

Grain size, size-distribution and dislocation structure from diffraction peak profile analysis

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Abstract

Diffraction peak profile analysis (or Line Profile Analysis, LPA) has recently been developed to such an extent that it can be applied as a powerful method for the characterization of microstructures of crystalline materials in terms of crystallite size-distribution and dislocation structures. Physically based theoretical functions and their Fourier coefficients are available for both, the size and the strain diffraction profiles. Strain anisotropy is rationalized in terms of the contrast factors of dislocations. The Fourier coefficients of whole diffraction profiles are fitted by varying the following fundamental parameters characterizing the microstructure: (i) m and (ii) σ , the median and the variance of the log-normal size distribution function, (iii) ρ and (iv) M , the density and the arrangement parameter of dislocations and (v) q or q_1 and q_2 for the average dislocation contrast factors in cubic or hexagonal materials, respectively. The method will be illustrated by showing results on ECA pressed copper and titanium.

Keywords: crystallite-size, size-distribution, dislocation-density, slip-geometry

1. Introduction

Grains, subgrains or dislocation cells and the dislocation structure in crystalline materials can directly be observed in micrographs of transmission electron microscopy (TEM). These observations provide details on the micron or submicron scales. Average properties of the microstructure, especially on the hundreds of microns up to millimeters scale like crystallite size-distributions [1-3] or specific properties of dislocations as long range internal stresses [4-7], dislocation densities [8-10], arrangement parameters [11,12] or statistical fluctuations [13-15] are better obtained by diffraction peak profile analysis [16].

Diffraction peaks broaden when crystallites are small or the material contains lattice defects. The diffraction order dependence of the two effects is different enabling their separation. The two classical methods for this are: (i) the Williamson-Hall [17] and (ii) the Warren-Averbach [18] procedures. The first is based on the Full Widths at Half Maximum (FWHM) or the integral breadths while the second on the Fourier coefficients of diffraction profiles. Both methods provide apparent size parameters of coherently scattering domains and values of the mean square strain. Strain anisotropy [19] and sometimes shape anisotropy [20] make the evaluation complicated. *Strain anisotropy* means that neither the breadth nor the Fourier coefficients of the diffraction profiles are monotonous functions of the diffraction angle or g where g is the absolute value of the diffraction vector [18-27]. Further difficulty is encountered by the fact that the mean square strain, $\langle \varepsilon_{L,g}^2 \rangle$, is never a constant, neither as a function of L nor g , where L is the Fourier length [2,5-16,18,21-24]. In order to separate strain and size broadening correctly strain anisotropy has to be treated properly. Two different models have been developed so far: (i) the phenomenological model based on the elastic anisotropy of crystals [27] and (ii) the dislocation model [22] based on the mean square strain of dislocated

crystals [8,9,11,12]. Latter takes into account that the effect of dislocations on strain broadening depends on the relative orientations of the line and Burgers vectors of dislocations and the diffraction vector, similarly as the contrast effect of dislocations in electron microscopy. Anisotropic contrast can be summarised in contrast factors, C , which can be calculated numerically on the basis of the crystallography of dislocations and the elastic constants of the crystal [11,21-24,28]. Using the average contrast factors the *modified* Williamson-Hall and the *modified* Warren-Averbach procedures have been suggested [22], enabling to determine (i) different averages of crystallite sizes, (ii) the density and (iii) the effective outer cut off radius of dislocations [22,29]. A method has recently been developed to determine (a) crystallite size distribution and the dislocation structure in terms of (b) density, (c) arrangement parameter and (d) character of dislocations [29,30]. In the present work diffraction peak profile analysis is outlined briefly and applied to characterise the size distribution of crystallites and the dislocation structure in submicron grain size copper and titanium.

2. Evaluation of broadened diffraction peak profiles

2.1. Fundamental equations

In the kinematical theory of diffraction the Fourier coefficients of the physical profiles of Bragg reflections can be given by the Warren-Averbach equation [18]:

$$A_L = A_L^S A_L^D = A_L^S \exp [- 2\pi^2 L^2 g^2 \langle \varepsilon_{g,L}^2 \rangle] , \quad (1)$$

where L is the Fourier variable: $L=na_3$, n are integers and a_3 is the unit of the Fourier length in the direction of the diffraction vector \mathbf{g} : $a_3=\lambda/[2(\sin\theta_2-\sin\theta_1)]$, the diffraction profile is measured in the angular range from θ_1 to θ_2 and λ is the wavelength of the X-rays (or neutrons). In dislocated crystals the mean square strain is [11,12]:

$$\langle \varepsilon_{g,L}^2 \rangle = - (b/2\pi)^2 \pi \rho C f(\eta) , \quad (2)$$

where ρ is the dislocation density, b and C are the Burgers vector and the contrast factor of dislocations, respectively, $\eta=L/R_e$, R_e is the effective outer cut-off radius of dislocations and $f(\eta)$ is a function derived explicitly by Wilkens for dislocations, see equations A.6 to A.8 in [12] or eqs. (22) and (23) in [29]. For small values of η the Wilkens function can be approximated by a logarithmic function [6, 11,12]:

$$\langle \varepsilon_{g,L}^2 \rangle \cong \frac{\rho C b^2}{4\pi} \ln(R_e/L) , \quad (3)$$

Inserting (3) into the Warren-Averbach equation in (1) the *modified* Warren-Averbach equation can be obtained [22]:

$$\ln A(L) \cong \ln A^S(L) - \rho B L^2 \ln(R_e/L) (K^2 \bar{C}) + O(K^4 \bar{C}^2) , \quad (4)$$

O stands for higher order terms in $K^2 \bar{C}$. The full width at half maximum (FWHM) or the integral breadths of profiles can be plotted versus $K=2\sin\theta/\lambda$ (where θ is the diffraction angle and λ is the wavelength of X-rays or neutrons) in the classical Williamson-Hall plot [17]. The intercepts and the slopes of the regressions through the measured data should provide apparent size parameters and values of the mean square strain, respectively. Due to strain anisotropy, however, the data points usually do not follow smooth curves making reliable regressions

impossible. It can be shown that the anisotropic contrast of dislocations enables the rationalisation of strain anisotropy in terms of the *modified* Williamson-Hall plot [22]:

$$\Delta K \cong \alpha/D + (\pi T b^2/2) \rho^{1/2} K^2 \bar{C} + O(K^4 \bar{C}^2), \quad (5)$$

where ΔK is either the FWHM or the integral breadth of profiles, D is the so called apparent size parameter, α is 0.9 or 1 for the FWHM or the integral breadth, respectively, and T is a constant depending on the effective outer cut-off radius of dislocations [22].

2.2. The contrast factors of dislocations

In a texture free cubic or hexagonal polycrystal or if the Burgers vector population on the different slip systems is random the contrast factors of dislocations C can be averaged over the permutations of the hkl indices and the so called averaged contrast factors, \bar{C} , are [31]:

$$\bar{C} = \bar{C}_{h00} (1 - qH^2), \quad (6)$$

or

$$\bar{C} = \bar{C}_{hk0} \left[1 + \frac{[A(h^2 + k^2 + (h+k)^2) + Bl^2]l^2}{[h^2 + k^2 + (h+k)^2 + \frac{3}{2}(\frac{a}{c})^2 l^2]^2} \right], \quad (7)$$

respectively, where \bar{C}_{h00} and \bar{C}_{hk0} are the average dislocation contrast factors for the $h00$ and $hk0$ reflections, respectively, $H^2 = (h^2k^2 + h^2l^2 + k^2l^2)/(h^2 + k^2 + l^2)^2$; q , A and B are parameters depending on the elastic constants and on the character of dislocations (e.g. edge or screw type) in the crystal and a and c are the two lattice constants in the hexagonal crystal.

The expression (7) can be rewritten as [33]:

$$\bar{C} = \bar{C}_{hk0} [1 + q_1 x + q_2 x^2], \quad (8)$$

where

$$x = \frac{2}{3a^2} \left(\frac{l}{g} \right)^2, \quad (9)$$

g is the absolute value of the diffraction vector and $q_1 = A$ and $q_2 = B - (3/2)A (a/c)^2$ [33].

2.3. The size Fourier coefficients

Log-normal is one of the most commonly used size distribution density function:

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} \frac{1}{x} \exp \left\{ -\frac{[\ln(x/m)]^2}{2\sigma^2} \right\}, \quad (10)$$

where x is the grain or crystallite size and σ and m are the variance and the median of the size distribution function, respectively. Assuming spherical crystallite shape the size Fourier coefficients in eq. (1) can be written as [29,30]:

$$A^S(L) \sim \frac{m^3 \exp(4.5\sigma^2)}{3} \operatorname{erfc} \left[\frac{\log(|L|/m)}{\sqrt{2}\sigma} - 1.5\sqrt{2}\sigma \right] - \frac{m^2 \exp(2\sigma^2)|L|}{2} \operatorname{erfc} \left[\frac{\log(|L|/m)}{\sqrt{2}\sigma} - \sqrt{2}\sigma \right] + \frac{|L|^3}{6} \operatorname{erfc} \left[\frac{\log(|L|/m)}{\sqrt{2}\sigma} \right], \quad (11)$$

where erfc is the complementary error function. Hinds has shown that the area-, volume- and arithmetically weighted mean crystallite sizes can be obtained from m and σ in a straightforward manner [32]:

$$\langle x \rangle_{\text{area}} = m \exp(2.5\sigma^2), \quad (12)$$

$$\langle x \rangle_{\text{vol}} = m \exp(3.5\sigma^2), \quad (13)$$

$$\langle x \rangle_{\text{arithm}} = m \exp(0.5\sigma^2). \quad (14)$$

Here we make the following note on the interpretation of crystallite size as determined by X-rays. Size broadening is caused by the column length of coherently scattering domains where this length is parallel to the diffraction vector. As stressed above, an assumption is made first on the shape and on the size distribution of the coherently scattering domains. In the present case the crystallite shape is considered as spherical and the crystallite sizes are supposed to fulfil a log-normal distribution. Hence the average diameters and the parameters of the size distribution function can be determined. These parameters, especially the average diameter, need not be identical with other length scales such as for example, the grain size or the particle size provided by scanning or transmission electron microscopy (SEM or TEM). Coherently scattering domain means the region wherein the amplitudes of the scattered X-rays sum up. When the crystallographic orientation between regions exceed a few degrees the amplitude summation ends and intensities are summing up. This means that the X-ray crystallite size corresponds to domains or regions wherein the variations of orientations are smaller than a few degrees. This type of regions may belong to the same grain or particle in a SEM or TEM micrograph. It is important to note, however, that single dislocations do not disturb the coherency of X-ray scattering since the misorientation they cause is of the order of $b\rho^{1/2}$. Taking typical values for b and ρ in plastically deformed copper, 0.26nm and $1 \times 10^{15} \text{m}^{-2}$, this misorientation is of the order of $\sim 0.5^\circ$. Special arrays or bundles of dislocations can easily create misorientations of a few degrees thus creating boundaries of the coherently scattering regions. There may be some sort of proportionality between the X-ray crystallite size and the grain or particle size determined by SEM or TEM. However, to the best knowledge of the authors this has not yet been studied and goes beyond the scope of this work. From these considerations it is concluded thereafter that: (i) the dislocation density (or, in other words, microstrain) is a microstructural parameter independent of crystallite size (domain size) and neither can be deduced from each other, (ii) the X-ray crystallite size can never be larger than the grain or particle size obtained by SEM or TEM.

2.4. The fitting procedure [30]

A numerical procedure has been worked out for fitting the Fourier coefficients of the experimentally determined physical profiles by the Fourier coefficients of the theoretical size

and strain functions as given in eqs. (1), (2), (6),(7) and (11), respectively. The measured profiles must first be corrected for background, instrumental effects and overlapping peaks. The numerical procedure is as follows: i) the Fourier coefficients of the measured physical profiles are computed making the instrumental correction by using the Stokes method, ii) the Fourier coefficients of the size and strain profiles are calculated by using eqs. (1) and (2) and (11), (iii) the calculated Fourier coefficients are fitted to the experimental values using the nonlinear Marquardt-Levenberg least squares procedure (Gnuplot program package under Unix system). The program for the fitting procedure is available on the web: <http://www.renyi.hu/mwp>, for more details see [30]. The following five or six fitting parameters are used: (i) m and (ii) σ , the median and the variance of the log-normal size distribution density function in the size profile, (iii) ρ and (iv) M , the density and the arrangement parameter of dislocations in the strain profile and (v) q or q_1 and q_2 for the average dislocation contrast factors as in eqs. (6) or (7) for cubic or hexagonal crystals, respectively. The values of \bar{C}_{h00} or \bar{C}_{hk0} are not fitting parameters since they are only multiplicative factors in the Fourier coefficients of the strain profiles. From eqs. (1) and (2) it can be seen that the value of ρ can only be determined if the values of \bar{C}_{h00} or \bar{C}_{hk0} are known. The values of q have been compiled in [28] for different dislocation types and elastic constants in cubic crystals. A similar compilation will be available for hexagonal crystals in [33]. A typical example of the fitting of the Fourier coefficients of the measured physical profiles (open circles) by the theoretical Fourier transforms (solid lines), where latter are given in eqs. (1), (2) and (11) together with the contrast factors defined in eq. (7), are shown in Fig. 1. for ECA pressed titanium.

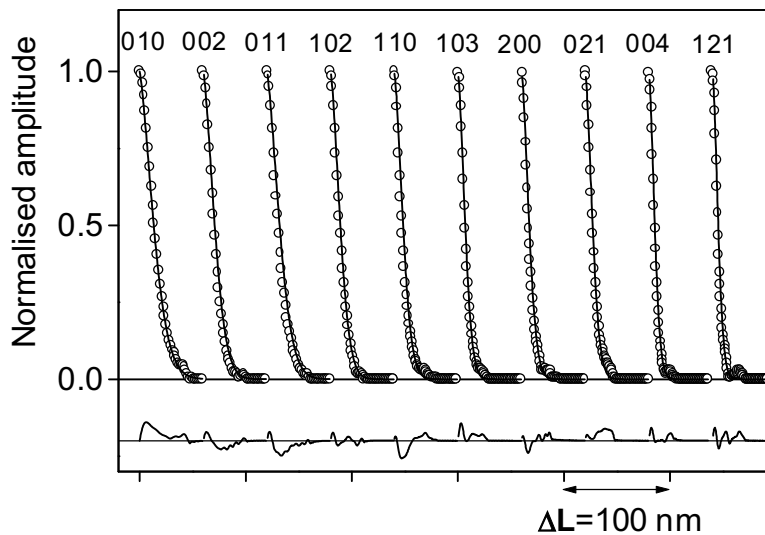


Figure. 1: The measured and fitted Fourier coefficients normalised to unity of ECA pressed titanium. The differences between the measured and fitted values are also shown in the lower part of the figure. The scaling of the differences is the same as in the main part of the figure. The indices of the reflections are also indicated.

3. Experimentals

3.1. Samples

A copper and a titanium sample having cubic and hexagonal crystal structure, respectively, were investigated. A 99.98% copper and titanium specimens (kindly provided by Professor R. Valiev and Prof. Y. T. Zhu) were deformed by ECA (equal-channel angular pressing) producing submicron average crystallite size [34,35]. In order to avoid machining effects an approximately 100 μm surface layer was removed from the specimen surface by chemical

etching before the X-ray experiments.

3.2. X-ray diffraction technique

The diffraction profiles for copper were measured by a special double crystal diffractometer with negligible instrumental broadening (Wilkins & Eckert, 1964). A fine focus rotating cobalt anode (Nonius FR 591) was operated as a line focus at 36 kV and 50 mA ($\lambda=0.1789$ nm). The symmetrical 220 reflection of a Ge monochromator was used in order to have wavelength compensation at the position of the detector. The $K\alpha_2$ component of the Co radiation was eliminated by an 0.16 mm slit between the source and the Ge crystal. The profiles were registered by a linear position sensitive gas flow detector, OED 50 Braun, Munich. In order to avoid air scattering and absorption the distance between the specimen and the detector was overbridged by an evacuated tube closed by mylar windows.

The diffractogram for titanium specimen was measured by a Philips X'pert diffractometer using Cu anode and pyrolytic graphite secondary monochromator. The instrumental peak broadening was corrected by the measurement of the Si standard (NBS 640) using the Stokes method [36].

3.3. Transmission electron microscopy

Transmission electron microscopy (TEM, JEOL JEM200CX) has been used for direct measurement of the size distribution of crystallites in copper sample. Bright field images were used to measure the crystallite size in the samples.

4. Results and discussions

4.1. The size distribution of grains or subgrains and the dislocation structure in ECA pressed copper

The median, m , and variance, σ , of the crystallite size distribution, the dislocation density, ρ , the arrangement parameter of dislocations, M , obtained for copper are listed in Table 1. It can be established that nanocrystalline materials was formed due to large deformation. The crystallite size distribution density function obtained from m and σ is plotted as a solid line in Fig. 2. For the q parameter in the contrast factors 1.90 ± 0.03 has been obtained. In a previous work the values of q have been calculated for the most common dislocation slip system in copper with the Burgers vector $\mathbf{b}=a/2\langle 110 \rangle$ [28]. It was found that for pure screw or pure edge dislocations the values of q are 2.37 or 1.68, respectively. The experimental value obtained in the present case is somewhat below the arithmetic average of the two limiting values of q . From this we conclude that the character of the prevailing dislocations is more edge than screw. This is in good agreement with previous theoretical and experimental observations which has revealed that in fcc metals during large deformations at low temperatures screw dislocations annihilate more effectively than edge dislocations [37].

The crystallite size distribution obtained from X-rays is compared with size distribution determined from TEM micrographs of the plastically deformed bulk copper specimen. In the TEM micrographs the crystallite sizes were determined by the usual method of random line section. As a first approximation the grains, which are in contrast, were selected and the sizes of them were measured in the micrographs. The distribution of these sizes is shown in Fig. 2 by open squares. As it can be seen the grain sizes obtained from TEM are considerably larger than the sizes of crystallites (coherently scattering domains) determined from X-rays. A more careful evaluation of the magnified TEM micrographs reveals that the grains can be divided into smaller subgrains. The size distribution corresponding to the subgrains is shown as a bar

graph in Fig. 2. The size distribution of subgrains is close to that of crystallites, however a small difference can be established in Fig.2. In the copper specimen investigated here the average dislocation distance is $\rho^{-1/2}=36$ nm. The volume and the area weighted mean crystallite size values (see eqs. (12) and (13)) are: 147 and 113 nm, respectively. These crystallite size values are 3-4 times larger than the average dislocation distance indicating that the coherent domain size is definitely different from the dislocation distance. These experimental observations are in good correlation with the theoretical considerations in paragraph 2.3.

Table 1. The median, m , and the variance, σ , of the crystallite size distribution functions, the densities, ρ , and the arrangement parameters, M , of dislocations and the parameters of the dislocation contrast factors, q , or q_1 and q_2 , obtained for copper and titanium by X-ray diffraction peak profile analysis.

sample	m [nm]	σ	ρ [10^{15} m^{-2}]	M	q	$q_1; q_2$
copper	59 ± 5	0.51 ± 0.05	1.6 ± 0.2	2.8 ± 1	1.9 ± 0.1	-
titanium	38 ± 3	0.49 ± 0.05	0.86 ± 0.08	6.5 ± 2	-	-0.05 ± 0.02 ; 0.18 ± 0.02

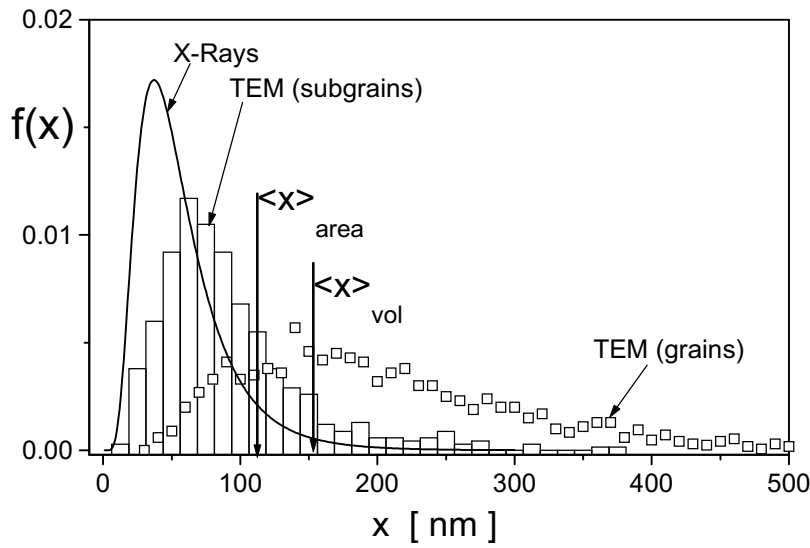


Figure. 2: The size distribution density of grains and subgrains measured by TEM and the size distribution density function of coherently scattering domains or crystallites measured by X-rays for ECA pressed copper sample. The area and volume average crystallite sizes, $\langle x \rangle_{\text{area}}$ and $\langle x \rangle_{\text{vol}}$, respectively, corresponding to the X-ray size distribution function, $f(x)$, and defined in eqs. (10) and (11) are also indicated in the figure.

4.2. The size distribution of grains or subgrains and the dislocation structure in ECA pressed titanium

The measured and the fitted Fourier coefficients of titanium sample are shown in Fig. 1. The difference between the measured and the fitted values are also shown in the figure. The

microstructural parameters obtained from X-ray peak profile analysis are listed in Table 1. It can be established that the severe plastic deformation of titanium resulted in nanocrystalline material. The volume- and the area-weighted mean crystallite sizes are 88 and 69 nm, respectively. The q_1 and q_2 parameters of the contrast factors depend on the character of dislocations therefore enable the determination of the prevailing dislocation slip systems in the sample. The q_1 and q_2 values were calculated for the most common slip systems in *hcp* metals. Due to the linear superposition of the displacement fields of different dislocations the contrast factors for dislocation population containing two or more slip systems can be calculated as the composition-weighted average of contrast factors of individual slip systems. It can be shown that the experimentally measured q_1 and q_2 values in titanium match only the weighted sum of specific pairs of the q_1 and q_2 values calculated theoretically for the different slip systems. This is the consequence of the fact that only a few well defined and specific dislocation slip system are activated during deformation [38]. Table 2. shows those calculated q_1 and q_2 values which correspond to the active slip systems in Ti. A complete list of the most common slip systems together with the corresponding q factors can be found in [33]. The calculated weighted averages of these three slip systems and the experimental contrast factors for titanium are matched by varying the composition of the dislocation population. A more detailed account of the matching procedure of the theoretical q_1 and q_2 values with the measured data can be found in [39]. As a result of this calculation the following composition of dislocation slip systems was obtained: $67 \pm 5\%$ (pyramidal edge 4) + $22 \pm 5\%$ (prismatic edge 1) + $11 \pm 5\%$ (basal screw). The dominance of the “pyramidal edge 4” system and the negligible presence of the “basal slip” system in titanium is in good agreement with previous TEM observations [38].

Table 2.: The values of q_1 and q_2 parameters in the dislocation contrast factors calculated for the three active slip systems in titanium [33].

slip system		q_1	q_2
basal screw	$\langle 11\bar{2}0 \rangle$	0.5949	-0.7104
prismatic edge 1	$\langle 11\bar{2}0 \rangle \{1\bar{1}00\}$	-1.1927	0.3556
pyramidal edge 4	$\langle 11\bar{2}3 \rangle \{11\bar{2}1\}$	1.5270	0.1462

5. Conclusions

The crystallite size distribution and the dislocation structure of nanocrystalline copper and titanium produced by severe plastic deformation were studied by X-ray peak profile analysis. The crystallite size distribution obtained from X-rays are in good agreement with the subgrain size distribution determined by TEM. It was found that the dominant dislocation slip system in titanium is “pyramidal edge 4” which correlates with previous TEM observations.

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