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APPLICATION OF A NEW MULTI-AGENT BASED PARTICLE SWARM OPTIMISATION METHODOLOGY IN SHIP DESIGN HAO CUI and OSMAN TURAN

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ABSTRACT

In this paper, a multiple objective 'Hybrid Co-evolution based Particle Swarm Optimisation' methodology (HCPSO) is proposed. This methodology is able to handle multiple objective optimisation problems in the area of ship design, where the simultaneous optimisation of several conflicting objectives is considered. The proposed method is a hybrid technique that merges the features of co-evolution and Nash equilibrium with ε -disturbance technique to eliminate the stagnation. The method also offers a way to identify an efficient set of Pareto (conflicting) designs and to select a preferred solution amongst these designs. The combination of co-evolution approach and Nash-optima contributes to HCPSO by utilising faster search and evolution characteristics. The design search is performed within a multi-agent design framework to facilitate distributed synchronous cooperation. The most widely used test functions from the formal literature of multiple objectives optimisation are utilised to test HCPSO. In addition, a real case study, the internal subdivision problem of a ROPAX vessel, is provided to exemplify the applicability of the developed method.

Keywords:

Optimisation, Particle Swarm Optimisation, Ship Design, Multi-Agent, ɛ-disturbance

1. Introduction

Ship design is a dynamic process, and in recent years the multi-objective optimisation in ship design has attracted a lot of interest. In ship design, the internal hull subdivision is very important for damage stability, survivability and cargo capacity performance, particularly for Roll-on/Roll-off (ROPAX) passenger vessels, which have to comply with SOLAS standards, including SOLAS 90 and 'water on deck', which is known as the Stockholm Agreement. In order to satisfy these strict regulations, the ship designer needs to optimise the hull subdivision to achieve high safety standards, while improving the capacity and performance of the ship, by utilising a simple and effective method.

Multi-objective optimisation is one of the main study areas of ship design. In recent years especially, there have been many multi-objective optimisation approaches used in ship design. Lee [1] proposed a multi-objective design of a marine vehicle via the ε -constraint method, coupled with a genetic algorithm where two objectives and three types of constraints were modelled. The GA (Genetic Algorithm) was used to find the separate optima required by the ε -constraint technique. Thomas [2], [3] used Pareto ranking, MOGA and NPGA to investigate the feasibility of full stern submarines. Three objectives were considered: maximize internal volume, minimize power coefficient for ducted propulsor submarines, and minimize cavitation index. Binary representation and different selection techniques were used. Thomas also compared several different algorithms and reached the conclusion that MOGA outperforms the other methods in all of the aspects considered. Brown and Thomas [4]

used a GA with Pareto ranking for naval ship concept design. Two objectives were considered: maximize overall measure of effectiveness (this factor represents customer requirements and relates ship measures of performance to mission effectiveness) and minimize life cycle cost. Binary representation and roulette wheel selection with stochastic universal sampling were used. Brown and Salcedo [5, 6] introduced a Multi-Objective Genetic Algorithm in naval ship design. Todd and Sen [7] used a variant of MOGA for the pre-planning of containership layouts (a large scale combinatorial problem). Four objectives were considered: maximize proximity of containers, minimize transverse center of gravity, minimize vertical center of gravity, and minimize unloading. Binary representation and roulette wheel selection with elitism based on non-dominance were used. They used the same algorithm for the cutting shop problem in the shipyard [8], [9]. Two objectives were considered: minimize makespan and minimize total penalty costs. Peri and Campana [10] proposed a multidisciplinary design optimisation of a naval surface combatant and also developed High-Fidelity Models and Multi-Objective Global Optimisation Algorithms in Simulation-Based Design [11]. Olcer [12] proposed a hybrid approach for multi-objective optimisation problems in ship design and shipping. In his study, software 'Frontier' was used to perform optimisation via MOGA. Boulougouris and Papanikolaou [13] introduced a multi-objective optimisation of a floating LNG terminal. The software 'Frontier' with MOGA was utilized.

The Particle Swarm Optimisation (PSO) algorithm, which was proposed by J.Kennedy and R. Eberhart in 1995 [14], has been successfully used in single-objective optimisation problems. Since Moore and Chapman [15] proposed the first extension of the PSO strategy for solving multi-objective problems in 1999, a great deal of interest has been shown in multi-objective optimisation and many different approaches/techniques have been presented in literature. PSO, which has been successfully applied in numerous engineering areas, has only a small number of parameters, which need to be adjusted and is easy to implement.

In ship design, Pinto et al. [16] emphasised the importance of initial points' configuration and addressed some preliminary aspects of global convergence of PSO towards stationary points. In their follow-up paper [17], they presented a deterministic method for multi-PSO and applied the method to the multi-objective (two objectives) seakeeping of containership problem.

Since Mistree [18] approached ship design from a decision perspective, the decision making based ship design environment has developed rapidly. In recent years, multi-agent based ship design decision making has received a great deal of attention and at the same time the distributed synchronous cooperative ship design method via the internet is becoming a new research field. However, in terms of simplicity and efficiency, it requires a new optimisation approach which is suitable for a multi-agent system.

This paper introduces a new 'Hybrid Co-evolution based Multi-objective Particle Swarm Optimisation' (HCPSO) method. The HCPSO combines co-evolution, game theory and ε -disturbance technique to develop an effective optimisation approach which performs remarkably well in the multi-agent system. The paper then demonstrates the application of HCPSO with three objectives on the internal subdivision arrangement of a ROPAX vessel.

The paper is organised as follows: Section 2 presents PSO and Multi Objective Particle Swarm Optimisation (MOPSO), and Section 3 presents a new multi-objective particle swarm optimisation methodology and the detailed explanation of this algorithm. the test functions are processed in section 4, while a real case study 'hull subdivision design optimisation' is performed in section 5. Finally, in section 6, discussions and conclusions are presented.

2. Background

The Particle Swarm Optimisation is a global optimisation algorithm and described as sociologically inspired. It was first proposed by Kennedy and Eberhard in 1995 [14]. In the PSO algorithm, the candidate solution is the particle position in search space. Every particle is structured with two parameters: position and velocity, then the particle searches the solution space by updating the position and velocity. There are two best positions in PSO. The first one is Pbest, which represents the best position that the particle itself can reach; the other is Gbest, which is the best position in the whole swarm.

The PSO can be described as following,

$$v_{id}^{n+1} = \omega v_{id}^{n} + c_1 r_1^{n} (p_{id}^{n} - x_{id}^{n}) + c_2 r_2^{n} (p_{gd}^{n} - x_{id}^{n});$$

$$x_{id}^{n+1} = x_{id}^{n} + \chi v_{id}^{n+1};$$
(1)

where x_{id}^n is the position of particle i, in n-th iteration and d dimension; v_{id}^n is the velocity of particle i,

in n-th iteration and d dimension; p_{id}^n as Pbest is the best position of particle reached and p_{gd}^n as

Gbest is the best position in current swarm; c_1 and c_2 are two coefficients; r_1 and r_2 are two random numbers with the range [0,1]; ω is the inertia weight and χ is the constriction factor.

PSO has been proven as a simple but effective algorithm in single objective optimisation and multi-objective research has rapidly developed in recent years. Since the first extension was proposed in 1999, many different multi-objective PSOs have been presented [19] and some of these approaches are briefly given below.

Aggregating approaches: They combine all the objectives of the problem into a single objective and three types of aggregating functions are adopted: conventional linear aggregating function, dynamic aggregating function and the Bang-bang weighted aggregation approach (Parsopoulos and Vrahatis [20], Baumgartner et al.[21] and Jin et al [22]).

Lexicographic ordering: In this algorithm, which was introduced by Hu and Eberh [23], only one objective is optimized at a time using lexicographic ordering Schema.

Sub-Population approaches: These approaches involve the use of several subpopulations as single-objective optimizers. Then, the subpopulations somehow exchange information or recombine amongst themselves, aiming to produce trade-offs amongst the different solutions, which were

previously generated for the objectives that were individually optimised. Parsopoulos et al. [24], Chow et al.[25] and Zheng et al.[26] use this approach.

Pareto-based approaches: These approaches use leader selection techniques based on Pareto dominance and references include Moore and Chapman [27], Ray and Liew [28], Fieldsend and Singh [29], Coello et al [30] and [31] and Li [32].

Some of the other approaches, which use different techniques such as *Combined Approach* and *MaxMin approach*, can also be found in literature.

Sefrioui and Periaux [33] introduced Nash equilibrium of game theory into the multi-objective optimisation. Nash equilibrium is a set of strategies with the property that no player can benefit by changing its strategy while the other players keep their strategies unchanged. A Nash genetic algorithm was given with comparisons to Pareto GAs. They concluded that Nash genetic algorithms offer a fast and robust alternative for multi-objective optimisation.

3. Description of the Proposed Approach - HCPSO

The proposed approach combines co-evolution approach, Nash equilibrium and ε -disturbance technique to form a new improved hybrid approach. At the same time, the agent-based structure is adopted for distributed synchronous cooperation.

In HCPSO, the co-evolution approach is combined with Nash optima, which looks for Nash Equilibrium. For an optimisation problem with M number of objectives in an agent environment, M numbers of agent-groups are employed to optimise their own objective while changing the objective of other/remaining agent-groups. When no agent-group can improve its objective further, it means that the system has reached a state of equilibrium called Nash Equilibrium. In HCPSO, the co-evolution approach provides a public information sharing mechanism to improve the communication amongst agent-groups.

The reason for adopting the co-evolution approach here is that on the one hand, the co-evolution approach can provide quicker search ability, and on the other hand, by using the co-evolution approach it is easier to perform simulation via a multi-agent system. In an engineering application, the approach can be studied in a multi-computer environment thereby reducing the time via parallel calculation.

The Nash optima [33] and [34] is deployed in HCPSO because the information sharing in Nash optima is simple and effective. Furthermore, in Nash optima, one agent, which has one objective, receives the information from other agents, and this is a good model for the multi-agent system in concept and computer realization.

In the multi-objective PSO method, sometimes the algorithm will generate local optima value and the ε -disturbance technique is deployed to avoid it. When both Pbest and Gbest stand on a fixed value and the particle position is stagnant on a boundary, a random ε -disturbance is needed to help the algorithm

jump out of the stagnation point. For a given step T, if the stagnant step ts > T, a random ε -disturbance is introduced to both Pbest and Gbest. For example, setting T=10 steps, the algorithm would check the value of Pbest and Gbest at every step. If both Pbest and Gbest keep the same values as the last step, the counter in algorithm will increase by one. In the next iteration, if both Pbest and Gbest still keep the same values, the counter will further increase by one, otherwise the counter returns to zero. When the counter is equal to 10, the algorithm will give a random ε -disturbance value to change Pbest and Gbest, so as to keep the particles moving.

For an optimisation problem with K design variables and M objectives, the algorithm would employ N particles to run optimisation and N should be multiples of M. Firstly, HCPSO divides N particles into M sub-swarm group according to objectives. Secondly, the design variables, K, are also divided into $K_1, K_2, ..., K_m$ sub-groups according to the objectives. This means every sub-swarm group has its own corresponding objectives and design variables. Then every sub-swarm group optimises relevant design variables according to relevant objectives in its own group. The optimised result would be sent to the "public board" as shared information. In the next step, the sub-swarm group would read other design variables and corresponding information from the public board as an update. At last, when a Nash Equilibrium is reached, the algorithm gives the final results. In every sub-swarm, in order to give enough pressure to push the solution space to Pareto space, particles in two generations are compared to update the position.

Algorithm HCPSO

The step-wise description of the proposed algorithm, HCPSO, is given below and shown in Fig.1:

- 1. initialize the population including position and velocity;
 - (i) create a public-board to store information; the public-board is a simple database to store all particles' information;
 - (ii) give the number of sub-swarms and size of each sub-swarm;
 - (iii) divide the population into sub-swarms;
- 2. every sub-swarm begins iteration; for example (m^{th} sub-swarm with (N/M) particles and K_m design variables);
- 3. read information from public-board and calculate fitness;
- 4. update Pbest via comparing individual position history according to mth objective ;
- 5. non-dominated sorting via Pareto-based approach;
- 6. give pointed number of best ranking particles to the public-board;
- 7. collect particles in step 6 from all sub-swarm to the public-board and form Gbest pool;
- 8. every sub-swam randomly selects Gbest from the pool;
- 9. compare Pbest and Gbest with past values to decide whether to introduce ɛ-disturbance or not;
- 10. calculate velocity and give limit velocity;
- 11. update and limit the position of particles;
- 12. combine last iteration particles with this iteration to form a new group with 2*(N/M) population and perform non-dominated sorting via Pareto-based approach;

13. select first (N/M) particles from new group with $2^{*}(N/M)$ population in step 12 and update position and velocity;

- 14. send corresponding information to the public-board;
- 15. if every solution can not be improved, stop and if it can be improved, continue iteration;

16. output final results;

Sub-swarm partition

In HCPSO, the whole swarm is divided into different sub-swarms according to the number of objectives. If an optimisation problem has M objectives, the swarm is divided in to M sub-swarms. The relationship between variable and sub-swarm is very important. For special objective functions, detailed analysis of these relationships should be processed before the partition. For example, a two objective problem: $f_1(x) = x_1, f_2(x) = g(x_2, x_3, ..., x_n)$;, following the above principle, the swarm should be divided into two sub-swarms. The first choice of variables is allocated to the first sub-swarm which contains variable x_1 and second sub-swarm includes the variables from x_2 to x_n .

The second choice is averaged out and every sub-swarm has half variables. In a particle application in engineering, when the relationship is unclear, the average distribution is recommended.

Information sharing mechanism

The information sharing mechanism is realised through a public-board in sub-swarm optimisation. The public-board concept in HCPSO comes from a multi-agent system environment. For easy and efficient communication in an agent environment, a black board is used for sharing the public information. The same mechanism is used here, and the black board is called a public board for public information sharing. In every sub-swarm, the particles optimise variables according to the sub-swarm optimisation objective, and send the information, including the optimised objective value, the best particle location etc. to the public board in the system. In synchronization, the sub-swarm reads the information from the other sub-swarm optimisation as the information for the next step.

Pbest and Gbest updating

The Pbest updating in HCPSO adopts the updating inside sub-swarm while Gbest uses updating outside sub-swarm. For Pbest, the particle in n^{th} sub-swarm compares the corresponding objective fitness value between the current position and the previous best position. If the current position in the n^{th} objective fitness is better than the previous value, the Pbest is replaced by the current value or if the current value is not better, then the previous value is retained.

The Gbest selection uses the Gbest pool in the public board. Every sub-swarm provides its best value to the public board and constructs a Gbest pool. HCPSO randomly selects a particle as the Gbest position from the Gbest pool.

Particle updating

In order to give enough pressure to Pareto front, an updating position approach is used to mutate every particle. In every sub-swarm, the system will compare the fitness in the last generation and the current generation (size of population is $2 \times N/M$), then select N/M position as this generation; some particles hold their own position and others will be replaced by the nearest neighbour.



Fig. 1. Flow chart of HCPSO algorithm.

4 Experiments 4.1 Test Functions

From the related literature, eight multi-objective test functions (Table1), are selected to evaluate this algorithm. Deb [35] introduced the design of a multi-objective test problem for EAs (Evolutionary Algorithms) and the test problems in Table 1 are chosen following the principles of Deb. Test 1 is selected by Pinto etc. [17] as a convex Pareto front. Test 2 is ZDT1 function in Zitzler etc. [36] with continuous Pareto front and a uniform distribution of solutions across the front. Test 3 is ZDT2 in which the Pareto front is not convex. Test 4 is obtained combining the test function of Test 2 and Test 3 (Jin et al. 2001) and explored by Pinto etc. [17]. Test 4 is neither purely convex nor purely non convex. Test 5 is ZTD3, which is difficult for a discontinuous Pareto front. Test 6 is ZTD4 and the difficulty of this problem is that the sheer number of multiple local Pareto-optimal fronts produce a large number of hurdles for an algorithm to converge to the global Pareto-optimal front.

Table 1

Two-objectiv	Two-objective test problems selected to evaluate HCPSO algorithm.								
Name	Variables n	Range	Test Function						
Test 1	30	[0,1]	$\begin{cases} f_1(x) = \frac{1}{n} \sum_{i=1}^n x_i^2, \\ f_2(x) = \frac{1}{n} \sum_{i=1}^n (x_i - 2)^2. \end{cases}$						
Test 2	30	[0,1]	$\begin{cases} f_1(x) = x_1, f_2(x) = g(x)h(f_1(x), g(x)). \\ g(x_2,, x_m) = 1 + \frac{9}{n-1} \sum_{i=2}^n x_i, \\ h(f_1, g) = 1 - \sqrt{f_1 / g}. \end{cases}$						
Test 3	30	[0,1]	$\begin{cases} f_1(x) = x_1, f_2(x) = g(x)h(f_1(x), g(x)) \\ g(x_2,, x_m) = 1 + \frac{9}{n-1} \sum_{i=2}^n x_i, \\ h(f_1, g) = 1 - (f_1 / g)^2. \end{cases}$						
Test 4	30	[0,1]	$\begin{cases} f_1(x) = x_1, f_2(x) = g(x)h(f_1(x), g(x)) \\ g(x_2, \dots, x_m) = 1 + \frac{9}{n-1} \sum_{i=2}^n x_i, \\ h(f_1, g) = 1 - \sqrt[4]{f_1 / g} - (f_1 / g)^4. \end{cases}$						
Test 5	30	[0,1]	$\begin{cases} f_1(x) = x_1, f_2(x) = g(x)h(f_1(x), g(x)) \\ g(x_2,, x_m) = 1 + \frac{9}{n-1} \sum_{i=2}^n x_i, \\ h(f_1, g) = 1 - \sqrt{f_1 / g} - (f_1 / g) \sin(10\pi f_1). \end{cases}$						

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Test 6 10
$$x_{1} \in [0,1], \\ x_{i} \in [-5,5], \\ i = 2,...30; \end{cases} \begin{cases} f_{1}(x) = x_{1}, f_{2}(x) = g(x)h(f_{1}(x), g(x)) \\ g(x_{2},...,x_{m}) = 1 + 10(n-1) + \sum_{i=2}^{n} (x_{i}^{2} - 10\cos(4\pi x_{i})), \\ h(f_{1},g) = 1 - \sqrt{f_{1}/g}. \end{cases}$$

Two three-objective test functions are selected according to Deb [37] in Table 2. Test 7 is DTLZ2 and is used here to investigate HCPSO's ability to scale up its performance in a large number of objectives. Test 8, as DTLZ4, is selected to test HCPSO's ability to maintain a good distribution of solutions.

Table 2

Infee-objective test problems selected to evaluate HCPSO algorithm.									
Name	Variables n	Range	Test Function						
Test 7	12	[0,1]	$\begin{cases} f_1(x) = (1 + g(x_M))\cos(x_1\pi/2)\cos(x_2\pi/2) \\ f_2(x) = (1 + g(x_M))\cos(x_1\pi/2)\sin(x_2\pi/2) \\ f_3(x) = (1 + g(x_M))\sin(x_1\pi/2) \\ g(x_M) = \sum_{x_i \in x_M} (x_i - 0.5)^2 \end{cases}$						
Test 8	12	[0,1]	$\begin{cases} f_1(x) = (1 + g(x_M))\cos(x_1^{100}\pi/2)\cos(x_2^{100}\pi/2) \\ f_2(x) = (1 + g(x_M))\cos(x_1^{100}\pi/2)\sin(x_2^{100}\pi/2) \\ f_3(x) = (1 + g(x_M))\sin(x_1^{100}\pi/2) \\ g(x_M) = \sum_{x_i \in x_M} (x_i - 0.5)^2 \end{cases}$						

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4.2 Parameters Setting

As a critical parameter for the PSO's convergence behaviour, ω is utilised to control the impact of prior velocities. Usually, a large ω facilitates global exploration while a small one tends to facilitate local exploration. The experimental results indicate that it is better to set the inertia to a large value initially, in order to promote global exploration of the search space, and gradually decrease it in order to obtain more refined solutions. The proper setting of parameters c1 and c2 may result in faster convergence and alleviation of local minima. The constriction factor χ controls the magnitude of the velocities, in a similar way to the Vmax parameter. (Parsopoulos and Vrahatis [38])

The standard PSO is the original algorithm provided by Kennedy and Eberhard (literature?), which is similar to equation (1) but without χ . The coefficient ω is equal to 1 and $c_1 = c_2 = 2.0$.

In order to perform a comparison with regards to the rate of convergence between standard PSO and its improved form, two test functions in the literature are selected[39][40]:

1. De Jong's function

$$f(x) = \sum_{i=1}^{n} x_i^2, \quad -5.12 \le x_i \le 5.12$$

Global minimum f(x) = 0 is obtainable for $x_{i=0}, i = 1, ..., n$.

2. Griewangk's function

$$f(x) = \frac{1}{4000} \sum_{i=1}^{n} x_i^2 - \prod_{i=1}^{n} \cos(\frac{x_i}{\sqrt{i}}) + 1, \quad -600 \le xi \le 600$$

2D
$$f(x,y) = \frac{x^2 + y^2}{4000} - \cos(x)\cos(\frac{y}{\sqrt{2}}) + 1$$

Global minimum (x,y)=(0,0) f = 0;

For a better and more comprehensive comparison of the rate of convergence, the Genetic Algorithms (GA) are also included in the comparison, and the parameters used for each approach are listed in Table 3.

Table 3

The parameters used for standard PSO, improved PSO and GA in comparing the rate of convergence

Parameters Name	Standard PSO	Improved PSO	Parameters Name	Genetic Algorithms
Constriction function χ	N/A	0.72	Crossover rate	1
Initial inertia weight	1 (fixed)	1	Mutation rate	1/n
Final inertia weight	1 (fixed)	0.4	SBX	20
Cognitive parameter <i>c</i> 1	2	2	Polynomial Mutation	100
Social parameter c2	2	2	Selection Method	Tournament selection

The number of particles and generation for both standard PSO and improved PSO are set to 200 and 100 respectively. The population and the cycle number for the corresponding GAs are set to 200 and 100 respectively. Every algorithm is run for 10 times and the best solution out of 10 runs is selected as the overall best solution. For standard PSO the coefficients are fixed and adjusting the convergence depends on the Vmax, which is set to 2% of the range for this case.



Fig.2. Comparison of the rate of convergence between standard PSO, improved PSO and GA; (a) De Jong's function; (b) De Jong's function with average fitness range from 0 to 1; (c) Griewangk's function; (d) Griewangk's function with average fitness range from 0 to 10;

Typical convergence of average fitness values as a function of generations is shown in Fig.2. As far as De Jong's function is concerned, the rate of convergence for standard PSO is better than GA, but the rate of convergence for the improved PSO is the best among three algorithms. With regards to Griewangk's function (Figure (c) and (d)), the improved PSO is still the best one while GA performs better than standard PSO. The reason for this is that the standard PSO has to adjust itself through Vmax, which is difficult to control.

Clerc and Kennedy [41] have given a mathematical analysis of algorithm parameters and derived a reasonable set of turning parameters. Based on this, Trela [42] provides a direct and simple guideline for parameter selection. A convergence triangle is given as a diagram (Fig. 3). Trela transfers classic PSO formula to the following and makes c=d=1:

$$v_{k+1} = av_k + b_1r_1 (p_1 - x_k) + b_2r_2 (p_2 - x_k);$$

$$x_{k+1} = cx_k + dv_{k+1};$$

$$b = \frac{b_1 + b_2}{2};$$
(2)

Corresponding to (1), a and b can be expressed as:

$$\begin{cases} a = \chi \omega; \\ b = \frac{\chi (c_1 + c_2)}{2} \end{cases}$$
(3)

These parameters are critically important for PSO. The different parameters setting is given in Table 4. Test 2 is selected as a standard test function to evaluate the effort of parameters in HCPSO. The number of particles and generation are set to 200 and 50 respectively, in order to compare the final results (Fig. 3).

Table 4

HPSCO parameters used for the comparison of the rate of convergence on a multi-objective optimization problem --- Test 2 in Table 1;

Parameters Name	Choice 1	Choice 2	Choice 3	Choice 4
Constriction Function χ	0.72	0.72	-0.72	1.5
Initial inertia weight	1	1	1	0.6
Final inertia weight	0.4	0.4	0.4	0.6
Cognitive parameter $c1$	2	0.5	0.5	2
Social parameter $c2$	2	0.5	0.5	2
al	0.72	0.72	-0.72	0.9
a2	0.288	0.288	-0.288	0.9
b	1.44	0.36	-0.36	3



Fig. 3. Comparison of results for the rate of convergence on a multi-objective optimization problem --- Test 2 in Table 1;

The line 1 in Fig. 3 is a zigzagging line and line 2 is a harmonic oscillation line. As can be seen from Fig. 3, choices 1 and 2 fit well after optimisation, but choice 3 and choice 4 can not fit Pareto solutions. Fig. 3 displays that the principle of Trelea is applicable to HCPSO.

4.3 Performance Metrics

Two evaluation criteria are selected: [35]

(1) GD (Generational Distance) finds an average of the solutions of Q from P* (Q is solution and p* is a known set of the Pareto-optimal)

$$GD = \frac{\left(\sum_{i=1}^{|\mathcal{Q}|} d_i^p\right)^{1/p}}{|\mathcal{Q}|}$$

For a two objective problem (p=2), d_i is the Euclidean distance between the solution $i \in Q$ and nearest member of P*.

(2) SpreadDeb et al. [35] suggested the following metric to alleviate the above difficulty

$$\Delta = \frac{\sum_{m=1}^{M} d_{m}^{e} + \sum_{i=1}^{M} |d_{i} - \overline{d}|}{\sum_{m=1}^{M} d_{m}^{e} + |Q|\overline{d}}$$

where \overline{d} can be any distance measured between neighbouring solution and \overline{d} is the mean value of the above distance measure. The parameter d_m^e is the distance between the extreme solutions of P* and Q, corresponding to mth objective function.

4.3 Results

The HCPSO is run 10 times and real-coded NSGAII, a multi-objective genetic algorithm, is used for comparison. In HCPSO, the parameters are set as following: the population of swarm is 200 and generation is 100 iteration steps. c_1 and c_2 are set to 0.5 while ω is gradually decreased from 1.0 to 0.4. Vmax is set to the boundaries of decision variable ranges. χ is 0.72. The ε -disturbance has 3 steps. The number of sub-swarm is 2 and population of sub-swarm is 100. In NSGAII, the number of individuals is 200 and the number of generation is set to 100. The SBX (Simulated binary crossover) is used with $\eta_c = 10$ and the polynomial mutation is used with $\eta_m = 20$. The crossover and mutation probabilities are set to 0.9 and 1/n respectively. The parameters of NSGAII are selected according to prior study, (Turkmen 2005 [43]). The results of performance metrics of Test 1 to 6 are averaged and summarised in Table 5. The non-dominated solutions found by HCPSO for all test functions are



displayed in Fig. 4 and they all perform very well for both 2D and 3D objectives. The HCPSO gives the last generation results as non-dominated solutions.



Fig. 4. Non-dominated solutions found by HCPSO on test functions in Table 1 with Pareto Fronts

Table 5

Comparison of mean and variance values of convergence metric GD and diversity metric Δ on six two-objective problems;

Algorithm	Test	t 1	Test	t 2	Test 3	
Algorithm	GD	δ_{GD}^{2}	GD	δ_{GD}^{2}	GD	δ_{GD}^{2}
HCPSO	2.35E-03	8.92E-05	1.12E-03	7.68E-05	8.22E-04	8.46E-04
NSGAII	2.42E-03	9.11E-05	1.85E-03	9.25E-05	9.57E-04	8.40E-04
	Δ	δ_{Δ}^{2}	Δ	δ_{Λ}^{2}	4	δ_{Λ}^{2}
HCPSO	4.12E-01	3.56E-02	3.86E-01	1.82E-02	3.82E-01	2.56E-02
NSGAII	4.29E-01	3.80E-02	4.72E-01	4.60E-02	4.80E-01	3.15E-02
Algorithm	Test 4		Test 5		Tes	t 6
Algorithm	GD	δ_{GD}^{2}	GD	δ_{GD}^{2}	GD	δ_{GD}^{2}
HCPSO	6.19E-03	3.81E-03	6.72E-03	6.92E-03	7.13E-03	8.13E-03
NSGAII	2.91E-02	8.52E-02	3.60E-02	3.82E-02	6.20E-02	4.56E-02
	Δ	δ_{Δ}^{2}	Δ	δ_{Λ}^{2}	Δ	δ_{Δ}^{2}
HCPSO	6.12E-01	2.82E-02	6.88E-01	2.12E-02	7.47E-01	4.67E-02
NSGAII	9.80E-01	3.93E-02	7.41E-01	2.60E-02	8.32E-01	3.55E-02

As can be seen in Table 5, in comparison to NSGAII, the HCPSO can perform very well for all six standard multi-objective optimisation test functions, which are tested in this paper.

For checking the rate of convergence, the convergence history of two algorithms on test 2 is given in Fig. 5. As it can be seen in Fig. 5, the HCPSO is converging faster (approximately 60%) than NSGAII and this means a significant reduction in computing time.





Fig. 5. Comparison of convergence history of HCPSO and NSGAII on a two-objective optimization problem --- Test 2 in Table 1;

5. Case Study in Ship Design

Due to the well publicised accidents in recent years, with the loss of many lives, Ropax vessels have gone through significant design changes, while the demand for passenger and cargo capacity in European waters has increased. Following the tragic accidents of the Herald of Free Enterprise in 1987 and the Estonia in 1994, a significant surge of research related to the capsizing of Roll on - Roll

off type ships was initiated. The 'Water on Deck' standards, which are known as Stockholm Agreement [44] determines the limiting wave height (Hs) in which a ROPAX vessel survives in a damaged condition. In response to these regulations, the shipping industry is in search of new modern designs to match these high safety standards, while maximizing the cargo capacity of vehicles in a cost effective approach.

The changes in design focus on the damage stability and survivability, cargo and passenger capacity. Therefore, the internal hull subdivision layout is an important problem especially for damage stability, survivability, internal cargo capacity and the general arrangement of the vessel.

In literature, different solution methods have been proposed. Sen and Gerick (1992) [45] suggested using a knowledge-based expert system for subdivision design using the probabilistic regulations for passenger ships. Zaraphonitis et al. [46] proposed an approach for the optimisation of Ro-Ro ships in which centre-casing, side-casing, bulkhead deck height and locations of transverse bulkheads are treated as optimisation variables. Ölçer et al. [47] studied the subdivision arrangement problem of a ROPAX vessel and evaluated conflicting designs in a totally crisp environment where all the parameters are deterministic. They also examined the same case study in a fuzzy multiple attributive group decision-making environment, where multiple experts are involved and available assessments are imprecise and deterministic (Ölçer et al. [48]). Turan et al. (2004) [49] approached the subdivision problem by using the case-based reasoning approach. Turkmen et al. (2005) [43] proposed NSGAII with TOPSIS (Technique for Order Preference by Similarity to Ideal Solution) to perform design optimisation for internal subdivision.

5.1 Problem Modelling

The case study naturally focuses on improving the performance of the Ropax vessels in terms of not only maximising the ship related parameters mentioned above but also reducing the time to perform the multi-objective design iteration.

As this study is based on the previous work of Ölçer et al. [47], [48] and Turkmen et al. [50] the same problem is selected and used in this study. The optimisation problem is an internal hull subdivision optimisation for a ROPAX vessel whose main particulars are given in Table 6. Therefore the main aim of this case study is to maximise the survivability and damage stability standards, as well as to improve the cargo capacity. These three parameters form the objectives of the study as presented in Table 7.

The recently developed 'Static Equivalent Method (SEM)' [51] is used to calculate the limiting significant wave height (H_s) value for the worst SOLAS'90 damage, determined from damage stability calculations.

The Stockholm 'Water on Deck' standards, which are applied specifically for Ropax vessels, determine the maximum significant wave height at which the Ropax vessel can survive and therefore is allowed to operate in wave heights, which are equal to or less than the maximum wave height. The Stockholm agreement allows model tests for demonstration of compliance to determine the maximum

wave height as an equivalent approach. The SEM is an empirical capsize model for Ro-Ro ships that can predict with reasonable accuracy the limiting sea-state for specific damage conditions. The SEM for Ro–Ro ships postulates that the ship capsizes quasi-statically, as a result of an accumulation of a critical mass of water on the vehicle deck, the height of which above the mean sea surface uniquely characterises the ability of the ship to survive in a given critical sea state. This method was developed following observations of the behaviour of damage ship models in waves and it was validated using several model experiments and a large number of numerical simulations. Therefore, in this particular case study, SEM is used as an equivalent approach to the Stockholm Agreement.

Table 6

Length overall(L _{oa})	194.4 m
Length between perpendiculars (L _{bp})	172.2 m
Breadth moulded (B)	28.4 m
Depth to car deck	9.7 m
Lower hold height (m)	2.6 m
Depth to upper deck	15.0 m
Draught design (T)	6.6 m
Displacement	20200 ton
Max number of persons on board	2660
Number of car lanes	8

Main dimensions of the vessel used in the case study.

There are three objectives and 16 design variables in this study (Table 7). Three of the design variables are: the depth of the ship to the car deck 'Car Deck Height', 'Lower Hold Height' and the width of the side casing at the car deck, 'Side Casing Width'. As presented, the original design has a 9.7 m depth to car deck, a 2.6 m lower deck height and no side casings at the car deck (Fig. 10 a). The remaining 13 design parameters are the locations of transverse bulkheads given in the format of frame numbers (starting from the stern of the ship). Table 7 also presents the lower and upper boundaries of the parameters with assigned increments to be used in the optimisation study.

Table 7

Optimisation variables with their types, boundaries, and objectives.

-						_	
		Original	Туре		Boundaries		
No	Variables	design	Discrete	Cont.	Lower	Upper	Increment
1	Car deck height	9.7 m			9.6m	9.9m	0.025m
2	Lower-hold height	2.6m			2.6m	5.2m	2.6
3	Side casing width	No	\checkmark		1m	2m	0.5m
4	Transverse Bulkhead 02	27			25	29	1
5	Transverse Bulkhead 03	39			37	41	1
6	Transverse Bulkhead 04	51	\checkmark		49	53	1
7	Transverse Bulkhead 05	63	\checkmark		61	65	1
8	Transverse Bulkhead 06	81			79	83	1
9	Transverse Bulkhead 07	99			97	101	1

10	Transverse Bulkhea	ıd 08	117			115	119	1	
11	Transverse Bulkhea	ıd 09	129			127	131	1	
12	Transverse Bulkhea	id 10	141			139	143	1	
13	Transverse Bulkhea	ıd 11	153			151	155	1	
14	Transverse Bulkhea	ıd 12	165			163	167	1	
15	Transverse Bulkhea	ıd 13	177			175	179	1	
16	Transverse Bulkhea	ıd 14	189			187	191	1	
Bou	Boundaries for transverse bulkheads are given in frame numbers								
No	Objectives		Туре			Descript	tion		
1	H _s value	M	aximization	for t	he worst t	wo compartme	nt damage	case	
2	KG limiting value	М	aximization	for t	for the worst two compartment damage case			case	
3	Cargo capacity	М	aximization	expi	expressed in car lanes				
	value								

The damage stability has been calculated according to the constraints of SOLAS'90 regulations as shown in Table 8.

Table 8

Constraints of SOLAS'90 requirements

No	Constraints	Requirements			
1	Range	Range of positive stability up to 10 degrees			
2	Min. GZ Area	Minimum area of GZ-curve more than			
		0.015mrad			
3	Maximum GZ	Maximum righting lever more than 0.1m			
4	Maximum GZ due to	Maximum righting lever after applied wind			
	Wind Moment	moment more than 0.04m			
5	Maximum GZ due to	Maximum righting lever after passenger			
	Passenger Moment	crowding more than 0.04m			
6	Maximum Heel	Maximum static heel less than 12degrees			
7	Minimum GM	Minimum GM more than 0.05m			
8	Margin Line	Margin line should not be immersed			
9	Progressive Flooding	No progressive flooding should occur			

JAVA language is used to code the optimisation system according to the multi-agent structure and the calculation is processed between the optimisation system and the NAPA software [52]. The Visual Basic (VB) is used to form the interface. The optimisation system uses NAPA to calculate the Hs, KG limiting and Cargo Capacity, and after optimisation, modified design variables are transferred to NAPA (Fig. 6).



Fig. 6. Work flow between the Optimisation System and third party software NAPA

The vessel is modelled in NAPA (Fig. 7) and can be modified for each design experiment (or design layout) with respect to each optimisation parameter via NAPA macro. For each design experiment, the relevant adjustments of Draught and Displacement are made during the optimisation process (Fig. 8).



Fig. 7. Ship model built in NAPA for optimization.

 NAME Ship Design Syst 	tem Input			NAME Ship Design System Running	
File Edit Tools windows Help Design Objective Objective 1 Objective 2	Selection	Design Constrains Add a new constrains	Line La	ShipModel HCPSO Particle Management Generation 1990 Link to NAPA	
Objective 3	Cargo capacity •				
Design Variable 1	Car deck height	Design Variable 9	Transverse Bulkheas •		
Design Variable 2	Lower-hold height	Design Variable 10	Transverse Bulkheas •		
Design Variable 3	Transverse Bulkheas •	Design Variable 11	Transverse Buildnea 💌		
Design Variable 4	Transverse Bulkheas •	Design Variable 12	Transverse Bulkhea		
Design Variable 5	Transverse Bolkhea •	Design Variable 13	Transverse Bulkheas •		
Design Variable 6	Transverse Buikheas •	Design Variable 14	Transverse Bulkhea		
Design Variable 7	Transverse Bulkheas •	Design Variable 15	Transverse Bulkheas •	LE FLET	

Fig. 8. Interface of ship design optimisation system.

5.2 Result and Analysis

TODOO D

The calculations are performed using both NSGAII and HCPSO, and the results are compared in terms of the numerical value of objectives and the computing time that each approach takes.

This optimisation has three objectives to maximize, thus three sub-swarms are set. The population size is 30 and the generation is 100. Therefore every sub-swarm has 10 particles. c_1 and c_2 are set to 2.0. ω is gradually decreased from 1.0 to 0.4. Vmax is set to the bounds of decision variable ranges. χ is 0.72. The ε -disturbance has 3 steps. The NSGA II uses the parameters setting of prior research in the same environment [49]. The HCPSO and NSGAII parameters are listed in Table 9.

Table 9

HCPSO Para	meters' Setting	NSGAII Parameters' Setting			
Parameters Name	Parameters Value	Parameters Name	Parameters Value		
Constriction Function	0.72	SBX (Simulated binary crossover)	10		
Inertia weight	1.0 to 0.4	polynomial mutation	20		
Cognitive parameter	2	crossover probabilities	0.9		
Social parameter	2	mutation probabilities	0.1		
Population	30	Population	30		
Generation	100	Generation	100		

• • • • •

The setting of the parameters in the case study for HCPSO and NSGAII

The optimisation is performed using a PC (Dual Core 2.4GHz, 3 GB RAM) environment and takes 80h (Fig. 9). At the end of this run, 2625 different designs are obtained in design space, with 615 of them being unfeasible designs. Therefore 2010 (=2625-615) feasible designs are filtered in design space to obtain only the designs that belong to the Pareto front. The selected HCPSO optimisation solutions are listed in Table 10 together with the NSGAII optimisation. The comparison of the original design and the selected design in amidships is also given in Fig. 10. In this solution (Table 10), the Hs in HCPSO is improved by more than 0.55 m compared to the original design, while the number of car lanes is increased by 6 extra lanes, which is equivalent to an increase of above 50%. The KG limiting value is also increased significantly (0.9 m) thus provides flexibility for future modifications on the basis of changing passenger demands as well as improvement in survivability. When comparing the two optimisation methods, the HCPSO design improves both the limiting KG and significant wave height (Hs) by 0.1m, compared to the NSGAII design. Both methods provide the same solution for the cargo capacity by increasing the lower-hold height and car deck height, thus yielding more cargo capacity.

More importantly, for the real design case application, compared to NSGAII, HCPSO converges faster and reduces the computing, and hence the design time significantly. In ship design, most of the computing time is not consumed on the optimisation approach, but rather on the naval architectural calculations using third party software (NAPA etc.). It is important to note that it takes sometimes hours for one fitness calculation [16]. In this study, the solution begins converging from 40th generations in HCPSO, while the NSGAII begins converging from 54th generation in NSGAII. This

means the HCPSO takes 35% less time in looking for Pareto solutions compared to NSGAII. In a more complex environment, such as a real ship application with many objectives, this provides an advantage in terms of completing the design faster and thus cheaper.



Fig. 9. Optimisation results of HCPSO; (a) Limiting KG vs Hs; (b) Cargo Capacity vs Limiting KG; (c) Cargo Capacity vs Hs (d) 3D optimization feasible designs

All feasible results are given in Fig. 8. The relationships between different variables are shown for designers to make a direct observation and to select the appropriate solution according to their practical preference. All of the feasible designs are listed in 3D space (Fig. 9 d).

Table 10

Comparison of the original design and selected designs which are optimal solutions for HCPSO and NSGAII

No	Optimisation Variables	Original Design	NSGAII Design	HCPSO design
1	Car deck height	9.7 m	9.9m	9.9m

2	Lower-hold height (from car deck)	2.6m	5.2m	5.2m
3	Side Casing width (m)	No side-casing	1m	1m
	Watertight transverse bulkheads			
	(In frame numbers)			
4	Transverse Bulkhead 02	27	27	27
5	Transverse Bulkhead 03	39	39	39
6	Transverse Bulkhead 04	51	52	53
7	Transverse Bulkhead 05	63	65	63
8	Transverse Bulkhead 06	81	83	83
9	Transverse Bulkhead 07	99	97	99
10	Transverse Bulkhead 08	117	115	118
11	Transverse Bulkhead 09	129	128	130
12	Transverse Bulkhead 10	141	141	143
13	Transverse Bulkhead 11	153	153	155
14	Transverse Bulkhead 12	165	164	167
15	Transverse Bulkhead 13	177	175	179
16	Transverse Bulkhead 14	189	189	189
	Optimisation Objectives			
1	H _s value (m)	4.641	5.082	5.179
2	KG limiting value (m)	14.012	14.813	14.9085
3	Cargo capacity value (lanes)	8	14	14



(a) Original design (b) selected design **Fig. 10.** Comparison between original design and selected design based on HCPSO.

6. Conclusions

This paper presents a new hybrid approach, HCPSO, which is a co-evolutionary based Multi-Objective Particle Swarm Optimisation methodology. The proposed algorithm is tested and validated successfully utilising the most widely used 2D and 3D test functions and applied on a real design case study with three objectives. In test functions, HCPSO converges significantly faster than NSGAII and provides 3D solutions using PSO comfortably.

With regards to the real ship design case, the internal subdivision optimisation of a ROPAX vessel, with three conflicting objectives (survivability, damage stability and cargo capacity), is carried out. For the search platform, a JAVA based optimisation system and NAPA have been integrated into a multi-agent search framework.

The proposed algorithm provides an improved design, compared to the original design, in every chosen objective with a significant margin, and demonstrates the value of HCPSO. In this design case, the HCPSO displays a better performance both in speed and final results compared to NSGAII. The co-evolution method used in HCPSO provides a good basis for distributed calculation and allows sub-swarm being updated dynamically. The proposed algorithm is structured via a multi-agent system and every agent works remarkably well. It can be concluded that the proposed approach has shown great potential and can be applied to similar and even more complex optimisation problems in ship design, as well as to related areas within the maritime industry.

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