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Total Temperature Measurements of Laminar Gas Flow at Micro-tube Outlet: Cooled from the Wall

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Abstract This paper presents experimental results on heat transfer characteristics of laminar gas flow in a micro-tube with constant wall temperature whose wall temperature is lower than the inlet temperature (cooled case). The experiment was performed for nitrogen gas flow through micro-tubes with 163 and 243 μ m in diameter and 50 mm in length. The gas was heated in an upstream section of the micro-tube to T_{in} =315K, 335K and 355K. The wall temperature was maintained at 305K by circulating water around the micro-tube. The stagnation pressure was chosen in such a way that the exit Mach number ranges from 0.1 to 0.7. The outlet pressure was fixed at the atmospheric condition. The total temperature at the outlet, the inlet stagnation temperature, the mass flow rate and the inlet temperature were measured. The numerical computations based on the Arbitrary – Lagrangian – Eulerian (ALE) method were also performed for the same conditions of the experiment for validation of numerical results. The both results are in excellent agreement. The total and bulk temperatures obtained by the present study are also compared with the temperature of the incompressible flow.

Keywords: Total temperature, Micro gas flow, Experimental heat transfer

1. Introduction

During the last two decades, flow and heat transfer through micro-geometrics have attracted an important research interest in micro-heat exchanger, micro-reactor and many other micro-thermal fluid devices. In the case of the gas flows in the micro-systems, it is found that the flow accelerates due to the gas expansion and thermal energy converts to kinetic energy. This results in a static temperature decrease of the gas [1].

Since the experimental work by Wu and who measured the friction Little [2], coefficient and Nusselt number for nitrogen, argon, and helium flows in silicon or glass experimental micro-channels, many numerical investigations have been undertaken. However, there seems to be few experimental investigations on the heat transfer compressible flow gas through geometries.

Asako [3], Asako and Toriyama [4] and Hong and Asako [5] performed numerical

investigations to obtain the heat transfer characteristics of laminar gaseous flows in a micro-channel and in a micro-tube with temperature, whose constant wall temperature is lower or higher than the inlet In the case of slow flow temperature. (Ma<0.3), identical heat transfer coefficients are obtained for both heated and cooled cases of incompressible flow. However, in the case of fast flow (Ma>0.3), different heat transfer coefficients are obtained for each cooled and heated case. The correlation for the prediction of the heat transfer rate of gaseous flow in a micro-channel and in a micro-tube In order to validate has been proposed. numerical results by their studies [3-5], Hong et al. [6] measured total temperatures at a with micro-tube outlet constant temperature whose temperature is higher than the inlet temperature (heated case) in the laminar flow regime.

Turner et al. [7] performed experimental investigation to measure the inlet and outlet temperatures and the micro-channel wall temperature in thermal boundary conditions of

constant temperature gradient along the microchannel length. Their measurement results were used to validate a two dimension numerical model for gaseous flow in a microchannel.

As can be seen from the literature survey, there seems to be no experimental study on laminar heat transfer characteristics of microtubes with constant wall temperature whose temperature is lower than the inlet temperature (cooled case). This is the motivation of the present experimental study to measure the total temperature at the micro-tube outlet, the inlet stagnation temperature, the mass flow rate, and the inlet pressure to determine quantitatively transferred amount of heat in a micro-tube with constant wall temperature.

2. Experimental setup

schematic representation the experimental setup used in the present study is shown in Fig. 1. The experiment was conducted with pressurized Nitrogen. Nitrogen from the tank passes through the regulator, the gas dryer and the mass flow meter (Kofloc 3300) which measures the mass flow rate. Then the gas flows into the heat transfer section and flows out to atmosphere. The gas flow is controlled by the regulator.

The detailed view of the heat transfer section is shown in Fig. 2. The heat transfer section consists of four components; the inlet section, the micro-tube, the water jacket, and outlet tube. The inlet tube is made of brass with nichrome wire curled around and is attached between the water jacket and the upstream chamber. The inner diameter of inlet tube is 8 mm. The gas was heated by heating the nichrome wire and the brass. The pressure transducer is attached to the upstream

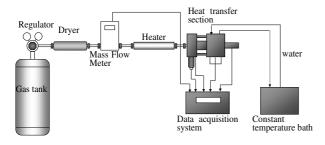


Fig. 1 Schematic of experimental setup

chamber of the inlet section. The thermocouple is inserted into the inlet tube and gas temperature in the inlet section is measured. Silicone RTV is used to seal the connections to prevent the gas leakage. The outlet tube is also made of bakelite and is attached to the water jacket. This is to decrease heat loss and to measure the total temperature accurately. The inner diameter of the outlet tube is 2 mm. The heat transfer section is put on a foamed polystyrene stage to decrease the heat loss from the heat transfer section to the ground.

A SEM picture of the micro-tube cross section for the case of D=163µm is shown in Fig. 3. The micro-tube is made of SUS 304 stainless steel whose outer diameter is 402 µm and inner diameter is 163 µm and the length is 50mm. The wall thickness of micro-tube is The measurement of the inner 119.5 µm. diameter of the micro-tube will be stated later. The micro-tube is placed inside the water jacket to make the wall temperature constant. The water was circulated between the water jacket and a constant temperature bath. water temperature in the water jacket was measured by three thermo-couples. three thermo-couples were type-K sheathed thermo-couples of diameter of 0.5 mm. were set at 5 mm, 22.5 mm and 45 mm from one end of the micro-tube in the axial direction and apart from 1mm in the radial direction.

Pressure transducer (Valcom VESX500G2) was attached to the upstream chamber to measure the inlet pressure of the micro-tube. The temperature of the gas near the inlet and the outlet of the micro-tube were measured as shown in Fig. 2. Then, bare wire type-K thermo-couples of 50 μ m in end-diameter

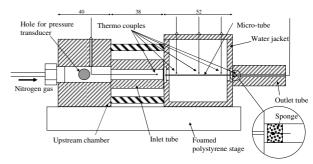


Fig. 2 Detailed view of heat transfer section

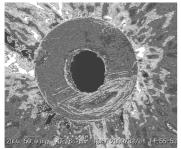


Fig. 3 SEM picture of the micro-tube cross section

Table 1. Measurement uncertainty

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Measurement	Uncertainty					
Pressure transducer	± 0.25 % of FS					
(0-500 kPa)	(1250 Pa)					
Flow meter I	± 0.25 % of FS					
$(0-8.0\times10^{-6} \text{ kg/s})$	$(2.0 \times 10^{-8} \text{ kg/s})$					
Flow meter II	± 0.25 % of FS					
$(0-1.3\times10^{-5} \text{ kg/s})$	$(3.25 \times 10^{-8} \text{ kg/s})$					
Thermocouple	$\pm 0.1 \text{ K}$					
(sheath type-K)						
Thermocouple	$\pm 0.1 \text{ K}$					
(bare wire type-K)						

were used. The uncertainty of the measurement is listed in Table 1.

The correlation between the total temperature and the static temperature is [3]

$$T_{\rm T} = T_{\rm b} + \frac{\int \rho u \frac{u^2}{2} dA}{\int \rho C_{\rm p} u dA}$$
 (1)

where

$$T_{b} = \frac{\int \rho C_{p} u T dA}{\int \rho C_{p} u dA}$$
 (2)

$$T_{T} = \frac{\int \rho C_{p} u T dA + \int \rho u \frac{u^{2}}{2} dA}{\int \rho C_{p} u dA}$$
(3)

Assuming the parabolic velocity profile, Eq. (1) at the outlet is rewritten as

$$T_{\rm T} = T_{\rm b} + \frac{U^2}{C_{\rm a}} \tag{4}$$

where U is the average velocity at a cross section. Note that the kinetic temperature of flow with the parabolic velocity profile can be expressed by the second term of the right hand side of Eq. (4) and it differs from a form for flow with the uniform velocity profile. The

average velocity can be obtained from

$$U = \frac{\dot{m}RT_b}{pA} \tag{5}$$

where A is cross sectional area, p is the average pressure at the cross section, R is gas constant and in is mass flow rate.

Then, Mach number is

$$Ma = \frac{U}{\sqrt{\gamma R T_b}}$$
 (6)

where γ is specific heat ratio.

The cross sectional area ratio of the outlet tube and the micro-tube of D=243 µm is about 70 and the gas slows down in a sponge. sponge in the outlet was attached at the microtube exit. It is made by Polyurethane cylinder of 2 mm in diameter and 4 mm in length. Its coefficient of permeability is 6.4-10 cell/cm. The distance between the thermo-couple and the micro-tube at exit is less than 1 mm. The kinetic energy of the gas would be small enough in the down stream the sponge. Therefore, temperature measured in the outlet tube can be considered as the total temperature. signals from the pressure transducer, the mass flow meter and thermocouples were connected to a data acquisition system (Eto Denki, CADAC21).

2.1 Inner diameter measurements of microtube

The inner diameter of the micro-tube was measured by flowing water in the tube. Details of the measurement are documented in our previous paper [1], and will not be given here. The mass flow rate was measured by measuring the weight of the water over the period of around 300 s. The inner diameter of the micro-tube was obtained by substituting the volumetric flow rate which was calculated from the mass flow rate, into the following equation.

$$\pi D^4 \rho g h - 64 \mu n D \dot{Q} = 128 \mu \ell \dot{Q} + \frac{16}{\pi} \kappa \rho \dot{Q}^2$$
 (7)

Note that Eq. (7) was derived from the assumption of the Hagen-Poiseuille flow. The n and κ in Eq. (7) are the length correction and the kinetic energy correction coefficients and they are n=0.7 and κ =1.12. Measurements

Table 2 Measured tube diameter

Tube	Average	Uncertainty
notation	diameter	(µm)
(μm)	(µm)	•
163	163.21	±0.9 -1.06
243	242.92	$\pm 1.16 - 2.82$

were conducted 6 times in an identical tube. An average of them was regarded as the inner diameter. Then, the measured diameters are tabulated in Table 2. The uncertainty for micro-tubes was also listed in the table.

3. Results and discussions

3.1 Experimental data

The experiments were conducted with two micro-tubes of 163 µm and 243µm in diameter. The temperature of the constant temperature bath was set to 305K and the inlet temperature was set to 315K, 335K and 355K, respectively. Heat transfer tests were conducted for 11 different gas flow conditions of D=163µm and 4 different gas flow conditions of D=243μm each constant temperature respectively. The experimental results for the case of $T_{stg} \approx 315 K$ and $T_w \approx 305 K$ are tabulated When nitrogen temperature in Table 3. ranges from 200K to 350K, the viscosity, μ of nitrogen ranges from 1.260×10^{-5} to 2.000×10^{-5} The change in the value is relatively The value of viscosity at the outlet bulk temperature was used for calculation of the Reynolds number. And, the Mach number at the outlet is obtained from Eq. (6) under the assumptions that the pressure at the outlet of the tube is identical to the ambient Then, the Reynolds number and pressure. outlet Mach number ranged from 520 to 3247 and from 0.145 to 0.734, respectively. As shown in Table 3, the total temperatures at the micro-tube outlet are higher than the wall temperature, although there are no heat sources whose temperature is higher than the wall temperature around the outlet tube. similar results were obtained in our previous numerical studies [5]

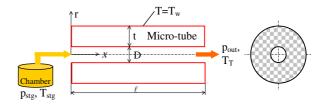


Fig. 4 A schematic diagram of problem

Table 3 Experimental results

#	D	p_{stg}	$T_{\rm w}$	T_{stg}	$T_{T,out}$	Re Ma _o	Ma
	(µm)	(kPa)	(K)	(K)	(K)		IVI a _{out}
1	163	150	305.1	315.5	305.1	520	0.145
2		175	305.0	315.1	305.3	768	0.212
3	_	200	305.0	315.2	305.9	1070	0.291
4		225	305.0	315.0	306.3	1370	0.365
5		250	305.1	315.1	306.8	1670	0.433
6		275	305.0	315.2	307.1	2010	0.505
7		300	305.0	315.1	307.3	2330	0.569
8		325	305.1	315.1	307.4	2620	0.622
9		350	305.0	315.2	307.4	2860	0.664
10		375	305.1	315.1	307.2	3090	0.701
11	_	400	305.1	315.1	306.9	3310	0.734
12	243	150	305.9	315.3	306.7	1299	0.240
13	_	175	305.9	315.3	307.7	1951	0.351
14		200	305.9	315.2	308.5	2596	0.451
15		225	305.9	315.2	309.2	3247	0.543

3.2 Numerical solutions

In order to compare with experimental results, numerical computations based on the Arbitrary-Lagrangian-Eulerian (ALE) method were conducted. The reason we choose ALE method is that it is very stable for the computation of the high speed compressible flow. The problem is modeled as a microtube with the wall thickness, t, its thermal conductivity, λ , and constant wall temperature, T_w at the outer surface of the tube as shown in A chamber at the stagnation Fig. 4. temperature, T_{stg}, and pressure, p_{stg}, is attached to its upstream section. The governing equations are identical to those documented in our previous works [4, 5] except the heat conduction in the wall. Then, the governing equations are not given here. In the present study, Knudsen number (Kn=σ/D_h, ratio of the gas mean free path to the characteristic length) that determines the degree of appropriateness of the continuum model is 4.2×10^{-4} for D=163µm under atmospheric pressure and room temperature. Therefore, the slip on the

wall is assumed to be negligible. The computations were performed for 9 cases (6 cases for $D_i=163\mu m$ and $D_o=402\mu m$ and 3 cases for D_i=243µm and D_o=426µm) for each wall temperature with axisymmetric conditions, respectively. The computational conditions and tube dimensions coincide with those of the experiments. The value of viscosity, μ at the outlet bulk temperature of the experiment was used for computations. The computational domain is divided into quadrilateral cells: 200 in the x-direction and 20 for the tube and 20 for the wall in the r-direction. Details of the numerical methodology are documented by Amdsen et al. [8] and Hong and Asako [5]. The mass flow rate, Reynolds and Mach number at the outlet numerically obtained well with those obtained coincide experimentally.

3.3 Bulk temperature

Attention will now be turned to the bulk temperature of an incompressible laminar flow. The bulk temperature of an incompressible laminar flow in a duct whose inner wall temperature is T_w is expressed as a function of mean Nusselt number and the location as (e. g., Burmeister [9])

$$T_{h} = T_{w} + (T_{w} - T_{in}) e^{-4Nu_{m}X^{*}}$$
 (8)

where Nu_m is the mean Nusselt number of a simultaneously developing flow in a duct and X^* is the inverse of Graetz number, defined by

$$X^* = \frac{X}{D \text{ Re Pr}}$$
 (9)

Note that Nu_m is also a function of X*. The laminar heat transfer characteristics for duct flows have been investigated by many researchers and Nusselt number are reported in the literature (e. g., Shah et al. [10]). The numerically obtained Nu_m for simultaneously developing flow in tubes by Hwang and cited in Shah et al. [9] was used for the calculation of the static bulk temperature incompressible flow. The calculated bulk temperature is normalized by $T_{w} - T_{in}$ for a tube and is listed in our previous report [3].

The correlation between the total temperature and the static temperature is expressed by Eq. (1). In the experiment, the

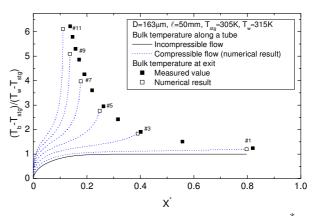
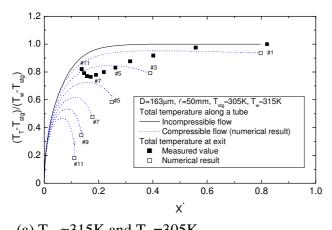


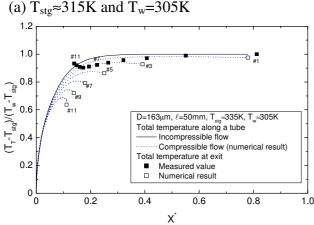
Fig. 5 Bulk temperature as a function of X*.

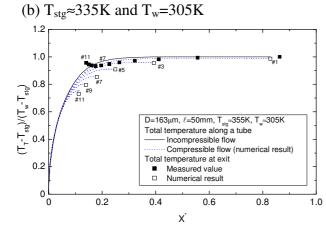
total temperature at the tube outlet and also the flow rate were measured. The pressure at the tube outlet is assumed to be equal to the bulk atmospheric pressure, then, the temperature at the outlet of the micro-tube can be obtained by solving Eqs. (4) and (5). normalized bulk temperature at the outlet of the micro-tube $(T_b - T_{stg})/(T_w - T_{stg})$ T_{in}≈315K are plotted in Fig. 5. The numerically obtained bulk temperature is also plotted in the figure with those of bulk temperature for incompressible flow. bulk temperature for the numerical data and incompressible flow are also normalized as $(T_b - T_{sto})/(T_w - T_{sto})$. In the case of slow (#1 and #2) flow, the numerically obtained normalized bulk temperature increases along the length to the downstream, and levels off it has similar trend that to incompressible flow. On the other hand, in the case of fast flow (#3 to #9), the numerically obtained normalized bulk temperature increases along the length to the downstream, and it takes a value greater than unity near the outlet due to the conversion of the thermal energy into the kinetic energy. The experimental data of the bulk temperature at the outlet of the micro-tube match well with those of numerical results. The qualitatively same tendency was obtained for cases of $T_{stg} \approx 335$ K and 355K. Also, the qualitatively same tendency was obtained for cases of $D=243 \mu m$.

3.4 Total temperature

Attention will now be turned to the total







(c) $T_{stg} \approx 355 K$ and $T_w = 305 K$ Fig. 6 Total temperature as a function of X^*

of the fluid, temperature T_{T} . experimentally measured total temperature for the cases of $T_{stg} \approx 315K$, 335K and 355K are plotted as a function of X* in Figs. 6 (a) to (c) the normalized form of $(T_{\rm T}-T_{\rm sto})/(T_{\rm w}-T_{\rm sto})$ $D=163\mu m$, for respectively. The experimentally measured total temperatures at the outlet of the microtube are also plotted in the figure. numerically obtained total temperature is lower than the bulk temperature of the incompressible flow. A part of the thermal energy converts into kinetic energy near the outlet when the flow is fast (Ma_{out}>0.3). This results in a temperature drop and heat transfer from the wall near the outlet as shown Fig. 5. That is, there exists the heat transfer from the wall due to the temperature drop and it corresponds to the increment of the total temperature. The maximum increment of the total temperature is less than 10% of T_w-T_{stg} in the case of T_{stg} =335K and T_{stg} =355K. In the case of T_{stg} =315 (Fig. 6 (a)), the maximum increment of numerical results reaches 50% of T_w-T_{stg}, however, the maximum increment of the experimental results is half of it. discrepancies Although, there are some between the numerical and experimental data, both data have similar trends, namely, it is obvious that the additional heat transfer from the wall was occurred.

In the case of large temperature difference between the inlet and wall temperature, the heat transfer from the wall due to the temperature drop is not so much. This fact indicates that the heat transfer of gaseous flow in a micro-tube can be predicted from correlation for the incompressible flow in a conventional-sized tube if the temperature difference, T_w-T_{stg}, is greater than 30K. However if the temperature difference, T_w-T_{stg} is less than 30K, the heat transfer from the wall becomes relatively large and the heat transfer for the gaseous flow in a micro-tube cannot be predicted from correlation for the incompressible flow in a conventional-sized tube. As can be seen in Figs. 6 (b) to 6 (c), the values of the normalized total temperature are close to those of incompressible flow with increasing T_w - T_{stg} .

The ratio of the actual recovery and the dynamic temperature is defined as [3, 4 and 5]

Recovery ratio =
$$\frac{T_{T} - T_{b,incomp}}{\int \rho \ u \frac{u^{2}}{2} dA / \int \rho \ C_{p} u dA} (10)$$

where the denominator represents the dynamic temperature, T_k . Note that the temperature difference between the total temperature and the bulk temperature of the incompressible flow represents the recovery temperature.

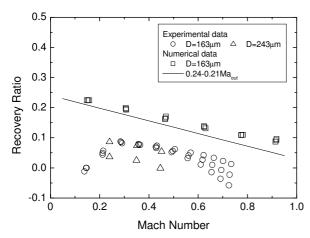


Fig. 7 Recovery ratio as a function of Ma_{out}

Eq. (10) can be rewritten as

$$T_{\rm T} = T_{\rm b,incomp} + \text{Recovery ratio} \times \frac{\int \rho u \frac{u^2}{2} dA}{\int \rho C_{\rm p} u dA}$$
(11)

Then, the total temperature of the gaseous flow in micro-tubes can be predicted from the bulk temperature of the incompressible flow, the recovery ratio and the dynamic temperature. The recovery ratio calculated from Eq. (10) for both experimental and numerical cases of T_{in} =315K, 335K and 355K is plotted in Fig. 7 as the function of the Mach number at the outlet. The numerically obtained recovery ratio is independent of the wall temperature and decreases with increasing the Mach number at the outlet. The solid line in the figure represents the correlation of recovery ratio proposed by Hong and Asako [5] as

Recovery ratio=
$$0.24+0.21$$
Ma_{out} (12)

Eq. (12) is in good agreement with the numerical results. The experimentally obtained recovery ratios depend on the wall temperature. The values of recovery ratio in some high flow cases are negative since total temperature was not accurately measured at the outlet of micro-tubes due to the heat loss into surroundings. However, they have similar trends with Eq. (12).

4. Conclusions

Experimental study to measure the total temperature at the outlet through a micro-tube

with constant wall temperature was performed to determine the quantitatively transferred amount of heat and the local values of the temperature. The following conclusions are reached.

- (1) Heat transfer characteristics of the gaseous flow are different from those of the liquid flow. (2) In the case of fast flow (Ma_{out}>0.3), the total temperature is higher than the bulk temperature of incompressible flow since additional heat transfer from wall to gas occurs due to temperature falls by the thermal energy conversion into kinetic energy near the microtube outlet.
- (3) The bulk temperatures obtained by the present experimental study were compared with numerical results. The results are in excellent agreement with them.
- (4) The total temperature of gaseous flow in a micro-tube to determine the quantitatively transferred amount of heat can be predicted from the bulk temperature of incompressible flow, the recovery ratio and the dynamic temperature.

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