A TCAD Approach to the Physics-Based Modeling of Frequency Conversion and Noise in Semiconductor **Devices Under Large-Signal Forced Operation**

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Abstract—The paper presents a novel, unified technique to evaluate, through physics-based modeling, the frequency conversion and noise behavior of semiconductor devices operating in large-signal periodic regime. Starting from the harmonic balance (HB) solution of the spatially discretized physics-based model under (quasi) periodic forced operation, frequency conversion at the device ports in the presence of additional input tones is simulated by application of the small-signal large-signal network approach to the model. Noise analysis under large-signal operation readily follows as a direct extension of classical approaches by application of the frequency conversion principle to the modulated microscopic noise sources and to the propagation of these to the external device terminals through a Green's function technique. An efficient numerical implementation is discussed within the framework of a drift-diffusion model and some examples are finally provided on the conversion and noise behavior of rf Si diodes.

Index Terms-Microwave devices, nonlinear systems, semiconductor device modeling, semiconductor device noise, sensitivity.

I. INTRODUCTION

R ECENTLY, great interest has been placed on the modeling and simulation of electron devices. conditions (LS). Such regime is particularly important in classical analog radio-frequency (rf) applications, either quasilinear, such as power amplifiers, or nonlinear, such as mixers and frequency multipliers. Owing to the increasing importance of silicon-based analog rf applications, a growing attention exists on the development of technology computer aided design (TCAD) tools able to analyze and optimize the LS device behavior [1], [2].

During the last few years, LS analysis techniques for analog circuit simulation such as the harmonic balance (HB) method [3]-[5] have been successfully applied to the LS physics-based numerical device modeling, see [6], [1], [7], [8]. However, further techniques, that have been developed in the field of circuit simulation, are relevant to the physics-based analysis of devices operating in the LS regime.

A first example concerns the analysis of frequency conversion in the presence of multi-tone inputs, which has paramount importance in simulating e.g., mixer operation or the intermod-

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ulation behavior of power amplifiers. Although the HB method can generally handle this case, the computational intensity of the solution is greatly increased. A useful approximation to frequency conversion in the presence of a strong input tone (such as a local oscillator) superimposed to one or more weak input tones (such a signal to be up- or down-converted) is provided by the so-called small-signal large-signal (SS-LS) analysis [9], which implies the model linearization around the instantaneous working point. SS-LS analysis provides a linear relationship between the (weak) input tone amplitude and the output tone resulting from frequency conversion through the so-called conversion matrix [9].

A second example is noise analysis under LS operation. As well known from circuit theory (see, e.g., [5] and [10]) noise and SS-LS analyses are strictly related, since noise can be interpreted as a small, random perturbation affecting a system operating in a steady-state LS regime. Induced noise therefore results as the frequency conversion of noise sources, which, owing to the periodic nature of the instantaneous working point, already experience amplitude modulation (and therefore frequency conversion) with respect to the conventional small-signal case. A comprehensive approach for the LS noise analysis of both nonautonomous and autonomous (self-oscillating) circuits has been presented in [10]; many of the theory keypoints, such as the use of modulated noise sources and the related noise frequency conversion, were already found in the pioneering paper [11].

The present paper focuses on the extension of the TCAD approaches to the analysis of frequency conversion and noise in LS operation. In particular, we propose a unified treatment of the two, which generalizes, as far as noise analysis is concerned, the Green's function approach proposed by some of the present authors [12]. The Harmonic Balance technique is applied to the discretized physics-based model to determine the LS steadystate solution, and a generalization of the circuit SS-LS HB analysis is exploited to determine, from physics-based models, the device conversion matrix. Concerning physics-based noise analysis, a first modeling technique was proposed in [13], extending the so-called active line approach [14]. The present approach directly generalizes the classical Green's function approach [12] and the related impedance field method (IFM) [15], allowing for the direct evaluation of the device noise sideband correlation matrix [16], which yields the power and correlation spectra of the noise spectral components at the device terminals resulting from the frequency conversion process, see Section II.

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The paper is structured as follows. Section II presents an outline of the frequency conversion and noise theory mainly from a system standpoint, and is intended to provide the basis for further discussion and application to physics-based modeling. Section III briefly reviews the LS formulation and introduces the SS–LS analysis through model linearization around the instantaneous working point. The LS noise analysis formulation is discussed in Section IV. Finally, implementation issues, including some computational aspects, and examples of application are presented in Section V, where the results of the physics-based model are compared and found to be in good agreement with conventional equivalent circuit analysis.

II. OUTLINE OF FREQUENCY-CONVERSION AND NOISE THEORY IN LS OPERATION

As well known, in the forced LS regime the device is excited by a large electrical input signal generally made of a superposition of harmonic components or tones. According to the application of interest, the device is driven into a mildly nonlinear regime (as in power amplifiers) or into full nonlinearity (as in mixers and frequency multipliers); in all cases, nonlinearity results in the generation of harmonics and intermodulation products. Simple, though practically important cases, are the single-tone input and the two-tone input cases. In the former, the input signal is strictly periodic with (angular) frequency ω_0 ; device nonlinearity produces signals with spectrum $\omega_k = k\omega_0$, k integer. In the latter, the input frequency components are ω_1 and ω_2 , and the resulting spectrum is the set $k\omega_1 + l\omega_2$, k and l integers. The operation is termed *quasiperiodic* when the input frequencies are incommensurate, i.e., their ratio is not a rational number; extension to the multi-tone regime is straightforward.

From an application standpoint, an important case occurs when two input tones are present, one strong, the other weak. In this case, the small-amplitude (weak) signal at frequency ω is superimposed to the LS (strong) input at ω_0 , thus linearly perturbing the LS regime. Linearization around the LS working point is the object of the small-signal large-signal (SS-LS) analysis [9]. In this case, the output spectrum results as the set $\omega_k \pm \omega$, where ω_k is the unperturbed LS spectrum, with the following interpretation: the input frequency ω is converted into an output set of spectral lines, usually referred to as sidebands, symmetrically placed with respect to each harmonic of the unperturbed LS regime (see Fig. 1). Due to linearity, the amplitude of the output sidebands is proportional to the amplitude of the (weak) input. This concept can be generalized if the weak input signal spectrum is already made of sidebands $\omega_k \pm \omega$; the same spectrum is found at the output, and the linear relation between the input and output sideband amplitudes can be represented by means of the so-called conversion matrix (CM). Notice that the CM is, in general, not diagonal, thus implying frequency conversion between each input and output sideband.

To formally derive the concept of frequency conversion within a system framework, let us consider a nonlinear system having a periodic input with fundamental frequency ω_0 . The

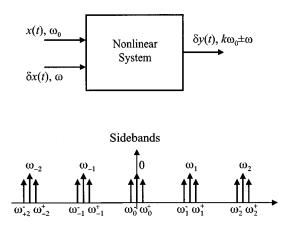


Fig. 1. Frequency conversion in a nonlinear system driven by a single tone LS excitation and a small-amplitude signal.

system output has a frequency spectrum composed of all the harmonics of the input frequency

$$\omega_k = k\omega_0 \qquad k \text{ integer} \tag{1}$$

and can be therefore expanded into a Fourier series. Consider now the case wherein a small-amplitude signal is superimposed to the system input, resulting in a perturbation of the LS periodic steady-state. The system response can be obtained by SS–LS analysis [9], i.e., through linearization around the LS solution, yielding a *linear periodically time-varying* (LPTV) system. A general theory of LPTV systems, based on the transfer function formalism, is beyond the scope of this paper, and can be found, e.g., in [17]. For the sake of our discussion, we confine the treatment to the simple case of a LPTV system defined by

$$\frac{d\delta y}{dt} + g(t)\delta y(t) = \delta x(t) \tag{2}$$

where $\delta x(t)$ is a forcing term (the input), and g(t) is a periodic function corresponding to the memoryless part of the system:

$$g(t) = \sum_{k=-\infty}^{k=+\infty} G_k e^{jk\omega_0 t}.$$
(3)

Since g(t) is a real function of time, $G_{-k} = G_k^*$ for any k.

According to SS–LS theory, the input (and therefore the output) signal spectra are the set of sideband frequencies

$$\omega_k^+ = \omega_k + \omega \qquad \omega_k^- = \omega_k - \omega \tag{4}$$

where the + refers to the *upper* sideband and the – to the *lower* sideband, displaced by an amount ω from the central frequency $\omega_k = k\omega_0$ (see Fig. 1). For instance, the Fourier expansion of the output signal is

$$\delta y(t) = \sum_{k=-\infty}^{k=+\infty} \left[\delta Y_k^+ e^{j\omega_k^+ t} + \delta Y_k^- e^{j\omega_k^- t} \right]$$
(5)

where $\delta Y_{-k}^{-} = (\delta Y_{k}^{+})^{*}$ and $\delta Y_{k}^{-} = (\delta Y_{-k}^{+})^{*}$. These symmetry conditions allow to express $\delta y(t)$ as the real part of the complex time varying function:

$$\delta y_c(t) = \sum_{k=-\infty}^{k=+\infty} \delta Y_k^+ e^{j\omega_k^+ t} \tag{6}$$

thus making the set of coefficients δY_k^+ sufficient to characterize the waveform in (5). Similar expressions hold for the input $\delta x(t)$. Notice that, hereafter, capital variables will always denote the frequency components of the corresponding time-domain quantities.

Introducing into (2) the complex signals and the expansion (3), the sideband amplitudes δY_k^+ are readily shown to satisfy the infinite algebraic linear system

$$j\omega_q^+ \delta Y_q^+ + \sum_{n=-\infty}^{+\infty} G_{q-n} \delta Y_n^+ = \delta X_q^+.$$
(7)

The inverse of the coefficient matrix of such infinite set of equations is the conversion matrix C of the LPTV linear system. By collecting the sideband amplitudes into infinite vectors, one has

$$\delta \boldsymbol{Y} = \boldsymbol{C}(\omega) \cdot \delta \boldsymbol{X} \tag{8}$$

where we have explicitly stated the dependency of the CM on the displacement frequency ω , which results from the memory part of the LPTV system. Suitable truncation must be performed on the spectra and on the CM to make the problem practically manageable. The CM approach (8) can be shown to apply to a generic LPTV system, see, e.g., [9] on the evaluation of C for a lumped-parameter network operating in the SS–LS regime.

The CM formalism is also the basis of LS noise analysis. As a first step, noise sources are amplitude-modulated by the periodic LS steady-state [11]; this process is equivalent to the passage of the stationary random process describing noise sources in dc conditions through a memoryless LPTV system of periodicity ω_k , thus implying noise frequency conversion into a sideband set $\omega_k \pm \omega$ (see also Section IV). Modulated noise sources can be characterized in terms of a cyclostationary random process [5], [17], [16], whose spectral representation is provided by the power and correlation spectra of its sideband components. It can be shown that sideband noise spectral components at $\omega_k \pm$ ω_1 and $\omega_l \pm \omega_2$ are uncorrelated unless $\omega_1 = \omega_2 = \omega$ (see Fig. 2); therefore, the noise spectral representation is reduced to the so-called sideband correlation matrix (SCM) S, which generally depends on ω and whose diagonal components are the sideband power spectra.

As a second step, the cyclostationary amplitude-modulated and frequency-converted (sideband) fluctuations can be interpreted as small-amplitude perturbations of the LS steady-state; therefore, the resulting output fluctuations can be analyzed through the SS–LS approach. This second frequency conversion through a LPTV system of the same periodicity ω_k results again in a cyclostationary process [17], and the relationship between the input and output SCM is easily derived by (8):

$$\boldsymbol{S}_{\delta \boldsymbol{y},\,\delta \boldsymbol{y}} = \boldsymbol{C}(\omega) \cdot \boldsymbol{S}_{\delta \boldsymbol{x},\,\delta \boldsymbol{x}} \cdot \boldsymbol{C}^{\dagger}(\omega). \tag{9}$$

Correlated Noise Sidebands ω_{-2}^{+} ω_{-1}^{+} ω_{0}^{+} ω_{1}^{+} ω_{2}^{+}

Fig. 2. Correlated noise sidebands.

From a circuit standpoint, the CM and noise SCM are the basis for the so-called multifrequency representation of a noisy *n*-port [9], generalizing the small-signal Norton or Thevenin equivalent circuits to the SS–LS regime. Consider in fact a noisy *n*-port operating in LS periodic conditions, and suppose to add a weak perturbation whose spectrum belongs to the sideband spectrum of the LS steady-state, with sideband frequency ω . The sideband amplitudes of port voltages and currents will be related by the Norton representation

$$\delta \boldsymbol{I} = \boldsymbol{Y}(\omega) \cdot \delta \boldsymbol{V} + \delta \boldsymbol{I}_n \tag{10}$$

where Y is the admittance CM and δI_n is the sideband shortcircuit (s.c.) current fluctuation vector described by the SCM $S_{\delta i_n, \delta i_n}$. Similarly, one has the Thevenin representation

$$\delta \boldsymbol{V} = \boldsymbol{Z}(\omega) \cdot \delta \boldsymbol{I} + \delta \boldsymbol{E}_n \tag{11}$$

where Z is the impedance CM and δE_n is a sideband opencircuit (o.c.) voltage fluctuation vector described by the SCM $S_{\delta e_n, \delta e_n}$; the open- and short-circuit fluctuation SCM's are related as

$$\boldsymbol{S}_{\delta \boldsymbol{e}_n, \, \delta \boldsymbol{e}_n} = \boldsymbol{Z}(\omega) \cdot \boldsymbol{S}_{\delta \boldsymbol{i}_n, \, \delta \boldsymbol{i}_n} \cdot \boldsymbol{Z}^{\dagger}(\omega). \tag{12}$$

Formally, each port of the multifrequency, multiport representation corresponds to a different sideband; as an example, Fig. 3 shows the relevant parallel representation for a two-port, where the input and output ports are expanded into a set of sideband ports.

Notice that the multifrequency, multiport model, exactly as the small-signal noisy model, provides both the small-signal response to an external sideband excitation, and the noise superimposed to it. In particular, in the absence of the external excitation, it enables to evaluate, once that the model is embedded into an external circuit, the noise spectrum in LS operation. The model therefore provides a complete noise characterization in the LS regime, and a full signal and noise characterization in the SS–LS regime. In the following sections, a physics-based evaluation of the multifrequency model will be developed, exploiting the concepts of frequency conversion of deterministic and random signals.

III. LARGE-SIGNAL AND SS-LS ANALYSIS

In the following discussion, attention will be focused on a simple bipolar drift-diffusion (DD) model, consisting of Poisson's equation and of the electron and hole continuity equations, see e.g., [18]. Although the limitations of the DD approach in the modeling of submicron devices are well known,

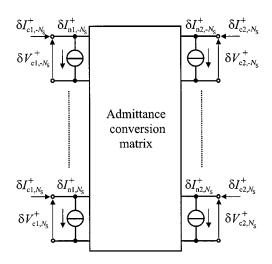


Fig. 3. Multifrequency representation of noisy two-port.

this technique can provide a first estimate of the device behavior. The extension of the approach proposed to higher-order transport models is in principle straightforward as far as the Green's function evaluation is concerned, though in practice extremely intensive from a computational standpoint. However, one has to consider that the modeling of the microscopic noise sources within a full hydrodynamic model is not completely established yet, see [19] and references therein for further details.

We assume that the DD model has been spatially discretized through the so-called finite-boxes approach (see, e.g., [20]) on a suitable grid, thus making the problem unknowns a set of time-domain spatial samples of the electrostatic potential φ and of the electron and hole densities n and p. For the sake of this discussion, let us define as N_i the number of nodes internal to the device volume, including those on the external boundaries but not pertaining to metallic contacts, and as N_x the number of external, boundary nodes lying on metallic contacts; N_c is, finally, the number of metallic contacts, ohmic or Schottky, corresponding to the device terminals, excluding the reference contact, which is grounded. Concerning the system unknowns, we denote with subscript i (x) the N_i (N_r) nodal values corresponding to the internal (external) nodes, which will be referred to as *nodal* unknowns. Finally, N_c contact voltages \boldsymbol{v}_c and currents i_c , collectively denoted as *circuit* unknowns, are also exploited.

A. LS Analysis

Let us discuss first the time-domain equations of the spatially discretized DD system under LS excitation. As well known, the LS regime requires the equations of the embedding circuit to be solved together with the physics-based model [21]. The discretized DD model leads to the following sets of nonlinear, dynamic nodal equations. The first corresponds to the $3 \times N_i$ discretized equations for the internal nodes

$$\boldsymbol{f}_{\varphi}(\boldsymbol{\varphi}_{i}, \boldsymbol{\varphi}_{x}, \boldsymbol{n}_{i}, \boldsymbol{p}_{i}) = \boldsymbol{0}$$
(13a)

$$\boldsymbol{f}_n(\boldsymbol{\varphi}_i, \boldsymbol{\varphi}_x, \boldsymbol{n}_i, \boldsymbol{n}_x, \boldsymbol{p}_i; \dot{\boldsymbol{n}}_i) = \boldsymbol{0}$$
 (13b)

$$\boldsymbol{f}_{p}(\boldsymbol{\varphi}_{i}, \boldsymbol{\varphi}_{x}, \boldsymbol{n}_{i}, \boldsymbol{p}_{i}, \boldsymbol{p}_{x}; \dot{\boldsymbol{p}}_{i}) = \boldsymbol{0}$$
 (13c)

where $\dot{x} = dx/dt$, and f_{φ} , f_n , f_p denote the discretized Poisson, electron continuity and hole continuity equations, respectively. Discretization of the boundary conditions on the external, contact nodes leads to the $3 \times N_x$ equations

$$\boldsymbol{b}_{\boldsymbol{\omega}}(\boldsymbol{\varphi}_{r},\boldsymbol{v}_{c}) = \boldsymbol{0} \tag{13d}$$

$$\boldsymbol{b}_n(\boldsymbol{\varphi}_i, \boldsymbol{\varphi}_x, \boldsymbol{n}_i, \boldsymbol{n}_x, \boldsymbol{p}_x; \dot{\boldsymbol{n}}_x) = \boldsymbol{0}$$
 (13e)

$$\boldsymbol{b}_{p}(\boldsymbol{\varphi}_{i}, \boldsymbol{\varphi}_{x}, \boldsymbol{n}_{x}, \boldsymbol{p}_{i}, \boldsymbol{p}_{x}; \dot{\boldsymbol{p}}_{x}) = \boldsymbol{0}$$
(13f)

which, in order, denote the boundary conditions relative to the Poisson and continuity equations. Boundary conditions on the noncontact device boundaries are already included in the equations for the internal nodes.¹

Finally, $2 \times N_c$ equations are further needed to close the system in the $3 \times (N_i + N_x) + 2 \times N_c$ unknowns. Such equations express the contact currents i_c as a function of the nodal unknowns

$$\boldsymbol{c}(\boldsymbol{\varphi}_i, \boldsymbol{\varphi}_x, \boldsymbol{n}_i, \boldsymbol{n}_x, \boldsymbol{p}_i, \boldsymbol{p}_x, \boldsymbol{i}_c; \, \boldsymbol{\dot{n}}_x, \boldsymbol{\dot{p}}_x) = \boldsymbol{0} \quad (13g)$$

and the constitutive relationships of the external circuit connected to the N_c ungrounded device terminals

$$e\left(\boldsymbol{v}_{c},\,\boldsymbol{i}_{c};\,\frac{d}{dt}\right)=\boldsymbol{s}$$
 (13h)

where s(t) is the set of periodic LS applied (voltage or current) sources.

According to the assumption of periodic LS steady-state, each unknown (nodal and circuit) is made of a superposition of harmonics, and therefore can be expressed according to

$$x(t) = \sum_{k=-N_L}^{N_L} X_k e^{j\omega_k t}$$
(14)

where the $2 \times N_L + 1$ complex spectral amplitudes correspond to $2 \times N_L + 1$ independent real numbers, since $X_{-k} = X_k^*$ for any k. We stress that such a complex representation is used in the formulation because it is well suited to introducing the SS–LS analysis; from a practical standpoint, a direct (real) Fourier representation is more convenient [21], and the present implementation, discussed in Section V, was made accordingly.

Further, notice that the harmonic decomposition has been truncated to a finite number of harmonics N_L ; this approximation is justified since, in practical circuits and devices characterized by a global low-pass response, the spectral amplitude finally decreases as the harmonic order k grows. For quasi periodic operation, the truncation criteria are more involved than for strictly periodic functions, although the present formulation still holds; for a discussion, see e.g., [21].

The HB method can be applied to solve the nonlinear algebraic system (13a)–(13h) as follows [22]. Let us define a set of $2 \times N_L + 1$ time samples t_k distributed in the fundamental period

¹Notice that the extension to the energy balance bipolar transport model requires to add the discretized energy transport equations for electrons and holes, and the corresponding boundary conditions, leading to $5 \times (N_i + N_x)$ equations. For the full hydrodynamic approach, moment conservation equations are further needed, leading to $7 \times (N_i + N_x)$ discretized equations.

[0, T[, where $T = 1/(2\pi\omega_0)$, and let us consider the collection \boldsymbol{x} of the sampled variable values $x(t_k)$, so that (14) yields

$$\boldsymbol{x} = \boldsymbol{\Gamma}^{-1} \cdot \boldsymbol{X} \qquad \boldsymbol{X} = \boldsymbol{\Gamma} \cdot \boldsymbol{x} \tag{15}$$

where matrix Γ^{-1} is given by

$$\mathbf{\Gamma}^{-1} = \begin{bmatrix} e^{j\omega_{-N_L}t_0} & \dots & e^{j\omega_0t_0} & \dots & e^{j\omega_{N_L}t_0} \\ \vdots & \vdots & \vdots & & \vdots \\ e^{j\omega_{-N_L}t_{N_L}} & \dots & e^{j\omega_0t_{N_L}} & \dots & e^{j\omega_{N_L}t_{N_L}} \\ \vdots & & \vdots & & \vdots \\ e^{j\omega_{-N_L}t_{2N_L}} & \dots & e^{j\omega_0t_{2N_L}} & \dots & e^{j\omega_{N_L}t_{2N_L}} \end{bmatrix}.$$
(16)

The choice of the time samples is often performed so as to make the condition number of matrix Γ as low as possible [22]. In the strictly periodic case, this amounts to choosing equispaced time samples, while for quasiperiodic regime an efficient approach, suitable for large-scale problems, is the frequency remapping technique [21], which enables the use of DFT algorithms for the time-frequency transformation.

The time derivative of (14) immediately yields the spectral components of $\dot{x}(t)$ as $\mathbf{\Omega} \cdot \mathbf{X}$, where $\mathbf{\Omega} = \text{diag}\{j\omega_k\}$ is a diagonal matrix of dimension $2 \times N_L + 1$. Moreover, given a memoryless function w[x(t)], its frequency-domain representation is given by $\mathbf{W} = \mathbf{\Gamma} \cdot \mathbf{w}[\mathbf{\Gamma}^{-1} \cdot \mathbf{X}]$ where \mathbf{w} is the collection of time-domain samples of w[x(t)].

Let us now introduce an expanded frequency-domain unknown vector collecting the frequency components of all node and circuit unknowns (i.e., including $2 \times N_L + 1$ scalar terms for each unknown), see Fig. 4. Moreover, scalar functions are expanded into their $(2 \times N_L + 1)$ frequency components as well. According to this notation, system (13a)–(13h) is translated, in the frequency domain, into the following set of $(2 \times N_L + 1)[3 \times (N_i + N_x) + 2 \times N_c]$ algebraic equations

$$\boldsymbol{F}_{\varphi}(\boldsymbol{\Phi}_{i},\,\boldsymbol{\Phi}_{x},\,\boldsymbol{N}_{i},\,\boldsymbol{P}_{i}) = \boldsymbol{0} \tag{17a}$$

$$\boldsymbol{F}_{n}(\boldsymbol{\Phi}_{i},\,\boldsymbol{\Phi}_{x},\,\boldsymbol{N}_{i},\,\boldsymbol{N}_{x},\,\boldsymbol{P}_{i};\,\boldsymbol{\Omega}_{i}\cdot\boldsymbol{N}_{i})=\boldsymbol{0}$$
(17b)

$$\boldsymbol{F}_{p}(\boldsymbol{\Phi}_{i},\,\boldsymbol{\Phi}_{x},\,\boldsymbol{N}_{i},\,\boldsymbol{P}_{i},\,\boldsymbol{P}_{x};\,\boldsymbol{\Omega}_{i}\cdot\boldsymbol{P}_{i})=\boldsymbol{0} \tag{17c}$$

$$\boldsymbol{B}_{\varphi}(\boldsymbol{\Phi}_x, \boldsymbol{V}_c) = \boldsymbol{0} \tag{17d}$$

$$\boldsymbol{B}_n(\boldsymbol{\Phi}_i, \, \boldsymbol{\Phi}_x, \, \boldsymbol{N}_i, \, \boldsymbol{N}_x, \, \boldsymbol{P}_x; \, \boldsymbol{\Omega}_x \cdot \boldsymbol{N}_x) = \boldsymbol{0}$$
(17e)

$$\boldsymbol{B}_{p}(\boldsymbol{\Phi}_{i}, \boldsymbol{\Phi}_{x}, \boldsymbol{N}_{x}, \boldsymbol{P}_{i}, \boldsymbol{P}_{x}; \boldsymbol{\Omega}_{x} \cdot \boldsymbol{P}_{x}) = \boldsymbol{0}$$
(17f)

$$C(\Phi_i, \Phi_x, N_i, N_x, P_i, P_x, I_c; \Omega_x \cdot N_x, \Omega_x \cdot P_x) = 0$$

$$\boldsymbol{E}(\boldsymbol{V}_c,\,\boldsymbol{I}_c;\,\boldsymbol{\Omega}) = \boldsymbol{S} \tag{17h}$$

where Ω_i and Ω_x are block diagonal matrices made, respectively, of N_i and N_x replicas of Ω . The solution of the nonlinear HB system can be performed by means of Newton or quasi-Newton iteration, see [21] for a discussion of the specific problems arising in device modeling. In particular, large-scale problems, such as those arising in 2-D device simulation, require to exploit iterative techniques for the solution of the linear systems arising in the Newton method; see e.g., [21], [23].

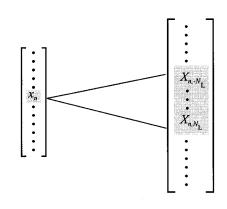


Fig. 4. Expanded vector for the frequency components of vector dynamical equations.

B. SS-LS Analysis

In order to introduce the SS–LS analysis, let us apply the equivalence theorem [24] to the external device terminals, so as to replace the circuit equation (13h) with a linear relationship with equivalent current (or voltage) sources \mathbf{s}_{eq} corresponding to the terminal currents (or voltages) evaluated in the LS steady-state

$$\boldsymbol{e}'(\boldsymbol{v}_c, \, \boldsymbol{i}_c) = \boldsymbol{s}_{eq}.\tag{18}$$

If we superimpose now a small-amplitude harmonic perturbation δs_{eq} to the LS steady-state, each model unknown (nodal and circuit) can be decomposed as the sum of the LS steady-state solution and a small perturbation $\delta x: x(t) = x_0(t) + \delta x(t)$. After linearization, (13a)–(13h) can be cast into the form

$$\boldsymbol{f}_{\varphi,\boldsymbol{\varphi}_{i}} \cdot \delta \boldsymbol{\varphi}_{i} + \boldsymbol{f}_{\varphi,\boldsymbol{\varphi}_{x}} \cdot \delta \boldsymbol{\varphi}_{x} + \boldsymbol{f}_{\varphi,\boldsymbol{n}_{i}} \cdot \delta \boldsymbol{n}_{i} + \boldsymbol{f}_{\varphi,\boldsymbol{p}_{i}} \cdot \delta \boldsymbol{p}_{i} = \boldsymbol{0}$$
(19a)

$$\begin{aligned} \boldsymbol{f}_{n,\boldsymbol{\varphi}_{i}} \cdot \delta \boldsymbol{\varphi}_{i} + \boldsymbol{f}_{n,\boldsymbol{\varphi}_{x}} \cdot \delta \boldsymbol{\varphi}_{x} + \boldsymbol{f}_{n,\boldsymbol{n}_{i}} \cdot \delta \boldsymbol{n}_{i} + \boldsymbol{f}_{n,\boldsymbol{n}_{x}} \cdot \delta \boldsymbol{n}_{x} \\ &+ \boldsymbol{f} \quad \cdot \delta \boldsymbol{n}_{i} + \boldsymbol{f} \quad \cdot \cdot \delta \dot{\boldsymbol{n}}_{i} = \boldsymbol{0} \end{aligned}$$
(19b)

$$\boldsymbol{f}_{p,\boldsymbol{\varphi}_{i}} \cdot \delta \boldsymbol{\varphi}_{i} + \boldsymbol{f}_{p,\boldsymbol{\varphi}_{x}} \cdot \delta \boldsymbol{\varphi}_{x} + \boldsymbol{f}_{p,\boldsymbol{n}_{i}} \cdot \delta \boldsymbol{n}_{i} + \boldsymbol{f}_{p,\boldsymbol{p}_{i}} \cdot \delta \boldsymbol{p}_{i}$$

$$+ \boldsymbol{J}_{p,\boldsymbol{p}_{x}} \cdot o\boldsymbol{p}_{x} + \boldsymbol{J}_{p,\boldsymbol{\dot{p}}_{i}} \cdot o\boldsymbol{p}_{i} = \boldsymbol{0}$$

$$(19c)$$

$$\boldsymbol{b}_{\varphi,\boldsymbol{\varphi}_x} \cdot \boldsymbol{\delta} \boldsymbol{\varphi}_x + \boldsymbol{b}_{\varphi,\boldsymbol{v}_c} \cdot \boldsymbol{\delta} \boldsymbol{v}_c = \boldsymbol{0} \tag{19d}$$

$$\boldsymbol{o}_{n,\boldsymbol{\varphi}_{i}} \cdot \boldsymbol{o}\boldsymbol{\varphi}_{i} + \boldsymbol{o}_{n,\boldsymbol{\varphi}_{x}} \cdot \boldsymbol{o}\boldsymbol{\varphi}_{x} + \boldsymbol{o}_{n,\boldsymbol{n}_{i}} \cdot \boldsymbol{o}\boldsymbol{n}_{i} + \boldsymbol{o}_{n,\boldsymbol{n}_{x}} \cdot \boldsymbol{o}\boldsymbol{n}_{x}$$

$$+ \boldsymbol{b} \quad \boldsymbol{\delta}\boldsymbol{x} + \boldsymbol{b} \quad \boldsymbol{\delta}\boldsymbol{x} - \boldsymbol{O} \quad (10a)$$

$$+ \boldsymbol{o}_{n,\boldsymbol{p}_{x}} \cdot \boldsymbol{o}_{\boldsymbol{p}_{x}} + \boldsymbol{o}_{n,\boldsymbol{n}_{x}} \cdot \boldsymbol{o}_{\boldsymbol{n}_{x}} = \mathbf{0}$$
(19e)

$$\boldsymbol{o}_{p,\boldsymbol{\varphi}_{i}} \cdot \boldsymbol{o}\boldsymbol{\varphi}_{i} + \boldsymbol{o}_{p,\boldsymbol{\varphi}_{x}} \cdot \boldsymbol{o}\boldsymbol{\varphi}_{x} + \boldsymbol{o}_{p,\boldsymbol{n}_{x}} \cdot \boldsymbol{o}\boldsymbol{n}_{x} + \boldsymbol{o}_{p,\boldsymbol{p}_{i}} \cdot \boldsymbol{o}\boldsymbol{p}_{i} \\ + \boldsymbol{b}_{p,\boldsymbol{p}} \cdot \boldsymbol{\delta}\boldsymbol{p}_{x} + \boldsymbol{b}_{p,\boldsymbol{p}} \cdot \boldsymbol{\delta}\boldsymbol{\dot{p}}_{x} = \mathbf{0}$$
(19f)

$$c_{\boldsymbol{\varphi}_i} \cdot \delta \boldsymbol{\varphi}_i + c_{\boldsymbol{\varphi}_x} \cdot \delta \boldsymbol{\varphi}_x + c_{\boldsymbol{n}_i} \cdot \delta \boldsymbol{n}_i + c_{\boldsymbol{n}_x} \cdot \delta \boldsymbol{n}_x + c_{\boldsymbol{p}_i} \cdot \delta \boldsymbol{p}_i + c_{\boldsymbol{p}_x}$$

$$\cdot \delta \boldsymbol{p}_x + \boldsymbol{c}_{\boldsymbol{n}_x} \cdot \delta \boldsymbol{n}_x + \boldsymbol{c}_{\boldsymbol{p}_x} \cdot \delta \boldsymbol{p}_x + \boldsymbol{c}_{\boldsymbol{i}_c} \cdot \delta \boldsymbol{i}_c = \boldsymbol{0}$$
(19g)

$$\boldsymbol{e}_{\boldsymbol{v}_c}' \cdot \delta \boldsymbol{v}_c + \boldsymbol{e}_{\boldsymbol{i}_c}' \cdot \delta \boldsymbol{i}_c = \delta \boldsymbol{s}_{eq} \tag{19h}$$

where the first factor of each term is the (matrix) gradient of the corresponding model equation evaluated in the LS steadystate. The vector system (19a)–(19h) is analogous to the scalar example of LPTV (2). Notice, however, that Poisson's equation (and its boundary condition) is memoryless, and that in (19h) the matrices e' are diagonal, with diagonal elements equal to either 0 or 1. If the equivalent source for terminal n is a current (voltage) generator, the (n, n) element of $e'_{i_c}(e'_{v_c})$ is 1, and the (n, n) element of $e'_{v_c}(e'_{i_c})$ is zero.

According to the procedure outlined in Section II, each unknown is expanded into the sideband formulation

$$\delta x(t) = \sum_{k=-N_S}^{N_S} \delta X_k^+ e^{j\omega_k^+ t}$$
(20)

where in general, as discussed later, $N_S \neq N_L$. Then, system (19a)–(19h) is expressed in the spectral domain leading to a conversion matrix formulation akin to (8)

$$C_{f_{\varphi,\varphi_i}} \cdot \delta \Phi_i^+ + C_{f_{\varphi,\varphi_x}} \cdot \delta \Phi_x^+ + C_{f_{\varphi,n_i}} \cdot \delta N_i^+ + C_{f_{\varphi,p_i}} \cdot \delta P_i^+ = 0$$
(21a)
$$C_{\mathcal{E}} \cdot \delta \Phi^+ + C_{\mathcal{E}} \cdot \delta \Phi^+ + C_{\mathcal{E}} \cdot \delta N^+$$

$$\begin{aligned} & + \boldsymbol{C}_{\boldsymbol{f}_{n,\boldsymbol{n}_{i}}} \cdot \delta \boldsymbol{N}_{x}^{+} + \boldsymbol{C}_{\boldsymbol{f}_{n,\boldsymbol{p}_{i}}} \cdot \delta \boldsymbol{P}_{i}^{+} \\ & + \boldsymbol{C}_{\boldsymbol{f}_{n,\boldsymbol{n}_{i}}} \cdot \boldsymbol{\Omega}_{i}^{+} \cdot \delta \boldsymbol{N}_{i}^{+} = \boldsymbol{0} \end{aligned}$$

$$(21b)$$

$$C_{f_{p,\varphi_{i}}} \cdot \delta \Phi_{i}^{+} + C_{f_{p,\varphi_{x}}} \cdot \delta \Phi_{x}^{+} + C_{f_{p,n_{i}}} \cdot \delta N_{i}^{+} + C_{f_{p,p_{i}}} \cdot \delta P_{i}^{+} + C_{f_{p,p_{x}}} \cdot \delta P_{x}^{+} + C_{f_{p,p_{i}}} \cdot \Omega_{i}^{+} \cdot \delta P_{i}^{+} = 0$$
(21c)

$$C_{\boldsymbol{b}_{\varphi},\boldsymbol{\varphi}_{x}} \cdot \delta \Phi_{x}^{+} + C_{\boldsymbol{b}_{\varphi},\boldsymbol{v}_{c}} \cdot \delta V_{c}^{+} = 0 \qquad (21d)$$

$$C_{\boldsymbol{b}_{n,\boldsymbol{\varphi}_{i}}} \cdot \delta \boldsymbol{\Phi}_{i}^{\top} + C_{\boldsymbol{b}_{n,\boldsymbol{\varphi}_{x}}} \cdot \delta \boldsymbol{\Phi}_{x}^{\top} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{i}}} \cdot \delta \boldsymbol{N}_{i}^{\top} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{x}}} \cdot \delta \boldsymbol{N}_{x}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{p}_{x}}} \cdot \delta \boldsymbol{P}_{x}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{x}}} \cdot \Omega_{x}^{+} \cdot \delta \boldsymbol{N}_{x}^{+} = \mathbf{0}$$
(21e)

$$C_{\boldsymbol{b}_{p,\boldsymbol{\varphi}_{i}}} \cdot \delta \Phi_{i}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{\varphi}_{x}}} \cdot \delta \Phi_{x}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{n}_{x}}} \cdot \delta N_{x}^{+} \\ + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{i}}} \cdot \delta P_{i}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{x}}} \cdot \delta P_{x}^{+} \\ + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{x}}} \cdot \Omega_{x}^{+} \cdot \delta P_{x}^{+} = 0$$

$$(21f)$$

$$C_{\boldsymbol{c}_{\boldsymbol{\varphi}_{i}}} \cdot \delta \boldsymbol{\Phi}_{i}^{+} + C_{\boldsymbol{c}_{\boldsymbol{\varphi}_{x}}} \cdot \delta \boldsymbol{\Phi}_{x}^{+} + C_{\boldsymbol{c}_{\boldsymbol{n}_{i}}} \cdot \delta \boldsymbol{N}_{i}^{+} + C_{\boldsymbol{c}_{\boldsymbol{n}_{x}}} \cdot \delta \boldsymbol{N}_{x}^{+} + C_{\boldsymbol{c}_{\boldsymbol{p}_{i}}} \cdot \delta \boldsymbol{P}_{i}^{+} + C_{\boldsymbol{c}_{\boldsymbol{p}_{x}}} \cdot \delta \boldsymbol{P}_{x}^{+} + C_{\boldsymbol{c}_{\boldsymbol{n}_{x}}} \cdot \boldsymbol{\Omega}_{x}^{+} \cdot \delta \boldsymbol{N}_{x}^{+} + C_{\boldsymbol{c}_{\boldsymbol{p}_{x}}} \cdot \boldsymbol{\Omega}_{x}^{+} \cdot \delta \boldsymbol{P}_{x}^{+} + C_{\boldsymbol{c}_{\boldsymbol{i}_{c}}} \cdot \delta \boldsymbol{I}_{c}^{+} = \mathbf{0}$$
(21g)

$$\boldsymbol{C}_{\boldsymbol{e}_{\boldsymbol{v}_{c}}^{\prime}} \cdot \delta \boldsymbol{V}_{c}^{+} + \boldsymbol{C}_{\boldsymbol{e}_{\boldsymbol{i}_{c}}^{\prime}} \cdot \delta \boldsymbol{I}_{c}^{+} = \delta \boldsymbol{S}_{eq}^{+}.$$
(21h)

The conversion matrices C in (21a)–(21h) are assembled according to the following rule, here presented, as an example, for $C_{f_{\varphi,\varphi_i}}$. For each node and for each nodal equation, each element of the matrix f_{φ,φ_i} is converted into frequency domain, resulting in a CM according to the memoryless part of (7), thus making $C_{f_{\varphi,\varphi_i}}$ a matrix of matrices, see Fig. 5. For instance, for node j and nodal equation i, the elements of the conversion submatrix are:

$$\left(\boldsymbol{C}_{\boldsymbol{f}_{\varphi_{i},\boldsymbol{\varphi}_{i},j}}\right)_{q,n} = \left(\boldsymbol{F}_{\varphi_{i},\boldsymbol{\varphi}_{i,j}}\right)_{q-n}$$
(22)

where q, n are sideband indices, and $\mathbf{F}_{\varphi_i, \varphi_{i,j}}$ is the vector of frequency components of $f_{\varphi_i, \varphi_{i,j}}(t)$. As far as the memory part of (19a)–(19h) is concerned, according to the easier example (7) we have introduced in (21a)–(21h) the matrices Ω_i^+ and Ω_x^+ . These are block diagonal matrices, replicating N_i and N_x times, respectively, the fundamental matrix $\Omega^+ = \text{diag}\{j\omega_k^+\}$.

To fully account for all the possible conversions among the sidebands up to the order N_S , the LS solution must be carried out to the order $N_L = 2 \times N_S$, see (7). System (21a)–(21h) is therefore a set of $(2 \times N_S + 1)[3 \times (N_i + N_x) + 2 \times N_c]$

Fig. 5. Expanded matrix for the frequency components of function (matrix) gradients.

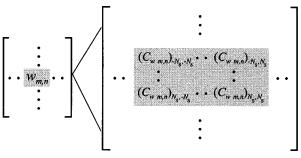
complex equations, to be compared with the $(2 \times N_L + 1)[3 \times (N_i + N_x) + 2 \times N_c]$ real equations to be solved in the LS case. From a computational standpoint it is also important to emphasize that if a Newton method is used to solve the LS equations, the harmonic component of each element of the matrix gradients in (19a)–(19h), necessary to assemble the conversion matrices as described in (22), are readily evaluated from the Jacobian matrix in the last iteration of the Newton loop [25].

In order to enable evaluating the device terminal CM, the source term δS_{eq}^+ in (21a)–(21h) must include an independent excitation for each sideband and each terminal; this implies that δS_{eq}^+ is a unit diagonal matrix of dimension $(2 \times N_S + 1) \times N_c$. In the source matrix, each block of $2 \times N_S + 1$ columns corresponds to the excitation of one device terminal (e.g., terminal *i*) for every sideband, and the solution of (21a)–(21h) allows to evaluate all the blocks of the device CM corresponding to injection in terminal *i*, i.e., the device conversion submatrices between terminal *i* and every device terminal (see Fig. 6). In particular, the device Y CM is evaluated when the forcing term is a voltage source, and the Z CM when the forcing term is a current source. The evaluation of hybrid CM's is similar.

IV. LS PHYSICS-BASED NOISE ANALYSIS

The aim of physics-based noise analysis is to evaluate the second order statistical properties of the fluctuations of the terminal electrical variables induced by the fundamental microscopic velocity and carrier number fluctuations that occur inside the device. For LS device operation, this corresponds to the evaluation of the SCM of the equivalent s.c. current (or o.c. voltage, or any set corresponding to hybrid representations) noise generators at the device ports, as shown in Fig. 3. According to the Langevin approach [26], the microscopic noise sources appear as stochastic forcing terms in the right-hand-side of the carrier continuity equations [12], and therefore are homogeneous to a generation-recombination (GR) rate.

The basic assumption is that microscopic fluctuations have small amplitude, so that the device response can be evaluated by linearizing the model equations around the noiseless steadystate working point, and thus enabling the conversion matrix formalism to be exploited. Due to linearity, the induced fluctuations at the device terminals can be evaluated by means of a convolution integral of the microscopic fluctuations with suitable Green's functions of the linearized system, thus extending to the LS case the Green's function approach in [12], originally



 $2 \times N_s + 1$ columns

Evaluation of the device terminal conversion matrix.

introduced for the noise analysis of devices operating in a stationary (dc) steady-state. The relevant Green's functions relate a unit injection in the electron or hole continuity equations to the o.c. voltage or s.c. current variations at the device terminals, depending on the boundary conditions enforced on the linearized system. Both microscopic and terminal fluctuations are expressed as sidebands, so that the Green's functions turn out to be conversion matrices, referred to as conversion Green's functions (CGF).

Injection in terminal i

♦ 2×N_s+1

rows

The physics based noise analysis is therefore carried out in two steps, depicted in Fig. 7. The first consists in assessing the statistical properties of the microscopic noise sources as a result of the time-varying, LS noiseless steady-state. The second step is the propagation of the microscopic noise sources to the device terminals by means of the relevant CGFs, thus expressing the terminal noise SCM according to a generalization of the Green's function technique for noise analysis in dc regime [12], [15]. The evaluation of the CGF can be carried out by applying SS-LS analysis to the Langevin system.

A. Microscopic Noise Sources

In the first place the statistical properties of the microscopic fluctuations must be evaluated in the LS regime. In our work, we consider two kinds of microscopic fluctuations, namely velocity (diffusion noise) fluctuations and population (GR noise) fluctuations [12]; both fluctuations are assumed to be spatially uncorrelated. Moreover, while hole and electron population fluctuations can be correlated, velocity fluctuations of electrons and holes are physically uncorrelated. In DC steady-state conditions, both are modeled as white processes [26] related to the fast microscopic dynamics of particles, with characteristic times of the order of less than 1 ps. For this reason, such processes can be considered as slowly modulated by the LS instantaneous working point [11], [27] (see Fig. 7). Such an amplitude modulation can be modeled as the passage through a time-varying, memoryless linear system, characterized by a CM independent of the input frequency. Following this, the local noise source becomes a cyclostationary noise process which can be characterized by a SCM, as outlined in Section II, implying that frequency components belonging to different sidebands are correlated only if their frequency deviation from the respective LS frequency is the same. Notice that GR noise

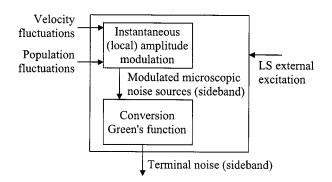


Fig. 7. Physics-based noise analysis in LS conditions.

is often modeled through equivalent current density noise sources [28] with a Lorentzian spectrum, characterized by time constants typically in the range 1 ms \div 1 μ s. In this case, the source modulation should be restricted to frequency components of the steady state below the Lorentzian cutoff frequency [29]. The same remark applies for the phenomenological source exploited to model 1/f noise [30]. Such a noise mechanism, despite its relevance in LS operated circuits, still lacks a widely accepted physical description, so that 1/f noise physics-based analysis would require a careful comparison to measured data (see also the discussion in [29]).

Let us consider first velocity fluctuations. These must be expressed in terms of equivalent current density fluctuations, in order to be included as forcing terms for the continuity equations [26]. Let us define as $\xi_{\alpha,\kappa}$ ($\alpha = n, p$ and $\kappa = x, y, z$) the κ (spatial) component of the vector current density fluctuation for carrier α . The elements of the SCM of the velocity fluctuations for spatial components κ_1 and κ_2 are given by

$$\begin{pmatrix} \boldsymbol{K}_{\xi_{n,\kappa_{1}},\xi_{n,\kappa_{2}}}(\boldsymbol{r}) \end{pmatrix}_{q,n} = 2q^{2} \begin{bmatrix} D_{n,\kappa_{1}\kappa_{2}} + D_{n,\kappa_{2}\kappa_{1}}^{*} \end{bmatrix} (\boldsymbol{N}(\boldsymbol{r}))_{q-n}$$
(23)

$$\begin{aligned} \mathbf{A}_{\xi_{p,\kappa_1},\xi_{p,\kappa_2}}(\mathbf{r}) \Big|_{q,n} \\ &= 2q^2 \left[D_{p,\kappa_1\kappa_2} + D^*_{p,\kappa_2\kappa_1} \right] (\mathbf{P}(\mathbf{r}))_{q-n}. \end{aligned}$$
(24)

for electrons and holes, respectively. In the previous equations, $D_{\kappa_1\kappa_2}$ is the (κ_1, κ_2) component of the diffusivity tensor for the corresponding carrier, and N(r), P(r) are the frequency components of the LS electron and hole density distributions.

Concerning population fluctuations, we indicate as γ_{α} ($\alpha =$ n, p) the microscopic noise source appearing in the continuity equation for carrier α . The SCM of population fluctuations can be obtained by amplitude modulation of the dc expression [28], which depends on the steady-state value of the sum of generation and recombination rates, and will be denoted as $K_{\gamma_{\alpha}, \gamma_{\beta}}(r)$.

B. Terminal Noise Evaluation Through the CGF Approach

According to the Langevin formulation and the linearization of the device model around the instantaneous LS working-point, the (sideband) device response is expressed as a function of the relevant Green's functions, depending on the variable chosen as output. Both contact o.c. voltages or s.c. currents can be sought for. Since microscopic noise sources are distributed within the device volume, the output is expressed through a convolution

Fig. 6.

Device terminal

Observation

in terminal j

conversion matrix

integral whose kernel is the (space-dependent) CGF, thus extending the result (8). For instance, the s.c. current induced at terminal i is evaluated with the superposition integral:

$$\delta I_{c,i}^{+} = \sum_{\alpha=n,p} \left[\int_{\Omega} G_{\alpha,i}(\boldsymbol{r}; \,\omega) \cdot \boldsymbol{\Gamma}_{\alpha}^{+}(\boldsymbol{r}) \, d\boldsymbol{r} + \sum_{\kappa=x,\,y,\,z} \cdot \int_{\Omega} \frac{\partial}{\partial \kappa} G_{\alpha,\,i}(\boldsymbol{r}; \,\omega) \cdot \boldsymbol{\Xi}_{\alpha,\,\kappa}^{+}(\boldsymbol{r}) \, d\boldsymbol{r} \right].$$
(25)

where Ω is the device volume, the Green's function $G_{\alpha,i}$ is the conversion matrix (CGF) for continuity equation α and terminal $i, \Gamma^+_{\alpha}(\mathbf{r}) (\Xi^+_{\alpha,\kappa}(\mathbf{r}))$ is the vector of sideband amplitudes for the microscopic noise source $\gamma_{\alpha}(\mathbf{r}) (\xi_{\alpha,\kappa}(\mathbf{r}))$, and ω is the sideband displacement frequency.

Finally, by properly extending (9) the SCM of the s.c. noise currents for terminals i and j is derived as:

$$S_{\delta i_{c,i},\delta i_{c,j}} = \sum_{\alpha,\beta=n,p} \int_{\Omega} \boldsymbol{G}_{\alpha,i}(\boldsymbol{r};\,\omega) \cdot \boldsymbol{K}_{\gamma_{\alpha},\gamma_{\beta}}(\boldsymbol{r}) \cdot \boldsymbol{G}_{\beta,j}^{\dagger}(\boldsymbol{r};\,\omega) \, d\boldsymbol{r} + \sum_{\alpha=n,p} \sum_{\kappa_{1},\kappa_{2}=x,y,z} \int_{\Omega} \frac{\partial}{\partial\kappa_{1}} \boldsymbol{G}_{\alpha,i}(\boldsymbol{r};\,\omega) \cdot \boldsymbol{K}_{\xi_{\alpha,\kappa_{1}},\xi_{\alpha,\kappa_{2}}}(\boldsymbol{r}) \cdot \frac{\partial}{\partial\kappa_{2}} \boldsymbol{G}_{\alpha,j}^{\dagger}(\boldsymbol{r};\,\omega) \, d\boldsymbol{r}.$$
(26)

The previous formulation allows to evaluate the global SCM of the s.c. noise current at the device terminals.

The CGFs are evaluated from the discretized linear system (21a)–(21h) already introduced for the SS–LS analysis, though for noise analysis the linearized system must be slightly modified. As no external forcing term is applied at the device terminals, (21h) is not needed anymore, while an auxiliary equation must be added to enforce s.c. (o.c.) boundary conditions if the s.c. (o.c.) CGF is sought for. To fix the ideas, we will refer in the following discussion to s.c. boundary conditions. A unit diagonal forcing term, i.e., an independent sideband by sideband excitation, is then added, for each node, to the right-hand-side of each continuity equation, enabling the evaluation of the CGFs. The resulting system of equations is

$$\begin{split} C_{f_{\varphi,\varphi_{i}}} \cdot \delta \Phi_{i}^{+} + C_{f_{\varphi,\varphi_{x}}} \cdot \delta \Phi_{x}^{+} + C_{f_{\varphi,n_{i}}} \cdot \delta N_{i}^{+} \\ + C_{f_{\varphi,p_{i}}} \cdot \delta P_{i}^{+} = 0 \end{split} \tag{27a} \\ C_{f_{n,\varphi_{i}}} \cdot \delta \Phi_{i}^{+} + C_{f_{n,\varphi_{x}}} \cdot \delta \Phi_{x}^{+} + C_{f_{n,n_{i}}} \cdot \delta N_{i}^{+} \\ + C_{f_{n,n_{x}}} \cdot \delta N_{x}^{+} + C_{f_{n,p_{i}}} \cdot \delta P_{i}^{+} \\ + C_{f_{n,n_{i}}} \cdot \Omega_{i}^{+} \cdot \delta N_{i}^{+} = S_{n}^{+} \delta_{\alpha,n} \end{aligned} \tag{27b}$$

$$C_{f_{p,\varphi_{i}}} \cdot \delta \Phi_{i}^{+} + C_{f_{p,\varphi_{x}}} \cdot \delta \Phi_{x}^{+} + C_{f_{p,n_{i}}} \cdot \delta N_{i}^{+} + C_{f_{p,p_{i}}} \cdot \delta P_{i}^{+} + C_{f_{p,p_{x}}} \cdot \delta P_{x}^{+} + C_{f_{p,\varphi_{i}}} \cdot \Omega_{i}^{+} \cdot \delta P_{i}^{+} = S_{n}^{+} \delta_{\alpha,p}$$
(27c)

$$C_{\boldsymbol{b}_{\varphi}, \varphi_{x}} \cdot \delta \Phi_{x}^{+} + C_{\boldsymbol{b}_{\varphi}, \boldsymbol{v}_{c}} \cdot \delta \boldsymbol{V}_{c}^{+} = \boldsymbol{0}$$
(27d)

$$C_{\boldsymbol{b}_{n,\boldsymbol{\varphi}_{i}}}^{\boldsymbol{\mu},\boldsymbol{\mu}_{x}} \cdot \delta \boldsymbol{\Phi}_{i}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{\varphi}_{x}}} \cdot \delta \boldsymbol{\Phi}_{x}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{i}}} \cdot \delta \boldsymbol{N}_{i}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{x}}} \cdot \delta \boldsymbol{N}_{x}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{p}_{x}}} \cdot \delta \boldsymbol{P}_{x}^{+} + C_{\boldsymbol{b}_{n,\boldsymbol{n}_{x}}} \cdot \boldsymbol{\Omega}_{x}^{+} \cdot \delta \boldsymbol{N}_{x}^{+} = \boldsymbol{0}$$
(27e)

$$C_{\boldsymbol{b}_{p,\boldsymbol{\varphi}_{i}}} \cdot \delta \Phi_{i}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{\varphi}_{x}}} \cdot \delta \Phi_{x}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{n}_{x}}} \cdot \delta N_{x}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{i}}} \cdot \delta N_{x}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{i}}} \cdot \delta N_{x}^{+} + C_{\boldsymbol{b}_{p,\boldsymbol{p}_{i}}} \cdot \delta N_{x}^{+} + \delta P_{x}^{+} = 0 \quad (27f)$$

$$C_{\boldsymbol{c}_{\boldsymbol{\varphi}_{i}}} \cdot \delta \Phi_{i}^{+} + C_{\boldsymbol{c}_{\boldsymbol{\varphi}_{x}}} \cdot \delta \Phi_{x}^{+} + C_{\boldsymbol{c}_{n_{i}}} \cdot \delta N_{i}^{+} + C_{\boldsymbol{c}_{n_{x}}} \cdot \delta N_{x}^{+} + C_{\boldsymbol{c}_{p_{i}}} \cdot \delta P_{i}^{+} + C_{\boldsymbol{c}_{p_{x}}} \cdot \delta P_{x}^{+} + C_{\boldsymbol{c}_{n_{x}}} \cdot \Omega_{x}^{+} \cdot \delta N_{x}^{+} + C_{\boldsymbol{c}_{p_{x}}} \cdot \Omega_{x}^{+} \cdot \delta P_{x}^{+} + C_{\boldsymbol{c}_{i_{c}}} \cdot \boldsymbol{G}_{\alpha} = 0 \quad (27g)$$

$$\delta V^{+} = 0. \quad (27b)$$

In (27a)–(27h) we have substituted the unknowns δI_c^+ with G_{α} corresponding to a global CGF collecting the CGF's $G_{\alpha, i}$ defined for each terminal; δ is the Kronecker symbol, expressing that the source is injected either in the electron or in the hole continuity equation, to solve for the electron or hole CGF, respectively. Source terms \boldsymbol{S}_n^+ and \boldsymbol{S}_p^+ correspond to the unit source terms, homogeneous to an injected current, and are unit diagonal matrices of dimension $(2 \times N_S + 1) \times N_i$. Notice that the source term is explicitly placed in the internal nodes of the discretized model only, since injection in a terminal node results in a unit diagonal CGF for that terminal current, and to zero for the other terminal currents. In order to directly evaluate the CGFs, one factorization and $2 \times (2 \times N_S + 1) \times N_i$ backsubstitutions of the linear system (27a)–(27h) are therefore needed, thus making LS noise analysis a formidable task, unless the numerical techniques discussed in the next Section are implemented.

V. NUMERICAL IMPLEMENTATION AND EXAMPLES

We have implemented the LS HB analysis in a two-carrier drift-diffusion model discretized by means of the finite-boxes technique. A mixed-mode approach was exploited, whereby the discretized model is solved together with the equations of the external circuit; solution of the HB system was obtained through Newton iteration. SS-LS and noise analyzes were implemented in the numerical model following the formulation presented in Sections III and IV; however, the evaluation of the CGF's was not carried out directly (as discussed in Section IV), due to the heavy computational burden corresponding to the $2 \times (2 \times$ $N_{S}+1$ × N_{i} backsubstitutions of the linear system (27a)–(27h). Rather, an efficient numerical technique, derived as a straightforward extension of Branin's approach proposed by some of the present authors in [12] for dc noise analysis, has been exploited to compute the unknown G_{α} , allowing for the reduction of the computational intensity to a number of system backsolves equal to $N_c \times (2 \times N_S + 1)$, i.e., the same number of backsolves needed for the evaluation of the terminal device CM by means of SS-LS analysis.

As an example of practical application, we have simulated an rf varactor frequency doubler, which can also be exploited to realize a subharmonic mixer. The circuit is shown in Fig. 8; subharmonic mixing can be achieved by injecting an IF signal across the diode terminals (i.e., into node A) through a bandpass filter centered at the IF frequency. The doubler consists of a reverse-biased silicon pn diode connected to a standard external circuit providing input and output matching together with suppression of unwanted harmonics through the idler resonators. The diode chosen is symmetrical, with a doping level 10^{17} cm⁻³, length 25 μ m and area $10^4 \mu$ m². The dc and small-signal behavior of the

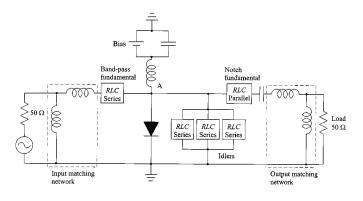


Fig. 8. Circuit scheme for the varactor frequency doubler.

diode, simulated by means of the drift-diffusion model, was exploited to extract a standard lumped-parameter LS equivalent circuit model, later used for circuit design by means of the HP MDS simulator. The circuit was optimized assuming as a goal the frequency conversion efficiency from the fundamental (at 1 GHz) to the second harmonic, obtaining a 60% conversion gain at 10 dBm input power. The physics-based HB LS simulation of the diode, embedded into the optimized circuit, was carried out with 350 grid points and $N_L = 4$ harmonics (plus dc).

For the sake of the application of the device as a mixer, the diode CM is relevant to predict circuit performance. Some of the elements of the diode admittance CM are shown in Fig. 9 as a function of the sideband frequency; the continuous line are results derived from the conventional LS equivalent circuit, diamonds are derived through SS-LS analysis of the physics-based model. The meaning of the CM elements shown can be explained as follows: out-of-diagonal elements such as $Y_{2,0}$ denote the amount of up-conversion to the second sideband (i.e., around 2 GHz) experienced by an intermediate frequency (IF) input signal. Diagonal elements such as $Y_{2,2}$ express on the other hand the current response in the second sideband for an applied voltage at the same absolute frequency; from a circuit standpoint, such elements can be interpreted as the small-signal admittance resulting from the quasistatic diode capacitance averaged on the instantaneous, periodically varying, working point. Since the embedding circuit has been optimized for frequency doubling rather than for IF upconversion, the element $Y_{2,1}$ denoting conversion from the first to the second harmonic actually is larger than $Y_{2,0}$. As seen from Fig. 9, excellent agreement exists between the predictions of the physics-based and circuit models.

Concerning noise, we evaluated the SCM of the external (s.c. current) diode noise sources and compared it with the results derived from standard circuit LS noise theory, i.e., by generalizing Nyquist theorem according to [11], [17]. The agreement is generally good, and is excellent for the diagonal elements of the SCM shown in Fig. 10. Since in reverse bias the shot-like diode noise is negligible, the varactor diode noise is expected to originate from resistive parasitics, consistent with the increasing frequency behavior shown in Fig. 10 which, from a circuit standpoint, can be derived through a simple series RC circuit where the resistor exhibits thermal noise. This behavior is confirmed, as discussed further on, by the results from physics-based analysis concerning the internal behavior of the diode noise distribution.

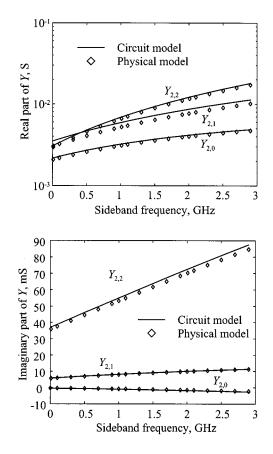


Fig. 9. Frequency dependence of the real (top) and imaginary (bottom) part of the elements $Y_{2,2}$, $Y_{2,1}$ and $Y_{2,0}$ of the varactor admittance conversion matrix. The full line is the result from circuit analysis, the symbols from the physical model.

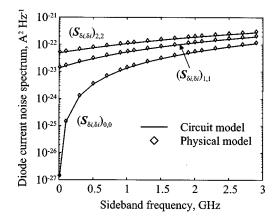


Fig. 10. Comparison between the frequency dependence of the diode noise current correlation spectra evaluated through circuit and physics-based analysis for the varactor frequency doubler. Only the power spectra of sidebands 0, 1 and 2 are shown.

The overall noise performance of the doubler is shown, as the noise power spectrum on the load resistor as a function of frequency, in Fig. 11. The total noise and the contribution from the 1 GHz input source internal impedance are shown separately; an ideal input signal generator with zero phase and amplitude noise was assumed. The noise contribution at the higher harmonics is found to be suppressed by the idler resonators, while, at the second (output) harmonic, the device contribution is slightly

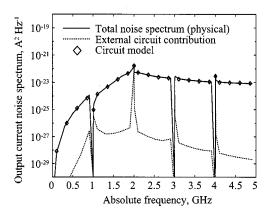


Fig. 11. Load current noise spectrum for the varactor frequency doubler.

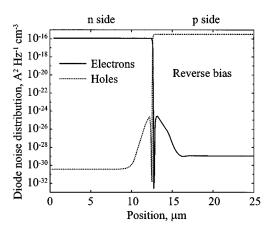


Fig. 12. Microscopic electron and hole noise distribution for the power spectrum of sideband 2 in the varactor frequency doubler.

smaller than the generator resistance contribution, thus yielding an operating noise figure around 1.5. Good agreement is again obtained with the circuit-oriented noise model.

In order to achieve a better understanding of the diode noise and noise conversion behavior in different operating conditions, a second, resistive, frequency multiplier operating with a zero-bias diode was also analyzed. The input frequency is again 1 GHz and the device and circuit were optimized so as to provide optimum frequency doubling (3.3 dBm output with 10 dBm input power); the circuit topology and element values are not reported for the sake of brevity. The diode chosen is symmetrical, with doping level 10^{17} cm⁻³, length 1 μ m and area 200 μ m². The physics-based simulation was carried out with $N_L = 10$; a higher number of harmonics was required due to the larger degree of resistive nonlinearity of the diode operating at zero bias.

With respect to the circuit model, the physics-based noise simulation yields a far deeper insight into the physical origin of noise. In fact, the noise sideband correlation matrix is obtained, through the generalized CGF formulation, as the spatial integral of a distributed, space dependent noise density, i.e., the integrand functions in (26). Inspection of this distributed noise density yields the position of the regions where noise (diagonal elements of the noise SCM) and noise frequency conversion (off-diagonal elements of the noise SCM) take place.

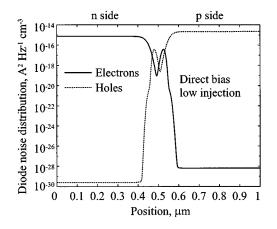


Fig. 13. Microscopic electron and hole noise distribution for the power spectrum of sideband 2 in the resistive frequency doubler; low input power case.

The spatial noise distribution of electron and hole diffusion noise were evaluated in three cases: the reverse-biased (varactor) diode, see Fig. 12, and the forward-bias (resistive) diode, for two operating conditions, corresponding to low (-3 dBm) or high (4 dBm) input power, respectively, see Figs. 13 and 14. In the low power case the instantaneous diode working point goes from -0.24 to 0.24 V, while in the high-power condition it goes from -1.5 V to 0.7 V. Only the electron and hole contributions to the diagonal element (2,2) of the noise SCM are considered; the other diagonal elements have a similar behavior. The results presented suggest the following discussion.

From the physical standpoint, high-frequency diode noise originates either as thermal noise in the resistive parasitics, or as diffusion noise in the injection regions; the latter causes the well-known shot-like behavior of diode noise [12] (GR noise, which mainly occurs in the depletion regions, was negligible in the structures considered and was not introduced in the simulation shown). This conventional picture of diode noise, although strictly valid in small-signal operation, can help in understanding LS noise as well.

First, in a reverse-bias diode the dominating contribution is due to thermal noise originating either in the p or n sides; this can be clearly seen in Fig. 12 as a constant plateau, while the injection contribution is much lower. Notice that, in nonlinear operation, the diode instantaneous operating point goes from -9.4 V to -1.2 V; thus, the overall result can be seen (at least in a quasistatic interpretation) as the average between a set of reverse-biased operating points.

In the forward biased structure, see Fig. 13, the importance of the injection contribution is clearly visible for both holes and electrons also in the low power, low-injection case. In high power, high-injection conditions something new occurs, since injected minority carriers induce, in the quasineutral regions near the depletion region, a large majority carrier population. The noise peak due to high injection is thus displaced from the minority to the majority side; the overall behavior is found to be somewhat similar to the small-signal one in high injection, but the relative amplitude of peaks and detailed behavior is affected by the instantaneous working point ranging from reverse to forward bias, rather than being confined to direct bias only.

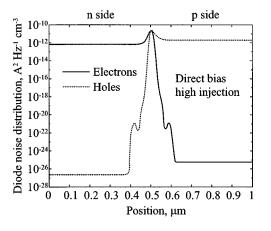


Fig. 14. Microscopic electron and hole noise distribution for the power spectrum of sideband 2 in the resistive frequency doubler; high input power case.

Finally, the distributed source related to the off-diagonal SCM elements (implying noise frequency conversion between sidebands) is uniformly negligible in the resistive regions, whereas it is large in the depletion region (reverse bias) or in the injection region (forward bias), thus supporting the interpretation that noise conversion, being a nonlinear effect, only takes place in the regions of the devices hosting reactive or resistive nonlinearities.

VI. CONCLUSION

A unified approach has been presented for the physics-based frequency-conversion and noise analysis of semiconductor devices operating in LS nonautonomous regime. The technique proposed applies to physics-based device numerical simulation the SS–LS analysis method and extends to LS regime the Green's function approach to noise analysis in dc and small-signal conditions. A detailed formulation of the theory has been provided, together with some implementation details within the framework of a two-carrier drift-diffusion model. Examples of application show that, in the test cases considered, the physics-based approach provides results consistent with circuit-oriented models.

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