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Hidden Structures: Using Graph Theory to Explore Complex System of Systems Architectures

Matthew Potts, Pia Sartor, Angus Johnson and Seth Bullock

Abstract The increasing interconnectivity of complex engineered system of systems (SoS) leads to difficulties ensuring systems architectures are of sufficient quality (availability, maintainability, reliability, etc.). Typically reductionist approaches are used during systems architecting which may fail to provide the desired insights into key relationships and behaviors. New approaches are therefore needed and this work shows how tools from complexity science can be applied. Data from a NATO Architecture Framework complex SoS architecture, based on a Search and Rescue Use Case, is modelled using graph theory. The analysis includes degree distribution, density, connected components and modularity. Such analysis supports architectural decision making such as dependency allocation, boundary identification, areas of focus and selection between architectures. It is shown how the analysis from complexity science can be used to analyze complex SoS architectures, to provide an alternative view, that explores relationships and structure in a non-reductionist, general approach when considering architecture decisions.

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1 Introduction

Large defense and space organizations are often faced with the challenge of designing a System of Systems (SoS) or a system that will operate within the context of a SoS. A SoS can be defined as "an assemblage of components with Operational and Managerial Independence" [1], a "set of systems for a task that none of the systems can accomplish on its own" [2]. A SoS may have key characteristics of "autonomy, belonging, connectivity, diversity and emergence" [3] where emergence here is "the principle that entities exhibit properties which are meaningful only when attributed to the whole, not to its parts" [4]. At the start of the Systems Development Process [5] some requirements may exist and a system architecture, the "fundamental concepts/properties of a system, embodies in elements, relationships, and principles of design" [6] is needed to assist understanding context, exploration of alternatives, understand trades and support decision making [7]. Such systems are increasingly likely to be complex [8]; formed of many heavily interconnected components whose behavior is emergent and cannot simply be inferred from the behavior of components [9].

Systems architecture methodologies, such as the NATO Architecture Framework (NAF) [10] provide practitioners with many tools, techniques and views to explore different perspectives of a system in order to create some shared understanding and support decision making. For example, system architecture methodologies can support investment decisions such as whether to bid for a particular project, or design decisions that will affect the subsequent system, sub-system and component design. The NAF v4 methodology is currently under development but is "likely to be based on The Open Group Architecture Framework (TOGAF) Architecture Development Method (ADM) with input from other sources" [10]. The ADM [11] proposes an iterative eight step approach to developing systems architectures. An architecture team uses the methodology to build a shared understanding within the team of the problem space and guides thinking towards a viable solution space through the creation of several Architecture Views (AVs) along several perspectives and considerations, shown in **Fig. 1**.



Fig. 1. NAF v4 Viewpoints and example AVs.

The concern with this approach however is that when constructing AVs several heuristics are used which are appear in conflict with complex systems approaches, for example reductionism and aggregation. The original work of Rechtin [12] and recent updates from Sillitto [13], suggests a practitioner should 'simplify, /simplify, simplify'. For complex SoS such reductionist approaches may mask the underlying structures and relationships that are important for understanding and characterizing the SoS. Design Structure Matrices (DSMs) [14], more specifically Multiple-Domain Matrices (MDM)[15] or Engineering System Matrices (ESM) [16], are potential solutions to visualize and analyze interdependencies however may generate large, and difficult to visualize or process, matrices. New approaches are therefore needed.

A potential solution resides in bringing complexity science to bear on systems engineering, with the path initially laid out in the work of Sheard [17] and Bolton [18]. Sheard's [19] more recent Complexity Primer serves as a good background to this line of inquiry. Structural assessments of system architectures are not new, with work by Sinha and de Weck [20] exploring complexity assessments of topologies. However such work is based on systems architectures that are not as broad as system architectures in the context of Architecture Frameworks, such as NAF.

More recently Harrison [21] explored the potential use of Graph Theory for Systems Engineering, specifically looking at a system design and calculating throughput, measuring complexity and trying to optimize design. While throughput may be an interesting property for some systems, its utility for systems that have no clear sink or source is perhaps limited. The design optimization approach and complexity measuring approaches are potentially interesting avenues of investigation however this paper seeks to build an abstraction of a complex SoS architecture from AVs, as opposed to the abstraction used by Harrison, and investigate the utility of complexity science tools from that starting point. Graph based models have been presented using 'higraphs', which extend graphs to a quadruple adding 'depth' (enclosure of one vertex within another) and 'orthogonality' (partitioning function), with potential applications to requirements management and system design [22-24].

This paper proposes a new methodology to explore the underling structure and relationships of complex System of Systems (SoS) architectures in order to support shared understanding and decision making. This research seeks to build on previous work. This work is novel because it starts from a new perspective, that of complex SoS architectures and Architecture Frameworks such as NAF. The contribution of this work is that it provides an additional view, coherent with SoS engineering approaches like that of Luzeaux [25] and current systems architecting methodologies.

A fictitious Search and Rescue Architecture, created to help refine NAF v4, is used to build a directed graph (digraph) which is then visualized and analyzed. The analysis includes degree distribution, density, strongly connected components and modularity. Such analysis supports architectural decision making, such as dependency allocation, boundary identification, areas of focus and support selection between architectures.

The approach suggests that complexity science tools, namely graph theory, can be used to visualize, understand and explore the hidden structure and relationships of complex SoS architectures. A discussion on the utility of such an approach is presented noting that the exploitation of this as a robust tool within industry requires careful consideration and further work is proposed to drive this forward.

2 Search and Rescue Architecture

This research took data from a Search and Rescue Architecture that was developed by Thales in order to inform systems architecture training and help the development of NAF v4. The system is based on a real life complex SoS, having the key characteristics detailed in **Table 1**, making it a useful use case for tangible products, having also been used by others to develop systems architecture analysis [26,27].

Key term	Important characteristics from definition	SAR SoS characteristics
System of Systems (SoS)	An assemblage of compo- nents with Operational and Managerial Independence.	Each constituent system is a system in their own right with their own management and operations, brought together for a common purpose.
	A set of systems for a task that none of the systems can accomplish its own	Although aspects of SAR could be conducted by individual systems, a full maritime SAR capabil- ity relies on the overall SoS availability.
	Autonomy, belonging, con- nectivity, diversity and emer- gence.	Each system can operate autonomously without the SoS, connectivity is open when systems join and have a range of communications and opera- tions available to them. The systems are diverse, emergence[4] is the ability of the SoS to effec- tively coordinate a search operation over a large area for a small, moving object and recover it with precision and speed to a place of safety. The individual parts of the SoS cannot carry this out alone.
Complex System	System formed of many inter- connected components; ca- pacity to exhibit emergence, behavior cannot be simply in- ferred from behavior of com- ponents.	The many interconnected components of the SAR SoS come from the myriad of individual systems within the SoS and the emergent behavior has already been considered.

Table 1. SAR Characterization.

The Search and Rescue SoS seeks to detect distressed persons or vessels and recover them to a place of safety in a maritime context. The SoS comprises many entities including rotary and fixed wing air assets with modules fitted such as sensors and recovery equipment, fast and slow maritime vessels, a plethora of personnel, command and control communications and information services and several agencies from procurement, training delivery, administration and execution, shown in **Fig. 2**.



Fig. 2. High Level Operational Concept Diagram Search and Rescue [28].

The use case views can be taken from the fictitious "Yellow" country, which is part of a wider fictitious "Rainbow" international organization, or from commercial entities that may wish to bid for aspects of a program to enhance the capability. In either case, in order to build a shared understanding of the SoS, an architecture is produced in accordance with NAF v4. A potential limitation of this approach however is that it requires the team to keep several of these views in mind at one time to attempt to make sense of the whole. Although some views exist to provide high level context, NAF does not have a view that exposes dependencies across the entire system. Referring back to **Table 1**, an approach is sought that explores key relationships and structures of the system as a whole, something the following approach attempts to address.

3 Results

Graph theory has been used extensively to analyze large complex networks by modelling system elements as vertices and the relationships between them as edges, with wide ranging applications in biology, networks and social science [29-31]. It is assumed the reader has an understanding of graph theory and basic analysis of graphs. Refer to [2931] for further information. As graph theory allows modelling of a large number of heterogeneous system components, elements and relationships it can be considered to be complimentary to architecture frameworks that seek to provide an overall understanding and characterization of a complex system but which may lack direct analytical tools to support decision making.

A digraph was constructed using several AVs from the SAR architecture, where capabilities, services and logical nodes (from logical views in NAF, not to be confused with nodes from graph theory) were modelled as vertices with relationships between them modelled as directed edges with no weightings. In NAF, services contribute to capabilities, and capabilities are contributed to by nodes (Fig. 1; for full definitions refer to NAF literature). However, it is worth noting that these terms are not independent. Edge weights could be added to address the importance of a link or interaction, with values taken from NAF views themselves or expert opinion. They are omitted here to simplify the model in order to more straightforwardly demonstrate the suitability of the approach. The ability to visualize the structure and relationships of the complex SoS architecture is shown below (Fig. 3) with Logical Nodes (red), Services (blue) and Capabilities (green) and vertices sized by degree, highlighting to an architecture team potential areas to focus on. The digraph was visualized and analyzed using Gephi [32], a common open source software package. Several software packages and algorithms offer ways to visualize a graph and a thorough review of these is not provided here, instead the interested reader is pointed to Tamassia [33]. The initial visualization of a digraph is likely to be in a random layout but is shown here in a common layout (Yifan Hu Force Directed Layout [34]) with manual adjustment of vertices for readability.

There is no obvious source or sink with this digraph, or edge weights added, so flow problems cannot be explored. AVs were taken that could be deemed as primary areas of interest, there is a concern however that the abstraction hides potentially significant information from view, for example in such a model there is currently no measure of how important individual relationships or vertices are in their own right. The main focus of this inquiry however is to explore structure and relationships. For a detailed explanation of individual elements one can return to the NAF views where such detail is readily available. Any number of other dependencies could be considered here too, such as common resources. However, this is left for future work.



Fig. 3. SAR Architecture Digraph

The digraph can be considered to be an integrated view of several individual architecture views which independently do not necessarily comprise all of the important relationships or highlight the inherent structure, but when combined do highlight these to an architect. Interestingly, the SAR AVs are predominantly hierarchical, suggesting the resulting digraph would resemble a hierarchy when combined together, in reality the SAR architecture digraph is far more interconnected. A common purpose of architecting and architecture frameworks is to build a shared understanding and by adjusting the visual layout of the digraph this view can add value, in this example showing clearly the vertices with the highest number of connections. The Rescue Node may be worthy of special consideration due to their number of connections, potentially indicating a challenge for interface design.

3.1 Degree Distribution

The degree for a digraph is the sum of edges entering the vertex and leaving the vertex. Examining the in and out degree distribution highlights potentially important vertices, for example vertices with high in degree and low out degree would be of interest as they have a large number of connections in but that connect onwards to one other node, suggesting the loss or removal of that vertex could have significant consequences. For example the Land SAR Service and Maritime SAR Service are the only contributors to the SAR Service however depend on a total of 21 other vertices. Vertices with a large great number of connections to them, or connect to a large number of other vertices, are worthy of special consideration and focus during systems architecting given their potential influence in the SoS.

3.2 Density

The density of the digraph is calculated as Equation (1) where E is the number of edges in the digraph and V is the number of vertices in the digraph. The density is therefore a measure of how densely connected the digraph is, a value of one corresponding to every possible connection between vertices being present.

$$D = \frac{|E|}{|V| (|V| - 1)} \tag{1}$$

The density of the SAR architecture digraph is 0.074, with each vertex in the SAR example only connected to a few other vertices. If the architecture had a great deal more connections between vertices this value would be higher but for the SAR SoS the loss of a vertex or an edge could have a large impact on the overall connectivity of the digraph suggesting its structure may not have much resiliency. Density could help decide between two competing complex SoS architectures, the higher density solution is likely to have a greater integration, or at least dependency management challenge, whereas the lower density solution may have less relationships to be concerned with. Conversely however a lower density digraph structure may not have as much resiliency to the loss of a connection or vertex.

3.3 Strongly Connected Components

A digraph is considered strongly connected if there is a path (a distinct sequence of edges connecting vertices [35]) in each direction between each pair of nodes, in other words if every node is reachable from every other nodes in both directions. This paper uses Tarjan's [36] depth-first search algorithm to detect strongly connected components; groupings of vertices that meet the above criteria.

By showing the groupings of vertices that can all reach each other it may suggest the existence of a core and periphery of the digraph. This may assist the overall understanding and characterization of the complex SoS, especially if considering an organization that is trying to understand where their systems influence in the wider SoS. This may help identify where to apportion responsibility, boundaries, or internal and external dependencies. The SAR architecture digraph has two separate strongly connected components (**Fig. 4**), the first strongly connected component (left) has 9 vertices all connected (22% of total vertices) while the second Strongly Connected Component (right) identifies 7 vertices all connected (17% of total vertices).



Fig. 4. SAR Architecture Strongly Connected Components

3.4 Modularity

Community detection (the identification of clusters or communities of vertices with many edges joining vertices of the same cluster or community and comparatively few between clusters or communities) within graphs remains an ongoing research inquiry, the interested reader is directed to Fortunato's [37] work. Network modularity (not to be confused with engineering design modularity) is a popular metric in the area of community detection within complex network research, providing a measure of how readily a digraph can be divided into modules, resulting in groupings of vertices that are more strongly connected to each other then they would be in a random digraph [38]. This paper utilizes the algorithm of Blondel et al [39] to calculate the modularity of the digraph. Analysis thus far has grouped vertices with similar quantitative properties whereas modularity groups by similar connections. A visualization of the digraph, colored by modules, is shown in Fig. 5. In the SAR example it appears that the Communication Service, Boat Service, Distress Monitoring Capability, Inform Capability, Communications Capability and SAR Asset Controller Node could be considered as one grouping of related aspects (orange vertices). This offers a different approach, contrasted with **Fig. 3**, when considering boundaries for complex SoS architectures; by focusing on communities of similar nodes in terms of their structure.



Fig. 5. SAR digraph with vertices colored by modularity class.

4 Discussion

By modelling a complex SoS architecture as a digraph a vast range of analytical tools from complexity science become available. The approach enables a visualization of the structure and relationships that would otherwise remain hidden or rely on the viewer to construct a model in their head. An architecture team can use this approach to identify areas to focus attention on and enable partitioning of the system architecture in an alternative way which may assist boundary and dependency allocation. The dependencies that are of interest may be different for different complex SoS and hence the choice of dependencies modelled as a digraph requires careful consideration and could equally include ownership or shared resource dependencies in some contexts. It is worth noting that the concepts modelled here are heterogeneous and hence reliance should not be placed solely on numerical results.

In the early phases of a project, when an organization is trying to make investment decisions, such as whether to make bids for aspects of a SoS, this analysis can help determine the influence of different aspects of the SoS. For example, if the "Yellow" country tendered for part of the SoS that is firmly on the periphery of the SoS, or has many external system dependencies, it may be of little interest to a commercial organization as the ability to intervene may have little influence on the overall success of the SoS. The indicators provided by this analysis are situation dependent and hence a prescriptive method to support decision making is not suitable. However it is envisioned that practitioners could add these insights to their organizational learning scheme to inform investment decisions or provide a comparison between candidate architectures. For example, an organization considered to have a large systems integration capability may select a candidate architecture with a higher density as it may prove to be a more resilient architecture, at the expense of a potentially larger integration or dependency management challenge.

Architectures are created using a blend of art and science, whereas the tools from graph theory are predominately empirically based, thus caution should be exercised when making decisions based on empirical values with a small number of architectural elements. Instead, an approach is recommended that uses the analysis and visualization from graph theory for specific purposes: to visualize structure, to identify areas of interest, and to temper architecture decisions such as which architecture to choose or investment appraisals. The proposed methodology cannot be seen as a wholly alternative approach, rather as a complimentary one to be used in conjunction with traditional methods to provide a view dedicated to what makes a complex SoS challenging; a perspective on underlying structure and relationships.

5 Conclusion and Future Work

This paper has introduced the problem of supporting decision making on complex SoS architectures. Traditional architecture framework methodologies and system architecture approaches may not provide sufficient insight into the underlying relationships and structure of the SoS as they create static views from a single perspective. A SAR

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Architecture was introduced and a methodology was described to model this as a digraph. This representation allows analysis into the structural properties of the model and visualization. From this analysis it is suggested that architectural decisions could be made around boundary selection or investment decisions.

The modelling could be improved through the additional of edge weights to characterize relative importance of connections. In a SoS, interactions may evolve throughout the course of a mission of a system. Hence future work could explore dynamic considerations of relationships, either by comparing architecture configurations at different times or setting up a dynamic graph that can be updated through the life of the system. Further work should concentrate on demonstrating the utility of this approach on different use cases with larger data sets, comparing a complex SoS to a non complex systems architecture and using different architecture frameworks for the data. The application of this approach to a real world complex system would provide further validation and would require an investigation into ways to focus the analysis on critical aspects of the system. The utility of the approach could be improved by the creation of a tool for the extraction of data from a collection of AVs and automatically conducting analysis, along with determining which metrics or properties are most valuable.

Although the work does not replace or challenge existing practices, it does suggest a complimentary view that can be taken when considering complex SoS architectures by integrating readily available data into a single digraph for analysis. Such analysis helps highlight important characteristics like structure and relationships which may support decision making however further work is needed to qualify the utility of such an approach against larger datasets and broader examples.

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