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A NASTRAN DMAP ALTER FOR DETERMINING A LOCAL

STIFFNESS MODIFICATION TO OBTAIN A SPECIFIED EIGENVALUE

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SUMMARY

This paper describes a technique, which has been programmed as a DMAP Alter to Rigid Format 3, for determining a stiffness matrix modification to obtain a specified eigenvalue for a structure. The stiffness matrix modifications allowable are those that can be described as the product of a single scalar variable and a matrix of constant coefficients input by the user. The program solves for the scalar variable multiplier which will vield a specified eigenvalue for the complete structure (provided it exists), makes the modification to the stiffness matrix, and proceeds in Rigid Format 3 to obtain the eigenvalues and eigenvectors of the modified structure.

INTRODUCTION

The motivation for devising a technique for determining a local stiffness modification to obtain a specified eigenvalue stemmed from several launch loads analyses performed at the Goddard Space Flight Center in which these analyses were updated using data from hardmount spacecraft vibration tests. Quite bften, spacecraft are attached to their launch vehicle via a Marmon type clamp band. Generally, the clamp band attaches the spacecraft to an adapter section which in turn is bolted to the launch vehicle. However, the stiffness of the clamp band is often not known well enough to make an accurate analytical prediction of the fundamental mode of the spacecraft adapter structure when cantilevered from the base of the adapter, as it is in the spacecraft vibration tests. Thus, the original launch loads analyses are updated to reflect these discrepancies once the modes of the spacecraft-adapter structure have been measured in tests.

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Updating any finite element model to agree with modal data obtained from tests usually requires a trial and error process in which some local stiffness is adjusted until the fundamental mode of the model agrees with the test data. However, if a value for the local stiffness exists which will give the finite element model the measured eigenvalue, then this stiffness can be found analytically.

The DMAP Alter presented computes the value of the stiffness (or stiffness change) and adds this to the original stiffness matrix for the finite element model. The program then proceeds in Rigid Format 3 to compute the remaining eigenvalues and eigenvectors for the finite element model.

THEORETICAL DESCRIPTION

In real eigenvalue analysis, NASTRAN solves for the eigenvalues and eigenvectors for the analysis (or U_a) degrees of freedom from

$$[K_{aa} - \lambda M_{aa}] \quad \{U_{aa}\} = 0 \tag{1}$$

The stiffness matrix for the U_a degrees of freedom is obtained from the original U_g degrees of freedom through the application of constraints and Guyan reduction. The stiffness matrix K_{gg} for the U_g degrees of freedom can be considered to be the sum of two matrices

$$K_{gg} = K_{gg} + \Delta K_{gg}$$
(2)

where K_{gg_0} contains the stiffnesses for the finite element model which will not be modified and ΔK_{gg} contains all of those stiffnesses that will be modified. The modification technique described in this paper is one in which the stiffnesses to be modified are <u>all</u> proportional to some scalar variable, which will be denoted as β . Thus, ΔK_{gg} can be written as

where K' are the values of the ΔK_{gg} coefficients per unit value of the scalar variable β . The K' matrix could represent, for example, the portion of the finite element model represented by several beam elements of the same cross section whose moment of inertia we wanted to vary. In this case, β would be the moment of inertia of those beams and K' would be the stiffness coefficients for these beams per unit moment of inertia.

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In general, ΔK_{gg} can be any portion of the finite element model whose stiffness coefficients vary proportionally to some known variable. This variable could not, therefore, be the thickness of plate elements since the bending stiffness varies as the cube of the thickness while the transverse shear and membrane stiffnesses vary with the first power of the thickness. If, however, the plates were pure bending plates (no membrane or transverse shear), then all of the stiffness coefficients would vary with the cube of the thickness and we would be able to express the stiffness of those plate elements by an equation of the type in equation (3) where β could be taken as the cube of the thickness or the bending rigidity D.

Thus, considering only those applications in which the stiffness matrix for a portion of the structure can be represented as in equation (3) where β is a single scalar variable, the stiffness matrix for the complete structure (eq. (2)) becomes

 $K_{gg} = K_{gg} + \beta K'_{gg}$ (4)

The stiffness matrix in equation (4) can be reduced to the analysis set of degrees of freedom U_a through the application of multi and single point constraints and through the Guyan reduction of the omitted points as mentioned above. The only restriction in the DMAP Alter presented herein is that the degrees of freedom that have stiffnesses that will be modified are not allowed to belong to the "0" set (omitted coordinates).

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(3)

Following the normal procedures for reducing from the U_g to the U_a degrees of freedom (with the restrictions mentioned above), the eigenvalue problem as stated in equation (1) can be written as

$$\begin{bmatrix} K_{aa} + \beta K_{aa} - \lambda M_{aa} \end{bmatrix} \begin{bmatrix} U_{a} \end{bmatrix} = 0$$
 (5)

The problem is to find a value of β that will result in one of the eigenvalues (usually the first nonzero eigenvalue) attaining a specified value, say λ_1 . Setting λ equal to the specified value λ_1 in equation (5) results in the equation

$$[(K_{aa} - \lambda_1 M_{aa}) + \beta K'_{aa}] \{U_a\} = 0$$
 (6)

In order for there to be a nontrivial solution to equation (6), the determinant of the coefficient matrix must vanish. This will result in a polynomial in β equal to zero, that is,

$$p(\beta) = 0$$

Thus, the solution for the value of β that will provide a specified eigenvalue (provided such value of β exists) may be obtained by solving an eigenvalue problem, using equation (6), for β . This can be readily accomplished in NASTRAN using the module READ by inputting to READ the matrix ($K_{aa} - \lambda_1 M_{aa}$) as the "stiffness" matrix and the matrix K'_{aa} as the "mass" matrix. The resulting "eigenvalue" found by READ will be the value of β that will provide the stiffness modification necessary for the structure to have the real eigenvalue λ_1 .

It should be pointed out that there is no guarantee that the process will always work. There may be no modification of the portion of the structure we are attempting to modify that will result in the specified eigenvalue λ_1 . However, the analyst can often tell, by comparison of his original finite element modes with those obtained from tests, what portion of the model appears to be too stiff or too flexible. In these instances, the procedure outlined in this paper for determining the stiffness

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nodification should relieve the analyst of the burden of making irbitrary changes in the stiffnesses and solving repeated eigenvalue problems until the model agrees with the test. Since the echnique outlined is one in which a stiffness change is deternined which will provide one eigenvalue equal to a specified value, it appears that it will be most useful when there is disagreement between the original model and test results in a fundamental mode. It should also be mentioned that the stiffhess change, while providing a specified fundamental mode, will bbviously yield higher modes different from those obtained from the original or unmodified finite element model. There is no guarantee that these new higher modes will agree any better with the test modes than those from the original model.

INPUT TO THE PROGRAM

The data deck required to make a run to modify part of the tructure and obtain the resulting eigenvalues will be discussed in terms of changes to a normal deck for Rigid Format 3, real igenvalue analysis.

Case Control Deck

Two subcases are required. In the first subcase, a METHØD ard selects an EIGB bulk data card which will be used for the sigenvalue extraction for β .

The second subcase contains the normal case control cards that the user would have in any Rigid Format 3 run including a ETH9D card which selects the EIGR bulk data card for the real igenvalues λ . The result of this subcase will be the normal ceal eigenvalue analysis output with one of the modes equal to the specified eigenvalue (to be specified in the Bulk Data Deck).

Bulk Data Deck

Input of the normal finite element model of the structure which would be used in a real eigenvalue analysis. From this finite element model the stiffness matrix K will be gg_0 built by NASTRAN. This could be the identical cards used to describe the structure if an original modal analysis had been performed and the user were now rerunning it to modify part of the structure. In this case, the value of β determined in the current run would be the change in stiffness of the modified part of the structure. Included in these cards, of course, is the EIGR card requested by subcase 2 which will find all desired modes subsequent to the modification.

- 2. DMIG input of K gg.
- 3. EIGB card requested by subcase 1 for finding the "eigenvalue" β . The normalization for the eigenvector must be MASS. If the scalar variable multiplier of K'_{gg} is, for example, the moment of inertia of some of the beam elements, then the search range should be the range over which the user expects the change in this variable to lie (change with respect to the value that is in the finite element model in item 1).
- 4. A PARAM bulk data card with parameter name = FREQ and value equal to the frequency (in Hz) of the mode the user wishes to specify.

DMAP ALTER DESCRIPTION

Appendix A lists the DMAP Alters to Rigid Format 3, Level 15.1.0, required to solve for the stiffness modification, to assemble the new stiffness matrix, and to proceed in Rigid Format 3 to obtain all of the desired eigenvalues and eigenvectors of the modified system. Several of the Alter statements are discussed in the appendix to clarify their function. In general, all the DMAP modules used but on are standard DMAP modules described in the NASTRAN User's or Programmer's Manuals. The module SCALAR, however, is a new module written and added to NASTRAN at the Goddard Space Flight Center and will be an available DMAP module in level 16 when it is released. Basically, this is a module that accepts matrices as input and will output one coefficient of the matrix as a NASTRAN complex, single or double precision parameter that can be used, for example, in the DMAP module ADD to multiply other matrices by. This was needed since the only way the scalar value of β could be obtained as data that could be used in subsequent DMAP statements was in the matrix

KHHK output from module GKAM following the eigenvalue extraction for β . The module SCALAR was used to extract p from KHHK. The matrix KHHK is the "modal stiffness" matrix found from the eigenvalue run to obtain β . If the normalization on the EIGB bulk data card requests normalization to unit modal mass, then the coefficient in KHHK will be β .

SAMPLE PROBLEMS

Using the DMAP Alter program, two sample problems have been run. Figure 1 shows a beam finite element model of the UK-5 spacecraft and adapter to be flown on the Scout vehicle. The spacecraft and adapter are attached via a Marmon clamp, which in this finite element model is modeled as a scalar spring. In the original analysis, the model contained no scalar spring element for the clamp band and the adapter and spacecraft were assumed rigidly connected. The fundamental bending mode obtained from this finite element model was 43 Hz. Subsequent tests of the system indicated that the first mode was at 33 Hz and that the Marmon clamp did not appear "infinitely" stiff. Thus, the model was modified by including a spring between the adapter and spacecraft. The second run, made to determine the value that the spring should have to obtain a 33 Hz first bending mode contained the following changes:

- 1. removal of the MPC rigid constraint at the adapter/spacecraft interface that was used in the original analysis to simulace zero bending flexibility at that joint
- 2. addition of DMIG matrix input of a scalar spring stiffness matrix per unit value of stiffness:

where the nonzero values correspond to the rows and columns

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represented by the grid points and rotational degrees of freedom to which the scalar spring connects

- 3. EIGB bulk data card to find k (β is k in this problem) with eigenvector normalization to MASS
- 4. PARAM FREQ bulk data card with value 33 Hz (complex single precision)

The data deck for this run is listed in Appendix B. The output from subcase 1 gave the value of k_s needed to obtain a 33 Hz first bending mode, namely, 4.3 x 10^9 N/m (24.5 × 10^6 lb/in). Subcase 2 then was executed to obtain the eigenvalues and eigenvectors for the system with this spring in the model. The resulting eigenvalues were a 33 Hz first mode with the second mode changing, in this case, by only a few percent from that obtained from the original model.

Figure 2 shows another problem run using the DMAP Alter. In this case, the structure is a stiffened plate simply supported on all four sides. The plate is stiffened with an I beam whose area and offset distance are specified but whose moment of inertia (about the beam centroidal axis) may be varied. The problem is to determine the moment of inertia of the beam that will give a 40 Hz first symmetric bending mode of the structure. The structure was modeled with a 5x5 mesh of grid points equally spaced in one quadrant of the plate. The DMIG matrix K'qq in this problem consisted of the stiffness of the beams (due to the bending moment of inertia only) for all of the grid points to which the beams were attached. The Bulk Data input for the finite element model consisted of the normal input for such a structure but with zero bending inertia for the beams (the area and offset distance were input on the CBAR cards). The first subcase solved for the moment of inertia of the beams that would result in a 40 Hz first symmetric bending mode of the structure. This was determined as 855.8 cm⁴ (20.56 in⁴). Subcase 2 then proceeded to obtain the eigenvalues and eigenvectors of the modified system and it was determined that the first mode was at 40 Hz.

ACKNOWLEDGEMENT

The help of Mr. Reginald Mitchell of the Goddard Space Flight Center is greatly appreciated for his programming efforts in writing the module SCALAR needed in the DMAP Alter.

APPENDIX A

DMAP ALTER FOR DETERMINING LOCAL STIFFNESS CHANGE TO OBTAIÑ A SPECIFIED EIGÈNVALUE (RIGID FORMAT 3)

1 ALTER 45

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- 2 MTRXIN •MATPOOL+EQEXIN•SIL•/DKGGP••/V•N•LUSET/V•N•NODKP/ C•N•0/C•N•0 \$
- 3 SAVE NODKP \$
- 4 MATGPR GPL, USET, SIL, DKGGP//C, N, G/C, N, G \$

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- 5 ALTER 48
- 6 EQUIV DKGGP+DKNNP/MPCF1 \$
- 7 ALTER 58
- 8 MCE2 USET, GM, DKGGP,,,/DKNNP,,, \$
- 9 ALTER 61
- 10 EQUIV DKNNP, DKFFP/SINGLE \$
- 11 ALTER 64
- 12 UPARTN USET, DKNNP/DKFFP, ,, /C, N, N/C, N, F/C, N, S \$
- 13 ALTER 67
- 14 EQUIV DKFFP, DKAAP/OMIT S
- 15 ALTER 70
- 16 UPARTN USET, DKFFP/DKAAP, , , /C, N, F/C, N, A/C, N, O S
- 17 ALTER 75,76
- 18 ADD MAA,/MAA1/C,Y,FREQ S
- 19 ADD MAAl,/MAA2/C,Y,FREQ \$
- 20 ADD MAA2,KAA/DAA/C,N,(39.47842,0.0)/C,N,(-1.0,0.0) \$
- 21 DPD DYNAMICS+GPL+SIL+USET/GPLD+SILD+USETD++++++ED+ EGDYN/V+N+LUSET/V+N+LUSETD/V+N+NOTFL/V+N+NODLT/ V+N+NOPSDL/V+N+NOFRL/V+N+NONLFT/V+N+NOTRL/ V+N+NOEED/C+N+123/V+N+NOUE \$

- 22 SAVE NOEED \$
- 23 COND ERKOR2, NOEED \$
- 24 CHKPNT EED \$
- 25 READ DAA,DKAAP,,,EED,USET,CASECC/LAMAK,PHIAK,MIK,OEIGSK/ C,N,BUCKLING/V,N,NEIGVK/C,N,1 %

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- 26 SAVE NEIGV \$
- 27 OFP LAM/.K+OEIGSK++++//V+N+CARDNOK \$

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- 28 SAVE CARDNOK S
- 29 GKAM •PHIAK•MIK•LAMAK•••••CASECC/MHHK••KHHK•PHIDHK/ C•N•-1/C•N•1/C•Y•LFREĀ=D•0/C•Y•HFREQ=0•0/C•N•-1/ C•N•-1/C•N•-1/V•N•NOCUP/V•N•FMODĒ \$
- 30 SCALAR KHHK//C+N+1/C+N+1/V+N+BETA \$
- 31 SAVE BETA \$
- 32 ADD DKAAP,KAA/KAAT/V,N,BETA 5
- 33 COND LBL6+REACT \$
- 34 RBMG1 USET+KAAT+MAA/KLL+KLR+KRR+MLL+MLR+MRR S
- 35 ALTER 85,90
- 36 READ KAAT, MAA, MR, DM, EED, USET, CASECC/LAMA, PHIA, MI, OEIGS/ C, N, MODES/V, N, NEIGV/C, N, 2 \$
- 37 SAVE NEIGV \$
- 38 CASE CASECC,/CASEX2/C,N,TRAN/V,N,REPEATT=2/V,N,NOLOOP \$
- 39 ALTER 105,105
- 40 SDR2 CASEX2+CSTM+MPT+DIT+EQEXIN+SIL+++BGPDP+LAMA+QG+ PHIG+EST+7+OQG1+OPHIG+OES1+OEF1+PPHIG/C+N+REIG \$
- 41 ALTER 109,109
- 42 PLOT PLTPAR.GPSETS.ELSETS.CASEX2.BGPDT.EQEXIN.SIP..OPHIG/ PLOTX2/V.N.NSIL/V.N.IUSET/V.N.JUMPPLOT/V.N.PLTFLG/ V.N.PFILE S

43 ENDALTER

DESCRIPTION OF DMAP ALTER STATEMENTS

- MTRXIN reads DMIG cards which contain the coefficients of the K gg matrix input by the user. These are the stiffness coefficients (for the portion of the structure which will be modified) per unit value of the parameter that they vary with. These can easily be determined by running Rigid Format 1, up through GP4, with the bulk data containing all grid points, coordinate systems, and elements for the portion of the model to be modified.
- 5-16. These Alters perform the reduction on the K'_{gg} matrix at the same location in Rigid Format 3 that the reductions are performed on the stiffness matrix for the remainder of the structure (K_{gg}) .
- 18-20. Formulate the matrix $K_{aa_o} \lambda_1 M_{aa}$ using the input parameter FREQ which is FREQ = $\frac{1}{2\pi} \sqrt{\lambda_1}$. That is, FREQ is the frequency in Hz of the mode we are specifying the eigenvalue for.
- 25. Solve an eigenvalue problem for β using the buckling option in READ. The resulting "modal stiffness" matrix, KHHK, which will be output from module GKAM, will contain β on the diagonal since the eigenvector normalization on the EIGB bulk data card is a normalization on unit modal mass.
- 29. GKAM outputs the matrix KHHK.
- 30. SCALAR (discussed above) extracts a value from KHHK and outputs it as a parameter (BETA).

32. ADD formulates the total stiffness $K_{aa} + \beta K'_{aa}$.

36. READ extracts the eigenvalues and eigenvector of the modified system, one of which will be the specified eigenvalue λ_1 .

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APPENDIX B

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CASE CONTROL AND BULK DATA DECKS FOR UK-5 S/C - ADAPTER STIFFNESS MODIFICAT

TITLE = UK5 SPACECRAFT AND EH SECTION SUBTITLE = CANTILE/ERED MJDE SHAPES (LATERAL) LABEL = STIFFNESS CALCULATION FOR CLAMP BAND FOR 33 HZ FIRST BENDING ECHO = UNSORT MPC = 52SUBCASE 1 METHOD = 1SUBCASE 2 METHOD = 2OUTPUT VECTOR = ALL ELFORCE = ALL SPCF = ALLBEGIN BULK S S LATERAL MODES S GRDSET 1345 0. 1. 0. 1 BAROR 1.-4 +EIG EIGB INV 5.+6 5.+7 1 1 1 +EIG1 MASS 3 +EIG INV 25. 400. 3 1.-4 EIGR 2 +EIG2 MAX PARAM GRDPNT 0 PARAM WTMASS .002591 S S EH SECTION S 47.77 123456 GRID 501 0. 0. 502 GRID 44. 0. 0. 0. GRID 503 40. 0. 37.27 GRID 504 0. 0. CBAR 5001 5001 502 501 CBAR 5002 503 502 5002 5003 5003 504 503 CBAR 5001 2.634 94.4 94.4 72.6 .989 +850 PBAR 5001 45.8 +B50 PBAR 5002 5001 2.138 59.5 59.5 .989 22.4 +850 .989 5001 29.2 29.2 5003 PBAR 1.710 +85011 +850_ +B5021 +850 +850 +850.31 .185 .185 +B5012 .185 .185 +B5022 +85032 .185 .185 MAT1 5001 1.+7 1.+7 .3 S CONSTRAIN S/C - ADAPTER INTERFACE GRID POINTS TO BE THE S SAME EXCEPT IN ROTATIONAL DEGREE OF FREEDOM S MPC 504 -1.0 51 1 1.0 601 1 504 2 Ż MPC 52 1.0 601 -1.0

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GRID	606 607		19.77 16.27	0.0				
GRID	608		12.77	0.0				
GRID	609		10.27	0.0				
CBAR	6001	6001	602	601				
CBAR	6002	6002	603	602				
CBAR	6003	6003	604	603				
CBAR	6004	6004	605	604				
CBAR	6005	6005	606	605				
CBAR	6006	6006	607	606				
CBAR	6007	6007	605	607				
CBAR	6008	6003	609	608				
PBAR	6001	6001	3.062	37.05			7.297	+B6011
PBAR	6002	6001	3.441	44.87			4.072	+B6021
PBAR	6003	6001	3.525	64.			8.861	+B6031
PBAR	6004	6001	3.225	89.1			10.809	+B6041
PBAR	6005	6001	3.075	118.5			13.492	+B6051
PBAR	6006	6001	3.165	156.5			10.618	+86061
PBAR		6001	3.505 3.965	199.5			7.328 25.31	+86071
PBAR +B6011	6008	6001	3.903	238.6			22+31	+86081 +86012
+86021								+B6022
+86031								+B6032
+86041								+86042
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+86071								+B6072
+86081								+86082
+86012	.1907							
+86022								
+86032	.1589							
+86042	.1591							
+B6052								
+86062								
+86072								
+86082 MAT1	2 .1067 6001	1.+7	1 47	. 7				
DMIG	DKGGP	0	1.+7 6	•3 1	2			
DHIG	DKGGP	504	6	*	504	6	1.0	+DK1
DMIG	DKGGP	601	6		504	6 6	~1.0	+DK2
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