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# EVIDENCE FOR A MILD STEEPENING AND BOTTOM-HEAVY INITIAL MASS FUNCTION IN MASSIVE GALAXIES FROM SODIUM AND TITANIUM-OXIDE INDICATORS 

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#### Abstract

We measure equivalent widths (EWs)—focusing on two unique features ( NaI and $\mathrm{TiO}_{2}$ ) of low-mass stars $\left(\lesssim 0.3 M_{\odot}\right)$ —for luminous red galaxy spectra from the Sloan Digital Sky Survey (SDSS) and X-Shooter Lens Survey (XLENS) in order to study the low-mass end of the initial mass function (IMF). We compare these EWs to those derived from simple stellar population models computed with different IMFs, ages, $[\alpha / \mathrm{Fe}]$, and elemental abundances. We find that models are able to simultaneously reproduce the observed $\mathrm{NaD} \lambda 5895$ and Na I $\lambda 8190$ features for lower-mass $\left(\sim \sigma_{*}\right)$ early-type galaxies (ETGs) but deviate increasingly for more massive ETGs, due to strongly mismatching NaD EWs. The $\mathrm{TiO}_{2} \lambda 6230$ and the $\mathrm{NaI} \lambda 8190$ features together appear to be a powerful IMF diagnostic, with age and metallicity effects orthogonal to the effect of IMF. We find that both features correlate strongly with galaxy velocity dispersion. The XLENS ETG (SDSS J0912+0029) and an SDSS ETG (SDSS J0041-0914) appear to require both an extreme dwarf-rich IMF and a high sodium enhancement $([\mathrm{Na} / \mathrm{Fe}]=+0.4)$. In addition, lensing constraints on the total mass of the XLENS system within its Einstein radius limit a bottom-heavy IMF with a power-law slope to $x \leqslant 3.0$ at the $90 \% \mathrm{CL}$. We conclude that NaI and TiO features, in comparison with state-of-the-art simple stellar population models, suggest a mildly steepening IMF from Salpeter $\left(d n / d m \propto m^{-x}\right.$ with $\left.x=2.35\right)$ to $x \approx 3.0$ for ETGs in the range $\sigma=200-335 \mathrm{~km} \mathrm{~s}^{-1}$.


Key words: dark matter - galaxies: elliptical and lenticular, cD - galaxies: evolution - galaxies: kinematics and dynamics - gravitational lensing: strong

Online-only material: color figure

## 1. INTRODUCTION

When constraining the star formation, metallicity, and gas/dust content of galaxies, the initial mass function (IMF) is often assumed to be universal and equal to that of the solar neighborhood (Kroupa 2001; Chabrier 2003; Bastian et al. 2010). However, evidence has recently emerged that the IMF might evolve (Davé 2008; van Dokkum 2008) or depend on the stellar mass of the system (e.g., Worthey 1992; Trager et al. 2000b; Graves et al. 2009; Treu et al. 2010; Auger et al. 2010a; Napolitano et al. 2010; van Dokkum \& Conroy 2010). van Dokkum \& Conroy (2010, hereafter vDC10) suggested that lowmass stars $\left(\leqslant 0.3 M_{\odot}\right)$ could be more prevalent in massive earlytype galaxies (ETGs). The increase in the mass-to-light ratio $(M / L)$ of galaxies with galaxy mass may thus be partly due to a changing IMF rather than an increasing dark matter fraction, consistent with previous suggestions (Treu et al. 2010; Auger et al. 2010b; Barnabè et al. 2011; Dutton et al. 2012; Cappellari et al. 2012). vDC10 showed that some spectral features, such as the Na i $\lambda \lambda 8183,8195$ doublet (called NaI 0.82 by CvD12), depend strongly on surface gravity at fixed effective temperature, betraying the presence of faint M dwarfs in integrated light spectra. If correct, then the low-mass end of the IMF can be inferred directly from red/near-IR spectra of old populations. Hence, the strength of the Na I doublet versus another sodium feature, such as the NaD doublet (called Na 0.59 by CvD 12 ), should provide a powerful means for separating the IMF from other effects. Specifically for the purpose of determining the low-mass IMF down to $\sim 0.1 M_{\odot}$ for metal-rich stellar populations with ages of 3-13.5 Gyr, Conroy \& van Dokkum (2012, hereafter CvD12) presented new population synthesis models. The NaD feature responds more strongly to Na -enhancement than IMF in the CvD12 models, while the Na I doublet is strong
in stars with a mass of $<0.3 M_{\odot}$ and weak or absent in all other types of stars. Unfortunately, NaI 0.82 is also sensitive to age and metallicity, and NaD is influenced by any interstellar medium (ISM). It is therefore necessary to test these models over a range of age and metallicity indicators, as well as against other lines caused by low-mass stars.

In this Letter, we focus on the NaI feature as an indicator of low-mass stars. We use NaD as an indicator of a change in sodium abundance and $\mathrm{H} \beta$ and $[\mathrm{MgFe}]$ as indicators of age and metallicity, respectively. This allows us to assess model degeneracies and deficiencies. We propose the use of the TiO feature at $\lambda 6230$ as an indicator of the presence of low-mass stars. We find that both of these features ( NaI and TiO ) correlate with galaxy velocity dispersion, implying a steepening of the IMF slope in ETGs with $\sigma>\sigma_{*}$. We assume $H_{0}=70 \mathrm{~km} \mathrm{~s}^{-1} \mathrm{Mpc}^{-1}, \Omega_{\mathrm{m}}=0.3$, and $\Omega_{\Lambda}=0.7$ throughout this Letter.

## 2. THE DATA

As part of the XLENS ${ }^{1}$ project, we obtained a UVB-VIS X-shooter spectrum of the massive and luminous early-type Sloan Lens ACS Survey (SLACS; Bolton et al. 2006) lens galaxy SDSS J0912+0029 at $z=0.1642$, with high enough signal to noise to perform stellar population analyses. The lens galaxy shows a surprisingly deep NaI0.82 feature (Figure 1), making it an extremely interesting target for studying the low-mass end of the IMF in ETGs. We measure the luminosity-weighted velocity dispersion of the lens galaxy from the reduced flux-calibrated one-dimensional UVB-VIS spectrum using the penalized pixel fitting (pPXF) code of Cappellari \& Emsellem (2004). We

[^0]

Figure 1. Galaxy (continuous lines) and model (dashed lines) spectra in the regions of the NaD (top) and NaI (bottom) features. The observed NaD EWs do not match the models for the most massive ETGs ( $\geqslant 300 \mathrm{~km} \mathrm{~s}^{-1}$ ). Na I absorption is stronger in the XLENS system and SDSS J0041-0914 and appears in both cases to require an IMF steeper than Salpeter, while the stacked SDSS spectrum shows a weaker Na i feature that matches a model with a Salpeter IMF. The bottom panels show the noise spectrum of the XLENS system.
obtain $\left\langle\sigma_{*}\right\rangle\left(\lesssim R_{\text {eff }}\right)=325 \pm 10 \pm 12 \mathrm{~km} \mathrm{~s}^{-1}$, in agreement with the previously published value ( $\sigma \simeq 313 \pm 12 \mathrm{~km} \mathrm{~s}^{-1}$; Bolton et al. 2006). We also used the spectra of $\sim 250$ galaxies with similar morphology and colors (all luminous red galaxies, hereafter LRGs) from the Sloan Digital Sky Survey (SDSS) DR8 (Aihara et al. 2011), in five velocity-dispersion bins spread over $200-335 \mathrm{~km} \mathrm{~s}^{-1}$ ( $\sim 50$ galaxies per bin). We examine one system, SDSS J0041-0914, separately because it has an NaI0. 82 feature comparably deep to the XLENS system.

## 3. STELLAR POPULATION SYNTHESIS MODELING

We use the synthetic spectra of CvD12 to analyze the stellar populations of these galaxies. The models make use of two separate empirical libraries, the MILES library covering 3500-7400 $\AA$ (Sanchez-Blazquez et al. 2007) and the Infrared Telescope Facility (IRTF) library of cool stars covering 8100-24000 $\AA$ (Cushing et al. 2005; Rayner et al. 2009). They also incorporate synthetic spectra with the purpose of investigating changes in the overall metallicity or changes in the abundances of individual elements and to cover the gap in wavelength between the two empirical libraries. We refer to CvD12 for details. The abundance variations of single elements are implemented at fixed $[\mathrm{Fe} / \mathrm{H}]$, which implies that the total metallicity

Table 1
Definition of the Index Around the Na I Doublet 8183, $8195 \AA$

| Index | Central Band <br> $(\AA)$ | Pseudo-continua <br> $(\AA)$ |
| :--- | :---: | :---: |
| NaI | $8168.500-8234.125$ | $8150.000-8168.400$ |
|  |  | $8235.250-8250.000$ |

$Z$ varies from model to model. We measure line-strength indices in the range $4000-8400 \AA$, including the standard Lick indices $\mathrm{H} \beta, \mathrm{Mg} b, \mathrm{Fe} 5270, \mathrm{Fe} 5335$, and NaD , and a TiO index $\left(\mathrm{TiO}_{2}\right)$ using the definitions of Trager et al. (1998), and the commonly used [ MgFe ] combination. ${ }^{2}$

We define a modified index around the Nai doublet $8183,8195 \AA$, which seems to be strongly dependent on the low-mass end of the IMF (Table 1). This index is slightly different from that used by vDC10 and CvD12, having a wider central index bandpass and slightly wider pseudo-continua. Our definition is more stable against velocity-dispersion variations and more suitable for massive ETGs. We convolve all the galaxy and model spectra to an effective velocity dispersion

[^1]

Figure 2. Index-index plots of the main absorption features. Lines and crosses are different SSP models from CvD12 with increasing IMF (Chabrier, Salpeter with a slope of $x=2.35$, a bottom-heavy IMF with slope of $x=3.0$ and an extremely dwarf-rich IMF with a slope of $x=3.5$ ). Points colored according to their velocity dispersions are individual SDSS galaxies, with index errors similar to SDSS J0041-0914. In the plots showing sodium, the XLENS system SDSS J0912+0029 requires a very steep IMF, violating lensing constraints on its total mass (see the text for further details). (a) $\mathrm{H} \beta$ as a function of [MgFe]. The most massive ETGs $\left(>300 \mathrm{~km} \mathrm{~s}^{-1}\right)$ best match an old stellar population ( 13.5 Gyr ) with super-solar total metallicity. Lower-mass systems are younger. (b) NaD as a function of NaI. Only low-mass ( $<250 \mathrm{~km} \mathrm{~s}^{-1}$ ) systems match the models. More massive ETGs require a higher [ $\mathrm{Na} / \mathrm{Fe}$ ] and the XLENS system and SDSS J0041-0914 also require a very steep IMF slope. (c) $\mathrm{TiO}_{2}$ as a function of $[\mathrm{MgFe}]$. The most massive ETGs require an IMF slope slightly steeper than Salpeter. A Chabrier-type IMF systematically underestimates the $\mathrm{SDSS} \mathrm{TiO}_{2} \mathrm{EWs}$. (d) $\mathrm{TiO}_{2}$ as a function of NaI. The ETGs match with the models using a Salpeter or slightly steeper IMF, but the XLENS system and SDSS J0041-0914 still do not match the SSP models well.
(A color version of this figure is available in the online journal.)
of $\sigma=335 \mathrm{~km} \mathrm{~s}^{-1}$ (the upper limit in our sample), to correct for kinematic broadening, before measuring indices. Indices in both the observed and synthetic spectra are measured with the same definitions and method (SPINDEX2; Trager et al. 2008). We do not place our indices on the zero-point system of the Lick indices and quote them as equivalent widths (EWs) in units of $\AA$, except for $\mathrm{TiO}_{2}$, which is given in magnitudes.

## 4. RESULTS AND DISCUSSION

$\mathrm{H} \beta$ is primarily an age indicator, while a combination of $\mathrm{Mg} b$, Fe5270, and Fe5335 yields information on the mean metallicity $[\mathrm{Z} / \mathrm{H}]$ of the population (Worthey 1994) while minimizing the effects of abundance ratio variations (e.g., González 1993; Trager et al. 2000a). These indices (panel (a), Figure 2) show a good agreement between the models and the galaxies EWs for old stellar populations, with an age of $13.5 \pm 3 \mathrm{Gyr}$ for $\sigma \geqslant 300 \mathrm{~km} \mathrm{~s}^{-1}$ (black points) and younger ages for lower-mass ETGs. The statistical error is deduced directly from variations in $\mathrm{H} \beta .^{3}$ The most massive ETGs have values of $[\alpha / \mathrm{Fe}]$ between solar and super-solar $(\sim 0.2)$, in good agreement with the prediction that massive galaxies have significantly super-solar abundance ratios because of rapid, high-efficiency star formation (Trager et al. 2000b; Thomas et al. 2005; Spolaor et al. 2009, 2010). Given the uncertainties in the line strengths of the two individual galaxies (SDSS J0912+0029 and SDSS J0041-0914), we are unable to

[^2]determine their ages and metallicities precisely, but their line strengths are similar to the mean of the highest-mass SDSS sample, with a deviation from the average EW smaller than $1 \sigma$ in both age and metallicity. The NaI and NaD indices can in principle be used to constrain the IMF slope (CvD12), and this relation is shown in Figure 2(b). Although the data match the models for low-dispersion systems ( $\lesssim 250 \mathrm{~km} \mathrm{~s}^{-1}$ ), the models with solar $[\mathrm{Na} / \mathrm{Fe}]$ abundance do not match the NaD strengths and only models with $[\mathrm{Na} / \mathrm{Fe}]=+0.3-+0.4$ dex match the NaD indices for higher-mass ETGs. We suggest two possible explanations for this behavior:

1. NaD is highly contaminated by the ISM for higher-mass ETGs; for example, dust lanes provide additional absorption in this resonance line (Sparks et al. 1997). Interstellar absorption within a galaxy may alter the stellar absorption profile and therefore the calculated EW, leading to an incorrect inference of the underlying stellar population.
2. Very massive ETGs have higher $[\mathrm{Na} / \mathrm{Fe}]$ abundances ( $>0.3$ dex) and slightly bottom-heavy IMFs that correlate with their stellar velocity dispersions. Therefore, if we explain the strengths of these features in giant ETGs using abundance ratios, we require an average iron abundance in excess of solar ( $[\mathrm{Fe} / \mathrm{H}] \sim 0.2$ ), and an IMF with $x=3.0$ and a high sodium abundance $([\mathrm{Na} / \mathrm{H}]>0.3)$. In the $\alpha$ enhanced bulge of the Galaxy, Fulbright et al. (2006) find an averaged $[\mathrm{Na} / \mathrm{Fe}]=0.2$ dex, and that $[\mathrm{Na} / \mathrm{Fe}] \leqslant 0.3 \mathrm{dex}$ in all stars. However, Lecureur et al. (2007) find that [ $\mathrm{Na} / \mathrm{Fe}$ ] ratios increase sharply with metallicity. They obtain values of $[\mathrm{Na} / \mathrm{Fe}] \sim 0.5$ for $[\mathrm{Fe} / \mathrm{H}]=0$ and even higher for

Table 2
Variation with IMF of $M / L$ and Stellar Mass Fraction within the Einstein Radius

| IMF Slope | $(M / L)_{\mathrm{DSEP}, B}^{*}$ | $(M / L)_{\mathrm{DSEP}, V}^{*}$ | $f_{B}^{*}$ | $f_{V}^{*}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\left(d N / d m=M^{\gamma}\right)$ | $([\alpha / \mathrm{Fe}]=0.0)$ | $([\alpha / \mathrm{Fe}]=0.0)$ | $\left(L_{\mathrm{Ein}} / M_{\mathrm{Ein}}\right) \times(M / L)_{B}^{*}$ | $\left(L_{\mathrm{Ein}} / M_{\mathrm{Ein}}\right) \times(M / L)_{V}^{*}$ |
| 2.35 | $10.2 \pm 3$ | $7.2 \pm 2$ | $0.75 \pm 0.2$ | $0.59 \pm 0.18$ |
| 3.00 | $22 \pm 6$ | $16 \pm 5$ | $1.6 \pm 0.5$ | $1.4 \pm 0.4$ |
| 3.50 | $43 \pm 13$ | $29 \pm 9$ | $2.4 \pm 0.8$ | $2.4 \pm 0.7$ |

Notes. The constraints on the mass and luminosity within the Einstein radius are taken from Auger et al. (2009) and Barnabè et al. (2009). All quantities are calculated in the rest-frame $V$ and $B$ bands.
$[\mathrm{Fe} / \mathrm{H}]>0$, but with a scatter of 0.29 dex resulting in a range of $[\mathrm{Na} / \mathrm{Fe}]$ from -0.1 to almost 1.0 . It is therefore possible for massive ellipticals to have high $[\mathrm{Na} / \mathrm{Fe}]$. In both cases, the models seem consistent with a Salpeter IMF at the low-dispersion end and a slightly bottom-heavy IMF for the high-dispersion end, if these effects are accounted for, but the models predict a steeper IMF slope of $x \sim 3.0-3.5$ for both the XLENS galaxy SDSS J0912+0029 and SDSS J0041-0914.
We note that a TiO feature at 8199 Å could partly contaminate NaI , although this feature should not vary strongly (CvD12). To test possible contamination, we use a model with $[\mathrm{Ti} / \mathrm{Fe}]=$ $\pm 0.3$ and calculate the NaI EW for a Chabrier IMF. We find that Ti enhancement only affects the NaI index by $1 \%$.

Overall, we conclude that the NaD EWs and its trend with stellar mass remain unexplained for systems with $\sigma \gtrsim$ $250 \mathrm{~km} \mathrm{~s}^{-1}$. We find that SSP models predict that TiO features also depend strongly on the slope of the low-mass end of the IMF, such as $\mathrm{TiO}_{2}$, shown in Figures 2(c) and (d). This indicator gives more support to the conclusion that the sodium strengths of the XLENS ETG, SDSS J0912+0029, still remain somewhat difficult to explain by current stellar population models, although most SDSS systems can be matched in NaI for most ETGs (if not in NaD ). Together, the $\mathrm{TiO}_{2}$ and NaI indices both imply a bottom-heavy IMF, steepening from Salpeter to possibly $x \approx 3$ for the most massive SDSS ETGs. As in Treu et al. (2010), a bottom-light IMF such as Chabrier IMF is inappropriate for the most massive ETGs.

### 4.1. Limits on the IMF from Strong Lensing

A strong case against an extreme bottom-heavy IMF can be made using the system with the strongest NaI EW (Figure 2), the XLENS galaxy SDSS J0912+0029. This system provides a hard upper limit on the stellar mass inside its Einstein radius, independent of the assumed IMF. If we assume that the SSP models are correct and that this galaxy has a high [ $\mathrm{Na} / \mathrm{Fe}$ ] abundance, we infer an IMF with a power-law slope $x=3-3.5$ (where the IMF follows $d n / d m=m^{-x}$, and the Salpeter slope is $x=2.35$ ). To assess whether these steep IMF slopes are consistent with the upper limit on the total mass, we calculate the total luminosity and the SSP stellar $M / L$ ratio in stars for each assumed IMF to infer the stellar mass fraction inside the Einstein radius $\left(R_{\text {Ein }}=\right.$ $4.55 \pm 0.23 \mathrm{kpc}$; Koopmans et al. 2006). Changes in the IMF of stars with $M \leqslant 0.3 M_{\odot}$ change the total luminosity of the lens galaxy by at most $\sim 10 \%$. Conversely, stars with masses of $0.1-0.3 M_{\odot}$ contribute $\gtrsim 60 \%$ of the stellar mass for bottomheavy IMFs with slopes steeper than Salpeter (see, e.g., Figure 2 of CvD12). To determine the stellar $M / L$ ratio, we use the isochrones at solar $[\mathrm{Fe} / \mathrm{H}]$ and $[\alpha / \mathrm{H}]$ for a 13.5 Gyr population from the Dartmouth Stellar Evolution Program (DSEP), a state-
of-the-art stellar evolution code (Chaboyer et al. 1999, 2001). We compare three different IMFs: Salpeter $(x=2.35)$, a bottom-heavy IMF ( $x=3.0$ ), and a very bottom-heavy IMF ( $x=3.5$ ). CvD12 use the same isochrones in their SSP for the bulk of the main sequence and red giant branch, except at $M<0.2 M_{\odot}$, where they use the Baraffe et al. (1998) isochrones. For each IMF, we compute the quantity

$$
f_{\mathrm{Ein}}^{*}=M^{*} / M_{\mathrm{Ein}}=\left(L_{\mathrm{Ein}} / M_{\mathrm{Ein}}\right) \times\left(M_{*} / L\right)_{\mathrm{DSEP}},
$$

where $M_{\text {Ein }}$ is a robust measurement of the total mass enclosed within the physical Einstein radius $\left(M_{\text {Ein }}=(39.6 \pm 0.8) \times\right.$ $\left.10^{10} M_{\odot}\right), L_{\text {Ein }}$ is the luminosity enclosed within the Einstein radius, evaluated using B -spline luminosity models, as a fraction of de Vaucouleurs total model luminosity $\left(L_{\text {Ein }}=(4.49 \pm 0.2) \times\right.$ $10^{10} L_{\odot}$, from Bolton et al. 2008), and ( $\left.M_{*} / L\right)_{\text {DSEP }}$ is the mass-to-light ratio from the DSEP isochrone using the appropriate IMF. The stellar $M / L$ ratio includes the contribution from stellar remnants and gas ejected from stars at the end of their life cycles. We list the results of this calculation in Table 2. For a Salpeter IMF, the stellar mass fraction of SDSS J0912+0029 in the rest-frame $V$-band is $f_{\text {Ein,Salp }}^{*}=0.59 \pm 0.15$, in agreement with previous results ( $0.60 \pm 0.09$; Auger et al. 2009). The mass-to-light ratio calculated from the DSEP isochrone for a Salpeter IMF is $M / L_{V}=7.2 \pm 2(M / L)_{\odot}$ in the $V$ band and $M / L_{B}=10.2 \pm 3(M / L)_{\odot}$ in the $B$ band. The latter value is consistent with the upper limit of $M / L_{B} \leqslant 9.08(M / L)_{\odot}$ derived from dynamical models of Barnabè at al. (2009) under the maximum bulge hypothesis. An IMF slope of $x=3.5$ yields $M / L_{V}=29 \pm 9(M / L)_{\odot}$, and $M / L_{B}=43 \pm 13(M / L)_{\odot}$ corresponding to $f_{\text {Ein } 3.5}^{*}=2.4 \pm 0.8$, inconsistent with the total lensing mass within the Einstein radius at the $>95 \%$ confidence level. An IMF of $x=3.0$ in the $B$ band is also excluded at the $>90 \%$ level, as this corresponds to a fraction $f_{\text {Ein } 3.0, B}^{*}=1.6 \pm 0.5$. For both of the bottom-heavy IMFs in the $B$ band and for the $x=3.5 \mathrm{IMF}$ in the $V$ band, we obtain a stellar mass fraction within the Einstein radius in excess of unity, thereby violating the lensing constraint on the total mass of the system at the $>90 \% \mathrm{CL}$. The $x=3$ model is only marginally consistent in the $V$ band, but $f_{\text {Ein, } 3.0, V}^{*}=1.4 \pm 0.4$ implies that there is no dark matter within the Einstein radius.

### 4.2. Systematic Uncertainties

The uncertainty on the value of $f_{\text {Ein }}^{*}$ has a number of contributions. The uncertainties in the mass and luminosity determinations from lensing are much smaller than differences in the values of $M / L$ arising from the use of different stellar population evolution models. The emerging picture is that, for a fixed IMF, it is difficult to constrain $M / L$ estimates to much higher accuracy than 0.1 dex (Gallazzi et al. 2008; Marchesini et al. 2009; Longhetti \& Saracco 2009; Conroy et al. 2009, 2010). We examine mass-to-light ratios predicted for different

IMF from different stellar population models in the rest-frame $V$ and $B$ bands and compare predictions from Worthey (1994), Bruzual \& Charlot (2003), Maraston (2005), and Vazdekis et al. (2010) for single stellar populations with ages $11.2-14.1 \mathrm{Gyr}$, and solar $(Z=0.02)$ or super-solar metallicity $(Z=0.05)$. For each SSP and each IMF, we calculate an average value and a standard deviation that we associate with the inferred values of $M / L$. Changing the $[\mathrm{Fe} / \mathrm{H}]$ abundance from 0 to 0.22 yields a $\sim 9 \%$ uncertainty on $M / L$, while changing the age of the stellar population changes $M / L$ by $\sim 20 \%$ at fixed IMF. The latter is the dominant contribution to the final uncertainties. We propagated these errors into the stellar mass fraction. The errors on the stellar mass fractions in Table 2 include both the random error contribution and the systematic uncertainties due to the use of a different set of isochrones, bands, and stellar population age and metallicity uncertainties.

## 5. CONCLUSIONS

In this Letter, we have studied the NaI $\lambda 8190$ and TiO $\lambda 6230$ features-both indicators of low-mass $\left(<0.3 M_{\odot}\right)$ stars in massive ETGs-as a function of each other, of age and metallicity indicators ( $\mathrm{Mg} b, \mathrm{Fe}$, and $\mathrm{H} \beta$ ), of NaD , and of stellar velocity dispersion. We find the following: (1) the observed $\mathrm{NaI}-\mathrm{NaD}$ trend depends strongly on stellar velocity dispersion of ETGs and only matches current state-of-the-art SSP models for ETGs with $\sigma \lesssim 250 \mathrm{~km} \mathrm{~s}^{-1}$. The most extreme NaI index strength in our sample is found in a gravitational lens system, which should have an IMF slope of $x \gtrsim 3$ based on the best current SSP models. The total enclosed mass of this system, however, excludes slopes steeper than $x=3.0$ at the $>90 \% \mathrm{CL}$ or slopes steeper than $x=3.5$ at the $>95 \%$ CL. We conclude that the NaD feature is still affected by as-of-yet not understood processes in the more massive ETGs ( $\sigma>250 \mathrm{~km} \mathrm{~s}^{-1}$ ). A full spectral comparison, in combination with lensing and dynamical constraints, is planned to further strengthen these results and assess whether NaI and NaD (in some instances) are contaminated. (2) We find that the TiO feature at $\lambda \sim$ $6230 \AA\left(\mathrm{TiO}_{2}\right)$ is a particularly promising feature to decouple the IMF from age, metallicity, and abundance pattern of the stellar population, especially when combined with metallicitydependent indices. We find that this feature correlates well with NaI, if the two most extreme cases as discussed in the text are excluded. This correlation can be a crucial piece of evidence against interstellar contamination of the NaI $\lambda 8190$ sodium absorption lines, although this does not solve the problem of NaD absorption. If strong NaI features are indeed not due to ISM contamination, then very massive ETGs have higher [ Na / Fe ] abundances ( $>0.3$ dex) and slightly bottom-heavy IMFs, correlated with their stellar velocity dispersions. We also find a clear trend of an increasing IMF slope between $\sigma=200$ and $335 \mathrm{~km} \mathrm{~s}^{-1}$ from Salpeter $(x=2.35)$ to $x \approx 3.0$, in agreement with the XLENS system, which excludes steeper IMFs at the high-mass end.

Our results are the first SSP-based indications of a steepening of the low-mass end of the IMF with increasing galaxy mass within the class of LRG/ETGs. Our results (1) support a similar trend first found by Treu et al. (2010), (2) extend the evidence based on SSP models that the IMF steepens from spiral to ETGs (vDC10), (3) suggest that NaI and NaD (in some instances) could be contaminated by interstellar absorption, and (4) support a similar trend found by Cappellari et al. (2012) based on stellar kinematics. The upper limit of $x \lesssim 3$, based on one of the most
massive ETGs in our sample, a gravitational lens, also supports our previous similar finding (Spiniello et al. 2011).

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[^0]:    1 The X-Shooter Lens Survey, Spiniello et al. (2011).

[^1]:    ${ }_{2}[\mathrm{MgFe}]=\sqrt{(\mathrm{Fe} 5270+\mathrm{Fe} 5335) / 2 \times \mathrm{Mg} b}$, González (1993).

[^2]:    3 For stellar populations with ages $>10 \mathrm{Gyr}$, an uncertainty of $0.1 \AA$ in $\mathrm{H} \beta$ corresponds to 1 Gyr uncertainty in the age (cf. Worthey 1994).

