Optimization–based reactive power control in HVDC–connected wind power plants

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Abstract

One application of high–voltage dc (HVdc) systems is the connection of remotely located offshore wind power plants (WPPs). In these systems, the offshore WPP grid and the synchronous main grid operate in decoupled mode, and the onshore HVdc converter fulfills the grid code requirements of the main grid. Thus, the offshore grid can be operated independently during normal conditions by the offshore HVdc converter and the connected wind turbines. In general, it is well known that optimized reactive power allocation might lower the component loading and power losses. This paper aims to propose and assess a reactive power allocation optimization within HVdc–connected WPPs. For these systems, the offshore converter operates the adjoining grid by imposing frequency and voltage. The reference voltage magnitude is used as additional control variable for the optimization algorithm. The loss function incorporates both the collection grid and the

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converter losses. The use of the proposed strategy results in an effective reduction of losses compared to conventional reactive power dispatch strategies alongside with improvements of the voltage profile. A case study for a 500 MW–sized WPP demonstrates an additional annual energy production of 6819 MWh or an economical benefit of 886 k€ yr^{-1} when using the proposed strategy.

1. Introduction

The use of wind energy at offshore locations is growing, especially in European waters. By the end of 2015 the cumulative grid connected offshore wind power installations raised to more than 11 GW, on top of an additional capacity of 63.5 GW in the planning phase [1]. Currently, wind turbines (WTs) are variable–speed machines using partly or fully–scaled voltage–source converter (VSC) to interface with the electrical grid [2]. These converters allow to control the active and reactive power exchange at their ac terminals independently within specific capability limits [3].

Most offshore wind power plants (WPPs) require a dedicated grid connection to the onshore grid. Depending on the project characteristics, namely the distance to shore and the total power rating, either an ac or dc–based technology is selected to connect the generation units to the transmission grid [4?].

In the case that the offshore WPP is connected via a high–voltage dc (HVdc) link, the collection grid is usually operated by the offshore high–

voltage dc voltage–source converter (VSC–HVdc) in islanded mode whereas the VSC–HVdc provides reference for both voltage and frequency. The onshore converter fulfills grid code (GC) requirements imposed by the transmission grid operator (TSO) of the main grid [4]. Amongst others, GCs define rules for the connection of generation units to a power system, such as operation characteristics, active and reactive power control, frequency response, fault behavior and ancillary services [5]. Besides the necessity of GC compliance, offshore wind power is exposed to the market competition with other energy sources. Therefore, it remains subject to significant pressures to improve its cost of energy (COE) and lower the associated risks [6]. One option to lower the COE is the increase of the annual energy production (AEP). This might be solved, among others, by e.g. alternative topologies [7, 8, 9, 10], WPP layout optimization [11] and/or concepts to lower losses due to wake effects [12]. Another option, which is investigated in this paper, is the implementation of appropriate reactive power control operation strategies to reduce steady–state losses in the collection grid and the power converters with the objective to boost the AEP.

System operators use optimization algorithms to minimize electrical losses by tuning set–points of on–load tap changer (OLTC) of transformers or other electrical equipment which can control voltage or reactive power (e.g. WPPs, static compensator (STATCOM) capable assets and reactive power compensators) [13, 14, 15, 16, 17]. The same approach can be applied to an internal WPP grid which has been studied for ac–connected WPPs in [18, 19, 20, 21] and dc–connected WPPs in [22, 23]. Based on the particle swarm optimization (PSO) algorithm of [24], the operation principle was investigated

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for doubly fed induction generator (DFIG)–based WPPs in [19]. In [20] a feasible solution search PSO algorithm was applied to the reactive power allocation problem of a DFIG–based WPP. Different control principles are analyzed concluding that a higher loss reduction is achieved for lower WPP power outputs. In terms of practicability for an online optimal reactive power allocation, the authors of [25, 26] propose optimal power flow (OPF) controllers based on mean–variance mapping optimization (MVMO) aiming to minimize losses while complying with the GC at the point of common coupling (PCC). In [27] the suggested OPF controller additionally considers to minimize the switching actions of the OLTC and uses a neural–network–theory–based wind speed prediction. In [21], the authors discuss a complete loss calculation including generator and converter losses for a DFIG–based WPP to solve the optimal reactive power allocation problem. The analysis made in [28] provides a fruitful insight of the necessity to include the WT converter losses in the problem formulation of these systems.

The authors of this article challenged the optimal reactive power allocation problem in HVdc–connected WPPs for the first time in [22]. Here, an optimization–based algorithm is used to perform the reactive power dispatch to the WTs comparable to similar algorithms proposed for ac–connected WPPs but under consideration of converter losses and the reactive power sharing between the WTs and the VSC–HVdc. Specifically, the influence of wake effects on the total active and reactive power production in the offshore grid is analyzed. Nevertheless, the reference voltage imposed by the VSC–HVdc is continuously contained to 1 p.u.. Besides this publication, the general characteristics regarding reactive power control in HVdc–connected

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WPPs are briefly commented in the technical brochures of *CIGRE* [29, 30]. The main difference to high–voltage ac (HVac)–connected WPPs is that the reactive power requirement demanded by the main grid does not constrain the reactive power allocation within the offshore grid because of the earlier mentioned decoupled operation. Additionally, a change of the reference voltage in the offshore grid is possible by means of the VSC–HVdc control. This study extends the methodology for HVdc–connected WPPs introduced in [22] by the same authors and proposes the inclusion of the reference voltage as a control variable in the optimization–based control algorithm.

The main aim of this paper is to propose a reactive power control strategy to optimize the operation of HVdc–connected WPPs in terms of losses. The optimization determines reactive power set–points for the WTs and the PCC reference voltage set–point imposed by the VSC–HVdc based on a combined converter losses and load flow model. A case study is defined to analyze the performance of the proposed strategy and variations thereof against conventional control concepts. A 500 MW–sized WPP which employs full–scale power converter–based wind turbines (type 4) [FSC–WTs] is used for this analysis. Six control principles are evaluated: two conventional and four optimization–based strategies, respectively. The result shows an improved performance specifically for the variable optimization–based strategies for both the total power losses and the voltage profile. The incorporation of the reference voltage as control variable inherently reduces the power losses in the system without harming the overall operation.

The remainder of this paper is organized as follows: Section II describes the methodology to analyze reactive power control in HVdc–connected WPPs

and proposes suitable optimization–based strategies. Section III defines a case study for a reference WPP. The results and discussion are outlined in Section IV. Finally, Section V provides the conclusions and recommendations.

2. Methodology

A possible HVdc–connected WPP system is shown in Figure 1 [29]. The full–scale converter (FSC) of the WTs comprises a machine–side converter (MSC) in back–to–back (B2B) arrangement with a grid–side converter (GSC) system. The GSC connects to the low–voltage (LV)–side of the WT transformer through a coupling inductance and a harmonic filter. A number of WTs is interconnected by medium–voltage (MV) submarine cables to form a string and interface the high–voltage ac offshore substation (HVac–OS). Here, high–voltage (HV) transformer(s) step up the voltage from MV to HV. The HVac–OS is linked to the high–voltage dc offshore substation (HVdc–OS) by HVac submarine cable(s). The HVdc–OS consists of the HVdc transformer(s), possible harmonic filter(s) and the offshore VSC–HVdc. The offshore VSC–HVdc station links to any dc–capable interface via submarine dc cables, in the usual execution a point–to–point connection to an onshore VSC–HVdc to connect to the main ac grid.

2.1. Calculation of relevant losses

In general, there are multiple electrical losses occurring in the operation of generators, converters, filters, transformers and cables. For the steady–state power flow analysis, lines, filters and transformers are modeled as lumped circuits (π–models) [31]. In a π–model, the series admittance between two nodes 1 and 2 is defined as:
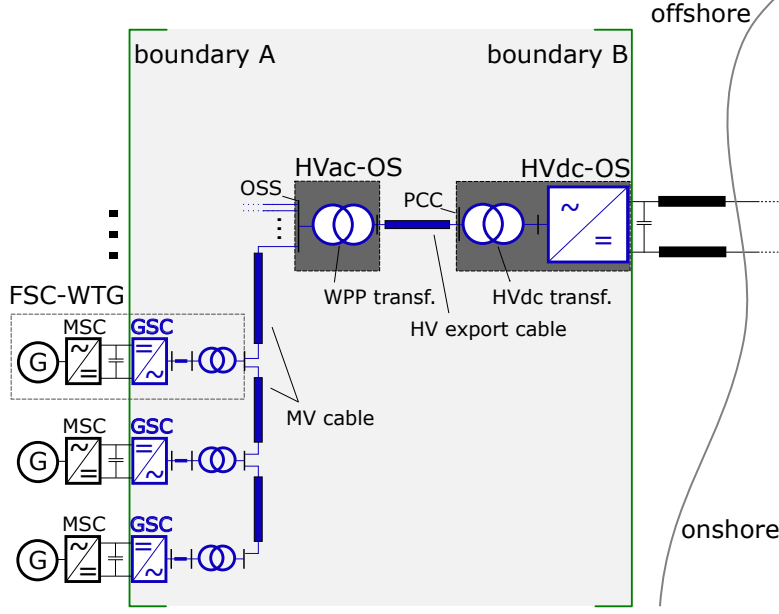
Figure 1: Typical arrangement of an HVdc–connected offshore WPP and system boundaries for loss assessment.

$$\underline{y}_{12} = g_{12} + j \cdot b_{12} = \frac{r_{12}}{r_{12}^2 + x_{12}^2} - j \frac{x_{12}}{r_{12}^2 + x_{12}^2} \tag{1}$$

where g_{12} and b_{12} are the series conductance and susceptance between the nodes 1 and 2, respectively, and r_{12} and x_{12} represent the series resistance and reactance, respectively.

The shunt admittance is calculated as:

$$\underline{y}_1^{sh} = \underline{y}_2^{sh} = g^{sh} + j \cdot b^{sh} \tag{2}$$

When considering power cables and lines the shunt conductance is very small ($g^{sh} \approx 0$) and can be neglected. Values for the series resistance r_{12}, series reactance x_{12} and shunt susceptance b^{sh} are chosen according to manufacturer data. For transformers, the series resistance r_{12} models the copper losses

(load losses) in the windings having the reactance x_{12}. The iron/core losses (no–load) due the magnetizing current can be represented by a shunt element. The active power imbalance or loss Δp can be calculated using (3) and the reactive power imbalance Δq composed of the reactive power generation by the shunt susceptance and reactive power loss is described in (4):

$$\Delta p = g_{12} \cdot (u_1^2 + u_2^2 - 2u_1u_2 \cos\theta_{12}) \tag{3}$$

$$\Delta q = -b^{sh} \cdot (u_1^2 + u_2^2) - b_{12} \cdot (u_1^2 + u_2^2 - 2u_1u_2 \cos\theta_{12}) \tag{4}$$

where u_1 and u_2 are the voltages of node 1 and 2, respectively, and $\theta_{12} = \theta_1 - \theta_2$ is the phase angle difference between the two nodes.

The compilation of losses is limited to the boundaries of the offshore grid as shown in Figure 1: boundary A is the interface between dc link of the GSCs and boundary B is the dc terminal the offshore VSC–HVdc. These boundaries are set following that the reactive power control at the ac terminal of a VSC is independent from the dc–side [3]. Therefore, the control of reactive power at the GSC does not cause additional currents (or losses) in the dc link, the MSC or even the generator. This is also valid for the offshore VSC–HVdc with respect to the HVdc interface. However, the injection of active and reactive power, P_c and Q_c, respectively, influences the converter current I_c according to (5):

$$I_c = \frac{\sqrt{P_c^2 + Q_c^2}}{\sqrt{3} \cdot U_{\text{LL,rms}}} \tag{5}$$

The switching and conduction losses $P_{\text{conv}}^{\text{loss}}$ of a VSC might be approximated by a quadratic polynomial function in dependence of the converter current I_c, considering three parts [32]: constant, linear and quadratic losses.

$$P_{\text{conv}}^{\text{loss}} = \left[a + b \cdot \frac{I_c}{I_r} + c \cdot \left(\frac{I_c}{I_r} \right)^2 \right] \cdot S_n \qquad (6)$$

where I_r is the rated converter current, S_n represents the nominal apparent power.

Typical loss data for a system rated to $U_{\text{dc}} = \pm 300\,\text{kV}$, $S_\text{n} = 600\,\text{MVA}$ based on a two–level VSC–HVdc (HVdc–2L) can be found in [33]. For a modular multi–level VSC–HVdc (HVdc–MMC) the current–dependent losses in the converter valves are approximately halved compared to a HVdc–2L [34]. Figure 2 shows the relative power losses of the considered power converters deploying (6) with the parameter values from Table 1. The effect of the absolute loss increase due to a reactive power exchange in comparison to exclusively active power injection is represented in Figure 3. The additional converter losses in the HVdc–MMC are up to $0.9\,\text{MW}$ when operated at $p = 0\,\text{p.u.}$ and $q = 1\,\text{p.u.}$. For $q = 1\,\text{p.u.}$, an equally scaled GSC system causes a value of $1\,\text{MW}$ additional losses at full power and up to $2.8\,\text{MW}$ additional losses for $p = 0\,\text{p.u.}$.

Table 1: Typical converter loss parameter values used in [32, 33, 34].

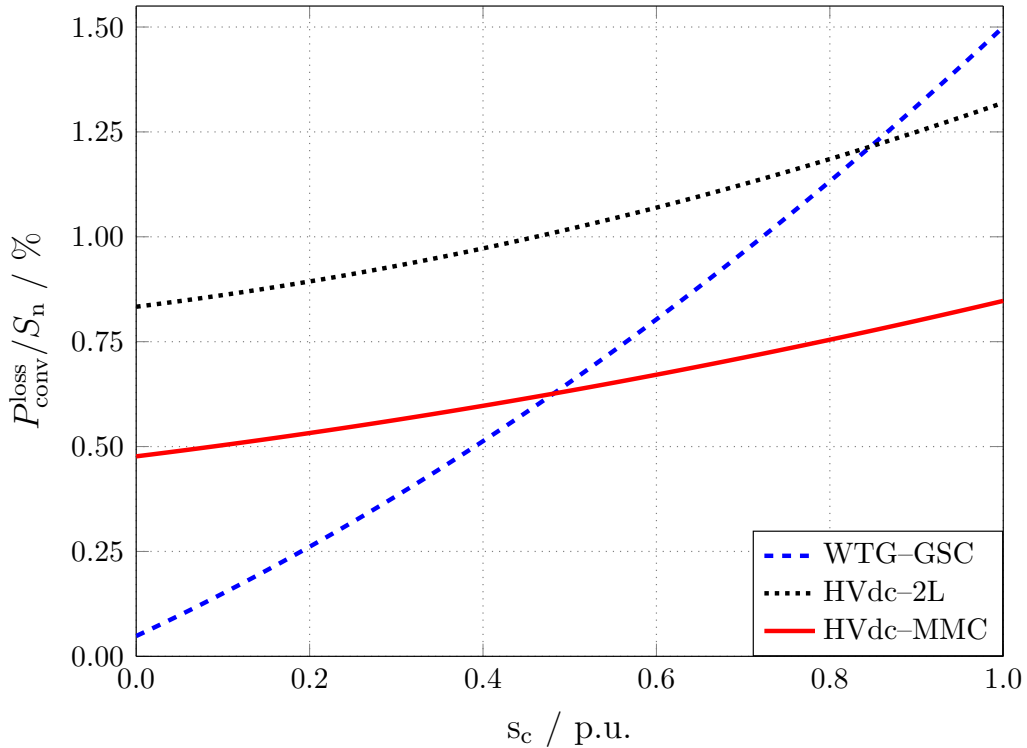| System	a	b	c
GSC	0.0005	0.0097	0.0048
HVdc–2L	0.0083	0.0030	0.0032
HVdc–MMC	0.0042	0.0015	0.0016

Figure 2: Relative losses of VSC systems based on their technology and power output.

2.2. Reactive power allocation strategies

The reactive power allocation strategies considered in this paper focus on the normal operation of the HVdc–connected WPP. During system disturbances (e.g. under or over–voltage events) each converter would operate based on a predefined control procedure usually according to the GC. Nonetheless, local reactive power limitations due to the availability and PQ capability curve of the WT have to be respected.

In principle, two conventional strategies might emerge to control reactive power in an HVdc–connected WPP when the control variable are limited to be the reactive power set–points:
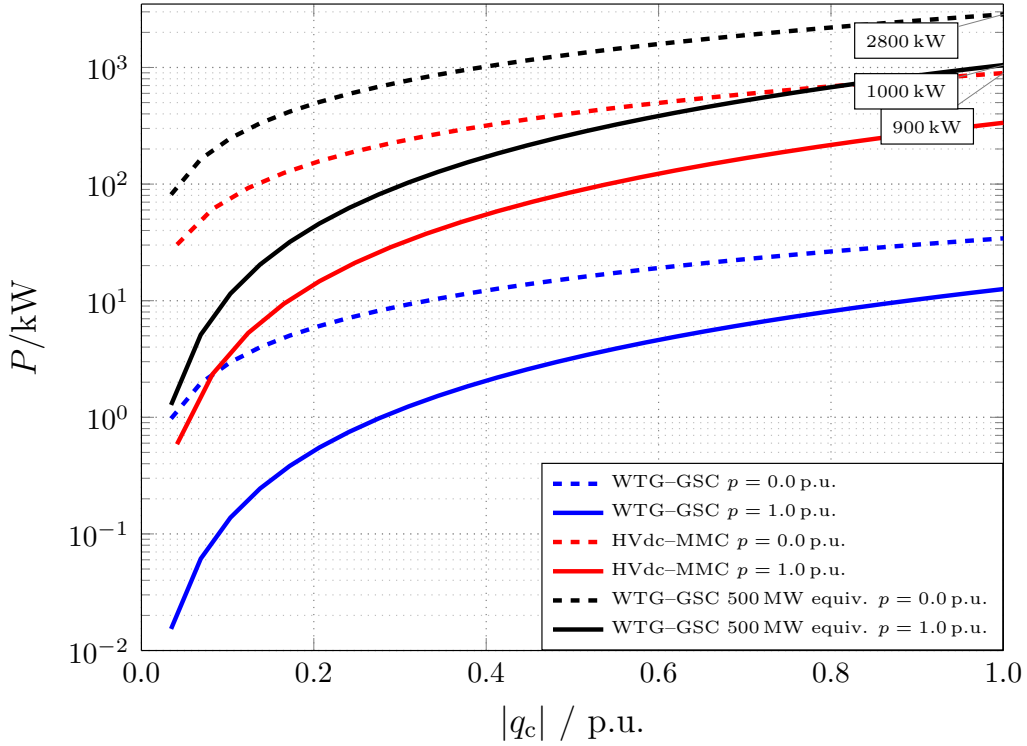
Figure 3: Absolute increase of losses caused by the reactive power injection of VSCs. GSC rating: $S_n = 6.67\,\text{MVA}$, $\cos\varphi = 0.9$, $u_{ac} = 0.9\,\text{kV}$; HVdc–MMC $S_n = 555.6\,\text{MVA}$, $\cos\varphi = 0.9$, $u_{ac} = 333\,\text{kV}$ ($u_{dc} = \pm320\,\text{kV}$, modulation index: $m = 0.85$); GSC 500 MW equivalent to compare with the VSC–HVdc.

1. Strategy 1 (S1): Each GSC operates locally with zero reactive power injection, thus $Q_i = 0\,\text{Mvar}$. This is equal to a unity power factor (PF) operation of the GSCs for $P_i \neq 0\,\text{MW}$.

2. Strategy 2 (S2): The VSC–HVdc aims to operate with zero reactive power injection ($Q_{\text{PCC}} = 0\,\text{Mvar}$) by adjusting remotely the reactive power set–points Q_i of the WTs. The VSC–HVdc is operated at a unity PF for $P_{\text{PCC}} \neq 0\,\text{MW}$.

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Furthermore, the optimization–based strategy as presented in [22] is considered:

3. Strategy 3 (S3): An optimization algorithm aims to maximize the power output of the system and calculates reactive power set–points for the GSCs according to the actual operating point of the complete system.

The strategies S1 to S3 are studied with a fixed PCC voltage reference of $\underline{u}_{\mathrm{PCC}} = 1\,\mathrm{p.u.}$ which is continuously controlled by the VSC–HVdc. Finally, the three initial strategies are extended by the varying voltage reference and introduced as variable strategies:

4. Variable strategy 1 (S1var): Optimization–based with the PCC voltage magnitude u_{PCC} as control variable whereas the WT inject $Q_i = 0\,\mathrm{Mvar}$ ($i \in N_{\mathrm{WT}}$).

5. Variable strategy 2 (S2var): Optimization–based with the PCC voltage magnitude u_{PCC} as control variable and a unique set–point for Q_i of the WTs.

6. Variable strategy 3 (S3var): Optimization–based similar to S3 adjusting the individual reactive power set–points for the GSCs as well as the PCC voltage magnitude u_{PCC} controlled by the offshore VSC–HVdc.

Strategy S1var to S3var allow a variable PCC voltage set–point within the continuous voltage operation boundaries. For all strategies, the VSC–HVdc injects or absorbs the active and reactive power to fulfill the power imbalance equations (acting as a reference bus).

Regarding data exchange requirements, the implementation of S1 does not necessarily use the communication system between the local WT control

and the central WPP control. In contrast, S2 deploys a closed–loop control to adjust the set–points Q_i controlling the measured Q_{PCC} to the reference of $0\,\mathrm{Mvar}$. The reactive power set–point for S1, S2, S1var and S2var is the same for all WTs. The strategies S3, S1var, S2var and S3var necessarily require a communication system as either inputs (active power measurements, operation status of WTs) and outputs (reactive power set–points, u_{PCC} set–point in case of the variable strategies) have to be transfered between WT control and central WPP control.
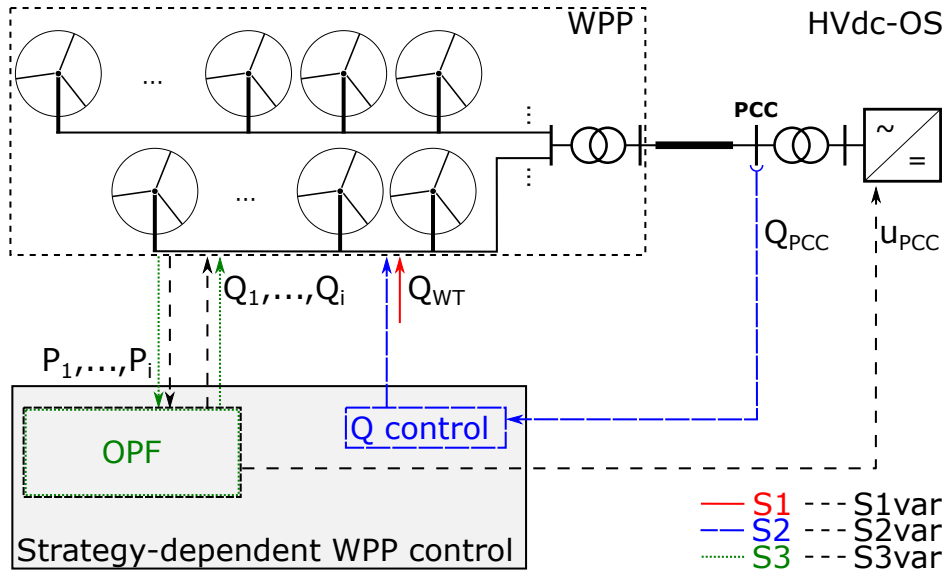

Figure 4: Schematic of control concepts and communication paths for each strategy.

Figure 4 sketches the communication and measurement needs for the presented strategies. To sum up, the six strategies and their characteristics are listed in Table 2.

Table 2: Overview of considered reactive power allocation strategies.

	S1	S2	S3	S1var	S2var	S3var
Objective:	unity PF WTs	unity PF VSC–HVdc		min $P_{\text{total}}^{\text{loss}}$		
Communication:	local	remote				
Q_i set–points:	0 Mvar	WPP control	OPF	0 Mvar	OPF	OPF
Q_i distribution:	uniform	uniform	variable	uniform	uniform	variable
Q_{PCC} set–point:[1]	power flow	0 Mvar	power flow			
u_{PCC} set–point:	fixed			variable		
Average execution time OPF:[2]	n/a	n/a	188.8 s	1.9 s	9.8 s	243.9 s

2.3. Formulation of the optimization problem

The total active power losses $P_{\text{total}}^{\text{loss}}$ in the system are calculated as:

$$P_{\text{total}}^{\text{loss}} = \sum_{\forall i} P_{\text{GSC}_i}^{\text{loss}} + P_{\text{grid}}^{\text{loss}} + P_{\text{VSC–HVdc}}^{\text{loss}}. \tag{7}$$

where $P_{\text{grid}}^{\text{loss}}$ are the total losses in the system including collection grid, export cable(s) and transformer(s), $P_{\text{GSC}_i}^{\text{loss}}$ reflects the GSC losses and $P_{\text{VSC–HVdc}}^{\text{loss}}$ represents the losses of the HVdc converter.

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[1]The reactive power at the PCC is determined by the power flow in the offshore grid.
[2]Data is given for the case study performed in this paper.

The design vector $\boldsymbol{x}$ accommodates the voltage set–point u_{PCC} and the reactive power set–points q_i of the GSCs:

$$\boldsymbol{x} = \left[u_{\mathrm{PCC}}, q_1, q_2, \ldots, q_i\right]^T \qquad i \in \boldsymbol{N}_{\mathrm{WT}} \tag{8}$$

where $\boldsymbol{N}_{\mathrm{WT}}$ is a vector of all WT elements. The optimization problem is stated as follows:

$$\text{Minimize} \quad f(\boldsymbol{x}) = P_{\mathrm{total}}^{\mathrm{loss}}(\boldsymbol{x}) \tag{9}$$

$$s.t. :$$

$$\text{Power flow equations} \tag{10}$$

$$\boldsymbol{u}_{\mathrm{k,min}} \le \boldsymbol{u_k}(\boldsymbol{x}) \le \boldsymbol{u}_{\mathrm{k,max}}, \qquad k \in \boldsymbol{N}_{\mathrm{bus}} \tag{11}$$

$$|\boldsymbol{i_l}(\boldsymbol{x})| \le \boldsymbol{i}_{\mathrm{l,max}}, \qquad l \in \boldsymbol{N}_{\mathrm{branch}} \tag{12}$$

$$q_{\mathrm{PCC,min}} \le q_{\mathrm{PCC}}(\boldsymbol{x}) \le q_{\mathrm{PCC,max}} \tag{13}$$

$$u_{\mathrm{PCC}} \in \left[u_{\mathrm{PCC,min}}, u_{\mathrm{PCC,max}}\right] \tag{14}$$

$$\boldsymbol{q_i} \in \left[\boldsymbol{q}_{\boldsymbol{i},\mathrm{min}}, \boldsymbol{q}_{\boldsymbol{i},\mathrm{max}}\right], \qquad i \in \boldsymbol{N}_{\mathrm{WT}} \tag{15}$$

where $\boldsymbol{N}_{\mathrm{bus}}$ and $\boldsymbol{N}_{\mathrm{branch}}$ are vectors of all buses (except PCC bus) and branches, respectively. The voltages $\boldsymbol{u}_{\mathrm{k}}(\boldsymbol{x})$ at the buses $\boldsymbol{N}_{\mathrm{bus}}$ are limited to the minimum and maximum voltages $\boldsymbol{u}_{\mathrm{k,min}}$ and $\boldsymbol{u}_{\mathrm{k,max}}$ being a deviation of $\pm 10\,\%$ of the nominal voltage. The current in a branch $\boldsymbol{i_l}(\boldsymbol{x})$ represents the highest absolute value of the current at both ends of the branch. It is limited to the corresponding rating $\boldsymbol{i}_{\mathrm{l,max}}$. The reactive power limitations at the PCC, $q_{\mathrm{PCC,min}}$ and $q_{\mathrm{PCC,max}}$, and for the WTs, $\boldsymbol{q}_{\boldsymbol{i},\mathrm{min}}$ and $\boldsymbol{q}_{\boldsymbol{i},\mathrm{max}}$, correspond to a PF of 0.9 at full power. The different PCC

voltage constraints between the optimization–based strategies (S3, S1var, S2var and S3var) are reflected by $u_{\mathrm{PCC,min}} = u_{\mathrm{PCC,max}} = 1.0\,\mathrm{p.u.}$ for S3 and $u_{\mathrm{PCC,min}} = 0.9\,\mathrm{p.u.}$ and $u_{\mathrm{PCC,max}} = 1.1\,\mathrm{p.u.}$ for S1var to S3var in (14). Strategy S1var is further restricted by $q_i = q_{i,\mathrm{min}} = q_{i,\mathrm{max}} = 0\,\mathrm{p.u.}$ ($i \in \boldsymbol{N}_{\mathrm{WT}}$) in (15). For strategy S2var the reactive power at the PCC is restricted to $q_{\mathrm{PCC}} = q_{\mathrm{PCC,min}} = q_{\mathrm{PCC,max}} = 0\,\mathrm{p.u.}$ (13) and additionally $q_i = q_j$ ($i, j \in \boldsymbol{N}_{\mathrm{WT}}$) meaning that all WTs receive an equal reactive power set–point.

2.4. Implementation of the optimization–based strategies

The implementation of the optimization–based strategies is made by the combination of the Matlab–based power flow solver package Matpower [35] and the fmincon function of the Matlab Optimization Toolbox. For the purpose of this study, lines and transformers are sufficiently modeled as a π–section model [36]. In Matpower, every GSC_i is defined as static generator G_i connected to a load bus (PQ bus), injecting active power P_i and reactive power Q_i ($i \in N_{\mathrm{WT}}$). The VSC–HVdc, which sets the PCC voltage reference, is introduced as the reference bus (slack bus). The integration of the converter losses is made sequentially: the GSC losses caused by Q_i are considered as real power demand at the corresponding WT load bus whereas the VSC–HVdc and HVdc transformer losses are calculated by (6) after each load flow computation. The fmincon function uses the interior–point algorithm. The optimization is deterministic as the interior–point algorithm reaches local minimums. Nevertheless, the solver runs from multiple starting points to increase the number of solutions. Furthermore, the total execution time is limited. The best solution is selected and verified through load flow

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calculation afterwards.

2.5. Conceptual implementation in the industrial application

A feasible implementation of the optimization–based strategies might consider a variable refresh rate between 5 min to 10 min. The optimization algorithm itself might have a maximum execution time (here set to 300 s). The average execution times recored for the case study in this paper are listed in the last row of Table 2. Obviously, the number of the control variables increases the calculation time. For S1var and S2var average calculation times below 10 s are reached (simulations are run on a 3.5 GHz–system with 16 GB RAM). New set–points might be sent as soon as the optimization algorithm ends. Further time requirements are: the communication times for the active power measurements of the WTs and the reference voltage/reactive power set–points, respectively, and the settling time after receiving the new set–points. The communication delays are negligible on the time frame of the proposed controller as modern communication systems in offshore WPPs consider refresh rates of a few hundreds of ms [37]. The settling times might be established as required for normal reactive power set–point changes in WPPs (e.g. 30 sec [38]). Fast voltage support to counteract voltage dips acts independently from this and supersedes the previous reactive power set–points during activation. For the variable strategies, the reference voltage might be changed first and afterwards the reactive power injections by the WTs. Real–time implementation might be improved by either short–term power or wind forecast to offset the time delay [26] or offline calculation of the optimization algorithm.

3. Case study

The analysis made in this paper aims to draw conclusions relied upon realistic data. Therefore, the WPP characteristics were derived from the French 498 MW Fécamp project [39, 40]. This WPP is planned with 83 individual FSC–WTs with a nameplate capacity of 6 MW each. For the sake of simplicity, it is assumed that each GSC can provide the equivalent reactive power of a PF of $\cos \varphi = \pm 0.9$ at full power.

The graphical data offered in [39] allows to estimate individual cable lengths and to define the distribution of the turbines as well as how they are interconnected (visualized in Figure 5). Further relevant reference data, including component parameters and voltage levels, are provided in Table A.4 in the Appendix. The array cable lengths were calculated according to the distance between the turbines and an additional offset of $l = 100$ m to incorporate the cable routing from the sea bed to the transition piece of the WTs. Table A.5 gives data for the cross–linked polyethylene (XLPE) submarine cables considered in this study.

Contrary to the reference project, the transmission grid connection is adapted to an HVdc connection for the purpose of this paper. Loss data for the offshore VSC–HVdc are calculated according to (6) and Table 1. An HVdc–MMC system is assumed as it presents the state–of–the–art solution in this application [29].

To compute an approximate value of the total energy losses of the WPP, the annual wind speed distribution of the specific site is required. In general, a Weibull probability distribution approximates the distribution of wind speed for WPP studies. The parameters for the case study are the mean wind
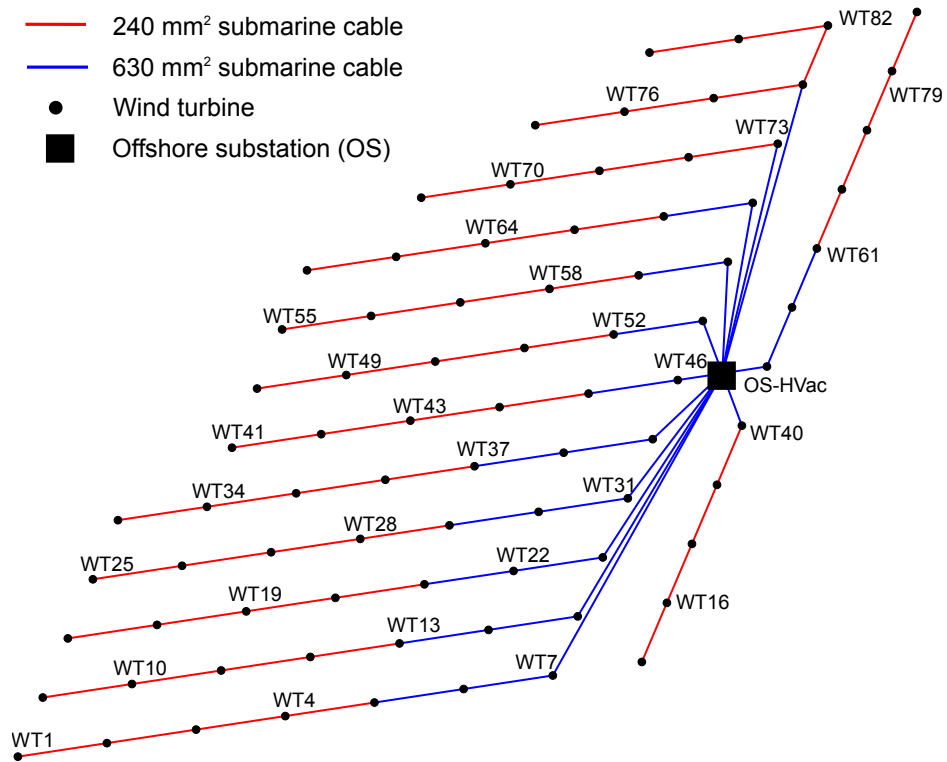
Figure 5: Layout of the 498 MW Fécamp reference WPP.

speed of $8.8\,\mathrm{m\,s^{-1}}$ [40] and a commonly used shape parameter for offshore locations of 2.2 [6]. The consideration of outages of WTs or the HVdc system due to maintenance or failure and wake effects is beyond the scope of this study. Thus, the wind speed and active power injection are assumed to be equal for each WT. In order to estimate the monetary value of the total energy losses, the French offshore feed–in tariff of $130\,\text{\texteuro}\,\mathrm{MWh^{-1}}$ is considered [41].

4. Results

The analysis was performed for the six strategies and active power values ranging from zero to full power ($p = 0.0$ p.u. to 1.0 p.u.). The first case, S1, is taken as a reference to evaluate the other strategies. The relative loss value shows the increase or reduction of losses for a strategy Sn in comparison to the strategy S1 and is calculated according to:

$$P_{\text{rel}}^{\text{loss}} = \frac{P_{Sn}^{\text{loss}}}{P_{S1}^{\text{loss}}} \cdot 100 \,\% \tag{16}$$

where $n \in \{1, 2, 3, 1\text{var}, 2\text{var}, 3\text{var}\}$ is used to compare the strategies to S1. Figure 6 depicts the total relative losses for all strategies according to (16). The results demonstrate that S2 causes higher losses than S1 for $0.0 < p < 0.6$ p.u. and less losses for $p > 0.6$ p.u.. Here, it is worth mentioning that an equal relative loss reduction along the whole power range reflects more valuable absolute loss reductions for higher powers. As expected, the employment of the optimization algorithm in S3 has the lowest loss values over the whole power range within the strategies with a fixed PCC voltage reference. Nevertheless, the difference of the total losses between the best conventional strategy (S1 or S2) for individual active power operating points against S3 is of maximal $0.57\,\%$ (at $p = 0.63$ p.u.). The variable strategies S1var to S3var demonstrate that the PCC voltage as control variable has an important impact on the power losses. Specifically in the higher power range for $p > 0.4$ p.u. the variable strategy performs better than its fixed voltage reference counterpart (S1var with respect to S1, etc.). It is remarkable that S1var causes a similar result as S3var although the latter uses a more complex optimization incorporating the individual reactive power set–points of
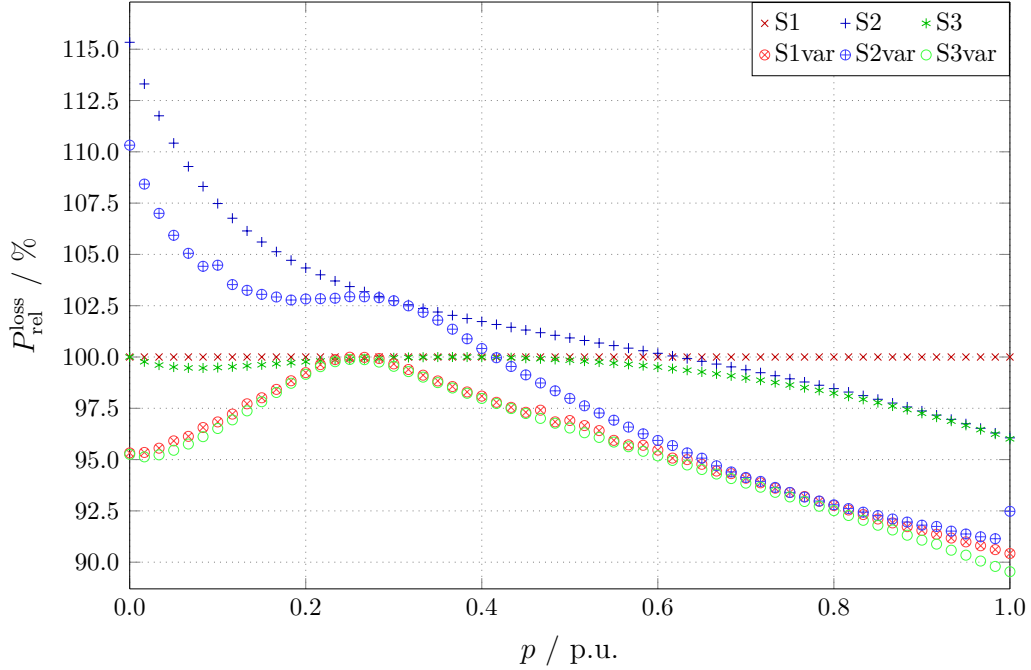
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the WTs.

Figure 6: Relative total system losses respective to S1 (set equal to 100 %).

The total amount of consumption and generation of reactive power by transformers, filters and submarine cables in the system has to be balanced by the GSCs and VSC–HVdc. In the following the reactive power injections by the VSC–HVdc q_{PCC} and by two GSCs q_{WT} are presented in Figure 7 and Figure 8 for the whole power range, respectively. For both graphs, $q = 1\,\mathrm{p.u.}$ is equal to a PF $= 0.9$ at full power. The most remote WT from the PCC busbar, WT1, and the closest one, WT46, have been selected for visualization.

The results of S1 indicate that the VSC–HVdc absorbs reactive power for lower powers and injects reactive power for higher powers. Similarly, for
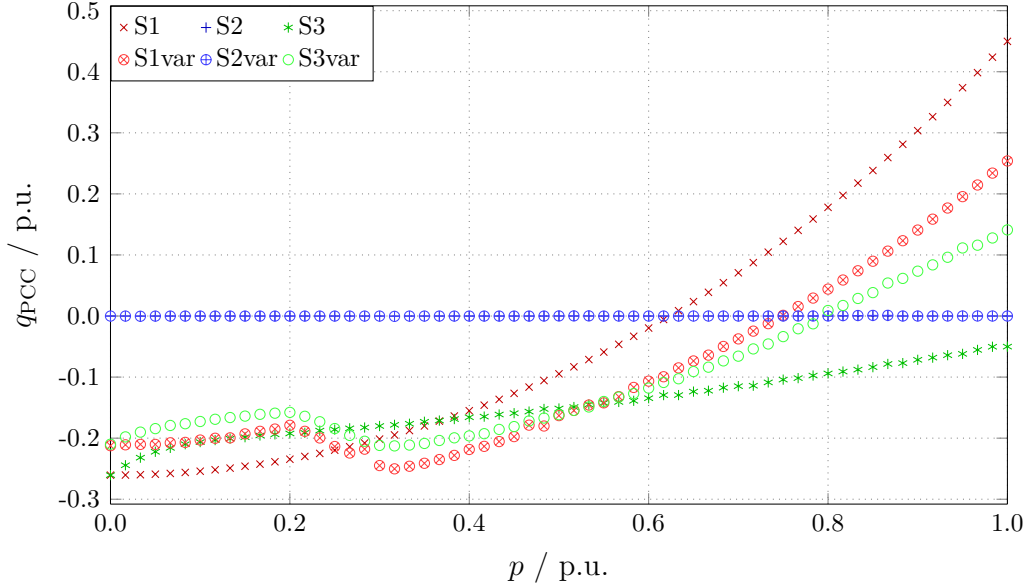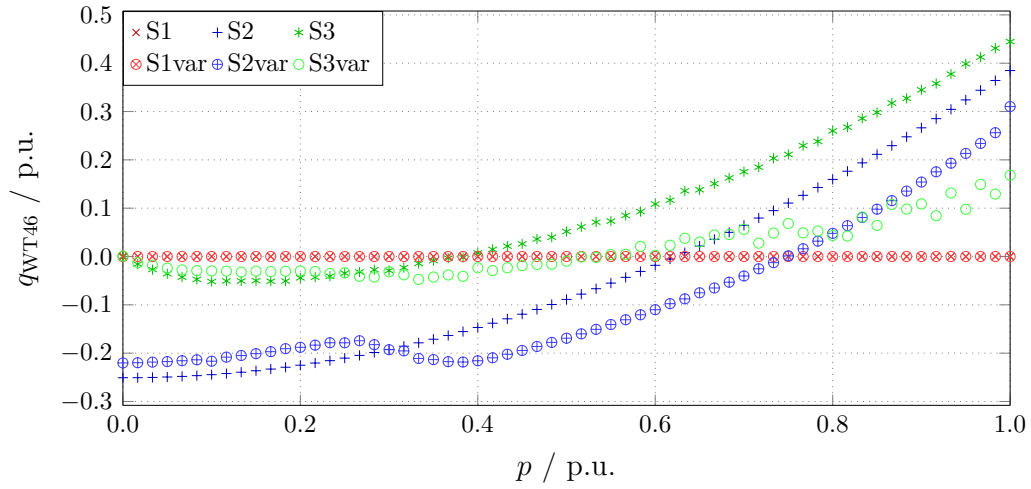
Figure 7: Reactive power injection by the VSC–HVdc. Positive values correspond to a reactive power injection (capacitive) by the converter.

strategy S2 the reactive powers of the WTs q_{WT} show the same behavior. In both cases, these reactive power sources solely compensate the mentioned amount of reactive power generated in the grid. Thus, the contributions by the VSC–HVdc for strategy S2 as well as by the WTs for strategy S1 are zero as expected. For strategy S1 and S2, respectively, the q_{WT} of WT1 and WT46 are identical due to the uniform set–point distribution for these strategies. For the strategy S3 the set–points for the closest turbine are only up to 0.04 p.u. higher than for the most remote one specifically for active powers higher than $p > 0.8$ p.u.. For lower active powers the difference is marginal. In fact, the optimization does not result in a significant non–uniform distribution of q_{WT} set–points. For the optimization-based strategies cases without uniform q_i set–points (S3 and S3var) the results in Figure 7
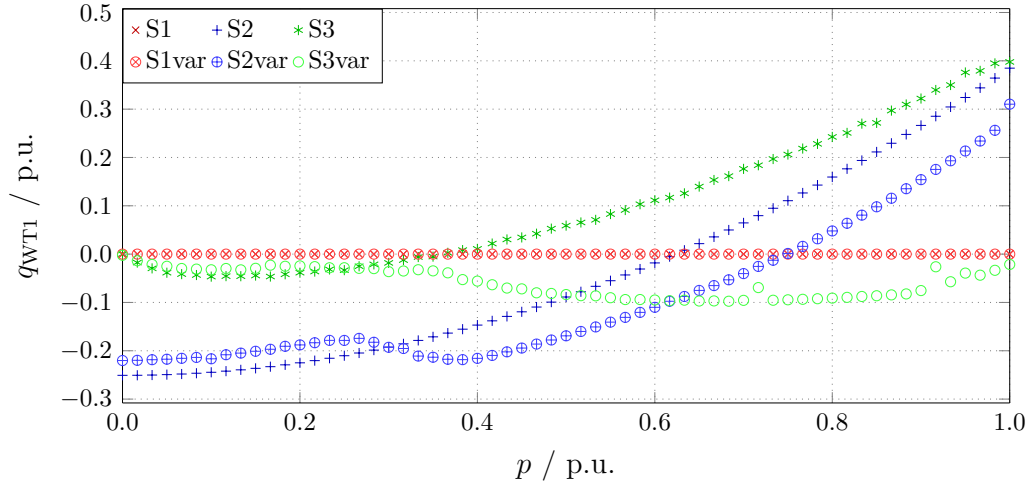
(a) WT1

(b) WT46

Figure 8: Reactive power injection by (a) the most remote and (b) the closest WT, respectively.

and Figure 8 show the contribution to the total amount of necessary reactive power by the WTs and the VSC–HVdc. Comparing the total reactive power

injection for S3 and S3var results in a lower value for strategy S3var than for S3. This effect is due to the additional variable PCC voltage reference u_{PCC} in strategy S3var which lowers the reactive power generation in the low power range by decreasing the system voltage. Furthermore, regarding the variation of the q_{WT} set–points for strategy S3var it can be seen that the values for WT1 and WT46 differ for active powers $p > 0.6\,\mathrm{p.u.}$ whereas WT1 is absorbing reactive power and WT46 is injecting reactive power. This operation of WT1 avoids a local voltage violation due to the higher PCC voltage for this strategy in this power range. Due to its vicinity to the PCC WT46 is not facing this constraint and injects reactive power to compensate. The other variable strategies S1var and S2var lower the reactive power requirement with respect to their counterpart S1 and S2, respectively. This holds true expect for an intermediate power range $0.25\,\mathrm{p.u.} < p < 0.68\,\mathrm{p.u.}$ for S1 against S1var whereas $0.3\,\mathrm{p.u.} < p < 0.7\,\mathrm{p.u.}$ for S2 versus S2var.

Figure 9 shows the PCC voltage set–point u_{PCC}. For the strategies S1 to S3 the u_{PCC} is fixed at $1.0\,\mathrm{p.u.}$. The variable strategies S1var and S2var result in similar u_{PCC} profiles as S3var. In the lower power range the system voltage is decreased to reduce the reactive power requirements (and related power losses) and the associated power losses in the converters whereas for higher powers the increase of the system voltage leads to lower losses.

The loss distribution in the system appears as component losses of the GSC, the WT transformer and filter, the $33\,\mathrm{kV}$ collection grid, the WPP transformers, the HVac export cables and the VSC–HVdc (incl. HVdc transf.). The loss distribution results in Figure 10 and Figure 11 consider the cases where zero or full power is generated, respectively. The power losses differ-
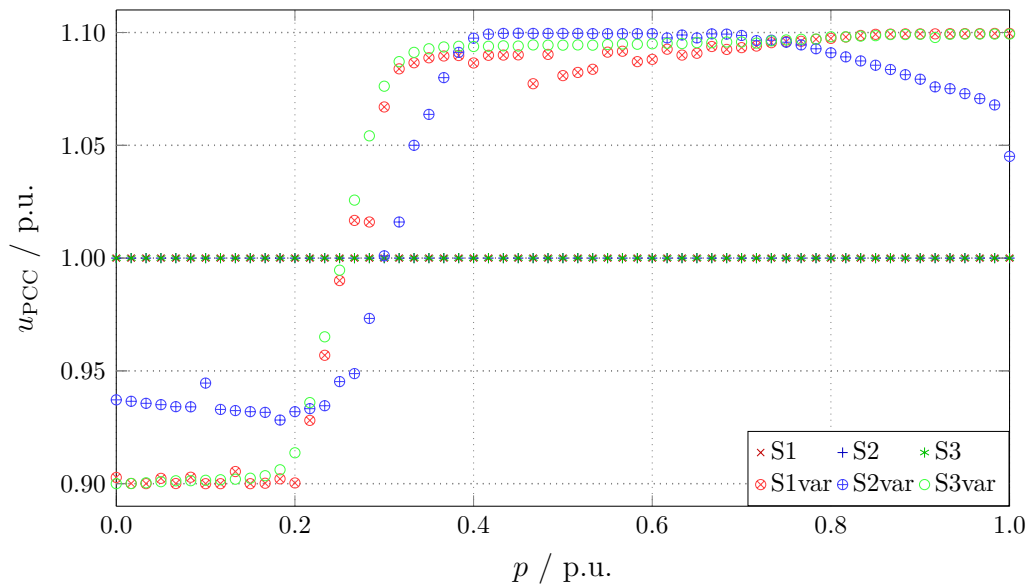
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Figure 9: PCC voltage reference set–point imposed by the VSC–HVdc.

ences between the strategies occur mainly in the converters and transformers (no–load losses) for low power (Figure 10) and in the grid components for the full power case (Figure 11). The higher voltage in the offshore grid for S1var to S3var reduces the losses of the grid components in general. From the results for the converter losses for S2 and S2var in the low power scenario it can be concluded that higher losses occur in the GSC and lower losses in the VSC–HVdc compared to the other strategies. Overall, this results in a higher relative loss for strategy S2 compared to S1 in the low power range as depicted in Figure 6.

Figure 12 provides information on voltage values for relevant busbars in the system. The plots use boxplots to display mean, 25 % and 75 % percentiles as well as minimum and maximum values of the corresponding sets over the whole power range. In Figure 12a the voltage levels are shown
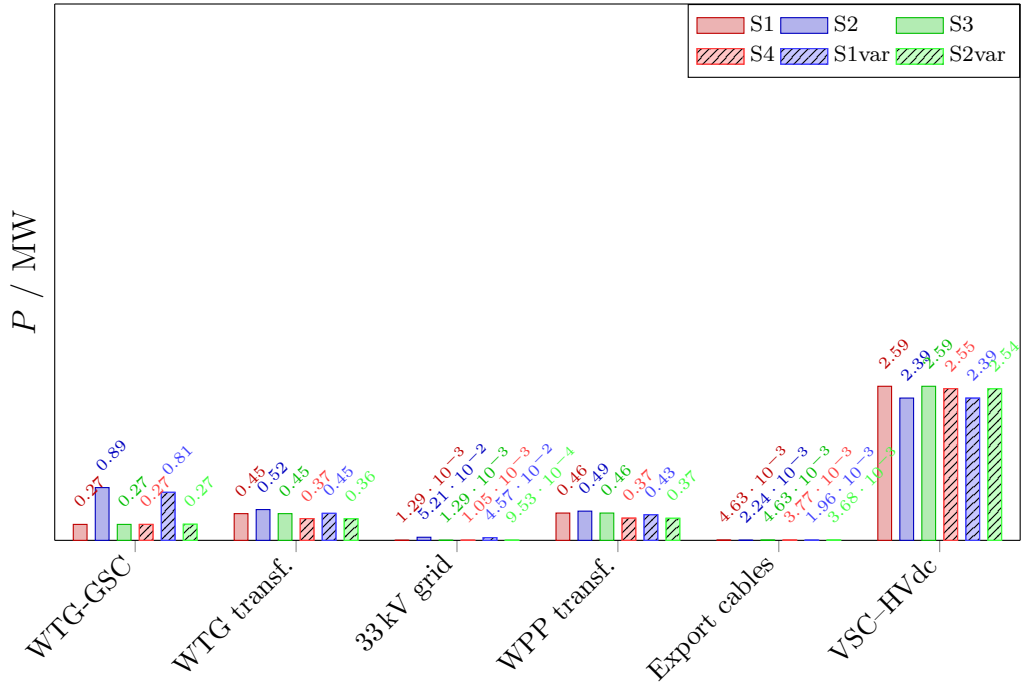
Figure 10: Distribution of losses in the system for $p = 0.0\,\mathrm{p.u.}$.

for strategies S1 to S3 specifically for the busbars of the HV–side of the WT transformers, the LV–side of the WPP transformers, denoted as offshore substation (OSS), and the PCC voltage. Figure 12b displays the voltage levels for the variable strategies S1var to S3var. Firstly, the voltages are kept within the admissible voltage limitations for all busbars and strategies. Secondly, it can be seen that the mean voltages for the WTs are higher for S3 compared to S1 and S2 due to the optimization procedure. The variable strategies S1var and S2var explore a wider voltage band compared to their counterparts. For strategy S1var and S3var the voltages of the WTs are almost exclusively close to the upper limit of $1.1\,\mathrm{p.u.}$. Among the fixed reference voltage strategies S1 has the most varying voltage profile at the OSS busbar whereas S2 keeps
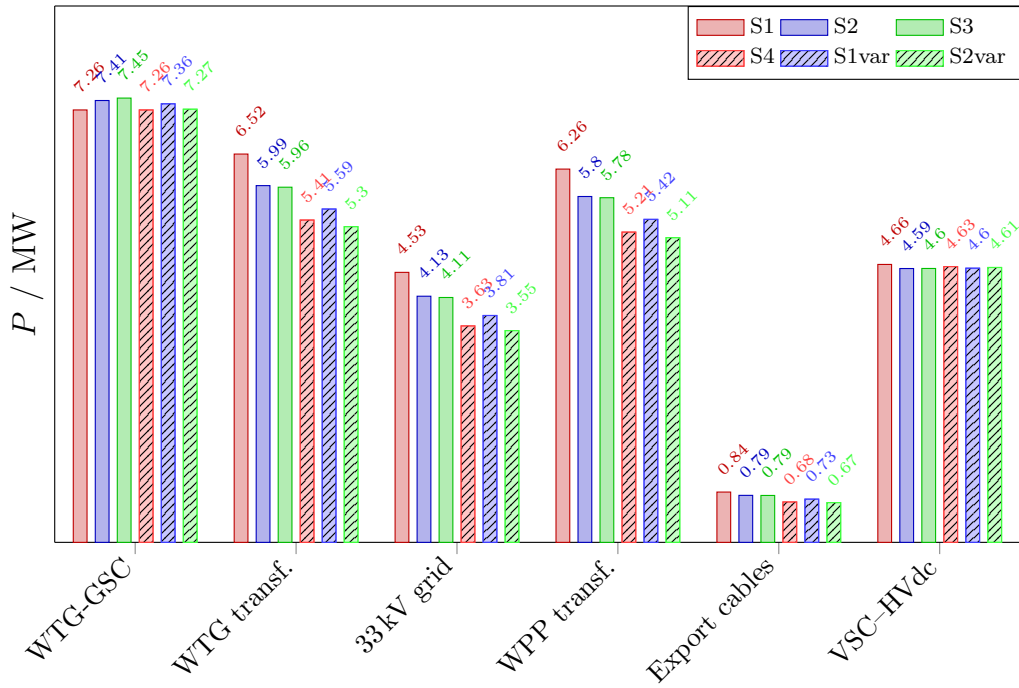
Figure 11: Distribution of losses in the system for $p = 1.0\,\mathrm{p.u.}$.

its values closely below $1\,\mathrm{p.u.}$. The values for S3 show insignificant variation for this busbar slightly above $1\,\mathrm{p.u.}$. For the variable strategies this busbar voltage correlates with the variable PCC voltage.

Figure 13 depicts the reactive power injections by the GSCs and the VSC–HVdc. Again, Figure 13a displays the results for the fixed voltage strategies whereas Figure 13b contains the results for the variable strategies. Firstly, the plots show that S1 and S2 both cause a uniform reactive power injection by the WTs. The values for S3 (for S3var, respectively) vary from each other and demonstrate the variable distribution of set–points caused by the optimization routine, respectively. For strategy S3, the reactive power values of the GSC are mainly injections which result in a generally higher voltage

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in the WPP grid when compared to S1 and S2. In contrast, for strategy S3var the use of a high PCC voltage reference results in a partly inductive operation of the GSCs in order keep the voltage inside the upper limit. This is especially the case for WTs which are very remote to the PCC busbar such as WT1 (see also Figure 8a). Secondly, the variation of the reactive power injection by the VSC–HVdc is the highest for S1 whereas S3 is kept within a moderate range absorbing reactive power. The plot of S2 consequently results to zero reactive power exchange. For strategy S3var the VSC–HVdc operates mainly absorbing reactive power unless for higher powers where it injects reactive power. Contemplating the combination of both the WT and the VSC–HVdc results it is obvious that S3 and S3var reach a sharing of reactive power injection within the WPP. The variable strategies result in less reactive power injection variation than their respective fixed strategies. This is caused by the variable PCC voltage which lowers the reactive power requirements of the converters in the system.

The annual energy loss (AEL) obtained by applying the different strategies is displayed in Table 3. For S2 the absolute energy losses are reduced by 696 MWh and for S3 by 2131 MWh compared to strategy S1, respectively. The variable strategies permit a further loss reduction: S1var 6320 MWh, S2var 4224 MWh and S3var 6819 MWh in comparison to S1, respectively. The monetary saving of these additional active power in–feeds is of 90 k€ for S2, 277 k€ for S3 and oscillates between 549 k€ and 886 k€ for the variable strategies, respectively.
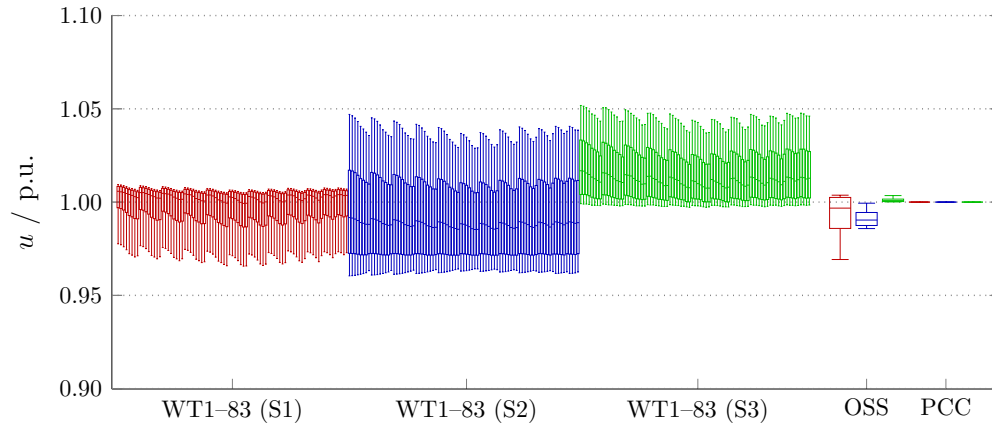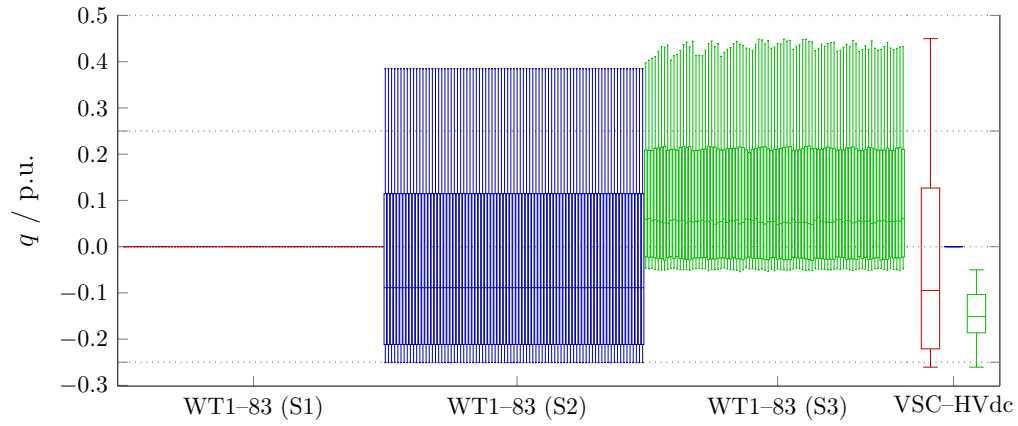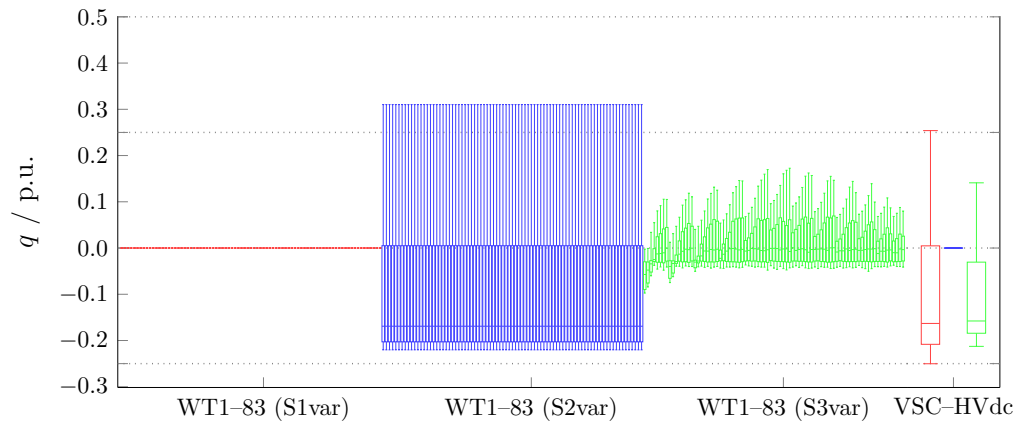
(a)
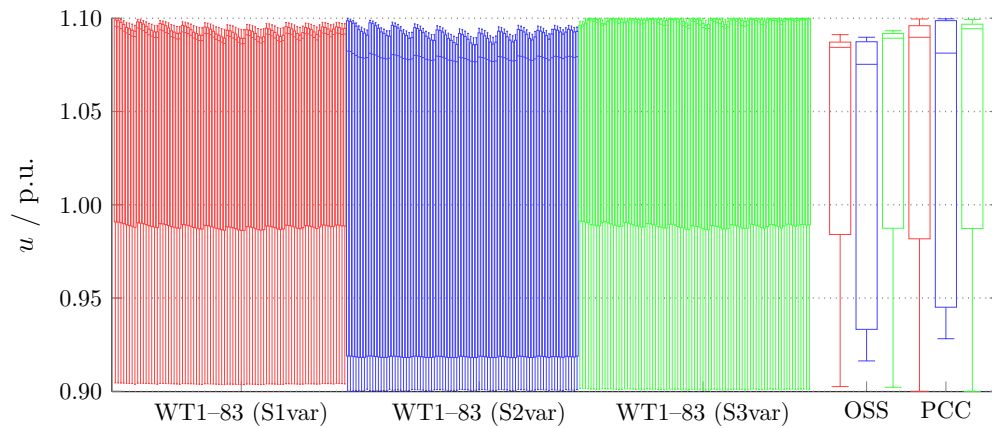
(b)

Figure 12: Voltage distribution of (a) fixed reference voltage strategies and (b) variable reference voltage strategies. The boxplots show mean, 25 %–, 75 %–percentiles, minimum and maximum values. The HV–side busbars of the WT transformers, the LV–side of the WPP transformer (OSS) and the PCC busbar are displayed.

5. Conclusions and recommendations

This work presented reactive power and voltage control concepts to operate HVdc–connected WPPs aiming to minimize overall system losses. The

(a)

(b)

Figure 13: Reactive power injections of (a) fixed reference voltage strategies and (b) variable reference voltage strategies. The boxplots show mean, 25 %–, 75 %–percentiles, minimum and maximum values. All GSC and VSC–HVdc reactive power injections are plotted. A positive value expresses to a reactive power injection (capacitive).

WT reactive power set–points and the PCC reference voltage imposed by the offshore VSC–HVdc are calculated to gain minimal losses in the system by

Table 3: AEL and the monetary equivalent (ME) thereof.

	S1	S2	S3	S1var	S2var	S3var
AEL / GWh	94.54	93.84	92.41	88.22	90.3	87.72
ME / M€ yr^{-1}	12.29	12.20	12.01	11.47	11.74	11.40

means of an optimization–based algorithm. First, a loss assessment has been conducted for such HVdc–connected WPPs where the collection grid and converter losses of the VSC–HVdc as well as of the WTs are considered. A case study for a 500 MW–sized reference WPP was performed for the whole active power range to draw conclusions for six different reactive power control concepts. From the results it was concluded that the optimization–based reactive power control contributes to a reduction of energy losses by up to 4 % for a fixed PCC voltage and up to 10 % with the incorporation of a variable PCC voltage set–point in comparison to unity PF operation of the WTs. Moreover, it was found that in case of the conventional reactive power allocation strategies the application of a single reactive power injection responsibility for either GSCs or the VSC–HVdc is not optimal considering the whole power range. Consequently, the use of an optimization–based algorithm results in a share of the reactive power injection responsibility between the WT and the VSC–HVdc. The application of the variable strategies S1var, S2var or S3var result in lower losses and mostly lower reactive power injections at the expense of a wider usage of the continuous voltage operation band. The deployment of the variable strategy might cause the system to operate continuously at its voltage limits which might inherently

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violate them if the system operating point changes. This drawback might be counteracted with an additional security margin on the voltage limits in the optimization algorithm. The results of the optimization–based controllers motivate the implementation of such into the central WPP control. Furthermore, the involved parties in the system which are generally the offshore transmission asset owner (HVdc system owner) and the WPP owner could share the additional benefits of a calculated $886\,\mathrm{k}{\mbox{\euro}}$ annual cost reduction for the $500\,\mathrm{MW}$ case study performed in this paper.

Acknowledgements

Appendix A.

Table A.4: Reference data and relevant system parameter.

WT grid connection

Nominal voltage (U_{ac}/kV)	0.9
GSC (S_n/MVA, $\cos\varphi$)	6.67, ±0.9
Coupling impedance (r/p.u., x/p.u.)	0.004, 0.13
MV transformer (*LV/HV*, S_n/MVA, r/p.u., x/p.u., *no–load losses*/p.u.)	0.9/33, 6.7, 0.009, 0.06, 0.0008

MV collection grid

Nominal voltage (U_{ac}/kV)	33
Total cable length (l/km)	118
Total number of turbines	83
HV transformer (*N*, *LV/HV*, S_n/MVA, r/p.u., x/p.u., *no–load losses*/p.u.)	2, 33/220, 280, 0.003, 0.15, 0.0004

HVac export cable

Nominal voltage (U_{ac}/kV)	220
Export cable(s) (*N*, A/mm², l/km)	2, 800, 10

HVdc transmission

Nominal voltages (U_{ac}/kV, U_{dc}/kV)	333, ±320
Converter (topology, S_n/MVA, $\cos\varphi$)	HVdc–MMC, 555.6, ±0.9

Table A.5: Data for XLPE submarine cables [42, 43, 44].

U_r / kV	A / mm²	I_r / A	R' / Ω km^{-1}	L' / mH km^{-1}	C' / μF km^{-1}
33	240	581	0.098	0.36	0.23
33	630	904	0.041	0.31	0.34
220	800	830	0.032	0.40	0.17

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