

# Hypervalence and the delocalizing versus localizing propensities of $\text{H}_3^-$ , $\text{Li}_3^-$ , $\text{CH}_5^-$ and $\text{SiH}_5^-$

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**Abstract** Lithium and silicon have the capability to form hypervalent structures, such as  $\text{Li}_3^-$  and  $\text{SiH}_5^-$ , which is contrasted by the absence of this capability in hydrogen and carbon, as exemplified by  $\text{H}_3^-$  and  $\text{CH}_5^-$  which, although isoelectronic to the former two species, have a distortive, bond-localizing propensity. This well-known fact is nicely confirmed in our DFT study at BP86/TZ2P. We furthermore show that the hypervalence of Li and Si neither originates from the availability of low-energy  $2p$  and  $3d$  AOs, respectively, nor from differences in the bonding pattern of the valence molecular orbitals; there is, in all cases, a 3-center-4-electron bond in the axial X–A–X unit. Instead, we find that the discriminating factor is the smaller effective size of C compared to the larger Si atom, and the resulting lack of space around the former. Interestingly, a similar steric mechanism is responsible for the difference in bonding capabilities between H and the effectively larger Li atom. This is so, despite the fact that the substituents in the corresponding symmetric and linear dicoordinate  $\text{H}_3^-$  and  $\text{Li}_3^-$  are on opposite sides of the central atom.

**Keywords** Carbon · Density functional calculations · Hydrogen · Hypervalence · Lithium · Silicon

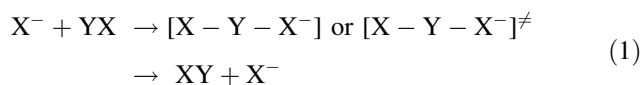
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## Introduction

Despite numerous studies, hypervalence in molecular and extended structures continues to be an issue of interest and debate, even to the extent of the meaningfulness of the concept and its very definition, already for about a century [1–5]. Here, we wish to address the different bonding capabilities of the two group-1 atoms H and Li, and two group-14 atoms C and Si. While H usually binds not more than one ligand [6] (except for some examples like the triangular  $\text{H}_3^+$ ), Li, despite being isoelectronic, can bind two or more ligands [7], thus exceeding its formal monovalence and constituting a hypervalent compound. Likewise, C can, in general, bind not more than four ligands [6] (except for some exotic or controversial examples [2, 8, 9a]), whereas its isoelectronic equivalent of the third period, i.e., Si, can bind five [2, 9–11] (or sometimes even six [2, 12]) substituents. The question we want to tackle here is, why lithium and silicon are able to violate their formal mono- and tetravalence, respectively, while hydrogen and carbon do not (or only in rudimentary form) possess this capability?

The nonhypervalence of hydrogen and carbon on one hand, and the hypervalence of lithium and silicon on the other hand, is nicely illustrated by comparing the potential energy surfaces of the corresponding  $\text{S}_{\text{N}}2$  reactions, which are of the general form:



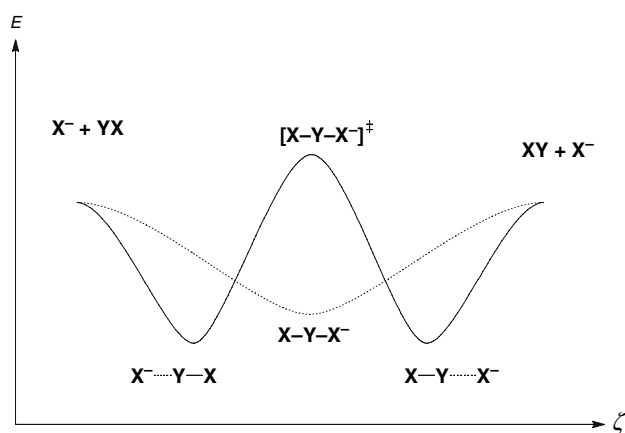
In the case of the group-1 atoms hydrogen and lithium, i.e., for  $\text{X} = \text{Y} = \text{H}$  or Li, the collinear exchange reaction of  $\text{H}^- + \text{H}_2$  proceeds via a transition state, while that of  $\text{Li}^- + \text{Li}_2$  proceeds via a stable transition complex (see also

plain and dotted lines, respectively, in Fig. 1). Thus, although the  $D_{\infty h}$  symmetric transition species  $H_3^-$  and  $Li_3^-$  are isoelectronic and structurally equivalent,  $H_3^-$  is a labile species that has the tendency to localize one of its bonds, while  $Li_3^-$  is a stable hypervalent equilibrium structure [13–15]. Likewise, in the case of the group-14 atoms carbon and silicon, i.e., for  $X = H$  and  $Y = CH_3$  or  $SiH_3$ , the hydride exchange reaction of  $H^- + CH_4$  proceeds via labile five-coordinate transition state, while that of  $H^- + SiH_4$  proceeds via a stable, pentavalent transition complex. Thus, again, although the  $D_{3h}$  symmetric species are isoelectronic and show equivalent trigonal bipyramidal geometries,  $HCH_3H^-$  is a transition state that tends to localize one of its axial C–H bond, while  $HSiH_3H^-$  is a stable transition complex [10, 11, 15–17].

Obviously, hypervalence is of relevance not only in structural chemistry but also in the field of chemical reactivity. Yet, in the present study, we focus rather on the symmetric transition species with a delocalized structure, and on the question of what causes this species to be hypervalent (i.e., stable) or nonhypervalent (i.e., with a tendency to localize one and partially break another bond). These different propensities can also be recognized in the potential energy surfaces depicted in Fig. 1.

Our first objective here is to characterize with density functional theory (DFT), the structures and the energetics of the stationary points in the above-mentioned model systems that involve hypervalently coordinated hydrogen, lithium, carbon, and silicon. To this end, we have conducted an extensive and systematic exploration of the potential energy surface (PES) of  $HCH_3H^-$ ,  $HSiH_3H^-$ ,  $H_3^-$ , and  $Li_3^-$ , using the ADF program and the generalized gradient approximation (GGA) of DFT at the BP86/TZ2P level [18].

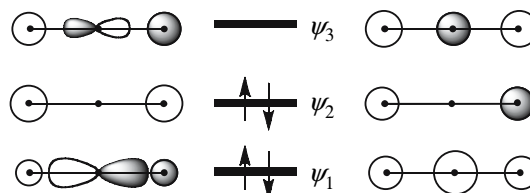
The main purpose is, however, to obtain a more qualitative, physical insight into the factors that determine *why*



**Fig. 1** Double-well (black line) and single-well (dotted line)  $S_{N2}$  potential energy surfaces of  $X^- + YX$ , along the reaction coordinate  $\zeta$

Li and Si can form hypervalent species, whereas H and C cannot. The first proposal to elucidate this puzzling problem was Pauling's idea that the hypervalence of the main group atoms in question derives from the availability of low-energy AOs, e.g.,  $2p$  and  $3d$  in the valence electron shell of lithium and silicon, respectively. However, modern ab initio calculations showed that, for providing bonding in hypervalent species, the central Si and Li atoms predominantly invoke their valence  $3s$  and  $3p$  (Si) or  $2s$  AOs (Li). The low-energy  $3d$  AOs of silicon merely act as corrective polarization functions, but not as valence orbitals [19]. This is again confirmed in the present study. On the other hand, the low-energy  $2p$  AOs have been shown to participate more actively in bonding [7b]. Here, we find, however, that their contribution is not essential for the hypervalence in  $Li_3^-$ .

Nowadays, the bonding in hypervalent species is described, instead, in terms of the 3-center-4-electron (3c-4e) bond [20]. This model was proposed simultaneously by Pimentel and Rundle [21] to account for the hypervalency of the central atom in species such as  $F_3^-$  and  $XeF_2$ . The 3c-4e bond was formulated in terms of the valence  $p_\sigma$  atomic orbitals (AOs), of a linear arrangement of three atoms that yields a well-known pattern of three MOs,  $\psi_1$ ,  $\psi_2$ , and  $\psi_3$ , similar to those shown in Scheme 1, left panel, which are bonding, nonbonding, and antibonding, respectively, with the four electrons in  $\psi_1$  and  $\psi_2$  [22]. A similar formulation in terms of the valence  $s$  orbitals was later introduced to account for the bonding in species like  $H_3^-$ , see Scheme 1 right panel.



**Scheme 1** Frontier orbitals involved in 3c-4e bonding with central  $p$  orbitals (left panel) and with central  $s$  orbitals (right panel)

Note that, whereas the 3c-4e MO model accounts for the bonding in hypervalent species, it does *not* explain *why*, for example, silicon and lithium can accommodate more ligands in their valence shell than carbon and hydrogen respectively. Indeed MO theory has so far not elucidated why similar bonding mechanisms (i.e. the 3c-4e bonds) yield, in some cases, labile species, such as  $H_3^-$  and  $CH_5^-$ , and in other cases stable minima as, for example,  $Li_3^-$  and  $SiH_5^-$ . Here we anticipate that our analyses highlight, in agreement with early work by Schleyer, Dewar or Gillespie [4, 11, 23], that steric factors are important for understanding the hypervalency of  $SiH_5^-$  and nonhypervalency of  $CH_5^-$ . Interestingly, steric factors also appear to be

responsible to account for the hypervalency of  $\text{Li}_3^-$ , as opposed to the nonhypervalency of  $\text{H}_3^-$ , even though the central atom in the latter species is only two-coordinate.

## Theoretical methods

All calculations were performed using the Amsterdam Density Functional (ADF) program developed by Baerends and others [18]. The numerical integration was performed using the procedure developed by te Velde et al. [18g, h]. The MOs were expanded in a large uncontracted set of Slater-type orbitals (STOs) containing diffuse functions: TZ2P (no Gaussian functions are involved) [18i]. The basis set is of triple- $\zeta$  quality for all atoms, and has been augmented with two sets of polarization functions, i.e.  $3d$  and  $4f$  on C and Li,  $4d$  and  $5f$  on Si and  $2p$  and  $3d$  on H. The  $1s$  core shell of carbon and lithium, and the  $1s2s2p$  core shell of silicon were treated by the frozen-core approximation [18c]. An auxiliary set of  $s$ ,  $p$ ,  $d$ ,  $f$ , and  $g$  STOs was used to fit the molecular density, represent the Coulomb, and exchange potentials accurately in each self-consistent field cycle [18j].

Equilibrium structures were optimized using analytical gradient techniques [18k]. Geometries, energies, and vibrational frequencies were computed at the BP86 level of the generalized gradient approximation (GGA): exchange is described by Slater's  $X\alpha$  potential [18l] with corrections due to Becke [18m, n] added self-consistently and correlation is treated in the Vosko-Wilk-Nusair (VWN) parameterization [18o] with nonlocal corrections due to Perdew [18p] added, again, self-consistently (BP86) [18q].

## Results and discussion

### Structures and relative energies

Initially, we focus on the geometries and relative energies of the various  $\text{XYX}^-$  species, computed at the BP86/TZ2P level of theory, which are collected in Fig. 2. Note that Fig. 2 shows relative energies of any  $\text{XYX}^-$  relative to  $\text{X}^- + \text{YX}$ . In line with previous work (see introduction), the  $D_{3h}$  symmetric five-coordinate  $\text{CH}_5^-$  (**1a**), which has two equivalent C–H bonds of 1.68 Å, is a first-order saddle-point. It has the propensity to localize one C–H bond to 1.10 Å, and stretch the other C–H bond to 3.83 Å, yielding  $\text{H}^- \cdots \text{CH}_4$  (**1b**) in  $C_{3v}$  symmetry. Whereas the five-coordinate **1a** is 40 kcal/mol above separate  $\text{H}^- + \text{CH}_4$ , the localized **1b** is at about  $-1$  kcal/mol (see Fig. 2). We note that **1b** is not the global minimum, but a second-order saddle point with two imaginary frequencies that are associated with the  $\text{H}^- \cdots \text{C-H}$  bending mode. The real

minimum is constituted by a  $C_s$  symmetric  $\text{H}^- \cdots \text{CH}_4$  species at  $-3.55$  kcal/mol in which, the hydride anion forms a hydrogen bond with one of the methane C–H bonds, to a slightly deformed methane weakly bound to the hydrogen anion via one of the hydrogen of the methane (not shown in Fig. 2).

At variance with the carbon species **1a**, the  $D_{3h}$  symmetric five-coordinate  $\text{SiH}_5^-$  (**2a**), which has two equivalent Si–H bonds of 1.64 Å, is a stable equilibrium structure without any labile, distortive mode (see Fig. 2). This pentavalent **2a** species is at  $-27$  kcal/mol relative to the separate  $\text{H}^- + \text{SiH}_4$ .

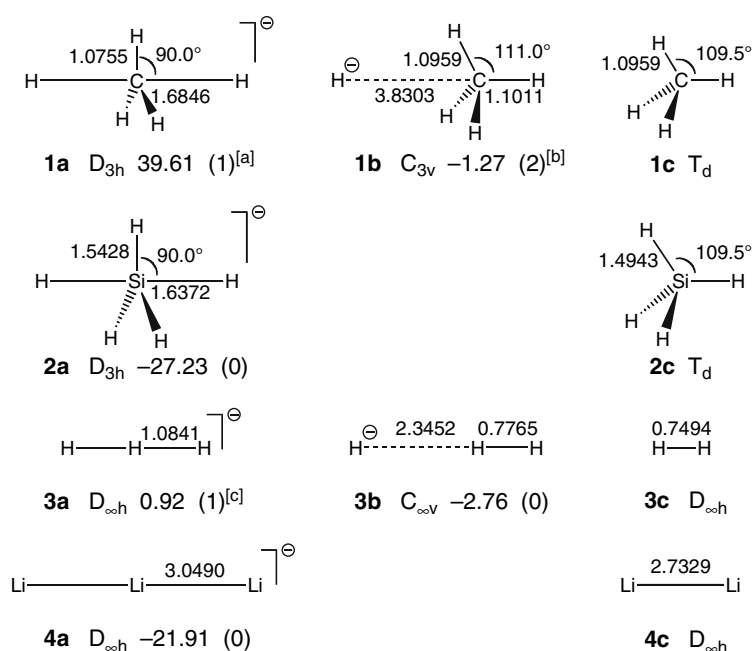
The group-1 atoms H and Li in  $A_3^-$  structures show a similar behavior as the group-14 central atoms in  $\text{AH}_5^-$ . Thus, the  $D_{\infty h}$  symmetric dicoordinate  $\text{H}_3^-$  (**3a**), which has two equivalent H–H bonds of 1.08 Å, is a first-order saddle-point with the propensity to distort toward a localized  $C_{\infty v}$  symmetric  $\text{H}^- \cdots \text{H}_2$  (**3b**) structure with a short and a long H–H bond of 0.78 and 2.35 Å, respectively (see Fig. 2). We find the dicoordinate **3a** at 1 kcal/mol above, and the localized **3b** at  $-3$  kcal/mol relative to separate  $\text{H}^- + \text{H}_2$ . At variance, the  $D_{\infty h}$  symmetric dicoordinate  $\text{Li}_3^-$  (**4a**), which has two equivalent Li–Li bonds of 3.05 Å is a stable, hypervalent species at  $-22$  kcal/mol relative to separate  $\text{Li}^- + \text{Li}_2$  (see Fig. 2).

In conclusion, all structural trends and features in potential energy surfaces computed here agree satisfactorily with earlier experimental and theoretical studies [10, 11, 13–17].

### Role of silicon $3d$ and lithium $2p$ AOs

As pointed out in the introduction, our analyses show that the availability of low-energy  $3d$  and  $2p$  AOs in silicon and lithium, respectively, is not responsible for the capability of these atoms to form hypervalent structures. This insight emerges from computations in which we removed the  $2p$  orbitals of lithium, and the  $3d$  orbitals of silicon from the respective basis sets. The net effect of deleting these low-energy AOs is destabilization of  $\text{Li}_3^-$  and  $\text{SiH}_5^-$  by 1.56 and 7.74 kcal/mol, respectively, relative to the separate reactants (not shown in Fig. 2). Importantly, however, both  $\text{Li}_3^-$  and  $\text{SiH}_5^-$  remain stable hypervalent equilibrium structures. The deletion of the low-energy  $2p$  and  $3d$  AOs does not lead to a distortive, bond localizing propensity. The only effect is the elongation in axial bond lengths compared to the computation with the full basis set. Thus, the Li–Li bonds in  $\text{Li}_3^-$  expand by 0.1038 Å compared to **4a**. The axial Si–H bonds in  $\text{SiH}_5^-$  expand by 0.0247 Å compared to **2a**, while the equatorial Si–H bonds are more or less unaffected (1.5401 Å compared to 1.5428 in **2a**). Thus, in line with previous work on other hypervalent compounds

**Fig. 2** Geometries (in Å, deg.), energies relative to reactants  $X^- + YX$  (in kcal/mol, see also Eq. 1), and number of imaginary frequencies (in parentheses) of selected species involved in bonding at C, Si, H, and Li (i.e., **1**, **2**, **3**, and **4**, respectively), computed at BP86/TZ2P. <sup>[a]</sup> i1234  $\text{cm}^{-1}$ . <sup>[b]</sup> i123  $\text{cm}^{-1}$ . <sup>[c]</sup> i1083  $\text{cm}^{-1}$



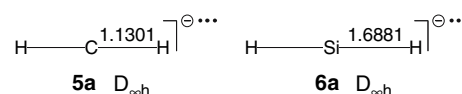
[19], we find that although the low-energy  $2p$  orbitals of lithium and the  $3d$  orbitals of silicon are important for a correct quantitative description, they are not responsible for the hypervalence of these atoms. Note that somewhat larger geometry effects in the case of Li  $2p$  deletion compared to Si  $3d$  deletion are in line with the earlier finding that lithium  $2p$  AOs participate more actively in bonding [7b].

#### Analysis of $\text{CH}_5^-$ versus $\text{SiH}_5^-$

The question remains, what *does* cause the difference in bonding capabilities between, on one hand, H and C and, on the other hand, Li and Si. Our analyses of the orbital electronic structure show that there are also no qualitative differences in terms of the presence or absence of 3c-4e bonding: this bonding pattern occurs pronouncedly in all four symmetric species, i.e.,  $\text{CH}_5^-$  and  $\text{SiH}_5^-$  (Scheme 1, left), and  $\text{H}_3^-$  and  $\text{Li}_3^-$  (Scheme 1, right).

The origin of the difference in bonding capabilities between C and Si in  $\text{CH}_5^-$  and  $\text{SiH}_5^-$ , respectively, appears to be related to the effective size of the central atom and the question if there is sufficient space to bind more than four substituents. A first indication for such steric mechanism is much larger expansion of the C–H bond in the trigonal bipyramidal  $\text{CH}_5^-$  (**1a**) compared to  $\text{CH}_4$  (**1c**), namely, by 0.59 Å, than that of the Si–H bond in  $\text{SiH}_5^-$  (**2a**) compared to  $\text{SiH}_4$  (**2c**), which amounts to only 0.14 Å (see Fig. 2).

This observation has inspired us to explore if removal of the steric bulk associated with the equatorial H substituents in  $\text{CH}_5^-$  (**1a**) would stabilize the resulting linear H–C–H anion



**Fig. 3** Geometries (in Å) of H–C–H $^{\bullet}$  (**5a**) and H–Si–H $^{\bullet}$  radicals (**6a**), computed at BP86/TZ2P

and, possibly, make it an equilibrium structure. Note that this species must be a triradical in order to have it in the valence state, that this moiety possesses in **1a**. Strikingly, this is exactly what happens as can be seen in Fig. 3. The optimized geometry of H–C–H $^{\bullet}$  is indeed stable with respect to bond localization. If we optimize H–C–H $^{\bullet}$  in  $C_{\infty v}$  symmetry the resulting species **5a** has two equivalent C–H bonds of 1.13 Å, nearly of the same length (only 0.03 Å longer) as those in  $\text{CH}_4$  (**1c**).<sup>1</sup> This agrees well with the idea that by going from five- to two-coordination, we have created sufficient space around carbon to accommodate the remaining H substituents in a stable fashion. The removal of the equatorial H substituents from  $\text{SiH}_5^-$  (**2a**) does not lead to a reduction of the Si–H bond length, in line with the picture that the larger silicon atom already had sufficient space to accommodate all five H substituents in **2a**. The resulting  $D_{\infty h}$  symmetric H–Si–H $^{\bullet}$  (**6a**) remains stable with respect to bond length alternation, and the Si–H bonds are even slightly (i.e., 0.05 Å) longer than in  $\text{SiH}_5^-$  (**2a**) (see Fig. 3).

The above results support the “steric model” of (non)hypervalence in which, the five H substituents,

<sup>1</sup> Whereas **5a** is stable with respect to C–H bond localization, it is labile with respect to H–C–H bending. The  $C_{2v}$  symmetric equilibrium structure is 2.06 kcal/mol more stable than **5a**, has an H–C–H angle of  $142^\circ$ , and C–H bonds of 1.12 Å, essentially the same as in **5a**.

especially along the axial direction, can not simultaneously approach the small carbon atom “sufficiently” close, i.e., they can not adopt an intrinsically (close-to) optimal C–H distance. This picture gains further support from the following numerical experiments. If  $\text{CH}_5^-$  (**1a**) is labile due to too long, especially axial C–H bonds, then simply displacing the central C atom along the molecular axis toward one of the axial hydrogen atoms in an otherwise frozen  $H_5$  structure (i.e., the five hydrogen substituents retain their relative positions as in **1a**), should cause a similar energy lowering, as allowing  $\text{CH}_5^-$  (**1a**) to fully relax toward  $\text{H}^- \cdots \text{CH}_4$  (**1b**). As shown in Fig. 4a, this is again exactly what happens. Note that the energy of  $\text{SiH}_5^-$ , as one might expect, increases if we carry out the corresponding numerical experiment of moving the central Si atom of **2b** toward an axial hydrogen atom, while keeping the five hydrogen atoms frozen to their geometry in **2b** (see Fig. 4a).

The same numerical experiments as shown in Fig. 4a have also been carried out in the absence of the equatorial H substituents, i.e., for  $\text{H}-\text{C}-\text{H}^{\bullet\bullet\bullet}$  and  $\text{H}-\text{Si}-\text{H}^{\bullet\bullet\bullet}$  species with frozen  $\text{H}^{\text{axial}}-\text{H}^{\text{axial}}$  distances taken from **1a** and **2a**, respectively (see Fig. 4b). As can be seen, the change in energy of these  $\text{H}-\text{C}-\text{H}^{\bullet\bullet\bullet}$  and  $\text{H}-\text{Si}-\text{H}^{\bullet\bullet\bullet}$  species (Fig. 4b) closely resembles that of the corresponding ones with the three equatorial H atoms (Fig. 4a). This suggests that as the  $\text{CH}_5^-$  species cannot accommodate all five H substituents at sufficiently short H distances, stabilization can be achieved by partially breaking (“giving up”) one of the anyway too long axial C–H bonds, and to localize the other one, yielding net stabilization. This is not necessary in  $\text{SiH}_5^-$ , because here all Si–H bonds are already relatively close to their intrinsic optimum, and localization rather destabilizes the system.

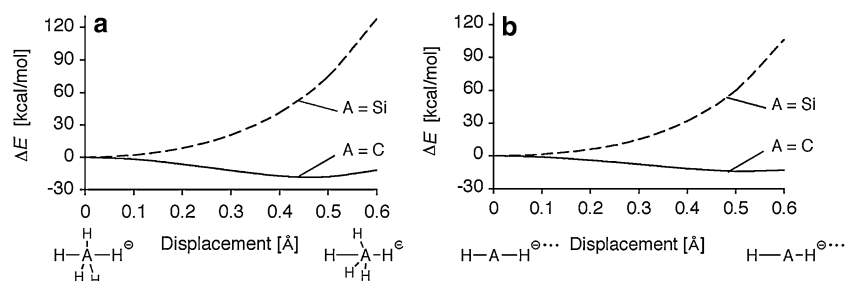
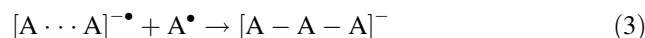
#### Analysis of $\text{H}_3^-$ versus $\text{Li}_3^-$

Thus, steric overcrowding around the smaller carbon atom in five-coordinate  $\text{CH}_5^-$  (**1a**) prevents the latter from being

stable, as opposed to the stable hypervalent  $\text{SiH}_5^-$  (**2a**), in which there is sufficient room around the larger silicon atom. Could such steric arguments also explain the difference in bonding capabilities between  $\text{H}_3^-$  and  $\text{Li}_3^-$ ? This seems not so plausible, at first sight, because the two terminal substituents in these species (**3a** and **4a** in Fig. 2) are on opposite sides of the central atom, and one might therefore expect that they are never in steric contact.

Strikingly, however, we find that steric factors make the difference between the nonhypervalent  $\text{H}_3^-$  and hypervalent  $\text{Li}_3^-$ . In the first place, the expansion of the H–H bond in the symmetric  $\text{H}_3^-$  (**3a**) compared to  $\text{H}_2$  (**3c**) is larger than that of the Li–Li bond in  $\text{Li}_3^-$  (**4a**) compared to  $\text{Li}_2$  (**4c**) (see Fig. 2). Note that, whereas in absolute numbers the bond-length expansions seem to be not so different, i.e., +0.33 versus +0.32 Å, respectively, these values correspond to an elongation by +45% for the H–H bond in **3a** compared to the much smaller expansion of +12% for the Li–Li bond in **4a**. This difference in behavior between  $\text{H}_3^-$  and  $\text{Li}_3^-$  is strongly reminiscent of the corresponding differences between  $\text{CH}_5^-$  and  $\text{SiH}_5^-$ .

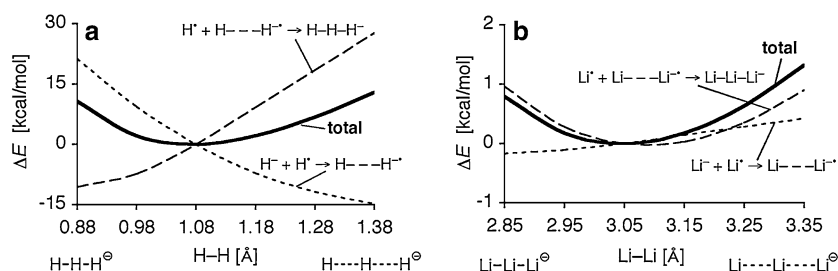
To further reveal the origin of the destabilization and H–H bond elongation in  $\text{H}_3^-$  (**3a**), we have scanned the potential energy surface as a function of a symmetric variation of both H–H bond distances, i.e.,  $D_{\infty h}$  symmetry is preserved. In Fig. 5a, one can see how the energy of  $\text{H}_3^-$  rises if, proceeding from the stationary point **3a**, the H–H distances decrease or increase. This is not unexpected, of course, and exactly the same happens in the analogous numerical experiment with  $\text{Li}_3^-$  (see Fig. 5b). It becomes interesting, however, if we decompose this net energy into two steps, corresponding with bringing together first the terminal substituents in  $[\text{A} \cdots \text{A}]^{\bullet-}$  (see Eq. 2) followed by the assembly of these substituents and the central atom  $\text{A}^{\bullet}$  to yield the overall  $\text{A}_3^-$  species (see Eq. 3,  $\text{A} = \text{H}, \text{Li}$ ):



**Fig. 4** Energy relative to the symmetric structure, (a) for  $\text{H}-\text{CH}_3-\text{H}$  and  $\text{H}-\text{SiH}_3-\text{H}$  and (b) for  $\text{H}-\text{C}-\text{H}$  and  $\text{H}-\text{Si}-\text{H}$ , as a function of the displacement of the central atom A along the

main symmetry axis toward an axial H substituent in the otherwise frozen  $\text{H}-\text{H}_3-\text{H}$  (a) and  $\text{H} \cdots \text{H}$  moiety (b), computed at BP86/TZ2P





**Fig. 5** Energy of  $D_{\infty h}$  symmetric  $\text{H}-\text{H}-\text{H}^-$  (a) and  $\text{Li}-\text{Li}-\text{Li}^-$  (b) relative to the transition state (3a) and stable transition complex (4a) structures, respectively, as a function of the A-A distance (A = H or

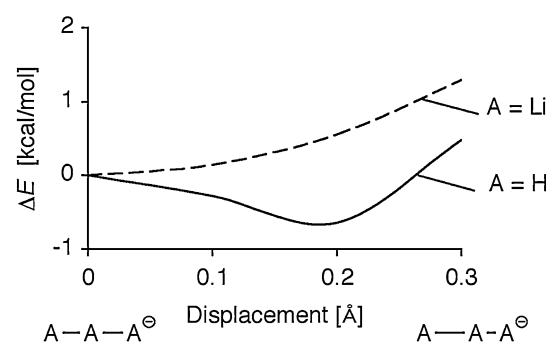
Li), computed at BP86/TZ2P. The relative energies (bold lines, designated “total”) are decomposed as indicated by the partial reactions (see also text)

As can be clearly seen in Fig. 5a, the energy of  $D_{\infty h}$  symmetric  $\text{H}_3^-$  as a function of the H-H distance is the result of a trade-off at  $\text{H}-\text{H} = 1.08 \text{ \AA}$  between, on one hand, minimizing by H-H expansion, the repulsive energy of the moiety of the outer substituents  $[\text{H} \cdots \text{H}]^\bullet$  and, on the other hand, maximizing by H-H contraction, the bonding with the central H atom. Clearly, the outer H substituents in  $\text{H}_3^-$  (3a) are in steric contact and repel each other.

The above situation for  $\text{H}_3^-$  differs dramatically from the one of  $\text{Li}_3^-$ , which is shown Fig. 5b. Here, the energy curve for the moiety of the outer substituents  $[\text{Li} \cdots \text{Li}]^\bullet$  is very shallow. Note that, in fact it is even slightly attractive at the equilibrium Li-Li distance of  $3.05 \text{ \AA}$  in 4a (see Fig. 5b). This is at variance with the  $[\text{H} \cdots \text{H}]^\bullet$  curve, which is pronouncedly repulsive around the H-H optimum in  $\text{H}_3^-$  (see Fig. 5a). Thus, the terminal Li substituents in  $\text{Li}_3^-$  (4b) only weakly interact. The driving force for the optimum Li-Li distance is predominantly the Li-Li bonding between the terminal substituents  $[\text{Li} \cdots \text{Li}]^\bullet$  and the central  $\text{Li}^\bullet$  atom (see Fig. 5b).

Thus, the direct repulsion between the terminal H atoms in  $\text{H}_3^-$  prevents them from coming sufficiently close to the central H atom. In line with this picture, displacing the central H atom in  $\text{H}_3^-$  (3a) toward one of the H substituents (while keeping the geometry of the outer substituents frozen to that in 3a) causes one strong H-H bond to be formed, which indeed goes with a stabilization of the system (see Fig. 6). A similar displacement of the central Li atom in  $\text{Li}_3^-$  (4a) yields instead a destabilization, as one might expect. This difference in behavior between  $\text{H}_3^-$  and  $\text{Li}_3^-$  is reminiscent of the difference in behavior between  $\text{CH}_5^-$  and  $\text{SiH}_5^-$ , described above.

Finally, in accordance with the steric model developed above, if we replace the central H atom in  $\text{H}_3^-$  (3a) by the larger Li atom, a stable  $D_{\infty h}$  symmetric  $\text{H}-\text{Li}-\text{H}^-$  species results. This  $\text{H}-\text{Li}-\text{H}^-$  species has two equivalent Li-H bonds of  $1.75 \text{ \AA}$ , and is at  $-55.74 \text{ kcal/mol}$  with respect to separate  $\text{H}^- + \text{LiH}$  (data not shown in the figures). The distance between the outer hydrogen substituents in  $\text{H}-\text{Li}-\text{H}^-$  ( $3.50 \text{ \AA}$ ) is significantly larger than that in  $\text{H}_3^-$  (3a:



**Fig. 6** Energy relative to the symmetric structure for  $\text{H}-\text{H}-\text{H}^-$  and  $\text{Li}-\text{Li}-\text{Li}^-$  as a function of the displacement of the central atom A (=H or Li) along the main symmetry axis toward an axial A substituent in the otherwise frozen A...A moiety, computed at BP86/TZ2P

$2.17 \text{ \AA}$ ). Consequently, the outer hydrogens in  $\text{H}-\text{Li}-\text{H}^-$  are (at variance to the situation of 3a) not in steric contact, and thus a stable hypervalent species can occur.

## Conclusions

The hypervalence of lithium and silicon as opposed to the nonhypervalence of the isoelectronic hydrogen and carbon atoms (exemplified in this theoretical study by  $\text{Li}_3^-$ ,  $\text{SiH}_5^-$ ,  $\text{H}_3^-$ , and  $\text{CH}_5^-$ , respectively) is shown to neither originate from the availability of low-energy  $3d$  and  $2p$  AOs, respectively, nor from differences in the bonding pattern of the valence molecular orbitals. In all model species analyzed, we find the 3-center-4-electron bonding pattern in the axial X-A-X unit. We show that instead the discriminating factor is the smaller effective size of C compared to the larger Si atom and the resulting lack of space around the former.

Interestingly, a similar steric mechanism appears to be responsible for the difference in bonding capabilities between H and the effectively larger Li atom. This may seem remarkable because of the fact that the substituents in the corresponding symmetric and linear dicoordinate  $\text{H}_3^-$  and  $\text{Li}_3^-$  are on opposite sides of the central atom, seemingly

out of each others way. However, the small effective size of hydrogen causes very short H–H bonds in  $H_3^-$ . This, in turn, yields a short mutual distance, less than 2.2 Å, between the terminal H atoms which, therefore, are in steric contact. The terminal Li atoms in  $Li_3^-$ , on the other hand, are separated by 6.1 Å and have virtually no steric contact.

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