
Specification, estimation and validation of a pedestrian walking behavior model

Gianluca Antonini

Javier Cruz

Michel Bierlaire

Thomas Robin

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Motivation

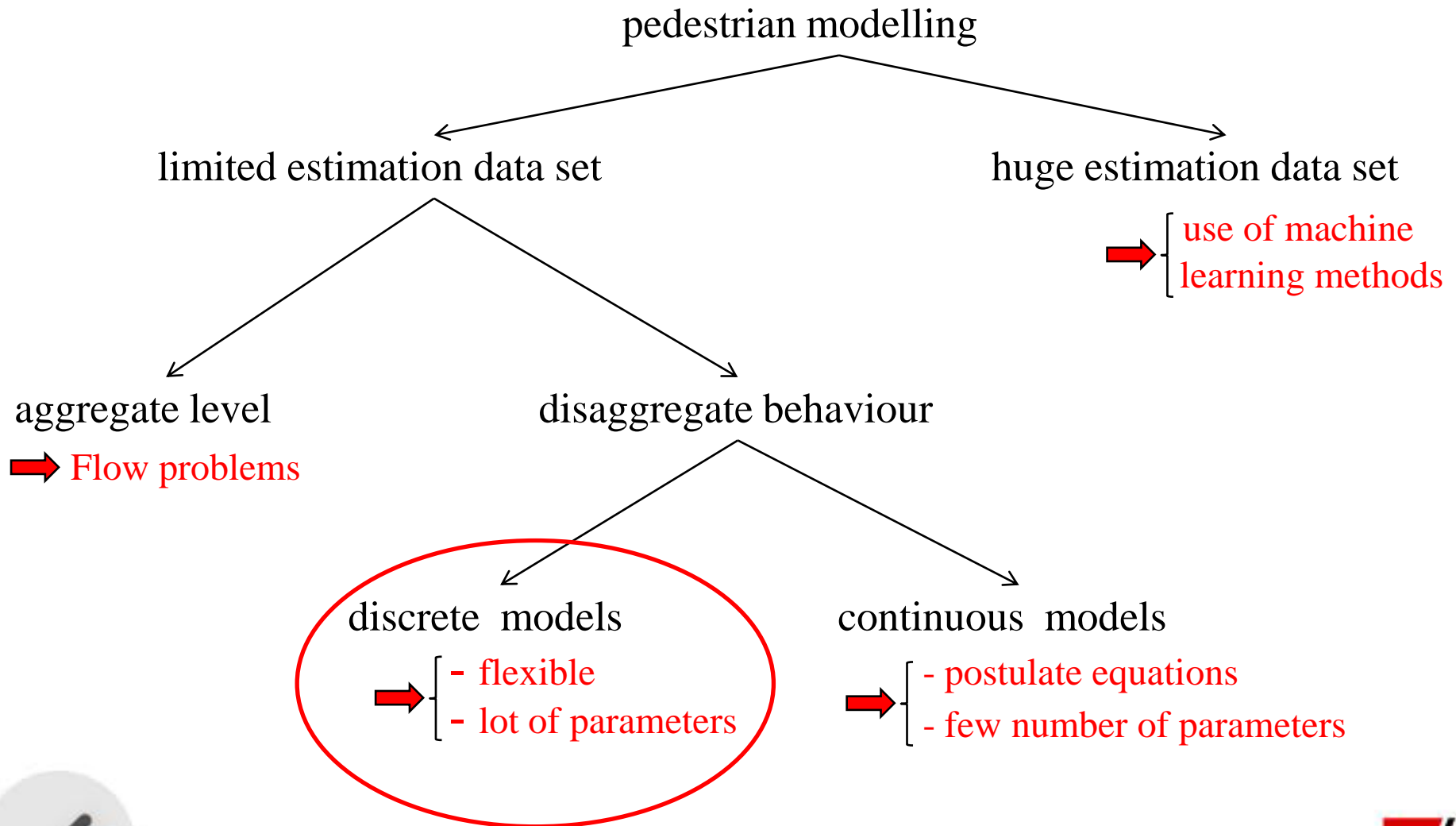
- Model the pedestrian behaviour



Motivation

- Model of the pedestrian behaviour
 - ➔ **incorporate the model in more global models**
- Use of econometric models
 - ➔ **visibility and control of the specification**
- Calibration on real data
 - ➔ **estimated parameters values**

State of the art



Objectives

- Model the pedestrian behaviour at **operational** level
- Develop a specification with ‘**constrained**’ and ‘**unconstrained**’ parameters
- **Estimate** the model
- **Validate** the model
- Implement the model in a **simulator**

Outline

- **Introduction**
- **Discrete choice models**
- **Model specification**
- **Model estimation**
- **Model validation**
- **Simulator**
- **Conclusion**

Introduction

- **Microscopic model** : capture the behavior of **each** pedestrian

➔ **Discrete choice model**

- Different **behavioral levels** :

Strategical : destination

Tactical : route choice

Operational level : short range behavior

instantaneous decisions

} **Fixed**

- Concept of **personal space** : interactions with other pedestrians

Leader follower

Collision avoidance

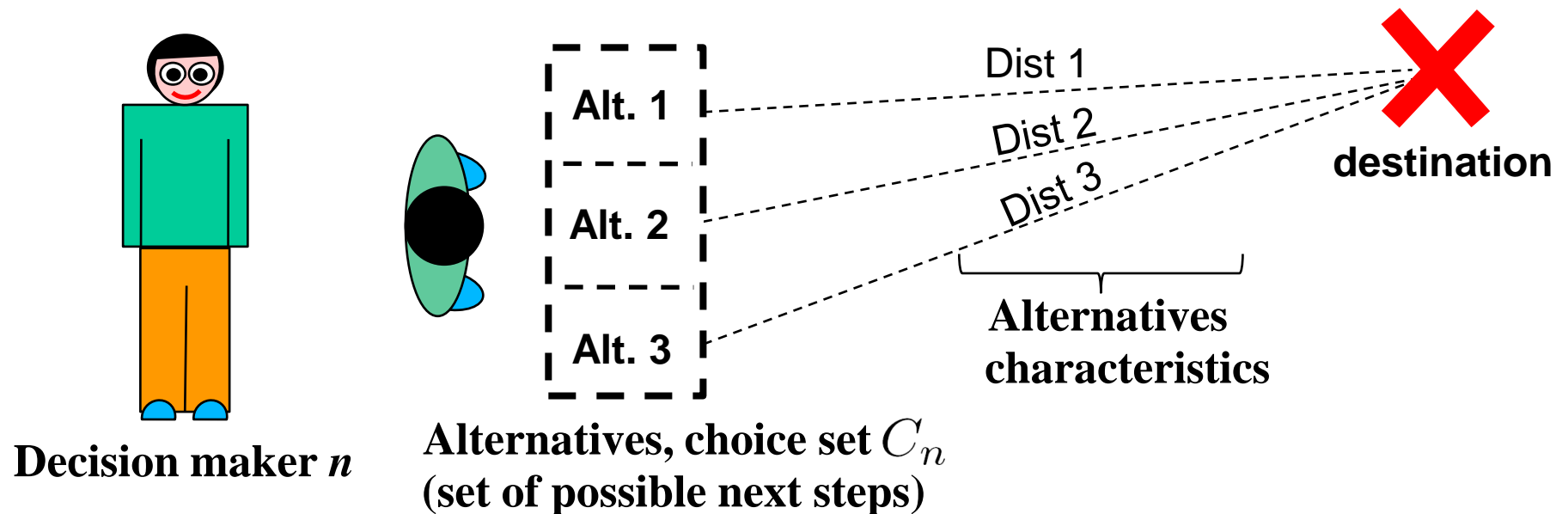
-
- Introduction
 - **Discrete choice models**
 - Model specification
 - Model estimation
 - Model validation
 - Simulator
 - Conclusion

Discrete choice models : introduction

- **Econometric** models developed since the 50's
- **Disaggregate** model
- A choice theory defines :
 - **a decision maker** : each pedestrian
 - **alternatives** : possible immediate future steps
 - **attributes of alternatives** : characteristics
 - **decision rule** : utility maximisation theory

Discrete choice model : our context

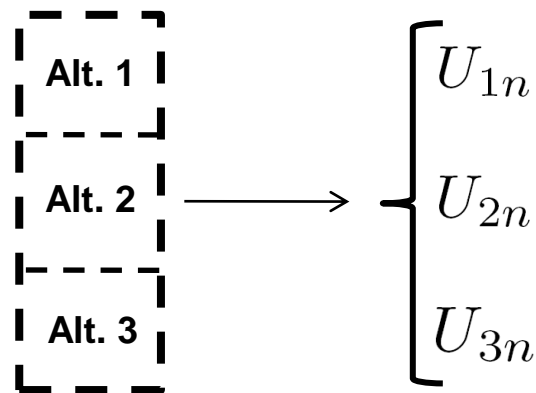
- At **each step** the pedestrian has to choose the next step in a choice set
- **Example** : only considering distance toward destination




→ Which alternative will he choose?

Discrete choice model : decision rule

- **Utility maximisation theory**
- Association of a function, called **utility** to each alternative
- It depends on the **alternative i** , and on the **decision maker n**



 The decision maker n will choose the alternative i which has the **higher utility**

Discrete choice model : utility function

- Utility is a **latent concept**
 - It can not be directly observed
 - Decision maker: stochastic decision rules
 - Analyst: Lack of information
- } **Uncertainty**

$$U_{in} = V_{in} + \epsilon_{in}$$

V_{in} : **deterministic part of the utility of alternative i for individual n**

ϵ_{in} : **error term, different assumptions can be made on its distribution**

Discrete choice model : utility specification

- **Example** : V_{in} depends only on the distance toward the destination

$$V_{in} = \beta dist_i$$

β : unknown parameter, **has to be estimated from the data**

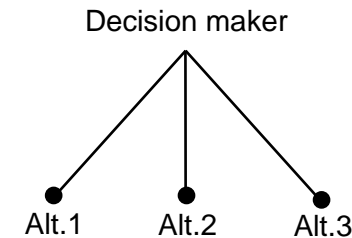
$dist_i$: distance between alternative i and the final destination

 **How do we estimate β ?**

Discrete choice model : error term

- **Example** : suppose ϵ_{in} independent and identically distributed (iid) with an extreme value distribution

➔ **Multinomial Logit model**



$P_n(i|C_n)$: probability for the individual n to choose the alternative i

$$P_n(i|C_n) = \frac{e^{V_{in}}}{\sum_{j \in C_n} e^{V_{jn}}}$$

C_n : Choice set, depends on the individual n

Discrete choice model : likelihood

- Maximisation of the likelihood function

$$l(\beta) = \prod_{n \in N} \prod_{i \in C_n} (P_n(i|C_n))^{y_{in}} = \prod_{n \in N} \prod_{i \in C_n} \left(\frac{e^{\beta \text{dist}_i}}{\sum_{j \in C_n} e^{\beta \text{dist}_j}} \right)^{y_{in}}$$

y_{in} : indicator equals to 1, if individual n has chosen alternative i , 0 otherwise

N : set of individuals in the population

- In practice use of the log-likelihood (numerical reasons)

$$L(\beta) = \sum_{n \in N} \sum_{i \in C_n} y_{in} \log \left(\frac{e^{\beta \text{dist}_i}}{\sum_{j \in C_n} e^{\beta \text{dist}_j}} \right)$$

 β estimated from the data

Why using a discrete choice model?

- **Disaggregate**

 - ➔ capture the behaviour of each pedestrian

- **Flexible**

 - ➔ easy to add behavioural modules

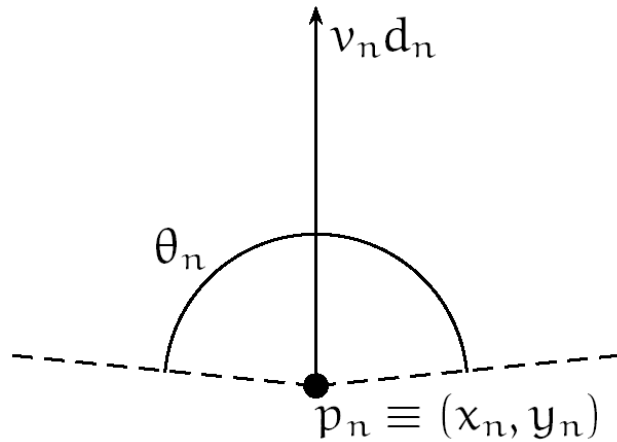
 - ➔ easy to add pedestrians characteristics

- **Estimation**

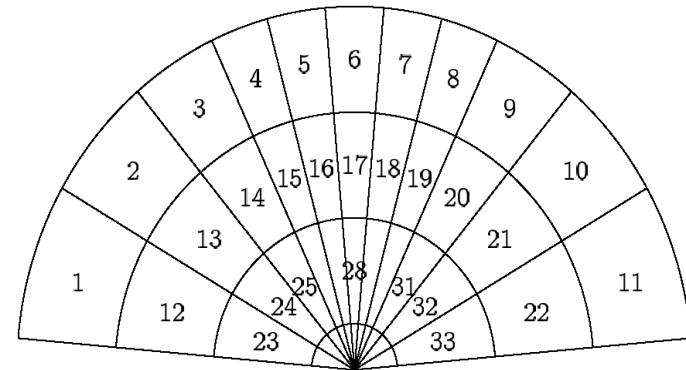
 - ➔ estimation on a real data set by likelihood maximisation

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Model specification : the space discretization



Pedestrian visual space



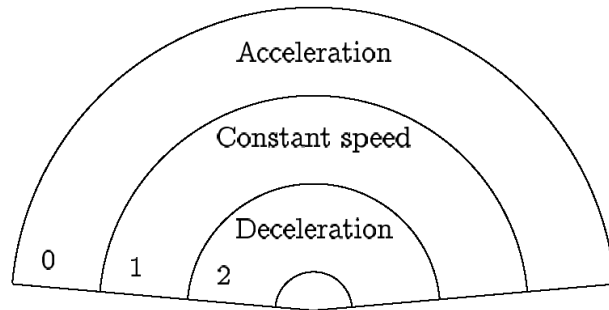
Choice set : discretization of the visual space

At each step the **choice set** depends on the pedestrian **speed** and **direction**

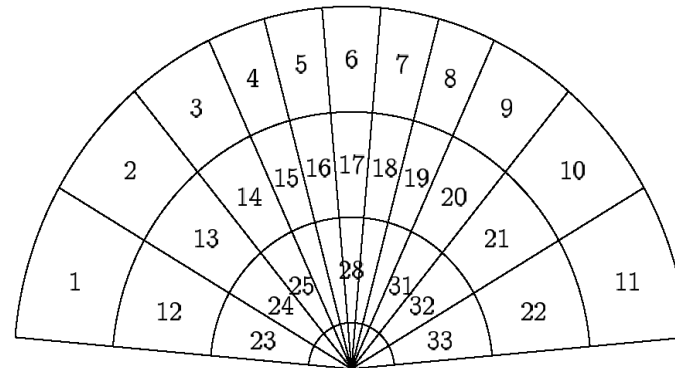
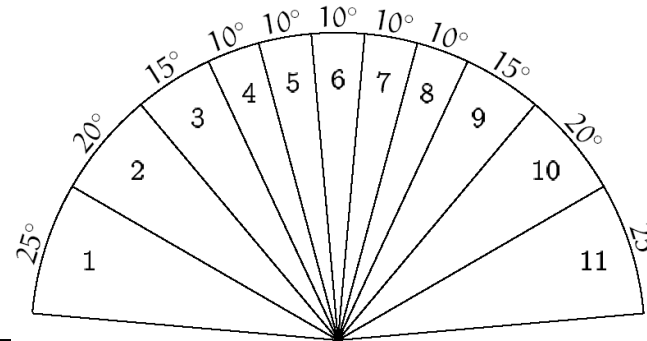
→ Dynamic choice set

Model specification : the choice set

3 speed regimes



11 directions



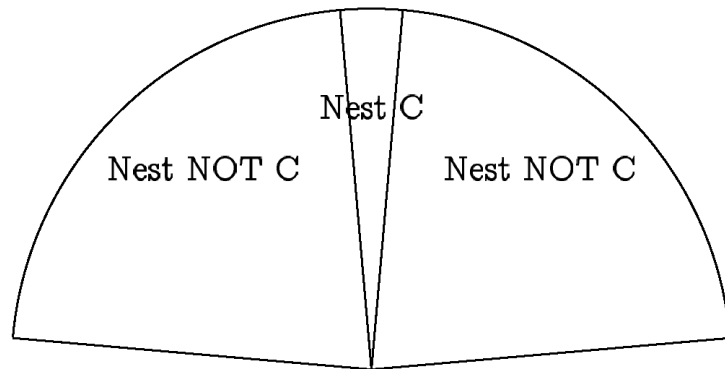
33 alternatives

Model specification : cross nested structure

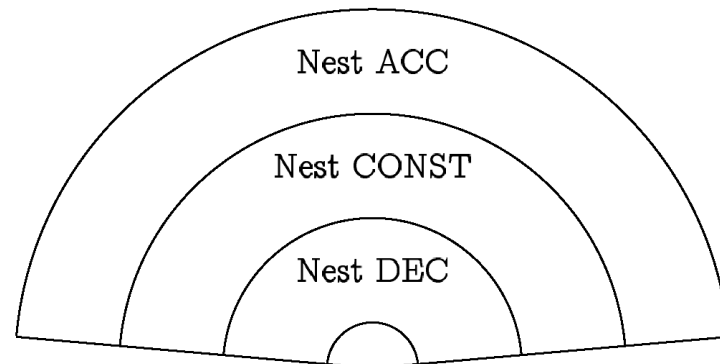
- Hypothesis : alternatives correlated along speed regimes and directions

➔ **Cross Nested Logit model**

- **Cross Nested structure** : each alternative belongs to 2 nests

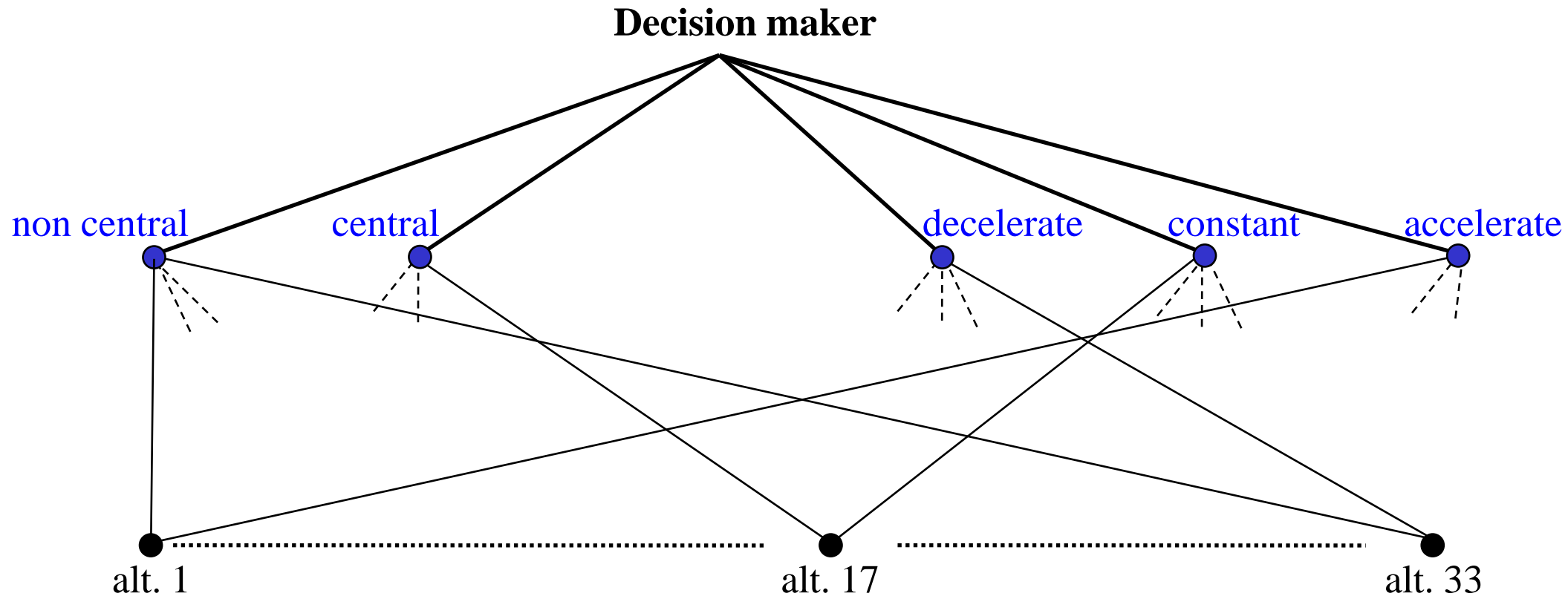


Nesting based on
direction



Nesting based on
speed regime

Model specification : cross nested structure



Model specification : cross nested structure

- Probability of choosing the alternative i :

$$P(i|C) = \sum_{m=1}^M \frac{\left(\sum_{j \in C} \alpha_{jm}^{\mu_m/\mu} y_j^{\mu_m} \right)^{\frac{\mu}{\mu_m}}}{\sum_{n=1}^M \left(\sum_{j \in C} \alpha_{jn}^{\mu_n/\mu} y_j^{\mu_n} \right)^{\frac{\mu}{\mu_n}}} \frac{\alpha_{im}^{\mu_m/\mu} y_i^{\mu_m}}{\sum_{j \in C} \alpha_{jm}^{\mu_m/\mu} y_j^{\mu_m}}$$

C : choice set

M : number of nests

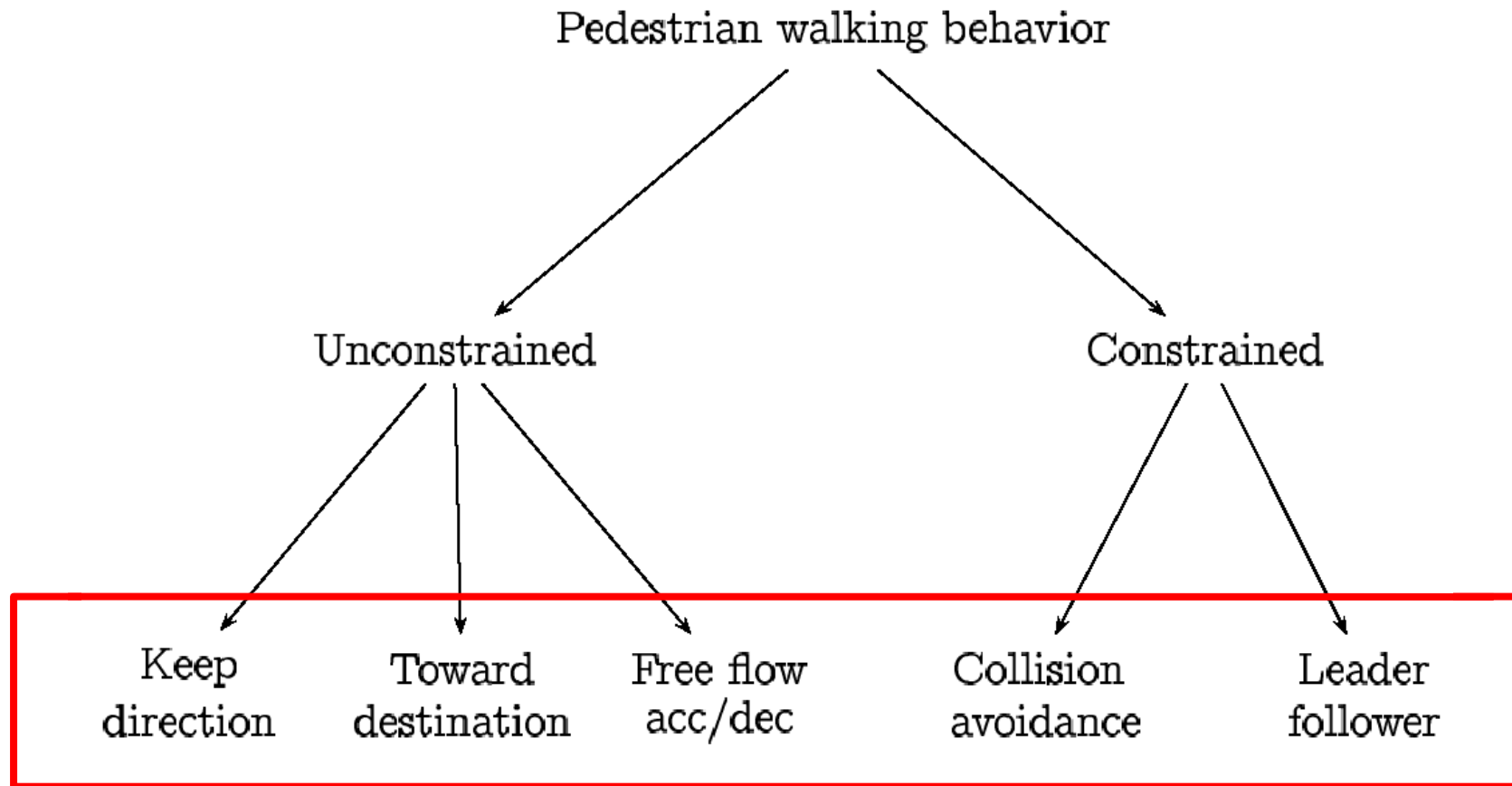
V_i : utility of alternative i

α_{jm} : membership degree of alternative j in the nest n

μ_m : parameter of the nest m

$y_i = e^{V_i}$

Model specification : utility specification



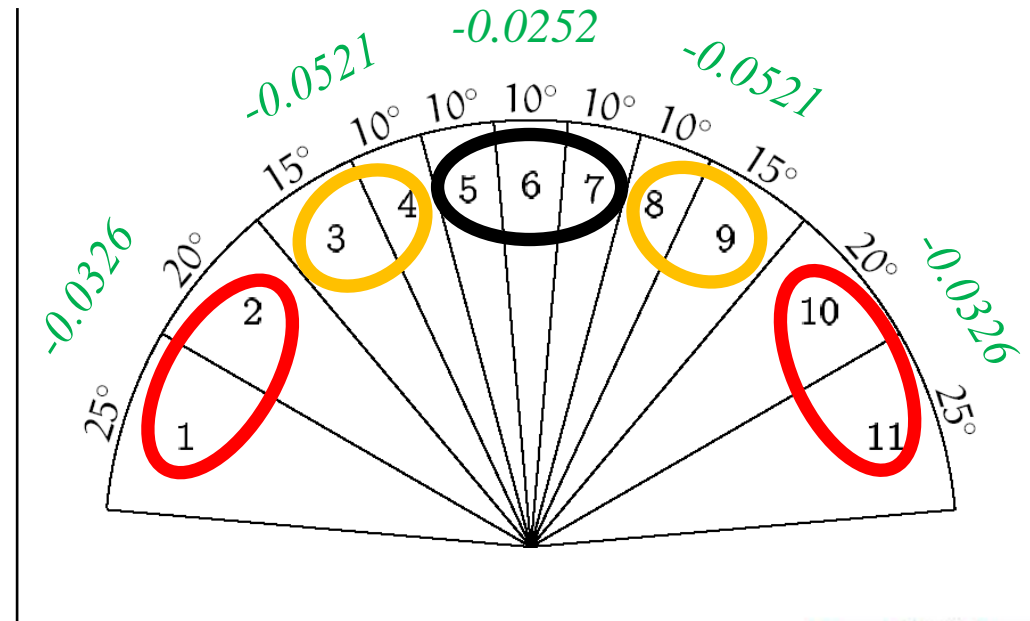
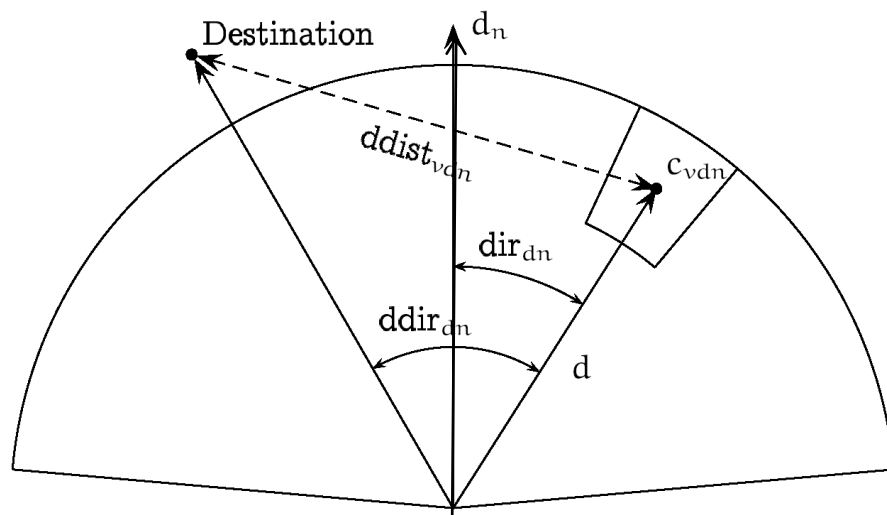
Model specification : utility specification

$$\begin{aligned}
 V_{\text{vdn}} = & \left. \begin{aligned}
 & \beta_{\text{dir_central}} \text{dir}_{\text{dn}} I_{\text{central}} & + \\
 & \beta_{\text{dir_side}} \text{dir}_{\text{dn}} I_{\text{side}} & + \\
 & \beta_{\text{dir_extreme}} \text{dir}_{\text{dn}} I_{\text{extreme}} & +
 \end{aligned} \right\} \textit{keep direction} \\
 & \left. \begin{aligned}
 & \beta_{\text{ddist}} \text{ddist}_{\text{vdn}} & + \\
 & \beta_{\text{ddir}} \text{ddir}_{\text{dn}} & +
 \end{aligned} \right\} \textit{toward destination} \\
 & \left. \begin{aligned}
 & \beta_{\text{dec}} I_{\text{v,dec}} (v_n/v_{\text{max}})^{\lambda_{\text{dec}}} & + \\
 & \beta_{\text{accLS}} I_{\text{LS}} I_{\text{v,acc}} (v_n/v_{\text{maxLS}})^{\lambda_{\text{accLS}}} & + \\
 & \beta_{\text{accHS}} I_{\text{HS}} I_{\text{v,acc}} (v_n/v_{\text{max}})^{\lambda_{\text{accHS}}} & +
 \end{aligned} \right\} \textit{free flow acceleration} \\
 & \left. \begin{aligned}
 & I_{\text{v,acc}} I_{\text{acc}}^L \alpha_{\text{acc}}^L D_L^{\rho_{\text{acc}}^L} \Delta v_L^{\gamma_{\text{acc}}^L} \Delta \theta_L^{\delta_{\text{acc}}^L} & + \\
 & I_{\text{v,dec}} I_{\text{dec}}^L \alpha_{\text{dec}}^L D_L^{\rho_{\text{dec}}^L} \Delta v_L^{\gamma_{\text{dec}}^L} \Delta \theta_L^{\delta_{\text{dec}}^L} & +
 \end{aligned} \right\} \textit{leader-follower} \\
 & \left. \begin{aligned}
 & I_{\text{d,dn}} I_C \alpha_C e^{-\rho_C D_C} \Delta v_C^{\gamma_C} \Delta \theta_C^{\delta_C} & +
 \end{aligned} \right\} \textit{collision avoidance}
 \end{aligned}$$

Model specification : utility specification

- Keep direction (unconstrained) :

$$\underbrace{\beta_{\text{dir_central}} \text{dir}_{\text{dn}} I_{\text{central}}}_{<0} + \underbrace{\beta_{\text{dir_side}} \text{dir}_{\text{dn}} I_{\text{side}}}_{<0} + \underbrace{\beta_{\text{dir_extreme}} \text{dir}_{\text{dn}} I_{\text{extreme}}}_{<0}$$

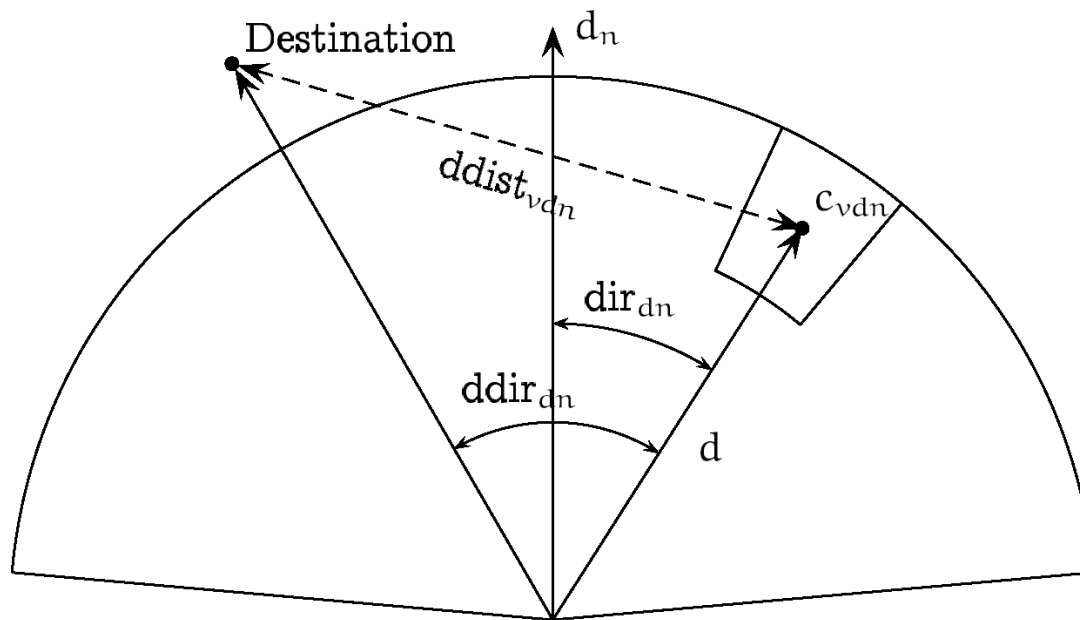


Model specification : utility specification

- Toward destination (**unconstrained**) : $\beta_{\text{ddist}} \underbrace{\text{ddist}_{\text{vdn}}}_{\text{distance}} + \beta_{\text{ddir}} \underbrace{\text{ddir}_{\text{dn}}}_{\text{direction}}$

-1.55
<0

-0.0790
<0



Model specification : utility specification

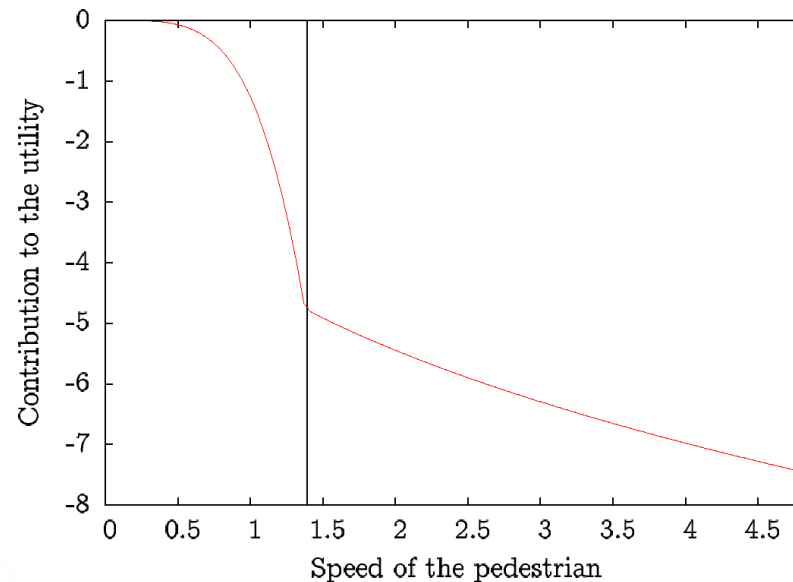
- Free flow acceleration (unconstrained) :

- Acceleration :

$$\underbrace{-4.97 I_{LS} I_{v,acc} (v_n/v_{maxLS})^{4.16}}_{\text{Low speed}} + \underbrace{-7.47 I_{HS} I_{v,acc} (v_n/v_{max})^{0.358}}_{\text{High speed}}$$

Low speed

High speed



Model specification : utility specification

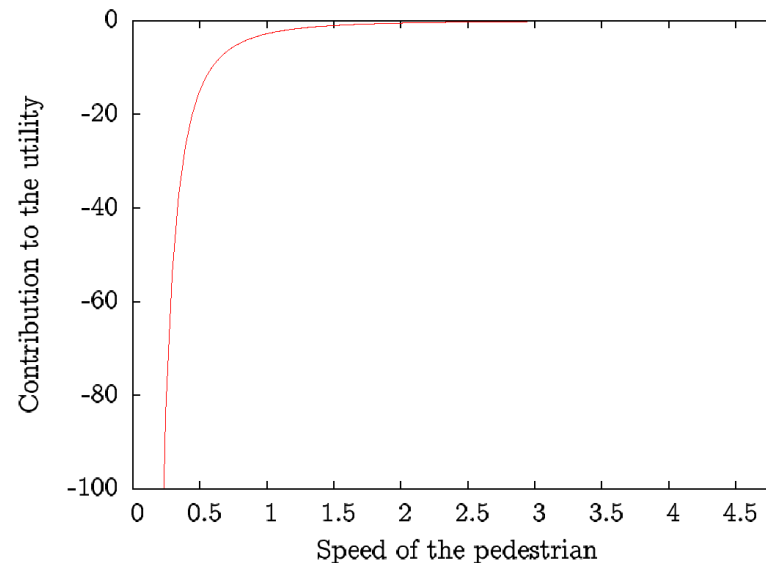
- Free flow acceleration (unconstrained) :

- Deceleration :

-0.0630

-2.41

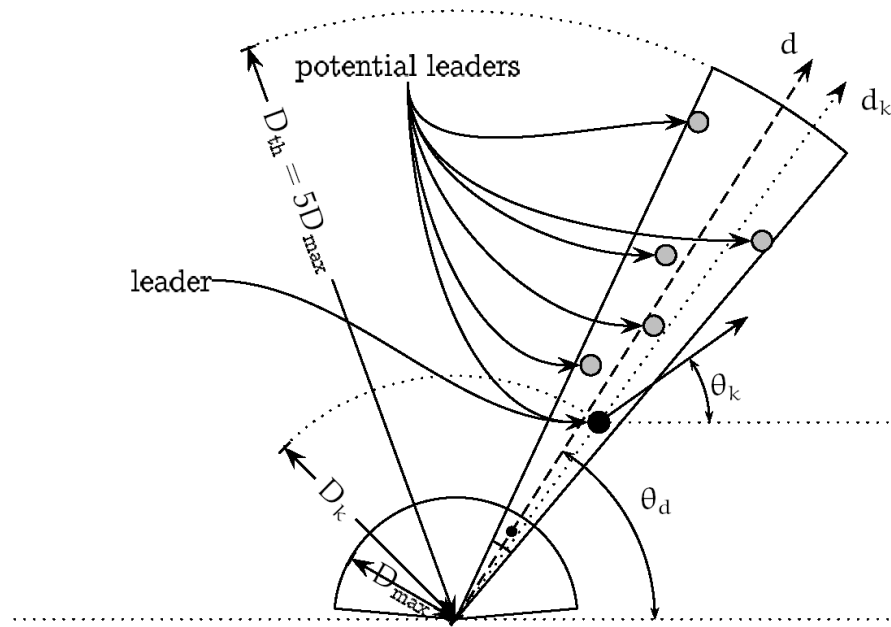
$$\beta_{\text{dec}} I_{v,\text{dec}} (v_n/v_{\text{max}})^{\lambda_{\text{dec}}}$$



Model specification : utility specification

- Leader follower (constrained) :

$$\begin{array}{ccccccc}
 0.942 & -0.489 & 0.625 & -0.171 & & 3.69 & -0.663 & 0.652 \\
 I_{v,acc} I_{acc}^L & \alpha_{acc}^L & D_L^{\rho_{acc}^L} & \Delta v_L^{\gamma_{acc}^L} & \Delta \theta_L^{\delta_{acc}^L} & + & I_{v,dec} I_{dec}^L & \alpha_{dec}^L & D_L^{\rho_{dec}^L} & \Delta v_L^{\gamma_{dec}^L} \\
 \underbrace{\hspace{10em}} & \underbrace{\hspace{10em}} & & & & & \underbrace{\hspace{10em}} & \underbrace{\hspace{10em}} & & \\
 \text{sensitivity} & & \text{stimulus} & & & & \text{sensitivity} & & \text{stimulus} &
 \end{array}$$



Model specification : utility specification

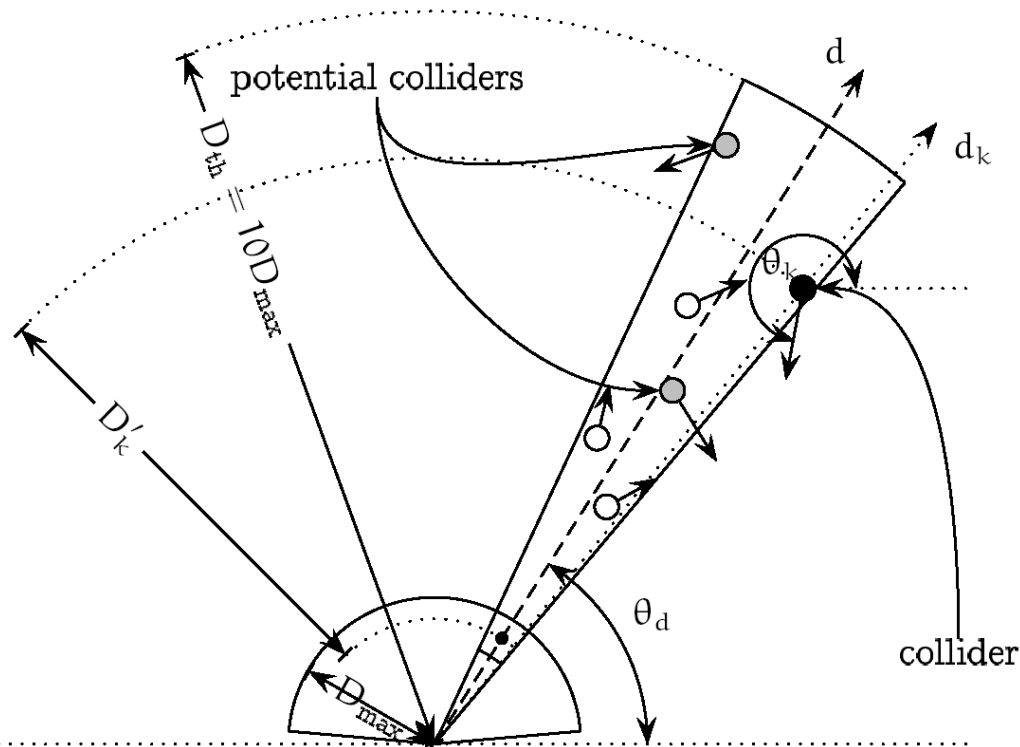
- Collision avoidance (**constrained**): $I_{d,d_n} I_C \alpha_C e^{-\rho_C D_C} \Delta v_C^{\gamma_C} \Delta \theta_C^{\delta_C}$

-0.00639 *0.239*

sensitivity

non significant

stimulus



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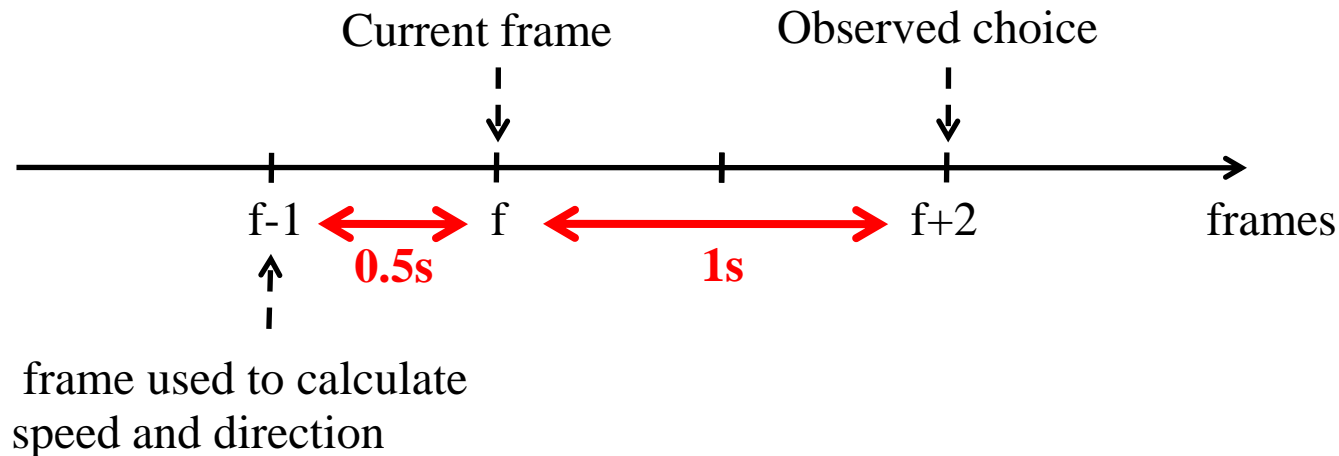
The Japanese data set : video sequence

- Collected in Sendai, Japan, on August 2000, large pedestrian **crossing road**



The Japanese data set : data processing

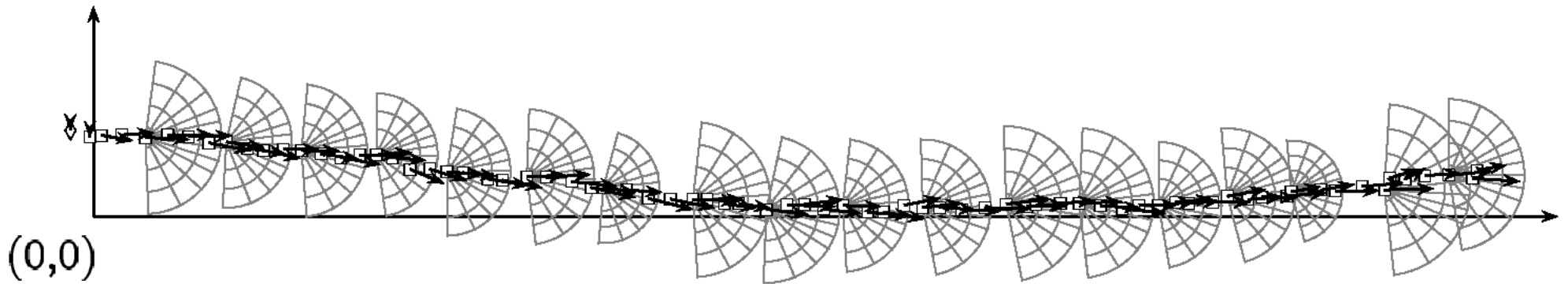
- Tracking from video sequence: **2 observations per second**
- Pedestrians trajectories extracted using 3D-calibration (DLT algorithm)
- For each pedestrian trajectory :



➔ 190 pedestrians, 9281 observations

The Japanese data set : pedestrian trajectory

- 4 alternatives are never chosen: 1, 12, 23, 33



Model estimation : general diagnosis

- Estimation made using the free Biogeme package (biogeme.epfl.ch)
- Estimation results :

Number of estimated parameters : 24

Init log-likelihood : -32451

Final log-likelihood : -13997.27

Likelihood ratio test : 36907

$\bar{\rho}^2 = 0.568$

- Parameters values consistent with hypothesis

Model estimation : parameters values

| Variable name | Coefficient estimate | t test 0 | t test 1 |
|------------------------|----------------------|----------|----------|
| β_{ddir} | -0.0790 | -24.53 | |
| β_{ddist} | -1.55 | -11.66 | |
| $\beta_{dir_extreme}$ | -0.0326 | -9.30 | |
| β_{dir_side} | -0.0521 | -21.87 | |
| $\beta_{dir_central}$ | -0.0252 | -8.74 | |
| β_{accLS} | -4.97 | -22.61 | |
| β_{accHS} | -7.47 | -5.21 | |
| β_{dec} | -0.0630 | -2.40 | |
| λ_{accLS} | 4.16 | 15.94 | |
| λ_{accHS} | 0.358 | 2.09 | |
| λ_{dec} | -2.41 | -8.43 | |
| α_{acc}^L | 0.942 | 2.28 | |
| ρ_{acc}^L | -0.489 | -2.19 | |
| γ_{acc}^L | 0.625 | 2.87 | |
| α_{dec}^L | 3.69 | 6.90 | |
| ρ_{dec}^L | -0.663 | -7.11 | |
| γ_{dec}^L | 0.652 | 6.19 | |
| δ_{acc}^L | -0.171 | -2.33 | |
| α_C | -0.00639 | -9.82 | |
| ρ_C | 0.239 | -8.28 | |
| μ_{acc} | 1.66 | 9.73 | 3.88 |
| μ_{const} | 1.50 | 13.46 | 4.48 |
| $\mu_{central}$ | 2.35 | 1.93 | 1.11 |
| $\mu_{not_central}$ | 1.75 | 9.46 | 4.04 |

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Model validation : methodology

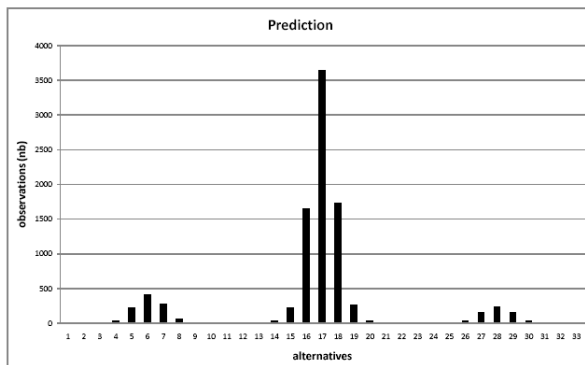
- Validation of the specification :
 - Development of a model with constants only (ASC model)
 - Simulation on the Japanese data set
 - Cross validation on the Japanese data set
- Validation of the model :
 - Simulation on an experimental Dutch data set, **not used for model estimation**
 - Comparison of the proposed model with the ASC model

Model validation : model constants-only

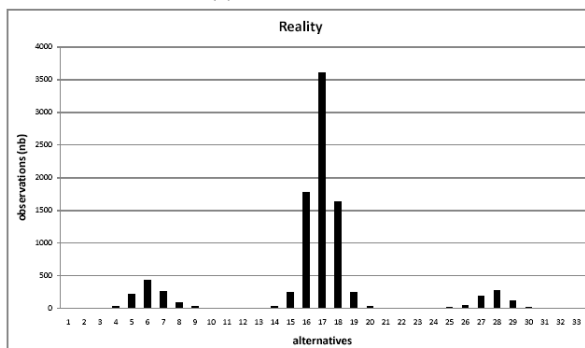
- The simplest model : utility of each alternative represented only by an alternative specific constant (ASC)
- This model with only constants (ASC model) estimated on the Japanese data set.
➔ **28 parameters (33, minus 4 never chosen, minus 1 for normalization)**
- It reproduces the aggregated observations proportions of the Japanese data set
- The ASC model **used for comparison** (for example the number of outliers)

Model validation : simulation on the Japanese data set (**Aggregate level**)

- The proposed model is applied to the Japanese data set (used for estimation)



(a) Predicted shares



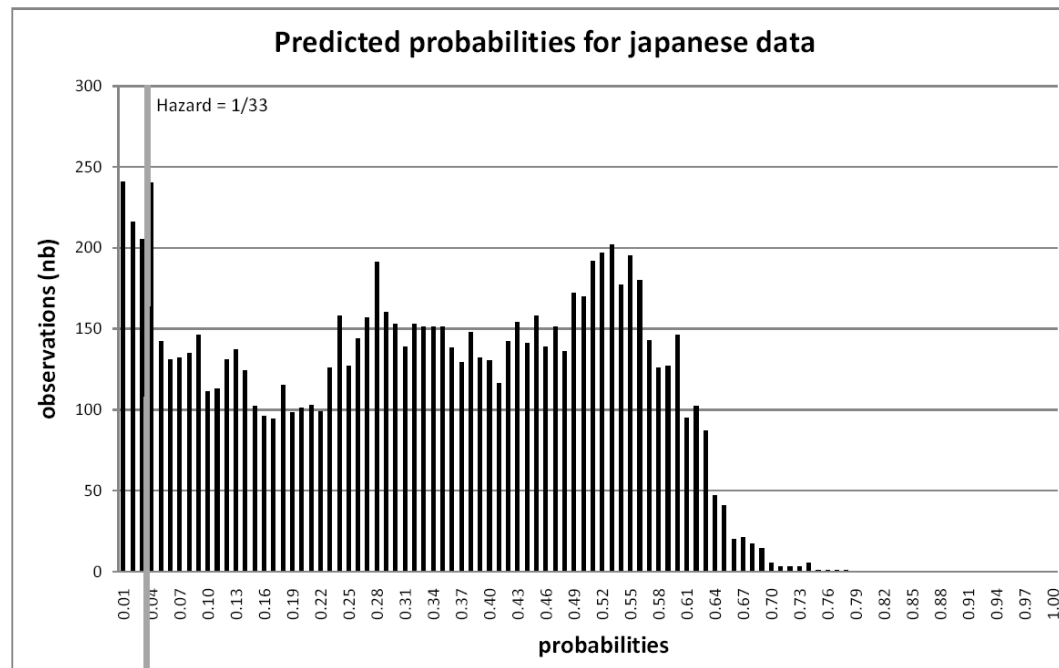
(b) Observed shares

| Cone | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|---------------|-------------------------|------------|------------|----------------------------------|
| Front | 5 – 7, 16 – 18, 27 – 29 | 8489.27 | 8481 | 0.10% |
| Left | 3, 4, 14, 15, 25, 26 | 349.67 | 367 | -4.72% |
| Right | 8, 9, 19, 20, 30, 31 | 415.41 | 407 | 2.08% |
| Extreme left | 1, 2, 12, 13, 23, 24 | 12.29 | 10 | 22.96% |
| Extreme right | 10, 11, 21, 22, 32, 33 | 14.30 | 16 | -10.59% |

| Area | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|----------------|----------|------------|------------|----------------------------------|
| acceleration | 1 – 11 | 1041.50 | 1065 | -2.21% |
| constant speed | 12 – 22 | 7606.49 | 7565 | 0.55% |
| deceleration | 23 – 33 | 633.02 | 651 | -2.76% |

Model validation : simulation on the Japanese data set (**Disaggregate level**)

- **Outlier** : Observation with predicted probability less than $1/33$ (hazard)



Number of outliers: $\left\{ \begin{array}{l} \mathbf{7.13\%} \text{ for proposed model} \\ \mathbf{19.90\%} \text{ for ASC model} \end{array} \right.$

Model validation : Cross-validation on the Japanese data set

- Japanese data splited into 5 subsets, each containing 20% of the observations

→ 5 experiments : $\left\{ \begin{array}{l} 1 \text{ subset saved for } \mathbf{validation} \\ \mathbf{estimation} \text{ of the model on the 4 remaining} \end{array} \right.$

- Number of **outliers** (compared with the ASC model cross validation)

| Model | Exp. 1 | Exp. 2 | Exp. 3 | Exp. 4 | Exp. 5 |
|----------------|--------|--------|--------|--------|--------|
| Proposed spec. | 8.78% | 6.36% | 7.60% | 7.87% | 5.87% |
| Constant only | 20.79% | 20.70% | 17.13% | 19.88% | 18.64% |

→ **Robust specification**

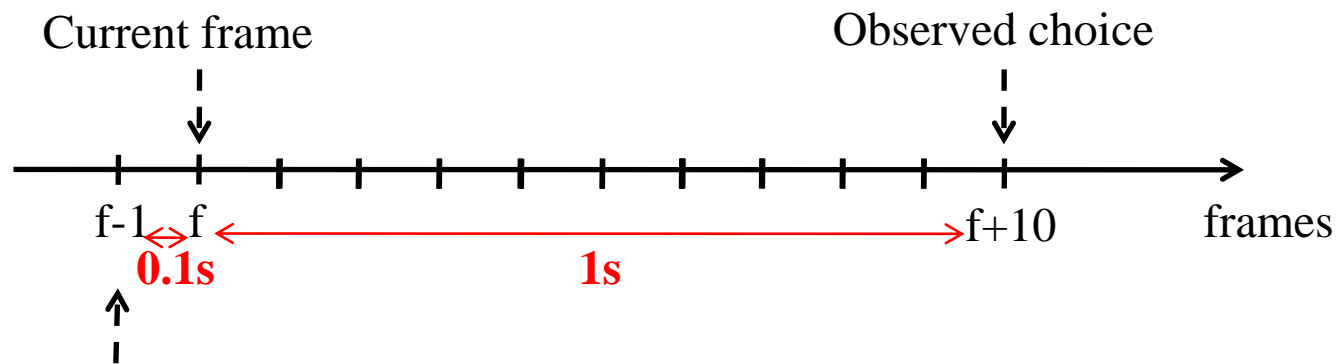
The Dutch data set : video sequence

- Collected at Delft university, in 2000-2001, 2 pedestrians crossing flows



The Dutch data set : general information

- **Experimental** data set
- Video sequence recorded at **10 frames per second**
- Pedestrians trajectories extracted from the video sequence
- For each pedestrian trajectory :

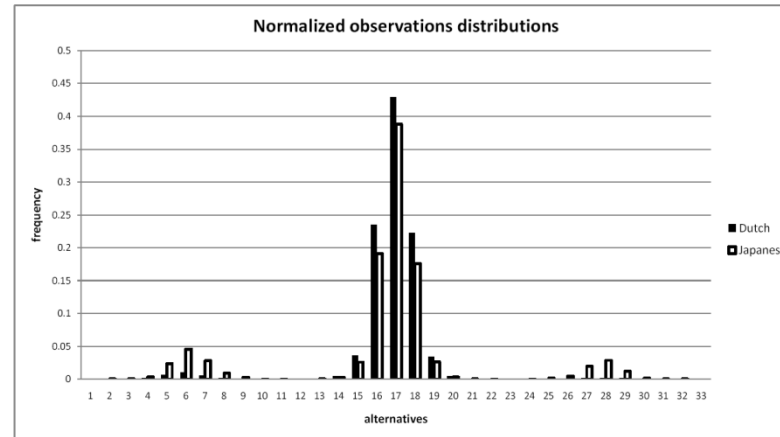


frame used to calculate
speed and direction

→ 724 pedestrians, 47481 observations

The Dutch data set : comparison with the Japanese data set

- Normalized observations distribution among alternatives



- Observations repartitions inside the nest (Japanese / Dutch)

| Nest | # steps | % of total |
|----------------|---------|------------|
| acceleration | 1065 | 11.48% |
| constant speed | 7565 | 81.51% |
| deceleration | 651 | 7.01% |
| central | 4297 | 46.30% |
| not central | 4984 | 53.70% |

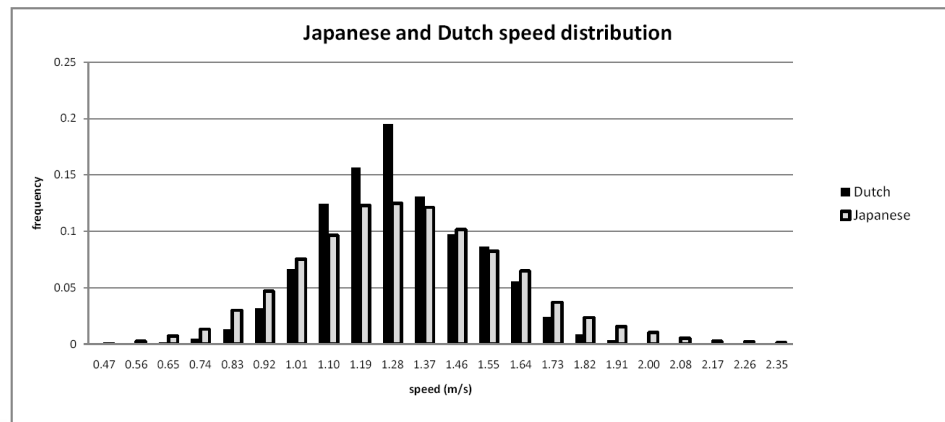
| Nest | # steps | % of total |
|----------------|---------|------------|
| acceleration | 1273 | 2.68% |
| constant speed | 45869 | 96.61% |
| deceleration | 339 | 0.71% |
| central | 20950 | 44.12% |
| not central | 26531 | 55.88% |

The Dutch data set : comparison with the Japanese data set

- Quite similar observations proportions in the **direction's cones** (not for speed regime)

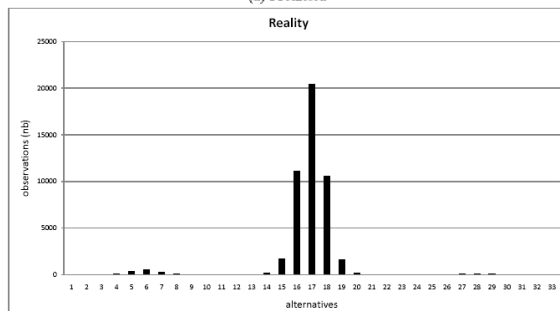
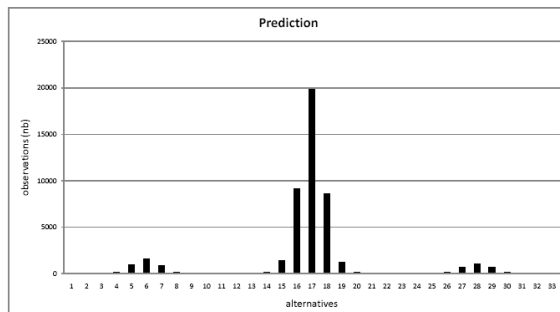
| Dataset | extremeleft | left | front | right | extremeright |
|----------|-------------|-------|--------|-------|--------------|
| Japanese | 0.11% | 3.95% | 91.38% | 4.39% | 0.17% |
| Dutch | 0.06% | 4.40% | 91.35% | 4.15% | 0.04% |

- Speed distributions have different shapes (experimental design of Dutch data set)



Model validation : simulation on the Dutch data set (**Aggregate level**)

- The proposed model is applied to the **Dutch** data set (**NOT** used for estimation)



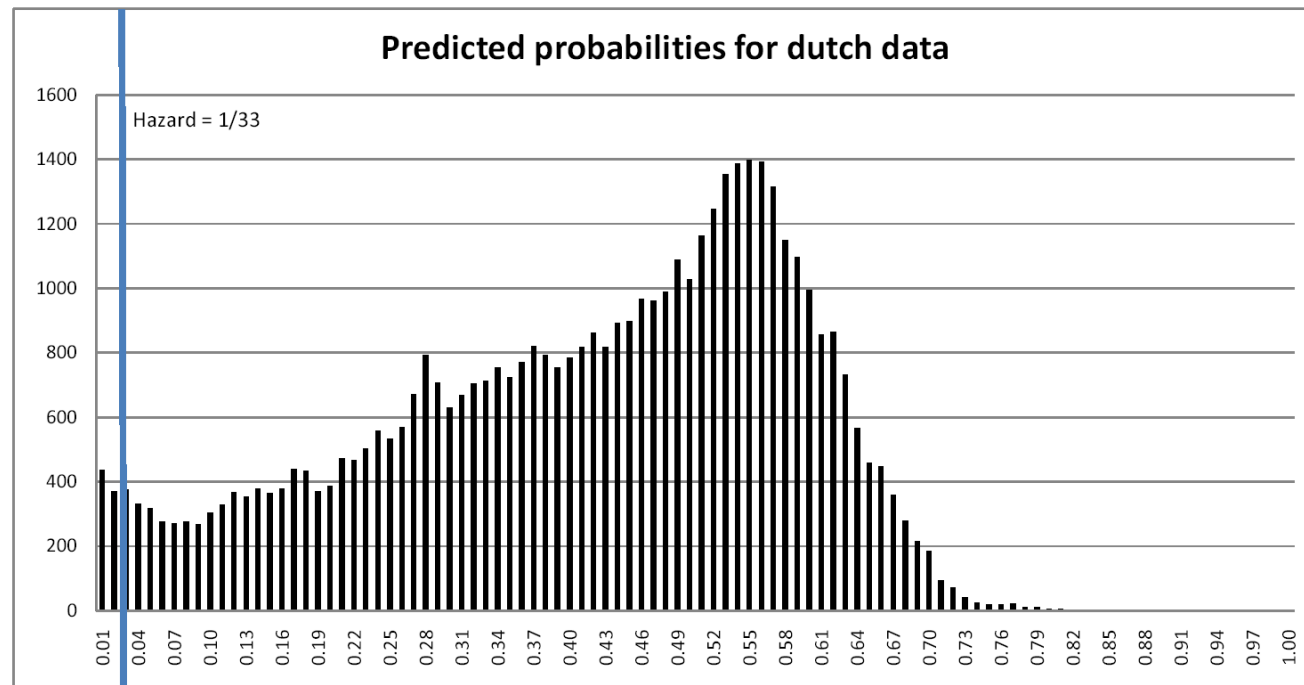
| Cone | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|---------------|-------------------------|------------|------------|----------------------------------|
| Front | 5 – 7, 16 – 18, 27 – 29 | 43619.98 | 43374 | 0.57% |
| Left | 3, 4, 14, 15, 25, 26 | 1968.79 | 2089 | -5.75% |
| Right | 8, 9, 19, 20, 30, 31 | 1764.39 | 1972 | -10.53% |
| Extreme left | 1, 2, 12, 13, 23, 24 | 45.86 | 27 | 69.85% |
| Extreme right | 10, 11, 21, 22, 32, 33 | 81.97 | 19 | 331.44% |

| Area | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|----------------|----------|------------|------------|----------------------------------|
| acceleration | 1 – 11 | 3892.35 | 1273 | 205.76% |
| constant speed | 12 – 22 | 40733.53 | 45869 | -11.20% |
| deceleration | 23 – 33 | 2855.12 | 339 | 742.22% |

→ Overprediction of acceleration and deceleration

Model validation : simulation on the Dutch data set (**Disaggregate level**)

- **Outlier** : Observation with predicted probability less than $1/33$ (hazard)



Number of outliers: **2.48%**

Model validation : Comparison with the ASC model on the Dutch data set (**Aggregate level**)

- The ASC model is applied to the Dutch data set and compared to the proposed model)

ASC model

| Cone | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|---------------|-------------------------|------------|------------|----------------------------------|
| Front | 5 – 7, 16 – 18, 27 – 29 | 43386.42 | 43374 | 0.03% |
| Left | 3, 4, 14, 15, 25, 26 | 1877.47 | 2089 | -10.13% |
| Right | 8, 9, 19, 20, 30, 31 | 2082.10 | 1972 | 5.58% |
| Extreme left | 1, 2, 12, 13, 23, 24 | 51.16 | 27 | 89.47% |
| Extreme right | 10, 11, 21, 22, 32, 33 | 81.85 | 19 | 330.80% |

Proposed model

| Cone | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|---------------|-------------------------|------------|------------|----------------------------------|
| Front | 5 – 7, 16 – 18, 27 – 29 | 43619.98 | 43374 | 0.57% |
| Left | 3, 4, 14, 15, 25, 26 | 1968.79 | 2089 | -5.75% |
| Right | 8, 9, 19, 20, 30, 31 | 1764.39 | 1972 | -10.53% |
| Extreme left | 1, 2, 12, 13, 23, 24 | 45.86 | 27 | 69.85% |
| Extreme right | 10, 11, 21, 22, 32, 33 | 81.97 | 19 | 331.44% |

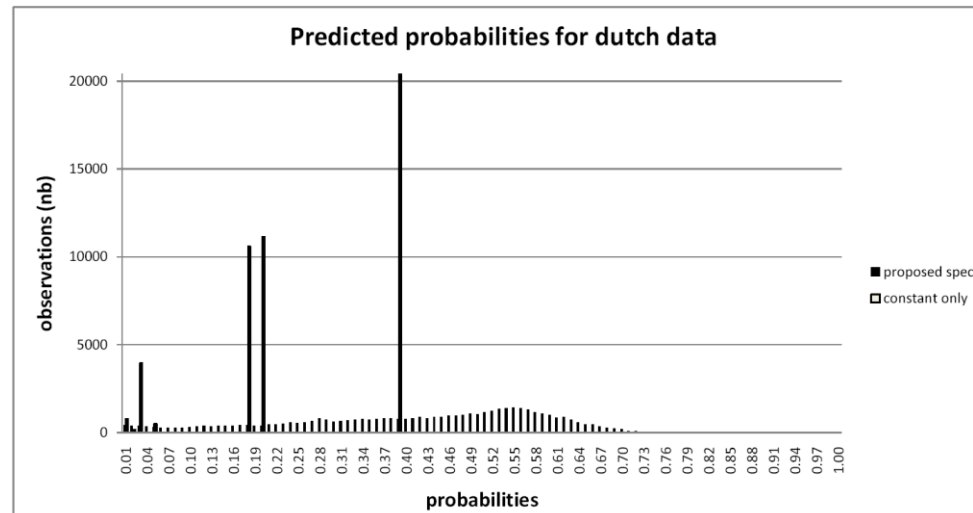
| Area | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|----------------|----------|------------|------------|----------------------------------|
| acceleration | 1 – 11 | 5448.24 | 1273 | 327.98% |
| constant speed | 12 – 22 | 38700.42 | 45869 | -15.63% |
| deceleration | 23 – 33 | 3330.34 | 339 | 882.40% |

| Area | Γ | M_Γ | R_Γ | $(M_\Gamma - R_\Gamma)/R_\Gamma$ |
|----------------|----------|------------|------------|----------------------------------|
| acceleration | 1 – 11 | 3892.35 | 1273 | 205.76% |
| constant speed | 12 – 22 | 40733.53 | 45869 | -11.20% |
| deceleration | 23 – 33 | 2855.12 | 339 | 742.22% |

 **Equivalent for direction (logical, due to proportions)**

Model validation : simulation on the Japanese data set (**Disaggregate level**)

- **Outlier** : Observation with predicted probability less than 1/33 (hazard)



Number of outliers: $\left\{ \begin{array}{l} \mathbf{2.48\%} \text{ for proposed model} \\ \mathbf{10.31\%} \text{ for ASC model} \end{array} \right.$

→ Superiority of the proposed model

-
- Introduction
 - Discrete choice models
 - Model specification
 - Model estimation
 - Model validation
 - **Simulator**
 - Conclusion

Simulator

- **Implementation** of the **developped specification** in a simulator
- Simulation of **2 pedestrian crossing flows** with the model
- Examples :
 - Simulation of 300s
 - Start : random speed and direction
 - Finish : random destination



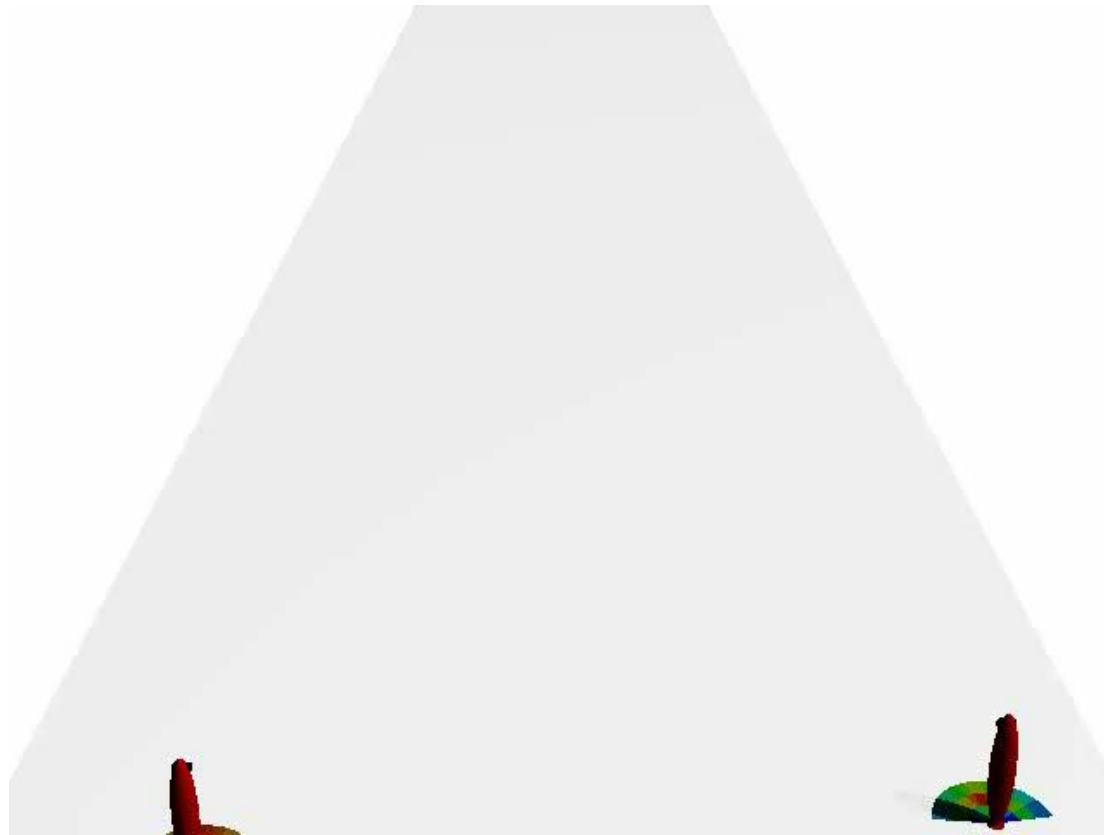
Simulator

- **Low density :**



Simulator

- **High density :**



Conclusions and Perspectives

- Conclusions :

- Discrete choice model for pedestrian walking behavior with ‘**unconstrained**’ and ‘**constrained**’ parameters
- Model **estimated** on a real data set, parameters values consistent with hypothesis
- Model validated on a real data set, **not used for estimation**
- Operating **Simulator**

- Perspectives :

- Improve the **acceleration** and **deceleration** patterns
- Incorporate **physical characteristics** of the pedestrians
- Model the **strategical** and **tactical** behavioural levels

Thanks for your attention

<http://transp-or2.epfl.ch/publications.php#techrep>