

Polarization compensation of Fresnel aberrations in telescopes

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ABSTRACT

Large aperture space telescopes are built with low F#’s to accommodate the mechanical constraints of launch vehicles and to reduce resonance frequencies of the on-orbit system. Inherent with these low F#’s is Fresnel polarization which affects image quality. We present the design and modeling of a nano-structure consisting of birefringent layers to control polarization and increase contrast. Analysis shows a device that functions across a 400nm bandwidth tunable from 300nm to 1200nm. This Fresnel compensator device has a cross leakage of less than 0.001 retardance.

Keywords: Polarization, exoplanet, telescope, birefringence, polyimide, wavefront, adaptive optics, and phase.

1. INTRODUCTION

Direct imaging of terrestrial exoplanets requires a telescope/instrument system capable of controlling and suppressing unwanted star light to approximately one part in 10^{12} over a wide wavelength bandpass spanning the UV to near IR spectrum¹⁻⁴. Terrestrial exoplanets are faint, requiring large aperture telescopes to record their image. Because of the required size of the aperture (3 to 8 meters), coronagraph designs that fit into launch vehicles employ low F#’s (typically 1 to 1.5) to collect and focus the radiation. These low F# systems require a highly reflective coated steeply curved mirror that introduces spatially varying polarization effects across the mirror surface. This polarization effect reduces system transmittance and increases scattered light. The properties of metal and coating anisotropic have been largely overlooked in the analysis and performance characterization of low F# telescopes for exoplanet missions⁵. Several coronagraph architectures have been proposed,¹⁻⁴ but each one of these have degraded performance because of Fresnel polarization apodization. This paper addresses the modeling and mitigation of Fresnel polarization effects in space-based coronagraphic telescopes using an innovative device (a Spatially Variable Retardance Plate or SVRP) that incorporates birefringent nanolayers⁶ to control the amplitude and phase of polychromatic white light wavefronts. The SVRP device provides control of the broadband white-light optical polarization and retardation to maximize coronagraph system transmittance, contrast, and to minimize losses to scattered light. As will be shown in Section 2, this device can be located at a much smaller pupil plane (~10-cm diameter) and will be much smaller, lighter, and easier to fabricate than an optical element located on or next to the primary mirror.

An understanding of the sources of partial polarization in full-scale coronagraphs is necessary for accurate performance modeling, specification of mirrors and coatings, and to design necessary alternatives to mitigate the effects of the internal polarization produced by Fresnel effects. Scattered light control to better than one part in 10^9 has been demonstrated¹⁻⁴ over a 10% optical bandwidth using wavefront sensing and control with an adaptive optics device in the High Contrast Imaging Testbed (HCIT) located in a vacuum system at JPL. However, this system functions at an F-number of 28.5 and does not include an optic representative of a large (2-8 m), low F#, primary mirror characteristic of modern space coronagraph designs (e.g., ATLAST, PECO, EPIC, ACCESS, and TPF-C).

2. CORONAGRAPH SYSTEM CONSIDERATIONS

Direct imaging of terrestrial exo-planets requires a coronagraph. Several coronagraph architectures have been proposed¹⁻⁴. Typical designs employ low F# large aperture telescopes necessary to collect and focus radiation. A schematic of an imaging coronagraph telescope system is shown in Figure 1. Referring to the figure, the chief ray is

dotted and the marginal ray is dashed. The location where the marginal ray crosses the optic axis is the image plane. The location where the chief ray crosses the optic axis is the pupil plane (an image of the pupil). As with most astronomical telescopes, the entrance pupil is co-located with the telescope aperture. Powered optical elements are shown at planes 1, 3 and 5. The ring mask, shown at plane 4 is not a powered element. Although the telescope primary optic may be quite large (8 meters as planned in NASA exoplanet missions)^{2,8}, the mitigation of Fresnel Polarization can be done at a much smaller and convenient pupil plane such as at plane 4 where the ring mask is located. The functions of the polarization compensator and ring mask can be combined. The diameter of the pupil in the NASA testbed system is on the order of 3 cm. For future exoplanet missions using an 8-m telescope, the ring mask would be much larger than 3 cm.

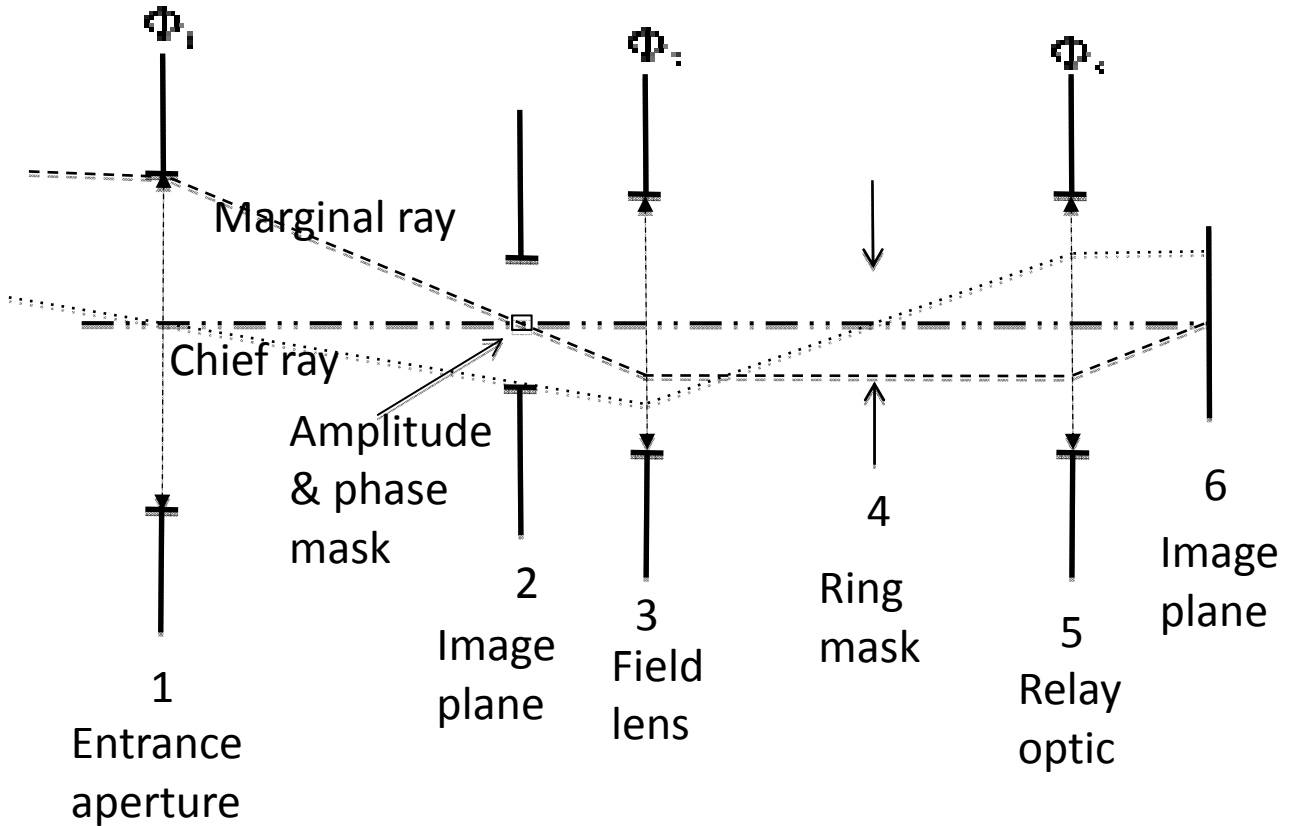


Figure 1. Schematic view of an imaging coronagraph-telescope. The coronagraph is used to control scattered light in optical systems built for high contrast stellar astronomy applications such as exoplanet and binary star atmospheric interaction research.

Breckinridge and Oppenheimer⁵ showed that polarization introduced in the telescope-coronagraph system increases scattered light to limit system performance. There are two sources of polarization. One is a characteristic of the natural curved shape of the primary mirror, called Fresnel polarization⁷. The other is a characteristic of the microstructure of high reflectivity coatings required for high efficiency, called anisotropy polarization. The curvature of the mirror introduces a polarization apodization across the pupil^{5,7} to produce aberrations which in turn affects the system image quality and lowers contrast. Spatially non-uniform anisotropies in the deposited thin film structure introduce unwanted phase and amplitude errors on the wavefront to increase scattered light, degrade image quality and lower contrast.

Fresnel polarization is introduced when a ray reflects from a tilted surface⁷. The reflectivity R_p for that portion of the incident ray whose electric vector is parallel to the plane of incidence is less than that (R_s) for the ray whose vector is

perpendicular to the plane of incidence. For a concave telescope mirror, the marginal ray angle deviation θ is given by

$$\theta = \arctan \left\{ \frac{1}{2F\#} \right\} \quad (1)$$

For a typical space telescope with $F\# = 1.3$, the angle is approximately 20 degrees. At this angle, for the case of the ray reflecting from a silver substrate, ~2% of the light is polarized. This means that at the highest angular resolution of the system ~2% of the light at the edge of the pupil is not contributing to an image, but rather to the background.

2.1 Polarization Analysis

There are several methods used to characterize the polarization in an optical system and optical devices. All of these methods are useful (or not so useful) depending on specific quantitative applications. Jones calculus⁸⁻⁹, which characterizes a birefringent network, is a powerful technique in which the state of polarization is represented by a two-component column vector, and each optical element (or layer) is represented by a 2x2 matrix. The Stokes vector and Muller matrix are based on the same physical approximations as the Jones vector⁸⁻⁹, but relate to the irradiance the detector sees and are often used in remote sensing applications. The Stokes vector and Muller matrix also include depolarization explicitly in the matrix. Since both Jones and Muller calculus are based on the same physics models, both methods are limited to normally incident and paraxial rays only. For example, the two polarization states of light incident on an anisotropic material (mirror, coating, and SVRP layer) are in general not mutually orthogonal for off-axis light. Both the Jones and Muller calculus methods neglect the Fresnel refraction and reflection at the surfaces¹¹⁻¹². These methods do not offer an explanation of the light leakage for off axis light. Hence other polarization techniques such as the extended Jones vector, Berreman's 4x4 matrices, or Finite Difference Time Domain (FDTD) are used instead¹⁰.

2.1.1 Extended Jones and Berreman's 4x4 Method

The telescope primary mirror in a coronagraph system for space flight is typically a low $F\#$. These low $F\#$ systems require a steeply curved highly reflecting mirror which introduces a spatially varying polarization effect across the aperture (or exit pupil). To accurately calculate the polarization effect, reflection at the highly reflecting metal coating interfaces cannot be ignored. The Berreman 4x4 method¹⁰⁻¹² is a powerful technique for treating the transmission of light in a complex system by treating the polarization as a general birefringent network. Exact solution can be obtained by the 4x4 matrix method as discussed in the literature¹⁰⁻¹². The 4x4 matrix method takes into account the effect of refraction and multiple reflections between interfaces. If the effect of multiple reflections can be neglected, the Berreman's method reduces to the extended Jones matrix methods¹¹. The extended Jones matrix is easier to manipulate mathematically and yet accounts for the Fresnel refraction and single reflection at the interfaces. For this paper the extended Jones method has been used for the telescope mirror and the Berreman's method for the SVRP device.

The Berreman 4x4 matrix method relates the propagation of polarized light to stratified media that are uniform in their dielectric properties in one plane, which is taken to be the xy plane. The method is discussed in this section and in more detail in the literature⁸⁻¹². The components of the electric field E and the magnetic field H in the plane of the layer can be solved from Maxwell's equations as:

$$\begin{bmatrix} E_x(x, y, z, t) \\ \mu_0 c H_y(x, y, z, t) \\ E_y(x, y, z, t) \\ -\mu_0 c H_x(x, y, z, t) \end{bmatrix} = \boldsymbol{\psi}(z) e^{-i\omega(t - \frac{nx}{c})} \quad (2)$$

Where $\boldsymbol{\psi}(z)$ is a column vector and the angular frequency ω is related to the wavelength in vacuum λ and the speed of light c by:

$$\omega = ck = \frac{2\pi c}{\lambda} \quad (3)$$

Here, $k = \frac{2\pi}{\lambda}$ is the magnitude of the wave vector in a vacuum. For the sake of convenience, the x axis is chosen such that the light wave propagates in the xz plane which the plane of incidence. The x component of the wave vector is equal to $\frac{\eta\omega}{c} = \eta k$, meaning that η is proportional to the in-plane wave vector component. The column vector Ψ satisfies the Berreman equation:

$$\frac{d\Psi}{dz} = ikD \cdot \Psi \quad (4)$$

where D is a 4x4 matrix generally referred to as the Berreman matrix (or simply the 4x4 matrix). Assuming that the magnetic susceptibility can be neglected, the optical properties of the dielectric can be described by the dielectric tensor with components $\epsilon_{\alpha\beta}$ ($\alpha, \beta = x, y, z$). The expression for the Berreman's matrix D is

$$D = \begin{bmatrix} -\eta \frac{\epsilon_{zx}}{\epsilon_{zz}} & 1 - \frac{\eta^2}{\epsilon_{zz}} & -\eta \frac{\epsilon_{zy}}{\epsilon_{zz}} & 0 \\ \epsilon_{xx} - \frac{\epsilon_{xz}\epsilon_{zx}}{\epsilon_{zz}} & -\eta \frac{\epsilon_{xz}}{\epsilon_{zz}} & \epsilon_{xx} - \frac{\epsilon_{xz}\epsilon_{zx}}{\epsilon_{zz}} & 0 \\ 0 & 0 & 0 & 1 \\ \epsilon_{xx} - \frac{\epsilon_{xz}\epsilon_{zx}}{\epsilon_{zz}} & -\eta \frac{\epsilon_{zx}}{\epsilon_{zz}} \epsilon_{xx} & -\frac{\epsilon_{xz}\epsilon_{zx}}{\epsilon_{zz}} & 0 \end{bmatrix} \quad (5)$$

Equation 4 and 5 are the central ones of the Berreman's 4x4 matrix method. There are several ways to solve these numerically as well as analytically¹¹⁻¹². For the current work, the Eidner-Olano¹³⁻¹⁵ method is used.

Berreman's method can be extended to compute the polarization apodization in terms of contrast and retardance as a function of angle of incidence θ and wavelength λ across the aperture (or corresponding pupil). The metallic mirror is approximated as a perfect conductor. In such a perfect conductor any electric field coming from external sources will be cancelled by the rearrangement of the freely moving charges. As a consequence the net electric field in the mirror must be zero, and at the interface $E_x = E_y = 0$.

For real metals the finite conductivity σ must be taken into account. As a consequence, the dielectric constant ϵ must be replaced by $\epsilon + \frac{i\sigma}{\epsilon_0\omega}$, thus, the refractive index $n = \sqrt{\epsilon + \frac{i\sigma}{\epsilon_0\omega}}$ is complex¹¹. For sufficiently large σ the electric field is inversely proportional to the square root of σ which implies that in the limit of a perfectly conducting metal ($\sigma \rightarrow \infty$) the electric field at the interface is restricted to the case of an ideal metallic mirror. Using this Berreman's extension, S_1 is defined as

$$S_1 = \frac{H}{V} \quad (6)$$

where H and V are the intensities measured for the light polarized horizontally and vertically, respectively. Figure 2(a) shows a three dimensional view of a plot of Log to the base 10 of S_1 as a function of the light beam incidence angle, from zero to thirty degrees onto a tilted thin film aluminum coated mirror and as a function of wavelength. The extended Berreman's 4x4 matrix approach can be used to calculate the retardance as a function of angle of incidence θ and wavelength λ as shown in Figure 2(b). Referring to Figure 2(b), the phase angle in degrees on the vertical axis between the H and the V components is a function of the incidence angle, from zero to thirty degrees on a tilted thin film aluminum coated mirror and is a function of wavelength. These figures show the significance of the birefringence and phase on reflection from a highly reflecting metal film. The model agrees very favorably with Breckinridge and Oppenheimer's results⁵ as shown in Figure 2(a). Moreover, the model provides the retardance induced by the mirror as shown in Figure 2(b). Figure 4 and 5 shows the significance of the birefringence and phase on reflection from a highly

reflecting metal film. Although these graphs are for an ideal mirror, a compensator can be designed and fabricated for any polarization state.

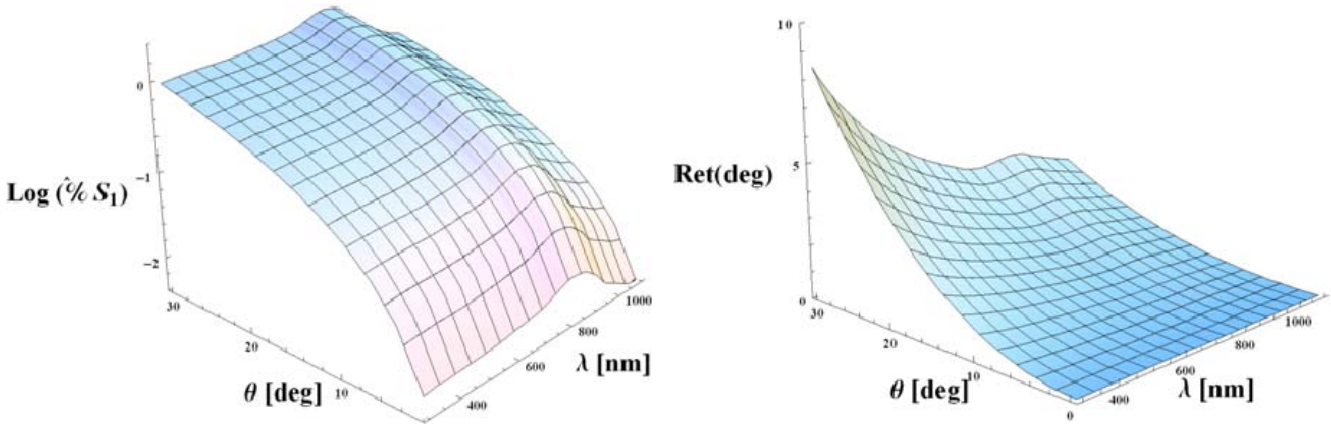


Figure 2. Polarization contrast (left) and retardance (right) as a function of angle of incidence θ and wavelength λ . The plots represent a horizontal “slice” through half of the mirror.

3. MITIGATING POLARIZATION USING A COMPENSATOR PLATE

A spatially varying retarder plate (SVRP) can be placed at a convenient pupil plane, such as the ring mask plane 4 shown in Figure 1. The SVRP device consists of a stack of nanolayers of anisotropic and/or isotropic materials $P_1, P_2, P_3 \dots P_n$ as illustrated in Figure 3. Each layer has its slow axis oriented at an azimuth angle $\gamma_1, \gamma_2, \gamma_3, \dots \gamma_n$. Optical birefringence describes the difference of a material’s refractive index with direction. When the birefringence is on the order of the change of the in-plane refractive index between adjacent materials, surprising and useful optical effects occur.

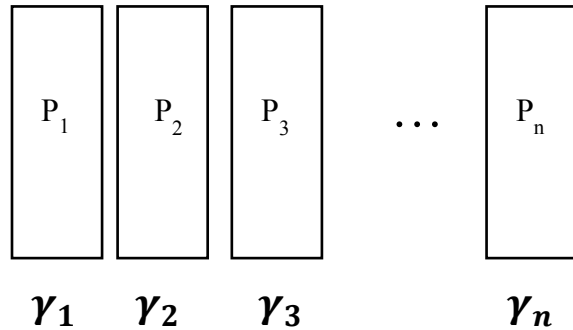


Figure 3. Synthesized Optical material A stack of anisotropic and isotropic material $P_1, P_2, P_3 \dots P_n$ can be stacked. Each layer thickness, birefringence, and orientation is layered to produce a custom polarization compensator. The SVRP consists of a pixelated array of these stacks. The resolution of each stack can be as small as 0.6 micron and with the appropriate boundary conditions the SVRP can act as a continuous spatially varying sheet or a discrete pixelated device.

An investigation has been conducted across a wide variety of birefringent materials and fabrication methods for developing an SVRP device most suitable at enabling $>10^{12}$ contrast. One such material is single layer MgF_2 . For multi layers, a device fabricated from quartz is useful. Quartz has a transparency range extending from $0.25 \mu\text{m}$ to $2.5 \mu\text{m}$ ($>99\%$) which is a suitable bandwidth of interest in coronagraphs. MgF_2 is transparent over an even broader spectral range. Both quartz and MgF_2 are birefringent, but quartz has a much smaller birefringence than MgF_2 . Hence these two materials are often used in tandem, for example in the design of achromat waveplates. Quartz and MgF_2 both are commonly used in high performance optical systems and are known to have high transmittances $>90\%$ over 300nm to 1200 nm . In addition the very low scattering making them a suitable candidate for the SVRP. Other potential materials include liquid crystals, polyimide, and photo polymers.

3.1 Optical Nanomaterial Synthesis Design Methodology

To design an SVRP, we first must consider the stack of dielectric (birefringent or isotropic layers) as shown in Figure 3. The Berreman's method is used to compute a propagator matrix P_j for each layer in the stack. The propagator matrix can be expressed in terms of D as

$$P = \exp(ikD) = \sum_{l=0}^{\infty} \frac{(ikd)^l}{l!} D^l \quad (7)$$

where the Taylor series of the exponential function is used to define that function for the matrices. The matrix D can be written in the diagonal form as

$$D = T\bar{D}T^{-1} \quad (8a)$$

$$T_{kl} = \psi_k^{(l)} \quad (8b)$$

$$\bar{D}_{lm} = \begin{cases} \mu_l & \text{if } l = m \\ 0 & \text{if } l \neq m \end{cases} \quad (8c)$$

Clearly D can be expressed in terms of the eigenvalues of D , whereas T can be expressed in terms of the eigenvectors of D . Substitution to equation (7) gives:

$$P = T\bar{P}T^{-1} \quad (9a)$$

$$\bar{P}_{lm} = \begin{cases} \exp(ik\mu_l d) & \text{if } l = m \\ 0 & \text{if } l \neq m \end{cases} \quad (9b)$$

Another relatively recent 4×4 matrix method for general biaxial media, differing from Berreman's method, has been proposed by Yuan and co-workers¹³. As noted in the literature, the two methods are equivalent as both are based on the exact solutions to Maxwell's equations. In particular, the quartic equation for the z component of the wave vector k_z given by Yuan corresponds to the quartic equation of the eigenvalues of the Berreman matrix μ , because these eigenvalues are equal to k_z/k .

For the stack of dielectric (birefringent or isotropic) layers shown in Figure 3, each layer is labeled $1,2,3,\dots,N$. The 4×4 propagation matrix P_j of each individual layer can be calculated using Equation 7. In order to find the overall propagation matrix P of the stack of dielectric layers, boundary conditions at the interface between two dielectric layers m and n are needed. According to Maxwell theory the components of the electric and magnetic fields E and H parallel to the interface between two dielectric media m and n must be continuous, provided that no charge or currents are present

at the interface. Consequently E_x , E_y , H_x , H_y are continuous at the interface; i.e., the column vector ψ satisfies the boundary condition

$$\psi_+ = P \cdot \psi_- \tag{10a}$$

$$P = P_n \dots P_3 P_2 P_1 \tag{10b}$$

Here ψ_+ and ψ_- are the Berreman column vectors at the two sides of the stack of dielectric layers.

3.2 Design Example of a SVRP

The design of an SVRP requires careful consideration of the material properties and fabrication techniques. Not only does the birefringence vary spatially across the mirror, but the orientation of the polarization state varies spatially as well, as depicted in Figure 4(a). The orientation of the polarization as a function of position is shown in Figure 4(a). Referring to the figure, two arbitrary small regions P1 and P2 have different birefringence and different polarization orientations. For example, the alignment layer can be in correspondence with the polarization orientation of the reflected light off the mirror at a pupil plane as depicted in Figure 4(b). The birefringent stack consisting of layer B_1 , $B_2 \dots B_n$, is shown in Figure 4(c). The nanolayers are stacked and the stacking arrangement varies spatially (to a resolution of 0.6 microns for the fabrication process discussed in Section 4) to yield the desired polarization compensation to mitigate the Fresnel effects. The final isotropic and amplitude layers compensate for the wavefront variation and amplitude variation respectively to yield a uniform, optically flat wavefront in a uniform polarization state. Although the design depicted in Figure 4 illustrates the case where the alignment layer is in the direction of the polarization state of the aperture (or pupil), in general the orientation of the alignment layer corresponds to the design of the birefringent stack used to compensate for the Fresnel polarization.

Consider the marginal ray of an F# 1 telescope that has a 30-degree angle of incidence. This represents the worst case scenario of a telescope system. The 2D plot of the retardance versus wavelength from Figure 2(b) is shown in Figure 5(a). Referring to the figure, the telescope has approximately 9 degrees of maximum retardance (around 300 nm in the figure) for a 30-degree angle of incidence. The retardance versus wavelength for a 15 degree angle of incidence is shown in Figure 5(b), which has 2 degrees of retardance.

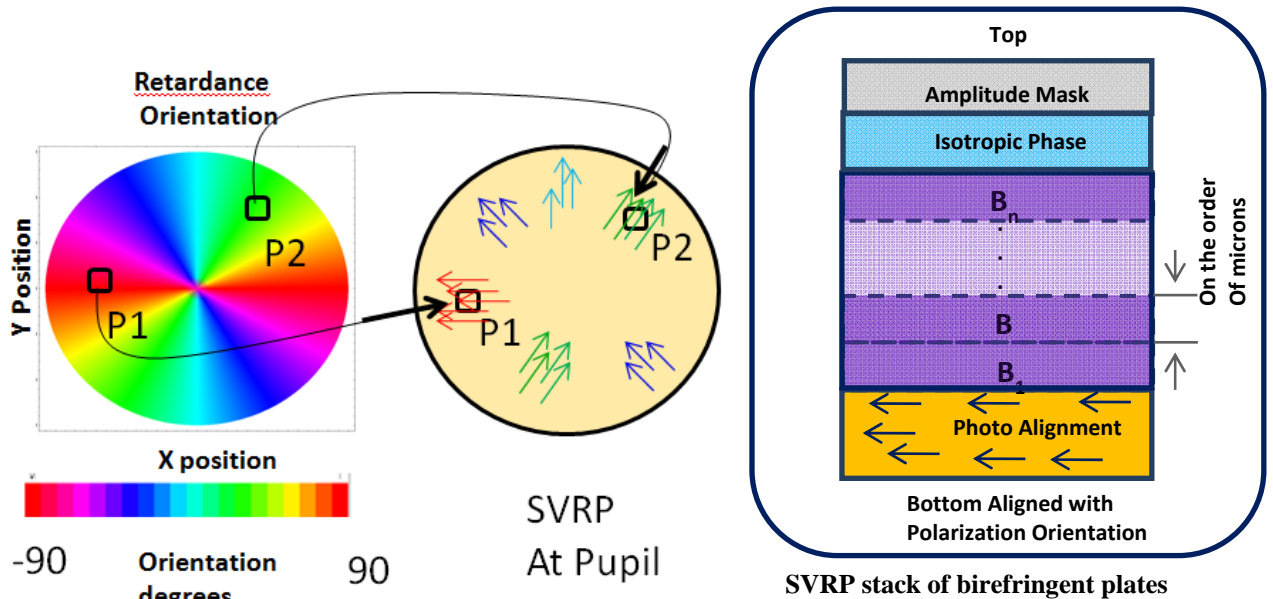


Figure 4. Photo alignment layer of a SVRP plate. (a) shows a spatially variable retarder plate (SVRP) face on (x,y) with retardance direction indicated by the colors shown in the stripe below which maps color into orientation in degrees as shown. (b) shows two particular regions, P1 and P2 which have two different polarization states and orientation are shown. (c) shows a diagram of the typical stack or sandwich. The bottom layer is a layer of homogeneous dielectric oriented to the polarization direction. Birefringent layers of B_1, B_2, \dots, B_n will be deposited with thickness layers and specific process recipe calculated and optimized to compensate for the Fresnel polarization of light reflected from the telescope.

The contrast $(I_{\max} - I_{\min}) / (I_{\max} + I_{\min})$ of a coronagraph system is related to the attenuation and retardance by

$$\text{contrast} = K(1 - \cos(\Gamma)) \tag{11}$$

For a simple 1 layer SVRP plate the polarization compensation for the 30 degree and 15 degree angle of incidence is shown in Figure 6. Since the dispersion of a nano layer is very small, the polarization compensation is not that dependent on the material selection. Hence, other materials will result in comparable polarization compensation to that shown in Figure 6. The material selection is however very important for consideration of clarity, transmission, alignment, fabrication, thermal and space-radiation effects.

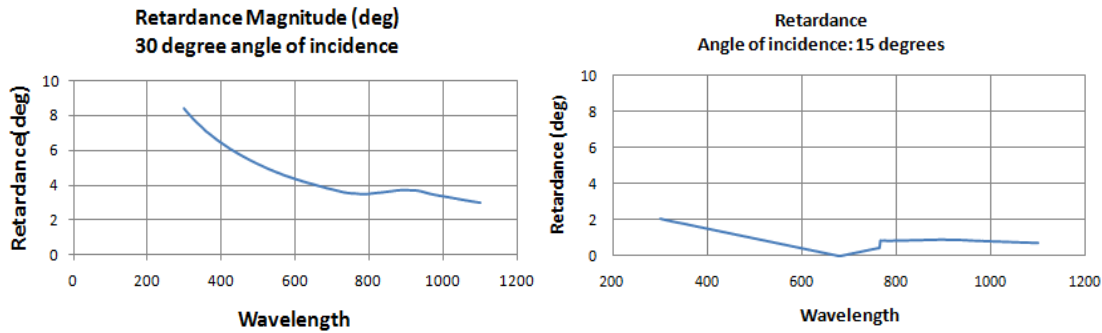


Figure 5. Retardance as a function of wavelength (a) at an angle of incidence 30 degrees (b) at an angle of incidence of 15 degree

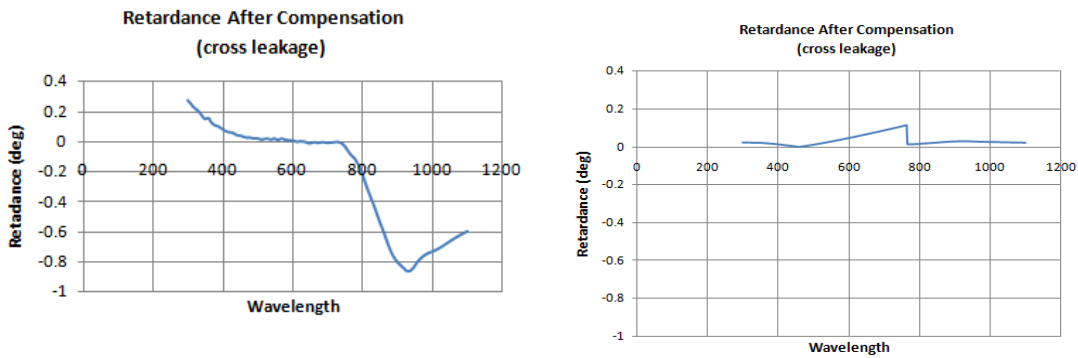


Figure 6. Single cell design of MgF_2 . (a) For an angle of incidence of 30 degrees retardance as a function of wavelength and after compensation by a single layered device reduces the retardance to better than 0.01 degree over 500-700nm. Note the scale is 1/10 that of Figure 5.

4. FABRICATION AND EXPERIMENTAL RESULTS

The Langley Optical Nanomaterials Synthesis and Fabrication Laboratory (ONSL) supports fabrication of devices with 50-nm position resolution and 0.6-micron feature sizes for advanced optical devices up to meters in diameter. Because the key fabrication equipment is digitally controlled, devices can be fabricated inexpensively and rapidly, facilitating design refinements and modifications. Hence, the facility can support fabrication of polarization compensation devices throughout the lifecycle of an exoplanet mission from demonstration in a prototype NASA coronagraph system to fabrication of a final flight device.

The ability of the birefringent layers to orient in a particular direction when in contact with a specially prepared surface is a phenomenon of major importance other SVRP plate fabrication. There are several methods used in the OSNL. The lab has made significant progress in the development of photo aligned materials. Manufacturers require alignment layers with a wide range of optimized properties. Thin films must easily be formed with high photosensitivity in order to facilitate rapid processing and also to avoid unwanted degradation. The resultant photo-aligned film must be insoluble and thermally, electrochemically and photo-chemically stable.

4.1 Photo-alignment using photo degradation

The successful photo-alignment of a polyimide is considered to be an important technological goal because of the high thermal stability of polyimides and their acceptance as the alignment layer of choice by the LC display industry. Hasegawa and Taira¹⁷ first reported photo-alignment of polyimide by polarized light exposure at 257 nm. Homogeneous LC alignment was obtained in a direction perpendicular to the polarization of the incident UV beam. This is the direction of the maximum density of unbroken polyimide chains on exposure. Therefore, alignment was attributed to the anisotropic depolymerization of the polyimide. Further studies confirmed this and the alignment direction was shown to switch by varying the polarization direction of the aligning beam¹⁸.

Figure 7 shows the birefringence for polyimide that was aligned by photo-degradation. Nissan SE-7492 in the form of polyamic acid was used as the alignment layer. The polyimide film was spin-coated onto a quartz substrate. It was cured at 250 degrees C for one hour or 200 degrees C for 1 1/2 hours. A 200-watt Hg (Xe) lamp equipped with a dichroic mirror reflecting from 230 to 430 nm was used as the light source. A dichroic UV linear polarizer was used to obtain the linearly polarized UV light. The average power density for the unpolarized and polarized light was approximately 40 and 10 mW/cm², respectively, measured using a radiant energy meter.

The transmittance curve from this rudimentary spectroscopic ellipsometer was processed along with a simple model to determine the dispersion of the birefringence. The standard expression for an *a*-plate with positive birefringence between crossed polarizers applies⁸⁻⁹:

$$T = \frac{1}{2} T_0 \sin^2(2\theta) \sin^2\left(\frac{\pi \Delta n d}{\lambda}\right) \quad (12)$$

where T_0 is the unpolarized irradiance incident on the first polarizer, λ is the wavelength, d is the film thickness, Δn is the birefringence, and θ is the angle between the effective optical axis of the birefringent film and the transmission axis of either polarizer (~always set to 45° in our geometry). Since T is a periodic function involving a square root, the value of Δn cannot be unambiguously determined without some additional steps. Two methods are used to find the dispersion of the birefringence from the transmittance. The first method involves a direct computation from the data. From Equation (12), the birefringence can be expressed as:

$$\Delta n = \frac{\lambda}{\pi d} [m\pi \pm \sin^{-1}(\sqrt{2T/T_0})] \quad (13)$$

where m is a non-negative integer that describes the order of the solution. From basic principles of these optically transparent materials, it is known that Δn is continuous across the visible spectrum. Hence, the sign of the \sin^{-1} function and the order m are constant between each maximum and minimum in T . Thus, one can simply manually or

computationally choose both parameters for each data point such that the ambiguity is resolved and a continuous solution $\Delta n(\lambda)$ is found.

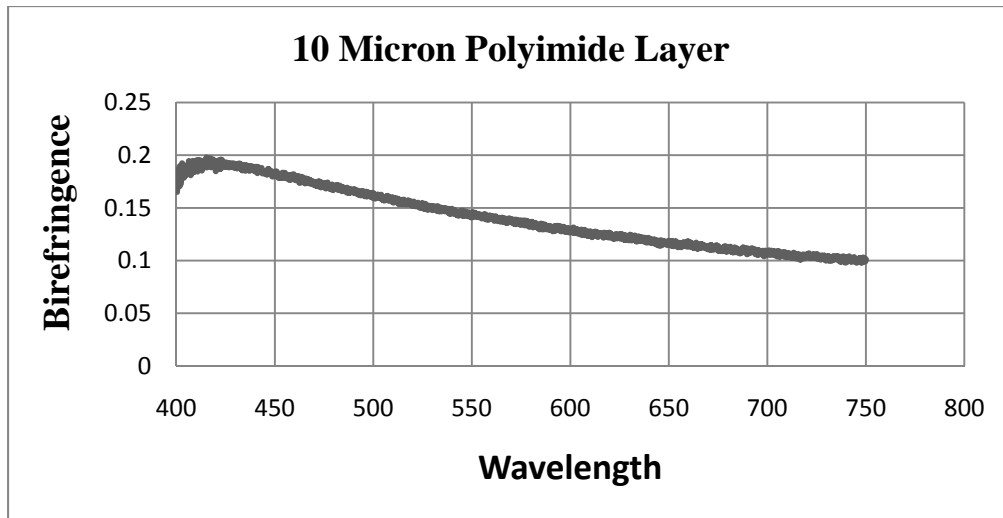
A second method that is often used and useful in optical system design⁸⁻⁹ involves an indirect solution that requires the least-squares fit of a dispersion model to the transmittance. Since polymer films are optically transparent throughout the visible region, the refractive index can be modeled by the first-order Sellmeier dispersion¹⁷ relation:

$$n(\lambda)^2 - 1 = a + b\lambda^2 / (\lambda^2 - \lambda_0^2) \tag{14}$$

where a , b , and λ_0 are constants. Granting the standard assumptions, this can be reduced to the slightly simpler Cauchy formula: $n(\lambda) = A + B/\lambda^2$, where A and B are constants for a given material. The dispersion of the birefringent film is therefore modeled by the following equation:

$$\Delta n(\lambda) = n_e(\lambda) - n_o(\lambda) \approx \Delta n_\infty + \frac{c}{\lambda^2} \tag{15}$$

where Δn_∞ is the birefringence at long wavelengths and c is a constant. Note that the absolute values of the ordinary (n_o) and extraordinary (n_e) indices are not required to determine $\Delta n(\lambda)$. In order to calculate the dispersion of the birefringence, Equations (14) and (15) are combined and utilize least squares minimization to find the parameters Δn_∞ and c that give the closest fit to our transmittance data.



(a)

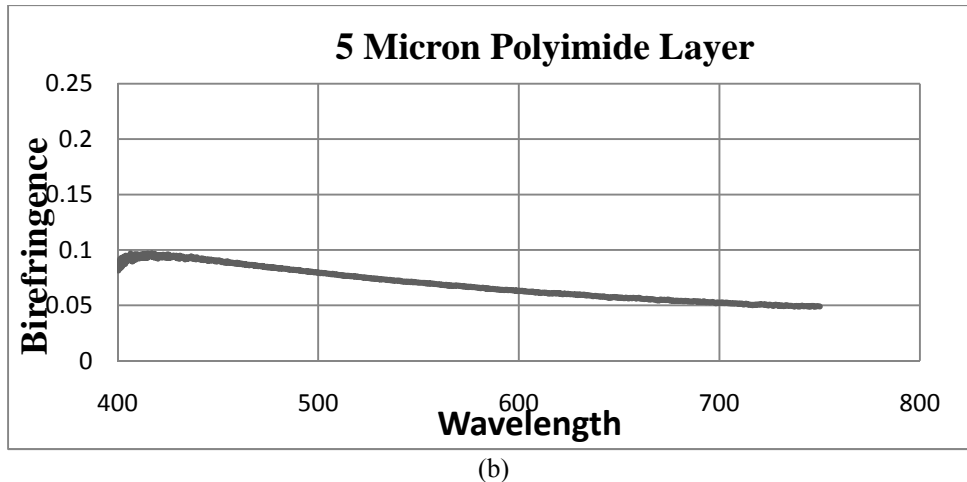


Figure 7. Representative data for uniaxial polyimide film: (a) transmittance between crossed polarizers and (b) birefringence calculated using equation (8).

4.2 PhotoAlignment using a Polymerized Photo Polymer

Another interesting method currently being investigated is an aligning method where photopolymers are polymerized with linearly polarized light¹⁹. The main advantage of this method is that it allows different orientations on the same glass or silicon substrate. Several polymers have been tried, in particular poly(vinyl 4-methoxy cinnamate)¹⁸ and poly(vinyl cinnamate)¹⁹ both of which exhibited some birefringence. Both polymers exhibit a depletion cinnamic acid side chain molecule along the direction of polarization, increasing in the mean time the number of photoinduced cyclo additions along a direction perpendicular to the polarization direction. Therefore, pre-irradiated isotropically oriented molecules change into an anisotropic distribution of photopolymerized side chains, which can induce a definite orientation of liquid crystal molecules by means of their in-line aromatic rings. These methods are at a very low technical readiness level and hence require more research and development. Such work will be performed at NASA Langley for use in exoplanet missions and will be reported in future publications.

5. SUMMARY

Large aperture space telescopes are built with low F#’s to accommodate the mechanical constraints of launch vehicles and to reduce resonance frequencies of the on-orbit system. Inherent with these low F# is Fresnel polarization which effects image quality. We have presented an approach of compensating for the Fresnel polarization apodization by using a spatially varying retarder plate (SVRP) along with modeling and experimental results.

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