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Published in:
Fortschritte der physik-Progress of physics

DOI:
[10.1002/prop.201200004](https://doi.org/10.1002/prop.201200004)

IMPORTANT NOTE: You are advised to consult the publisher's version (publisher's PDF) if you wish to cite from it. Please check the document version below.

Document Version
Publisher's PDF, also known as Version of record

Publication date:
2012

[Link to publication in University of Groningen/UMCG research database](#)

Citation for published version (APA):
Dibitetto, G., Guarino, A., & Roest, D. (2012). Vacua analysis in extended supersymmetry compactifications. *Fortschritte der physik-Progress of physics*, 60(9-10), 987-990. DOI: 10.1002/prop.201200004

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Vacua analysis in extended supersymmetry compactifications

Giuseppe Dibitetto*, Adolfo Guarino, and Diederik Roest

Centre for Theoretical Physics, University of Groningen, Nijenborgh 4, 9747 AG Groningen, The Netherlands

Received 11 January 2012, accepted 11 January 2012

Published online 27 January 2012

Key words Flux compactifications, extended supersymmetry, supergravity models.

We analyse geometric type IIA flux compactifications leading to $\mathcal{N} = 4$ gauged supergravities in four dimensions. The complete landscape of isotropic vacua is presented, which turns out to belong to a unique theory. The solutions admit an uplift to maximal supergravity due to the vanishing of the flux-induced tadpoles for all the supersymmetry-breaking branes. Such an uplift is sketched out and the full $\mathcal{N} = 8$ mass spectra are discussed. We find the interesting presence of a non-supersymmetric and nevertheless stable minimum.

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1 Introduction

Half-maximal and maximal gauged supergravities in four dimensions are the low-energy effective theories arising from flux compactifications in string theory, provided that only internal manifolds and extended objects are included which are compatible with such amounts of supersymmetry. In the last decade the embedding tensor formalism has been used extensively in the context of (half-)maximal supergravity in order to describe all the deformations of the free theory in a duality-covariant way. Nevertheless, it has already been pointed out in the literature that not all the gaugings of supergravity have a higher-dimensional origin in terms of a geometric flux compactification in string theory. This indicates that gaugings coming from geometric flux compactifications are not a closed set under general duality transformations and this is the origin of non-geometric fluxes [1]. Gaugings associated with such fluxes might yet have a higher-dimensional description in terms of a double field theory (DFT) [2,3], in which duality covariance becomes the fundamental principle to start with, independently of the compactification procedure. Because of this interpretation, gauged supergravities with extended supersymmetry seem to be suitable frameworks for investigating the nature of non-geometric fluxes, as summarised in Table 1.

Table 1 Half-maximal and maximal gauged supergravities in four dimensions seem to be suitable playgrounds to understand how to restore duality covariance in flux compactifications.

SUSY	G	stringy interpretation
$\mathcal{N} = 4$	$SL(2) \times SO(6, 6)$	S- and T-duality
$\mathcal{N} = 8$	$E_{7(7)}$	U-duality

After introducing the $SO(3)$ truncation of half-maximal supergravity as the effective theory arising from specific type IIA orientifold reductions with background fluxes, we analyse the landscape of isotropic vacua in geometric backgrounds, i.e. including metric and gauge fluxes. We find a set of anti-de Sitter (AdS) critical points admitting an uplift to $\mathcal{N} = 8$, one of which is remarkably stable without preserving

* Corresponding author E-mail: g.dibitetto@rug.nl, Phone: +31 (0)50 363 9043, Fax: +31 (0)50 363 4947

any supersymmetry. More details on this work can be found in [4–6]. The goal of finding de Sitter (dS) vacua motivates the analysis of non-geometric flux compactifications as possible future extensions.

2 The geometric type IIA with O6/D6 setup

Upon the $SO(3)$ truncation, half-maximal supergravity in four dimensions reduces to a three-field STU model in the following way

$$SL(2) \times SO(6, 6) \longrightarrow SL(2) \times SO(2, 2) = SL(2)_S \times SL(2)_T \times SL(2)_U . \quad (1)$$

The truncation allows for forty $SO(3)$ -singlet embedding tensor components that can be written in terms of an $SL(2) \times SO(2, 2)$ tensor $\Lambda_{\alpha ABC} = \Lambda_{\alpha(ABC)}$, with $\alpha = \pm$ and $A = 1, \dots, 4$ being $SL(2)$ and $SO(2, 2)$ fundamental indices, respectively. As shown in [4], these forty embedding tensor components correspond exactly with the set of generalised fluxes in type II orientifold reductions on a $\mathbb{Z}_2 \times \mathbb{Z}_2$ isotropic orbifold. As a consequence of the truncation, the theory preserves only $\mathcal{N} = 1$ supersymmetry out of the original $\mathcal{N} = 4$. Therefore, the corresponding scalar potential can be written in terms of a (logarithmic) Kähler potential K and a holomorphic superpotential W by using the standard $\mathcal{N} = 1$ expression

$$V^{(SO(3))} = e^K (-3|W|^2 + |DW|^2) . \quad (2)$$

At the effective level, fluxes appear as arbitrary superpotential couplings up to linear in S and up to cubic in T and U . The scalar potential computed from (2) turns out to coincide with the scalar potential given in [7] up to terms projected out by a set of $\mathcal{N} = 4$ quadratic constraints on the embedding tensor Λ [4].

Table 2 The set of $SO(3)$ -invariant embedding tensor components of Λ admitting a higher-dimensional origin as type IIA fluxes: a metric flux ω together with R-R $F_{0,2,4,6}$ and NS-NS H_3 gauge fluxes.

W couplings	Type IIA fluxes	Embedding tensor components
a_0	F_6	$-\Lambda_{+333}$
a_1	F_4	Λ_{+334}
a_2	F_2	$-\Lambda_{+344}$
a_3	F_0	Λ_{+444}
b_0	H_3	$-\Lambda_{-333}$
b_1	ω	Λ_{-334}
c_0	H_3	Λ_{+233}
c_1, \tilde{c}_1	ω	$\Lambda_{+234}, \Lambda_{+133}$

Restricting to the components of Λ that can be interpreted as metric or gauge fluxes in a type IIA realisation of the model, we are left with the following superpotential

$$W_{\text{IIA}} = a_0 - 3 a_1 U + 3 a_2 U^2 - a_3 U^3 - b_0 S + 3 b_1 S U + 3 c_0 T + (6 c_1 - 3 \tilde{c}_1) T U , \quad (3)$$

consisting of nine flux-induced couplings (see Table 2). These fluxes are demanded to satisfy the set of $\mathcal{N} = 4$ quadratic constraints

$$\begin{aligned} c_1 (c_1 - \tilde{c}_1) = 0 \quad , \quad b_1 (c_1 - \tilde{c}_1) = 0 \quad (\omega^2 = 0) \quad , \\ -a_3 c_0 - a_2 (2 c_1 - \tilde{c}_1) = 0 \quad (N_6^\perp = 0) \quad , \end{aligned} \quad (4)$$

where the first two constraints are related to the nilpotency of the twisted exterior derivative operator, whereas the third one imposes the absence of D6-branes wrapping the directions orthogonal to the O6-planes, which would break supersymmetry explicitly down to $\mathcal{N} = 1$. In contrast, D6-branes parallel to

the O6-planes are compatible with $\mathcal{N} = 4$ supersymmetry, hence being allowed. Their corresponding flux-induced tadpole reads

$$N_6^{\parallel} = 3 a_2 b_1 - a_3 b_0 = \frac{N_{O6}}{2} - N_{D6}. \tag{5}$$

After observing that the set of fluxes given in Table 2 is closed under non-compact duality transformations (i.e. real shifts and rescalings of S, T and U), we can restrict the search for critical points of the scalar potential to the point $S_0 = T_0 = U_0 = i$ without losing generality. The field equations become then quadratic conditions in the fluxes that have to be satisfied together with the quadratic constraints in (4). These equations generate a quadratic ideal which we decompose in terms of prime ideals by using the Gianni-Trager-Zacharias (GTZ) decomposition [8] with the help of *Singular* [9]. By solving them, the complete set of critical points of the scalar potential is presented in Table 3. They turn out to be (modulo the discrete \mathbb{Z}_2 symmetry introduced in the caption) different AdS critical points of a unique theory with an underlying gauging given by the gauge group $G_0 = \text{ISO}(3) \times \text{U}(1)^6$.

Table 3 The set of critical points of the scalar potential for geometric type IIA isotropic flux compactifications. The solutions labelled with 1_s turn out to preserve $\mathcal{N} = 1$ supersymmetry for $s = +1$ and to be non-supersymmetric for $s = -1$, whereas all the others are non-supersymmetric. It is worth noticing that $s = \pm 1$ appears as an accidental \mathbb{Z}_2 symmetry which relates solutions having exactly the same energy and the same mass spectrum. The parameter λ is a global scaling parameter such that $V \propto \lambda^2$.

ID	a_0	a_1	a_2	a_3	b_0	b_1	c_0	$c_1 = \tilde{c}_1$
1_s	$s \frac{3\sqrt{10}}{2} \lambda$	$\frac{\sqrt{6}}{2} \lambda$	$-s \frac{\sqrt{10}}{6} \lambda$	$\frac{5\sqrt{6}}{6} \lambda$	$-s \frac{\sqrt{6}}{3} \lambda$	$\frac{\sqrt{10}}{3} \lambda$	$s \frac{\sqrt{6}}{3} \lambda$	$\sqrt{10} \lambda$
2_s	$s \frac{16\sqrt{10}}{9} \lambda$	0	0	$\frac{16\sqrt{2}}{9} \lambda$	0	$\frac{16\sqrt{10}}{45} \lambda$	0	$\frac{16\sqrt{10}}{15} \lambda$
3_s	$s \frac{4\sqrt{10}}{5} \lambda$	$-\frac{4\sqrt{30}}{15} \lambda$	$s \frac{4\sqrt{10}}{15} \lambda$	$\frac{4\sqrt{30}}{15} \lambda$	$s \frac{4\sqrt{30}}{15} \lambda$	$\frac{4\sqrt{10}}{15} \lambda$	$-s \frac{4\sqrt{30}}{15} \lambda$	$\frac{4\sqrt{10}}{5} \lambda$
4_s	$s \frac{16\sqrt{10}}{9} \lambda$	0	0	$\frac{16\sqrt{2}}{9} \lambda$	0	$\frac{16\sqrt{2}}{9} \lambda$	0	$\frac{16\sqrt{2}}{9} \lambda$

Regarding stability at the critical points, we computed in [4] the full mass matrix for the 38 physical scalars in $\mathcal{N} = 4$ making use of the results in [10]. At this point, we can say two things: firstly, the solutions 1_s are fully stable because of (fake-) supersymmetry, and secondly the solutions 2_s are already unstable because of the presence of a tachyon whose mass is below the Breitenlohner-Freedman (BF) bound. However, this is not enough since all the critical points turn out to be compatible with the total absence of sources, i.e., the flux-induced tadpole (5) does accidentally vanish at these points. As a result, they admit an uplift to $\mathcal{N} = 8$ and hence one should analyse the full mass matrix for the 70 scalars spanning the coset $E_{7(7)}/\text{SU}(8)$ in order to make any final statement about stability. We worked out the uplifting by embedding the R -symmetry group of half-maximal theory, i.e. $\text{U}(4) = \text{U}(1) \times \text{SU}(4)$, into that of the maximal, i.e. $\text{SU}(8)$, and relating the fermionic shifts given in [7] to those ones in [11] according to the decomposition

$$\begin{array}{ccc}
 & \text{SL}(2) \times \text{SO}(6, 6) & \\
 \text{E}_{7(7)} \begin{array}{l} \nearrow \\ \searrow \end{array} & & \begin{array}{l} \searrow \\ \nearrow \end{array} \\
 & \text{SU}(8) & \underbrace{\text{U}(1) \times \text{SU}(4)_m}_{R\text{-symmetry of the } \mathcal{N}=4 \text{ theory}} \times \text{SU}(4)_a .
 \end{array} \tag{6}$$

After this uplifting, the whole set of critical points are found to satisfy the equations of motion and the quadratic constraints of the maximal theory. Subsequently we computed the mass matrix for the scalars in

the $\mathcal{N} = 8$ theory using the results in [12]. The results are summarised in Table 4. We find that the solutions 3_s are non-supersymmetric and nevertheless stable. Up to our knowledge, this is the second example in the literature (after the one in [13]) of such a solution in maximal supergravity; as opposed to the first example, though, this solution is completely tachyon-free rather than presenting tachyons although still above the BF bound. A final remark is that now, what used to be an accidental \mathbb{Z}_2 symmetry in the solutions has a proper interpretation within the $\mathcal{N} = 8$ theory, i.e. it interchanges $SU(4)_m$ and $SU(4)_a$ in Eq. (6).

ID	V_0	$m^2_{(\mathcal{N}=4)}$	$m^2_{(\mathcal{N}=8)}$	Stability
1_s	$-\lambda^2$	$-\frac{2}{3}$	$-\frac{2}{3}$	stable
2_s	$-\frac{32}{27}\lambda^2$	$-\frac{4}{5}$	$-\frac{4}{5}$	unstable
3_s	$-\frac{8}{15}\lambda^2$	0	0	stable
4_s	$-\frac{32}{27}\lambda^2$	0	$-\frac{4}{3}$	unstable

Table 4 The values of the energy and the normalised mass for the lightest scalar at the set of critical points. One observes that, when lifting from $\mathcal{N} = 4$ to $\mathcal{N} = 8$, the solutions 4_s become unstable because of the appearance of an unstable tachyonic direction within the new scalar modes. We remind the reader that in four dimensions the BF bound is given by $m_{\text{BF}}^2 = -3/4$ in units of the scalar potential.

3 Conclusions

The study of isotropic type IIA orientifolds including geometric fluxes and preserving half-maximal supersymmetry reveals the presence of only AdS vacua in the landscape. The solutions turn out to be all liftable to maximal gauged supergravity where they appear as four different critical points of a unique theory: one is supersymmetric and stable, another one is non-supersymmetric and nevertheless stable and the remaining two are non-supersymmetric and unstable. The natural extension of this work will be to study the effect of non-geometric fluxes in this setup in order to get a richer landscape, maybe even containing dS solutions.

Acknowledgements We are grateful to Andrea Borghese for stimulating discussions. The work of the authors is supported by a VIDI grant from the Netherlands Organisation for Scientific Research (NWO). Furthermore, G.D. would like to thank the organisers of the “XVII European Workshop on String Theory”, held in September 2011 in Padua, for a very stimulating experience.

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