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Front cover: “Circle Limit III” by M. C. Escher (computer generated picture by V. Bulatov, <http://bulatov.org>). It represents the Poincaré disk model of a 2-dimensional hyperbolic space. This type of geometry is a central topic of the present thesis, as at the core of the cosmological attractor phenomenon.

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Inflation, Universality and Attractors

PhD thesis

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