PROPERTIES OF THE IRREGULAR SATELLITE SYSTEM AROUND URANUS INFERRED FROM K2, HERSCHEL AND SPITZER OBSERVATIONS[*]

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(Dated: August 2, 2017)

ABSTRACT

In this paper we present visible range light curves of the irregular Uranian satellites Sycorax, Caliban, Prospero, Ferdinand and Setebos taken with Kepler Space Telescope in the course of the K2 mission. Thermal emission measurements obtained with the Herschel/PACS and Spitzer/MIPS instruments of Sycorax and Caliban were also analysed and used to determine size, albedo and surface characteristics of these bodies. We compare these properties with the rotational and surface characteristics of irregular satellites in other giant planet systems and also with those of main belt and Trojan asteroids and trans-Neptunian objects. Our results indicate that the Uranian irregular satellite system likely went through a more intense collisional evolution than the irregular satellites of Jupiter and Saturn. Surface characteristics of Uranian irregular satellites seems to resemble the Centaurs and trans-Neptunian objects more than irregular satellites around other giant planets, suggesting the existence of a compositional discontinuity in the young Solar system inside the orbit of Uranus.

Keywords: planets and satellites: individual (U XVI Caliban, U XVII Sycorax, U XVIII Prospero, U XIX Setebos, U XXI Trincluo, U XXIV Ferdinand);

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arXiv:1706.06837v2 [astro-ph.EP] 1 Aug 2017

1. INTRODUCTION

Giant planets possess basically two distinct types of satellites concerning orbital dynamics. *Regular* satellites are characterized by orbits with small eccentricity that are very close to the planets' equatorial plane with always prograde orbit within $\sim 0.05\,r_H$, where r_H is the radius of Hill sphere of host planet. In contrast, *irregular* satellites have moderate-to-high eccentricities and inclinations with prograde or retrograde orbits up to $0.65\,r_H$ from their host planets. The existence of two classes of satellites reflects two different ways of evolution: regular satellites likely formed in the same subnebula as the host planet while irregular satellites could not have formed at their present orbits. The most accepted scenario currently is that they have been captured from the inside of the planet's subnebula in the last phase of planet formation on temporarily orbits, then settled through some kind of loss of angular momentum (see Nicholson et al. 2008, for a review).

There were several deep surveys of irregular satellites in the 2000s that established the basis of the currently known set of irregular satellites (Gladman et al. 2000, 2001; Holman et al. 2003; Sheppard et al. 2003a,b, 2005, 2006). These surveys provided the main orbital characteristics of the satellites found and allowed the identification of orbital grouping/families around the specific planets (Nicholson et al. 2008).

Unlike the members of other small body populations in the Solar System, irregular satellites may have remained close to their formation locations and their compositions may be an intermediate one between that of the main belt asteroids and the icy trans-Neptunian objects. The physical characterization of these satellites is, however, still a challenging task due to the large distance and the typical size below $100\,\mathrm{km}$, even in the case of the closest Jovian system. Among these characteristics, light curves provide information on the shape and/or surface albedo variegations and may give hints of the internal structure and strength in the case of fast rotators; the distribution of rotational frequencies and amplitudes are important properties of a small body population (Pravec et al. 2002). High-quality light curve is available for the largest Jovian irregular, Himalia (Pilcher et al. 2012), rotational properties are known for the Jovian satellites Lysithea, Ananke, Carme and Sinope (Luu 1991) and the Cassini spacecraft provided rotation periods for many irregular satellites in the Saturnian system (Denk & Mottola 2013, 2014, 2015). In the Uranian system, Maris et al. (2001, 2007) performed the investigation of the light curves of irregular satellites and obtained rotational characteristics for Sycorax, Caliban, Prospero and Setebos. However, in these latter cases the results are based on sparsely sampled data due to the observing capabilities of the telescopes and the large distance (hence faintness) of these satellites.

Broad-band colors are the most readily available tools that can be used to characterize the surface of the irregular satellites (see Nicholson et al. 2008, and references therein). In the Jovian system the colors are similar to those of carbonaceous asteroids and Jovian Trojans, while in the Saturnian system they show somewhat redder surfaces. However, in both systems the colors are still far from that of the red material typically found in the Kuiper belt. In the Uranian system the colors show a wide variety, but there are certainly satellites that show typical "Kuiper belt" colors (Maris et al. 2001, 2007; Romon et al. 2001; Grav et al. 2004).

Well-established size and albedo values are available for a limited sample only, mainly from data of space probes – e.g. Himalia and Phoebe by Cassini (Porco et al. 2003, 2005), or Nereid by Voyager-2 (Thomas et al. 1991). Recently, thermal emission data obtained with the MIPS camera of the Spitzer Space Telescope (Rieke et al. 2004) and the PACS camera of the Herschel Space Observatory (Poglitsch et al. 2010) also provided independent size and albedo estimates for Sycorax (Lellouch et al. 2013) and Nereid (Kiss et al. 2016).

As we noted above, ground-based observations could not place strong constraints on the rotation of most of the irregular satellites observed earlier. However, it is demonstrated in recent works (Pál et al. 2015, 2016; Szabó et al. 2016, 2017) that data from the extended *Kepler* mission (Howell et al. 2014, K2) can be very effectively used to obtain rotational light curves of Solar system bodies due to uninterrupted photometric time series of several tens of days in length, including main belt and Jovian Trojan asteroids, and trans-Neptunian objects, even at the brightness level of typical irregular satellites. Lately, a thorough light curve analysis of the Neptunian irregular satellite Nereid was also performed (Kiss et al. 2016), showing the great capabilities of K2 measurements for this kind of applications.

In this paper we present the results of Uranian irregular satellite observations performed with the *Kepler* space telescope in Campaign 8 of the K2 mission. We provide light curves and derive rotational characteristics for Sycorax, Caliban, Prospero, Setebos and Ferdinand (Sect. 4). In addition, we use thermal emission measurements of the Spitzer Space Telescope and the Herschel Space Observatory to derive more accurate size and albedo for Sycorax; we also give constraints on the size and albedo of Caliban, Trinculo and Ferdinand (Sect. 3) based on Herschel/PACS observations. Our results are compared with the properties of other irregular satellites and other small body populations of our Solar system (Sects. 5 and 6).

2. OBSERVATIONS

2.1. *Kepler/K2 measurements*

Continuous photometry from the *Kepler* space telescope may provide accurate and unbiased rotation rates and amplitudes for solar system targets. The telescope gathers light in a wide visual band spanning from 420 to 900 nm, and follows a step–and–stare scheme in the K2 mission, observing different fields for up to 80 days along the Ecliptic plane (Howell et al. 2014). *Kepler* ob-

served Uranus and its vicinity during Campaign 8 of the mission for 78.73 days, between 2016 January 4.55 and March 23.28. Apart from the planet, four irregular moons, Caliban, Setebos, Sycorax, and Prospero, were also proposed and selected for observations (GO8039, PI: A. Pál)[1].

We applied the same pipeline for the reduction of the *Kepler* observations that we used in previous works, e.g., to determine the light variations and rotation rates of various Trans-Neptunian Objects, main-belt and Trojan asteroids, or of the moon Nereid (Kiss et al. 2016; Pál et al. 2015, 2016; Szabó et al. 2016, 2017). The method is based on the FITSH[2] software package (Pál 2012): the processing steps are detailed in the previous papers and in the companion paper that describes the light curves of main-belt asteroids drifting though the same image mosaic (Molnár et al. 2017), also providing information on the limitations and capabilities. In short, we created mosaic images from the individual Target Pixel Files (TPFs) which contain the time-series photometric information (time, flux, flux error, background) for each downloaded pixel around a given target, as opposed to light curve files that contain a pipeline-extracted brightness summed in an aperture as a function of time. For more details the reader is directed to Kepler Archive Manual[3]. We then derived the astrometric solutions for the mosaic images, using the USNO-B1.0 catalog (Monet et al. 2003), where the K2 full-frame images from the campaign were exploited as initial hints for the source cross matching. Then, we registered the images into the same reference system, and subtracted a median image from each image. This median image was created from a selection of individual images that did not include the obvious diffractions pattern contamination from Uranus. We then applied aperture photometry at the positions of the satellites. The sharp

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[1] https://keplerscience.arc.nasa.gov/k2-approved-programs.html

[2] http://fitsh.net

[3] https://archive.stsci.edu/kepler/manuals/archive_manual.pdf

images of the stars that were shifted to compensate the attitude changes of the telescope create characteristic residuals in the differential images that may contaminate our photometry. Therefore we filtered out the epochs when the scatter of the background pixels in the photometric annulus was high. The per-cadence photometric uncertainty values were derived from the shot noise of Kepler and from the estimated background noise.

All observations were collected in long cadence mode, with a sampling of 29.4 min. Three of the proposed satellites fell into, or near the large mosaic that also covered the apparent motion of Uranus (Fig. 1). Other satellites were also present in the same mosaic, and we successfully detected the light variations of a fourth one, Ferdinand.

Prospero fell onto an adjacent CCD module, and its motion was covered with a narrow band of pixels. In that case we collected the Target Pixel Files of nearby, unrelated targets into a small mosaic around the track of Prospero in order to have a good astrometric solution. The log of observations is summarized in Table 1. The duty cycle there shows the ratio of accepted photometric data points to the number of cadences when the satellites were present on the images. We note that Ferdinand was observed twice, at the beginning and the end of the campaign: the two rows in the table refer to the entire length of the observation and the sections when Ferdinand was on the Kepler CCD array, respectively. The temporal distribution of data points we used for photometry is presented in Fig. 2. We also checked other satellites that fell on the CCD array, e.g., Stephano (24.5 mag) or Trinculo (25.5 mag), but found no meaningful signals in their photometry.

2.2. *Infrared data*

2.2.1. *Sycorax*

Sycorax was observed with the MIPS camera of the Spitzer Space Telescope (Rieke et al. 2004) at two epochs, on December 27 and 29, 2008, both at 24 and 70 μm. The summary of these obser-

Name	Start	Length	Points	Duty	K_p
	TBJD (d)	d		cycle	mag
Caliban	7419.16	22.23	1019	0.93	21.99
Setebos	7416.15	28.85	495	0.35	22.87
Sycorax	7418.55	13.67	599	0.89	20.18
Prospero	7416.48	28.89	793	0.56	22.94
Ferdinand	7392.12	74.01	270	0.07	23.12
on array		16.14		0.32	

Table 1. Log of the *Kepler* observations. TBJD means truncated BJD, BJD-2450000. The last line shows the values for Ferdinand if we ignore the 57.87 d long period it spent off the detector array during the campaign. Duty cycle is 1.0 when all photometric points are retained and 0 when all had to be discarded. K_p is the mean brightness of the target in the Kepler photometric system.

vations is given in Table 2 below. Sycorax was successfully detected at both epochs and at both wavelengths. We used the same data reduction and photometry pipeline as in Stansberry et al. (2008, 2012). The MIPS instrument team data analysis tools (Gordon et al. 2005) were used to produce flux-calibrated images for each band, and the contribution of background objects were subtracted (see Stansberry et al. 2008). Aperture photometry was performed both on the original and final images and the final flux values were obtained using the aperture corrections by Gordon et al. (2007) and Engelbracht et al. (2007). Color correction of the in-band fluxes were done following (Stansberry et al. 2007). The flux densities obtained are presented in Table 3.

Sycorax was also observed in dedicated observations with the PACS camera of the Herschel Space Observatory, in the framework of the 'TNOs are Cool!' Herschel Open Time Key Program (Müller et al. 2009). The flux densities derived from these observations have already been presented in Lellouch et al. (2013).
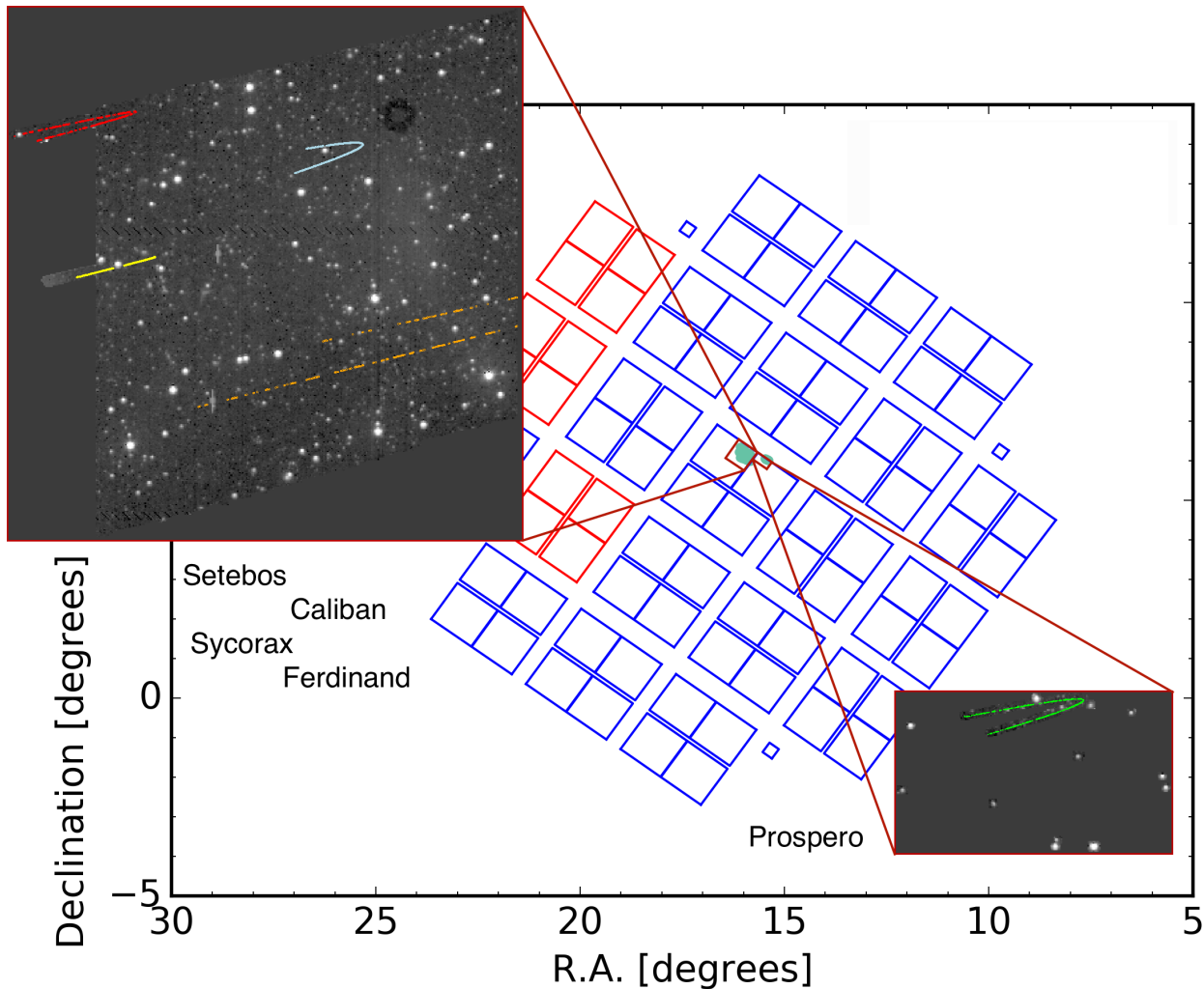
Figure 1. The median image of the Uranus mosaic we used for differential image photometry, plus the vicinity of Prospero on the adjacent CCD module, as seen by *Kepler*, overplotted on the K2 Campaign 8 field-of-view. Colored dots show the positions of the satellites at each successful photometric measurement. Red: Setebos; yellow: Sycorax; light blue: Caliban; orange: Ferdinand; green: Prospero.

We used both the Spitzer/MIPS and Herschel/PACS data for modeling of the thermal emission of the satellite (see Sect. 3.1).

2.2.2. *Serendipitous Herschel/PACS observations of irregular satellites*

Caliban was identified as potentially present on some far-infrared maps taken with the PACS camera of the Herschel Space Observatory. Herschel/PACS observed the environment of Uranus at two epochs: on January 7, 2012 (OBSIDs: 1342236891/92 / scan and cross-scan) and on January 13, 2012 (OBSIDs: 1342237436/37), under the proposal ID OT1_ddan01_1 in both cases.

All measurements used the $70/160\,\mu$m filter combination in all four cases. The data reduction pipeline we used is the same as the one used in the 'TNOs are Cool!' Herschel Open Time Key Programme Müller et al. (2009), described in detail in Kiss et al. (2014), and identical to that we used to reduce the Herschel/PACS maps of Nereid (Kiss et al. 2016). As our aim was to obtain photometry of a point source, we used the `photProject()` task with high-pass filtering to create maps from the time domain detector data. The `photProject()` task performs a simple coaddition of the frames using the drizzle method

Instrument	AORKEY/ OBSID	Target	Band (μm)	Date (JD)	r (AU)	Δ (AU)	α (deg)
Spitzer/MIPS	28832512	Sycorax	24	2454827.702	20.081	19.672	2.68
	28832512		70	2454827.718	20.081	19.672	2.68
	28832768		24	2454829.672	20.081	19.704	2.71
	28832768		70	2454829.688	20.081	19.704	2.71
Herschel/PACS	1342221837-38	Sycorax	70	2455710.589	20.084	20.519	2.62
	1342221875-76		70	2455710.939	20.084	20.514	2.62
	1342221839-40		100	2455710.617	20.084	20.519	2.62
	1342221877-78		100	2455710.966	20.084	20.513	2.63
	1342221837-40		160	2455710.589	20.084	20.519	2.62
	1342221875-78		160	2455710.939	20.084	20.514	2.62
Herschel/PACS	1342236891-92	Caliban	70	2455933.979	20.119	20.359	2.73
	1342237436-37		70	2455940.001	20.117	20.457	2.63
	1342236891-92		160	2455933.979	20.119	20.359	2.73
	1342237436-37		160	2455940.001	20.117	20.457	2.63
Herschel/PACS	1342236891-92	Trinculo	70	2455933.979	20.051	20.293	2.73
	1342237436-37		70	2455940.001	20.048	20.390	2.64
	1342236891-92		160	2455933.979	20.051	20.293	2.73
	1342237436-37		160	2455940.001	20.048	20.390	2.64
Herschel/PACS	1342236891-92	Ferdinand	70	2455933.979	19.930	20.174	2.75
	1342237436-37		70	2455940.001	19.929	20.173	2.65
	1342236891-92		160	2455933.979	19.930	20.174	2.75
	1342237436-37		160	2455940.001	19.929	20.173	2.65

Table 2. Summary of thermal infrared observations. The columns are: (1) Telescope/instrument; (2) AORKEY (Spitzer/MIPS) or OBSID (Herschel/PACS); (3) target – in the case of Caliban the target was caught in a larger, off-Uranus field; (4) band (nominal wavelength in μm); (5) date of the observation (Julian date); (6) heliocentric distance; (7) distance from observer; (8) phase angle;

([Fruchter & Hook 2002](#)), and the high-pass filtering applies a sliding median-filter on individual pixel timelines. More details on the procedure can be found in The PACS Data Reduction Guide[4].

Maps were created from the detector scans in the co-moving frame of Uranus that was practically identical to that of the satellites due to the small relative velocities of Uranus and the satellites ($<0.''5\,\mathrm{h}^{-1}$).

We identified a faint source at both epochs in the 70 μm band at the expected location of Caliban, obtained from the NASA Horizons System considering the Herschel-centric observing geometry (see Fig. 5), and derived a combined flux of $F_{70} = 1.4 \pm 0.8$ mJy. No obvious source could be

[4] see http://herschel.esac.esa.int/hcss-doc-14.0/ for version 14 documentation

Target	Detector/ filter	λ_{eff} (μm)	F_i (mJy)	C_λ	F_m mJy	$H_{V/R}$ (mag)
Sycorax	MIPS 24	23.68	3.017±0.045	0.96±0.01	3.14±0.16	7.50±0.04
	MIPS 70	71.42	14.68±2.78	0.92±0.01	16.07±2.89	(Grav et al., 2004)
	MIPS 24	23.68	3.109±0.046	0.96±0.01	3.17±0.17	
	MIPS 70	71.42	19.12±2.70	0.92±0.01	20.78±3.11	
	PACS 70	70.0	16.7±0.6	0.98±0.01	17.0±1.0	
	PACS 100	100.0	15.3±1.6	1.00±0.01	15.3±1.8	
	PACS 160	160.0	5.3±3.1	1.04±0.01	5.5±3.2	
Caliban	PACS 70	70.0	1.4±0.8	0.98±0.01	1.4±0.8	9.16±0.016
	PACS 160	160.0	<3 mJy	1.04±0.01	<3 mJy	(Grav et al., 2004)
Trinculo	PACS 70	70.0	<0.8 mJy	0.98±0.01	<0.8 mJy	11.92±0.18
	PACS 160	160.0	<3 mJy	1.04±0.01	<3 mJy	(Grav et al., 2004)
Ferdinand	PACS 70	70.0	<0.8 mJy	0.98±0.01	<0.8 mJy	12.5±0.1(R)
	PACS 160	160.0	<3 mJy	1.04±0.01	<3 mJy	(this work)

Table 3. Summary of thermal infrared observations. The columns are: (1) target – in the case of Caliban the target was caught in a larger, off-Uranus field; (2) detector and filter combination; (3) effective wavelength of the band (λ_{eff}); (4) in-band flux density (F_i); (5) colour correction factor (C_λ); (6) monochromatic flux ($F_m = F_i/C_\lambda$); (7) absolute magnitude in V or R band; Herschel/PACS flux densities of Sycorax are taken from Lellouch et al. (2013)
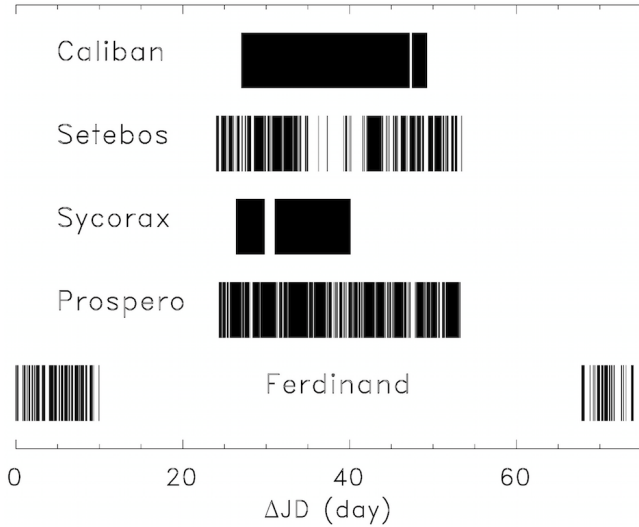

Figure 2. Temporal distribution of data points used for photometry and light curve construction for Caliban, Setebos, Sycorax, Prospero and Ferdinand. ΔJD is the date from the start of Campaign 8.

identified on the 160 μm maps, and the general photometric accuracy obtained using the implanted

source method (see Kiss et al. 2014) defined a 1-σ upper limit of $F_{160} < 3$ mJy for the 160 μm brightness of Caliban.

While Trinculo and Ferdinand could be potentially present on the same set of Herschel/PACS images as Caliban, these were not detected neither at 70, nor at 160μm, therefore we consider that their flux densities are below 0.8 mJy and 3 mJy at 70 and 160μm, respectively.

2.3. Konkoly Observatory 1m-telescope observations of Sycorax

Sycorax was also observed on the night of 2015 November 05/06 with the 1-m Ritchey-Cretien Coude (RCC) telescope of the Konkoly Observatory, located at Piszkéstető Mountain Station. In total, 70 frames were acquired with an exposure time of 300 seconds each, using an Andor iXon-888 electron-multiplying CCD (EMCCD) camera. Although it is not so relevant for such long expo-
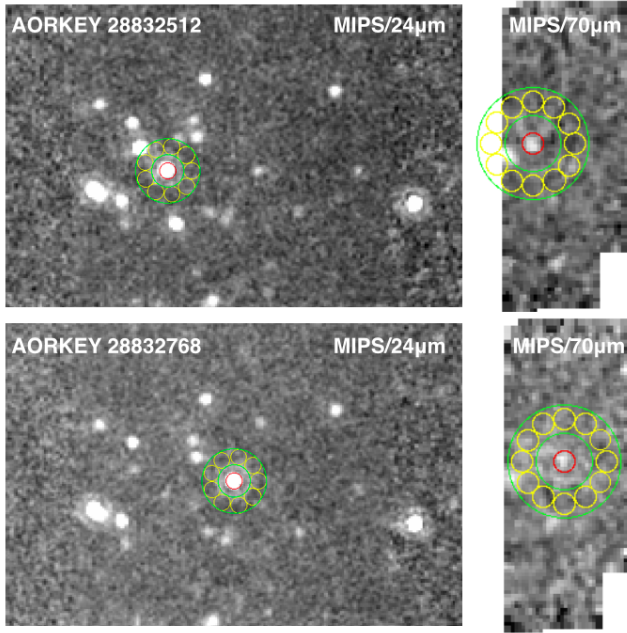
Figure 3. Spitzer/MIPS 24 and 70 μm images of Sycorax. The top and bottom rows present the images corresponding to the AORKEYs 28832512 and 28832768, respectively. On each image, red circles mark the target aperture and yellow apertures mark the positions used for background determinations (see Stansberry et al. 2008, 2012, for details)

sures, we note here that the camera was operated in frame transfer readout mode in order to have an effectively zero dead time between the subsequent frames. The frames were taken in Sloan r' filters and used the SDSS-III DR9 catalogue (Ahn et al. 2012) for reference magnitudes of the comparison stars. Standard calibration procedures and aperture photometry were performed using the various tasks of the FITSH package (Pál 2012). The resulted light curve is plotted in Fig. 6.

3. THERMAL EMISSION MODELS

To model the thermal emission of some of our targets, infrared monochromatic flux densities were derived from the in-band flux densities applying the appropriate color corrections, based on the surface temperatures of the targets (see Müller et al. 2011; Colbert et al. 2011, for the Herschel/PACS and Spitzer/MIPS color corrections, respectively), see also Table 3.
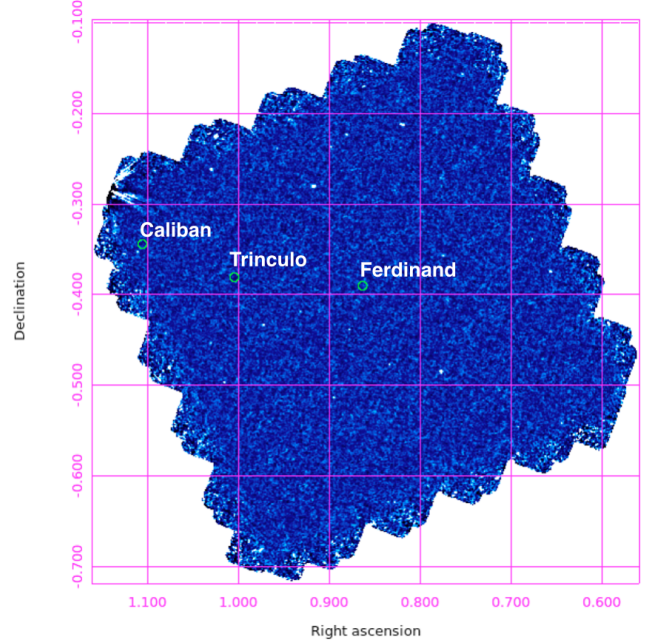
Figure 4. Locations of three potentially observable irregular satellites on the Herschel/PACS 70μm Level-2.5 map of two combined OBSIDs 1342237436/37.

We used these monochromatic flux densities and the observing geometry parameters listed in Table 2 to constrain the thermal emission models of our targets by calculating the χ^2 values of the modeled and observed monochromatic flux densities (see e.g. Vilenius et al. 2014, for details). We applied either the Near-Earth Asteroid Thermal Model (NEATM, Harris 1998) or a thermophysical model (TPM Lagerros 1996, 1997, 1998; Müller & Lagerros 2002) to obtain the model flux densities. TPM was only chosen in the case of Sycorax, as in the case of the other satellites with limited amount of thermal data (low degrees of freedom) it is not meaningful to run a complex TPM model over a more simple NEATM one. We used our own NEATM code written in IDL[5], and a TPM code developed by J.S.V. Lagerros and T.G. Müller (see the references above).

3.1. *Sycorax*

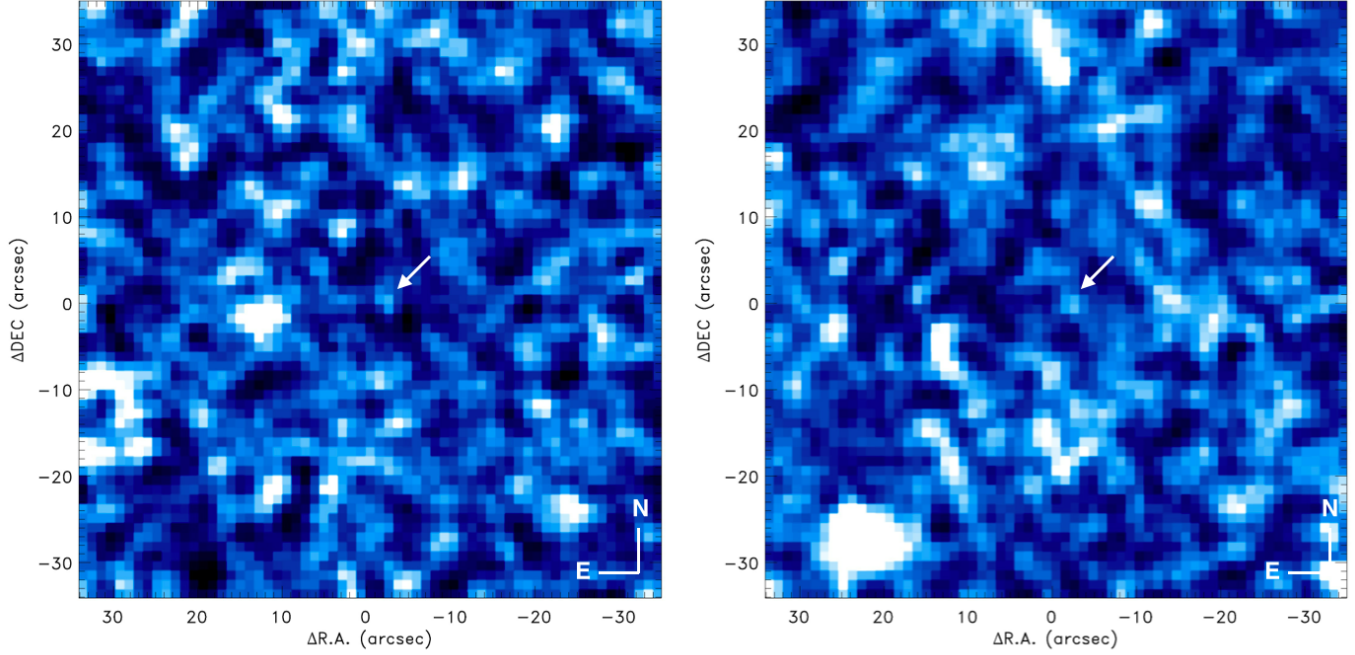
[5] Interactive Data Language, Harris Geospatial Solutions

Figure 5. Herschel/PACS 70 μm images of the region around the expected position of Caliban on 2012 January 7 (left) and January 13 (right). At both epochs a faint source is visible at the expected position (marked by white arrows). At both figures the brightness scaling is set in a way that white colour correspond to fluxes over 3σ r.m.s.
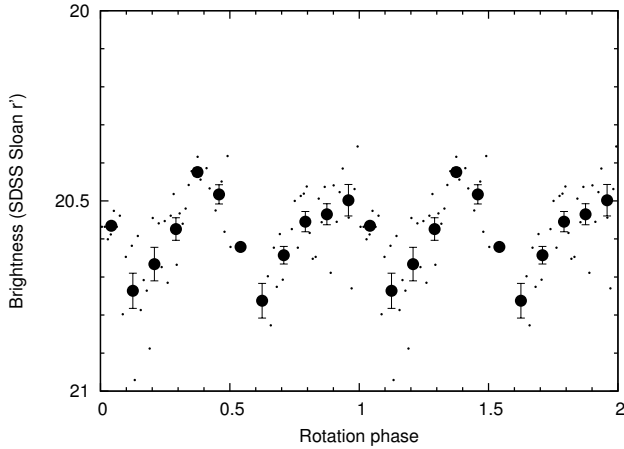

Figure 6. Sloan r'-band light curve of Sycorax observed with the 1m-RCC telescope of Konkoly Observatory, folded with the double period of $P = 6.9162$ h, obtained from the combination of K2 and 1m-RCC measurements.

Figure 7. Best-fit NEATM results of Sycorax. Flux densities of Spitzer/MIPS (24 and 71 μm) and Herschel/PACS (70, 100 and 160 μm) measurements are marked by diamonds and filled circles. The dotted and dashed curves correspond to the same set of best-fit NEATM parameters seen at the epoch of the Spitzer/MIPS and Herschel/PACS measurements.

The thermal emission of Sycorax was modeled using the flux densities listed in Table 3 applying a NEATM model. Due to the notable difference in observing geometry at the PACS and MIPS epochs, for a specific model (given size

and beaming parameter) the corresponding observation geometries were considered at the PACS and MIPS epochs separately, and the χ^2 values

were derived accordingly. The best-fit model is presented in Fig 7, where the flux densities of the MIPS and PACS epochs are shown individually. The NEATM model provided a best-fit effective diameter and albedo estimate of $D = 165 \pm 13$ km, $p_V = 0.065^{+0.015}_{-0.011}$, with a beaming parameter of $\eta = 1.20^{+0.25}_{-0.20}$.

In addition to the NEATM model we also applied thermophysical modeling (TPM, see Müller & Lagerros 1998, 2002, and references therein) considering an absolute magnitude of $H_V = 7^m\!.50 \pm 0^m\!.04$ (Grav et al. 2004), a default slope parameter of $G = 0.15$ and a wavelength-dependent emissivity (Müller & Lagerros 2002). We used $P = 6.9162$ h for the rotation period, as determined from the combination of K2 and Konkoly 1m-RCC measurements (see Sect. 4.1); possible thermal inertia values were considered in the $\Gamma = 0.1$–50 J m^{-2} s$^{-1/2}$ K^{-1} range and surface roughness values were allowed between $\rho = 0.1$ and 0.9. As the spin-axis orientation of Sycorax is not known, we considered three possible scenarios, a pole-on (spin-axis orientation of $\lambda = 356°$, $\beta \approx 0°$ in ecliptic coordinates), an equator-on ($\lambda = 0°$, $\beta = 90°$), and an intermediate one ($\lambda = 356°$, $\beta = 45°$). The equator-on and intermediate solutions provide a low best-fit reduced χ^2 of $\chi^2_r < 1$, and give very similar best fit values for the size. However, no acceptable solution with sufficiently low χ^2_r could be obtained for the pole-on case ($\chi^2_r \gg 1$ in all cases) and a non-pole-on configuration is also supported by the presence of a definite visible-range light curve. Our best estimates for the size and albedo are $D = 157^{+23}_{-15}$ km and $p_V = 0.07^{+0.02}_{-0.01}$, associated with a likely intermediate surface roughness ($\rho \approx 0.5$) and a close-to-equator-on spin axis configuration. Based on this analysis, very low levels of thermal inertia ($\Gamma < 1$ J m^{-2} s$^{-1/2}$ K^{-1}) can be excluded for Sycorax.

The diameter and geometric albedo obtained by our analysis is close to the best-fit values obtained by Lellouch et al. (2013) using Herschel/PACS
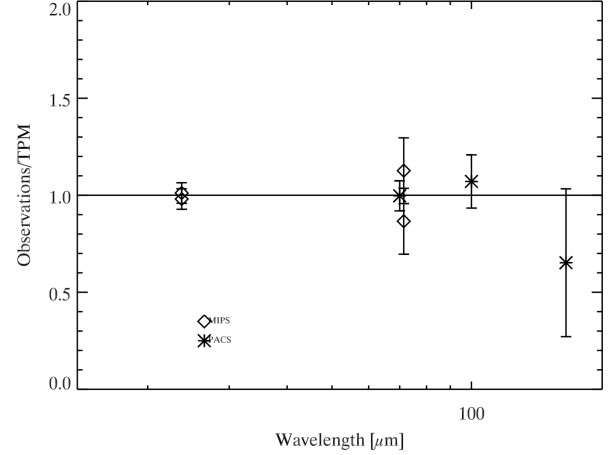

Figure 8. Ratio of the observed thermal infrared fluxes of Sycorax to those obtained in the best-fit thermophysical model, as detailed in the text.

data alone ($D = 165^{+36}_{-42}$, $p_V = 0.049^{+0.038}_{-0.017}$), but in our case with smaller error bars. However, the beaming parameter is much better constrained with the consideration of the Spitzer/MIPS fluxes, as the Herschel/PACS data could not restrict the models further due to the lack of short wavelength ($\lesssim 40\,\mu$m) data ($\eta = 1.26^{+0.92}_{-0.78}$ in Lellouch et al. 2013). Our best-fit $\eta = 1.20$ is very close to the median values obtained for Centaurs and trans-Neptunian objects based on a large sample of Spitzer/MIPS and Herschel/PACS measurements ($\eta \approx 1.2$, Stansberry et al. 2008; Lellouch et al. 2013). The thermal inertia value of $\Gamma = 3$–4 J m^{-2} s$^{-1/2}$ K^{-1} we obtained for Sycorax is also in agreement with the $\Gamma = 5 \pm 1$ J m^{-2} s$^{-1/2}$ K^{-1} value found by Lellouch et al. (2013) for Centaurs at heliocentric distances < 25 AU.

3.2. Small irregular satellites on Herschel/PACS images

For all potentially detectable satellites we used a NEATM model with a constant emissivity of $\epsilon = 0.9$ to estimate the expected flux densities in the 70 μm Herschel/PACS band for a range of diameters/geometric albedos and beaming parameters. The beaming parameter η was allowed to vary between 0.6 and 1.6, while the diameters were chosen to match a V-band geometric albedo

range of $0.01 \leq p_V \leq 0.3$. Phase integrals were calculated applying both the geometric albedo-dependent phase integral developed for the outer Solar system by Brucker et al. (2009) and the 'standard' value using the canonical slope parameter of $G = 0.15$ (see e.g. Muinonen et al. 2010). The difference between the $70 \, \mu m$ thermal emission flux densities obtained by the two methods were $\leq 4 \, \mu Jy$ in all cases, and are negligible for our purposes.

As described above, Caliban was tentatively detected on Herschel/PACS $70 \, \mu m$ maps with a combined monochromatic flux density of $F_{70} = 1.4 \pm 0.8 \, mJy$. A generally assumed dark surface of $p_V \approx 0.04$ and the corresponding diameter of $\sim 70 \, km$ would produce a $70 \, \mu m$ flux density of $F_{70} > 2.4 \, mJy$, easily detectable on our Herschel/PACS maps, over 3σ of the $0.8 \, mJy$ $70 \, \mu m$ flux uncertainty of the Herschel/PACS maps. The fact that the detected flux density of Caliban is *smaller* than that already indicates a brighter surface. We obtained $D = 42^{+20}_{-12} \, km$ and $p_V = 0.22^{+0.20}_{-0.12}$ as the best-fit NEATM solution using the single available $70 \, \mu m$ flux density, with no real constraint on the beaming parameter in our originally chosen $0.6 \leq \eta \leq 1.6$ range, with our best-fit model having a corresponding η of 0.8. The $70 \, \mu m$ flux of Caliban can, however, be equally well fitted with $D \approx 50 \, km$ and $p_V \approx 0.15$, using a higher η value of ~ 1.4. The uncertainties in the size and albedo due to the unconstrained beaming parameter are reflected in the errors of the best-fit values quoted above. The geometric albedo we obtained for Caliban may seem to be surprisingly high in the Uranian irregular satellite system, taking into account the low albedo of Sycorax. On the other hand, relatively bright surfaces exist among other irregular satellites, e.g. Nereid has a surface with $p_V > 20\%$ (Kiss et al. 2016), but it is notably larger than Caliban, $\sim 350 \, km$ in effective diameter.

Trinculo and Ferdinand were not detected on the Herschel/PACS images. However, considering the $0.8 \, mJy$ $70 \, \mu m$ flux uncertainties as an up-
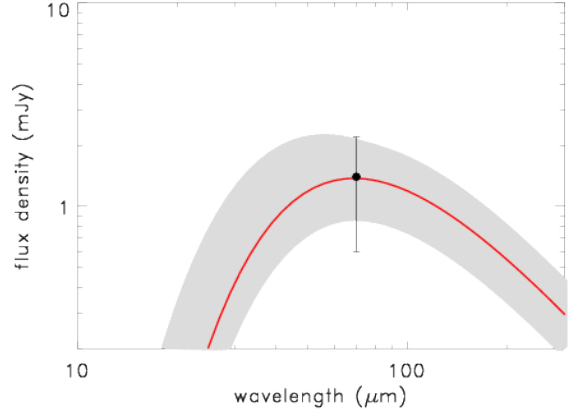

Figure 9. NEATM modeling results for Caliban. The black filled circle with error bar shows the only available measurement at $70 \, \mu m$ (Herschel/PACS). The red curve represent the best-fit result ($D = 42 \, km$, $p_V = 0.22$ and $\eta = 0.8$), the gray area contains the model curves that are compatible with the $70 \, \mu m$ flux (see the text for details).

per limit for both targets we can put some constraints on their geometric albedos and diameters. We note that for Ferdinand we calculated the R-band absolute magnitude using data in the Minor Planet Circular MPEC-2003-S105, assuming an R-band specific linear phase correction of $\beta_R = 0.119$ (Belskaya et al. 2008) and obtained $H_R = 12.06 \pm 0.15 \, mag$. For Trinculo we used the value provided by Grav et al. (2004) (see also Table 3). The $0.8 \, mJy$ 1σ upper limit indicates a geometric albedo of $p_V > 0.03$ for both satellites, and correspondingly their diameters are $D < 50 \, km$.

4. ROTATIONAL CHARACTERISTICS FROM K2 MEASUREMENTS

We searched for significant periodicities using the Fourier method as implemented in the *Period04* program package (Lenz & Breger 2005) and also the Lomb-Scargle periodogram in the *gatspy* Python package[6]. We got very similar results in several test cases, therefore we decided to stick to the Lomb-Scargle periods. We note that

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[6] https://github.com/astroML/gatspy/

| Satellite | Previous works | | | This work | | | | |
| | P | Δm | Ref. | f_0 | P | Δm | comm. | P_s |
	(h)	(mag)		(cycle day^{-1})	(h)	(mag)		(h)
Sycorax	4.12±0.04	0.032±0.008^s	M01	6.9374±0.0083	6.9190±0.0082	0.121±0.020	K2,d	67.3423
	3.60±0.02	0.067±0.004^s	M07	6.9402±0.0013	6.9162±0.0013	0.120±0.019	K2+1m,d	
Caliban	2.66±0.04	0.13±0.01^s	M01	4.8249±0.0092	9.948±0.019	0.16±0.03	K2,d	7.0026
Prospero	4.55±0.04	0.22±0.03^s	M07	3.359±0.044	7.145±0.092	0.41±0.07	K2,s	16.5871
Setebos	4.38±0.05	0.189±0.03^s	M07	5.640±0.022	4.255±0.017	0.27±0.06	K2,s	13.1705
Ferdinand				2.027±0.039	11.84±0.22	0.54±0.09	K2,s	82.715

Table 4. Summary of previous and present light curve observations of the Uranian irregular satellites Sycorax, Caliban, Prospero, Setebos and Ferdinand with the most likely rotation periods identified. The Δm light curve amplitudes are peak-to-peak values, unless marked with an 's' upper index – in this case they represent a sinusoidal amplitude. The references used in the table are: M01 – Maris et al. (2001); M07 – Maris et al. (2007). In the last column 'K2' and '1m' indicates data obtained from the K2 mission and with 1m-telescope of Konkoly Observatory, while 'd' and 's' mark single-peak and double-peak rotation periods. The last column (P_s) lists the stroboscopic periods calculated from the single peak periods.

the errors of the individual photometric points are taken into account. Only those signals were considered that were significant on the 3σ-level compared to the background local noise periodogram. We phase-folded the light curves with the best period and its double value, then decided which gave a better fit based on a visual inspection. As we have shown previously (Szabó et al. 2016) period determination of Solar system object with K2 long cadence measurements is solid if the coverage exceeds five days and the duty cycle is above 60%. These conditions are fulfilled for three of our targets, as we have shown in Table 1 already. The other two, Setebos and Ferdinand, have lower duty cycles, but the long baseline of the observations compensates for them. Overall, we were able to derive reliable solutions for most Uranian irregular satellites in our sample. The results are presented in Figs. 10, 11 and in Table 4 below. Table 4 also lists the rotation periods obtained from previous investigations. We emphasize that we do not accept all formally significant periods, but simply choose the one with the highest amplitude.

4.1. *Sycorax*

Maris et al. (2001) performed the first detailed study of the light curve in the R band using the 3.6 m ESO NTT telescope at La Silla, on 1999 October 8 and 9. The amplitude of light variation they found was $A = 0^{\mathrm{m}}032 \pm 0^{\mathrm{m}}008$ with a $P = 4.12 \pm 0.04$ h period. Measurements taken with the VLT in 2005 (Maris et al. 2007) provided the most likely light curve period and amplitude of $P = 3.6 \pm 0.02$ h and $A = 0^{\mathrm{m}}067 \pm 0^{\mathrm{m}}004$.

Our K2 measurements revealed a well-defined rotational period with a frequency of $f = 6.9374 \pm 0.0083$ cycle day^{-1} ($P = 3.458 \pm 0.001$ h, see Fig. 10). We assume that the light curve of Sycorax is double-peaked which is supported by the slight asymmetry of the light curve when it is folded with the half frequency / double rotation period (Fig. 10). This gives a double-peaked rotation period of $P = 6.9190 \pm 0.0082$ h. The single-peaked period is very close to that obtained by Maris et al. (2007) using VLT measurements. The peak-to-peak light curve amplitude obtained from K2 data is $A = 0^{\mathrm{m}}12 \pm 0^{\mathrm{m}}02$, consistent with that obtained by Maris et al. (2007) as sinusoidal amplitude.

There is a second significant peak on the frequency diagram at 0.35 cycle day^{-1} (Fig. 9, up-

most panel). Such secondary periods are often explained by tumbling rotation or a companion. Although a companion around Sycorax (a moon of a moon) would be an intriguing possibility, we suggest that this second peak is a sampling artifact. The interaction of a strictly periodic sampling (such as that of *Kepler*) and a strictly periodic process (such as a rotation of the asteroid) results in periodic phase shifts in the sampling, and hence, an emergence of a stroboscopic period that can modulate timing, brightness, shape modulations etc. In Szabó et al. (2013) we calculated the stroboscopic period as $P_s/P = 1/\min(]P/C[,]1 - P/C[)$, where P_s is the stroboscopic period, P is the observed actual period, C is the cadence, and $][$ denotes the fractional part. Substituting the rotation period (6.9162 ± 0.0013 h) and the cadence (1765.5 s) into the formula, the stroboscopic period is calculated to be 9.5–10.0-times the rotation period. Since the ratio of the two detected periods is 9.97, this is perfectly compatible with the stroboscopic origin of the long period brightness variation. Stroboscopic periods were calculated from the single peak periods of the other targets, too (see below), as listed in Table 4. We note that a stroboscopic period is not accepted simply by an amplitude criterion as a possible rotation period, but should be rejected due to its stroboscopic nature.

Since the series of ground-based observations with the 1m telescope of Konkoly Observatory was roughly 3 months before the K2 measurements and the precision of K2 measurements are rather fine, one can extrapolate the rotation cycle numbers in an unambiguous manner for such a relatively short period. This allows us to combine the two series of measurements (K2 and 1m RCC) to get an accurate rotational frequency, for which we obtained n=3.47012 ± 0.00067 cycle day^{-1}, i.e. P=6.9162 ± 0.0013 h.

4.2. *Smaller satellites*

Caliban: —Maris et al. (2001) determined a light curve period of 2.66 h that is not confirmed by our data (see Fig. 10). Instead, we obtained a most likely frequency of f = 4.8249 ± 0.0092 cycle day^{-1} and the asymmetry of the folded light curve indicates that the real rotation period corresponds to the half frequency, i.e. P = 4.9742 ± 0.0095 h. The single peak period of Caliban is the only one apart from that of Sycorax for which the corresponding stroboscopic frequency ($P_s = 7.0026$ h or $f_s = 3.4256$ cycle day^{-1}) is close to a significant peak in Fig. 10.

Prospero: —In our analysis the least unambiguous light curve period was obtained for Prospero. We identified the most likely period of 3.359 ± 0.044 cycle day^{-1} (P = 7.145 ± 0.092 h), but a strong, secondary peak is also visible at f = 4.415 ± 0.045 cycle day^{-1} that corresponds to a single-peak rotation period of P = 5.346 ± 0.055 h, very close to the light curve period obtained by Maris et al. (2007).

Setebos: —For this satellite we confirm the light curve period of 4.38 ± 0.05 h obtained by Maris et al. (2007) as we derived a most likely rotation period of P = 4.255 ± 0.017 h, very close to the previously mentioned value, without indication of a double-peak light curve.

Ferdinand: —The light curve period of Ferdinand was not determined earlier. The most likely frequency of 2.027 ± 0.039 cycle day^{-1} corresponds to a rather long rotation period of 11.84 ± 0.22 h, the longest one in our sample (assuming a single-peak light curve). Such long rotation periods are, however, not rare and present e.g. in the Saturnian system where the rotation periods of 10 from 16 irregular satellites in a recently studied sample show rotation periods longer than that of Ferdinand (Denk & Mottola 2013).

5. COMPARISON WITH THE ROTATIONAL CHARACTERISTICS OF OTHER IRREGULAR SATELLITES AND ASTEROIDS

Rotation of small body populations in the Solar system is often characterized by the so-called
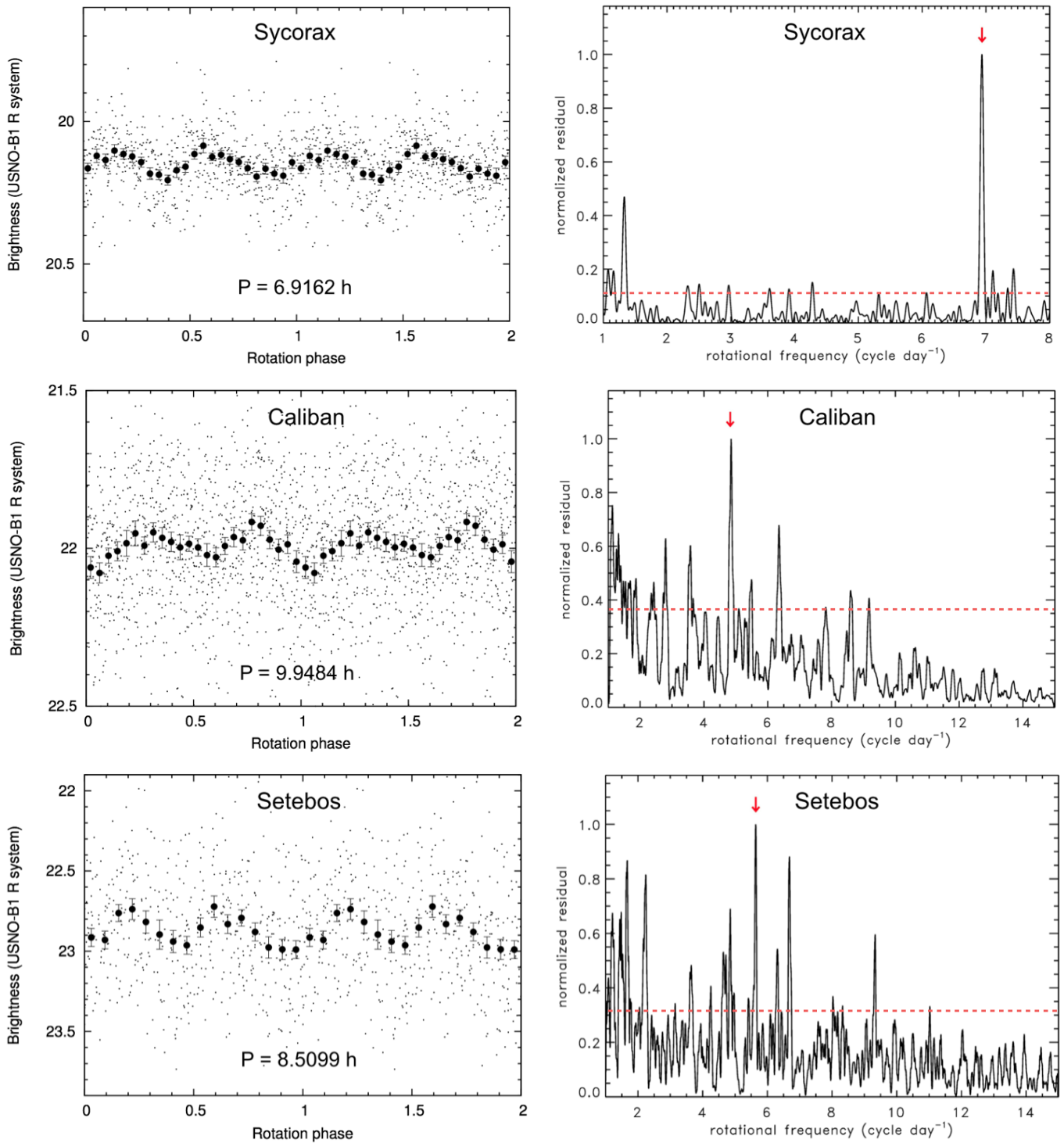
Figure 10. Folded K2 (USNO-B1 R-band) light curves and normalized residual vs. frequency diagrams of Sycorax, Caliban and Setebos. The folding periods are indicated on the left panels. The most likely frequencies are marked by red arrows in the normalized residual figures. The 3 σ significance levels are indicated by red horizontal lines in the normalized residual vs. frequency diagrams.
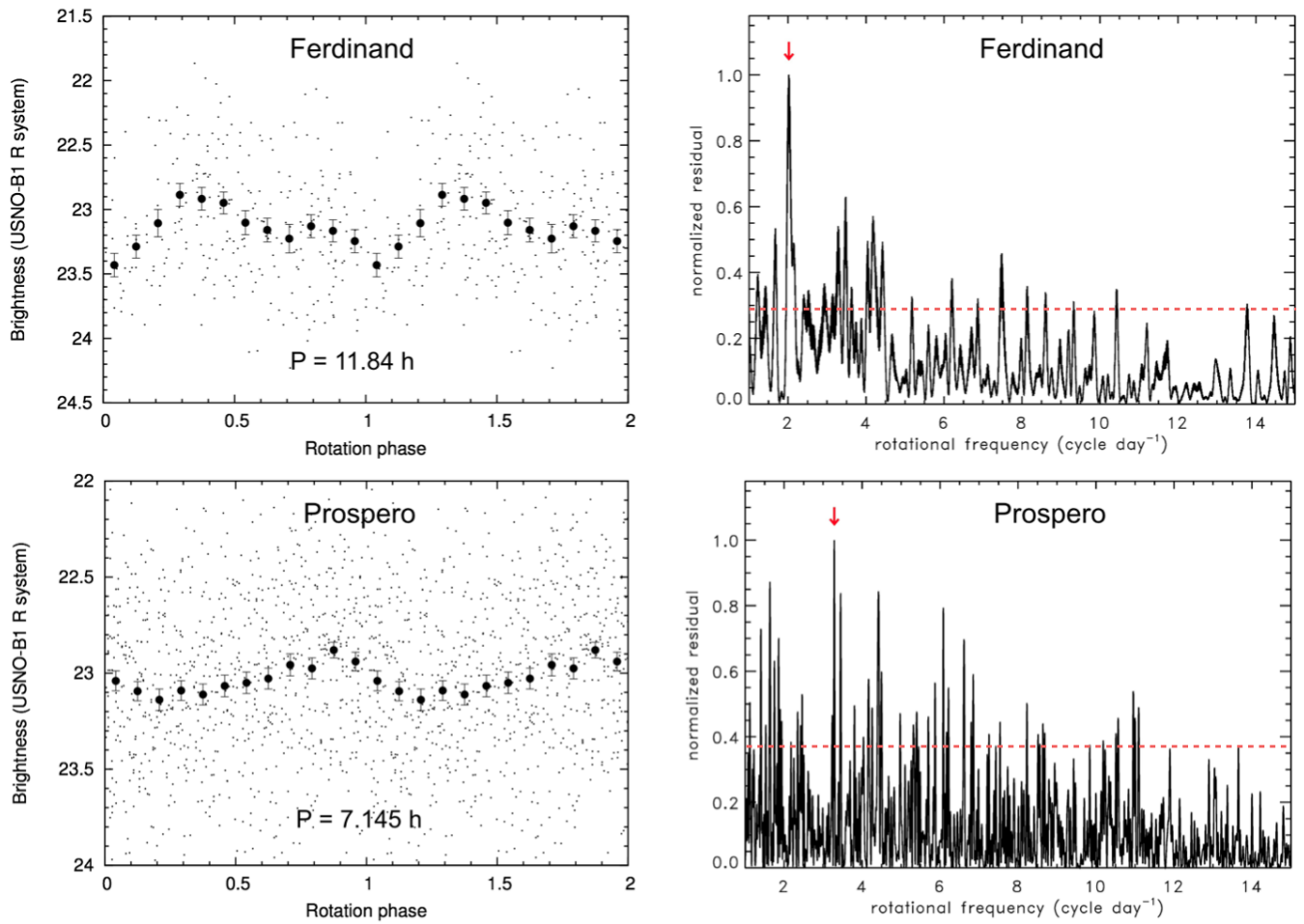
Figure 11. The same as Fig. 10 but for Ferdinand and Prospero.

spin barrier, a critical rotation period at which a rubble pile asteroid would fly apart due to its centripetal acceleration. This spin barrier is well established for Main Belt asteroids, the critical rotation period is ~2.2 h (dashed horizontal line in Fig. 12), resulting in a ρ_{crit} critical density estimate of ~2.0 g cm^{-3}, using the formula by Pravec & Harris (2000). In Fig. 12 we plot the rotation period versus size for various small body populations as well as for irregular satellites of the giant planet systems.

Considering our sample, the *median* rotational frequencies are notably higher in the Uranian system (≈ 3.4 cycle day^{-1}) than in the other giant planet systems (≈ 2 cycle day^{-1} for Jupiter, Saturn and Neptune). Also, assuming the double-peak rotation periods for Sycorax and Caliban provides us with critical densities $\rho_{crit} \leq 0.76$ g cm^{-3}. When the single-peak periods are considered for all Uranian irregular satellites ρ_{crit} still remains below 1 g cm^{-3}. These values are below the upper limits of ~2 g cm^{-3} of main belt asteroids, but higher than the ~0.5 g cm^{-3} obtained for e.g. Jovian Trojans (Szabó et al. 2017), the typical densities of cometary nuclei and trans-Neptunian objects (A'Hearn 2011; Brown 2013; Vilenius et al. 2014), and also those critical densities that can be estimated for the irregular satellites of the other giant planet systems, based on rotational light curves alone. However, e.g., the mass of the largest Jovian irregular Himalia has been estimated from its perturbations on other satellites (Emelyanov et al. 2005), and it gives an independent estimate on the density, $\rho > 2.6$ g cm^{-3}, using the size obtained during the Cassini flyby (effective radius of ~67 km Porco et al. 2003). This is significantly larger than the critical density of ~0.2 g cm^{-3} that can be obtained from the rotation period of 7.78 h and the light curve amplitude of $0^{\mathrm{m}}20 \pm 0^{\mathrm{m}}01$ (Pilcher et al. 2012).

The Uranian irregular satellites in our sample are in the size range where Maxwellian distribution of rotational frequencies starts for main belt asteroids ($D \gtrsim 40$ km, Pravec et al. 2002). While our sample is small and certainly not unbiased, the large median rotational frequency of the Uranian irregular satellites (3.4 cycle day^{-1}) may indicate that this irregular satellite system had a collisional evolution different from those around Jupiter and Saturn and Uranian irregulars suffered from a higher number and/or more energetic collisions. The median rotation period of 7.1 h in the Uranian system is close to that obtained for Centaurs (7.35 h, Duffard et al. 2009) and somewhat smaller than that of trans-Neptunian objects (8.6 h, Thirouin et al. 2014), however, these populations certainly went through a different collisional evolution than that of the Uranian irregular satellite system.

6. THE ALBEDO-COLOUR DIVERSITY OF IRREGULAR SATELLITES

In Fig. 13 we plotted the colors (represented by spectral slopes, Luu & Jewitt 1990) versus the geometric albedos of those irregular satellites for which these information were available. The Jovian irregular satellites are typically found in the same albedo-color region as the Centaurs/trans-Neptunian objects with dark-neutral surfaces (pale blue dots in Fig. 13). This is also the characteristic region for cometary nuclei and Jovian Trojan asteroids (see e.g. Lacerda et al. 2014). Only two Jovian irregular satellites show red surfaces, both extremely red and dark, already outside the bright-red group of outer Solar systems objects (pale red dots in Fig. 13). Saturnian irregulars (red symbols) are obviously in the dark-neutral group. Here we included Hyperion, too (highest albedo Saturnian point in Fig. 13), although this is strictly speaking not an irregular satellite, but shows characteristics different from the typical regular Saturnian satellites (elongated shape, highly cratered surface, likely porous interior). The Neptunian irregular, Nereid is also a likely dark-neutral object. Triton, however, is clearly distinct from all other irregulars, and, as it is expected due to its large size, resemble more the group of large dwarf planets than any other irregular satellites – in that case in-
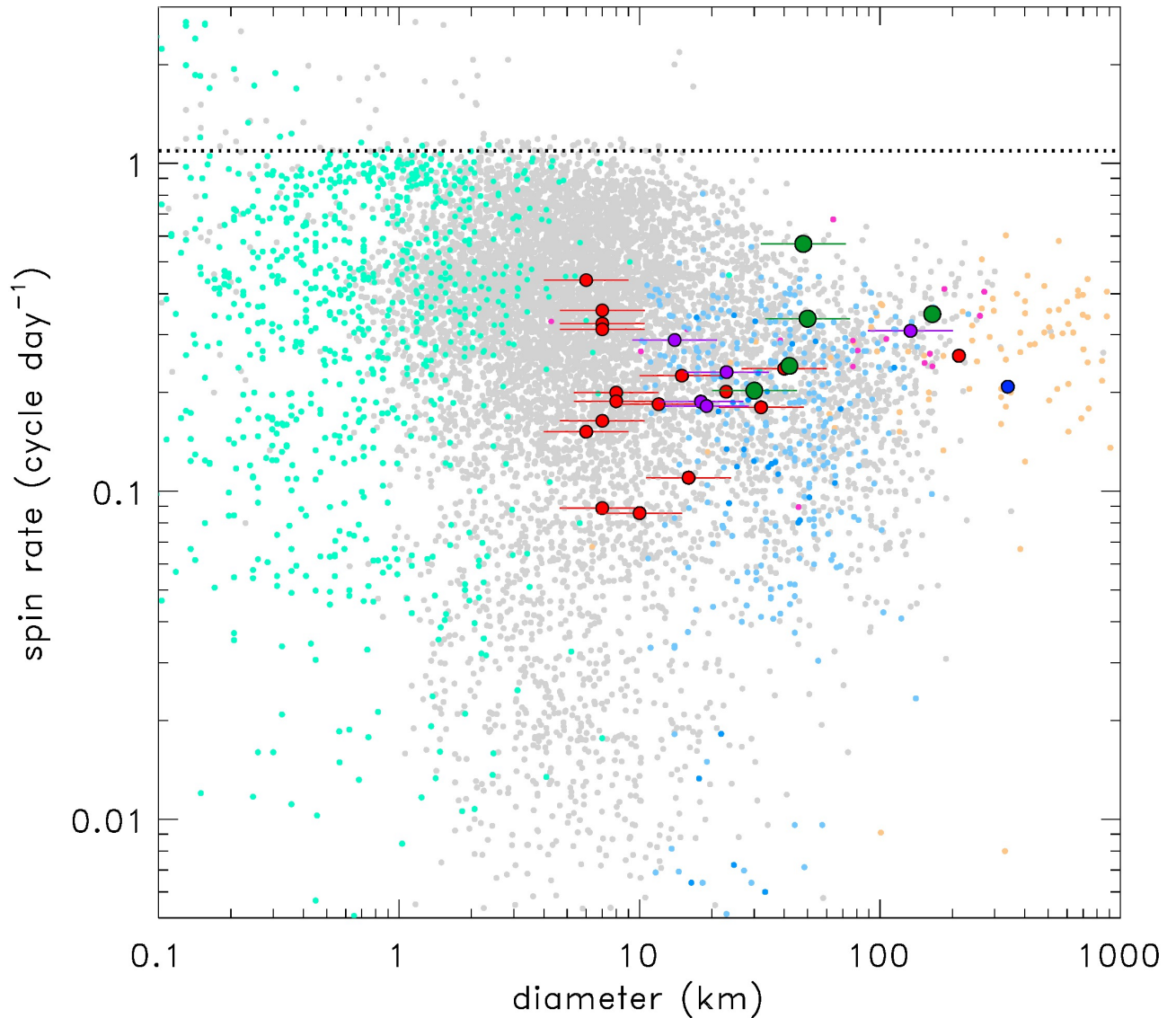
Figure 12. Diameter vs. rotational frequency of irregular satellites and asteroids. Filled green circles mark the four Uranian irregulars discussed in this paper. Purple and red filled circles mark the Jovian (Luu 1991; Pilcher et al. 2012) and Saturnian irregular satellites (Denk & Mottola 2013; Bauer et al. 2004), while the blue filled circle mark the Neptunian irregular satellite Nereid (Kiss et al. 2016). Horizontal bars around some satellites indicates the possible size range due to a large uncertainty in the estimation of the effective diameter from the visible range absolute magnitude. Pale-colored dots in the background correspond to the data of various minor planet populations throughout the Solar system (green: near-Earth asteroids; gray: main belt asteroids; blue: Jovian Trojans; magenta: Centaurs; orange: trans-Neptunian objects).

ternal processes (cryovolcanism) may have significantly altered the original surface. The surface of Triton, as well as those of the large regular satellites are more similar to the largest dwarf planets

(green symbols in Fig. 13) and the members of the Haumea collisional family (yellow symbols).

The two irregular Uranian satellites, Sycorax and Caliban, for which albedo and color data are avail-
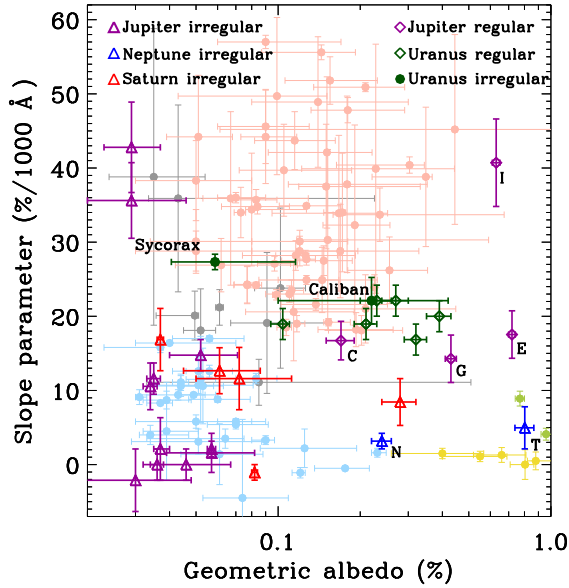
the Jovian and Saturnian systems, and also Nereid are generally darker and more neutral in color. If the surfaces of the Uranian irregular satellites and those in other giant planet systems are intrinsically different, and not a consequence of a different evolution of surfaces, this may be a further indication of a compositional discontinuity in the young Solar system. This discontinuity should have existed close to the heliocentric distance of Uranus, caused by the same processes that induced the bimodality among Centaurs and trans-Neptunian objects (Lacerda et al. 2014).

Figure 13. Albedo and colour characteristics of irregular satellites of the giant planet systems. Purple, red, green and blue correspond to the satellites of Jupiter, Saturn, Uranus and Neptune, respectively. Error bars mark the uncertainties in geometric albedo and color. Pale dots in the background correspond to the data of outer Solar system objects (Centaurs and trans-Neptunian objects), taken from Lacerda et al. (2014). Europa, Io, Ganymede, Callisto, Nereid and Triton are marked with their initials. References: Buratti & Veverka (1983), Cruikshank & Brown (1982), Denk & Mottola (2013), Grav et al. (2003, 2004, 2015), Hicks & Buratti (2004), Karkoschka (2001), Kiss et al. (2016), Lellouch et al. (2013), Millis & Thompson (1975), Morrison et al. (2009), Rettig et al. (2001), Showalter (2006), Simonelli & Veverka (1984), Smith (1989).

able both seem to fall into the bright-red group, along with some regular Uranian satellites (Puck, Miranda, Ariel, Umbriel, Titania, Oberon). Currently no other irregular satellites in other giant planet system can be assigned to this albedo-color group.

Although our sample is limited, the location of the irregular satellites on the albedo-color diagram may indicate that the surfaces of satellites in the Uranian system may resemble those of the bright-red trans-Neptunian objects. Irregular satellites in

Software: FITSH (Pál 2012), Period04 (Lenz & Breger 2005), gatspy (https://github.com/astroML/gatspy/)

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