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## Efficient and accurate calibration for radio interferometers

Kazemi, Sanaz

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# Efficient and Accurate Calibration for Radio Interferometers

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**Sanaz Kazemi**

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Promotores: Prof. dr. S. Zaroubi  
Prof. dr. A.G. de Bruyn  
Copromotor: Dr. S. Yatawatta

Beoordelingscommissie: Prof. dr. W. Brouw  
Prof. dr. A.J. van der Veen  
Prof. dr. A. Leshem

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