

The orientation and kinematics of inner tidal tails around dwarf galaxies orbiting the Milky Way

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ABSTRACT

Using high-resolution collisionless N -body simulations, we study the properties of tidal tails formed in the immediate vicinity of a two-component dwarf galaxy evolving in a static potential of the Milky Way (MW). The stellar component of the dwarf is initially in the form of a disc and the galaxy is placed on an eccentric orbit motivated by cold dark matter based cosmological simulations. We measure the orientation, density and velocity distribution of the stars in the tails. Due to the geometry of the orbit, in the vicinity of the dwarf, where the tails are densest and therefore most likely to be detectable, they are typically oriented towards the MW and not along the orbit. We report on an interesting phenomenon of ‘tidal tail flipping’: on the way from the pericentre to the apocentre, the old tails following the orbit are dissolved and new ones pointing towards the MW are formed over a short time-scale. We also find a tight linear relation between the velocity of stars in the tidal tails and their distance from the dwarf. Using mock data sets, we demonstrate that if dwarf spheroidal (dSph) galaxies in the vicinity of the MW are tidally affected their kinematic samples are very likely contaminated by tidally stripped stars which tend to artificially inflate the measured velocity dispersion. The effect is stronger for dwarfs on their way from the pericentre to the apocentre due to the formation of new tidal tails after pericentre. Realistic mass estimates of dSph galaxies thus require removal of these stars from kinematic samples.

Key words: galaxies: dwarf – galaxies: fundamental parameters – galaxies: kinematics and dynamics – Local Group – dark matter.

1 INTRODUCTION

The population of dwarf galaxies in the Local Group offers a unique possibility to test current models of structure formation in the Universe based on Λ cold dark matter (Λ CDM) cosmology. Among those, the dwarf spheroidal (dSph) galaxies have attracted most attention, as they are believed to be strongly dark matter dominated. Many formation scenarios of these objects have been proposed, including gravitational processes such as tidal interactions with the host galaxy (Mayer et al. 2001; Kazantzidis et al. 2004; Kravtsov, Gnedin & Klypin 2004) and those inherent to the baryonic com-

ponent, such as cooling, star formation, feedback from supernovae and UV background radiation that can occur also for galaxies in isolation (Ricotti & Gnedin 2005; Mayer et al. 2007; Tassis, Kravtsov & Gnedin 2008; Sawala, Scannapieco & White 2009).

According to the tidal stirring scenario (Mayer et al. 2001) dSph galaxies of the Local Group formed via tidal interaction of low-surface-brightness discy dwarfs with the host galaxy such as Milky Way (MW). Inherent in this process is a significant mass loss which accompanies the morphological transformation. Matter stripped from the dwarf galaxy forms tidal tails which will eventually become completely unbound and form larger tidal extensions tracing approximately the original orbit of the dwarf in the MW halo. The dynamics of the tidal debris in the immediate vicinity of the dwarf turns out to be different from the behaviour of the debris at larger

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scales. In this paper, we concentrate on the properties of the inner tidal tails, within a few characteristic radii of the dwarf which are the most observable, given their high surface density. This debris has been lost recently and remains close to the dwarf and is thus most likely to contaminate the kinematic samples of dSph galaxies.

The presence of tidal tails around observed dSph galaxies has been detected in many cases. Martínez-Delgado et al. (2001) found tidal extensions in Ursa Minor, and Coleman et al. (2005) showed differences in surface brightness around Fornax depending on the direction of measurement. Tidally induced overdensities in the distribution of stars were also detected around Carina (Muñoz et al. 2006) and Leo I (Sohn et al. 2007). However, owing to their low surface brightness, tidal tails are still very difficult to detect by photometric techniques. Another possibility is to look for velocity gradients that should be present in kinematic data sets. Such features seem to be present in Leo I where the intrinsic rotation appears reversed further away from the centre of the dwarf (Łokas et al. 2008). Note however that the features usually interpreted as tidal could also originate from multiple stellar populations (Tolstoy et al. 2004; McConnachie, Peñarrubia & Navarro 2007) or accretion and merger events (Coleman et al. 2004; Battaglia et al. 2006).

It has long been debated whether the inferred large dark matter content of dSph galaxies can in fact be due to the tidal effects and models with no dark matter were constructed (e.g. Kroupa 1997). In our previous work, we showed (Klimentowski et al. 2007, 2009) that tidal stripping naturally coexists for a long time with a substantial bound stellar component embedded in a relatively massive dark matter halo. We have also demonstrated that stars originating from tidal tails can contaminate kinematic samples of dSph galaxies leading to significant overestimates of their velocity dispersions, especially at larger projected radii. Modelling of such contaminated velocity dispersion profiles results in biased inferences concerning the dark matter distribution and the anisotropy of stellar orbits, i.e. more extended dark matter haloes or more tangential orbits are obtained (see the discussion of the case of Fornax in Klimentowski et al. 2007; Łokas 2009).

The degree of this contamination depends however critically on the orientation of the tails with respect to the line of sight of the observer, which is approximately the direction towards the MW. A question thus arises if there is a correlation between their orientation and the orbit of the dwarf galaxy. If such a correlation exists, it would also help to study dSph orbits and serve as a complement to proper motions measurements which still have rather large errors (e.g. Dinescu et al. 2004; Piatek et al. 2007). Such studies were already made, for example, by Piatek & Pryor (1995) and Johnston, Choi & Guhathakurta (2002).

In this paper, we study the orientation of the tails and their kinematic properties using high-resolution N -body simulations of a two-component dwarf galaxy described in Klimentowski et al. (2007, 2009). Although the properties of the tails depend in general on a number of factors, such as the host potential (Piatek & Pryor 1995) or the mass of the satellite (Choi, Weinberg & Katz 2007), we believe that the orbit is the crucial factor. The potential of the MW is rather well determined and, as we will show, the tails behave similarly in spite of the fact that during the whole evolution the mass of the dwarf decreases by more than two orders of magnitude due to tidal stripping.

Although we consider only a single orbit, our choice is strongly motivated by studies of the statistics of subhalo orbit shapes in the context of Λ CDM cosmology for cluster-size (Ghigna et al. 1998) and Local Group size haloes (Diemand, Kuhlen & Madau 2007). In particular, Diemand et al. find in their Via Lactea simulations that

the distribution of pericentre to apocentre values r_p/r_a of subhaloes is strongly peaked at about 0.1 with a median of 0.17 with the range of 0.07–0.40 corresponding to the 68 per cent region. Our orbit, with $r_p/r_a = 0.2$, is thus very typical and the results should be valid for most dwarf galaxies. We rely on this result because the orbits of dwarf satellites are at present poorly constrained observationally.

The amount of tidally stripped matter is controlled by the orbit-averaged tidal force which depends on the size of the orbit and can be quantified by the orbital time (Mayer et al. 2001). The orbital time in our simulations, of 2 Gyr, is typical for MW satellites (Johnston, Sigurdsson & Hernquist 1999) and results in relative mass-loss rates of the order of 10–20 per cent per Gyr near apocentre (Klimentowski et al. 2009), again in agreement with estimates for nearby dwarfs by Johnston et al. (1999) who find values between a few up to more than 30 per cent per Gyr. Therefore, the density of tidal tails forming in our simulations, and the consequent amount of expected contamination, should be representative of many MW satellites.

This paper is organized as follows. The simulation details are summarized in the next section. In Section 3, we measure the orientation of the tidal tails with respect to the line of sight of an observer placed at the centre of the MW. In Section 4, we describe the densities and velocities of the stars in the tails. Section 5 discusses the actual contamination of the kinematic samples by unbound stars and its effect on the estimated velocity dispersion. The discussion follows in Section 6.

2 THE SIMULATIONS

The simulations used for the present study are described in detail in Klimentowski et al. (2007, 2009). Here, we provide a short summary of the most important parameters. The dwarf progenitor of total mass $M = 4.3 \times 10^9 M_\odot$ consists of a baryonic disc embedded in a dark matter halo. The initial mass of the disc is $1.5 \times 10^8 M_\odot$ (it is modelled by $N = 10^6$ particles of mass $149.5 M_\odot$) and its density drops exponentially with radius in the rotation plane (with the radial scale length $R_d = 1.3$ kpc), while its vertical structure is modelled by isothermal sheets (with the vertical scaleheight $z_d = 0.13$ kpc). The mass of the dark matter halo is $4.1 \times 10^9 M_\odot$ (it is modelled by $N = 4 \times 10^6$ particles of mass $1035.7 M_\odot$) and its density distribution follows the Navarro, Frenk & White (NFW) profile with virial mass $M_{\text{vir}} = 3.7 \times 10^9 M_\odot$ and concentration $c = 15$. The halo is exponentially truncated outside the virial radius $r_{\text{vir}} \simeq 40.2$ kpc to keep the total mass finite.

We performed three simulations with the disc initially positioned at the inclination of 0° , 45° and 90° to the orbital plane. Although the evolution is slightly different in each case, with stronger mass loss for lower inclinations (see section 4 of Klimentowski et al. 2009), the orientation does not strongly affect the properties of tidal tails. Since the results are similar in all cases, here we present only the intermediate, and therefore the most representative, case of 45° inclination.

The dark matter halo is initially much more extended than the disc, so the mass-to-light ratio is not constant with radius but increases strongly outside $r = 2$ kpc. In the final stage, since the dark halo is more heavily stripped, the mass-to-light ratio is almost constant and of the order of 10 solar units. Our dwarf galaxy is thus moderately dark matter dominated, so the results apply directly to objects such as Fornax or Leo I dSph galaxies, rather than more strongly dark matter dominated objects like Draco.

The dwarf galaxy evolves on an eccentric orbit with apocentre $r_a = 120$ kpc and pericentre-to-apocentre ratio of $r_p/r_a \approx 0.2$ around the host galaxy. The evolution is followed for 10 Gyr corresponding

to five orbital times. The host galaxy is modelled by a static gravitational potential assumed to have the present-day properties of the MW as described by mass model A1 of Klypin, Zhao & Somerville (2002). It consists of an NFW halo with the virial mass of $M_{\text{vir}} = 10^{12} M_{\odot}$ and concentration $c = 12$, a stellar disc with mass $M_{\text{D}} = 4 \times 10^{10} M_{\odot}$, the scalelength $R_{\text{d}} = 3.5$ kpc and the scaleheight $z_{\text{d}} = 0.35$ kpc, and a bulge of mass $M_{\text{b}} = 0.008 M_{\text{vir}}$ and scalelength $a_{\text{b}} = 0.2 R_{\text{d}}$.

The simulation was performed using the PKDGRAV N -body code (Stadel 2001). The gravitational softening length was 50 pc for stars and 100 pc for dark matter. We used 200 outputs of the simulation saved at equal snapshots of 0.05 Gyr.

3 THE ORIENTATION OF INNER TIDAL TAILS

The evolution of the dwarf galaxy in the potential of the host proceeds via a sequence of tidal shocks when the galaxy passes the pericentre. The pericentre passages are characterized by significant mass loss so that after 10 Gyr of evolution the galaxy mass decreases by more than two orders of magnitude. The mass loss is accompanied by the morphological transformation of the stellar component. Already at the first pericentre passage the disc transforms into an elongated bar and the prolate shape is preserved until the end, although the galaxy becomes more spherical with time. At all times, pronounced tidal tails can be identified around the dwarf. Here we focus on the innermost tidal formations, starting near the dwarf, where the stellar density distribution starts to flatten, up to 10 kpc from the centre of the dwarf. In the following, we will refer to this fraction of the tails as ‘inner tidal tails’.

There are always two tidal tails emanating from the two opposite sides of the galaxy. While the two tails are not always equilinear (they rarely intersect the centre of the galaxy), they are always almost parallel to each other so the direction of both tails can be represented by a single straight line. The alignment of the inner tidal tails in the simulation was calculated by fitting a straight line to the direction where the density of the tail reaches a maximum. The fitting was done separately for each of the two tails and the average angle was taken as the final measurement (the two values never differ by more than a few degrees). In the final output of the simulation, the density profile of the stars starts to flatten at about 2 kpc, signifying the transition to tidal tails. Thus, our chosen distance of 10 kpc corresponds to about 5 final radii of the dwarf. The stars in this region are still marginally bound (see below) but are no longer good tracers of the potential of the dwarf. Except for the moments of abrupt changes in the orientation of the tails, the estimated alignment extends much further than 10 kpc.

Fig. 1 plots the orbit of the simulated dwarf galaxy during the course of its evolution (solid line) with dotted lines showing the direction of the tidal tails at a given position on the orbit. No dotted lines are plotted for the initial stage of the simulation when there were no clear tidal tails formed yet. According to Fig. 1, tidal tails are parallel to the orbit only during very short periods of time around the pericentres. In the outer parts of the orbit, near the apocentre (where the dwarf galaxy spends most of its time) tidal tails always point almost radially towards the host galaxy. The upper panel of Fig. 2 presents the same results in a more quantitative way by plotting the angle between the tidal tails and the direction to the host galaxy. Tidal tails tend to be oriented radially: their direction is similar to the direction of the dwarf’s position vector for most of the time. Only for a short time near pericentres they are roughly parallel to the orbit. This result is illustrated further in Fig. 3 where

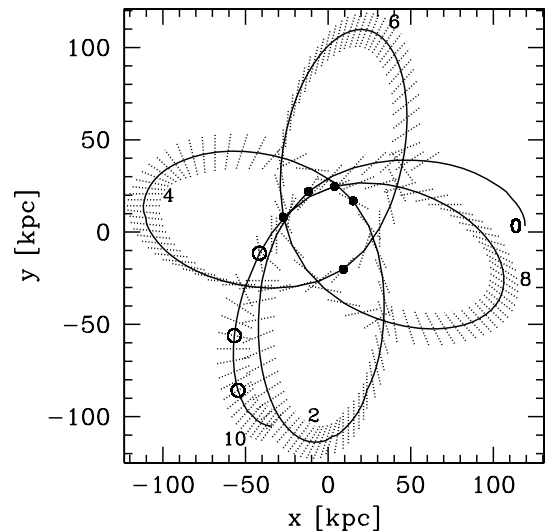


Figure 1. The solid line shows the orbit of the simulated dwarf galaxy projected on the plane of the MW disc. The simulation starts on the right-hand side of the figure. Numbers marking the apocentres indicate the time from the start of the simulation in Gyr. Filled circles mark pericentres of the orbit. Open circles indicate the positions corresponding to the snapshots presented in Fig. 4. The dotted lines overlotted on the orbit show the direction of the tidal tails. In the initial part of the orbit that lacks dotted lines, no well-defined tidal tails were formed yet.

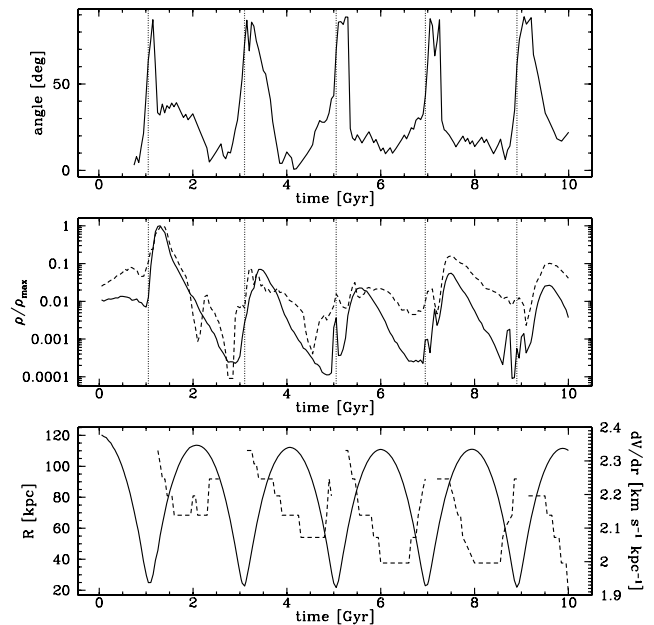


Figure 2. Properties of the tidal tails. The upper panel shows the angle between the tails and the direction towards the centre of the MW as a function of time. The middle panel plots the density of the tidal tails. The solid line corresponds to the mean density of all stars at the distance of 10 kpc from the dwarf (calculated in a ring of 1 kpc in size), while the dashed line shows the same density but measured on the axis of the tails (calculated in two boxes with 1 kpc on a side placed at 10 kpc from the centre of the dwarf in opposite directions). Densities are plotted relative to their respective maximum values. Vertical dotted lines indicate pericentre passages. The lower panel shows the values of dV/dr , the slope of the relation between the velocity of stars in the tidal tails and their distance from the dwarf (dashed line) fitted to velocity diagrams similar to Fig. 5 along with the distance of the dwarf from the host galaxy (solid line) as a function of time.

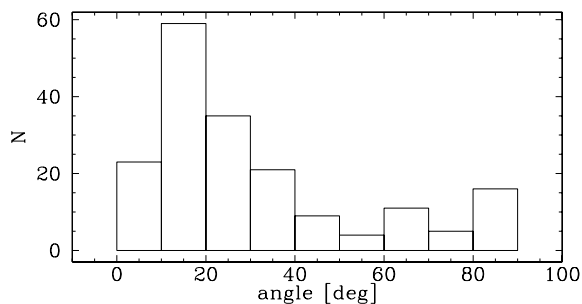


Figure 3. The distribution of the angle between the direction to the MW centre and the nearest tidal tail of the dwarf galaxy. The histogram was constructed from 185 simulation outputs (excluding only the initial 15 outputs where the tidal tails are not yet fully formed).

we plot the distribution of this angle which shows a strong peak for low values of 0° – 30° .

Fig. 1 and the upper panel of Fig. 2 demonstrate that while the transition from the radial to the orbital (i.e. parallel to the orbit) orientation of the tidal tails happens rather smoothly when the dwarf approaches pericentre, the transition from the orbital to the radial orientation after a pericentre passage is rather abrupt. This is very well visible after the third, fourth and fifth pericentre passages and happens roughly halfway between the pericentre and the apocentre over a rather short time-scale. Fig. 4 presents three snapshots from the simulation showing this remarkable transition starting at 9.1 Gyr after the beginning of the simulation, when the dwarf has almost reached its final form. The dwarf has just passed the pericentre and its tidal tails are perpendicular to the radial direction (towards the host galaxy). The tidal force acts perpendicular to the tails and dissolves them. This process is accompanied by the stripping of a new material from the dwarf galaxy and formation of new, much denser and radially aligned tidal tails. We propose to call this phenomenon the ‘tidal tail flipping’.

The orientation of the tails results from the interplay between the change of orbital velocity and the direction of tidal force. For circular orbits, the configuration does not change in time: the velocity of the dwarf is always perpendicular to the direction to the MW and the tidal force acts always perpendicular to the velocity. The orientation of the tails will therefore be the same in all parts of the orbit, but it will depend on the host potential and the mass of the dwarf. In the immediate vicinity of the dwarf, the tails consist of stars recently ejected from the dwarf so they point along the tidal force, i.e. along the direction to the MW. As the ejected stars become unbound, they

will travel on their own orbits in the MW potential: those that were ejected towards the MW will travel faster than the dwarf and form a leading tail, while those that were ejected away from the MW will travel slower and form a trailing tail.

If the orbit is eccentric, the situation becomes more complicated because the tidal force still acts towards the MW but the velocity of the dwarf changes. At any moment the picture is similar to the case of circular orbit, but the orientation of the tails will change in time, so it is better to speak about an inside and outside tail (with respect to the dwarf’s orbit). For example, when approaching the apocentre the unbound stars in the inside tail will reach their apocentres sooner than the dwarf (they are on tighter orbits in the MW potential) and will slow down, while those in the outside tail will not yet reach their apocentres and will move faster. The net effect we see is that near apocentres the tails are oriented along the direction to the MW. On the other hand, when the dwarf is on the way to its pericentre, the stars in the inside tail speed up with respect to the dwarf (those in the outside tail slow down) and the tails become elongated along the orbit. After the pericentre, the situation is not exactly symmetrical because of the impulsive mass loss at that time. This new material is ejected mainly along the direction to the MW, and the orbits of these newly ejected stars behave as always when approaching the apocentre (the radial alignment of the tails is preferred). The two factors combine so that the net effect is the formation of strong tails along the direction to the MW that we have referred to as the ‘tidal tail flipping’.

4 THE KINEMATICS OF INNER TIDAL TAILS

The middle panel of Fig. 2 shows the relative density of stars in the tidal tails at the distance of 10 kpc from the dwarf galaxy (dashed line) compared to the density everywhere around the galaxy (measured in a ring placed in the orbital plane, solid line). These measurements illustrate the mechanism for tail formation. Most matter is stripped during the pericentre passages but tidal tails enhance their density a little later along the orbit reaching the maximum density typically about 0.5 Gyr after pericentre. This happens because some time is required for stars to travel several kpc away from the galaxy and form the tails. After reaching the maximum, the density drops exponentially until the next pericentre passage, after which the previously formed tails are dissolved and new tails are formed, as described in the previous section.

This picture suggests that it should be much easier to detect tidal tails for dwarf galaxies shortly (few hundred Myr) after pericentre,

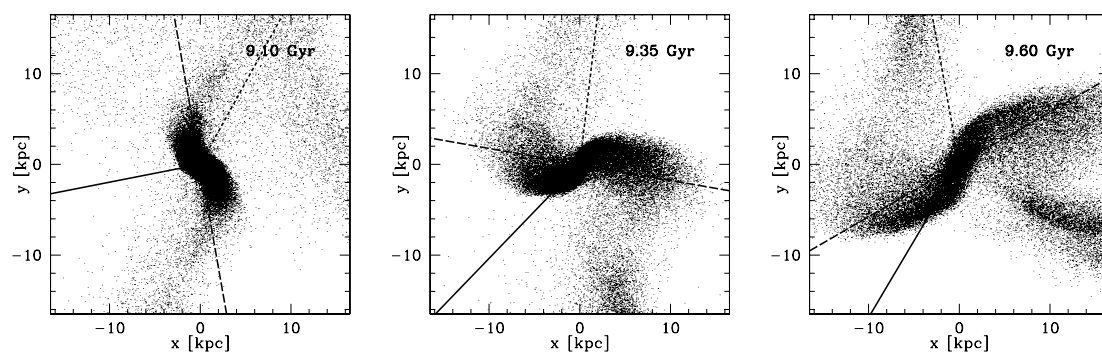


Figure 4. Tidal tail flipping. The three panels present three snapshots from the simulation at 9.1, 9.35 and 9.6 Gyr from the start, corresponding to the positions on the orbit marked with open circles in Fig. 1. Dots show positions of 20 per cent of stellar particles projected on to the orbital plane. The solid line indicates the direction to the host galaxy, the short-dashed one is parallel to the velocity vector of the dwarf and the long-dashed one shows the direction of the inner tidal tails. Old tidal tails oriented almost along the orbit decay and new ones pointing almost radially towards the host galaxy are formed.

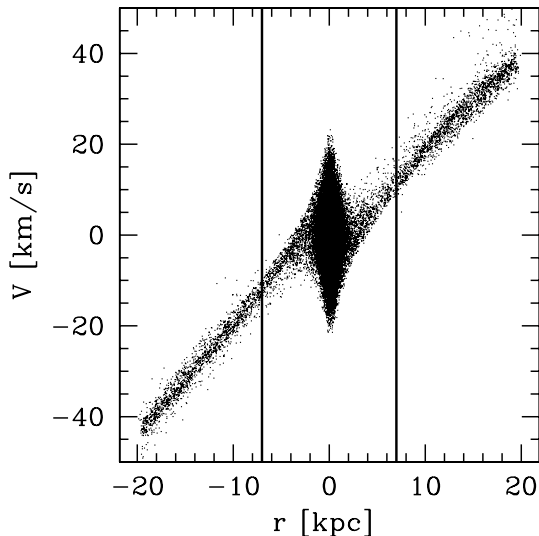


Figure 5. Velocities of stellar particles of the simulated galaxy at $t = 8.5$ Gyr projected on to the axis parallel to the tidal tails (and intersecting the centre of the dwarf galaxy). The coordinate r measures the distance from the centre of the dwarf projected on to this axis. Vertical solid lines show the limits within which most stars are bound. Only 15 per cent of the stars were plotted for clarity.

i.e. when they have positive radial velocities with respect to the host. The parts of the diagram shown in the middle panel of Fig. 2 where the solid line is higher than the dashed indicate that the tidal tails are then highly diffuse. There are always a significant number of stars distributed uniformly around the galaxy but prominent tidal tails are not always present as a dwarf satellite evolves in the primary’s potential.

Fig. 5 plots velocities of the stellar particles inside the dwarf galaxy and its tidal tails projected on an axis parallel to the tidal tails as a function of the distance from the centre of the dwarf measured along the same axis. The dependence of velocity on distance is a well-known feature of tidal formations commonly referred to as the ‘velocity gradient’ (e.g. Piatek & Pryor 1995). Interestingly, we find that there is a tight linear relation between the radial velocity of a star and its distance from the galaxy. It turns out that this relation is valid during most of the time except for the pericentre passages. Only the slope of the $V(r)$ relation varies with time.

The stars enclosed between the vertical solid lines in Fig. 5 nearly all have velocities lower than the escape velocity, thus they are still bound to the galaxy and are expected to fall back, while stars outside will eventually feed the tidal streams. The lower panel of Fig. 2 shows with dashed lines the values of dV/dr (the slope of the relation) along with the distance of the dwarf from the host galaxy (solid line) as a function of time. Clearly, the slope of the relation is anticorrelated with the distance from the host galaxy. After the pericentre passage, when the tails are created, the $V(r)$ relation is steeper and it flattens with time. After the apocentre the relation becomes steeper again. The numerical values plotted in the lower panel of Fig. 2 were obtained by fitting a linear function to the velocity diagrams similar to the one presented in Fig. 5 for every simulation output. The fitting was done for stars within the distance range $5 < |r| < 20$ kpc from the centre of the dwarf.

It is important to emphasize that the presence of a star in the tidal tails does not imply that it is unbound to the galaxy. Some of the stars from the tidal tails are actually falling back on to the dwarf. The bound region marked by the vertical solid lines in Fig. 5 varies with

time. When the dwarf travels from pericentre to apocentre unbound stars leave its vicinity quickly, while the fastest bound stars reach their turnaround points shortly after the apocentre. This extended region, dominated by bound stars, can reach up to 10 kpc from the galaxy.

5 THE CONTAMINATION OF KINEMATIC SAMPLES

In this section, we address the question of how the kinematic samples and measured velocity dispersions are affected by the presence and properties of tidal tails in the immediate vicinity of a dwarf galaxy. The problem has already been discussed in detail by Klimentowski et al. (2007) using a single, final output of a similar simulation. Here we consider a similar problem but taking into account the actual variation of the orientation and density of the tails as the dwarf travels on its orbit around the host galaxy. We restrict the analysis to the last full orbit, i.e. the time between the two last apocentres, between 8 and 10 Gyr from the start of the simulation. This time is representative so that all configurations of the tails are covered and, on the other hand, the dwarf is already evolved enough so that it can actually be described as a dSph galaxy (see Klimentowski et al. 2009; Łokas et al. 2009 for details).

The kinematic samples are constructed in a similar way as in real observations. We place an observer in the centre of the MW and project the velocities of the stars in the dwarf along the line of sight and their positions on the surface of the sky. Three examples of velocity diagrams constructed in this way are shown in Fig. 6 for the outputs at 8.5, 9.1 and 10 Gyr from the start of the simulation. The diagrams show the line-of-sight velocities of the stars versus their projected radii. To select the stars, we have applied a rather conservative cut-off in velocity $|V_{\text{los}}| < 30 \text{ km s}^{-1}$ with respect to the dwarf’s mean and the projected radius $R < 2.5$ kpc. The stars bound to the dwarf are plotted with filled circles, those unbound with open circles.

At 8.5 and 10 Gyr (the left- and right-hand panels of Fig. 6), where the dwarf is close to apocentres, the velocity diagrams are regular, with a characteristic triangular shape typical of relaxed objects. At 9.1 Gyr (middle panel), the dwarf has just passed its pericentre and is strongly perturbed. The forming tidal tails are visible at larger R as two separate branches. Note that although the stars clearly belong to the tails, very few of them are actually already unbound, but they are in the process of being stripped and cannot be considered as reliable tracers of the dwarf potential. The unusual shape of the velocity diagram in this case could be used as a warning against using such samples for dynamical modelling.

For further analysis, we restricted the sample to the projected radii $R < 2$ kpc and introduced a cut-off in the line-of-sight velocity $|V_{\text{los}}| < 3\sigma_0$ with respect to the dwarf’s mean, where σ_0 is the central velocity dispersion measured in each simulation output for stars within $R < 0.2$ kpc where the contamination is very low. This is the standard procedure used in selecting kinematic samples for dynamical analysis, based on the assumption that the velocity distribution is approximately Gaussian. We adopted a variable velocity cut-off because the bound mass of the dwarf changes between 8 and 10 Gyr by more than a factor of 2, from 8×10^7 to $3 \times 10^7 M_{\odot}$ due to tidal stripping (see Klimentowski et al. 2009). The radius $R = 2$ kpc corresponds to the size of the dwarf at the final stage, i.e. at larger radii the tidal tails start to dominate.

For kinematic samples constructed in this way, we measured the fraction of unbound stars in the total sample, the line-of-sight velocity dispersion of bound and all stars and the ratio of the two.

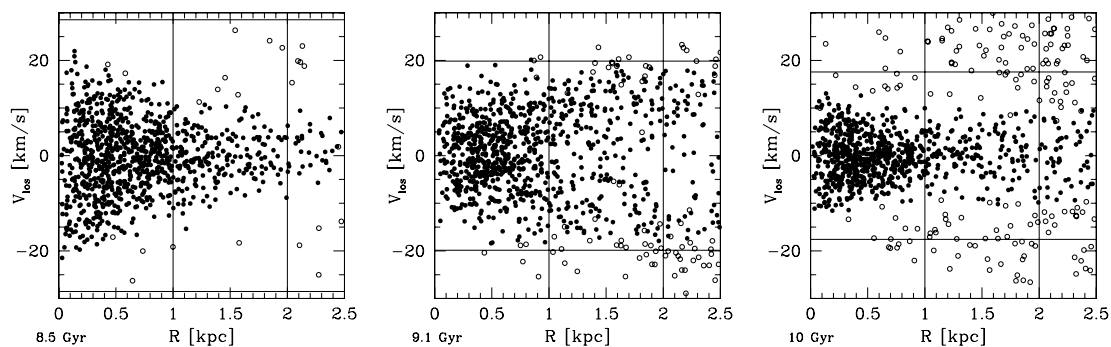


Figure 6. Velocity diagrams of the stars at 8.5, 9.1 and 10 Gyr (from the left- to the right-hand panels). The plots show the line-of-sight velocities of a thousand randomly selected stars with respect to the dwarf mean velocity as a function of their projected distance from the centre of the dwarf. Filled circles indicate bound stars, open circles the unbound ones. Horizontal lines show the velocity cut-off $|V_{\text{los}}| < 3\sigma_0$ and the vertical lines the boundaries in projected radius defining the kinematic subsamples with $R < 1$ kpc and $1 < R < 2$ kpc.

Velocity dispersions were calculated using the standard unbiased estimator (see e.g. Łokas, Mamon & Prada 2005). We made separate measurements for the whole sample with $R < 2$ kpc, the stars with radii $R < 1$ kpc (inner sample) and $1 < R < 2$ kpc (outer sample). The results are illustrated in the four panels of Fig. 7 with the solid line corresponding to the whole sample, the dashed one to the inner sample and the dotted one to the outer sample.

We immediately see that the contamination is rather different before and after the pericentre passage. After the pericentre the fraction of unbound stars is much higher (it reaches 26 per cent for the outer sample) and has two maxima, the first one due to the formation of new strong tidal tails and the second due to the tails becoming more radially oriented. The velocity dispersions are obviously most affected at the pericentre when the dwarf is most strongly perturbed, even if its tidal tails are not oriented along the line of sight. As already mentioned, the stars which are being ejected at this moment, although formally still bound to the dwarf cannot be reliably used for dynamical modelling. After the pericentre, the presence of the tails can increase the central velocity dispersion by up to 20 per cent, the total velocity dispersion by up to 40 per cent, but the dispersion of the outer sample can be inflated by almost a factor of 2.

An obvious remedy to this effect would be to use for dynamical modelling only the inner sample where the contamination is relatively low. Note, however, that with growing kinematic samples presently available for dSph galaxies restricting the analysis to the innermost part of the dwarf would mean to lose a lot of information. It is now common in such analyses to use velocity dispersion profiles rather than single dispersion values since only the profiles allow us to constrain the actual distribution of mass in the dwarfs rather than just the total mass. Without this, addressing such issues as the shape of dark matter profile or the cusp/core problem would be impossible. In addition, as demonstrated by Klimentowski et al. (2007) such contamination can be effectively removed by common procedures for interloper rejection.

6 DISCUSSION

We studied the properties of tidal tails in the immediate vicinity of dwarf galaxies orbiting in an MW potential. We find that for most of the time tidal tails point almost radially towards the host galaxy. This behaviour is in agreement with Montuori et al. (2007) who found the same effect in their N -body simulations of globular clusters. Therefore, the orientation of tidal tails in the immediate

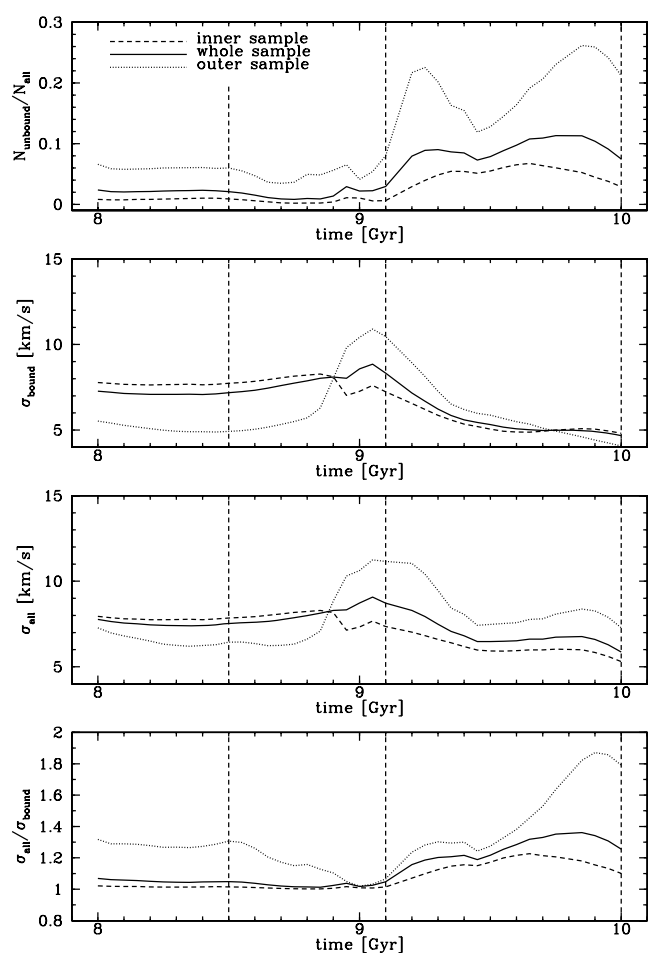


Figure 7. The effect of tidal tails on the measured velocity dispersion of the dwarf as a function of time over the last orbit. All panels refer to the kinematic sample obtained by selecting stars within a given range of projected radii R and introducing the velocity cut-off $|V_{\text{los}}| < 3\sigma_0$. In each panel, the solid line corresponds to all stars within $R < 2$ kpc, the dashed line to the inner sample with $R < 1$ kpc and the dotted line to the outer sample with $1 < R < 2$ kpc. The upper panel shows the fraction of unbound stars in each sample. The second and third panels plot the velocity dispersion of the bound and all stars, respectively, and the fourth panel shows the ratio of the two. Vertical dashed lines indicate snapshots for which the velocity diagrams in Fig. 6 are shown.

vicinity of the galaxy is not directly related to the direction of the orbital motion. Only unbound stars lost much earlier and forming large-scale extensions further out from the bound component of the dwarf tend to follow the orbit.

In contrast, Combes, Leon & Meylan (1999) and Dehnen et al. (2004) find that the tidal tails in their globular cluster simulations follow the orbit. The difference is mainly due to the fact that they study tails out to much larger distances than we did here. Some differences are also expected because of the different orbits which they assumed to be less eccentric than in our case. Johnston et al. (2002) have shown that indeed for almost circular orbits tidal tails are pointed radially towards the host galaxy only very close to the cluster. Other differences come from the fact that globular cluster simulations do not involve dark matter and all simulations performed to date started with a spherical object while our dwarf initially possessed a stellar disc.

The radial alignment of tidal tails may at least partially explain the difficulty of detecting them by photometric observations. Since we are looking at the dwarfs from the inside of the MW, their tidal tails are most probably oriented along the line of sight and they are likely to be confused with a much brighter dwarf galaxy itself. In the rare cases when the line of sight is perpendicular to the tidal tails, the tails will generate an excess of star counts at a few core radii from the centre, which will show up as a flattening of the outer part of the star counts profile (Klimentowski et al. 2007; Peñarrubia et al. 2009). Such a flattening might have been observed in some dSphs but not in all of them (Muñoz et al. 2006; Muñoz, Majewski & Johnston 2008).

The most important consequence of the radial alignment of tails is the fact that the tails are aligned with the line of sight of the observer who is placed inside the host galaxy. This means that even far away from pericentre, when the dwarf appears unperturbed and relaxed, the kinematic samples of stars will be contaminated by unbound stars from the tails. This contamination should be highest for dwarfs receding from the MW right after the tidal tail flipping. Given the tight and steep relation between the distance of stars in the tails and their velocity, this means that even the relatively near tidally stripped stars must artificially inflate the measured velocity dispersion, especially in the outer regions of the dwarfs. It is therefore essential to remove these unbound stars in order to obtain reliable mass estimates for dwarf galaxies.

Klimentowski et al. (2007) showed that this can be very effectively done using a procedure proposed by den Hartog & Katgert (1996). This procedure has been recently applied by Łokas (2009) to new, large kinematic samples for the Fornax, Carina, Sculptor and Sextans dwarfs published by Walker, Mateo & Olszewski (2009). It has been shown there that the contamination is indeed significant, and once it is removed the velocity moments are well reproduced by solutions of the Jeans equations for models where mass follows light, as predicted by the tidal stirring scenario (Klimentowski et al. 2007, 2009; Mayer et al. 2007; Łokas et al. 2008, 2009).

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