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Numerical simulation of two-phase flow in offshore environments

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Numerical Simulation of Two-Phase Flow in Offshore Environments

Rik Wemmenhove

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