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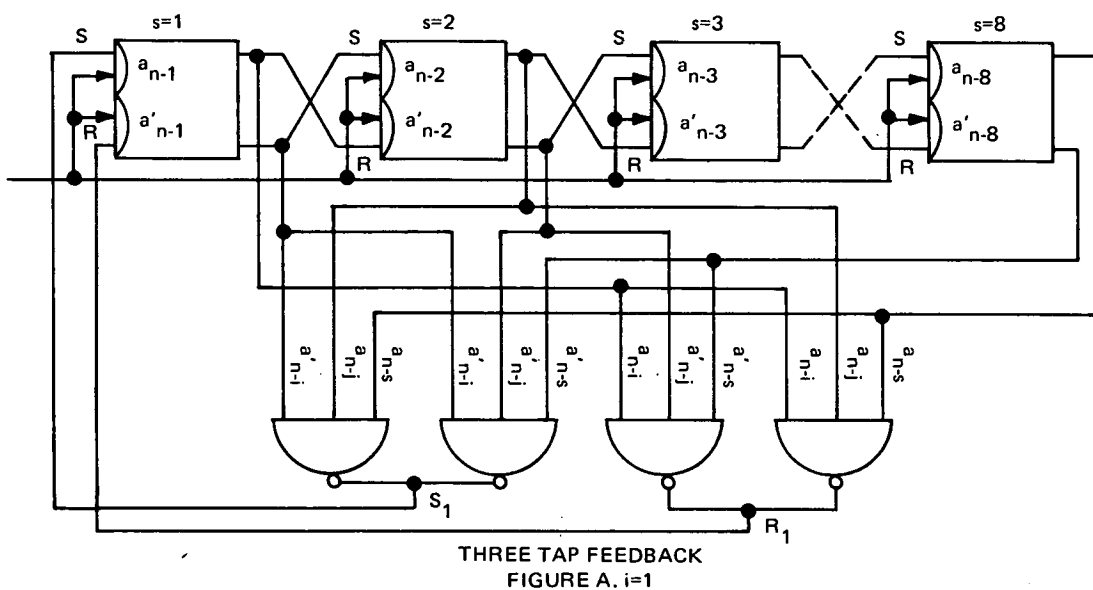
# NASA TECH BRIEF

## NASA Pasadena Office



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### Improved Feedback Shift Register



#### The problem:

Currently feedback shift registers (FSR) of  $s$  stages, which use a two tap feedback decoding structure, cannot generate a maximal length sequence ( $2^s - 1$  states), when  $s$  takes on the value of certain integers.

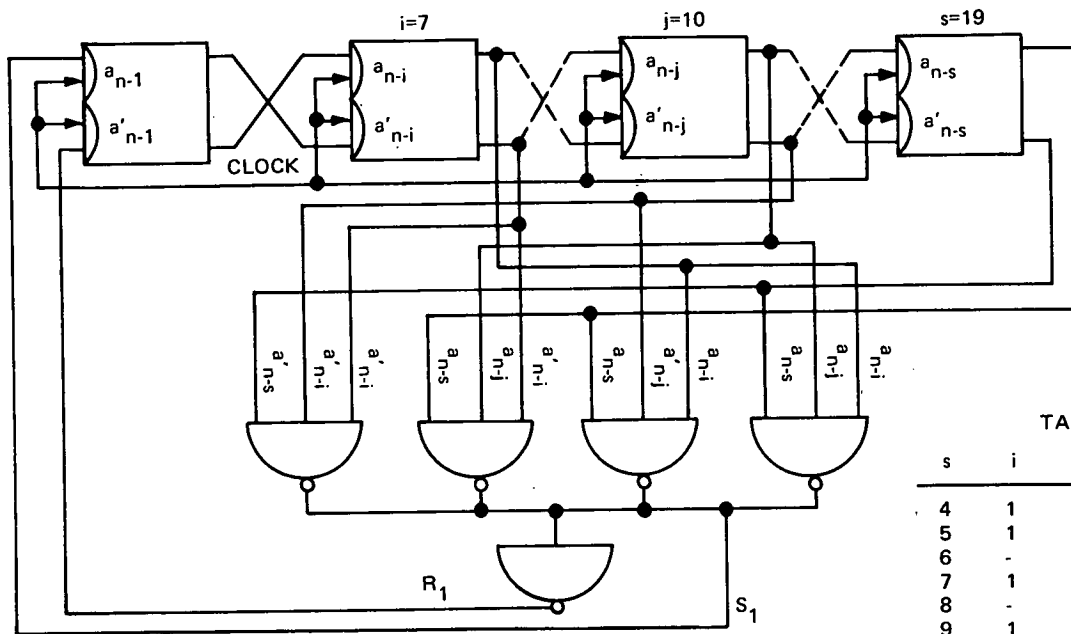
#### The solution:

A design has been formulated which uses a three tap feedback decoding scheme. The taps are selected from appropriate stages of the feedback register. This results in the generation of near maximal length sequences ( $2^s - 2$  or  $2^s - 4$  states) for any integral value of  $s$ . These sequences will be either 1 or 3 increments shorter than a maximal length sequence. In addition the autocorrelation function of the three tap FSR shows a large negative correlation at  $180^\circ$  out of phase, in addition to the normal positive  $0^\circ$  phase. This is very useful in obtaining sequence synchronization patterns.

TABLE 1

$s$	$i$	$j$	$2^s - 2$
4	1	2	14
5	1	3	30
6	1	2	62
7	1	5	126
8	1	2	254
9	2	6	510
10	2	3	1022
11	1	3	2046
12	2	7	4094
13	-	-	-
14	1	2	16382
15	3	5	32766
16	1	2	65534
17	1	11	131070
18	1	12	262142
19	1	7	524286
20	1	14	1048574

(continued overleaf)



THREE TAP FEEDBACK  
FIGURE B.  $i \neq 1$

TABLE 2

s	i	j	$2^s - 4$
4	1	3	12
5	1	2	28
6	-	-	-
7	1	4	124
8	-	-	-
9	1	2	508
10	1	5	1020
11	1	4	2044
12	1	3	4092
13	1	2	8188
14	-	-	-
15	1	12	32764
16	1	7	65532
17	1	14	131068
18	5	9	262140
19	7	10	524284
20	5	7	1048572

### How it's done:

It has been found that for every integer value of  $s$  number of stages (except for  $s$  equal to 13 in the  $2^s - 2$  case) up to relatively large values, at least one near maximal length sequence can be generated providing the three stages (designated as  $i, j, s$ ) to be used in the feedback gating structure are properly selected. The last stage of the feedback register is always used. This is the  $s$  parameter. The  $i$  and  $j$  stages may vary depending on the sequence length. As shown in Figure A, an 8 stage feedback shift register with a three-tap structure is connected to provide a 254 counting ( $2^8 - 2$ ) sequence. The selected feedback stages are  $i=1, j=2$ , and  $s=8$ . When  $i=1$  (first stage) only four nand gates are required to implement the feedback logic.

In Figure B, the nineteen-stage three-tap feedback shift register is connected to provide a 52,484 counting ( $2^s - 4$ ) sequence. The selected feedback stages are  $i=7, j=10$ , and  $s=19$ . Since  $i \neq 1$  five nand gates are required for this implementation.

By utilizing the data shown in Tables 1 & 2 (which indicate the appropriate feedback stage selections) and connecting the feedback logic as shown in the figures, near maximal length cycles can be realized for each value of  $s$  for cycle lengths of  $2^s - 2$  and  $2^s - 4$ .

### Note:

Requests for further information may be directed to:  
Technology Utilization Officer  
NASA Pasadena Office (JPL)  
4800 Oak Grove Drive  
Pasadena, California 91103  
Reference: B72-10226

### Patent status:

This invention has been patented by NASA (U.S. Patent No. 3,535,642). Inquiries concerning non-exclusive or exclusive license for its commercial development should be addressed to:

Patent Counsel  
NASA Pasadena Office  
4800 Oak Grove Drive  
Pasadena, California 91103

Source: M. Perlman of  
Jet Propulsion Lab  
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