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# Optical Solar Sail Degradation Modeling

**Bernd Dachwald<sup>1</sup>, Giovanni Mengali<sup>2</sup>, Alessandro A. Quarta<sup>2</sup>,  
Malcolm Macdonald<sup>3</sup>, Colin R. McInnes<sup>4</sup>**

<sup>1</sup>German Aerospace Center (DLR), Oberpfaffenhofen, Germany

<sup>2</sup>University of Pisa, Italy

<sup>3</sup>SciSys Ltd., Bristol, UK

<sup>4</sup>University of Strathclyde, Glasgow, Scotland, UK

1st International Symposium on Solar Sailing  
27–29 June 2007, Herrsching, Germany

# The Problem

- The optical properties of the thin metalized polymer films that are projected for solar sails are assumed to be affected by the erosive effects of the space environment
- Optical solar sail degradation (OSSD) in the real space environment is to a considerable degree indefinite (initial ground test results are controversial and relevant in-space tests have not been made so far)
- The standard optical solar sail models that are currently used for trajectory and attitude control design do not take optical degradation into account  
→ its potential effects on trajectory and attitude control have not been investigated so far
- Optical degradation is important for high-fidelity solar sail mission analysis, because it decreases both the magnitude of the solar radiation pressure force acting on the sail and also the sail control authority
- **Solar sail mission designers necessitate an OSSD model to estimate the potential effects of OSSD on their missions**

# Our Approach

- We established in November 2004 a "Solar Sail Degradation Model Working Group"<sup>1</sup> (SSDMWG) with the aim to make the next step towards a realistic high-fidelity optical solar sail model
- We propose a simple parametric OSSD model that describes the variation of the sail film's optical coefficients with time, depending on the sail film's environmental history, i.e., the radiation dose
- The primary intention of our model is not to describe the exact behavior of specific film-coating combinations in the real space environment, but to provide a more general parametric framework for describing the general optical degradation behavior of solar sails

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<sup>1</sup>the authors and Volodymyr Baturkin, Victoria L. Coverstone, Benjamin Diedrich, Gregory P. Garbe, Marianne Görlich, Manfred Leipold, Franz Lura, Leonel Rios-Reyes, Daniel J. Scheeres, Wolfgang Seboldt, Bong Wie

# Overview

Different levels of simplification for the optical characteristics of a solar sail result in different models for the magnitude and direction of the SRP force:

## Model IR (Ideal Reflection)

Most simple model

## Model SNPR (Simplified Non-Perfect Reflection)

Optical properties of the solar sail are described by a single coefficient

## Model NPR (Non-Perfect Reflection)

Optical properties of the solar sail are described by 3 coefficients

## Generalized Model by Rios-Reyes and Scheeres

Optical properties are described by three tensors. Takes the sail shape and local optical variations into account

## Refined Model by Mengali, Quarta, Circi, and Dachwald

Optical properties depend also on light incidence angle, surface roughness, and temperature

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# The Non-Perfectly Reflecting Solar Sail

The non-perfectly reflecting solar sail model parameterizes the optical behavior of the sail film by the optical coefficient set

$$\mathcal{P} = \{\rho, s, \varepsilon_f, \varepsilon_b, B_f, B_b\}$$

The optical coefficients for a solar sail with a highly reflective aluminum-coated front side and with a highly emissive chromium-coated back side are:

$$\mathcal{P}_{Al|Cr} = \{\rho = 0.88, s = 0.94, \varepsilon_f = 0.05, \\ \varepsilon_b = 0.55, B_f = 0.79, B_b = 0.55\}$$

## Nomenclature

$\rho$ : reflection coefficient

$s$ : specular reflection factor

$\varepsilon_f$  and  $\varepsilon_b$ : emission coefficients of the front and back side, respectively

$B_f$  and  $B_b$ : non-Lambertian coefficients of the front and back side, respectively

# Overview (Reprise)

## Model IR (Ideal Reflection)

Most simple model

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Optical properties depend also on light incidence angle, surface roughness, and temperature

Those models do not include **optical solar sail degradation (OSSD)**

# Data Available From Ground Testing

- Much ground and space testing has been done to measure the optical degradation of metalized polymer films as second surface mirrors (metalized on the back side)
- No *systematic* testing to measure the optical degradation of candidate solar sail films (metalized on the front side) has been reported so far and preliminary test results are controversial
  - ▶ Lura et. al. measured considerable OSSD after combined irradiation with VUV, electrons, and protons
  - ▶ Edwards et. al. measured no change of the solar absorption and emission coefficients after irradiation with electrons alone
- Respective in-space tests have not been made so far
- The optical degradation behavior of solar sails in the real space environment is to a considerable degree indefinite

# Simplifying Assumptions

For a *first* OSSD model, we have made the following simplifications:

- 1 The only source of degradation are the solar photons and particles
- 2 The solar photon and particle fluxes do not depend on time (average sun without solar events)
- 3 The optical coefficients do not depend on the sail temperature
- 4 The optical coefficients do not depend on the light incidence angle
- 5 No self-healing effects occur in the sail film

## Solar radiation dose (SRD)

Let  $p$  be an arbitrary optical coefficient from the set  $\mathcal{P}$ . With OSSD,  $p$  becomes time-dependent,  $p(t)$ . With the simplifications stated before,  $p(t)$  is a function of the **solar radiation dose**  $\tilde{\Sigma}$  (dimension  $[\text{J}/\text{m}^2]$ ) accepted by the solar sail within the time interval  $t - t_0$ :

$$\tilde{\Sigma}(t) \triangleq \int_{t_0}^t S \cos \alpha dt' = S_0 r_0^2 \int_{t_0}^t \frac{\cos \alpha}{r^2} dt'$$

SRD per year on a surface perpendicular to the sun at 1 AU

$$\tilde{\Sigma}_0 = S_0 \cdot 1 \text{ yr} = 1368 \text{ W}/\text{m}^2 \cdot 1 \text{ yr} = 15.768 \text{ TJ}/\text{m}^2$$

## Dimensionless SRD

Using  $\tilde{\Sigma}_0$  as a reference value, the SRD can be defined in dimensionless form:

$$\Sigma(t) = \frac{\tilde{\Sigma}(t)}{\tilde{\Sigma}_0} = \frac{r_0^2}{T} \int_{t_0}^t \frac{\cos \alpha}{r^2} dt' \quad \text{where} \quad T \triangleq 1 \text{ yr}$$

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$\Sigma(t)$  depends on the solar distance history and the attitude history  $\mathbf{z}[t] = (r, \alpha)[t]$  of the solar sail,  $\Sigma(t) = \Sigma(\mathbf{z}[t])$

## Differential form for the SRD

The equation for the SRD can also be written in differential form:

$$\dot{\Sigma} = \frac{r_0^2}{T} \frac{\cos \alpha}{r^2} \quad \text{with} \quad \Sigma(t_0) = 0$$

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Assumption that each  $p$  varies exponentially with  $\Sigma(t)$

Assume that  $p(t)$  varies exponentially between  $p(t_0) = p_0$  and  $\lim_{t \rightarrow \infty} p(t) = p_\infty$

$$p(t) = p_\infty + (p_0 - p_\infty) \cdot e^{-\lambda \Sigma(t)}$$

The **degradation constant**  $\lambda$  is related to the "half life solar radiation dose"  $\hat{\Sigma}$  ( $\Sigma = \hat{\Sigma} \Rightarrow p = \frac{p_0 + p_\infty}{2}$ ) via

$$\lambda = \frac{\ln 2}{\hat{\Sigma}}$$

Note that this model has 12 free parameters additional to the 6  $p_0$ , 6  $p_\infty$  and 6 half life SRDs  $\hat{\Sigma}_p$  (too much for a simple parametric OSSD analysis)

Reduction of the number of model parameters

We use a degradation factor  $d$  and a single half life SRD for all  $p$ ,  $\hat{\Sigma}_p = \hat{\Sigma} \forall p \in \mathcal{P}$

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## EOL optical coefficients

Because the reflectivity of the sail decreases with time, the sail becomes more matt with time, and the emissivity increases with time, we use:

$$\begin{aligned} \rho_\infty &= \frac{\rho_0}{1+d} & s_\infty &= \frac{s_0}{1+d} & \varepsilon_{f\infty} &= (1+d)\varepsilon_{f0} \\ \varepsilon_{b\infty} &= \varepsilon_{b0} & B_{f\infty} &= B_{f0} & B_{b\infty} &= B_{b0} \end{aligned}$$

## Degradation of the optical parameters in dimensionless form

$$\frac{p(t)}{p_0} = \begin{cases} (1 + de^{-\lambda\Sigma(t)}) / (1 + d) & \text{for } p \in \{\rho, s\} \\ 1 + d(1 - e^{-\lambda\Sigma(t)}) & \text{for } p = \varepsilon_f \\ 1 & \text{for } p \in \{\varepsilon_b, B_f, B_b\} \end{cases}$$

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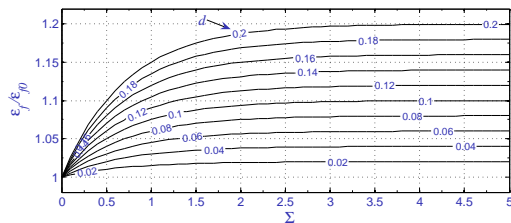
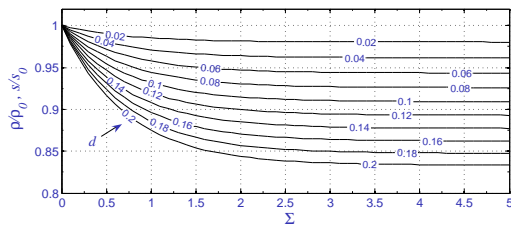
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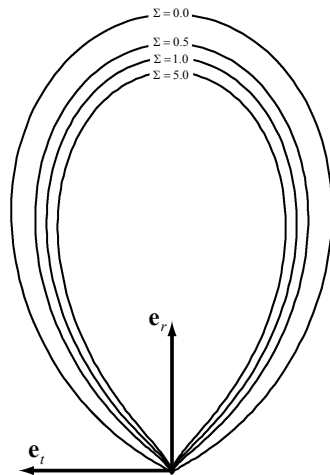


# OSSD Effects

on the optical coefficients and the SRP force bubble



"degradation" of optical coefficients



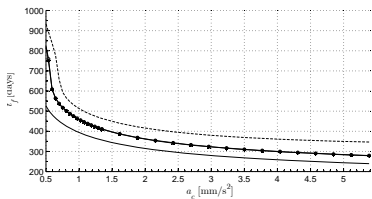
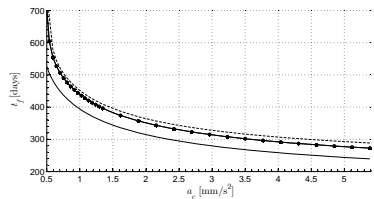
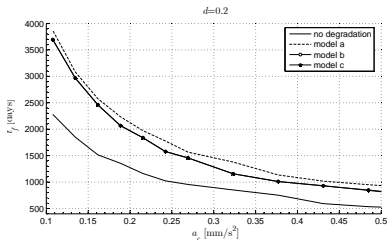
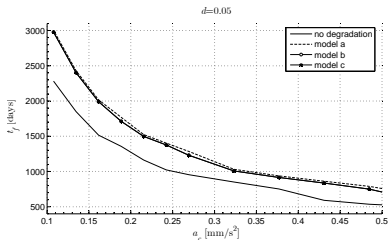
"degradation" of SRP force bubble

# Mars Rendezvous

- Solar sail with  $0.1 \text{ mm/s}^2 \leq a_c < 6 \text{ mm/s}^2$
- $C_3 = 0 \text{ km}^2/\text{s}^2$
- 2D-transfer from circular orbit to circular orbit
- Trajectories calculated by G. Mengali and A. Quarta using a classical indirect method with an hybrid technique (genetic + gradient-based algorithm) to solve the associated boundary value problem
- Degradation factor:  $0 \leq d \leq 0.2$  (0–20% degradation limit)
- Half life SRD:  $\hat{\Sigma} = 0.5 (S_0 \cdot \text{yr})$
- Three models:
  - ▷ Model (a): Instantaneous degradation
  - ▷ Model (b): Control neglects degradation ("ideal" control law)
  - ▷ Model (c): Control considers degradation

# Mars Rendezvous

Trip times for 5% and 20% degradation limit



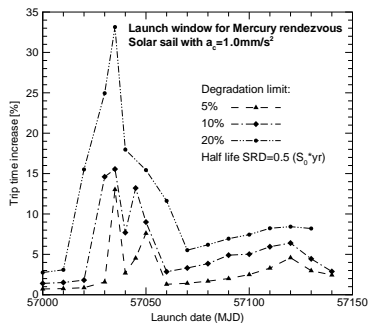
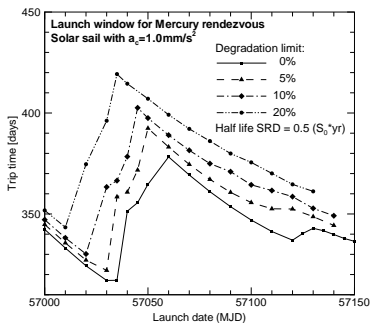
- OSSD has considerable effect on trip times
- The results for model (b) and (c) are indistinguishable close

# Mercury Rendezvous

- Solar sail with  $a_c = 1.0 \text{ mm/s}^2$
- $C_3 = 0 \text{ km}^2/\text{s}^2$
- Trajectories calculated by B. Dachwald with the trajectory optimizer GESOP with SNOPT
- Arbitrarily selected launch window  $\text{MJD } 57000 \leq t_0 \leq \text{MJD } 57130$   
(09 Dec 2014 – 18 Apr 2015)
- Final accuracy limit was set to  $\Delta r_{f,\max} = 80\,000 \text{ km}$  (inside Mercury's sphere of influence at perihelion) and  $\Delta v_{f,\max} = 50 \text{ m/s}$
- Degradation factor:  $0 \leq d \leq 0.2$  (0–20% degradation limit)
- Half life SRD:  $\hat{\Sigma} = 0.5 (S_0 \cdot \text{yr})$

# Mercury Rendezvous

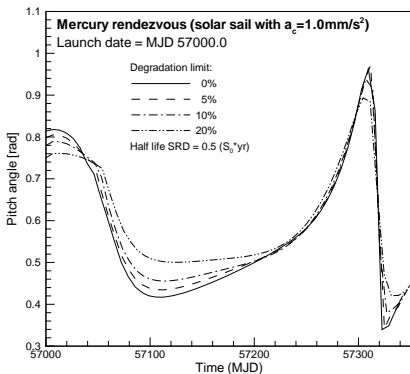
## Launch window for different $d$



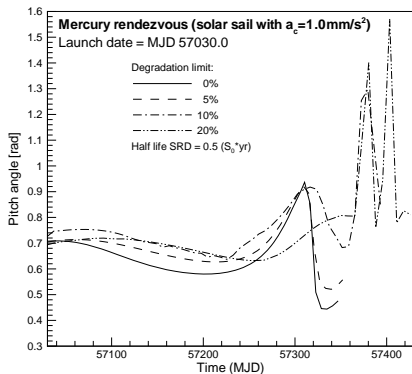
- Sensitivity of the trip time with respect to OSSD depends considerably on the launch date
- Some launch dates considered previously as optimal become very unsuitable when OSSD is taken into account
- For many launch dates OSSD does not seriously affect the mission

# Mercury Rendezvous

## Optimal $\alpha$ -variation for different $d$



Launch at MJD 57000.0



Launch at MJD 57030.0

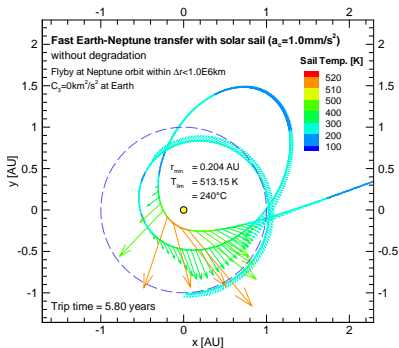
- OSSD can also have remarkable consequences on the optimal control angles
- Given an indefinite OSSD behavior at launch, MJD 57000.0 ( $S_0$ ) would be a very robust launch date

# Fast Neptune Flyby

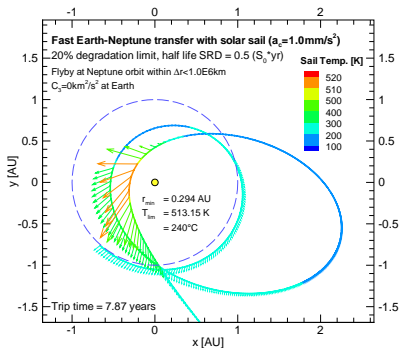
- Solar sail with  $a_c = 1.0 \text{ mm/s}^2$
- $C_3 = 0 \text{ km}^2/\text{s}^2$
- Trajectories calculated by B. Dachwald with the trajectory optimizer InTrance
- To find the absolute trip time minima, independent of the actual constellation of Earth and Neptune, no flyby at Neptune itself, but only a crossing of its orbit within a distance  $\Delta r_{f,\max} < 10^6 \text{ km}$  was required, and the optimizer was allowed to vary the launch date within a one year interval
- Sail film temperature was limited to  $240^\circ\text{C}$  by limiting the sail pitch angle
- Degradation factor:  $0 \leq d \leq 0.2$  (0–20% degradation limit)
- Half life SRD:  $0 \leq \hat{\Sigma} \leq 2$  ( $S_0 \cdot \text{yr}$ )

# Fast Neptune Flyby

## Topology of optimal trajectories for different $d$



$d = 0$



$d = 0.2$

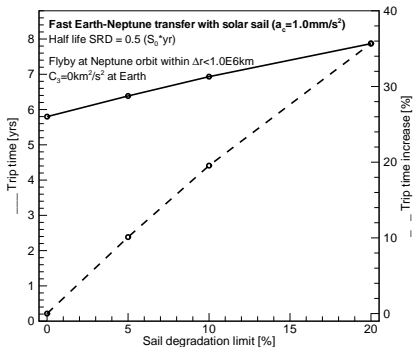
With increasing degradation:

- Increasing solar distance during final close solar pass
- Increasing solar distance before final close solar pass
- Longer trip time

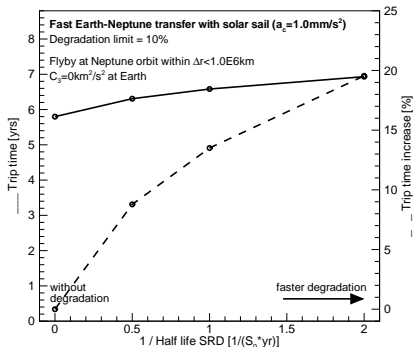


# Fast Neptune Flyby

Trip time and trip time increase for different  $d$  and  $\hat{\Sigma}$



Different degradation factors  $d$  ( $\hat{\Sigma} = 0.5 (S_0 \cdot \text{yr})$ )

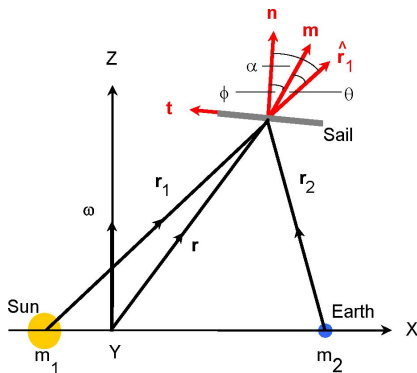


Different half life SRDs  $\hat{\Sigma}$  ( $d = 0.1$ )

Comparable results have been found by M. Macdonald for a mission to the heliopause.

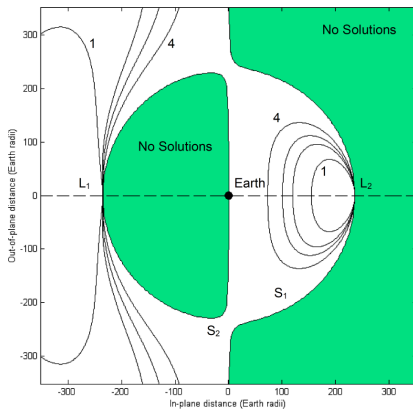
# Artificial Lagrange-Point Missions

- Sun-Earth restricted circular three-body problem with non-perfectly solar sail
- SRP acceleration allows to hover along artificial equilibrium surfaces (manifold of artificial Lagrange-points)
- Solutions calculated by C. McInnes

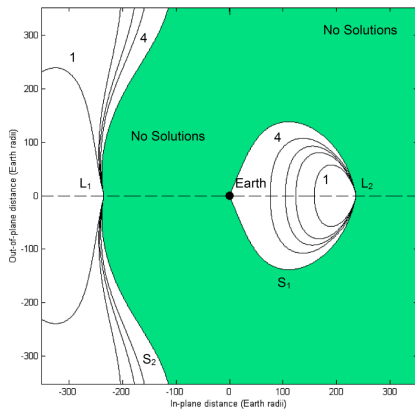


# Artificial Lagrange-Point Missions

Contours of sail loading in the  $x$ - $z$ -plane



$\rho = 1$

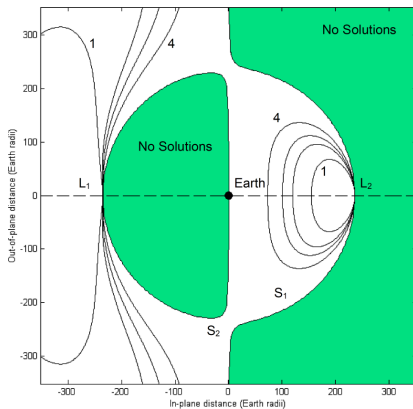


$\rho = 0.9$

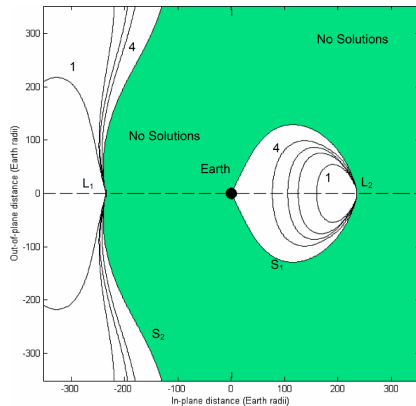
[1]  $30 \text{ g/m}^2$  [2]  $15 \text{ g/m}^2$  [3]  $10 \text{ g/m}^2$  [4]  $5 \text{ g/m}^2$

# Artificial Lagrange-Point Missions

Contours of sail loading in the  $x$ - $z$ -plane



$\rho = 1$

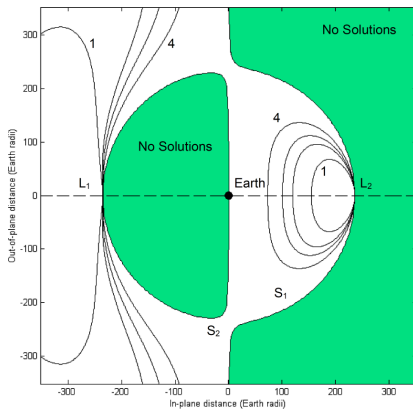


$\rho = 0.8$

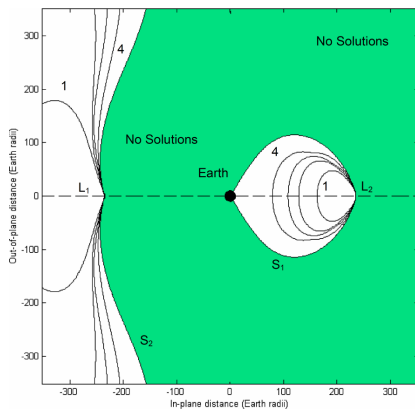
[1]  $30 \text{ g/m}^2$  [2]  $15 \text{ g/m}^2$  [3]  $10 \text{ g/m}^2$  [4]  $5 \text{ g/m}^2$

# Artificial Lagrange-Point Missions

Contours of sail loading in the  $x$ - $z$ -plane



$\rho = 1$



$\rho = 0.7$

[1] 30 g/m<sup>2</sup> [2] 15 g/m<sup>2</sup> [3] 10 g/m<sup>2</sup> [4] 5 g/m<sup>2</sup>

## Summary and Outlook

- All our results show that optical solar sail degradation has a considerable effect on trip times and on the optimal steering profile. For specific launch dates, especially those that are optimal without degradation, this effect can be tremendous
- Having demonstrated the *potential* effects of optical solar sail degradation on future missions, more research on the *real* degradation behavior has to be done
- To narrow down the ranges of the parameters of our model, further laboratory tests have to be performed
- Additionally, before a mission that relies on solar sail propulsion is flown, the candidate solar sail films have to be tested in the relevant space environment
- Some near-term missions currently studied in the US and Europe would be an ideal opportunity for testing and refining our degradation model

# Optical Solar Sail Degradation Modeling

**Bernd Dachwald<sup>1</sup>, Giovanni Mengali<sup>2</sup>, Alessandro A. Quarta<sup>2</sup>,  
Malcolm Macdonald<sup>3</sup>, Colin R. McInnes<sup>4</sup>**

<sup>1</sup>German Aerospace Center (DLR), Oberpfaffenhofen, Germany

<sup>2</sup>University of Pisa, Italy

<sup>3</sup>SciSys Ltd., Bristol, UK

<sup>4</sup>University of Strathclyde, Glasgow, Scotland, UK

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