

How to bend galaxy disc profiles – II. Stars surfing the bar in Type-III discs

J. Herpich,¹★† G. S. Stinson,¹ H.-W. Rix,¹ M. Martig¹ and A. A. Dutton^{1,2}

¹Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany

²New York University Abu Dhabi, PO Box 129188, Abu Dhabi, UAE

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ABSTRACT

The radial profiles of stars in disc galaxies are observed to be either purely exponential (Type-I), truncated (Type-II) or antitruncated (Type-III) exponentials. Controlled formation simulations of isolated galaxies can reproduce all of these profile types by varying a single parameter, the initial halo spin. In this paper, we examine these simulations in more detail in an effort to identify the physical mechanism that leads to the formation of Type-III profiles. The stars in the antitruncated outskirts of such discs are now on eccentric orbits, but were born on near-circular orbits at much smaller radii. We show that, and explain how, they were driven to the outskirts via non-linear interactions with a strong and long-lived central bar, which greatly boosted their semimajor axis but also their eccentricity. While bars have been known to cause radial heating and outward migration to stellar orbits, we link this effect to the formation of Type-III profiles. This predicts that the antitruncated parts of galaxies have unusual kinematics for disc-like stellar configurations: high radial velocity dispersions and slow net rotation. Whether such discs exist in nature, can be tested by future observations.

Key words: methods: numerical – galaxies: formation – galaxies: kinematics and dynamics – galaxies: structure.

1 INTRODUCTION

1.1 Observed disc breaks

Most late-type galaxies share one common property: an approximately exponential stellar surface density profile (de Vaucouleurs 1957, 1958; Freeman 1970) which extends over several scale-lengths. As observations reached fainter surface brightness limits, a more diverse picture of late-type morphologies has become apparent: a major portion of such galaxies actually exhibit broken exponential profiles (e.g. van der Kruit 1979; Pohlen et al. 2004). First, truncated or down-bending disc profiles were discovered (e.g. Pohlen et al. 2002). These discs' profiles feature a break at a radius outside of which the surface brightness profile is still exponential, but steeper. By contrast, Erwin, Beckman & Pohlen (2005) observed antitruncated or up-bending profiles in barred S0–Sb galaxies. The breaks in these galaxies have the opposite behaviour: the slope of the exponential profile outside of the break is shallower than its

inner counterpart. Thus stellar disc profiles fall into three different categories:

- Type-I: pure exponential profiles
- Type-II: truncated or down-bending profiles
- Type-III: antitruncated or up-bending profiles.

Several studies investigated the abundance of each type of disc breaks in different observational samples (e.g. Pohlen & Trujillo 2006; Erwin, Pohlen & Beckman 2008; Gutiérrez et al. 2011; Maltby et al. 2012b, 2015) with the result that the relative abundances vary with morphological type. Pohlen & Trujillo (2006) found that pure exponential (Type-I) discs are rather rare (10 per cent). Head, Lucey & Hudson (2015) find that more than 70 per cent of the galaxies with broken disc profiles in the Coma Cluster have a bar, despite a low bar fraction (about 20 per cent) in the overall sample. They therefore relate the origin of Type-III profiles to bars. A similar statement has been made by Kim et al. (2014) for Type-II profiles in galaxies with small bulges. Another possible cause for Type-III profiles, dubbed *disc fading*, are stellar haloes that outshine the stellar disc at large radii, although Maltby et al. (2012b, 2015) found that this can only explain a minor fraction of observed Type-III light profiles.

* E-mail: jakob@jkherpich.de

† Member of the International Max Planck Research School for Astronomy and Cosmic Physics at the University of Heidelberg, IMPRS-HD, Germany.

1.2 Theoretical explanations of breaks

The formation of stellar Type-II disc profiles has been studied in numerical models of isolated galaxies (e.g. Debattista et al. 2006; Foyle, Courteau & Thacker 2008; Roškar et al. 2008; Minchev et al. 2012). Simulations (Roškar et al. 2008) and analytical models (Dutton 2009) suggest that the size of the inner disc, i.e. the radial position of the disc break, is related to an upper limit of gas angular momentum in a rotationally supported star-forming gaseous disc. In this picture, stars that populate the regions outside the break radius must have been born inside the break. Roškar et al. (2008) showed that radial migration, induced by transient spiral arms (first described by Sellwood & Binney 2002, hereafter SB02), can move a sufficient number of stars outside the break radius and populate that region. Stars that migrate via this mode are heavily biased to be on near-circular rather than eccentric orbits and to be vertically cool (SB02; Roškar et al. 2012; Solway, Sellwood & Schönrich 2012; Vera-Ciro et al. 2014). An important diagnostic of this mechanism is that the migrated stars preserve their circularity and, hence, the majority of the migrating stars stay on near-circular orbits (see also SB02; Roškar et al. 2012; Solway et al. 2012; Vera-Ciro et al. 2014). This mechanism predicts positive stellar age gradients outside the break in Type-II discs (Roškar et al. 2008). The existence of such age profiles has been confirmed by observed colour profiles (Azzollini, Trujillo & Beckman 2008; Bakos, Trujillo & Pohlen 2008), spectroscopic observations of NGC 6155 (Yoachim, Roškar & Debattista 2010) and by resolved stellar populations (Radburn-Smith et al. 2012). Recent work by Ruiz-Lara et al. (2016) found that positive age gradients in galaxy outskirts are not unique to Type-II discs. They claim that these age profiles are not linked to Type-II profiles but do not rule out stellar migration as a possible mechanism to populate the regions beyond the disc break.

The origin of Type-III disc profiles is still poorly understood. Most of the proposed mechanisms resort to external forces (e.g. Younger et al. 2007; Kazantzidis et al. 2009; Roediger et al. 2012; Borlaff et al. 2014). However, Maltby et al. (2012a) and Head et al. (2015) found no dependence of a galaxy's disc break type on its environment. This disfavours an external origin of breaks in stellar discs. The first successful attempt to produce Type-III disc profiles in simulations of isolated galaxies was put forward in a preceding letter (Herpich et al. 2015, *paper I* hereafter).

1.3 Halo spin disc break correlation

In *paper I*, we analyse a set of controlled simulations of galaxy formation in Milky Way mass haloes with varying initial angular momentum. We found that the type of the profile break correlates with initial host halo spin. Low-spin haloes produce Type-III disc profiles, and high-spin haloes yield Type-II profiles. In a sharp transition between these two regimes (intermediate spin), pure exponential Type-I profiles formed.

In this paper, we present results of a more thorough analysis of the low-spin simulations that were the subject of *paper I*, i.e. the simulations that formed Type-III profiles. Thus, we will only briefly review the properties of the simulations and refer the reader to *paper I* for a more detailed description.

In this paper, we seek a more analytic understanding of how Type-III profiles may form. We start out with a short overview of previous theoretical work on stellar dynamics in non-axisymmetric rotating potential perturbations such as spiral patterns or bars (Section 2). In Section 3, we quickly review the simulations from

paper I. The simulations with the lowest spin will be analysed in more detail and with a particular focus on stellar orbit evolution and bar properties in Section 4. There we also identify the physical cause for the formation of Type-III profiles and illustrate it with a simple toy model in Section 5. Observational signatures of such Type-III profiles are presented in Section 6. Finally, we summarize and discuss our results in Section 7.

2 DYNAMICS IN STELLAR DISCS

In their landmark work, SB02 show that non-axisymmetric perturbations in the potential (e.g. spiral arms or bars) can drive radial migration of stars in stellar discs. Binney & Tremaine (2008) describe the respective physics in Sections 3.3.2 and 3.3.3 which we briefly summarize here.

In such a potential Jacobi's integral e_j is an integral of motion, i.e. it is constant. It is defined as

$$e_j = e - \Omega_p j_z, \quad (1)$$

where e is a test particle's specific orbital energy and j_z is the z -component of the specific angular momentum in a non-rotating frame,¹ If e_j and Ω_p are constant, equation (1) implies that changes in energy e are proportional to changes in angular momentum j_z :

$$\Delta e = \Omega_p \Delta j_z. \quad (2)$$

It is conceptually useful to plot e versus j_z . That plot is commonly referred to as a *Lindblad diagram*. Given these idealized conditions, equation (2) governs the trajectory of test particles in the Lindblad diagram: it must have a slope that equals the pattern speed Ω_p . (See fig. 1 in SB02.)

Trajectories along other slopes in the Lindblad diagram are possible, but such motions cannot be caused by perturbations rotating with a constant pattern speed, such as bars.

SB02 also find that to first-order changes in the radial action J_R are proportional to the difference between the pattern speed Ω_p and the azimuthal angular velocity of the star's guiding centre Ω_* :

$$\Delta J_R / m_* = \frac{\Omega_p - \Omega_*}{\omega_R} \Delta j_z, \quad (3)$$

where ω_R and m_* are the radial frequency and mass of the star, respectively. Consequently, changes in angular momentum at the corotation resonance ($\Omega_p = \Omega_*$, hereafter CR) do not introduce any radial heating and orbits preserve their circularity in this linear limit.

In a reference frame that is rotating with the spiral perturbation, particles can be 'trapped' at the CR. Such particles experience significant oscillations in the radial direction. For an individual transient spiral perturbation, SB02 find that the magnitude of angular momentum changes peaks near the CR and, therefore, a succession of transient spirals with different pattern speeds can cause angular momentum changes in the entire stellar disc. SB02 argue that such spiral perturbations have to be transient because otherwise they would undo the (radial) changes in stellar orbits they caused (see also section III.C.1. in the review by Sellwood 2014).

Roškar et al. (2012) find that stars may be transported to the CR of another coexisting transient spiral perturbation and therefore may migrate significant distances in a short time without being heated.

Steady (i.e. not transient) rotating perturbations are not expected to modify stellar orbits that are not in resonance with the perturbation (Lynden-Bell & Kalnajs 1972). Such resonances occur at

¹ We implicitly assume the perturbation to rotate about the z -axis.

CR (see above) and at *Lindblad resonances*, where the frequency at which a star experiences the perturbation $m(\Omega_* - \Omega_p)$ equals the absolute value of its radial frequency. m is the azimuthal multiplicity of the perturbation. This condition can be satisfied inside and outside of the CR. The corresponding resonances are being referred to as the *inner* and *outer* Lindblad resonances (OLR). At the Lindblad resonances, orbits will experience radial heating [equation (3)]. However, the widely accepted paradigm is that CRs are the dominant source of radial motions due to spiral perturbations (SB02). SB02 also find that particles on near-circular orbits migrate more efficiently than those on eccentric orbits. This bias has been confirmed in later works by Solway et al. (2012) and Vera-Ciro et al. (2014). These studies also find a similar bias towards stars that are dynamically cool in the vertical direction. The terms *radial migration* or *churning* have been established for the above mechanism (Schönrich & Binney 2009; Sellwood 2014). We will use both terms interchangeably throughout the rest of this paper.

It has long been known that bars cause considerable radial mixing. Migration can also be generated by a bar perturbation but, unlike churning, bar-induced mixing dynamically heats stars (Hohl 1971) and gas (Friedli, Benz & Kennicutt 1994). Bar and spiral resonances can overlap and cause chaotic or non-linear evolution of stellar orbits (Quillen 2003). Such overlaps may move stars across the disc even more effectively than churning (Minchev & Famaey 2010; Minchev et al. 2011). Bars have also been linked to the formation of outer rings (Romero-Gómez et al. 2006, 2007; Athanassoula, Romero-Gómez & Masdemont 2009) indicating that they can drive radial redistribution. However, the formation of rings is generally believed to be caused by gas that it driven to the OLR by bars (Mo, van den Bosch & White 2010).

SB02 point out that despite the significant amount of radial migration in their simulations, there is no significant influence on the morphology of the stellar disc. Bars, however, are known to significantly change a disc’s appearance (Hohl 1971).

Roškar et al. (2008) showed that churning can move stars beyond the truncation radius of simulated discs ultimately forming the outer part of a Type-II disc profile. The predicted ‘U-shaped’ age profile for this scenario has been confirmed by observations (see Section 1.2). However, churning could not be linked to Type-III profiles.

In this paper, we will show that bars can, indeed, be responsible for Type-III disc breaks by substantially heating a subset of disc stars. We will also present arguments that disfavour churning in Roškar et al. (2008) as the cause for the outward migration occurring in our slowly rotating simulations from paper I.

3 SIMULATIONS

We set up a $10^{12} M_\odot$ NFW (Navarro, Frenk & White 1997) halo with 10 per cent of its mass in gas. The halo concentration is $c = 10$. Dark matter (DM) and initial gas particle masses are 1.1×10^6 and $1.2 \times 10^5 M_\odot$, respectively. The gravitational softening length is $\epsilon_{\text{soft}} = 227$ pc.

The DM particles’ velocities were drawn from the equilibrium distribution function (Kazantzidis, Magorrian & Moore 2004). The gas particle velocities were set according to the cosmologically motivated angular momentum profile from Bullock et al. (2001) and are purely tangential with no velocity dispersion as that is modelled by the hydrodynamics solver. The velocities are normalized

according to the halo’s spin parameter λ which is the free parameter in our set-up. We use the definition from Bullock et al. (2001):

$$\lambda = \frac{J}{\sqrt{2} M V R} \Big|_{R=R_{200}}. \quad (4)$$

The initial temperature profile satisfies hydrostatic equilibrium.

For further details about the initial conditions, the reader is referred to paper I.² Since the simulations are self-consistent, the level of control we have is limited, i.e. we are not able to tune certain features of the simulated galaxies independently, e.g. the bar strength or the disc scalelength.

The simulations were evolved with a slightly modified version of the publicly available treeSPH code CHANGA (Jetley et al. 2008, 2010; Menon et al. 2015). The employed version features stochastic star formation (Stinson et al. 2006, $c_* = 0.1$) following the Kennicutt–Schmidt law (Kennicutt 1998), radiative metal line cooling, metal diffusion and stellar feedback (Dalla Vecchia & Schaye 2012; Stinson et al. 2013). This recipe has proven to produce realistic galaxies in cosmological simulations (Wang et al. 2015).

The simulations were evolved for a period of 8 Gyr. We explored the spin parameter range of $0.02 \leq \lambda \leq 0.1$. For the analysis, we used the N -body analysis framework PYNBODY (Pontzen et al. 2013).

4 RESULTS

In this paper, we study the orbit evolution of individual stellar particles in the lowest spin simulation from paper I which forms an Type-III disc break ($\lambda = 0.02$). The goal is to determine how these profiles form. Throughout the rest of this paper, we will use the term *outer disc* to refer to stars that are located outside the position of the break in the radial profile in the final simulation output after 8 Gyr.

In Fig. 1, we present mock observational images of all simulated galaxies from paper I. They were created using the radiative transfer code SUNRISE (Jonsson 2006). The galaxies are more extended and less radially concentrated as λ increases. All galaxies are disc-like with albeit rather thick discs. Fig. 1 in paper I presents the surface density profiles of the respective galaxies (see paper I for details).

In Fig. 2, we present the average stellar overdensity relative to the mean density $\delta = \Sigma_*(R, \varphi) / \langle \Sigma_* \rangle(R) - 1$ at the respective radius in polar coordinates. For the lowest spin simulation (top left panel), we see a small but strong bar (vertical features offset by $\Delta\varphi = \pi$ indicated by the small vertical arrows). The bar signature gets weaker with increasing spin and completely disappears for the highest spin simulation. While the discs of the high-spin galaxies ($\lambda > 0.04$) feature complex trailing patterns, the lowest spin galaxies exhibit a one-armed leading pattern. This is consistent with the visual impression from Fig. 1.

The middle panel of fig. 2 in paper I shows the ratio of inner to outer scalelengths as a function of λ from a broken exponential fit. It shows that a high initial spin yields galaxies with Type-II disc surface density profiles, while low initial spin yields Type-III profiles.

4.1 Outer discs

Based on very similar simulations, Roškar et al. (2008) reproduced the formation of Type-II disc breaks. The position of the break in

² The initial conditions code PYICS is publicly available and can be downloaded from <https://github.com/jakoberpich/pyICs>.

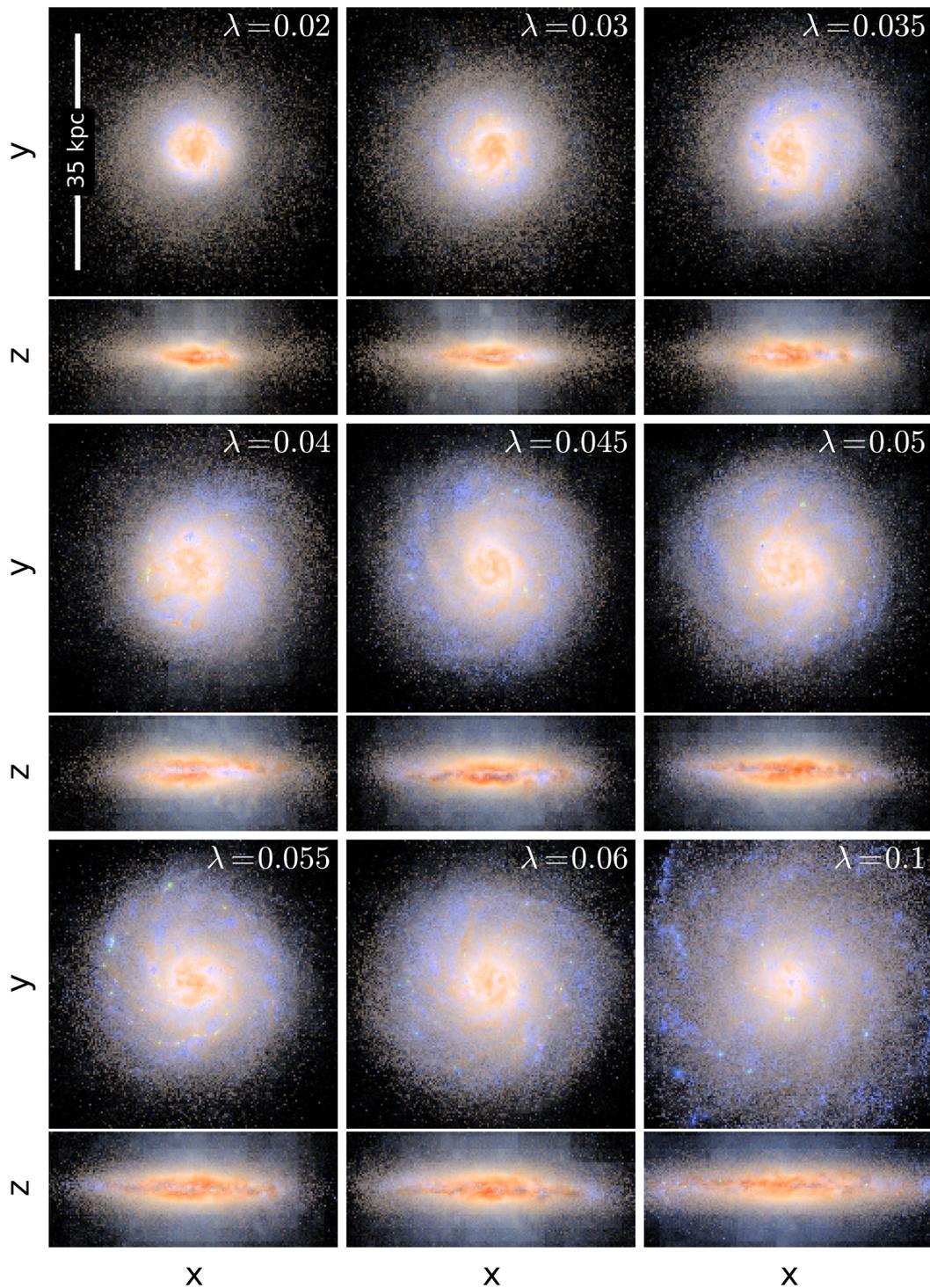


Figure 1. Mock observational images of all simulated galaxies. The image shows face-on and edge-on images of all simulated galaxies from low spin ($\lambda = 0.02$) in the top left to high spin ($\lambda = 0.1$) in the bottom right. Each panel is 35 kpc across. The images have been created with the radiative transfer code *SUNRISE* (Jonsson 2006). The low-spin galaxies are compact and red but they do have a disc component that is clearly visible in the edge-on view. The edge-on views also reveal a massive central bulge for the lowest spin simulations. As the initial spin increases, the galaxies get more and more radially extended and less centrally concentrated. All galaxies with $\lambda > 0.04$ show signs of spiral structure in the blue components. In all cases, the discs are rather thick.

the disc profile is set by a radial cut-off of star formation due to the radial termination of the gaseous disc. In their simulations, stars later found in the disc outskirts formed inside the break radius. They found no evidence for radial heating causing migration but instead resonant scattering off of transient spiral arms (SB02) to be

responsible for the outward migration of stars. An important signature of this mechanism is that the migrated stars in the outer disc are predominantly on near-circular orbits, i.e. rotationally supported (see also Roškar et al. 2012). In this section, we will show that the migration mechanism in our high-spin simulations is consistent

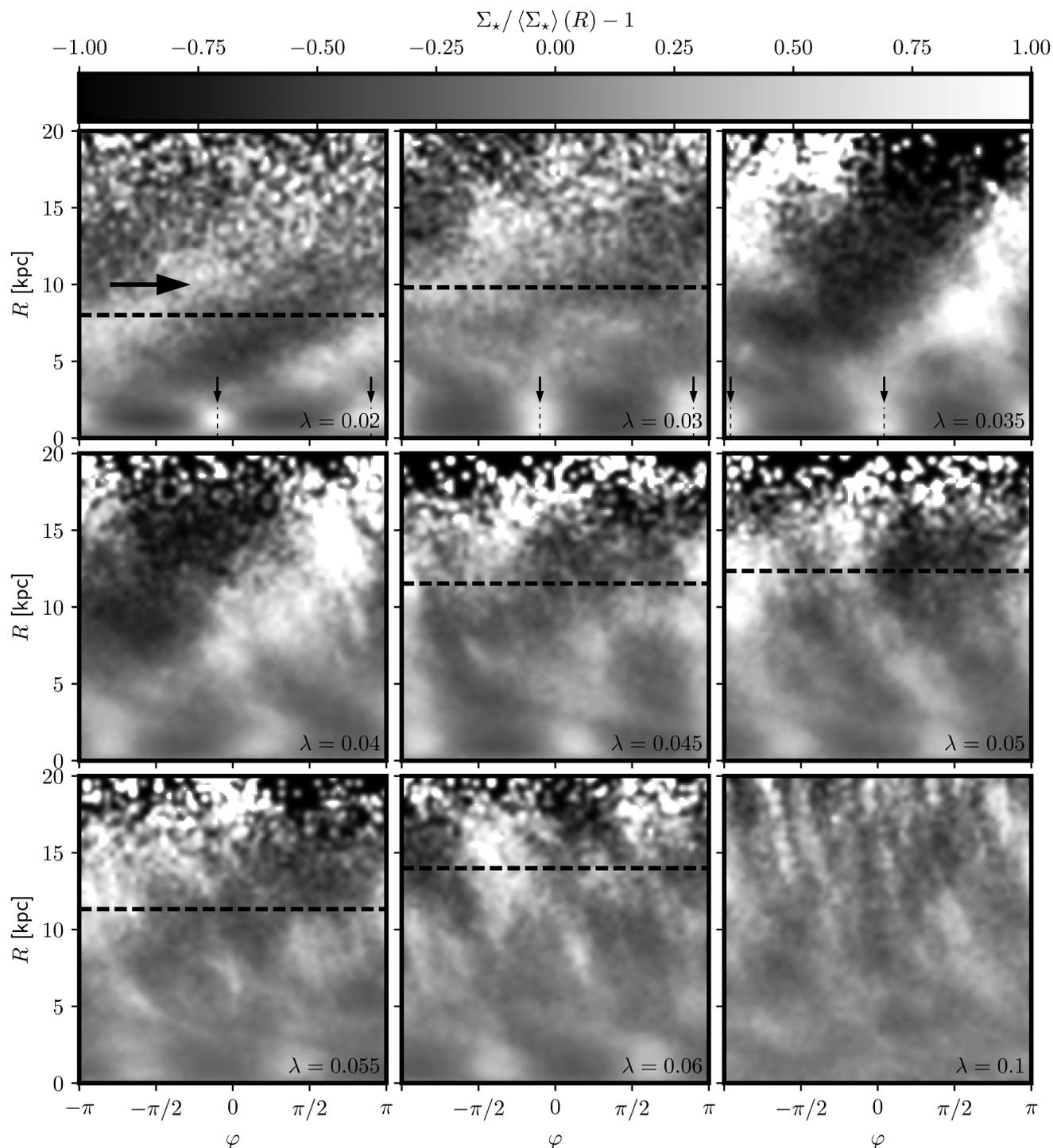


Figure 2. The plot shows the relative stellar overdensity $\delta = \Sigma_*(R, \varphi) / \langle \Sigma_*(R) \rangle - 1$ in polar coordinates for each simulated galaxy after 8 Gyr. The horizontal arrow in the top left panel indicates the sense of rotation of all galaxies. The horizontal dashed lines indicate the position of the break (except for the Type-I discs, for $\lambda = 0.1$ the break is located just outside the plotted range). The small vertical arrows and corresponding dotted lines in the top row indicate the position of the bars in the lowest spin simulations.

with this mechanism. These can produce Type-II disc profiles as well. We also show that the low-spin simulations, which exhibit Type-III breaks, are not.

We first confirm the finding of [paper I](#) that all outer disc stars in all of the simulated galaxies must have migrated outward from inside the respective break radii. Additionally, we will show that the outer disc stars in the discs with Type-III profiles stem from the

vicinity of the galactic centre, while their counterparts in the discs with Type-II profiles were born further out in the disc. This will be followed by showing that the outer disc stars in the Type-III cases are on very eccentric orbits.

Fig. 3 shows the distribution of birth radii of the stars in the outer disc. We see that practically all outer disc stars are born inside the respective break radius. Here, we find a stark

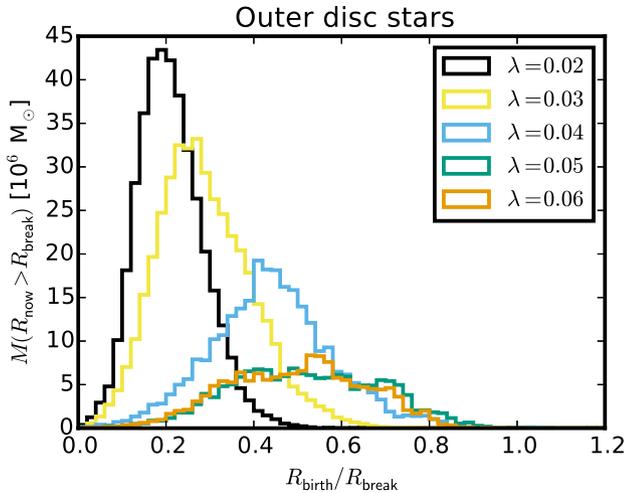


Figure 3. The distribution of birth radii for outer disc stars. The radii are normalized by the break radius in the final snapshot. Practically all stars beyond the break region were born at smaller radii. The effect is most extreme for the Type-III breaks ($\lambda \lesssim 0.03$).

difference between the low- and high-spin cases. In low-spin simulations, almost all outer disc stars are born well inside the break radius, $R_{\text{birth}} < R_{\text{break}}/3$. In the high-spin cases, the birth radii are located at larger galactocentric distances, $R_{\text{birth}} \approx R_{\text{break}}/2$. This difference is even more clear in absolute values as the break radii grow with λ (paper I). We summarize that in all cases the outer disc stars migrate from inside the break region and in the case of the lowest spin simulations originate from predominantly very small radii.

We now characterize stellar orbits in our simulations through their circularity parameter $\frac{j_z}{j_c(e)}$. The circularity parameter is the z -component of a star's specific angular momentum normalized by the specific angular momentum of a circular orbit at the same specific orbital energy. By construction, a particle on a perfectly circular orbit has $\frac{j_z}{j_c(e)} = 1$. Particles on perfectly radial orbits satisfy $j_z = 0$ and thus have a circularity parameter of 0. In practice, we will consider every particle with $0.8 \lesssim \frac{j_z}{j_c(e)} \lesssim 1$ to be on a near-circular orbit and particles with $\frac{j_z}{j_c(e)} \approx 0$ on radial orbits. Eccentric orbits cover the range in between these two limiting cases. Negative values correspond to counter-rotating orbits.

In Fig. 4, we present mass-weighted histograms of the distribution of $\frac{j_z}{j_c(e)}$ for stars that are beyond the break radius for selected simulations. For the Type-II breaks ($\lambda > 0.04$), most of the orbits are near circular and thus consistent with the mechanism proposed by Roškar et al. (2008). The presence of complex spiral patterns in those galaxies (see Fig. 2) supports this hypothesis. The simulations with Type-III breaks, on the other hand, only have very few stars in their outskirts that are on near-circular orbits. Contrary to the higher spin simulations, the distribution of the circularity parameter drops to 0 at values of ≈ 0.8 – 0.9 in these cases. The $\frac{j_z}{j_c(e)}$ distribution peaks roughly at 0.5, which corresponds to rather eccentric orbits. This lack of near-circular orbits beyond the break in our simulations with Type-III disc breaks disfavors radial migration as described in Section 2 as a possible formation mechanism because it is less efficient for eccentric orbits (SB02).

As there is no evidence that the formation mechanism of the Type-II breaks differs from that of Roškar et al. (2008), we will focus our further analysis on the yet unexplained Type-III breaks.

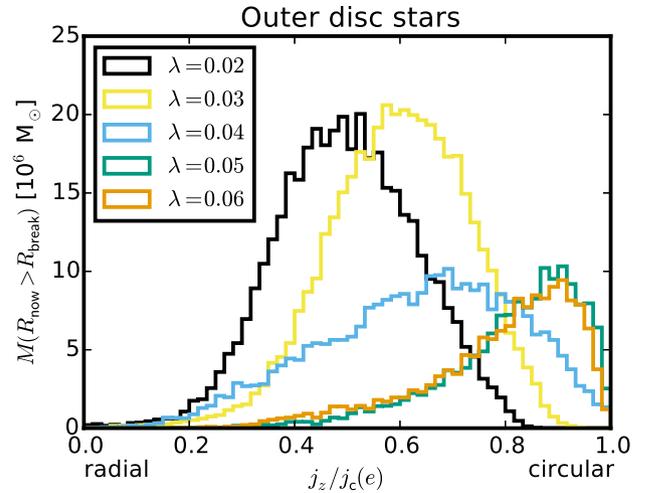


Figure 4. Circularity distribution in outer disc. The figure shows the circularity distribution of stars in the disc outskirts ($R > R_b$) for a choice of simulations spanning the range from low ($\lambda = 0.02$) to high spins ($\lambda = 0.06$). Most orbits in the high-spin simulations ($\lambda > 0.04$) are circular while there is not a single star with $\frac{j_z}{j_c(e)} \gtrsim 0.85$ in the lowest spin simulation. Intermediate spin simulations show a broad circularity distribution in the outskirts ranging from completely radial (0) to circular (1). For pure exponential discs, we interpolated the ‘break radius’.

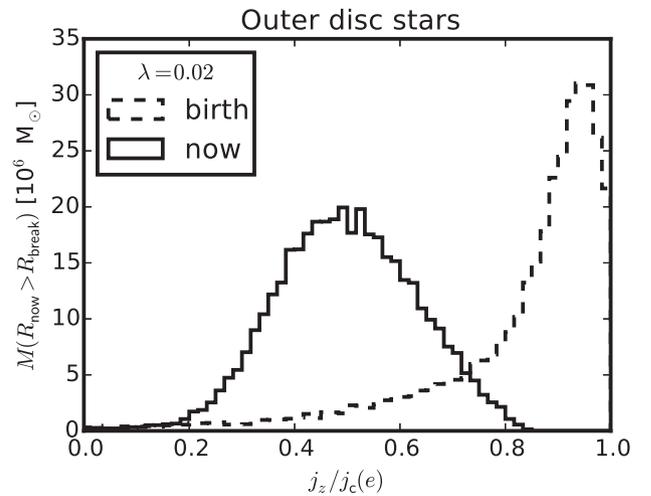


Figure 5. Circularity evolution in a low-spin simulation. The figure shows the distribution of the circularity parameter $\frac{j_z}{j_c(e)}$ of the stars outside the break radius at their formation (dashed) and in the final snapshot (solid). When these stars are born, most of them are on a circular orbit but as they migrate outwards, their orbits get more and more eccentric.

4.2 Orbit evolution in Type-III discs

Given the substantial radial mass redistribution in Type-III discs, we are now going to explore what mechanism is most important in driving this redistribution. We focus our analysis on the lowest spin simulation ($\lambda = 0.02$). The break radius of this galaxy is $R_{\text{break}} = 8.0 \pm 0.5$ kpc.

Fig. 5 shows the distribution of the circularity parameter $\frac{j_z}{j_c(e)}$ of the outer disc compared to the star's $\frac{j_z}{j_c(e)}$ distribution at birth (dashed line). Most of the outer disc stars were born on nearly circular orbits. Thus, there must be a mechanism that transforms

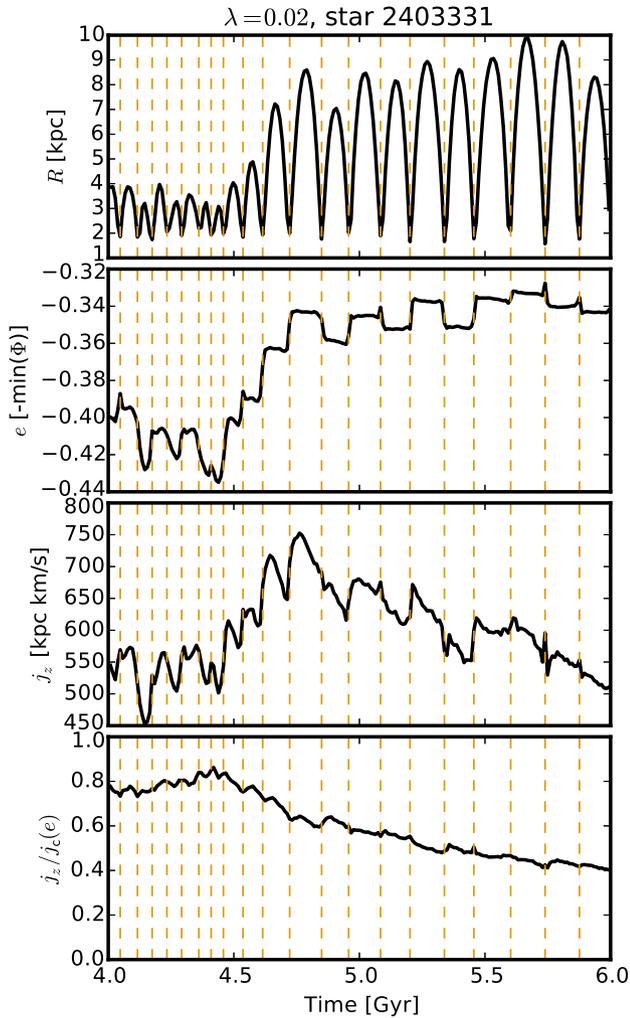


Figure 6. Orbit evolution of an individual star. The vertical dashed lines indicate the pericentre passages of that star. The top panel shows the evolution of its radial position, the second panel shows its orbital energy, the third panel shows the evolution of its z -component of specific angular momentum and the bottom panel shows its circularity parameter. While the star’s apocentre is still small ($t \lesssim 4.5$ Gyr) its binding energy is almost permanently changing. After approximately 4.5 Gyr, its apocentre grows significantly and the star’s binding energy turns into a step function with steps occurring only at pericentres. The star particle instantaneously gains energy and angular momentum during many pericentre passages. In between these passages, its energy stays constant but it loses angular momentum that causes the particles circularity to decrease steadily.

orbits from circular to radial and significantly increases the orbits apocentre.

In order to figure out how orbits get transformed we looked into the time evolution of the orbit of one particular stellar particle. Fig. 6 presents the evolution of orbital parameters of a sample star particle from the outer disc. The four panels show (from top to bottom) the evolution of the star’s radial position R , specific orbital energy e , specific angular momentum z -component j_z and circularity parameter $\frac{j_z}{j_c(e)}$. The times of pericentric passage are marked by vertical dashed lines.

After 4.5 Gyr, the star gains or loses energy (second panel) and angular momentum (third panel) at each pericentre passage. When the star is far away from pericentre, its energy stays constant, but it

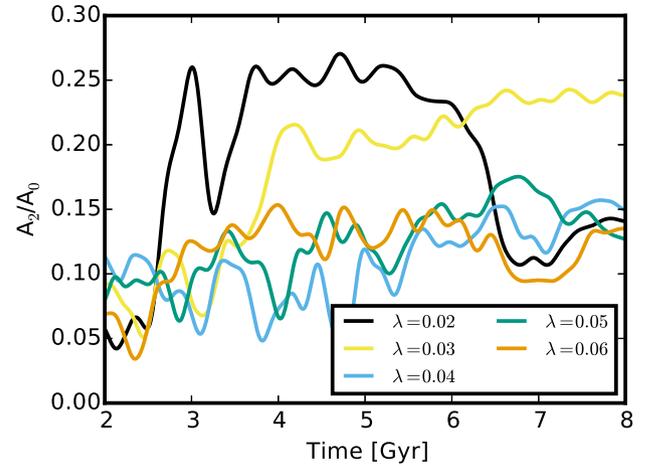


Figure 7. Bar strength evolution. The figure shows the relative amplitude of the $m = 2$ Fourier mode of all stellar particles inside 1 kpc as a function of time. While the values for intermediate and high spin are rather low, there is an excess in bar strength for the lowest spin ($\lambda = 0.02$ – 0.03) simulations for a period of about 4 Gyr.

loses specific angular momentum (third panel), which reduces the circularity of its orbit (bottom panel).

During this time span, the binding energy evolves approximately following a step function. The steps occur at pericentre. If the star gains energy e at pericentre, its semimajor axis increases and vice versa. The pericentre, however, stays more or less constant at approximately 2 kpc. This particular star has a net gain in energy which is not surprising as it has been selected from the outer disc in the final simulation output. In general, it is also possible for a star to have a net loss of energy. Such stars migrate towards the galaxy centre and, therefore, cannot be found in the outer disc.

Before 4.5 Gyr, the star in Fig. 6 has a rather small semimajor axis (< 4 kpc) and the steps in the evolution of its binding energy are smoother and not as well defined yet. Generally, the binding energy of the star is constant when it is far away from the centre and varies only near the centre. Thus, we expect the source of the variation of binding energy to be in the centre of the galaxy. As we will show later (Sections 4.4 and 5), the source is the central bar. We stress that the behaviour of the star displayed in Fig. 6 is qualitatively similar to that of other stars found in the outskirts of our low-spin discs.

4.3 The bar in Type-III discs

Since particle orbits seem most affected in the centre of galaxies near a possible bar, we characterize the bar using the coefficient of the $m = 2$ Fourier mode:

$$A_2 = \sum_j \exp(i2\varphi_j) m_j, \quad (5)$$

where m_j and φ_j are the mass and azimuthal angle of the stars. The sum is over all stars in the considered region³ of the galaxy. This $m = 2$ mode encodes two relevant quantities, namely the relative bar strength

$$A_2/A_0 = \frac{|A_2|}{\sum_j m_j} \quad (6)$$

³ For example, annular bins or spherical regions of variable size.

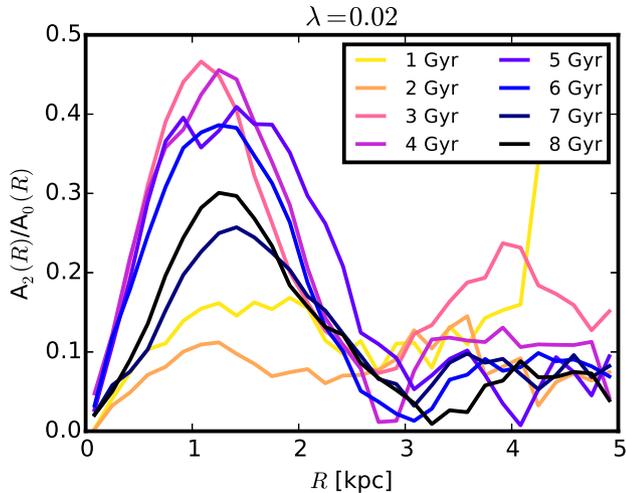


Figure 8. Evolution of the bar strength profile. The plot shows the relative amplitude of the $m = 2$ mode in radial bins of the stars in the simulation at different times. We see that the bar forms after 2–3 Gyr (see also Fig. 7) and that it extends out to 2 kpc.

and the bar’s position angle

$$\theta_2 = \frac{\arg(A_2)}{2} \bmod \frac{2\pi}{2}. \quad (7)$$

In Fig. 7, we present the time evolution of the bar strength in the innermost kpc for a selection of simulations. The lowest spin simulation has the strongest bar. Its bar strength exceeds that of the high-spin simulations for a continuous period of 4 Gyr or more. During this period, its value is remarkably constant.

The only other simulation that exhibits a strong bar is the one with the second lowest initial spin. Thus, the only simulations in our sample with a strong bar are also the only ones that form a Type-III break. This correlation encouraged us to search for a possible dynamical link between bars and Type-III breaks in our simulations.

Fig. 8 shows the relative bar strength in different radial bins at different output times for the $\lambda = 0.02$ galaxy. The size of the bar does not evolve significantly. It ends at 2–3 kpc, so it makes sense to look for possible effects on star particles inside that region.

The pattern speed of the bar is the time derivative of the bar’s position angle. Fig. 9 presents the pattern speed of the bar in the low-spin ($\lambda = 0.02$) simulation as a function of time. Once the bar has formed, its pattern speed is remarkably constant, which will be important when we discuss the interaction of stellar particles and the bar in Section 4.4.

To summarize, low angular momentum simulations develop strong and long-lived bars that have a stable pattern speed over a number of Gyrs. When the bar forms, it may trap particles at its resonances. These stars are expected to oscillate radially (SB02) but stay bound to the bar. Note, that such strong bars are known to cause considerable heating of stellar orbits (Hohl 1971).

4.4 Orbit migration from star–bar interaction

In the top row of Fig. 10, we show the current position of the star particle from Fig. 6 during one direct interaction with the bar that significantly increased its binding energy e and apocentre.

The panels in the top row of the figure show that the star and the bar have the same sense of rotation and that the azimuthal phase of

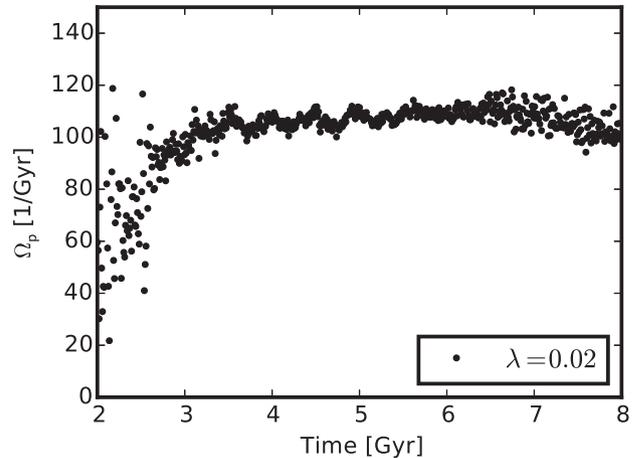


Figure 9. Bar pattern speed evolution in the low-spin simulation. The figure shows the bar pattern speed of the $\lambda = 0.02$ simulation as a function of time. Before its formation (≈ 3 Gyr, see Fig. 7), it is not well defined but later on it is constant.

the star lags behind that of the bar. During the period that is shown in these images, the star gains a significant amount of binding energy e (bottom right panel). The slope of the star’s trajectory in the Lindblad diagram (bottom left panel) is remarkably similar to Ω_p , particularly for $4.721 < t/1 \text{ Gyr} < 4.734$, which is the time period in which the time evolution of the binding energy e is the strongest. According to equation (2), this is the trajectory we expect from the interaction of a star with the bar, given its constant pattern speed. Taking into account that the orbital binding energy only changes in the vicinity of the bar (see Fig. 6), we interpret this as a clear signature of the bar as the dominant driver of the star’s energy gains (losses).

The encounter of the star and the bar are analogous to a *swing-by*. The star is exposed to an extended period of acceleration due to the moving potential well of the bar – it is *surfing* in the bar’s potential.

So far we investigated the behaviour of a single star. However, finding a mechanism that drives a single star’s migration out into the outer disc does not explain the existence of the outer disc. In order to show that the behaviour of that star is typical, we will show that there is a prominent signature of the bar in the outer disc stars’ orbit evolution.⁴ We will use equation (2) that implies that the ratio of Δe and Δj_z equals the bar’s pattern speed Ω_p .

Fig. 11 shows the normalized mass-weighted distribution of $\Delta e/\Delta j_z$ of stars in the $\lambda = 0.02$ simulation. It covers the time range from 4.0 to 5.4 Gyr when the bar was both, strong and had a constant pattern speed. The black histogram considers stars that are located outside the break radius at 5.4 Gyr into the simulation. The break radius at this time was $R_{\text{break}, 5.4 \text{ Gyr}} = 7.6 \text{ kpc}$. The grey histogram shows the same for all stars in the simulation that were born before 4.0 Gyr. Stars now outside the profile break show a clear peak in their orbit evolution of $\Delta e/\Delta j_z$ which coincides remarkably well with the bar’s pattern speed Ω_p (vertical lines). There is a small feature in the global distribution (grey) but it is offset from Ω_p and much less prominent. Given the constant pattern speed of the bar, this agreement for the stars in the outskirts matches the prediction of equation (2) for the imprint of the bar on stellar orbits. Thus, it

⁴ This signature can also be caused by different non-axisymmetric perturbations that are rotating with the same pattern speed. However, the only such perturbation that was found in the simulation is the bar.

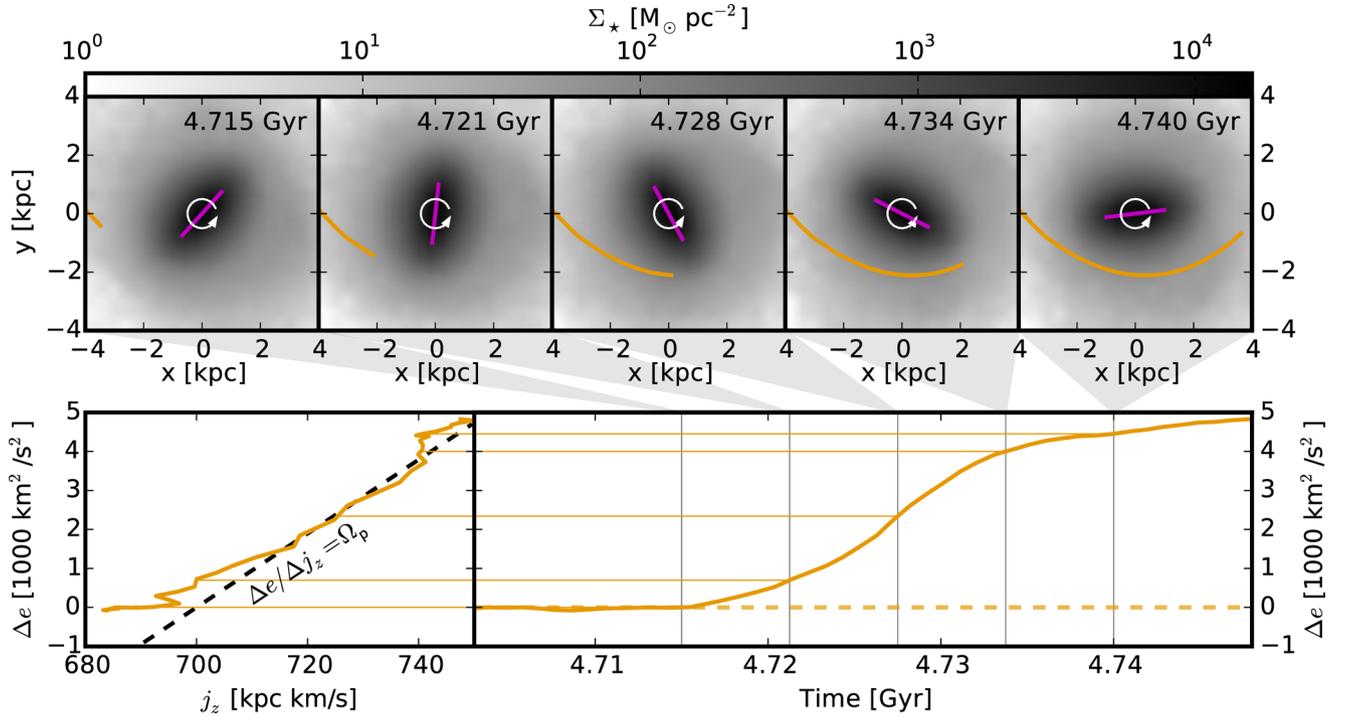


Figure 10. The panels in the top row show the trajectory of an individual star in the low-spin simulation during one pericentre passage. The stellar surface density is projected as a grey-scale in logarithmic scale. The bar’s position is indicated by the magenta line. Its sense of rotation is indicated by the white arrow. The star is the same as in Fig. 6. The bottom left panel shows the star’s trajectory in the Lindblad diagram. The slope of the dashed line in the bottom left panel is the bar’s pattern speed Ω_p indicating the trajectories of constant Jacobi energy. The bottom right panel shows its relative binding energy e as a function of time. The binding energy is given relative to its value before the encounter which is indicated by the orange dashed line. The corresponding time of each panel in the top row is indicated by a vertical line in the bottom right panel. The figure shows that significant evolution of the star’s orbital energy occurs during pericentre passage. Its trajectory in the Lindblad diagram is consistent with a constant Jacobi energy during pericentre. This indicates that the bar-induced potential perturbation is responsible for the energy gain.

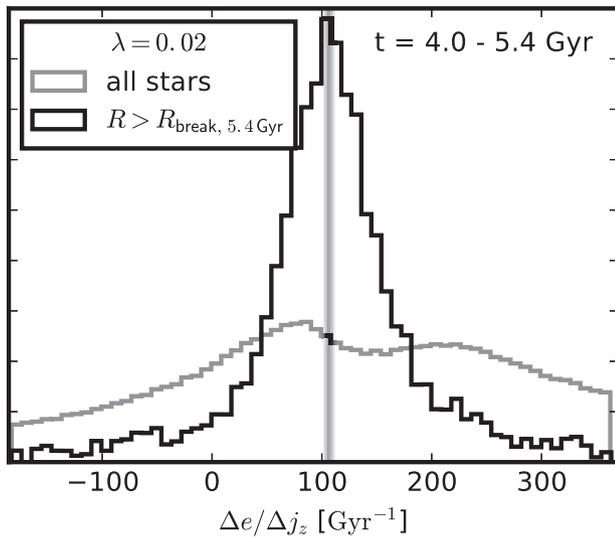


Figure 11. Mass-weighted distribution of $\Delta e/\Delta j_z$ of stars located outside the break radius at 5.4 Gyr (black) and all stars (grey) of the lowest spin ($\lambda = 0.02$) simulation. The time range (4.0–5.4 Gyr) was chosen to coincide with the times where the bar strength is at its peak value and its pattern speed is approximately constant simultaneously (see Figs 7 and 9). The vertical lines indicate the measured values of the bar pattern speed that occurred in the respective time span. It coincides remarkably well with the peak of the distribution for the outer disc stars. The peak is not present in the global distribution.

suggests that the bar is the dominant driver of the outward migration happening in the simulations.

5 ‘SURFING THE BAR’ IN A TOY MODEL

5.1 Motivation for a toy model

We created a very simple toy model to illustrate that our proposed mechanism (see Section 4.4) is indeed capable of increasing the semimajor axes of stellar orbits. Here, the only asymmetry will be a bar-like, rotating, non-axisymmetric perturbation in an otherwise axisymmetric potential. Its purpose is to support our interpretation from Section 4. We will show that the interactions of test particles with a bar-like perturbation can reproduce the qualitative behaviour of stellar particles in the outer disc of the simulation. Thus, other effects are not necessary to qualitatively reproduce the kinematics of outer disc stars. This supports our result that the bar is the main driver in the formation of Type-III disc profiles.

5.2 The time-dependent potential

In this model, test particles move in an NFW potential

$$\Phi_0(|\mathbf{r}|) = \Phi_{\min} \frac{\ln(1 + |\mathbf{r}|/r_s)}{|\mathbf{r}|/r_s} \quad (8)$$

Table 1. Toy model parameters. N is the number of test particles and ϵ_{init} their initial orbit eccentricity. R_{exp} is the scalelength of the initial exponential surface density profile. All other quantities correspond to those in equations (8)–(10).

	Units	Model Weak	Strong
f		0.01	0.05
Φ_{min}	[km ² s ⁻²]	-3×10^5	
r_s	[kpc]	10	
σ_x	[kpc]	2	
σ_y	[kpc]	$\sqrt{2}$	
Ω_p	[rad Gyr ⁻¹]	100	
φ_0	[rad]	Random	
$R_{\text{exp, init}}$	[kpc]	1	
ϵ_{init}		0	
N		10^5	
t_{final}	[Gyr]	4	

with a rotating non-axisymmetric Gaussian perturbation

$$\Phi_p(\mathbf{r}, t) = f \Phi_{\text{min}} \exp \left[-0.5 \left(\frac{x'(t)^2}{\sigma_x^2} + \frac{y'(t)^2}{\sigma_y^2} \right) \right] \quad (9)$$

in the centre, where

$$\begin{pmatrix} x' \\ y' \end{pmatrix} (t) = R(-\Omega_p t - \varphi_0) \begin{pmatrix} x \\ y \end{pmatrix}. \quad (10)$$

In the above equations, Φ_{min} is the minimum unperturbed potential, r_s the scale radius of the NFW potential, f the relative strength of the perturbation, $\sigma_{x,y}$ the extent of the perturbation in x and y direction,⁵ $R(\varphi)$ the rotation matrix for rotation by an angle φ , Ω_p the perturbation's pattern speed and φ_0 the initial phase of the perturbation's position angle. The total potential then is

$$\Phi(\mathbf{r}, t) = \Phi_0(|\mathbf{r}|) + \Phi_p(\mathbf{r}, t). \quad (11)$$

This yields a static NFW potential superimposed with a 2D-Gaussian perturbation that is rotating with an angular speed of Ω_p in the positive sense of rotation. Note, that the particles in this model are *not* self-gravitating.

5.3 Mass redistribution in the toy model

In this section, we describe technical details of our toy model that are necessary for reproducing the results.

We apply this potential to an initially exponential surface density profile with two different perturbation strengths: $f = 0.01, 0.05$. We refer to them as the *weak* and *strong* models, respectively. The values of the model parameters are given in Table 1. The initial velocities have been set such that the orbits would be circular in the azimuthally averaged potential.

We evolved the test particles' coordinates with a Leap-Frog integration scheme. We used a time step of 10^{-3} kpc s km⁻¹ $\approx 10^{-3}$ Gyr. The relative error of the Jacobi-integral is of order $\mathcal{O}(10^{-4})$ except for a few particles with very small initial radii ($\lesssim 0.02$ kpc). We restricted the treatment to the x - y plane for simplicity.

In principle this setup is overly simplistic. We model a disc with particles on perfectly circular orbits and expose it to a bar perturbation that grows instantly. This is problematic for two reasons: (i) Circular orbits experience the stronger interactions with

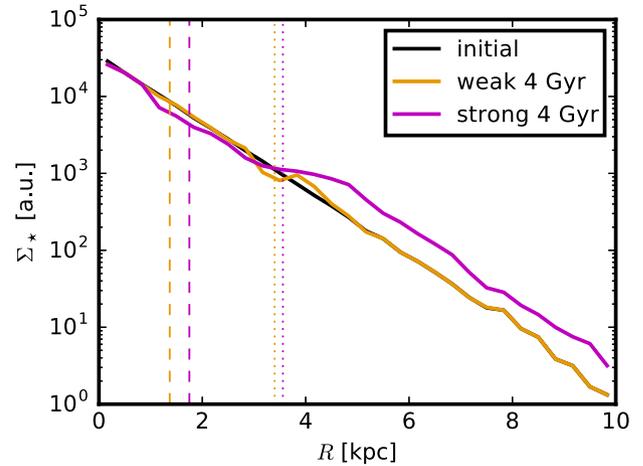


Figure 12. The surface density profiles after 4 Gyr for the weak (orange) and strong (magenta) models compared to the initial profiles (black). Where the black line is not visible, it is hidden behind the orange line. The dashed and dotted vertical lines represent the location of the CR and OLR, respectively. While the strong model shows a dip at CR and an excess of particles outside of the OLR, the profile of the weak model remains mostly unchanged except for a small wiggle at the OLR.

non-axisymmetric perturbations than (mildly) eccentric orbits and hence, the amount of migration is likely to be overestimated in our simplistic setup (Sellwood & Binney 2002; Solway et al. 2012; Vera-Ciro et al. 2014); (ii) the instant growth of the bar causes the equilibrium system to be in a non-equilibrium state that will have to equilibrate again.

We performed tests about the effects of both of these problems. (i) We added a velocity perturbation on top of the initially circular orbit that has a random direction and the magnitude of the perturbation is drawn from a normal distribution with a standard deviation of 5 per cent of the value of the circular velocity of the respective particle. (ii) We linearly grew f in time from 0 to its final value with different growth rates. The duration of the bar-growth phase ranges from 0.5 to 5 Gyr. Neither of these tests had any measurable effect on the results of the model.

In Fig. 12, we compare the evolved surface density profile of the weak (orange) and the strong (magenta) model to the initial (black) profile. In the weak case, there is no significant evolution of the surface density profile. There is merely a small feature at the location of the OLR (3.4 kpc). This is consistent with the results of SB02.

The profile of the strong model has a dip at the position of the CR and just inside the OLR as well as an excess outside the OLR. This indicates that there is significant outward migration from CR and OLR. Note that the determination of the position of the CR and OLR is somewhat dubious because it is based on the existence of nearly circular orbits. In a strict sense, such orbits cannot exist in a non-axisymmetric potential. When we calculate the location of the resonances, we use the azimuthally averaged potential. We show later (Fig. 13) that the resulting resonances agree well with major changes in particles' angular momentum.

Fig. 12 demonstrates that a strong bar can cause a mass excess at large radii. However, the model does not reproduce a Type-III profile as in the simulations. In this toy model, the profile looks more like a Type-II.o-OLR profile with a bump that can be associated with the OLR of the bar (Erwin et al. 2008; Gutiérrez et al. 2011). The mass deficiency inside the OLR compared to the Type-III disc profiles in the simulations may be due to the simplistic setup of this model.

⁵ Note that non-axisymmetry requires $\sigma_x \neq \sigma_y$.

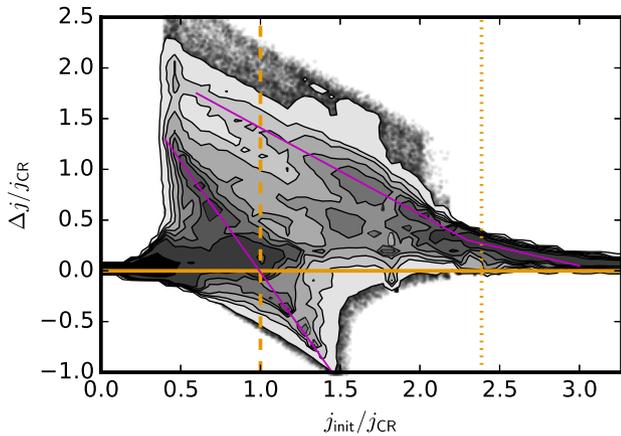


Figure 13. The change in specific angular momentum j of the test particles in the strong model after 4 Gyr as a function of their initial specific angular momentum. The horizontal solid line indicates the locus of zero change in j . It separates outward migration ($\Delta j > 0$) from inward migration ($\Delta j < 0$). The dashed and dotted vertical lines indicate the values of j that correspond to the CR and OLR, respectively. The two most prominent features are highlighted by the magenta lines.

Due to the lack of self-gravity of the particles, inward migration is likely to be underestimated in this model. Furthermore, we do not model star formation processes here, which are still going on in a real disc and are strongest in the centre.

We now explore where these excess particles in the strong model come from. Fig. 13 shows the change of specific angular momentum of each test particle in the strong model as a function of its initial specific angular momentum. There is a strong feature that intersects $\Delta j = 0$ at the CR. A second strong feature corresponds to the OLR but does not intersect $\Delta j = 0$. Generally there is only moderate inward migration ($\Delta j < 0$). This can be associated with the CR. Since we can associate the two main features with the resonances we conclude that they are the main drivers of the outward migration. It is not obvious from this figure which of the resonances is dominant.

To determine which of the resonances is dominant, we perform a modified resimulation of the strong model. We change the initial radial distribution of test particles to be a normal distribution centred around the two resonances, CR and OLR with a standard deviation of 0.2 kpc. We sampled 10^5 particles in each case. All other parameters are identical to those given in Table 1.

Fig. 14 shows histograms of the last peri- (top panel) and the last apocentre distance (bottom) of the test particles. The thick orange and black histograms correspond to the particles centred around the CR and OLR, respectively. The thin histograms show the distribution of the corresponding initial radii. The figure shows that the pericentre positions of the particles do not significantly differ from the particles' initial radii. A large fraction of the particles' apocentre distances, however, evolve to quite large values.

At intermediate radii (4–6 kpc), particles initially at the OLR outnumber the particles initially at CR. This excess is however biased as the particle density at the OLR and CR are the same in our toy model. In real galaxies, however, the particle density decreases with radius. For realistic values of the disc scalelength, the particle density at the OLR is overestimated by no more than a factor of 3. Thus, correcting for this the particles in resonance with the OLR will still dominate over those from the CR at these radii. At larger radii, the distribution of the last apocentre distances is clearly dominated by particles originating from the CR. We conclude that the excess of particles in the outer disc is caused by particles in resonance with

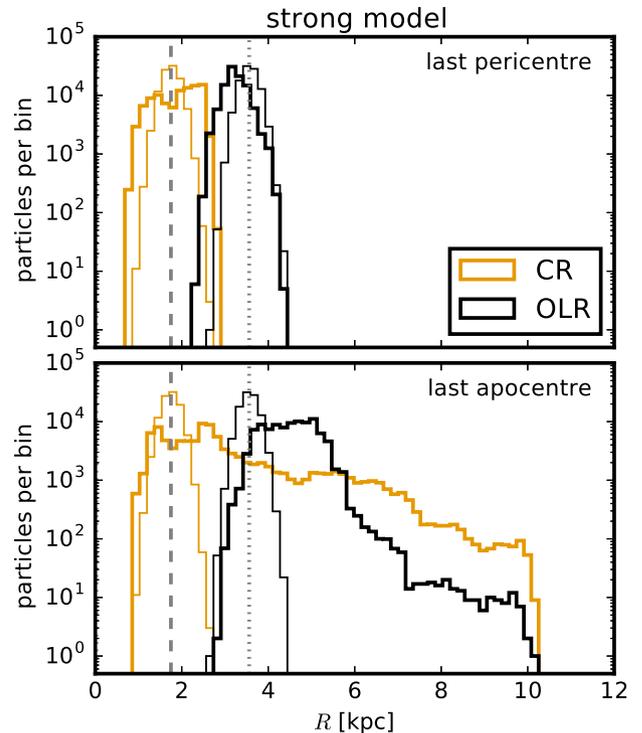


Figure 14. The distribution of last peri- (top panel) and apocentres (bottom) for the strong model. The thin histograms show the initial radial distribution of particles on a circular orbit centred around the CR (orange) and the OLR (black). The corresponding thick histograms show the respective distribution of the particles' last peri- (top) and apocentre (bottom). For a significant fraction of the particles, the apocentre is much larger than the pericentre indicating significant radial heating. At intermediate radii (4–6 kpc), the heating is dominated by the OLR, at larger radii by the CR.

the CR and the OLR. However, the CR is more efficient at scattering particles to very large radii.

Fig. 14 also shows that a lot of particles of the strong simulation that are in CR with the perturbation have apocentre distances that are much larger than their pericentres. This means that they experience severe radial heating indicating that the approximation of SB02 (equation 3) breaks down for such a strong perturbation. This is also evident in the altered radial surface density profile (Fig. 12). SB02 showed that migrating particles in resonance with a weak perturbation exchange orbits with another particle resulting in an unchanged global profile. In the case of our toy models, only the weak case seems to agree with this result of SB02.

We note that in our idealized toy model all the orbits stay bound to the region of the perturbation. As long as the perturbation persists, they may also return to their original orbit. In fact, the radial position of the particles shows a beat pattern. These are however not synchronous among the different particles such that the global radial distribution of the particles will eventually reach an equilibrium distribution. It takes about a Hubble time for such an equilibrium distribution to be reached in our toy model.

In the simulations, the scattered outer disc stars also stay bound to the bar (top panel in Fig. 6). The situation in the simulations is more complex though, e.g. the angular momentum changes even when the stars are far away from the bar region. As a result the star particles' orbits do not show a clear beat pattern. A consequence is that the star's usually never return to their birth orbit.

5.4 Toy model summary

We demonstrate here that a strong, non-axisymmetric, steady and rotating perturbation can cause significant radial heating at the CR. As a consequence, the radial density profile of a disc can change significantly for such a strong perturbation. This is in qualitative agreement with the properties of the low-spin simulation ($\lambda = 0.02$) we analysed in Section 4. For the weak model, there is no significant change in the radial profile and only very little heating, even at the OLR. In this case, the approximation of no radial heating at the CR holds and it agrees well with the results of SB02.

Since we treat particles as test particles and ignore their self-gravity, our toy model is not self-consistent. Due to the way we set up the potential perturbation, the additional potential well of the perturbation at the OLR is shallower than that at the CR. This may limit the extent of radial heating caused by the OLR and thus it is most likely underestimated.

Despite the possible underestimation of radial heating by the OLR, we have shown here that particles in CR or OLR with a strong rotating perturbation in the centre experience significant radial heating. It is strong enough to alter the radial surface density profile of an initially exponential disc. This is incompatible with the results of SB02 for weak perturbations that do not significantly alter the global profile of their simulated discs.

In our case of a strong bar, however, we violate the approximation of a weak perturbation (SB02). Hence, the result that particles in CR do not experience radial heating no longer holds. This approximation was based on the fact that at the CR the slope of the trajectory in the Lindblad diagram is equal to that of the circular velocity curve (fig. 1 in SB02). If the change in angular momentum due to the interaction with the perturbation is strong enough, the particle may depart from the circular velocity curve (or increase its distance to that). This results in radial heating and appears to be what happens in our strong model and in our simulations that produce Type-III disc breaks, given that these are the simulated galaxies with strong bars (Fig. 7).

Due to the lack of self-consistency and the non-axisymmetric external potential, global angular momentum of the test particles is not necessarily conserved (see Fig. 13). This may lead to an underestimation of inward migration in the toy model and might be the reason for the mass deficiency in the central regions of this toy model. The model does still demonstrate the capability of such a perturbation to alter the global mass distribution of a stellar disc.

6 OBSERVATIONAL SIGNATURES

In this section, we will give some observational signatures of the mechanism that we described above. We will compare the disc dynamics of a simulated Type-III disc (low-spin, $\lambda = 0.02$) and a Type-II disc (high-spin, $\lambda = 0.06$).

We have shown that the eccentricity distribution of the outer discs in the simulations with Type-II and Type-III disc breaks is significantly different (cf. Section 4.1). This leads to distinct dynamical properties of the discs that can be observed.

The upper panel of Fig. 15 shows the mean tangential velocity profile $\langle v_\phi \rangle(R)$ of the stellar discs (dashed lines) for the low-spin ($\lambda = 0.02$) and high-spin ($\lambda = 0.06$) galaxies. They are compared to the expected tangential velocities for circular orbits (solid lines). As the stellar discs host stars on non-circular orbits, we expect the mean tangential velocity to be smaller than the circular velocity as stars at apocentre have low velocities. The effect is much stronger for the low-spin galaxy that exhibits a discrepancy by a factor of 4 in

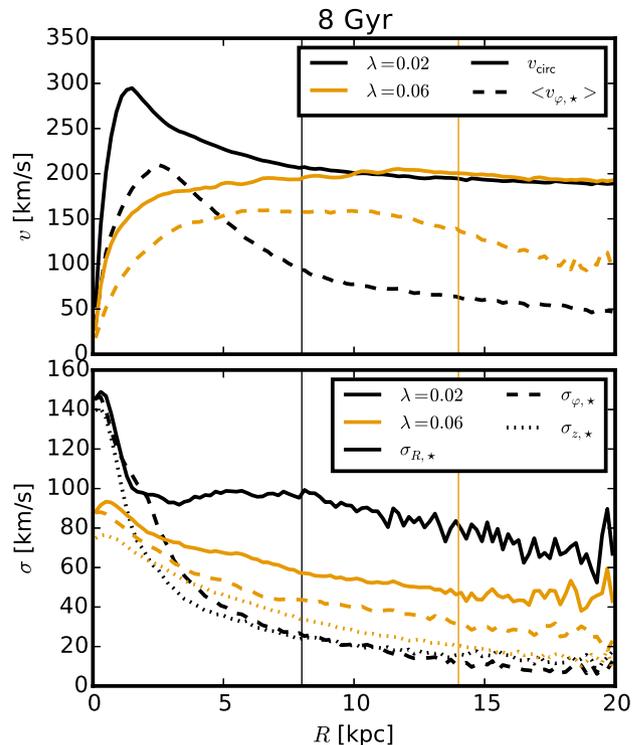


Figure 15. Rotation velocity and velocity dispersion profiles. The upper panel shows the mean tangential velocity of stars (dashed lines) in annular bins and the circular velocity curve (solid lines). The lower panel shows the velocity dispersion in radial (solid), tangential (dashed) and vertical (dotted) direction. The vertical lines indicate the location of the breaks.

the entire outer disc. For the high-spin galaxy, the mean tangential velocity is only off by a factor of up to 2. This trend of decreasing tangential velocities in the outer discs with decreasing spin is expected as the distribution of circularity parameters shifts towards more eccentric orbits for the low-spin simulations.

The difference between the tangential velocity profile and the circular velocity curve is difficult to observe, as the circular velocity curve cannot be observed easily. A better diagnostic for both types of disc breaks (Type-II and Type-III) is the velocity dispersion profile as these can be observed. The velocity dispersion profiles in each direction are presented in the lower panel of Fig. 15. The prominent difference between both simulations is that the radial velocity dispersion in the $\lambda = 0.02$ (Type-III profile) disc is much higher than the tangential and vertical component. This is a signature of the large amount of eccentric orbits in these discs. In the disc with a Type-II break, all velocity dispersion components are comparable as it hosts a much smaller number of stars on eccentric orbits.

The resulting Type-III disc is dynamically peculiar. While it has as disc shape (Fig. 1), it is very slowly rotating and has an excess in radial velocity dispersion and, thus, the rotational contribution to support the disc is unusually small.

Observing these signatures is challenging as the outskirts of Type-III discs are very faint (>27 mag arcsec $^{-2}$). Thus, they are not observable through stellar absorption-line spectroscopy, even with integral field spectroscopy. A possible way to measure the kinematics of the outskirts of such discs would be to observe planetary nebulae. Planetary nebulae have been used previously to measure velocity dispersions of galaxies at very low surface brightness (e.g. Douglas et al. 2000; Herrmann & Ciardullo 2009) and, thus, would provide

a possible tool to observe an excess of radial velocity dispersion, the smoking gun of stars surfing in the bar's potential.

7 DISCUSSION

We have presented a thorough analysis of stellar orbit evolution in one of the simulated discs of [paper I](#) with a Type-III break. The goal was to identify a mechanism that produces Type-III breaks via secular evolution. We chose a simple simulation set-up of disc formation within non-cosmological isolated haloes to have full control over the halo spin and to facilitate the identification of secular, i.e. internal, mechanisms.

We showed that the stars that make up the outer parts of these Type-III discs were born on circular orbits well inside the final break radius (Fig. 3 and [paper I](#)). Furthermore, the stars in the outer parts of these discs have very eccentric orbits. Therefore, the mechanism that produces Type-III discs is inconsistent with that found by Roškar et al. (2008). They found that the stars that populate the truncated region of Type-II discs have been churned there from their birth radii while retaining near-circular orbits. Instead, there has to be a mechanism that is able to drive stars to larger radii and that can turn those stars' orbits from circular to eccentric in our low-spin simulations.

We investigated the bar as a potential cause for the formation of Type-III profiles because the two simulations that form Type-III discs have significantly stronger bars than all other simulations of our sample (Fig. 7). We find that the increase of orbital radii (or more accurately their semimajor axes) is driven by an increase in orbital energy (Fig. 6) which, in turn, is driven by encounters of the stars with the bar potential at their pericentres. Our main argument for the bar as the dominant cause is the fact that the ensemble of orbits of stars, that make up the outer disc, shows a clear signature of the bar: the distribution of the ratio $\Delta e/\Delta j_z$ peaks at the value of the bar's pattern speed (Fig. 11). This is a clear signature that is expected from a rotating bar [equation (2), see also [SB02](#)], with a constant pattern speed (Fig. 9).

Roškar et al. (2008) found that radial migration in simulated galaxies with Type-II breaks is dominated by churning of stars on near-circular orbits. This preserves the stars' circularity and thus does not cause significant radial heating. We found those results to be consistent with our simulations with Type-II profiles. In our low-spin galaxies, which feature strong bars, the stars in CR with the bar may experience radial heating. This is possible because the churning mechanism is based on a first-order approximation for moderate perturbations which states that stars in CR do not experience radial heating. This first-order approximation breaks down for the strong bars in our simulations. Here, the stars may be driven away from the circular orbit curve while in CR with the bar. This effect of bars has been known for decades (Hohl 1971) but has never been linked to the formation of Type-III stellar disc profiles.

We confirmed our interpretation of the simulations with the help of a simple toy model that qualitatively mimics the situation in the simulations. We showed that a strong bar-like perturbation may scatter stars to large radii in a very similar fashion as the bar in our low-spin simulations. An excess of stars at large radii could be reproduced in this model with a strong perturbation but not in a model with a weaker perturbation (Fig. 12) which is in qualitative agreement with the results from our simulations. However, the detailed shape of the final profile in the toy model does not feature at Type-III break which is due to the lack of modelling the full complexity of galaxy evolution.

As of now the literature only provided models that associate environmental effects (satellites, accretion) with the formation of Type-III discs. As this work presents a mechanism that is capable of producing these discs in simulations of isolated galaxies, we show that galaxies can form Type-III discs purely via secular evolution. This does not preclude that external forces (Younger et al. 2007; Kazantzidis et al. 2009; Roediger et al. 2012; Borlaff et al. 2014) or other internal processes may also play a role.

We find that the initial halo spin matters as it locally sets the rate at which stars form. This in turn determines the size of the stellar disc and its central surface density. Hence, it also sets the strength and longevity of any bar at the centre. This effect cannot be explored in simulations with prepared discs (e.g. Foyle et al. 2008). For high-spin parameters, the gaseous disc is very extended but the gas surface density is comparatively low. This leads to more extended star formation at a rather low rate. In low-spin haloes, the opposite happens. Due to the large amount of low angular momentum gas, a large portion of this gas is able to settle at low radii forming a concentrated massive gas disc with a high star formation rate. In this case, a massive and concentrated disc forms which is highly susceptible to disc instabilities and thus very prone to bar formation (Toomre 1964; Hohl 1971). Since the stellar mass density in the centre is very large, the bar is also very massive. As we have shown in this work, this massive bar is driving the formation of Type-III discs.

We previously reported a correlation between disc scalelength and the type of truncation (middle panel of fig. 2 in [paper I](#)), i.e. the inner scalelengths increase from compact discs for Type-III profiles through intermediate scalelengths for Type-I profiles and extended discs for Type-II profiles. While Maltby et al. (2012a) and Head et al. (2015) do not find such a correlation in their galaxy samples, Gutiérrez et al. (2011, section 5.2) report a trend that qualitatively agrees with our simulations ([paper I](#)). Gutiérrez et al. (2011) cannot rule out a common distribution for the inner scalelengths of Type-I and Type-II discs but find that Type-III discs have significantly shorter inner scalelengths compared to pure exponentials. Despite this qualitative agreement between a subset of observational data and our simulated galaxies, it is not the goal of this project to reproduce previous observational results but to take a first step to a possible explanation of the formation of Type-III discs which relies purely on secular stellar dynamics.

We stress that we do not claim the proposed mechanism to be exclusively responsible for the existence of Type-III discs. Instead we show that the proposed mechanism is potentially capable of producing Type-III discs and characterize its dynamical signature that can be used to observationally verify or falsify our model.

The eccentric orbits of the stars in the outskirts of Type-III give rise to very unusual properties of a stellar disc: While being flat the outer disc rotates very slowly and its velocity dispersion is dominated by the radial component.

Minchev et al. (2012) find similar kinematic signatures in Type-III discs that form through external gas accretion. This degeneracy does not undermine the potential capability of falsifying our model if no Type-III discs with bars can be found that have a strong excess in radial velocity dispersion in their outskirts.

We showed that stars in the outskirts of simulated Type-III discs are on very eccentric orbits. They were formed on circular orbits at much smaller galactocentric radii. This outward migration was caused by a strong bar that formed 3–4 Gyr into the simulation and trapped the migrating particles in its rotating potential. This caused a change of the trapped stars' radial distribution which is

responsible for the formation of the antitruncated part of Type-III discs. This conclusion is based on a dominant signature of the bar on stellar orbits. We describe signatures of this mechanism that allow to test our predictions in future observations.

8 CONCLUSION

Analysing controlled disc-galaxy simulations, we showed that strong bars can form antitruncated breaks in the radial surface density profile of stellar discs (Type-III discs). Strong bars can boost the semimajor axis of stellar orbits to very large galactocentric distances, while also changing the distribution of orbit circularity of the affected stars. The initial distribution of stars that later comprise the outskirts of a simulated Type-III stellar disc was initially dominated by near-circular orbits at smaller radii. In the final distribution, near-circular orbits are almost completely absent. It is dominated by very eccentric orbits. This bar-induced transformation of orbits has the capability of changing the global radial mass distribution of the stellar disc ultimately leading to a Type-III break in the radial surface-density profile.

This process is not efficient for discs with weak bars. In this case, the dominant radial migration mechanism is spiral-induced churning and the discs form Type-II breaks in their radial profile. The reason is that the first-order approximation of only very little or no radial heating holds only for weak but not for strong bars.

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