systems: An application to psychophysiological
745 emotion data. *Psychometrika*, *76*, 124–152.
- 746 Huang, N. E., Shen, Z., Long, S. R., Wu, M. C., Shih, H. H.,
747 Zheng, Q., . . . , Liu, H. H. (1998). The Empirical Mode
748 Decomposition and Hilbert Spectrum for nonlinear and
749 nonstationary time series analysis. *Proceedings of the Royal
750 Society London A*, *454*, 903–995.
- 751 Q2 Huang, N. E. (2005). Introduction to the Hilbert-Huang Trans-
752 form and its related mathematical problems. In N. E. Huang
753 & S. S. P. Shen (Eds.), *Hilbert-Huang Transform and its
754 applications* (pp. 1–25).
- 755 Kim, D., & Oh, H.-S. (2009). EMD: A package for Empirical Mode
756 Decomposition and Hilbert Spectrum. *The R Journal*, *1*, 40–46.
- 757 Kim, D., Paek, S. H., & Oh, H.-S. (2008). A Hilbert-Huang
758 Transform approach for predicting cyber-attacks. *Journal of
759 the Korean Statistical Society*, *37*, 277–283.
- 760 Kramer, M. A., Edwards, E., Soltani, M., Berger, M. S., Knight,
761 R. T., & Szeri, A. J. (2004). Synchronization measures of
762 bursting data: Application to the electrocorticogram of an auditory
763 event-related experiment. *Physical Review E*, *70*, 011914–03.
- 764 Kulathinal, S. B., Kuulasmaa, K., & Gasbarra, D. (2002).
765 Estimation of an errors-in-variables regression model when
766 the variances of the measurement errors vary between the
767 observations. *Statistics in Medicine*, *21*, 1089–1101.
- 768 Levenson, R. W., & Gottman, J. M. (1983). Marital interaction:
769 Physiological linkage and affective exchange. *Journal of
770 Personality and Social Psychology*, *45*, 587–597.
- 771 Levenson, R. W., & Gottman, J. M. (1985). Physiological and
772 affective predictors of change in relationship satisfaction.
773 *Journal of Personality and Social Psychology*, *49*, 85–94.
- 774 Mauss, I. B., Levenson, R. W., McCarter, L., Wilhelm, F. H., &
775 Gross, J. J. (2005). The tie that binds? Coherence among
776 emotional experience, behavior, and autonomic physiology.
777 *Emotion*, *5*, 175–190.
- 778 McAssey, M., & Hsieh, F. (2010). Slope estimation in structural
779 line-segment heteroscedastic measurement error models.
780 *Statistics in Medicine*, *29*, 2631–2642.
- 781 McAssey, M., Hsieh, F., & Ferrer, E. (2010). Optimal and robust
782 design for efficient system-wide synchronization in networks
783 of randomly-wired neuron-nodes. *Statistics and its Interface*,
784 *3*, 159–168.
- 785 Mirollo, R. E., & Strogatz, S. H. (1990). Synchronization of
786 pulse-coupled biological oscillators. *SIAM Journal on
787 Applied Mathematics*, *50*, 1645–1662.
- 788 Patriota, A. G., Bolfarine, H., & de Castro, M. (2009).
789 A heteroscedastic structural errors-in-variables model with
790 equation error. *Statistical Methodology*, *6*, 408–423.
- 791 Pikovsky, A., Rosenblum, M., & Kurths, J. (2001). *Synchroni-
792 zation: A universal concept in nonlinear sciences*. Cam-
793 bridge, UK: Cambridge University Press.
- 794 Qu, M., Zhang, Y., Webster, J. G., & Tompkins, W. J. (2006).
795 Motion artifact from spot and band electrodes during
796 impedance cardiography. *IEEE Transactions on Biomedical
797 Engineering*, *BME-33*, 1029–1036.
- 798 Quian Quiroga, R., Kraskov, A., Kreuz, T., & Grassberger, P.
799 (2002). Performance of different synchronization measures in
800 real data: A case study on electroencephalographic signals.
801 *Physical Review E*, *65*, 041903–14.
- 802 R Development Core Team. (2009). R: A language and environ-
803 ment for statistical computing. R Foundation for Statistical
804 Computing. R: A language and environment for statistical
805 computing. R Foundation for Statistical Computing,. Vienna,
806 Austria: ISBN 3-900051-07-0, Retrieved from [http://www.
807 R-project.org](http://www.R-project.org)
- 808 Sbarra, D. A., & Hazan, C. (2008). Coregulation, dysregulation,
809 self-regulation: An integrative analysis and empirical agenda
810 for understanding adult attachment, separation, loss, and
811 recovery. *Personality and Social Psychology Bulletin*, *12*,
812 141–167.
- 813 Song, H., & Ferrer, E. (2009). State-space modeling of dynamic
814 psychological processes via the Kalman smoother algorithm:
815 Rationale, finite sample properties, and applications. *Struc-
816 tural Equation Modeling*, *16*, 338–363.
- 817 Thomson, A., & Bolger, N. (1999). Emotional transmission in
818 couples under stress. *Journal of Marriage & the Family*, *61*,
819 38–48.
- 820 Weishenbush, C., Nishioka, M., Ishikawa, A., & Arakawa, Y.
821 (1992). Observation of the coupled exciton-photon mode
822 splitting in a semiconductor quantum microactivity. *Physical
823 review letters*, *69*, 3314.
- 824 Wu, Z., & Huang, N. E. (2004). A study of the characteristics of
825 white noise using the empirical mode decomposition method.
826 *Proceedings of the Royal Society A*, *460*, 1597–1611.
-
- Emilio Ferrer 828
829
-
- Department of Psychology 830
University of California 831
One Shields Ave. 832
Davis, CA 95616 833
USA 834
Tel. 1 530 752-0184 835
Fax 1 530 752-2087 836
E-mail eferrer@ucdavis.edu 837
-
- 838
- ## Appendix 839
- ### R Code for Obtaining the Empirical Mode Decomposition of a Time Series and Extracting its Trend 840–843
- ```

library(EMD) ## load EMD package previ- 844
ously installed 845
EMDResult <- emd(Series, boundary= 846
‘wave’, plot.imf=FALSE) 847
choose ‘wave boundary condition; to 848
plot IMFs, change to TRUE 849
Freq <- rep(0, EMDResult$nimf) ## Identify 850
the frequency having the 851
most 852
power for each IMF 853
for(i in 1:EMDResult$nimf) { 854
Pgram <- spec.pgram(EMDResult$imf[i], 855
taper=0, plot=FALSE) 856
Freq[i] <- min(Pgram$freq[which(P- 857
gram$spec == max(Pgram$spec))]) 858
} ## Identify the last IMF whose strongest 859
frequency is above a 860
threshold of 0.002 861
M <- min(max(which(Freq > 0.002)), EMDRe- 862
sult$nimf-1) 863
Trend <- EMDResult$residue ## Add the lat- 864
ter IMFs to the residual 865
for(i in (M+1):EMDResult$nimf) Trend <- 866
Trend + EMDResult$imf[i] 867
Trend contains the signal of interest 868
869

```