1 INTRODUCTION

Feature extraction (this includes face segmentation because the face itself is considered a global feature) is a very useful step in face recognition and in pattern matching in general. The goodness of a particular feature extraction method is judged on the basis of how much it is efficient and accurate in discrimination between objects of interest herein called human faces. The current investigated features can be categorized into four categories:

- Visual features
- Statistical features
- Transform coefficient features
- Algebraic features
2 FACE SEGMENTATION

This section is concerned about the literature using the so-called “Top-Down” approach for Face Recognition, that means a face is detected first then its features will be constrained within the segmented face-like region. The most recent (State of the art) approach which attracted many researchers, is first discussed.

2.1 Based on RGB Information

“Most methods of color image analysis do not differ significantly from those applied to gray-scale images, they just entail application of the same methods as those used for a single gray-level image, but applied threefold to the different color images.” (M.Seul et al., 2000, p 52).

A special transformation map called (IHS), which stands for Intensity, Hue and Saturation can be obtained from the RGB bases, see figure 3.

Intensity is a measure of brightness:
\[ I = \frac{R+G+B}{3} \quad (1) \]

Hue represents the color value:
\[ H = \cos^{-1}\left\{\frac{[(R-G)+(R-B)]}{2\sqrt{[(R-G)^2+(R-B)(G-B)]}}\right\} \quad (2) \]

Saturation refers to the depth of the color:
\[ S = 1 - \min(R,G,B)/I \quad (3) \]
YCbCr is another transformation that belongs to the family of television transmission color spaces. Skin detection for face location in color images has benefited from these. R. Hsu et al. (2002) introduced a skin detection algorithm which starts with lighting compensation “reference white” which can be chosen from the top 5% of the luma if the sum of its pixels (>100). They detect faces based on the cluster in the (Cb/Y)-(Cr/Y) subspace. A sample of their result is shown next figure 1.

T. Chang et al. (1994) followed the same approach, while H. Wang and S. Chang (1997) choose the following system to convert form (RGB) to (Y, Cb, Cr):

\[
\begin{bmatrix}
Y \\
Cb \\
Cr
\end{bmatrix} = \begin{bmatrix}
(0.299)(0.587)(0.114) \\
(-0.169)(-0.331)(0.500) \\
(0.500)(-0.419)(-0.081)
\end{bmatrix} \begin{bmatrix}
R \\
G \\
B
\end{bmatrix}
\]

Their algorithm results in 85.92% of correct detection.
S. Sirohey and A. Rosenfeld (2001) describe a method for extracting the skin area from an image using normalized color information. The flesh region is extracted and its color distribution is compared with a manually cropped model. J. Wang and E. Sung (1999) obtained 90% of correct detection rate with an identical method.

In earlier work, K. Sobottka and I. Pitas (1996) define a face localization based on (IHS) described earlier, they found that human flesh can be approximation from a sector out of the hexagon depicted in figure 2 with the constraints: $S_{min}=0.23$, $S_{max}=0.68$, $H_{min}=0^\circ$ and $H_{max}=500$
Figure 2  Skin color segmentation in HS space. (K. Sobottka and I. Pitas, 1996)

Figure 3  Illustration of the IHS Color Space. (MATLAB documentation)
J. Dowdall et al. (2003) created a special hardware they call it Triple-band System where a Near-IR illumination generator is included figure 4. Their idea is centered in the fact that human skin has special reflection in the near-IR illumination. Next is an example of their output figure 5.

**Figure 4**  Software diagram of the tri-band system proposed by J. Dowdall et al. (2003).
Whether using IHS or YCbCr transformation, the face region is checked to detect the elliptical shape. This method (color based) normally gives large false alarms, which require further processing either by considering other information or by calling other techniques for a relief, besides generating a skin color model is not a trivial task, for example M. Hu et al. (2004) used 43 million skin pixels from 900 images to train the skin-color model, B. Kwolek (2003) manually segmented a set of images containing skin regions for generating a skin model. It should be noticed too that RGB face databases are rare to be found and constructing them needs special expensive devices.

The apparent color of the skin (color constancy) depends on the light source that illuminates the skin that is why in many cases the segmented face region tends to have holes. Thus, the skin-color appears different under different lighting condition such as ambient light, bright light, or multiple light sources. The movement of an object in the image (blurring) can cause blurring of the skin color. Skin tones variations. Skin color varies within and across individuals. However, it has been shown that intensity normalization can reduce this problem.
2.2 Based on Boundary

Frequently, an important visual element considered in image segmentation is the contrast between the face region and its background. The approaches for detecting such high contrast regions are called edge detection operators. From reviewing the literature it’s found that the most relied on operators are Sobel and Canny. The latter is proven to be the most efficient among all since it detects strong as well as weak edges and minimizes the noise, while it consumes more computational time than others do.

K. Kirchberg et al. (2002) calculate an edge magnitude image with the Sobel operator that uses the following mask:

\[
\Delta x = [-1, 0, 1; -2, 0, 2; -1, 0, 1] \Rightarrow \text{Horizontal Magnitude Detection}
\]
\[
\Delta y = [1, 2, 1; 0, 0, 0; -1, -2, -1] = [\Delta x]^T \Rightarrow \text{Vertical Magnitude Detection}
\]

They created then a face model and superimposed it on a variety of discrete position and calculate the similarities using Hausdorff distance. F. Shih and C. Chuang (2004) adjust the edge generated image and use a raster scan from top to bottom and from left to right to yield the extreme points of the head whereby the bounding box can hug the whole face. A. Al-Qayedi and A. Clark (1999) use similar way however they have chosen SUSAN edge detector and they introduce an edge repairing method (for getting the chin segment). J. Wang and T. Tan (2000) use the Zero-crossing operator followed by an energy function to link cut edges.

M. Rizon and T. Kawaguchi (2000) examined the \((x, y)\) location of each pixel of the Sobel edge, the head contour obtained by this method is not exact but they claimed that in all cases face features were present. S. Jeng et al. (1998) used a boost filtering window that combines a normalized Sobel filter coupled with normalized gray level; after this process is done they extract the edge and group blocks according to a predefined rule.

Active contour which is called also “Snake” is widely used for its efficiency and shape best approximation. V. Perlibakas (2003) uses this method to segment the face outline; his snake implies the sum of the internal as well as the external forces with
weigh coefficients. He initializes it on certain points of a previously Canny detected edge. “Snake” uses a controlled continuity spline function, transforming the shape of the curve to make the energy function minimized from the initial state of the curve (energy minimization). The final curve will end up hugging the shape of the object. The main difficulties of this method are the computational burden is so expensive, sensitivity to noise and hair; a good initial point is very hard to be estimated and the method will always converge onto a solution whether it is the desired one or false one. These methods under this section tend to work quite well for Binary images.

A. Somaie (1996) uses a specific 3*3 mask for edge detection to clip faces from the background, his mask operation on the image responds by a closed contour. The images were all shot in black background and a black cloth was draped around the subject’s neck. Therefore in his case, clipping such faces was not a trivial task. Rather it was one of the ancient direct techniques for face segmentation.

2.3 Based on Thresholding

Suppose that the gray-level histogram corresponds to an image, \( f(x, y) \), composed of dark face in a light background, in such a way that face and background pixels have gray levels grouped into two dominant modes. One obvious way to extract it from the background is to select a threshold ‘\( T \)’ that separates these modes. Then any point \( (x, y) \) for which \( f(x, y) > T \) is called an object (face) point, otherwise, the point is called a background point. This is for bimodal oriented images. Multimodal ones need more complicated work known as Adaptive Thresholding, which can be described as follows:
1. Divide the original image into sub images and for each sub image do

2. Select an initial estimate for T

3. Segment the image using T. This will produce two groups of pixels. G1 consisting of all pixels with gray level values >T and G2 consisting of pixels with values \( \leq T \)

4. Compute the average gray level values mean1 and mean2 for the pixels in regions G1 and G2

5. Compute a new threshold value

\[
T = \frac{1}{2} (\text{mean1} + \text{mean2}) \tag{5}
\]

6. Repeat steps 2 through 4 until difference in T in successive iterations is smaller than a predefined parameter T0

C. Lin and K. Fan (2000) use Thresholding method to generate 4-connected components. After labeling process, they get the center of mass of each block and find any three centers of three different blocks that form an isosceles triangle. They claim to have 98% correct detection rate on their set of database (500 images). L. Tao and H. Kwan (2002) use similar method to extract faces based on geometrical properties of faces features.

2.4 Based on Eigen faces

In K. Wong et al. (2001), a pair of eye candidates are selected by means of the genetic algorithm to form a possible face candidate. The fitness value of each candidate is measured based on its projection on the eigenfaces. In order for them to improve the level of detection reliability, each possible face region is normalized for illumination. After a number of iterations, all the
face candidates with a high fitness value are selected for further verification.

Turk and Pentland (1991) earlier developed this technique for face recognition. Their method exploits the distinct nature of the weights of eigenfaces in individual face representation. Since the face reconstruction by its principal components is an approximation, a residual error is defined in the algorithm as a preliminary measure of “faceness”. This residual error which they termed “distance-from-face-space” (DFFS) gives a good indication of face existence through the observation of global minima in the distance map. Each PCA vector is called eigenvector, and when converted back to matrices these vectors can viewed as the eigenfaces of the dataset figure 6.

Figure 6 Some examples of eigenfaces computed from the ORL dataset (the number below each image indicates the principal component number, ordered according to eigenvalues). (E. Hjelmas, 2001)
Eigenfaces and Color based approaches are among the most well known methods, and they are the state of the art in this field. Therefore, a comparison between the two is shown next (table 1).

Table 1 A comparison between Skin color and eigen based approaches

<table>
<thead>
<tr>
<th>Criterion</th>
<th>Skin color based approach</th>
<th>Eigen-Faces approach</th>
</tr>
</thead>
<tbody>
<tr>
<td>Handling more than one face</td>
<td>It detects each face</td>
<td>It fails</td>
</tr>
<tr>
<td>Rotation, profile and tilted face</td>
<td>It is dependent on the skin color not on the orientation</td>
<td>In case if the eigen space contains such information then it works</td>
</tr>
<tr>
<td>Size of the face</td>
<td>Not necessarily, since neck can be included</td>
<td>It depends on the size of the eigenface size</td>
</tr>
<tr>
<td>Complex background</td>
<td>If it has color similar to the skin color than it suffers</td>
<td>Usually it handle this situation</td>
</tr>
</tbody>
</table>

2.5 Based on Neural Network

Neural networks have become a popular technique for pattern recognition problems, including face detection. J. Dargham et al. (2004) use neural networks which were trained using only the red chrominancce of the normalized rgb color scheme. The training was done using 10% to 80% of the skin data and a similar number
of non-skin data generated randomly from the In-house database.

The networks trained on the In-house database were tested on all images in both the In-house and the WWW databases. The results are compared with a histogram-based skin detection system using the same databases Figure 7. The time taken for a neural network to be trained depends on the number of samples of the training data as well as on the number of neurons used.

![Figure 7](image-url) Skin Detection on Sample Images from the WWW Database using Threshold Technique (Center) and Neural Network (Right). (J. Dargham et al., 2004)

The first advanced neural approach which reported results on a large difficult dataset was by H. Rowley et al. (1998). Their system incorporates face knowledge in a retinally connected neural network shown in Figure 8. The neural network is designed to look at windows of 20 * 20 pixels (thus 400 input units). There is one hidden layer with 26 units, where 4 units look at 10 * 10 pixel sub-regions, 16 look at 5 * 5 sub-regions, and 6 look at 20 * 5 pixels overlapping horizontal stripes. The input window is pre-processed through lighting correction (a best fit linear function is subtracted) and histogram equalization.
Neural network method needs a lot of training samples in order to increase its efficiency level. The complexity of the network is considered to be its disadvantage because it cannot be known whether the network has “cheated” or not. It is almost impossible to find out how the network comes up with its answers. This is also known as a black box model.

2.5 Based on Genetic Algorithm (GA)

Genetic algorithm is an optimization technique that operates on a population of individual solutions. G. Yen and N. Nithianandan (2002) defined a GA algorithm for face location whereby each so-called chromosome in the population during the evolutionary search has five parameters genes, the centre of the ellipse (x and y), x directional radius (rx), y directional radius (ry) and the angle ($\theta$). The fitness of the chromosome is defined by the number of edge pixels (Sobel) in the approximated ellipse like face to the actual
number of pixels in the actual ellipse. The ratio is large when both ellipses overlap perfectly.

K. Wong et al. (2001) use GA to select a pair of eyes among various possible blocks. The fitness value for each face candidate is calculated by projecting it onto the eigenfaces space. Even though GA is accurate, however like “snakes” it suffers from being a time consuming technique, because it will fire its chromosomes to all and every location.

2.6 Based on Voronoi Diagram

M. Suhail et al. (2002) explain how to extract some feature points from an image and then segment it based on these features. They determined a gradient magnitude which is larger than 75% to be extracted as point features from a window of size (3*3). Each of which forms the voronoi cell. These cells will generate the segmented image. In fact they use this method for non face images, however since the basic of it is the gradient magnitude, then it will not work properly for face segmentation. Besides determining the size of the window and the tolerance value of the accepted gradient is in itself a critical problem.

More related to the proposed work, Y. Xiao and H. Yan (2003) propose a symmetry based method for face boundary extraction from a binarized facial image. Basically, they construct Delaunay Triangles (which is the dual of voronoi diagram) from points of edged image. They examine the property of each triangle geometrically and then they identified the so-called J-Triangle (Junction Triangle), this type of triangles will act as a linker for the broken edges. The purpose of this is to split the mergence of face boundary with the background (see Figure 9). This method might experience a non-deniable computational load if the image size increases or/and its task will be extremely difficult when dealing with images with complex background. Their proposed method has limitations in cases of rotation or wearing glasses as they stated in
their paper. It is also sensitive to noise and beard. Their correct rate of detection of facial features upon segmentation is 89%.

![An edge of the J-triangle splits the mergence of face skin and background (Y. Xiao and H. Yan, 2003)](image)

**Figure 9**  An edge of the J-triangle splits the mergence of face skin and background (Y. Xiao and H. Yan, 2003)

### 3 Features Extraction

#### 3.1 Chain Code

In practice, the best alternative, when exact representation is not possible, is to seek features allowing the original shape to be reconstructed to a reasonable degree of precision. This situation, which is opposite to the ideal exact representation, will be designated as an approximated representation. More formally, it can be said that a feature vector $F$ provides an approximated representation of the shape $S$ in case the respective reconstructed version:

$$\tilde{S} = T^{-1}(\tilde{F})$$  \hspace{1cm} (6)

is such that:
\[ \text{Dist}\{S, \tilde{S}\} = \| S - \tilde{S} \| \leq \xi \] (7)

Where
\[ \xi \] denotes a maximum allowed errors.

The Chain Code, Contour Code or Direction Code is a data structure to represent the boundary of a binary image on a discrete grid in an efficient way (B. Jähne, 1997).

The algorithm is first coined by Freeman (H. Freeman, 1974). It encompasses a very compact representation since it is sufficient to use three bits to indicate which direction the next boundary is (M. Ren et al., 2002). It is a standard input format to many shape analysis algorithms because of its usefulness in detecting area, perimeter, moments, centers, eccentricity, projection and sharp turns (corners).

The starting point can be any point on the border of the object, however the often used way is to use an algorithm which scans the image line by line figure 10, thus the point will be the upper-most left pixel of the object. The boundary is followed in clockwise direction and the resultant code sequence is stored each time figure 11. If the object is not connected or has holes, then there will be a need to more than one chain code to represent it. When the pointer reaches to the first point, a normal practice is to delete the former coded edge pixels to allow for another tracing which takes the same steps unless the end of the array is reached. It is important to remember two pieces of information. First, the operation must remember the previous coded pixel for it will be used to eliminate the back-tracing to occur, which results normally with an infinite loop. Secondly, the (x, y) coordinates of the first tracked pixel for when it is revisited it will indicate that the contour is completely coded and thus the end of the operation on the object (G. Baxes, 1994).

The precision of boundary representation is just an approximation and not an exact one. In their work (K. Dunkelberger and O. Mitchell, 1985) tried to enhance the chain
code algorithm by introducing what is commonly known as Crack Code, they argued that is more precise, they claimed too getting an unbiased estimate of the area under straight line sections of a contour. However, they omitted analyzing their methods error rate due to sharp turns. Their method is characterised by using a point on the boundary between two pixels rather than the pixel centers (Chain Code), the rest of the method is almost similar to Chain Code principal. This approach resulted in greater memory requirements, and somehow slower processing although having produced more accurate representation (G. Awcock and R. Thomas, 1996). Figure 12 visualizes the method. Another attempt to manipulate the Chain Code algorithm was done by (M. Ren et al., 2002), where they extracted the inner and outer contours of complex regions. Moreover, several generalizations have been made to make the Chain Code more efficient and accurate (R. Haralick and L. Shapiro, 1993), among which the Primitive Chain Code (PCC) which is discussed briefly in (M. Seul et al., 2000) but it is more complex to code and decode than Freeman Code. Contours are applicable for thin shapes not thick ones (L. Costa and R. Cesar, 2001). These coordinates are associated with rows and columns (matrix-like) and not with the traditional (x, y) Cartesian coordinates Figure 13.

![Figure 10](image_url)  
**Figure 10** Scheme illustrating the process of finding the first pixel from which the contour will start (Raster scan)
**Figure 11** Labeled neighborhood used by the contour tracking algorithms

**Figure 12** Benefits and penalties of crack coding. The crack code vectors (thick lines) clearly give a better presentation, but there are more vectors to process and more storage must be used.
Figure 13  The two pixel representations used for neighborhood tracking

Where
\[ V_0=(r, s+1), V_1=(r-1, s+1), V_2=(r-1, s), V_3=(r-1, s-1), V_4=(r, s-1), \]
\[ V_5=(r+1, s-1), V_6=(r+1, s), \text{ and } V_7=(r+1, s+1). \]

A contour traces a connected path between two pixels A and B which is a sequence of N pixels: P1,P2,..,PN where each pair of consecutive pixels Pi,Pi+1 is such that Pi is a neighbor of Pi+1, with P1=A and PN=B. A connected component is a set of pixels such that there is a connected path between any pair of pixels in that set.

The inverse of a Chain Code is a geometric process and is given by:

\[ (a_1,a_2,\ldots,a_n)^{-1} = a_n^{-1} \ldots a_1^{-1} \]

\[ a_i^{-1} = \text{mod}[8, (a_i+4)] \]

The length of a Chain is given by:

\[ L=n_e+n_0\sqrt{2} \]  

(8)
Where
ne and n0 are the number of the even and odd-value links.
The width and height of an enclosed contour is given by:

\[
\text{Width} = \max_j (X_j) - \min_j (X_j) \quad (9)
\]

\[
\text{Height} = \max_j (Y_j) - \min_j (Y_j) \quad (10)
\]

Distance between two points is given by:

\[
d = \left[ \left( \sum_{i=1}^{n} a_{ix} \right)^2 + \left( \sum_{i=1}^{n} a_{iy} \right)^2 \right]^{1/2} \quad (11)
\]

In the array of Chain Code usually the following are recorded:
E (1) Total number of all contour steps
E (2) X coordinate of the initial point
E (3) Y coordinate of the initial point
E (4) Label
E (5) Chain

Chain Code is said to be invariant to Translation. However, it is
proved to suffer from the choice of starting point. To eliminate
this sensitivity, the row code may be normalised (e.g.: Circularly
rotating the raw code until the largest code value is leftmost). The
chain code shows a number of obvious advantages over the matrix
representation of a binary object.

**Advantages:**

- Compact Representation:

  Given a disk-like object with a diameter R. In a direct matrix
  representation, the bounding box of the object needs to be stored
i.e.: about R2 pixels which need an R2 bit of storage. The bounding box is the smallest rectangle enclosing the object. However, if an 8 neighbor based chain code is used, the disk will be represented by far away less memory storage.

- Translation Invariance:

  The Chain Code is translation invariant representation of a binary object which makes the comparison easier, and eliminated adding another algorithm to translate the object to the desired position.

- Fast Algorithm:

  Since the Chain Code is a complete representation of an object or curve, any shape features can be computed, as well as the number of shape parameters (perimeter, area...etc), more efficiently using Chain Code representation than in the matrix representation.

- Voronoi Diagram:

  A Voronoi Diagram (VD) is easily (with less computing time) constructed using Chain Code generated points.

- Moments Invariant can reduce their computation time by at least half if they were to use Chain Code representation instead of the real object.

Disadvantages:

- No Rotation Invariance:

  The most significant disadvantage in Chain Code is that it cannot be used directly as a base for rotation-invariant object recognition. But, it is possible to extract parameters such as area that is rotation invariant.
- No Scale Invariance
- Noise Sensitivity

Chain Code is sensitive to noise. Similar objects which have almost the same shape can have different Chain Code in presence of noise. Using black and white morphing and opening and closing operations can lessen down the noise and connect a broken Chains.

This method is used in some literature as a means to link edges of face contour to form a closed one, and that by examining the behaviour of the segments.

A. Kouzani et al. (1996) propose 8-neighbours based chain code to represent the edge of the features. The extracted string is then smoothed using a two step process to remove undesired symbols caused by noise, then the two adjacent inverse code are deleted and finally within a group of three or four codes having zero total vector rotation, each pair is replaced by a digit or a pair of digits based on its combination. As an example of the extracted features vectors the following:

Iris:

\[
\begin{align*}
\text{0^6}\text{7}\text{0}\text{(0}\text{6})^5\text{7}\text{6}\text{6}\text{7}\text{6}^5\text{5}^3\text{4}\text{6}\text{(6}\text{4})^3\text{5}\text{4}\text{5}\text{4}^8\text{(3}\text{4})^3 \\
\text{3}\text{2}\text{4}\text{2}\text{4}\text{2}\text{2}\text{4}\text{2}\text{7}\text{1}\text{2}\text{2}\text{2}\text{1}^5\text{0}\text{1}\text{0}^4.
\end{align*}
\]

Pupil:

\[
\begin{align*}
\text{0^5}\text{7}\text{0}^3\text{7}\text{0}\text{0}\text{7}\text{0}\text{0}\text{(0}\text{7})^{12}\text{0}\text{6}\text{6}\text{5}\text{4}\text{4}^3\text{(5}\text{4}\text{4})^3\text{5}\text{4}\text{5} \\
\text{4}\text{4}\text{5}\text{4}\text{4}\text{5}\text{4}^3\text{5}\text{4}^{10}\text{3}\text{4}^4\text{(3}\text{4}\text{4})^7\text{(3}\text{4})^3\text{(2}\text{4})^3\text{2}^4\text{1}^1 \\
\text{(0}\text{1})^3\text{001}\text{0}^4\text{1}\text{0}^6\text{1}\text{0}^{11}.
\end{align*}
\]

After this smoothing process, the vectors are fed into a Fuzzy logic system for further verification.
3.2 Template Matching

The simplest form of template matching is the comparison of the image of interest with a template image. A multiple templates can be used while searching for the closest one to its best fit feature. In here, lightening effects produce low fit even between images of same person. A deformable template was introduced, whereby a model of a face having its features (e.g.: eyes, nose...etc) linked with a spring-like was developed. This allowed a dynamic interaction with the image, which successfully eliminates the need for constructing multiple templates. However, the scale and rotation remain a problem. P. Hallinan et al.(1999) were accredited for introducing the deformable version of templates (elastic ones).

Correlation of a test pattern with a face template involves computing a measure of disparity between the face pattern and the test pattern. A threshold is set for the degree of disparity that can be associated with the given face (O.Ayinde and Y.Yang, 2002).

In their paper (J.Wang and T.Tan, 2000) used six templates. Two eyes templates and one mouth template were used to verify a face and locate its main features, then two cheek templates and one chin template were fired to extract the face contour. The performance claimed to be favorable except that it cannot detect faces with shadow, rotation and bed lighting conditions.

One thing that they presented as an advantage was that they were able to choose a relatively big step in matching so as to reduce the computation cost. While it holds true that the said process reduces the computation burden, however it might bring along—usually true—a loss of significant information because of the said “big step”. The interesting point here is that they admit it indirectly when they reach to the conclusion by saying “We suspect that one reason for this (failure) is that our template does not include enough information to distinguish faces in very complex background”. Most importantly their algorithm gave false alarms when rotation occurs, and when having unwanted objects whose shapes are similar to ellipses.
Going back to the deformable template, R. Chellappa et al. (1995) stated that when this kind of template started above the eyebrow, the algorithm failed to distinguish between the eye and the eyebrow. Another drawback to this approach is its computational complexity. In spite of these drawback points, some authors are in favor to it, because it is a logical way to be taken for feature extraction (R. Brunelli and T. Poggio, 1993).

3.3 Moments

Basically moments are designed to describe the properties of an object in terms of its area, position, orientation and other parameters. The basic equation of moment of an object is given as:

\[
\mu_{pq} = \sum_{x=1}^{M} \sum_{y=1}^{N} B(x, y)(x - x_S)^p (y - y_S)^q
\]  

Where

\(p, q\) is the order of the moment, \((x, y)\) pixel coordinates and \(X_S, Y_S\) represent the coordinates of the focal point.

Moment Centroid:

\(X' = \frac{m_{10}}{m_{00}}\)  \hspace{1cm} (13)

\(Y' = \frac{m_{01}}{m_{00}}\) \hspace{1cm} (14)

are the coordinates of the centroid.

Moments are proven to be scale, translation and rotation invariant. Further details can be found in (M. Seul et al., 2000; G. Awcock and R. Thomas, 1996).

A significant alteration in brightness would alter the result because moments are sensitive to the distribution of the gray values in the object (B. Jähne, 1997), additionally inference of noise would affect the accuracy of the moments invariant. But the main problem of using moments in practice is the computational burden (G. Ji et al., 1997).
Moments invariants are among the statistical based approaches for features extraction, it has received a considerable attention in the recent years for its invariant properties. J. Haddadnia et al. (2002) use a modified version of moments called Pseudo Zernike Moment Invariant (PZMI) to generate a feature vector for each sub-image of the face possible features’ areas and fed these vectors to a classifier called Radial Basis Function (RBF) to determine a specific feature.

### 3.4 Color Based Algorithm

In here the deal is with non-binary images. Color is a good indicator for the presence of certain features, this fact led many researchers to look for clues to use color characteristics to extract features. In their paper (K. Sobottka and I. Pitas, 1996) noticed that in intensity images, eyes and mouth differ from the rest of the face because of their lower brightness. The reason for that is the color of the pupils, the sunken eye-sockets and the light red color of the lips. The rate of detection of facial features was 86%.

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In general, it is a representation of scenes with only two possible gray values for each pixel typically 0 and 1 contains object (foreground) and background, whether the object is represented by white or black pixels is just a matter of convention (L.Costa and R.Cesar, 2001) and chromaticity space, then the holes in the skin segmented image were thresholded to yield pixels of low intensity (e.g.: pupils,iris). The nostrils however, were found by thresholding the normalized red component of the colors, finally for detecting the lips a thresholding was imposed again but this time on the normalized (Red+Blue-2*Green).

R. Hsu et al. (2002) proposed a face detection and face features detection algorithm that is able to handle a wide range of
variations in static color images, based on lighting composition technique and non-linear color transformation. They extracted the eyes, mouth and face boundary based on their feature maps derived from both the luma and chroma of an image. They eye map is constructed by:

\[
\text{EyeMapC} = \frac{1}{3} \left\{ (C_b^2) + (\tilde{C}_r)^2 + (C_b/C_r) \right\}
\]

(15)

Where

\(C_b, (\tilde{C}_r)^2, C_b/C_r\) are all normalized to the range [0,255], and the second parameter is denoted for the negative of \(C_r\) (e.g.: 255-\(C_r\)). By using morphological operations on the eye maps, eye candidates are brightened and other facial areas are suppressed Figure 14.

As for the mouth mapping, they based their algorithm on the observations that mouth region has stronger red component and weaker blue one than other features, therefore \(C_r>C_b\), and the mouth has lower response in the \(C_r/C_b\) feature, but has a high response in \(C_2r\). Figure 15 shows the operation. Finally, for the face boundary map they used Hough Transformation.

\[\text{Figure 14} \quad \text{Construction of the eye maps for two subjects. (R. Hsu et al., 2002)}\]
3.5 Morphological Operations

All morphological algorithms operate on binary images, which are the simplest, and yet one of the most useful image types. They are popular approaches where the operators work on the form of objects. In general, it is a representation of scenes with only two possible gray values for each pixel typically 0 and 1 contains object (foreground) and background, whether the object is represented by white or black pixels is just a matter of convention (L.Costa and R.Cesar, 2001). The convention of assigning 0 to background has a logical intuitive interpretation:

0 (“false”, “off”) \(\rightarrow\) Lack of object.
1 (“true”, “on”) \(\rightarrow\) Presence of object.

Assigning the 0 to background is a wise action because it saves ink.

Binary images can be a result of a direct acquisition or through application of specific image processing technique. They are important because shapes are herein understood as connected sets of points, help also for finding the center of mass, area, counting objects.

- Erosion and Dilation

They are the two fundamental operations to morphological analysis.
Erosion of set $A$ by a structuring element $B$ is defined as:

$$A \Theta B = \{ P \mid B_p \subset A \} \quad (16)$$

Where

$B_t$ is the transpose of $B$, and $B_p$ is $B$ centered at point $p$.

Erosion can enlarge holes in the object, shrink its boundary, eliminate ‘islands’ and remove narrow ‘peninsulas’ on the boundary (G. Awcock and R. Thomas, 1996).

Dilation is the ‘dual’ of erosion. It operates on the complement of set $A$ namely $A^*$, and it is defined as:

$$A^* \Theta B_t = \{ p \mid B_p \cap A \neq \emptyset \} \quad (17)$$

Dilation fills in holes and expands the boundary of an object.

- Closing and Opening

These are two operations based on the previous ones, and which are defined as follows:

‘Closing’ $\rightarrow$ (dilate then erode) $AB : (A \oplus B_t) \Theta B$ \quad (18)

‘Opening’ $\rightarrow$ (erode then dilate) $AB : (A \Theta B_t) \oplus B$ \quad (19)

The benefits of closing are that it blocks up small ‘lackes’ inside the object and links nearby objects. However opening may be used to eliminate small ‘islands’ and isolate objects which are just touching each other.

In their paper C. Han et al. (2000), demonstrate a detection system for the eye using morphological operation (explained earlier). They call it morphology-based eye-analogue segmentation. It is aim is to reduce the interference of the background as they claimed up to 95% which might speed the process significantly. Basically it performs a closing operation and clipped different operations to find the candidate eye-analogue pixels. Four matching rules were launched to verify the candidates and select a potential one as eye location. For more information about their
algorithm the reader is advice to pay a visit to their paper, however a show next a rough example figure 2.16.

![Figure 2.16](image)

**Figure 16** The morphological operation process (a) The original image, (b) the profile signals of the dash line in (a), (c) the signals after performing the erosion operation, (d) the signals after performing the dilation operation, (e) the signals after performing the closing operation, and (f) the signals after performing the closing and clipped different operations. (C. Han et al., 2000)

### 3.6 Hough Transform

It is more specific than the morphological algorithms, whereby it is most often used to find straight lines, circles or ellipses but it is a technique that can be extended to detect any parameterized curve and transfer it into the ‘parameter space’ or ‘Hough space’. The points in the ‘Hough space’ where many curves intersect give a strong likelihood of boundary shape detection. Its main advantages are that it is unaffected by noise or missing portions of the boundary, however it suffers from an expensive computational
requirement, especially when the one knows the other name given to this method namely “Accumulator array” (M. Seul et al., 2000).

A well-known version of this is the Generalized Hough Transform (GHT), where the detected edge pixels vote for a shape according to a parametric representation or boundary orientation by referring to the centroid positions.

According to H. Moon et al. (2002) this method has a poor localization performance since it depends on the location of edges and points orientations, and it is hard to formulate the point spread function of the voting process. In addition, it is difficult to determine whether a peak is significant besides the size of the discrete parameter space increases rapidly as the number of parameters increases (B. Jähne, 1997).

Another alteration for the Hough transform is found in the paper (A. Nikolaidis et al., 1997), where they used the Adaptive Hough Transform (AHT) to extract the cheeks and chin on a relevant sub image defined according to the ellipse containing the main connected component of the image, while they encountered problems in cheek extraction when the false symmetry of the ellipse leads to bad definition of the relevant sub image, and thus to an erroneous extraction of some other feature considered as predominant.

R. Chellappa et al. (1995) highlighted the fact that the application of Hough transform to detect the perimeter of the shape of the region below the eyebrows appears on average to yield a spacing 20% larger than the spacing between the irises.

### 3.7 Projection Function

This is without doubt one of the most popular technique which is still being used up-to-date. It is simply dividing the ROI into Rows and columns whereby a statistical measurement is derived and projected for gray scale values.
S. Sirohey and A. Rosenfeld (2001) use the term “eyeness” to address the fact that human eye projection (mean value) has the “W” shape. They use this criterion to vote for eye-like region.

G. Feng and P. Yuen (1998) produced a system with a variance projection function that benefits from horizontal and vertical integral projections.

K. Sobottka and I. Pitas (1998) get the horizontal and vertical projections then the resulting x-reliefs are smoothed in x-direction by an average filter of width 3 and minima and maxima are determined. As a result, they obtain for each face candidate one smoothed y-relief with an attached list of its minima and maxima and, for each significant minima of the y-relief, smoothed x-reliefs with attached lists of their minima and maxima. By searching through the lists of minima and maxima, candidates of the three facial feature groups are determined. The groups and their characteristics as described next (table 2).

Table 2  Description of facial feature groups (K. Sobottka and I. Pitas, 1998)

<table>
<thead>
<tr>
<th>Group 1: eyebrows, eyes</th>
<th>Group 2: nostrils</th>
<th>Group 3: mouth, chin</th>
</tr>
</thead>
<tbody>
<tr>
<td>Two significant minima</td>
<td>Two significant minima</td>
<td>Two significant maxima</td>
</tr>
<tr>
<td>Upper/middle part of head</td>
<td>Middle part of head</td>
<td>Middle/lower part of head</td>
</tr>
<tr>
<td>Significant maximum between minima</td>
<td>Significant maximum between minima</td>
<td>Significant minimum between maxima</td>
</tr>
<tr>
<td>Ratio of distance between minima to head width is in certain range</td>
<td>Small distance between minima</td>
<td>Ratio of distance between maxima to head width is in certain range</td>
</tr>
<tr>
<td>Similar gray-levels</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
REFERENCES


