

University of Groningen

Envelope Surfaces, Surface Design and Meshing

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Envelope Surfaces

Surface Design and Meshing

Nico Gerard Hugo Kruithof

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