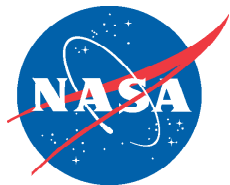


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# **Build-up Approach to Updating the Mock Quiet Spike<sup>TM</sup> Beam Model**

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**May 2007**

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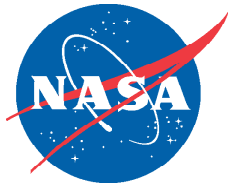
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## ABSTRACT

A crucial part of aircraft design is ensuring that the required margin for flutter is satisfied. A trustworthy flutter analysis, which begins by possessing an accurate dynamics model, is necessary for this task. Traditionally, a model was updated manually by fine tuning specific stiffness parameters until the analytical results matched test data. This is a time consuming iterative process. The NASA Dryden Flight Research Center has developed a mode matching code to execute this process in a more efficient manner. Recently, this code was implemented in the F-15B/Quiet Spike™ (Gulfstream Aerospace Corporation, Savannah, Georgia) model update. A build-up approach requiring several ground vibration test configurations and a series of model updates was implemented to determine the connection stiffness between aircraft and test article. The mode matching code successfully updated various models for the F-15B/Quiet Spike™ project to within 1 percent error in frequency and the modal assurance criteria values ranged from 88.51–99.42 percent.

## NOMENCLATURE

CAD	computer aided design
CG	center of gravity, in
CONM2	concentrated mass element
<b>F</b>	temporary variable
FE	Finite Element
G	target value for optimization
GAC	Gulfstream Aerospace Corporation
GVT	ground vibration test
<i>i</i>	index term
$I_{xx}$	moment of inertia about the x-axis with respect to the x-axis, lb-in <sup>2</sup>
$I_{xxG}$	moment of inertia about the x-axis with respect to the x-axis, lb-in <sup>2</sup> , target
$I_{yy}$	moment of inertia about the y-axis with respect to the y-axis, lb-in <sup>2</sup>
$I_{yyG}$	moment of inertia about the y-axis with respect to the y-axis, lb-in <sup>2</sup> , target
$I_{zz}$	moment of inertia about the z-axis with respect to the z-axis, lb-in <sup>2</sup>
$I_{zzG}$	moment of inertia about the z-axis with respect to the z-axis, lb-in <sup>2</sup> , target
$I_{xy}$	moment of inertia about the x-axis with respect to the y-axis, lb-in <sup>2</sup>
$I_{xyG}$	moment of inertia about the x-axis with respect to the y-axis, lb-in <sup>2</sup> , target
$I_{yz}$	moment of inertia about the y-axis with respect to the z-axis, lb-in <sup>2</sup>
$I_{yzG}$	moment of inertia about the y-axis with respect to the z-axis, lb-in <sup>2</sup> , target
$I_{zx}$	moment of inertia about the z-axis with respect to the x-axis, lb-in <sup>2</sup>
$I_{zxG}$	moment of inertia about the z-axis with respect to the x-axis, lb-in <sup>2</sup> , target
<i>j</i>	second index term

$J$	objective function
$\mathbf{K}$	stiffness matrix
$\mathbf{M}$	mass matrix
MAC	Modal Assurance Criteria
$m$	number of degrees of freedom
$n$	number of modes that will be correlated in eq. (2)
NaN	not a number
QS	Quiet Spike™
$\mathbf{R}$	temporary variable
$\mathbf{T}$	transformation matrix
x-CG	center of gravity, x-axis
y-CG	center of gravity, y-axis
$\beta$	scaling factor
$\Phi$	analytical Eigen matrix
$\omega_i$	test frequencies
$\Omega_i$	analytical frequencies
$\Psi$	temporary variable

## INTRODUCTION

When a new aircraft is designed or a modification is made to an existing aircraft, the aeroelastic properties of the aircraft need to be examined to ensure it is flightworthy. Evaluating the aeroelastic properties of a new or modified aircraft can include performing a variety of analyses, such as modal and flutter analyses. To produce accurate results from these analyses, it is imperative to work with finite element (FE) models that have been validated by or correlated to ground vibration test (GVT) data. Updating an analytical model using measured data is a challenge in the area of structural dynamics. The analytical model update process encompasses a series of optimizations that match analytical frequencies and mode shapes to the measured modal characteristics of a structure. In the past, the method used to update a model to match testing data has been ‘trial and error.’ This is an inefficient method; running a modal analysis, comparing the analytical results to the GVT data, manually modifying one or more structural parameters [mass, center of gravity (CG), inertia, area, etc.], rerunning the analysis, and comparing the new analytical modal characteristics to the GVT modal data make up a time-consuming process. If the match is close enough (close enough defined by the analyst’s updating requirements), then the updating process is finished. If the match does not meet updating requirements, then the parameters are changed again and the process is repeated. Clearly, this manual optimization process is highly inefficient for large FE models and/or a large number of structural parameters.

The NASA Dryden Flight Research Center (DFRC) has developed, in-house, a mode matching code that automates the above-mentioned optimization process. Moreover, it facilitates

the development of reduced-order models that simplify analyses and therefore, reduce computation time. The DFRC in-house mode matching code reads mode shapes and frequencies that were measured from a GVT to create the target model. It also reads the current analytical model as the ‘initial guess,’ as well as the variable parameters and their upper and lower limits as assigned by the analyst. It performs a modal analysis on this initial model and modifies its variable properties to create an updated model that has similar mode shapes and frequencies to those of the target model. The mode matching code outputs frequencies and modal assurance criteria (MAC) values that allow for the quantified comparison of the updated model versus the target model.

The mode matching code assists in determining the airworthiness of the aircraft flown at DFRC. Recently, this code was implemented on a project flown on the DFRC F-15B (The Boeing Company, Chicago, Illinois) supersonic flight-testing platform, the Gulfstream Aerospace Corporation (Savannah, Georgia) (GAC) Quiet Spike™ (QS). This code allowed for a build-up approach that was necessary because the flight test article itself was unavailable. Researchers were able to make progress in the analyses even without the flight hardware.

The objective of this work was to use the mode matching code to determine the connection stiffness on the airplane radar bulkhead where the QS and the F-15B airplane mate, such that when the FE model of the flight QS was validated, it could be readily mated to the airplane FE model. This approach was established to enable the project to progress the model development and flutter predictions without the actual QS flight test hardware.

## **MATHEMATICAL BACKGROUND**

Three optimization phases are used to refine a model with the DFRC mode matching code. The mass properties are modified to match measured mass properties, the mass matrix is orthogonalized, and then the natural frequencies and mode shapes are matched. Design variables for the optimization can include structural sizing information (thickness, cross-sectional area, area moment of inertia, torsional constant, etc.), point properties (lumped mass, spring constant, etc.), and material properties (Young’s modulus, etc.).

### **Phase 1: Mass properties**

Matching mass properties by using lumped masses (CONM2)(ref. 1) reduces the computational effort required to match stiffness properties and ensures that a physically meaningful and accurate solution is achieved. In this first optimization phase, 10 objective functions are minimized to match analytical to measured mass properties. The mass properties that are updated include total mass, center of gravity location, and mass moments of inertia. As an objective function is minimized, a constraint function is implemented to prevent the updated variable from changing in the minimization of the following objective function. The constraint functions limit the amount of change allowed in the previously optimized variables. The objective functions and constraints applied in this phase are listed in order in table 1. This optimization phase places the model within the vicinity of a physically viable solution (feasible region), facilitating the second and third optimization phases.

Table 1. Optimization problem statement for phase 1 of model update.

Statement	Objective Function	Constraint Function
1	$J_1 = (W-W_G)^2/W_G^2$	Unconstrained
2	$J_2 = (X-X_G)^2/X_G^2$	$ J_1  < \varepsilon$
3	$J_3 = (Y-Y_G)^2/Y_G^2$	$ J_i  < \varepsilon \quad i = 1, 2$
4	$J_4 = (Z-Z_G)^2/Z_G^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 3$
5	$J_5 = (I_{XX}-I_{XXG})^2/I_{XXG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 4$
6	$J_6 = (I_{YY}-I_{YYG})^2/I_{YYG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 5$
7	$J_7 = (I_{ZZ}-I_{ZZG})^2/I_{ZZG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 6$
8	$J_8 = (I_{XY}-I_{XYG})^2/I_{XYG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 7$
9	$J_9 = (I_{YZ}-I_{YZG})^2/I_{YZG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 8$
10	$J_{10} = (I_{ZX}-I_{ZXG})^2/I_{ZXG}^2$	$ J_i  < \varepsilon \quad i = 1, \dots, 9$

### Phase 2: Mass Matrix Orthogonalization

The orthonormalized mass matrix is shown in eq. (1).

$$\underline{\mathbf{M}} = \Phi_G^T \mathbf{T}^T \mathbf{M} \mathbf{T} \Phi_G \quad (1)$$

The off-diagonal terms of this orthonormalized matrix are reduced to improve mass orthogonality. In eq. (1), the mass matrix, denoted as  $\mathbf{M}$ , represents the analytical mass matrix, while  $\Phi_G$  represents the target Eigen matrix that is obtained from the GVT. The target Eigen matrix,  $\Phi_G$ , remains unchanged during the optimization. The transformation matrix,  $\mathbf{T}$ , is based on Guyan reduction (ref. 2) or improved reduced system (ref. 3). The optimization problem statement then becomes:

Minimize

$$J_{11} \equiv \sum_{i=1, j=1, i \neq j}^n (\underline{\mathbf{M}}_{ij})^2 \quad (\text{Off-diagonal terms of } \underline{\mathbf{M}}) \quad (2)$$

Such that  $|J_i| < \varepsilon$  where  $i = 1, 2, \dots, 10$  ( $J_i$  values are given in table 1), and  $n$  denotes the number of modes that will be correlated in eq. (2). The positive-definiteness characteristic of the lumped mass elements also acts as a constraint during this optimization procedure.

### Phase 3: Frequencies and Mode Shapes

In this phase, certain modes can be given a higher level of importance by applying a scaling factor,  $\beta$ , in eq. (3) and eq. (5). This scaling factor helps to more closely tune the frequencies



of these analytical modes of interest after the mode shape vectors have been matched to within required accuracy.

Two optimization methods are used in this phase. In the first method, the objective function considered combines an index which identifies normalized errors between test ( $\omega_i$ ) and analytical ( $\Omega_i$ ) frequencies with a second index that defines the total error associated with the off-diagonal terms of the orthonormalized stiffness matrix. The optimization problem statement then becomes:

Minimize

$$J_{12} \equiv \sum_{i=1}^n \left( \frac{\Omega_i - \omega_i}{\Omega_i} \right)^2 + \beta \sum_{i=1, j=1, i \neq j}^n (\underline{\mathbf{K}}_{ij})^2 \quad (3)$$

Such that  $|J_i| < \varepsilon$  for  $i = 1, 2, \dots, 11$ . The matrix  $\underline{\mathbf{K}}$  is a result of the matrix multiplication shown in eq. (4), where the stiffness matrix,  $\mathbf{K}$ , is the analytical stiffness matrix.

$$\underline{\mathbf{K}} = \Phi_G^T \mathbf{T}^T \mathbf{K} \mathbf{T} \Phi_G \quad (4)$$

In the second optimization method, the objective function combines the same frequency error index used above, with a second index that defines the total error between test and analytical mode shapes at specified sensor locations. The optimization problem statement then becomes:

Minimize

$$J_{12} \equiv \sum_{i=1}^n \left( \frac{\Omega_i - \omega_i}{\Omega_i} \right)^2 + \beta \sum_{i=1}^m (\Phi_i - \Phi_{iG})^2 \quad (5)$$

Such that  $|J_i| < \varepsilon$  for  $i = 1, 2, \dots, 11$ , and  $m$  denotes the number of degrees of freedom measured. The frequencies  $\omega_i$  and mode shapes  $\Phi_i$  are calculated based on the direct-iterative Eigen solution technique for large eigenvalue problems (ref. 4):

- |  |   |
|--|---|
| 1) Compute $\mathbf{K}_T$ and $\mathbf{M}_T$ : | $\mathbf{K}_T = \mathbf{T}^T \mathbf{K} \mathbf{T}$ and $\mathbf{M}_T = \mathbf{T}^T \mathbf{M} \mathbf{T}$     |
| 2) Compute $\mathbf{F}$ :                      | $\mathbf{F} = \mathbf{M}_T \Phi_G$  |
| 3) Compute $\mathbf{R}$ :                      | $\mathbf{K}_T \mathbf{R} = \mathbf{F}$  |
| 4) Compute $\mathbf{K}_R$ and $\mathbf{M}_R$ : | $\mathbf{K}_R = \mathbf{R}^T \mathbf{K}_T \mathbf{R}$ and $\mathbf{M}_R = \mathbf{R}^T \mathbf{M}_T \mathbf{R}$ |
| 5) Compute $\omega_i$ and $\Psi$ :             | $\mathbf{K}_R \Psi = \omega_i^2 \mathbf{M}_R \Psi$  |
| 6) Compute $\Phi$ :                            | $\Phi = \mathbf{R} \Psi$  |

For the direct-iterative Eigen-solution technique, the analytical stiffness and mass matrices,  $\mathbf{K}$  and  $\mathbf{M}$ , are correlated, while the measured mode shapes,  $\Phi_G$ , remain unchanged during the model updating process. Notice that the transformation matrix,  $\mathbf{T}$ , in eq. (1) and eq. (4) is calculated using the analytical mass and stiffness matrices  $\mathbf{M}$  and  $\mathbf{K}$ . Therefore, the constraint equation  $|J_{11}| < \epsilon$  is needed for the third optimization phase.

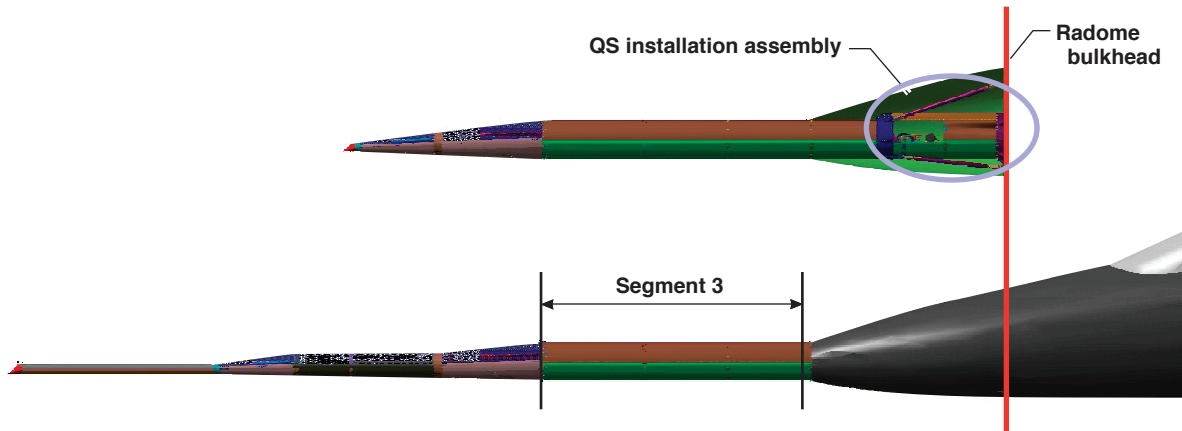
Current model updating approaches consist of updating only stiffness properties and assume that the modeled mass distribution is accurate. This can create erroneous stiffness properties in a model. The DFRC mode matching code is capable of updating both mass and stiffness in a model by updating mass properties such as total mass, CG, and mass moments of inertia, improving the orthogonalization of the mass matrix, and matching frequencies and mode shapes to test data. Updating both mass and stiffness properties of a model will provide a higher degree of confidence in a model's resemblance of the actual hardware.

## APPLICATION

An example of an application of the mode matching code is the F-15B research testbed. The DFRC possesses a modified F-15B airplane that is used as a testbed for supersonic flight experiments. Traditionally, the FE model of the flight test article is generated and updated by GVT data and then mated to the updated F-15B FE model. A GVT is then conducted with the test article mated to the airplane. The mated FE model is correlated to this mated GVT data with the going-in assumption that, at this point, the only unknown variable is the interface stiffness between the test article and the airplane.

Recently, GAC expressed a desire to test a modified nose, the Quiet Spike™, on the DFRC F-15B (ref. 5) airplane. Because of flight test article availability and a compressed project schedule, a non-traditional-testing and model update method had to be implemented. A build-up approach was devised in which a Mock QS was designed and fabricated to replace the flight QS in the tests and analyses. A detailed FE model of this Mock QS was created. A reduced-order model of this detailed FE model was created in the form of a beam model to expedite the model update process. The beam model was then matched to data provided by the first GVT using a strongback. This beam model was mated to the F-15B model and the interface stiffness was updated by a second GVT using the airplane. The flight QS was tested and its model was updated separately at GAC. It was then mated to the aircraft model and its modal analysis results were compared to frequencies and mode shapes from a final GVT of the flight QS mated to the F-15B airplane. Ultimately, the goal of this build-up approach was to completely eliminate the need for a model update of this final flight test configuration.

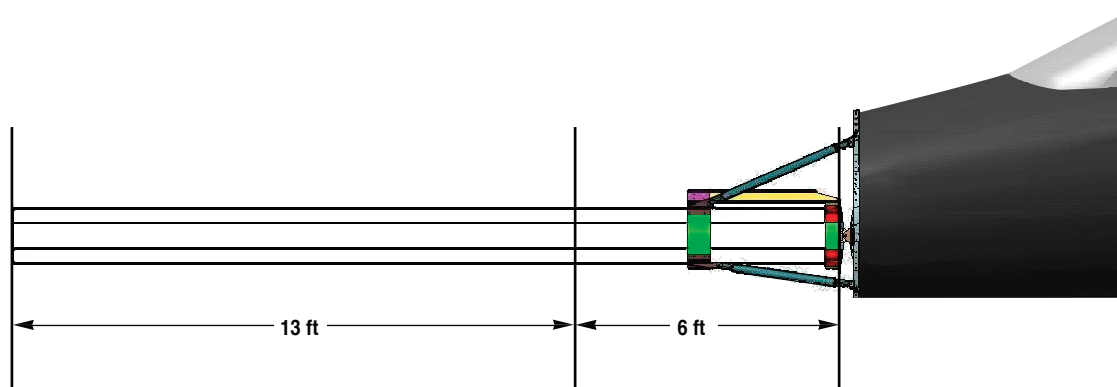
The flight QS measures 30 ft in length when fully extended and 20 ft when fully retracted. Figure 1 shows the GAC flight QS.



070066

Figure 1. Flight QS description.

The Mock QS was designed with the purpose of replacing the flight QS in the build-up GVT approach. For the Mock QS to fulfill this purpose, it was necessary that its design meet the following requirements: 1) similar weight to flight QS weight, 2) similar CG to flight QS CG, and 3) similar  $I_{xx}$  for the third segment of the flight QS. A final design requirement imposed on the Mock QS was an interface with the Strongback and F-15B radar bulkhead in the same manner and with the same hardware as the flight QS installation assembly. A study was done that considered different materials, beam types, thicknesses, diameters, and lengths to determine the best design for the Mock QS. The Mock QS measures 19 ft and is shown in figure 2.



070067

Figure 2. Mock QS description.

Several model updates coupled with a series of four GVTs were performed to acquire a correlated mated F 15B/QS FE model that could be used in flutter analyses. Figure 3 shows the various models of the Mock QS that were developed to accomplish this task. The first FE model created was a detailed FE model of the Mock QS, which was created in Patran and MSC.Nastran (MSC Software Corporation, Santa Ana, California) using the Mock QS computer aided design (CAD) models. It consisted of beam, plate, and solid elements and was fixed in a manner that represented how the flight QS mounted to the airplane. A modal analysis was performed on the detailed FE model. The results from this modal analysis rendered the target frequencies and mode shapes for the beam model, shown on the far right in figure 3.

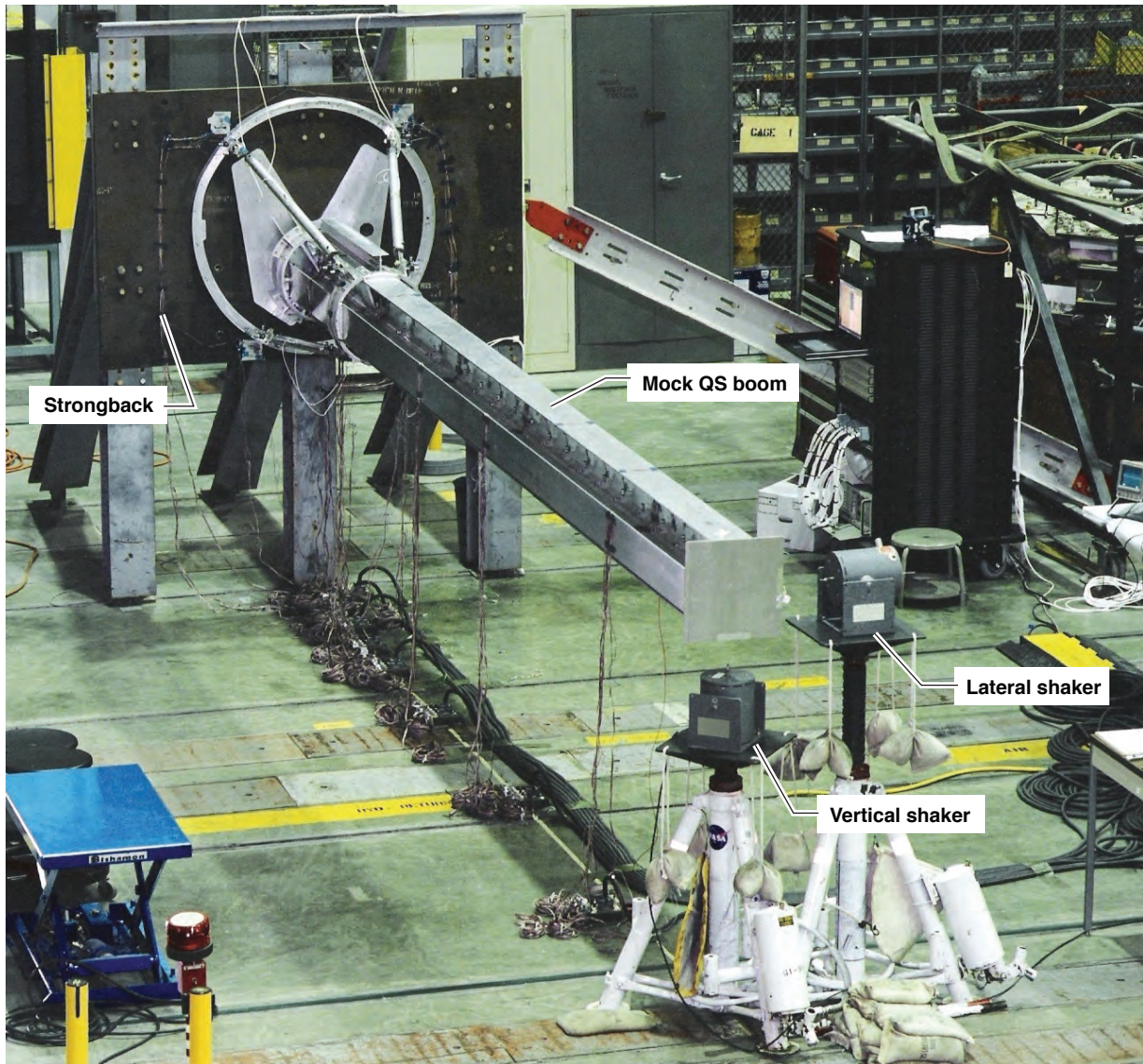


Figure 3. Mock QS model development.

The original beam model was developed in Patran and MSC.Nastran. The lumped mass and beam elements were created manually based on the numerical mass properties of the detailed model. Because the model update process requires much iteration, using a reduced-order model decreases the computational effort required to match model structural properties to test data. This beam model decreased the computational effort in all analyses including the flutter analyses required at the conclusion of the model update process. Furthermore, matching the beam model to the detailed model first provided a good ‘initial guess’ for the Mock QS beam model and would, therefore, facilitate correlating the beam model to test data.

The next step in this task was to correlate the Mock QS beam model to the actual Mock QS structure. This was accomplished in the first GVT, which consisted of attaching the Mock QS boom to a strongback and exciting it in the lateral and vertical directions as shown in figure 4. The results from this GVT were used to update only the structural properties of the beam model. The interface stiffness was not updated until the second GVT. Frequencies and mode shapes were extracted from all the following GVTs to provide target data for model validation (ref. 6). Attaching the Mock QS structure to the Strongback provided a nearly rigid foundation for the boom that ensured the boom modes were excited well. This also matched well with the boundary condition modeled.





070069

Figure 4. Mock QS ground vibration testing on the Strongback structure.

When mating the updated Mock QS beam model to the updated airplane beam model, it was assumed that any discrepancies between the numerical and the test mode shapes and frequencies could be attributed to the unknown connection stiffness between the test article and airplane. The second GVT would empirically provide this connection stiffness. The airplane was constrained laterally and vertically, to achieve airplane modes that were decoupled from the Mock QS modes. The Mock QS was again excited both laterally and vertically. This GVT configuration is illustrated in figure 5.



Photo courtesy Tony Landis

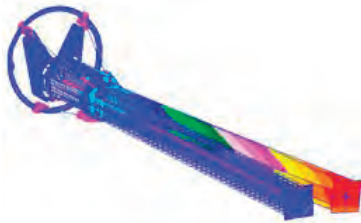
Figure 5. Mock QS boom ground vibration testing on the F-15B airplane.

The third GVT consisted of the flight QS mounted on a strongback that provided the modal parameters to update the flight QS model. The fourth and final GVT served as a final check for the mated F-15B/QS frequencies and mode shapes.

## RESULTS AND DISCUSSION

Because of the simplicity of the structure and the fidelity of the detailed FE model of the Mock QS, there was confidence in its representation of the actual Mock QS hardware. Therefore, in performing the first model update, the target modal values were provided by the numerical results of the detailed model to update the beam model. The first three modes of the detailed model or, target modes, are shown in figure 6.

Mode 1-lateral bending (5.675 Hz)



Mode 2-vertical bending (6.602 Hz)



Mode 3-torsion (7.876 Hz)



070070

Figure 6. Detailed Mock QS mode shapes and frequencies.

The first three modes of the detailed Mock QS were lateral bending at 5.68 Hz, vertical bending at 6.6 Hz, and torsion at 7.88 Hz. Table 2 quantifies the similarity in the modal parameters between the beam and detailed Mock QS models before the beam model was updated.

Table 2. Comparison of frequencies and MAC values before update.

Mode	Detailed FE Model (Hz)	Beam Model (Hz)	MAC (%)	Freq. Error (%)
1	5.675	7.285 (3 <sup>rd</sup> detailed mode)	0.05	28.37
2	6.602	7.515 (1 <sup>st</sup> detailed mode)	0.02	13.83
3	7.876	8.977 (2 <sup>nd</sup> detailed mode)	0.03	13.98

Table 2 indicates that, initially, the beam model did not correlate well with the detailed model. The beam model modes were ordered differently: 1) torsion at 7.285 Hz, 2) lateral bending at 7.515 Hz, and 3) vertical bending at 8.977 Hz. Consequently, this resulted in very low MAC values and high errors in frequency. The higher-than-expected frequencies imply that either the masses were underestimated or the stiffnesses were overestimated in the beam model.

As discussed in the previous section, the first phase of updating the beam model consisted of updating the mass properties. The optimization variables were assigned upper and lower limits of  $\pm 10$  percent of the original values and included the mass values, CGs and inertias of the lumped mass elements. All mass properties were matched to within 0.5 percent error with the exception of the y-CG because the detailed model possesses a y-CG at zero. A comparison for all mass properties is shown in table 3.

Table 3. Comparison of mass properties after update.

	Mass, lb	x-CG, in	y-CG, in	z-CG, in	$I_{xx}$ , lb-in <sup>2</sup>	$I_{yy}$ , lb-in <sup>2</sup>	$I_{zz}$ , lb-in <sup>2</sup>	$I_{yz}$ , lb-in <sup>2</sup>	$I_{zx}$ , lb-in <sup>2</sup>
Detailed	400.01	114.67	0.00	108.08	2.60E+04	2.16E+06	2.15E+06	7.40	2.41E+04
Beam	400.59	114.55	0.03	108.10	2.60E+04	2.16E+06	2.15E+06	7.38	2.41E+04
Error	-0.14%	0.10%	NaN	-0.02%	-0.14%	0.01%	0.01%	0.21%	0.10%



The second phase of this model update consisted of producing an orthogonalized mass matrix. The variables were the same as in the previous phase; however, with the implementation of the constraint functions, the variables were limited to changing in such a way that the objective functions errors from the previous phase would not increase to a value greater than  $\epsilon$  (See table 1). At the conclusion of this phase, the off-diagonal term in the mass matrix of the greatest value was 0.0135. The resulting orthogonalized mass matrix (in percent) was:

$$\begin{bmatrix} 100.00 & -0.02 & 1.35 \\ -0.02 & 100.00 & 0.38 \\ 1.35 & 0.38 & 100.00 \end{bmatrix}$$

The third phase of implementing the DFRC mode matching code matches the beam model frequencies and mode shapes to the detailed model results. For this phase, the design variables were expanded to include element stiffness properties such as beam cross sectional area, area moment of inertias, and torsional constants. This set of design variables was also allowed to range  $\pm 10$  percent to complete the model update procedure. Table 4 demonstrates how the DFRC in-house mode matching code correlated the beam model to the detailed model.

Table 4. Comparisons of frequencies after the first update.

Mode	Detailed FE Model (Hz)	Beam Model (Hz)	MAC (%)	Freq. Error (%)
1	5.675	5.674	98.29	-0.02
2	6.602	6.607	98.14	0.08
3	7.876	7.867	78.64	-0.11

The updated beam model showed good correlation to the detailed model. The first two mode shape vectors were matched to less than two percent error, and the frequencies for all three modes were matched to within one percent error. The third mode shape, which was the torsion mode, did not possess as good a MAC value as the first two. Because of the geometry of the QS and the additional torsional stiffness provided by the radome, the first torsion mode of the actual QS does not appear until approximately 100 Hz. Therefore, it was deemed not critical to match the torsion mode with as much rigor as the lateral and bending modes, and a MAC value of 78 percent sufficed for this mode.

Figure 7 shows the first three mode shapes of the Mock QS beam model after it was updated.



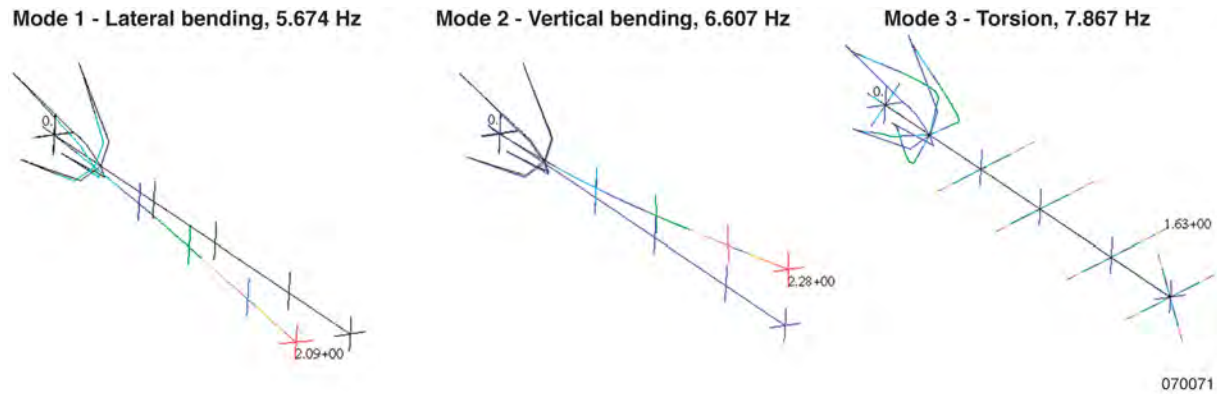


Figure 7. Mock QS beam model mode shapes and frequencies.

The beam model was next updated to match test data that resulted from the first GVT. This first Mock QS GVT required that the Mock QS be mounted to a strongback. The first three modes of the Mock QS were 1) lateral bending at 5.583 Hz, 2) vertical bending at 7.752 Hz, and 3) torsion at 8.105 Hz. Updating the beam model to the detailed model first made updating the beam model to test data faster and less computationally intensive. Table 5 compares the beam model to the Strongback GVT results after only updating the mass properties. In this case, the only mass properties that were measured were total weight and x-CG. The numerical values were kept for all other mass properties.

Table 5. Comparison of frequency and MAC values at update start.

Mode	GVT (Hz)	Beam Model (Hz)	MAC (%)	Freq. Error (%)
1	5.583	5.643	99.29	1.08
2	7.752	7.529	99.49	-2.88
3	8.105	8.142	67.66	0.45

Because the beam model had already been through one update, its modal parameters already correlated well with the measured modal parameters. The design variables were treated similarly as before. They were assigned upper and lower limits of  $\pm 10$  percent of the original values and included the mass values, CGs and inertias of the lumped mass elements. The total weight and x-CG were updated to within a one percent error.

The second phase of the model update, mass matrix orthogonalization, was also treated as previously done. The design variables were the same as in the previous phase. At the conclusion of this phase, the off-diagonal term in the orthogonalized mass matrix of the greatest value was 0.0737. The resulting orthogonalized matrix (in percent) was:

$$\begin{bmatrix} 100.00 & -1.54 & 7.37 \\ -1.54 & 100.00 & -6.17 \\ 7.37 & -6.17 & 100.00 \end{bmatrix}$$

Finally, the beam model was updated to have frequencies and mode shapes that matched the measured data. The design variables were again expanded to include element stiffness properties such as beam cross sectional areas, area moment of inertias, and torsional constants that were allowed to range  $\pm 10$  percent. Table 6 shows how the DFRC in-house mode matching code correlated the beam model to the actual Mock QS boom.

Table 6. Comparisons of frequencies after update to GVT data.

Mode	GVT (Hz)	FE Model (Hz)	MAC (%)	Error (%)
1	5.583	5.594	99.25	0.20
2	7.752	7.764	99.42	0.15
3	8.105	8.093	88.51	-0.15

The resultant numerical modal parameters showed an excellent correlation to the measured modal parameters for the Mock QS test article. The first two mode shape vectors were matched to less than one percent error, and the frequencies for all three modes were matched to within 0.5 percent error. Regarding the third mode shape, we see the same results as before. This mode, the torsion mode, did not possess as good a MAC value as the first two and was again, not regarded as being of great importance.

The final model update required that only the spring element stiffnesses that connected the Mock QS hardware to the aircraft be updated. Initially, they were assumed to be nearly rigid and therefore, were assigned high values. The second GVT would provide their true values. The second GVT consisted of mating the Mock QS boom to the F-15B airplane. The airplane was constrained vertically by supporting it with aircraft jacks and laterally through use of an erector set. This configuration decoupled the aircraft modes from the boom modes. The measured modes and frequencies of this configuration were lateral at 6.06 Hz and vertical at 7.75 Hz. The torsion mode was not extracted for this configuration. Table 7 computes the frequency errors between the numerical and test modes.

Table 7. Comparison of test and numerical modes of the mated Mock QS/F-15B airplane.

Mode	GVT (Hz)	FE Model (Hz)	Freq. Error (%)
1	6.064	5.583	8.62
2	7.756	7.752	0.05

The first airplane test mode was at a higher frequency than the first numerical mode by almost 0.5 Hz. This was not expected, because the mated model already assumed a nearly rigid connection between the Mock QS and the airplane. The higher frequency of the first airplane test mode indicates that the airplane was stiffer laterally than the Strongback was, which can be explained by the high inertia of the airplane compared to the Strongback with the erector set providing a true lateral constraint. This also indicates that the assumption of a nearly rigid connection was accurate and is further supported by the fact that the second numerical mode frequency already matched the second test mode frequency to within a tenth of a percent.

After the flight QS model was updated by test data, it was mated to the F-15B model using this nearly rigid connection stiffness. The project then proceeded to perform flutter analyses using the mated model. This final mated model matched well to GVT data, and therefore, no model update was necessary, and the flutter analysis did not need to be redone. The QS team could quickly proceed to the flight-testing portion of this project.

## **CONCLUSIONS**

The Dryden Flight Research Center has developed an in-house mode matching code that updates both the mass and stiffness properties of a model. This method renders a more accurate model than the method of only updating stiffness properties. The three phases of optimization that the code employs are 1) updating mass properties, 2) orthogonalization of mass matrix, and 3) updating frequency and mode shape. The code has been applied in the GAC QS project flown on the DFRC F-15B supersonic flight testbed. The build-up approach used to update the QS/F-15B mated model was completed using this code. During this project, it was used to perform two model updates. It successfully updated each model used for each mode of interest to within one percent error. This code was applied in such a way that allowed the project to proceed with flutter analyses, such that when the flight test article arrived at Dryden, the project could quickly move into flight testing.

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14. ABSTRACT A crucial part of aircraft design is ensuring that the required margin for flutter is satisfied. A trustworthy flutter analysis, which begins by possessing an accurate dynamics model, is necessary for this task. Traditionally, a model was updated manually by fine tuning specific stiffness parameters until the analytical results matched test data. This is a time consuming iterative process. The NASA Dryden Flight Research Center has developed a mode matching code to execute this process in a more efficient manner. Recently, this code was implemented in the F-15B/Quiet Spike™ (Gulfstream Aerospace Corporation, Savannah, Georgia) model update. A build-up approach requiring several ground vibration test configurations and a series of model updates was implemented to determine the connection stiffness between aircraft and test article. The mode matching code successfully updated various models for the F-15B/Quiet Spike™ project to within 1 percent error in frequency and the modal assurance criteria values ranged from 88.51–99.42 percent.					
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