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# NASA TECH BRIEF



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## Interaction of Crippling and Torsional-Flexural Instabilities for Centrally Loaded Columns

An empirical technique is proposed for prediction of failure loads for centrally loaded columns, with thin-walled, open cross sections, which may fail by a combination of torsional-flexural buckling and crippling. Knowing the torsional-flexural buckling load and the crippling load for a column, their interaction can be predicted by a modification of the Johnson-Euler equation which is often used to relate crippling and Euler-type buckling:

$$P_c = P_{cs} - (P_{cs}^2 / 4P^*)$$

where  $P_c$  is the critical load (pounds) in combined crippling and torsional-flexural buckling,  $P_{cs}$  is the crippling load (pounds), and  $P^*$  is the critical load (pounds) in torsional-flexural buckling.

For such loaded columns that fail at stresses within the elastic range, the critical mode of failure is often torsional buckling or a combination of torsional and flexural buckling; it depends primarily on the geometry of the cross section and the length of the column.

There are methods for evaluation of this torsional or torsional-flexural buckling load for many variations in cross-sectional geometry and restraint conditions. All such methods, however, are based on the assumption that the cross-sectional shape does not change during buckling; that is, the theories consider primary failure of columns, rather than secondary failure, characterized by distortion of the cross section. Formulation of a theory incorporating coupling distortion and flexure with local buckling would be extremely complex.

For very short columns of thin-walled, open cross sections the failure stress is determined by the crippling-stress method, which does provide for local distortion of elements of the cross section.

Thus the coupling of these two failure modes by empirical means would provide a simple means for prediction of failure loads of columns that may fail by a combination of the torsional-flexural mode and the crippling mode. This approach has been followed already in the coupling of crippling and Euler buckling for closed sections (Johnson-Euler equation); the approach is the same in this coupling of crippling and torsional-flexural buckling. Although no attempt has been made to generate or correlate test data to confirm the accuracy of this technique, it is believed to be accurate.

Notes:

1. The following documentation may be obtained from:

Clearinghouse for Federal Scientific  
and Technical Information  
Springfield, Virginia 22151  
Single document price \$3.00  
(or microfiche \$0.65)

Reference:

NASA-CR-61287 (N69-32465), Interaction of Crippling and Torsional-Flexural Instability for Centrally Loaded Columns

2. Technical questions may be directed to:  
Technology Utilization Officer  
Code A&TS-TU  
Marshall Space Flight Center  
Huntsville, Alabama 35812  
Reference: B70-10598

(continued overleaf)

**Patent status:**

No patent action is contemplated by NASA.

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