# The Red Radio Ring: a gravitationally lensed hyperluminous infrared radio galaxy at z = 2.553 discovered through the citizen science project SPACE WARPS

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# ABSTRACT

We report the discovery of a gravitationally lensed hyperluminous infrared galaxy (intrinsic  $L_{\rm IR} \approx 10^{13} \, \rm L_{\odot}$ ) with strong radio emission (intrinsic  $L_{1.4 \, \rm GHz} \approx 10^{25} \, \rm W \, Hz^{-1}$ ) at z = 2.553. The source was identified in the citizen science project SPACE WARPS through the visual inspection of tens of thousands of iJKs colour composite images of luminous red galaxies (LRGs), groups and clusters of galaxies and quasars. Appearing as a partial Einstein ring ( $r_e \approx 3$ arcsec) around an LRG at z = 0.2, the galaxy is extremely bright in the sub-millimetre for a cosmological source, with the thermal dust emission approaching 1 Jy at peak. The redshift of the lensed galaxy is determined through the detection of the  $CO(3 \rightarrow 2)$  molecular emission line with the Large Millimetre Telescope's Redshift Search Receiver and through [O III] and  $H\alpha$  line detections in the near-infrared from Subaru/Infrared Camera and Spectrograph. We have resolved the radio emission with high-resolution (300–400 mas) eMERLIN L-band and Very Large Array C-band imaging. These observations are used in combination with the nearinfrared imaging to construct a lens model, which indicates a lensing magnification of  $\mu \approx 10$ . The source reconstruction appears to support a radio morphology comprised of a compact (<250 pc) core and more extended component, perhaps indicative of an active nucleus and jet or lobe.

Key words: methods: miscellaneous - galaxies: high-redshift.

# **1 INTRODUCTION**

Strong gravitational lenses are striking astrophysical laboratories that allow us to study the structure and distribution of matter in and around massive galaxies and clusters (Koopmans et al. 2006; Ruff et al. 2011; Sonnenfeld et al. 2013; Richard et al. 2014), cosmography through quasar time delays (Refsdal 1964; Tewes, Courbin & Meylan 2013; Suyu et al. 2013), perform highly detailed investigations of early galaxies (e.g. Kneib et al. 2005; Stark et al. 2008; Swinbank et al. 2009) and even detect the first galaxies (Kneib et al. 2004; Zheng et al. 2012; Zitrin et al. 2014). The number of confirmed gravitational lenses is still relatively low: only some 500 are confirmed to date. With diverse astrophysical and cosmological

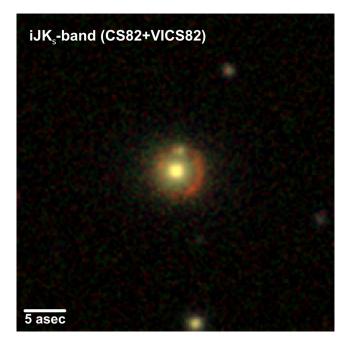
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applications, surveys for new strong gravitationally lensed systems remain a useful endeavour. In this article, we present new results from a novel search for new gravitational lens systems using widefield near-infrared and optical data. Lens searches in the visible bands are typically optimized for finding blue arcs, representing the images of star-forming galaxies in the early Universe (which are abundant). Searches at longer (near-infrared and beyond) wavelengths have the advantage of selecting dust-obscured or very high redshift sources that could easily be missed in optical searches (e.g. Negrello et al. 2010; Vieira et al. 2013).

The VISTA-CFHT Stripe 82 survey (VICS82; Geach et al., in preparation) is a wide area near-infrared survey of the Sloan Digital Sky Survey (SDSS) Stripe 82 with Canada-France-Hawaii Telescope (CFHT)/WIRCam and VISTA/VIRCAM, covering 130 deg<sup>2</sup> to a  $5\sigma$  depth of approximately 22nd AB magnitude in the J and  $K_{\rm s}$  bands. Stripe 82 is also covered by deep (24th magnitude) *i*band imaging from the CFHT in the CS82 survey (Moraes et al. 2014; Erben et al., in preparation) with comparable image quality (sub-arcsecond), as well as the deeper coverage from SDSS itself across the equatorial stripe. The combination of moderately deep optical-near-infrared imaging over a wide area is ideal for searches for strong, 'red' gravitational arcs. After serendipitously finding a handful of promising lens candidates through visual inspection, we decided to pass the data set to SPACE WARPS (Marshall et al. 2015; More et al. 2015). SPACE WARPS is a citizen science project to discover gravitational lenses run as part of the Zooniverse family<sup>1</sup> of online projects (Marshall et al. 2015; More et al. 2015).

Gravitational lens discovery remains a labour-intensive process, even automated algorithms produce highly impure samples that require visual inspection for verification (Marshall et al. 2009; More et al. 2012; Gavazzi et al. 2014; Chan et al. 2014; Brault & Gavazzi 2015). SPACE WARPS was conceived to mitigate this issue for gravitational lens searches in the era of large surveys which have the potential to increase current sample sizes by several orders of magnitude. Through an online interface, users (the general public) are presented with tens of thousands of images, each of which are inspected for evidence of strong gravitational lensing. A sophisticated training scheme using images containing realistic simulated lenses, built into the inspection interface, is used to simultaneously train users and calibrate the classification process (Marshall et al. 2015; More et al. 2015). Humans are highly proficient at detecting the often very subtle - features associated with gravitational lenses, and so harnessing the power of a natural neural network of several tens of thousands of 'nodes' is a particularly efficient approach to this problem.

The VICS82+CS82 search with SPACE WARPS (actually the second incarnation of the project, the first was an optical search within the CFHT-Legacy Survey) was accelerated by being launched on *Stargazing Live!*, broadcast on 2014 January 7 to approximately 2 million viewers in the United Kingdom by the British Broadcasting Corporation. The goal of *Stargazing Live!* is to engage the public with astronomy-related activities ranging from amateur pursuits through to the communication of the latest scientific research, major missions and projects. The wide reach of this programme (which was run over three consecutive nights) makes it an exceptionally successful and efficient public engagement tool for promoting astronomy, and indeed science in general. SPACE WARPS was phenomenally successful: by the end of the final programme on January 9, over 7.5 million classifications of images had been logged,



**Figure 1.** The colour composite image of 9io9 that was presented to online visitors to SPACE WARPS . Users were presented with a (random) sequence of 40 arcsec cut-out images where the blue channel represents *i*-band data from the CHFT Stripe 82 (CS82) survey (Erben et al., in preparation) and the green and red channels are *J*- and *K*<sub>s</sub>-band imaging from the VISTA-CFHT Stripe 82 (VICS82) survey (Geach et al., in preparation). Images were centred on luminous red galaxies (LRGs), groups and clusters and quasars. Volunteers were asked to identify potential lensed features, having been trained using simulated images. In this case, a red ring of radius  $\approx 3$  arcsec can be seen around the central galaxy (an LRG at z = 0.2). This system was independently identified by several users and quickly became a high-confidence lens candidate.

such that each  $iJK_s$ -band image in the sample was independently viewed approximately 200 times. Out of several tens of excellent lens candidates identified by the collective efforts of all participants of SPACE WARPS, the best candidate we have appears to be an active, dust-obscured source at  $z \approx 2.5$ . Dubbed '9io9' (a shortening of its SPACE WARPS identifier ASW0009io9<sup>2</sup>), the target appears as an incomplete red Einstein ring of radius approximately 3 arcsec around a luminous red galaxy (LRG) at z = 0.2 (Fig. 1).

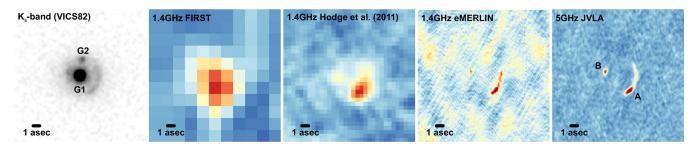
In this paper, we present follow-up observations and lens modelling of 9io9 that reveal the galaxy to be an intrinsically radio- and sub-millimetre-bright hyperluminous infrared galaxy  $(L_{\rm IR} > 10^{13} \, {\rm L_{\odot}})$  at z = 2.553. In Section 2, we describe archival and new observations of 9io9, in Section 3 we constrain the integrated spectral energy distribution (SED) of the galaxy and model the lens itself, and in Section 4 we conclude with a brief discussion of the likely nature of 9io9. Throughout we assume a fiducial cosmology where  $\Omega_{\rm m} = 0.3$ ,  $\Omega_{\Lambda} = 0.7$  and  $H_0 = 70 \, {\rm km \, s^{-1} \, Mpc^{-1}}$ .

# 2 OBSERVATIONS

# 2.1 Radio

Immediately upon the discovery of the lens candidate during SPACE WARPS we cross-checked the position of the source

<sup>2</sup> http://talk.spacewarps.org/#/subjects/ASW0009io9.



**Figure 2.** Images of 9io9 (aligned north up, east left): left to right: (a)  $K_s$ -band image. The small point source (G2) to the north of the central (lensing) galaxy G1 is not a background source, but likely a satellite of the lensing galaxy at z = 0.202 (b) VLA FIRST 1.4 GHz image showing the radio detection, peaking slightly SW of the central LRG, (c) higher resolution 1.4 GHz VLA imaging from the survey of Hodge et al. (2011), showing that the radio emission resolves into a ring configuration that traces the near-infrared light, but with a clear peak at the SW, (d) eMERLIN 1.4 GHz map (300 mas beam) resolving two main radio components: an arc (A) and point source (B), (e) VLA 5 GHz image at similar resolution, again resolving the radio morphology. Our lens model (Section 3.2) indicates that B is the counterimage of the bright, compact component at the southern extent of A.

(02<sup>h</sup>09<sup>m</sup>41<sup>s</sup>3, +00°15′58″.6) in other imaging surveys. The Very Large Array (VLA) Faint Images of the Radio Sky at Twenty-Centimeters (FIRST) 1.4 GHz survey (Becker et al. 1994) reveals a 4 mJy radio source at this position, but the angular resolution of FIRST is too coarse to determine whether the radio emission originates from the background galaxy, or the lensing galaxy. Hodge et al. (2011) present higher resolution VLA (A and B configuration,  $\theta = 1.8$  arcsec) 1.4 GHz imaging of Stripe 82 that partially resolves the radio flux into a ring that follows the  $K_s$ -band light (Fig. 2). This motivated us to obtain higher resolution radio imaging of 9io9, which we describe here.

# 2.1.1 eMERLIN L band

We obtained eMERLIN observations over 10.25 h between 1415 UT 2014 January 9 to 0030 UT 2014 January 10 (during the television broadcast). The target source was interspersed with the phase reference calibrator (J0208-0047) with a cycle time of 10 min with 7 min on the target and 3 min on the phase reference. Thirty seconds of data were flagged at the start of each scan to remove corrupted data logged during telescope drives with a resulting total time on the target source of 6.72 h. The data were divided into eight intermediate frequencies (IFs) with a total observing bandwidth of 512 MHz at a centre frequency of 1.5185 GHz. Data calibration was performed from calibration scans on the resolved flux density calibrator 3C 286 (1331+305) and the point source calibrator OQ208 (1407+284). The flux density scale assumed for 3C 286 incorporated the latest coefficients from Perley & Butler (2013) and a standard model of spatial resolution of the source as observed by eMERLIN. These were used to derive flux densities for the point source OQ208 which has a rising spectrum across the observed band (IF1: 0.815 Jy, IF8: 1.208 Jy), with a value at the central frequency of 1.0078 Jy. Estimated errors in the flux density scale are at the level of 5-10 per cent. Residual delay corrections for the data throughout the run were derived from all three calibration sources. After performing phase and minor gain corrections derived from the phase calibrator, the target was imaged and several rounds of phase-only self-calibration applied. The data calibration and image processing was performed in AIPS. The final beam is nearly circular with Full Width at Half Maximum (FWHM) 300 mas, and the map rms is 16  $\mu$ Jy beam<sup>-1</sup>.

#### 2.1.2 Karl G. Jansky Very Large Array C band

Data were obtained during 2014 March 1 using the three-bit samplers and an advanced mode of the immensely powerful WIDAR correlator at the heart of the Karl G. Jansky VLA (proposal 13B-458), with eight sub-bands in each of the A1/C1, A2/C2, B1/D1 and B2/D2 basebands. We used the VLA's C-band receivers with the correlator instructed to record a band comprising  $1024 \times 62.5$  kHz full-polarization channels centred on the 22.23508 MHz water line, tracking a barycentric redshift of 2.5529. We also recorded 31 wider bands to sample continuum emission, each comprising  $128 \times 1$  MHz dual-polarization channels, covering 4.05–7.96 GHz contiguously, with a few small regions of overlap. To mitigate time smearing, since we used the widest (A) configuration of the VLA, the integration time was set to 2 s, which resulted in a total data rate of 62 Gb  $h^{-1}$ , with 26  $\times$  287 s (roughly 2 h) spent integrating on 9io9,  $27 \times 31$  s on the gain calibrator, J0215–0222, and 226 s on 0137+331 (3C 48) to set the flux density scale. The data were calibrated using version 4.1 of CASA, starting with a pass through the initial stages of the VLA data pipeline, then flagging extensively by hand, then re-starting the pipeline where we had previously paused. CASA was also used for imaging, which required us to map and clean a number of bright, nearby sources to reduce contamination of the region around 9io9 by strong sidelobes. The resulting image of 9io9, centred at 5 GHz, has a  $500 \times 400$  mas beam (position angle,  $PA = 7^{\circ}$ ), with an rms noise level of 3–4 µJy beam<sup>-1</sup>.

# 2.2 Sub-millimetre and millimetre

A large area of Stripe 82 has been mapped at 250, 350 and 500  $\mu$ m with *Herschel*, as part of The *Herschel* Stripe 82 Survey (Viero et al. 2014). At the position of 9io9, there is bright sub-millimetre detection, with  $S_{250} = 826 \pm 7$ ,  $S_{350} = 912 \pm 7$  and  $S_{500} = 717 \pm 8$  mJy. The low resolution of *Herschel* cannot spatially resolve the emission, but the sub-millimetre colours are consistent with the emission originating from the background source at  $z \sim 2-3$  (the lensing galaxy is not expected to be a significant source of sub-millimetre emission). In order to better constrain the shape of the far-infrared SED and determine the redshift of the lensed source, we obtained further sub-millimetre imaging and spectroscopy that we describe in the following.

### 2.2.1 James Clerk Maxwell Telescope SCUBA-2

We obtained a 30 min observation of 9io9 with the SCUBA-2 camera on the James Clerk Maxwell Telescope (JCMT) on 2014 January 15 as part of Director's Discretionary Time (project M13BD12). SCUBA-2 records both 450 and 850 µm data simultaneously. We employed the DAISY scanning mode, appropriate for point sources, and the zenith opacity at 225 GHz was  $\tau_{225 \text{ GHz}} = 0.07-0.1$  over the course of the observation. The data were reduced with the dynamic iterative map maker of the SMURF package (Jenness et al. 2011; Chapin et al. 2013) and optimally filtered for detection of point sources. We applied flux conversion factors (FCFs) of 491 and 537 Jy pW<sup>-1</sup> at 450 and 850 µm, respectively, which are the canonical FCFs derived from observations of hundreds of standard sub-millimetre calibrators observed by SCUBA-2 since operations began (Dempsey et al. 2013). An additional correction of 10 per cent is made to the FCFs to account for flux lost during the filtering steps. The absolute flux calibration at 850 µm is accurate to within 15 per cent.

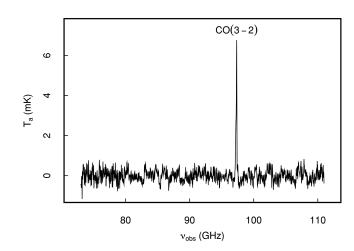
9io9 is detected with  $S_{850} = 167 \pm 4$  mJy (the JCMT beam at 850 µm is 15 arcsec, and so this can be considered an integrated measurement). At the same position in the 450 µm map, we measure  $S_{450} = 217 \pm 72$  mJy, this is a factor of 3 lower than the *Herschel* measured flux at approximately the same wavelength. Given the ~5 × finer resolution of JCMT/SCUBA-2 compared to *Herschel*/SPIRE at 500 µm, it is possible that SCUBA-2 is resolving the emission into several beams, rendering some of the sub-millimetre emission undetectable. This offers a first insight into the distribution of cold dust in 9io9: higher resolution sub-millimetre mapping with a powerful interferometer such as the Atacama Large Millimeter Array will allow us to compare the dust and radio morphologies on comparable angular scales.

# 2.2.2 Large Millimeter Telescope AzTEC 1.1 mm and Redshift Search Receiver

The Large Millimeter Telescope Alfonso Serrano, hereafter LMT, is a 50 m diameter millimetre-wavelength radio telescope on Volcán Sierra Negra, Mexico, at an altitude of 4600 m. LMT 'Early-Science' observations were conducted towards 9io9 with AzTEC (Wilson et al. 2008) and the Redshift Search Receiver (RSR; Erickson et al. 2007), operating in the 1 and 3 mm atmospheric windows, respectively. During the 'Early-Science' programme only the inner 32 m diameter of the LMT primary surface was aligned and coupled to the scientific instruments.

Continuum imaging of 9io9 was first conducted at 1.1 mm with the AzTEC camera on 2014 January 16 UT, and then repeated on 2014 January 24 ut due to a poor focus in the original observations. The highest quality observations however were obtained during the early evening of 2014 November 2 ut under improved weather conditions with a 225GHz zenith opacity of  $\tau_{225 \text{ GHz}} \approx 0.08$ . The measured beam-size at 1.1 mm was  $8.5 \times 7.9$  arcsec<sup>2</sup> FWHM in azimuth and elevation, respectively. The AzTEC observations were made in the standard Photometry Map Mode using a Lissajous scanning pattern, and reduced using the standard AzTEC data-analysis pipeline (Scott et al. 2008). Flux calibration was performed against Neptune, assuming a 1.1 mm flux density of 18.38 Jy. A short 4 min AzTEC integration detected the source 9io9 with a signal-to-noise ratio, S/N=39 and a flux density of 95.5  $\pm$  2.4 mJy, with no suggestion of extended emission. The accuracy of the absolute flux calibration is estimated to be  $\sim 10$  per cent.

The LMT operates with an ultra-wideband spectrometer, the RSR that covers the full 3 mm atmospheric window (73–111 GHz) at low spectral resolution (31 MHz channels,  $\sim$ 100 km s<sup>-1</sup> at 90 GHz). The RSR is a dual-beam dual-polarization spectrometer, with 38 GHz instantaneous bandwidth, designed to detect molecular gas, typically CO line transitions, from high-redshift galaxies. A 1 h integration with the RSR was conducted towards 9io9 on 2014 January 19 UT



**Figure 3.** The Redshift Search Receiver spectrum of 9io9 showing the full 38 GHz instantaneous bandwidth spectral coverage in the 3 mm atmospheric window (73–111 GHz). The detected molecular line at 97.312 GHz is <sup>12</sup>CO(3–2) from the lensed background source at a redshift z = 2.553.

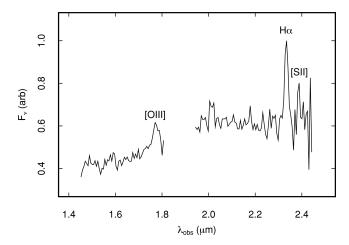
with a measured  $T_{sys}$  at 90 GHz of 85 K. The RSR data were reduced and calibrated using the LMT DREAMPY (Data REduction and Analysis Methods in PYthon) package. A single strong spectral-line was detected at 97.31 GHz (Fig. 3). The combination of the photometric redshift of  $z \sim 2.6$ , determined from the (sub-)millimetre and FIR observations presented in this paper, with the RSR spectrum eliminates alternative redshift solutions and any ambiguity in the measured spectroscopic redshift. We conclude that the detected line at 97.31 GHz is <sup>12</sup>CO(3–2) from the lensed background source at z = 2.553. Full details of the LMT observations towards 9io9, together with a more complete analysis of the AzTEC and RSR data, are presented in Sanchez-Argüelles et al. (in preparation) and Harrington et al. (in preparation).

#### 2.3 Near-infrared spectroscopy

We observed 9io9 with the Infrared Camera and Spectrograph (IRCS; Kobayashi et al. 2000) instrument on the Subaru telescope on the night of 2014 January 15 UT as a back-up target for the scheduled observing program.<sup>3</sup> The instrument was setup with the HK low-resolution grism covering the wavelength range 1.4–2.45 µm. We used the 0.9 arcsec wide slit of the 'Reflective 3W' slitmask, resulting in a spectral resolving power of  $R \approx 95$  at the central wavelength. The entrance slit was set at a PA of 155° east of north to align it to the bright, western half of the red ring. We observed 9io9 using the nod-on-slit technique with slit positions separated by 7 arcsec. We obtained 12 exposures for a total of 1 h on source. Calibration data comprised of argon lamp exposures for wavelength calibration.

The data were reduced with the IRAF TWODSPEC package, and standard procedures for flat-fielding and sky subtraction for the nod-on-slit technique were used. The final data product is a two-dimensional spectrum of 9io9 with a regular sampling along the spatial and spectral directions. To increase the S/N, we binned the data in spectral direction by a factor of  $6 \times$  and in the spatial direction by a factor of  $4 \times$ . The total integrated spectrum of the western arc of the red ring of 9io9 is shown in Fig. 4. The redshifted nebular

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<sup>3</sup> Proposal ID S13B-002.
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**Figure 4.** Observed near-infrared HK spectrum of the primary arc of 9io9 taken with IRCS on Subaru. The low-resolution spectrum shows the clear rest-frame optical emission lines of the unresolved [O III]  $\lambda\lambda$ 4959, 5007 doublet, H $\alpha$ +[N II], and the [S II]  $\lambda\lambda$ 6717, 6731 doublet, confirming the redshift of the lensed galaxy at z = 2.553 (see Section 2.3).

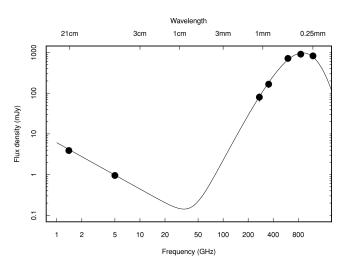
emission lines of H $\alpha$ +[N II] and (unresolved) [O III]  $\lambda\lambda$ 4959, 5007 and [S II]  $\lambda\lambda$ 6717, 6731 doublets are detected confirming the CO redshift of 2.553.

#### **3 ANALYSIS**

#### 3.1 Spectral energy distribution

In Fig. 5, we plot the (integrated) observed radio–sub-millimetre SED of 9io9. We model the sub-millimetre–millimetre photometry with a single temperature (T) modified blackbody

$$S_{\nu} \propto \frac{(1 - e^{-\tau(\nu)})\nu^3}{e^{h\nu/kT} - 1},$$
 (1)



**Figure 5.** Observed radio-to-sub-millimetre spectral energy distribution (SED) of 9io9, showing the integrated flux density of the lensed galaxy (we assume no contribution from the lensing galaxy at these frequencies). The SED is well modelled by a combination of modified blackbody with  $T \approx 40$  K, describing the cold dust thermal emission, and a simple power law  $v^{-\alpha}$  at v < 50 GHz, with spectral index  $\alpha \approx 1.1$ , describing radio synchrotron emission.

where the optical depth  $\tau(\nu) = (\nu/\nu_0)^{\beta}$  is normalized to 100 µm (rest) and  $\beta$  is the emissivity parameter. Since the redshift is accurately known, we allow  $\beta$  and *T* to be free parameters. The best-fitting parameters are  $\beta = 2.2 \pm 0.4$ ,  $T = (38 \pm 4)$  K which provides a good model of the observed emission over 250– 1100 µm. The integrated (rest-frame) 8–1000 µm luminosity is  $\mu L_{\rm IR} = (1.3 \pm 0.1) \times 10^{14} \, {\rm L}_{\odot}$ , where  $\mu$  is the lensing magnification. Note that this might underestimate the total infrared luminosity since we have not modelled mid-infrared emission from warmer dust components. We fit the radio portion of the SED with a power law  $S_{\nu} \propto \nu^{-\alpha}$ , with  $\alpha = 1.11 \pm 0.05$ . The combined model SED is shown in Fig. 5.

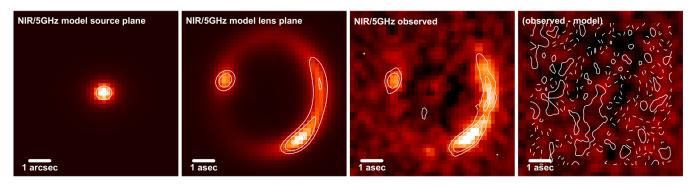
#### 3.2 Lens modelling

The system shows a primary lensing galaxy G1 and a secondary satellite galaxy G2, probably at the same redshift (z = 0.206, see Figs 1 and 2). We choose an isothermal ellipsoid for the density profile of G1. Since G2 is located close to, and likely part of, the lens system, we model its density profile with an additional isothermal sphere. The parameters of the model are: positions and critical radius (*b*) for G1 and G2, ellipticity ( $\epsilon$ ) and PA for G1 ( $\theta_{\epsilon}$ ), together with an external shear magnitude ( $\gamma$ ) and PA ( $\theta_{\gamma}$ ). We use a Gaussian prior ( $\epsilon = 0.1 \pm 0.1$ ) on the ellipticity of G1 and a uniform prior on the position of G2 obtained from the optical light profile fitting of the galaxies.

The lens mass model is optimized to simultaneously fit the extended images from the K<sub>s</sub>-band image (seeing  $\theta = (0.8 \pm 0.1)$  arcsec) and the VLA 5 GHz data where the lensed arc and the counter image are detected with sufficient signal to noise. The absolute astrometric calibration of the radio images is better than 100 mas, and we cannot improve the relative alignment of the near-infrared and VLA images. Furthermore, we acknowledge that setting the source model to be coincident in the near-infrared and radio is an assumption that does not take into account the possibility that these have different source plane morphologies. However, it is necessary to make this assumption with the current data in order to reduce free parameters and degeneracies in the modelling. An annulus centred on the lens enclosing the arc and the counterimage is used as a constraint when optimizing the lens model. We model the background source in the near-infrared with a Sérsic profile (flux, position, ellipticity and PA, effective radius and Sérsic index) and in the radio with a Gaussian profile. We set the sources at both wavelengths to be coincident as we expect them to be physically associated.

To construct the mass model, we use *gravlens* (Keeton 2011) and a Markov Chain Monte Carlo (MCMC) simulation for the fitting procedure (using the PYTHON module EMCEE; Foreman-Mackey et al. 2013) to optimize the parameters and explore degeneracies in the model. Initially, the position of G1 is held fixed during optimization and after a reasonable model is found the position is allowed to be free. The source plane model, model lensed images and residuals (for both wavelengths) are shown in Fig. 6. The magnification in the near-infrared is  $\mu_{\text{NIR}} \approx 11$  and in the radio is  $\mu_{5 \text{ GHz}} \approx 13$ , the unlensed magnitude of the source is  $K_{\text{s}} = 20.75$  mag and  $S_{5 \text{ GHz}} = 1.2$  $\mu$ Jy beam<sup>-1</sup>. The parameters of the best-fitting lens model are summarized in Table 1. The critical radii from Table 1 can be taken with the lens and source redshifts to calculate the lens velocity dispersion for G1 and G2:  $\sigma_{\text{G1}} = 316 \pm 1$  and  $\sigma_{\text{G2}} = 80 \pm 4 \text{ km s}^{-1}$ .

Although the eMERLIN data are of somewhat lower signal to noise, their higher resolution allows at least preliminary investigation of the radio source structure. Using the galaxy mass model



**Figure 6.** Mass modelling results based on joint fitting of the near-infrared imaging (colour map) and 5 GHz imaging (shown as contours at levels of  $0.0033 \times (3.9,27)$  mJy beam<sup>-1</sup>). Left: source plane model (centre left) the reconstructed image in the lens plane with the lensing galaxies G1 and G2 subtracted, (centre right) observed data linearly scaled between  $-3\sigma$  and  $10\sigma$ , (right) residual (observed-model). The residual colour scale (near-infrared) is the same as the previous panel and the contours are at levels of  $0.0033 \times (-1,1)$  mJy beam<sup>-1</sup>. Images are orientated north up, east left.

**Table 1.** Best-fitting parameters describing the lens system comprised of components G1 and G2. Positions are given relative to the coordinates  $(02^{h}09^{m}41^{s}268, +00^{\circ}15'58''_{.5}59)$ . Note that there is a degeneracy between the ellipticity of G1 and the shear magnitude and similarly, between the mass (or the critical radius) of G1 and G2. Uncertainties reflect the 16th and 84th percentile range derived from the MCMC fitting of the mass model.

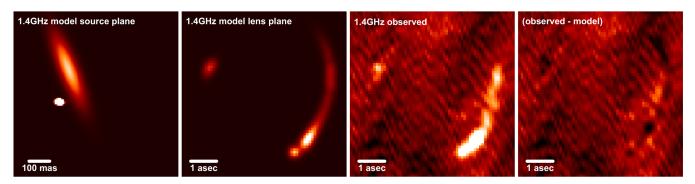
Parameter	G1	G2
$\overline{x \text{ (mas)}}$	$-94^{+9}_{-13}$	$377^{+17}_{-32}$
y (mas)	$126^{+4}_{-10}$	$2332^{+255}_{-2}$
Critical radius (b, arcsec)	$2.48^{+0.02}_{-0.01}$	$0.16^{+0.02}_{-0.01}$
Ellipticity $(\epsilon)$	$0.12\pm0.02$	-
PA ( $\theta_{\epsilon}$ , deg)	$84^{+3}_{-1}$	-
Shear magnitude $(\gamma)$	$0.064^{+0.005}_{-0.004}$	_
Shear PA ( $\theta_{\gamma}$ , deg)	83 <sup>+1</sup>	_

established above for the  $K_s$ -band and VLA imaging, we can attempt to reconstruct the eMERLIN data using a parametrized Gaussian fit to represent the source. The results are shown in Fig. 7. In general, the source reconstruction is subject to considerable degeneracy because the main constraint provided by the lensing concerns the source distribution around the high-magnification region corresponding to the caustic running across it. Nevertheless, the data indicate a double rather than a single Gaussian fit, if we believe the

structure at the southern end of the arc which is difficult to reproduce with a single component. The best-fitting model is subject to some degeneracies with the existing data, which can be investigated using a standard MCMC procedure. Specifically, the relative position of the centres of the components has an error approximately equal to their separation in the best-fitting model, with the more compact component contributing most of the positional error. The parameters describing the compact component, including its precise position, are uncertain apart from its size, which needs to be below approximately 30 mas, or 250 pc in the source plane. The more extended component is preferred to be elliptical  $(b/a = 0.27^{+0.15}_{-0.10})$ with PA  $15^{\circ} \pm 24^{\circ}$ ), and together the radio structure is reasonably consistent with that of a small radio core and jet, although higher signal-to-noise data would be needed to make a more definitive statement, we defer this, together with a more systematic source reconstruction using other methods to a future work.

# **4 DISCUSSION**

By simultaneously fitting the  $K_s$ -band and 5 GHz imaging we have derived a lens model that allows us to determine a magnification factor of approximately  $10 \times$ . The magnification-corrected infrared luminosity of 9io9 is  $L_{\rm IR} \approx 10^{13} \, {\rm L}_{\odot}$ , ranking it amongst the most luminous galaxies in the Universe, in the 'hyperluminous' class. If the entire infrared luminosity budget is dominated by star formation (i.e. reprocessed ultraviolet emission from massive stars),



**Figure 7.** Left: the reconstructed 1.4 GHz source model, using a two-Gaussian fit and the lens model described in Section 3.2. Note that the relative positions of the compact and extended components are not well constrained in the current model. Centre left: the reconstructed image in the lens plane, (centre right) eMERLIN observed data linearly scaled between  $-5\sigma$  and  $10\sigma$ , (right) residual (observed-model). The residual colour scale is the same as the previous panel. Note the scale bar for the source plane is 100 mas, corresponding to 820 pc in physical projection. With the exception of the first panel, images are centred on the position of the lensing galaxy G1 (Fig. 1). The source plane image is slightly offset from centre for illustration purposes. Images are orientated north up, east left.

then the implied star formation rate of 9io9 is  $\dot{M}_{\star} \approx 2500 \,\mathrm{M_{\odot}} \,\mathrm{yr^{-1}}$ (Kennicutt & Evans (2012), assuming a Chabrier initial mass function), a thousand times the star formation rate of the Milky Way. Given the radio flux density and reconstructed radio morphology described above, it is likely that 9io9 contains an active galactic nucleus (AGN) that contributes non-negligibly to the energy output, and therefore  $\dot{M}_{\star}$  should be taken as an upper limit, with the actual star formation rate scaling like  $\gamma L_{\mathrm{IR}}$ , where  $\gamma \approx 0.6$  for starburst/AGN composite systems at similar epoch with comparable  $L_{\mathrm{IR}}$ , determined through mid-infrared diagnostics (Coppin et al. 2010). Even with a 40 per cent correction for AGN contribution to  $L_{\mathrm{IR}}$ , the implied star formation rate is still remarkably high, at over a thousand solar masses per year.

In the absence of other diagnostics (such as the observation of broad lines, or emission line ratios such as  $[O ext{iii}]/H\beta$ ), the infrared-to-radio luminosity ratio can be used as a basic diagnostic for the presence of an AGN, described by the parameter

$$q = \log_{10} \left( \frac{L_{\rm IR}/3.75 \times 10^{12} \,{\rm W} \,{\rm m}^{-2}}{L_{1.4 \,{\rm GHz}}/{\rm W} \,{\rm m}^{-2} \,{\rm Hz}^{-1}} \right)$$
(2)

with the monochromatic radio luminosity K-corrected to the restframe 1.4 GHz assuming the measured  $\nu^{-1.1}$  spectral slope. Starforming galaxies have a rather tight distribution of q, with  $\langle q \rangle \approx 2.5$ and scatter of approximately  $\sigma_q \approx 0.25$  (e.g. Ivison et al. 2010). The radio-far-infrared correlation is thought to arise from two linked processes associated with massive star formation: (a) cosmic ray electrons from supernovae that emit synchrotron radiation as they are accelerated in magnetic fields, leaking out of dust-enshrouded HII regions, and (b) infrared emission originating from dust-reprocessed ultraviolet photons emitted by young massive stars. In galaxies hosting AGN, synchrotron emission associated with black hole accretion can contribute to the radio flux, resulting in lower q. In this case, the magnification-corrected radio luminosity is  $L_{1.4 \text{ GHz}} = (1.7 \pm 0.1) \times 10^{25} \text{ W Hz}^{-1}$ , implying  $q = 1.8 \pm 0.1$  (here we have assumed the same magnification correction for the radio and infrared emission,  $\mu = 13$ ). Thus, 9io9 is not consistent with a pure starburst, with significant nuclear activity associated with the growth of the central black hole contributing to the radio emission.

The current data allow us to postulate, with a reasonable degree of confidence, the basic nature of the radio source. There are some hints that the radio spectral index is flatter in the core component,  $\alpha \approx 0.2$  steepening to  $\alpha \approx 1$  along the ring. This would be consistent with the classic picture of optically thick emission due to synchrotron self-absorption around a compact, dense nuclear source. The steepening spectrum could indicate aging of the relativistic electron population (which lose their energy as  $E^2$ ) along a possible jet, but a more detailed analysis that takes into account the different visibilities sampled by eMERLIN and VLA, improved sampling of the radio spectrum and a more accurate lens model will be needed to investigate this. Considering the reconstructed source plane morphology, with compact core and potential jet/lobe structure, the radio power of 9io9 places it in the Fanaroff–Riley II class of radio galaxies ( $L_{1.4 \text{ GHz}} > 10^{25} \text{ W Hz}^{-1}$ ).

# 5 SUMMARY

Through a citizen science project – SPACE WARPS – we have discovered an extremely luminous galaxy at z = 2.5, close to the peak in stellar mass and black hole growth in the Universe, lensed by a foreground LRG, possibly part of a small group (given the large Einstein radius compared to typical single-galaxy lenses) at z = 0.2. The lensed source, dubbed 9io9, appears as a red Einstein ring, prominent in the near-infrared, but very faint in the optical (and thus would have been overlooked in an optical survey), characteristic of either a heavily dust-obscured or predominantly old stellar population. This lensed system would have been overlooked in an optical survey. Archival and subsequent follow-up observations revealed that 9io9 is extraor-dinarily bright in the sub-millimetre, with a flux density approaching 1 Jy at the peak of the thermal dust emission. We have resolved the lens at two radio frequencies, with sub-arcsecond eMERLIN and VLA mapping at 1.4 and 5 GHz, respectively, revealing radio emission from the source tracing the near-infrared light. The strong radio and infrared emission indicates a galaxy undergoing an episode of rapid growth, either in an intense starburst episode, through significant matter accretion on to a central supermassive black hole, or both.

A plausible evolutionary scenario for 9io9 is that the galaxy is destined to evolve into a massive  $(M_{\star} \approx 10^{11-12} \,\mathrm{M_{\odot}})$  elliptical galaxy by z = 0, perhaps located at the centre of a large group or cluster of galaxies. Seen when the Universe was less than 3 Gyr old, we are gaining an insight into the major growth phase of this massive galaxy, with gravitational lensing providing a unique window on to spatial scales not possible for an equivalent non-lensed field source. The fact that high-luminosity sources such as this are intrinsically rare even in the absence of lensing highlights the benefits that citizen science can offer in the mining of (ever growing) astronomical imaging archives, albeit at the cost of rather complex selection functions for the objects found. We plan further follow-up of 9io9 to improve our understanding of the source. Particularly exciting is the possibility that we could detect and monitor variability in the source, which - if associated with the compact nuclear core - could be measured with cadences of days, weeks or months.

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