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# LIGHT ABSÓRPTION IN PARAMAGNETIC IONS IN STATE OF SOLUTION. PART 1-CUPRIC IONS

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ABSTRACT. The light absorption from 3900 Å to 10,000 Å for eighteen cupric salts in equeous solution have been studied with a Hilger "UVINPER" spectrophotometer with an accuracy of 2 Å to 10 Å in different regions.

It is observed that  $Cu^{++}$  ions in aqueous solution have sharp absorption bands lying between \$110 Å and 6180 Å for different salts. The results are discussed in relation to the observed magnetic moments and g-values. From a study of the calculated covalency factors it is concluded that the mean magnetic moments do not change from salt to salt amongst the sulphates, chloridos and nitrates but are appreciably different for acctate, amines etc. In state of aqueous solution the salts are more ionic than in crystalline state if  $\Delta E$  is the same. In animosalts, acetate and propionate the covalency factor is made up of two factors arising from the  $\sigma$  and  $\pi$  orbital overlap.

#### 1. INTRODUCTION

Extensive magnetic measurements on single crystals of cupric sulphate pontahydrate (Krishnan and Mookherji, 1936 & 1938) and other salts (Krishnan and Mookherji, 1938; Mookherji, 1945, Bose, 1948 and Bose *et al.* 1957) have revealed that magnetic behaviour of Cu<sup>++</sup> ions in crystals may be explained in several details by assuming the Cu<sup>++</sup> ions to be under the influence of a strong and asymmetric crystalline electric field arising out of an axially distorted octahedral cluster of water dipoles, surrounding the metal ion. The effect of such a field is to split the ground state of the ion into a Stark pattern. According to Bethe (1929, 1930) and others (Abragam & Pryce, 1951 and Owen, 1954) Stark splitting of the original ground state,  ${}^{2}D_{5/2}$ , of free Cu<sup>++</sup> ion due to a crystalline electric field conforming to a potential

$$V = D(X^{4} + Y^{4} + Z^{4}) + A(X^{2} + Y^{2} - 2Z^{2}) + B(Z^{4} + 6X^{2}Y^{2})$$
(1)

is shown in figure 1, spin-orbit splitting being neglected. The first fourth degreeterms in this expression represent a field of cubic symmetry the coefficient  $D^{\gamma}$ of which is positive here (Gorter, 1932 and Van Vleck, 1932) and the remaining two terms represent the second and fourth degree components of the axial' (tetragonal) field with symmetry about z-axis and both the coefficients are positive for the usual Cu<sup>++</sup> salts (Bleaney, Bowers & Pryce, 1955; Abragam-& Pryce, 1951; Bleaney, Bowers and Ingram, 1955 and Bose *et al*, 1957). A numerical estimate in  $Cu(KSO_4)_2$ .  $6H_2O$  by Polder (1942) using a model  $Cu^{++}(H_2O)_6$  gives the tetragonal splitting of the same order of magnitude as due to the cubic field. Experimental observations do not support this (Abragam and Pryce, 1951 and others).



Fig. 1. Stark splitting of ground state of Cu++ion.

According to these workers the cubic splitting may be taken as  $\sim 10^4$  cm<sup>-1</sup>, and totragonal splitting as  $\sim 10^3$  cm<sup>-1</sup>. Hence the transitions between the levels so split will produce absorption spectra lying between ultraviolet and infra-red regions and as such will be capable of optical verification. Dreisch and Trommer (1937) working on the selective absorption for CuSO<sub>4</sub>.5H<sub>2</sub>O and [Cu(NH<sub>3</sub>)<sub>4</sub>]Cl<sub>2</sub> H<sub>2</sub>O in state of solution find that the absorption bands are roughly at 12,297 cm<sup>-1</sup> and 14,160 cm<sup>-1</sup> respectively.

In the state of solution of a given salt the lattice structure breaks down completely while the anisotropic ionic clusters retain their identities (Krishnan, 1939 and Chakravarty, 1942). But since they are oriented at random the medium will show no anisotropy of susceptibility. But optical absorption should reveal the fine structure in the Stark pattern arising from the anisotropic field splittings.

A systematic optical investigation of the consequences of the crystal field on the paramagnetic ions both in the crystalline state and in state of solution is under progress in this laboratory. The present communication deals with the absorption of light by a number of cupric salts in state of solution (aqueous) and are discussed in the light of the findings from magnetic measurements and paramagnetic absorption experiments.

# 2. EXPERIMENTAL

The selective absorption bands of paramagnetic salts of iron group of metals in state of solution show very broad absorption bands when photographed by a spectrograph; as such it is not possible to determine with any degree of accuracy, the position of the absorption maximum from an examination of the absorption spectra of these salts with a spectrograph (Dreisch and Trommer, 1937). Consequently the measurements on light absorption were carried out by a Hilger's "UVISPEK" spectrophotometer.

The description of the instrument is available from the literature (H700.307/57887) supplied by the company. Interested readers may refer to it.

The image of the lamp was accurately focussed on the entrance slit. The wavelength drum was calibrated by a hydrogen discharge tube and a mercury discharge lamp. The absorption cells were cleansed thoroughly and their percentage of transmission checked. The wavelength drum was set to the desired wavelength and the absorption cell tray was set such that the reference medium was in the light beam. The test solutions were then brought one by one in the light beam and for each of them the percentage of transmission was directly noted from the scale for that wavelength. This was repeated for various wavelengths.

The absorption due to the solvent and the absorption cell was nullified by filling the absorption cell with the solvent and putting it in place of the reference medium. Chemicals used were of 'Merck's' analytical reagent quality.

The accuracy of the measurements in the region 10,000Å to 6500Å is approximately 10 Å $\pm$ 2Å, from 6500Å to 5000Å is approximately 5Å $\pm$ 1Å and from 5000Å to 3900Å is approximately 2Å $\pm$ 1Å. Measurements are centred round about 27°C but no observable change in the position of the absorption bands was noticed for small room temperature variations.

### 3. RESULTS

~ Results of the measurements are collected in Table I. The location of the absorption bands for various cupric salts in the state of solution are given both in wavelength and wavenumbers. In order to get prominent absorption peaks for the slats studied we had to use dilute solutions. Progressive dilution from that concentration at which prominent absorption peak is obtained does not change the position of the absorption peak.

The variation of absorption in different salt solutions are shown graphically in figures 2 to 19. No fine structure of the lines corresponding to tetragonal splitting could be observed. -

#### 4. DISCUSSION

# (a) Crystal field and energy levels

According to the calculations of Polder (1942) the mean centres of the energy levels  $\Gamma_5$  and  $\Gamma_3$  (figure 1) are at  $\frac{6}{21}D'$  and  $-\frac{4}{21}D'$ , where  $D' = \frac{2}{5}er^4 \cdot D$ , D

# TABLE I

a 37-	Salts		Abe (Δ	orption E) at	74 0	1.17	Baarka		
5.NO.		Concentration	λÅ	Wave numbers cm <sup>-1</sup>	D = 2	.ιΔ <i>Ι</i> Δ	Rearks		
1. C	CuSO₄	1.0	8060	12,405	26,055	Not shar λ 805	p, lies bet 0 to λ 807	ween 5	
2. C	Ju(NH4.SO4)2	1.0	8050	12,420	26,085	Not sharp λ 805	, lies betw 0 to λ 806	veen 3	
3. C	u(K.SO4)2	10	8055	12,415	26,070	,			
4. C	u(Rb.SO₄)₂	1.5	8085	12,370	. 25,977				
5. C	u(Tl.SO4)2	1.0	8075	12,385	26,010				
6 C	℃uCl <sub>2</sub>	1.0	8075	12,385	26,010				
7.2	NH4Cl.CuCl2	1.0	8075	12,385	26,010				
8.2	KCl.CuCl <sub>2</sub>	1.0	8075	12,385	26,010				
9. C	baBr <sub>2</sub>	1.1	8110	12,330	25,893				
10. C	u(NO3)2	0.5	8060	12,405	26,055				
11. C	հւ <sub>ց</sub> Bi <sub>2</sub> (NO <sub>3</sub> ) <sub>12</sub>	1.16	8075	12,385	26,010				
12. C	ել(CHOO) <sub>2</sub>	0.5	7775	12,860	27,005				
13. C	u(CH <sub>3</sub> COO) <sub>2</sub>	0.25	7675	1 <b>3,03</b> 0	27,360				
14. C	$Cu(CH_8CH_2COO)_2$	0.4	7710	12,970	27,237				
15. [0	Cu( <b>NH₃)₄](SO₄</b> )	.080 1:1 ]NH₄ОН	6250	16,000	33,600	Band head conc. of	ł changes SNH₄OH	with	
16. [(	Cu(NH <sub>3</sub> )₄](OH)₂	·120 1:1]NH4OH	6230	16,050	89,705	-do	-		
17. [0	Cu(NH3)4](CH3COO)2	. 150 1:1 }NH₄OH	6200	16,130	33,875	-do	-		
18. [	[Cu( <b>NH</b> 3)4](Cl)2	· 150 1 : 1 ] NH₄OH	6180	10,180	<b>33,</b> 980	de	)—		







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Fig. 16. Absorption curve of (all) .080% Cu(NH<sub>3</sub>)<sub>4</sub>(SO<sub>4</sub>) solution.





being the cubic field coefficient (Eqn. 1) and  $r^4$  is the average value of the fourth powers of the radii of 3*d* electrons. Thus  $\Delta E$ , the cubic splitting is given by

$$\Delta E = \frac{10}{21} D'$$
 or  $D' = 2.1 \Delta E$ 

Hence it will be interesting to calculate D' from the observed  $\Delta E$  values which gives us an idea of the size of the octahedron of water molecules surrounding the Cu<sup>++</sup> ion. This is given in Table I.

It will be seen from these values that the octahedral clusters about  $Cu^{++}$ ion are of nearly the same size in all the halides,  $Cu (Tl.SO_4)_2$ ,  $Cu(RbSO_4)_2$  and  $Cu_3Bi_2(NO_3)_{12}$ . Single sulphate, single nitrate and other double sulphates have also practically the same size of octahedron. This indicates further that in the solution state probably all the six members of the cluster are the same namely water molecules, though this was not the case in the solid state e.g. in the single sulphate and the halides. In copper formate, copper acetate and copper propionate solutions these octahedra are much smaller. Amino-salts have the smallest octahedra. Thus at least some of the coordination members in solution are very probably other than water molecules.

### (b) Calculation of the covalency factor

Abragam and Pryce (1951) have calculated the "spectroscopic splitting factor"g in a tetragonal field for Cu<sup>++</sup> ion in crystals. For directions parallel

and perpendicular to the tetragonal axis, neglecting square and product terms we have

$$g_{\parallel} = 2 - \frac{8\lambda}{F_4} \cdot \frac{f^2}{F_5} \approx 2 - \frac{8\lambda}{\Delta E'}$$

$$g_{\perp} = 2 - \frac{2\lambda}{F_5} \cdot \frac{f^2}{F_5} \approx 2 - \frac{2\lambda}{\Delta E'}$$
(2)

in which  $f^2$  is the covalency factor arising from the partial overlap of the 3d orbitals with  $\sigma$  and  $\pi$  orbitals of the surrounding atoms (Owen 1954) assumed isotropic for the present; and  $F_4-F_3 \approx F_5-F_3 = \Delta E = \Delta E' \cdot f^2$ , is valid since the tetragonal separation in state of solution will be even less than  $\sim 10^3 \, \mathrm{cm}^{-1}$  owing to the absence of the effect of the long range field in solution state (Bose & Mitra, 1952; Bose. Mitra and Datta, 1957).

Using experimentally determined g-values from paramagnetic resonance both for solids and liquids we have calculated  $1/\Delta E'$ , for the various salts using relation (3) taking  $\lambda = -828$  cm<sup>-1</sup> (Shenstone and Wilets, 1951)

$$g = \sqrt{\frac{g_{\perp}^2 + 2g_{\perp}^2}{3}} \approx 2\left(1 - \frac{2\lambda}{\Delta E'}\right) \qquad \dots \quad (3)$$

These are given in Table III. It is observed that  $1/\Delta E'$  values of solutions differ considerably from those of the solid values, indicating the effect of long range field as mentioned above.

Now following Polder (1942), Bleaney *et al* (1949) and Owen (1954) the principal moments along and normal to the tetragonal axis of the paramagnetic units calculated from the susceptibilities of the crystalline salts are

$$\frac{\mu_{\rm el}^2}{3} = \left(1 - \frac{4\lambda \cdot f^2}{F_4 - F_3}\right)^2 + \frac{8kT \cdot f^2}{F_4 - F_3}$$

$$\frac{\mu_{\rm s}^2}{3} = \left(1 - \frac{\lambda \cdot f^2}{F_5 - F_3}\right)^2 + \frac{2kT \cdot f^2}{F_5 - F_3}$$
(4)

Taking as before

$$F_4 - F_3 \approx F_5 - F_3 = \Delta E = \Delta E' \cdot f^2$$

wehave

and

$$\tilde{\mu}^2 = (\tilde{\mu}_1^2 + 2\mu_1^2)/3 = \frac{3}{4}g^2 + \frac{12kT}{\Delta E'} = 3 \left[ 1 - \frac{4}{\Delta E'} (\lambda - kT) \right] \quad \dots \quad (5)$$

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S. N	Sulta.	g-va	luos	$\mu = \operatorname{Val}_{g\operatorname{-Ve}}$	ues from lues	$\mu$ — Values from succeptibility		
5.NO.	Suits	Crystal	Solution	Crystal	Solution	Crystal	Solution	
1.	CuSO4.5H2()	2.2081	2.1848	1.952	1.9265	1.9230	1.970	
2.	$Cu(NH_4.SO_4)_2.6H_2O$	2 180 <sup>2</sup>		1.922		1,9389		
3.	Cu(K.SO4)2 6H2O	2.1842		1 926		1,9200		
4,	$Cu(Rb.SO_4)_2.6H_2O$	2 2042		1.947		1.93010		
5.	Cu(Tl.SO4)2 6H2O	2.1772		1 918		1.97010		
6.	ԸսԸl₂.2 <b>ℍ</b> ₂Օ	2.1605	2.1848	1.902	1 9265	$1.932^{11}$	1.9850	
7.	CuCl <sub>1</sub> .2NH₄Cl	2.1603		1,901		1.88010	1.9678	
8.	CuCl <sub>2</sub> ,2KCl	2 1673		1 908		1.85010		
9.	CuBr <sub>2</sub>		2 1758		1 9175		2.0006	
10.	Cu(NO <sub>3</sub> ) <sub>2</sub> .3H <sub>2</sub> O		2 1848		1.9265	1.92212	1.9569	
11.	$\mathrm{Cu}_{\mathfrak{z}}\mathrm{B1}_{\mathfrak{z}}(\mathrm{NO}_{\mathfrak{z}})_{\mathfrak{1}\mathfrak{z}}.\mathfrak{2}\mathfrak{z}\mathfrak{H}_{\mathfrak{z}}\mathrm{O}$	2 1844		1.962				
12.	Cu(CHOO)2.4H2O	2.1505					1 740	
13.	$Cu(CH_3COO)_2,H_2O$	2.1645		1.45		1,41010	1.488	
14.	$\mathrm{Cu}(\mathrm{CH_{3}CH_{2}COO})_{2}.\mathbf{H}_{2}\mathrm{O}$	2.1845					1.560	
15.	[('u(NH <sub>3</sub> )4] (SO4)	2.0747	2.1008	1 811	1.838	1.84518		
16	$[CU(\mathbf{NH}_3)_4]$ (CH) <sub>2</sub>		2.1008		1.838			
17.	$[Cu(NH_3)_4] (CH_3COO)_2$		2.1008		1.838			
18.	[Cu(NH <sub>J</sub> ) <sub>4</sub> ] (Cl) <sub>2</sub>		2.100 <sup>s</sup>		1.838			

1-Bauggley & Griffiths (1950), 2-Bleaney, Penrose and Plumpton (1949), 3-Abe, Ono, Hayashi, Shimada and Iwanaga (1954), 4-Trenam R. S. (1953), 5-Abe, (1953), 6-Mathur, S. C. (Unpublished, 7-Okamura and Date (1954), 8-B.M. Kozyrev (1957), 9-Bose (1948), 10-Mookherji (1945), 11-Birch (1928), 12-Welo (1929), 13-Janes(1935).

		$1/\Delta E' \times 10^{-6}$				f²				
S.No.	Salts	From	g-values	From	µ-values	From	q-valuos	From	#-values	
		crystal	solution	crysta	solution	crystal	solution	crysta	l solution	
1,	CuSO4.5H2O	62.8	55.6	54 7	68 9	. 779	. 689	.679	.855	
2.	Cu(NH4.SO4)2.6H2O	54.4		51.0	)	676		.633		
3.	Cu(K.SO4)2.6H2O	55.6		53.6	i	. 690		.664		
4	$Cu(Rh.SO_4)_2.6H_2O$	61.6		56.7		. 762		.702		
б.	$Cu(Tl.SO_4)_2.6H_2O$	53.5		68 2	2	. 662		.844		
6.	CuCl <sub>2</sub> .2H <sub>2</sub> O	48.5	55.6	57 (	5 72.9	.600	.688	.713	.903	
7.	CuCl <sub>2</sub> .2NH <sub>4</sub> Cl	48.3	i	42.0	) 67.45	.600		.520	. 835	
8.	CuCl <sub>2</sub> 2KCl	50.4		33.6	5	624		.416		
9.	CuBr <sub>2</sub>		52.84	ł	94 85		.65		990	
10.	Cu(NO <sub>3</sub> ) <sub>2</sub> 3H <sub>2</sub> O		55 6	54 3	8 64.2		.689	.674	.795	
11,	$Cu_3Bi_2(NO_3)_{12}.24H_2O$	66.0	)	54 3	8	.817		.672		
12.	Cu(CHOO)2,4H2O	45.3	ł			.58		.028	.69	
13	$Cu(CH_JCOO)_2,H_2O$	49.4	1	48,	8 51.4	.644		. 636	.67	
14	Cu(CH <sub>7</sub> CH <sub>2</sub> COO) <sub>2</sub> .H <sub>2</sub> C	) 55.(	3			72			.68	
15.	[Cu(NH <sub>3</sub> )4] (SO4)	22.3	8 30.1	9 32.	0	.357	. 483	.512		
16.	$[\mathrm{Cu}(\mathrm{NH}_3)_4]$ (OH) <sub>2</sub>		<b>3</b> 0,1	9			, 485			
17.	[Cu(NH <sub>3</sub> )4] (CH <sub>3</sub> COO)	2	30 1	9			. 489			
18.	$[\mathrm{Cu}(\mathbf{NH}_8)_4]$ (Cl) <sub>2</sub>		30.1	9			.487			

# TABLE III

We have calculated the values of  $\overline{\mu}$  from the resonance values of 'g' using the above equation and have given them for comparison with experimental susceptibility values of  $\mu$  for both solids and solutions in Table II.

The experimentally determined values do not agree with the calculated values. So we have calculated  $1/\Delta E'$  from experimentally determined  $\mu$ -values of solids and solutions. There also the two values are different. Hence we presume that we can not utilize our optically observed value of  $\Delta E$  from solutions to calculate  $f^2$  for crystals. To get the values of  $f^2$  for crystals we need optical data in crystal state. However, taking the  $\mu$ -values of solutions and using our optical data in state of solution, we have calculated  $f^2$  for various cupric ions in state of solution which are given in Table III It is seen that the single sulphate, the chloride, bromide and the nitrate are predominantly ionic;  $f^2$  values tend to be  $\sim 0.9$  in state of solution.

In the case of copper acetate according to Bleaney and Bowers (1952) pairs of Cu<sup>++</sup> ions in the crystal are coupled together by exchange forces. Thus they will form a triplet state with parallel spin and a singlet state with anti-parallel spin. The triplet state will show a resonance spectrum similar to nickel salts with effective spin unity. Here again g is given by the expression (3). Using this expression and taking g for copper acetate from table II, we have calculated  $f^2$  which is 0.644.

Bleaney and Bowers (1952) have deduced expressions for the principal susceptibilities for copper acetate from which  $\bar{\mu}^2$  is given by

$$\mu^{2} = 4 \left( 1 - \frac{4\lambda \cdot f^{2}}{\Delta E} \right) \left[ \frac{1}{1 + \frac{1}{5} e^{-J/RT}} \right] + \frac{12kT}{\Delta E} \cdot f^{2} \qquad \dots \quad (6)$$

Taking  $\bar{\mu}^2$  value for the crystal (Table II) using  $J = -315 \text{ cm}^{-1}$  (Bleaney and Bowers, 1952) and our observed  $\Delta E$  for solution we have calculated  $f^2$ , which comes out as 0.636; now taking mean of these two values we have calculated Jutilising  $\bar{\mu}$  and  $\Delta E$  values for solution which is found to be  $\approx -270 \text{ cm}^{-1}$ . If one calculates  $f^2$  with  $J = -315 \text{ cm}^{-1}$  as in crystal and  $\bar{\mu}$  and  $\Delta E$  for the solution  $f^2$  comes out as 1.022 which is inadmissible. This anomaly may be attributed to the value of J which should be different in different states.

An examination of  $f^2$  values in different states suggests that the most probable value of  $f^2$  should be  $\approx .67$ , which gives the parameter J = -275 cm<sup>-1</sup>.

Anomalous resonance absorption spectra similar to copper acetate has been observed by Abe (1953) in case of copper propionate monohydrate. Our magnetic measurements on the moment of Cu<sup>++</sup> ion in Cu(CH<sub>3</sub>CH<sub>2</sub>COO)<sub>2</sub>. H<sub>2</sub>O salt m state of solution shows that  $\mu = 1.56$ . These findings point to the fact that the behaviour of  $Cu^{++}$  ions in the propionate will be similar to that of  $Cu^{++}$  ions in the accetate. Hence expression (6) is applicable in this case also.

Supplying experimental g-value and our observed  $\Delta E$  for copper propionate in expression (3) we have calculated  $f^2$  which comes out to be 0.72 (table II). Now substituting this values of  $f^2$  and using  $\mu$  value for solution in the expression (6) we have calculated J the exchange integral which comes out to be  $-244 \text{ cm}^{-1}$ . Since  $f^2$  in solution is not the same as in solid state, hence this value of J will be slightly different in state of solution. Due to want of  $\bar{\mu}$  value for the crystal it is not possible to suggest a most probable value for  $f^2$  but a comparison of the solution  $\bar{\mu}$  values of acetate and propionate suggests that  $f^2$  should be almost like the acetate; hence taking  $f^2$  as 0.68, J comes out  $\approx -230 \text{ cm}^{-1}$ .

The behaviour of Cu<sup>++</sup> ion in formate from our observed  $\Delta E$  value seems to be alike the acetate and propionate; but paramagnetic rosonance spectrum as observed by Abe (1953) does not support this The moment value as observed by us in state of solution goes to suggest that this is the limiting case between the Tutton salts with  $\bar{\mu}$  values more than the spin—only value on one side and the acetate and propionate on the other with  $\bar{\mu}$  values less than the spin—only value.

If  $Cu^{++}$  ions in formate behave like that in Tutton salts then  $f^2$  from expression (5) comes out to be .028 which is madmissible This led us to presume that the behaviour of  $Cu^{++}$  ion in formate should be like those of the acetate and propionate.

On evaluating  $f^2$  from the observed g-value in solid state and  $\Delta E$  value from solution, it comes out as 58; but  $f^2$  in state of solution should be different. A study of the  $f^2$  values for propionate and acetate suggests that the probable value of  $f^2 \approx .69$ . This when substituted in (6) gives J = -130 cm<sup>-1</sup>, with  $\bar{\mu} = 1.74$  as given in Table II. It is observed that the exchange integral in these three salts are in the right direction.

The acctate, propionate, formate and the amino-salts suggest that  $f^2$  is really made up of two factors arising from the  $\sigma$ -orbital overlap and the other from  $\pi$ -orbital overlap eg., in the amino-salts  $f^2$  may be,  $f_a^2 \sim .62$  and  $f_\pi^2 \sim .85$ making  $f^2 = f_a^2 \cdot f_\pi^2 = .53$  as observed (very nearly so), while for the acctate, propionate and formate  $f_a^2 \sim .75$  and  $f_\pi^2 \sim .9$  giving  $f^2 = .68$  which is very near the observed values.

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