

2-2014

# A Compartmentalized Mathematical Model of the $\beta_1$ -Adrenergic Signaling System in Mouse Ventricular Myocytes

Vladimir E. Bondarenko

*Georgia State University*, [vbondarenko@gsu.edu](mailto:vbondarenko@gsu.edu)

Follow this and additional works at: [https://scholarworks.gsu.edu/math\\_facpub](https://scholarworks.gsu.edu/math_facpub)



Part of the [Mathematics Commons](#)

---

## Recommended Citation

Bondarenko VE (2014) A Compartmentalized Mathematical Model of the  $\beta_1$ -Adrenergic Signaling System in Mouse Ventricular Myocytes. PLoS ONE 9(2): e89113. doi:<http://dx.doi.org/10.1371/journal.pone.0089113>

This Article is brought to you for free and open access by the Department of Mathematics and Statistics at ScholarWorks @ Georgia State University. It has been accepted for inclusion in Mathematics and Statistics Faculty Publications by an authorized administrator of ScholarWorks @ Georgia State University. For more information, please contact [scholarworks@gsu.edu](mailto:scholarworks@gsu.edu).

# A Compartmentalized Mathematical Model of the $\beta_1$ -Adrenergic Signaling System in Mouse Ventricular Myocytes

Vladimir E. Bondarenko\*

Department of Mathematics and Statistics and Neuroscience Institute, Georgia State University, Atlanta, Georgia, United States of America

## Abstract

The  $\beta_1$ -adrenergic signaling system plays an important role in the functioning of cardiac cells. Experimental data shows that the activation of this system produces inotropy, lusitropy, and chronotropy in the heart, such as increased magnitude and relaxation rates of  $[Ca^{2+}]_i$  transients and contraction force, and increased heart rhythm. However, excessive stimulation of  $\beta_1$ -adrenergic receptors leads to heart dysfunction and heart failure. In this paper, a comprehensive, experimentally based mathematical model of the  $\beta_1$ -adrenergic signaling system for mouse ventricular myocytes is developed, which includes major subcellular functional compartments (caveolae, extracaveolae, and cytosol). The model describes biochemical reactions that occur during stimulation of  $\beta_1$ -adrenoceptors, changes in ionic currents, and modifications of  $Ca^{2+}$  handling system. Simulations describe the dynamics of major signaling molecules, such as cyclic AMP and protein kinase A, in different subcellular compartments; the effects of inhibition of phosphodiesterases on cAMP production; kinetics and magnitudes of phosphorylation of ion channels, transporters, and  $Ca^{2+}$  handling proteins; modifications of action potential shape and duration; magnitudes and relaxation rates of  $[Ca^{2+}]_i$  transients; changes in intracellular and transmembrane  $Ca^{2+}$  fluxes; and  $[Na^+]_i$  fluxes and dynamics. The model elucidates complex interactions of ionic currents upon activation of  $\beta_1$ -adrenoceptors at different stimulation frequencies, which ultimately lead to a relatively modest increase in action potential duration and significant increase in  $[Ca^{2+}]_i$  transients. In particular, the model includes two subpopulations of the L-type  $Ca^{2+}$  channels, in caveolae and extracaveolae compartments, and their effects on the action potential and  $[Ca^{2+}]_i$  transients are investigated. The presented model can be used by researchers for the interpretation of experimental data and for the developments of mathematical models for other species or for pathological conditions.

**Citation:** Bondarenko VE (2014) A Compartmentalized Mathematical Model of the  $\beta_1$ -Adrenergic Signaling System in Mouse Ventricular Myocytes. PLoS ONE 9(2): e89113. doi:10.1371/journal.pone.0089113

**Editor:** Xun Ai, Loyola University Chicago, United States of America

**Received:** September 29, 2013; **Accepted:** January 14, 2014; **Published:** February 21, 2014

**Copyright:** © 2014 Vladimir E. Bondarenko. This is an open-access article distributed under the terms of the Creative Commons Attribution License, which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.

**Funding:** This work was supported by the American Heart Association (<http://www.heart.org/HEARTORG/>) (10GRNT4720012), Georgia State University (<http://www.gsu.edu>) Seed Grant from Brain and Behavior Program, and Research Initiation Grant to V. E. Bondarenko. The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

**Competing Interests:** Vladimir Bondarenko is an Academic Editor of PLOS ONE. This does not alter his adherence to all the PLOS ONE policies on sharing data and materials.

\* E-mail: vbondarenko@gsu.edu

## Introduction

Cardiac cells belong to a wide class of excitable cells which include electrical activity,  $Ca^{2+}$  dynamics, and protein signaling networks. While early experimental studies of cardiac cells are predominantly devoted to their electrical activity, and later to  $Ca^{2+}$  dynamics, more recent studies involve investigations of protein signaling systems, which modulate both action potentials and intracellular  $Ca^{2+}$  transients [1,2]. On the tissue and whole heart levels, the activation of such signaling systems either promotes or suppresses pro-arrhythmic behavior. In addition, in diseased hearts, protein signaling networks become modified and do not properly regulate the electrical activity or  $Ca^{2+}$  handling system [3]. As a result, the studies of major signaling protein networks in cardiac cells identified new potential therapeutic targets for treatment of heart diseases; some of the targets include signaling proteins involved in  $\beta_1$ -adrenergic signaling system [4,5,6,7].

Mathematical modeling of protein signaling networks is a supplementary tool for understanding their functions in the heart. Recently, particular attention has been paid to the development of

comprehensive models for  $\beta_1$ -adrenergic system in ventricular myocytes of different species [8,9,10,11,12]. The first model developed by Saucerman et al. [10] for rat ventricular myocytes set high standards for simulation of the  $\beta_1$ -adrenergic signaling system. The model included biochemical and electrophysiological parts with two major protein kinase A targets, phospholamban and the L-type  $Ca^{2+}$  channel, and consisted of one cytosolic compartment (single-compartment model). Later, a similar model was developed for rabbit ventricular myocytes and included several new PKA targets: ryanodine receptors, troponin I, and slow delayed rectifier  $K^+$  current,  $I_{Ks}$  [11]. The model was further extended to simulate the effects of the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes, predominantly on  $Ca^{2+}$  dynamics [12]. Finally, a model of  $\beta_1$ -adrenergic signaling system in guinea pig ventricular myocytes [9] was developed based on the model of Saucerman et al. [10], which is devoted to the analysis of the changes in action potential, intracellular  $[Ca^{2+}]_i$  transients, and ionic fluxes upon stimulation of  $\beta_1$ -adrenoceptors with agonist isoproterenol.

Simultaneously, multi-compartmental models of protein signaling networks, including the  $\beta_1$ -adrenergic signaling system, were developed [8,13,14]. The compartmentalized models of Iancu et al. [13,14] included only the biochemical part of  $\beta_1$ -adrenergic and  $M_2$ -muscarinic signaling systems and described the dynamics of cAMP and PKA in different subcellular compartments (caveolae, extracaveolae, and cytosol). The only compartmentalized model of cardiac protein signaling network, which includes both biochemical and electrophysiological parts,  $\beta_1$ - and  $\beta_2$ -adrenergic and CaMKII-mediated signaling systems, was developed recently for canine ventricular myocytes by Heijman et al. [8]. The model was extensively verified by experimental data and reproduced major features of stimulation of the three signaling systems.

Compartmentalization of the signaling systems in cardiac cells is an important property. This property allows for regulation of multiple cellular functions, such as electrical activity,  $Ca^{2+}$  dynamics, and cellular contraction (for examples see reviews [1,15,16,17,18]). The experimental data demonstrates differential localization of the components of the  $Ca^{2+}$ -mediated,  $\alpha$ - and  $\beta$ -adrenergic signaling systems [19,20,21,22]. In cardiac myocytes,  $\beta_1$ -adrenergic receptors are mostly localized in membrane compartments that lack caveolin-3, while  $\beta_2$ -adrenergic receptors are mostly found in caveolin-3-rich domains [20]. Investigations of the physiological role of the  $\beta$ -receptors have shown their differing effects in the development of disease states: excessive activation of  $\beta_1$ -adrenergic signaling led to cardiac hypertrophy and heart failure [23], while moderately increased stimulation of  $\beta_2$ -adrenergic signaling was cardioprotective [24]. In addition,  $\beta_1$ - and  $\beta_2$ -adrenergic receptors modulate differently cardiac ionic currents and contraction proteins, which are also localized in different cellular compartments [15,16]. In the  $\beta_1$ -adrenergic signaling system alone, which is the major topic of this paper, multiple signaling molecules are also distributed among the major cellular compartments related to caveolin-3, non-caveolae cellular membrane, or cytosol, and these molecules are differentially modulated upon activation of  $\beta_1$ -receptors. In particular, the recent discovery of the two subpopulations of the L-type  $Ca^{2+}$  channels, the major players in cardiac excitation-contraction coupling, which are localized in caveolin-3-rich and non-caveolae compartments and play different physiological roles, requires more comprehensive, compartmentalized models of cardiac cells [22].

In this paper, we developed a new compartmentalized model for the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes. The model is based on our previously published models for action potential and  $Ca^{2+}$  dynamics in mouse ventricular myocytes [25,26]. The new model includes both biochemical and electrophysiological parts, as well as compartmentalization of the  $\beta_1$ -adrenergic signaling system, which includes three major compartments: caveolae, extracaveolae, and cytosol. Both biochemical and electrophysiological parts are verified by extensive experimental data, primarily obtained from the rodent cardiac cells. Activation of the major proteins in the signaling system, such as adenylyl cyclases and phosphodiesterases, is compared directly to the data from the mouse ventricular myocytes in absolute magnitudes. The model successfully reproduced existing experimental data on cAMP dynamics, activation of adenylyl cyclases and phosphodiesterases, protein kinase A and phosphorylation of its targets, and the effects of phosphodiesterases inhibition on cAMP transients. Simulations also reproduced data obtained from voltage-clamp protocols for major repolarization currents of mouse ventricular myocytes. The model is able to simulate action potential shape and duration upon stimulation of  $\beta_1$ -adrenergic receptors ( $\beta_1$ -ARs). The model elucidated the mechanism of

relatively moderate AP prolongation, significant increase in intracellular  $[Ca^{2+}]_i$  transients, modification of the intracellular and transmembrane  $Ca^{2+}$  fluxes, and  $[Na^+]_i$  fluxes and dynamics. The model includes two pools of the L-type  $Ca^{2+}$  channels, one in the caveolae and the other in the extracaveolae compartments. The simulations demonstrated their different modulations upon stimulation of  $\beta_1$ -ARs and their different effects on the action potentials and  $[Ca^{2+}]_i$  transients. The model simulated frequency dependences of  $[Ca^{2+}]_i$  transient decays for control conditions and after stimulation of  $\beta_1$ -ARs, and made testable predictions for the frequency dependences of  $[Ca^{2+}]_i$  transient amplitudes, AP amplitudes and durations. The simulation results are compared to the results obtained from other models of  $\beta_1$ -adrenergic signaling system in other species, and the model limitations are discussed.

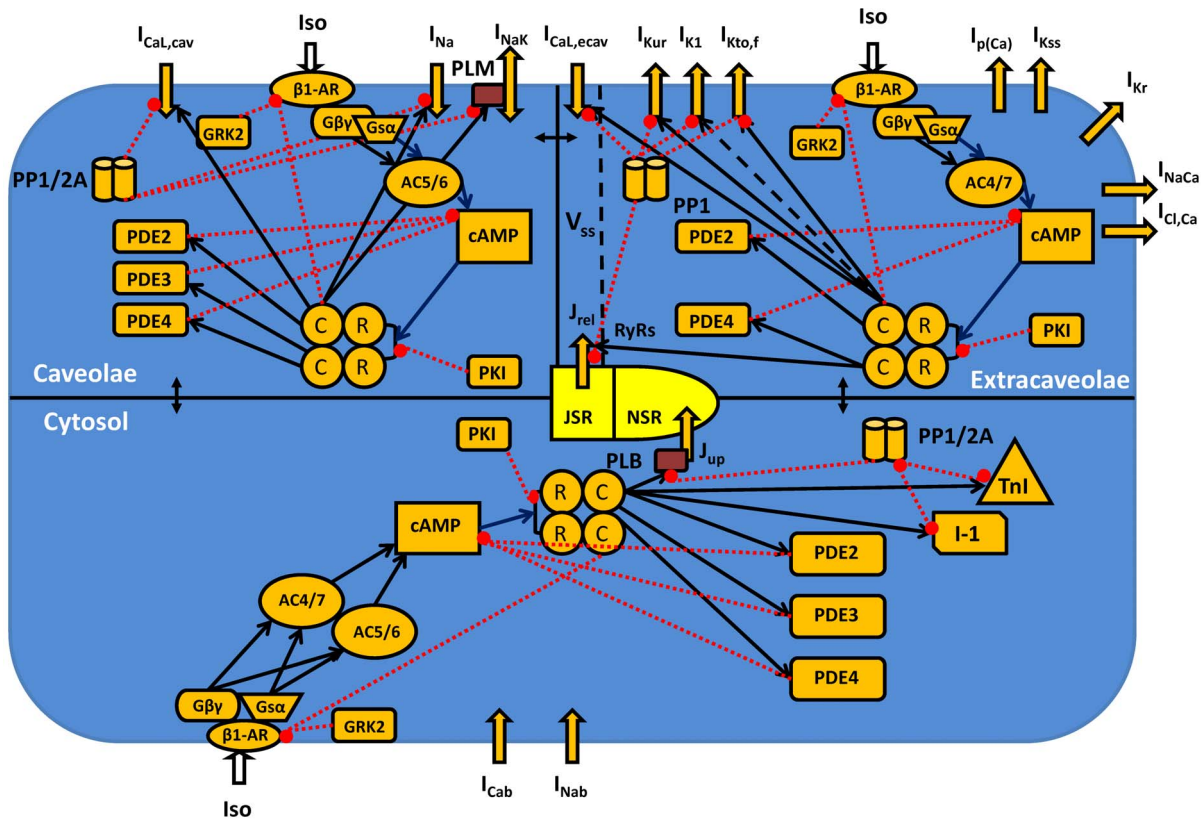
## Methods

A mathematical model for the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes is a natural extension of the previously published model for action potential and  $Ca^{2+}$  dynamics in mouse ventricular myocytes [25], with model improvements from [26] (Fig. 1). We incorporated a  $\beta_1$ -adrenergic signaling pathway in our model of electrical activity and  $Ca^{2+}$  handling with modifications [25,26] (see Appendix S1).

Our model cell consists of several compartments (Fig. 1; Appendix S1). For the  $\beta_1$ -adrenergic signaling system we consider three major *functional* compartments: caveolae (cav), extracaveolae (ecav), and cytosol (cyt) [8,13]. The caveolae compartment is a submembrane compartment associated with the protein caveolin-3. The extracaveolae compartment is also a submembrane compartment associated with cholesterol-rich lipid rafts, but it does not include caveolin-3. Both caveolae and extracaveolae compartments together represent the particulate fraction. The cytosolic compartment (the soluble fraction) represents the rest of the cell volume, excluding mitochondria. As the dynamics of  $Ca^{2+}$  concentration does not directly depend on the  $\beta_1$ -adrenergic signaling system, we use the same compartmentalization of  $Ca^{2+}$  handling as in Bondarenko et al. [25]. The subspace volume ( $V_{ss}$ ) of the  $Ca^{2+}$  handling system is completely located in the extracaveolae compartment of the  $\beta_1$ -adrenergic signaling system.

Total protein concentrations and their activities are normalized to the cell volume as in [8]. In most cases, we used Table 9 from [27] to convert protein concentrations from pmol/mg cell protein to the concentrations in  $\mu M$ . The localization of different signaling proteins and protein kinase A substrates in subcellular compartments can be found in Fig. 1 and Appendix S1 and will be described below in the corresponding chapters. The experimental data in the Methods chapter are used for constraining the model; the experimental data in the Results chapter are used for testing the developed model. The latter experimental data were not used for constraining the model.

In all compartments, the  $\beta_1$ -adrenergic signaling system is activated by agonist (isoproterenol) (Fig. 1). Stimulation of  $\beta_1$ -ARs leads to activation of the stimulatory G protein,  $G_s$ , which dissociates into  $G_{s\alpha}$  and  $G_{s\beta\gamma}$  subunits. Both subunits activate adenylyl cyclases (AC5/6 or AC4/7, depending on the cellular compartment), which produce cyclic AMP. cAMP is degraded by phosphodiesterases, three isoforms of which, PDE2, PDE3, and PDE4, are included in our model. Balanced activities of ACs and PDEs establish steady-state levels of cAMP in different compartments. cAMP further activates protein kinase A holoenzyme, which consists of two regulatory and two catalytic subunits. Binding four cAMP molecules to PKA holoenzyme causes



**Figure 1. Schematic representation of the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes.** Transmembrane currents are the fast  $\text{Na}^+$  current ( $I_{\text{Na}}$ ), the two components of the L-type  $\text{Ca}^{2+}$  current in caveolae and extracaveolae compartments ( $I_{\text{CaL,cav}}$  and  $I_{\text{CaL,ecav}}$  respectively), the sarcolemmal  $\text{Ca}^{2+}$  pump ( $I_{\text{p(Ca)}}$ ), the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger ( $I_{\text{NaCa}}$ ), the rapidly recovering transient outward  $\text{K}^+$  current ( $I_{\text{Kto,f}}$ ), the rapid delayed rectifier  $\text{K}^+$  current ( $I_{\text{Kr}}$ ), the ultrarapidly activating delayed rectifier  $\text{K}^+$  current ( $I_{\text{Kur}}$ ), the noninactivating steady-state voltage activated  $\text{K}^+$  current ( $I_{\text{Kss}}$ ), the time-independent  $\text{K}^+$  current ( $I_{\text{K1}}$ ), the  $\text{Na}^+/\text{K}^+$  pump ( $I_{\text{NaK}}$  is regulated by phospholemman, PLM), the  $\text{Ca}^{2+}$  and  $\text{Na}^+$  background currents ( $I_{\text{Cab}}$  and  $I_{\text{Nab}}$ ). The  $\text{Ca}^{2+}$  fluxes are uptake of  $\text{Ca}^{2+}$  from the cytosol to the network sarcoplasmic reticulum (NSR) ( $J_{\text{up}}$ ) by the SERCA pump and  $\text{Ca}^{2+}$  release from the junctional sarcoplasmic reticulum (JSR) ( $J_{\text{rel}}$ ) through the ryanodine receptors (RyRs). There are three intracellular compartments in the  $\beta_1$ -adrenergic signaling system: caveolae, extracaveolae, and cytosol. The subspace volume ( $V_{\text{ss}}$ ) is located in the extracaveolae domain. Components of the  $\beta_1$ -adrenergic signaling system are the  $\beta_1$ -adrenergic receptors ( $\beta_1$ -AR), the  $\alpha$ -subunit of stimulatory G-protein ( $G_{\text{ss}}$ ), the  $\beta\gamma$ -subunit of stimulatory G-protein ( $G_{\beta\gamma}$ ), the adenylyl cyclases of type 5/6 or 4/7 (AC5/6 or AC4/7, respectively), the phosphodiesterases of type 2, 3, or 4 (PDE2, PDE3, or PDE4, respectively), the cyclic AMP (cAMP), regulatory (R) and catalytic (C) subunits of protein kinase A holoenzyme, the protein kinase A inhibitor (PKI), the G-protein-coupled receptor kinase of type 2 (GRK2), the protein phosphatases of type 1 or 2A (PP1 or PP2A, respectively), the inhibitor-1 (I-1). The cytosolic proteins which are the substrates of the  $\beta_1$ -adrenergic signaling system are the phospholamban (PLB) and troponin I (TnI). Stimulatory links are shown by black arrows and inhibitory links are shown by red dashed lines with balls.  $[\text{Ca}^{2+}]_{\text{iv}}$ ,  $[\text{Na}^+]_{\text{iv}}$ , and  $[\text{K}^+]_{\text{iv}}$  are the intracellular  $\text{Ca}^{2+}$ ,  $\text{Na}^+$ , and  $\text{K}^+$  concentrations in the caveolae, extracaveolae, and cytosol;  $[\text{Ca}^{2+}]_{\text{ov}}$ ,  $[\text{Na}^+]_{\text{ov}}$ , and  $[\text{K}^+]_{\text{ov}}$  are the extracellular  $\text{Ca}^{2+}$ ,  $\text{Na}^+$ , and  $\text{K}^+$  concentrations.

doi:10.1371/journal.pone.0089113.g001

dissociation of two catalytic subunits that phosphorylate target proteins, among them are PDE3 and PDE4.  $\beta_1$ -ARs are phosphorylated by PKA, as well as by G protein coupled receptor kinase of type 2 (GRK2). PKA is also regulated by heat-stable protein kinase inhibitor (PKI). Intracellular proteins are dephosphorylated by two types of phosphatases, protein phosphatase 1 and 2A. PKA target proteins are located in different compartments. In our model, 20% of the L-type  $\text{Ca}^{2+}$  channels (the L-type  $\text{Ca}^{2+}$  current,  $I_{\text{CaL}}$ ), the fast  $\text{Na}^+$  current,  $I_{\text{Na}}$ , and the phospholemman, which regulates the  $\text{Na}^+/\text{K}^+$  pump,  $I_{\text{NaK}}$ , are localized in the caveolae compartment; 80% of the L-type  $\text{Ca}^{2+}$  channels, the ryanodine receptors, RyRs, the ultra-rapidly activating delayed rectifier  $\text{K}^+$  current,  $I_{\text{Kur}}$ , the rapidly inactivating transient outward  $\text{K}^+$  current,  $I_{\text{Kto,f}}$  and the time-independent  $\text{K}^+$  current,  $I_{\text{K1}}$ , are localized in the extracaveolae compartment; and phospholamban and troponin I are localized in the cytosolic compartment (more details are shown below).

## Model Development: Biochemical Part

**$\beta_1$ -adrenergic receptor module.** According to the experimental findings [19,20,28], the vast majority of  $\beta_1$ -adrenergic receptors are located in non-caveolae fractions. The estimated total concentration of  $\beta_1$ -ARs in mouse ventricular myocytes is  $0.0103 \mu\text{M}$  [29]. In our model, we distribute the  $\beta_1$ -ARs almost evenly between the extracaveolae and cytosolic compartments, with only 1% located in the caveolae compartment (see Appendix S1). Such distribution of  $\beta_1$ -ARs allowed us to obtain in the model approximately equal cAMP transients in the caveolae and extracaveolae compartments, which is in line with the measurements of local cAMP concentrations in similar compartments in rat and mouse ventricular myocytes [30]. In the  $\beta_1$ -adrenergic receptor module, we separate relatively fast biochemical reactions (ligand-receptor and G-protein-receptor interactions, with time scales of tens milliseconds [31]), which are described by algebraic equations in steady-state approximation, and slower reactions

(G-protein activation (hundreds milliseconds [31]), PKA- and GRK2-mediated phosphorylation (hundreds seconds [31]; GRK2, G-protein-coupled receptor kinase of type 2)), which are described by ordinary differential equations (see Appendix S1).

In order to derive algebraic equations which describe ligand-receptor and G-protein-receptor interactions in the caveolae compartment (equations (A.7)-(A.11) in the Appendix S1), we consider mass conservation laws for non-phosphorylated  $\beta_1$ -adrenergic receptors and G-proteins in that compartment:

$$[R_{\beta_1}]_{np,tot}^{cav} = [LR_{\beta_1}]_{np}^{cav} + [LR_{\beta_1}G_s]_{np}^{cav} + [R_{\beta_1}G_s]_{np}^{cav} + [R_{\beta_1}]_{np,f}^{cav}, \quad (1)$$

$$[G_s]_{\alpha\beta\gamma}^{cav} = [LR_{\beta_1}G_s]_{np}^{cav} + [R_{\beta_1}G_s]_{np}^{cav} + [G_s]_{f}^{cav}, \quad (2)$$

where  $[R_{\beta_1}]_{np,tot}^{cav}$  is the total concentration of non-phosphorylated (*np*)  $\beta_1$ -ARs in the caveolae compartment,  $[LR_{\beta_1}]_{np}^{cav}$  is the concentration of  $\beta_1$ -ARs with bound ligand *L* (concentration [*L*]),  $[LR_{\beta_1}G_s]_{np}^{cav}$  is the concentration of  $\beta_1$ -ARs with bound ligand *L* and stimulatory G-protein  $G_s$ ,  $[R_{\beta_1}G_s]_{np}^{cav}$  is the concentration of  $\beta_1$ -ARs with bound  $G_s$ ,  $[R_{\beta_1}]_{np,f}^{cav}$  is the concentration of free  $\beta_1$ -ARs,  $[G_s]_{\alpha\beta\gamma}^{cav}$  is the total concentration of the stimulatory G-protein  $G_s$ , and  $[G_s]_{f}^{cav}$  is the concentration of free  $G_s$ .

Concentrations of complexes  $[LR_{\beta_1}]_{np}^{cav}$ ,  $[LR_{\beta_1}G_s]_{np}^{cav}$ , and  $[R_{\beta_1}G_s]_{np}^{cav}$  can be obtained from the steady-state approximation for corresponding biochemical reactions, provided that the related dissociation constants are known (equations (A.12)-(A.14) in the Appendix S1). The steady-state approximation for a chemical reaction describes the formation of complex AB from the substances A and B:  $A+B \leftrightarrow AB$ . For this reaction,  $k^+$  and  $k^-$  are the forward and backward rates, respectively, and *K* is the dissociation constant ( $K = k^-/k^+$ ). The complex formation is described by the differential equation  $d[AB]/dt = k^+[A] \cdot [B] - k^- [AB]$ , where  $[A]$ ,  $[B]$ , and  $[AB]$  are the concentrations of the substances A, B, and complex AB, respectively. In steady state,  $d[AB]/dt = 0$ , therefore,  $k^+[A] \cdot [B] - k^- [AB] = 0$ . From the last equation, we can determine the concentration of complex AB in the steady-state approximation:  $[AB] = [A] \cdot [B] / (k^- / k^+) = [A] \cdot [B] / K$ .

Substitution of the equation for  $[LR_{\beta_1}G_s]_{np}^{cav}$ , and  $[R_{\beta_1}G_s]_{np}^{cav}$  into equation (1) and solution with respect to  $[G_s]_{f}^{cav}$  yields equation (A.11). Further substitution of the expressions for  $[LR_{\beta_1}]_{np}^{cav}$ ,  $[LR_{\beta_1}G_s]_{np}^{cav}$ ,  $[R_{\beta_1}G_s]_{np}^{cav}$ , and  $[G_s]_{f}^{cav}$  into equation (2) results in equation (A.10). The complete system of algebraic equations for ligand-receptor and G-protein-receptor interactions for the caveolae, extracaveolae, and cytosolic compartments is given in Appendix S1.

Activation of  $G_s$ -proteins, with dissociation of  $[G_s]_{\alpha,GTP}^{cav}$  and  $[G_s]_{\beta\gamma}^{cav}$ -subunits, occurs through a relatively fast process with  $[LR_{\beta_1}G_s]_{np}^{cav}$  complex or a relatively slow process with  $[R_{\beta_1}G_s]_{np}^{cav}$  complex, and  $[G_s]_{\alpha,GTP}^{cav}$  is hydrolyzed further to  $[G_s]_{\alpha,GDP}^{cav}$ .  $[G_s]_{\alpha\beta\gamma}^{cav}$  is formed back through re-association of  $[G_s]_{\alpha,GDP}^{cav}$  and  $[G_s]_{\beta\gamma}^{cav}$  (equations (A.17)-(A.19) in Appendix S1) [8,10].

Phosphorylation (desensitization) of  $\beta_1$ -ARs occurs by both protein kinase A and G-protein-coupled receptor kinase of type 2, GRK2 [8,10] (equations (A.15) and (A.16) for the caveolae compartment). PKA phosphorylates  $\beta_1$ -ARs both in ligand- and G-protein-bound states and unbound states, while GRK2 phosphorylation affects only ligand-bound states [8,10]. According to the experimental finding [32], application of 10  $\mu$ M of  $\beta_1$ -ARs

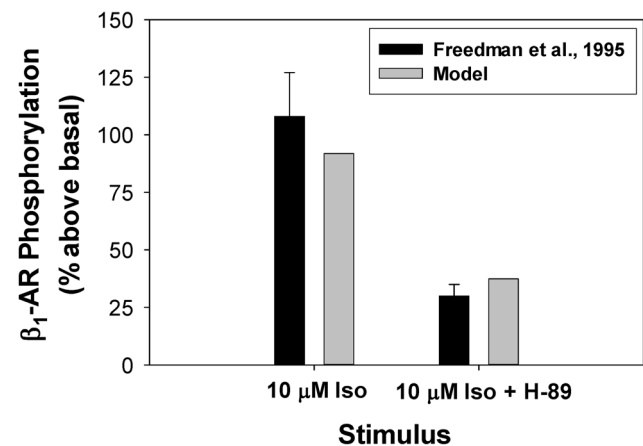
agonist isoproterenol increased the phosphorylation level of  $\beta_1$ -ARs by about 108% (Fig. 2), which is reproduced by our model. Moreover, about 30% of phosphorylation of  $\beta_1$ -ARs occurs by GRK2, as it is found from the suppression of PKA by H-89 (Fig. 2). Our model is also able to reproduce this effect.

**Adenylyl cyclase module.** In a  $\beta_1$ -adrenergic pathway, adenylyl cyclases are responsible for synthesis of cAMP from ATP. Our model includes four major types of adenylyl cyclases (AC) found in mouse ventricular myocytes, AC4, AC5, AC6, and AC7 [33,34]. Two of them, AC5 and AC6, are located in caveolae and have similar properties (we denote them as AC5/6) [35]. Two others, AC4 and AC7, also have similar properties: they do not co-immunoprecipitate with caveolin-3 and they are excluded from caveolae (we denote them as AC4/7) [13,28,36].

We simulated activation of adenylyl cyclases by the  $\alpha$ -subunit of G-protein,  $G_{s\alpha}$ , [8,13] (see Appendix S1). In addition, we considered the stimulation of adenylyl cyclases AC5/6 and AC4/7 by  $\beta\gamma$ -subunit,  $G_{s\beta\gamma}$ , according to the experimental data [37,38,39,40]. The total amount of adenylyl cyclases in a cardiac cell is estimated as 0.02622  $\mu$ M [41], with 74% of AC5/6 type [8].

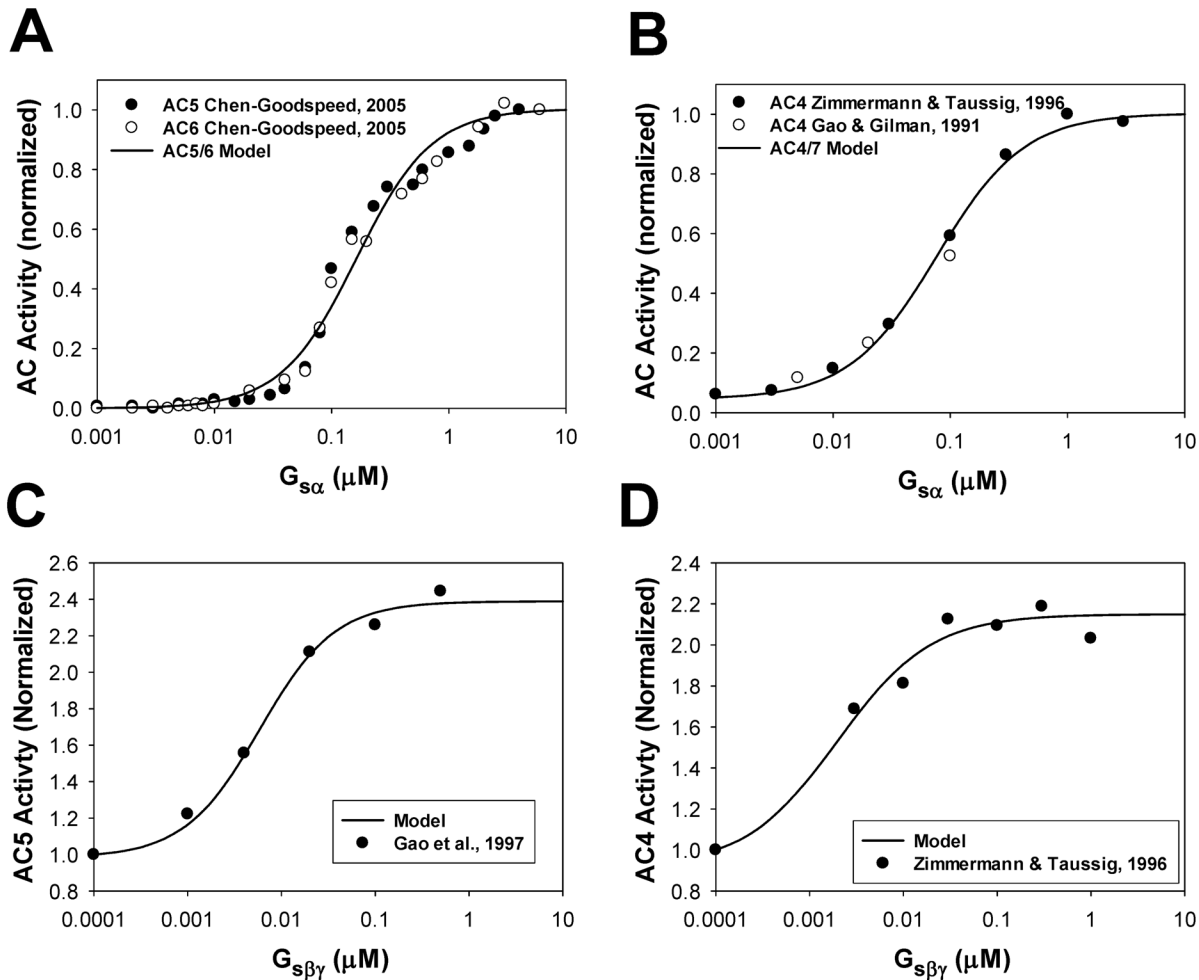
Figure 3A shows experimental data on activation of AC5 and AC6 by  $G_{s\alpha}$  [37] and corresponding simulation data using our model for AC5/6 activation. In Fig. 3B, simulation data on activation of AC4/7 by  $G_{s\alpha}$  is compared to the experimental data for AC4 [38,40]. Figures 3C and 3D compare the experimental data from [39,40] to our simulations for the dependence of AC5/6 and AC4/7 activities on  $G_{s\beta\gamma}$ . Both figures show good agreement between the experimental and simulated results.

We also simulated the effects of different concentrations of  $\beta_1$ -adrenoceptor agonist isoproterenol on adenylyl cyclase activity in mouse ventricular myocytes (Fig. 4A). Experimental data on total AC activity in mouse ventricles and cardiac cells as a function of isoproterenol concentration after 10-min exposures are shown by unfilled [42] and filled circles [43] with error bars. Simulation data on AC activity at the 10<sup>th</sup> minute after the exposure to different concentrations of isoproterenol are shown by a solid line. As seen in Fig. 4A, our model was able to reproduce absolute values of the total cellular adenylyl cyclase activity as a function of isoproterenol.



**Figure 2.  $\beta_1$ -adrenoceptors phosphorylation.**  $\beta_1$ -adrenoceptors phosphorylation above basal level after 15-minute application of 10  $\mu$ M isoproterenol or 10  $\mu$ M isoproterenol+PKA inhibitor H-89. Experimental data from Freedman et al. [32] are shown with black bars with errors, simulation data are shown with gray bars. Effect of H-89 was simulated by setting  $[PKA]_{tot} = 0$   $\mu$ M.

doi:10.1371/journal.pone.0089113.g002



**Figure 3. Normalized activity of adenylyl cyclases as functions of  $G_{s\alpha}$  and  $G_{s\beta\gamma}$ .** Panel A: Experimental normalized activity of AC5 (filled circles) and AC6 (unfilled circles) as functions of  $G_{s\alpha}$  [37]. Simulated data for normalized activity of AC5/6 is shown by a solid line. Panel B: Experimental normalized activity of AC4 (filled circles from [40] and unfilled circles from [38]) as functions of  $G_{s\alpha}$ . Simulated data for normalized activity of AC4/7 is shown by a solid line. Panel C: Experimental normalized activity of AC5 (filled circles) [39] as functions of  $G_{s\beta\gamma}$ . Simulated data for normalized activity of AC5/6 is shown by a solid line. Panel D: Experimental normalized activity of AC4 (filled circles) [40] as functions of  $G_{s\beta\gamma}$ . Simulated data for normalized activity of AC4/7 is shown by a solid line. doi:10.1371/journal.pone.0089113.g003

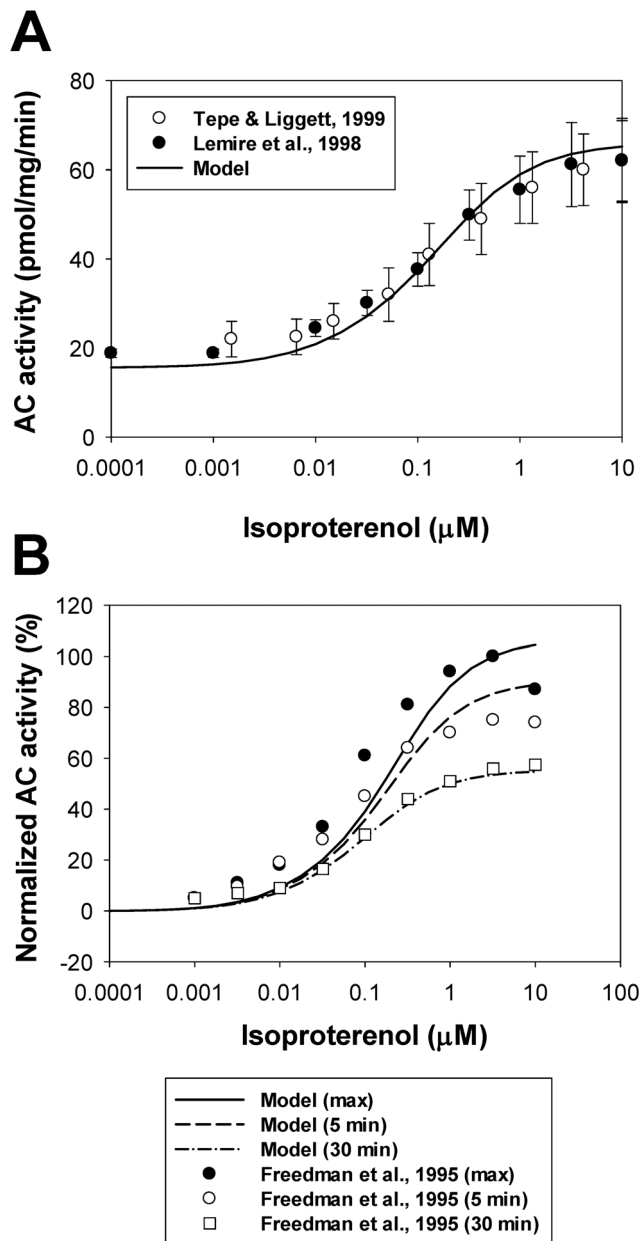
Adenylyl cyclase activity can also be used as an indicator of desensitization of  $\beta_1$ -ARs. Experimental data on AC activity as a function of isoproterenol were obtained by Freedman et al. [32] at three time moments after exposure to an agonist (at the maximum activity (from 50<sup>th</sup> to 75<sup>th</sup> seconds, depending on isoproterenol concentration), 5<sup>th</sup> min, and 30<sup>th</sup> min). It is shown that the AC activity decreases in time, reflecting  $\beta_1$ -ARs desensitization (phosphorylation by PKA and GRK2) (symbols in Fig. 4B). Our model satisfactorily reproduced this phenomenon. Simulation data also demonstrates the decrease in AC activity as a function of time at different concentrations of isoproterenol (solid, dashed, and dash-dotted lines in Fig. 4B).

**Phosphodiesterase module.** Phosphodiesterases in the  $\beta_1$ -adrenergic signaling system degrade cAMP into inert molecule 5'-AMP. We included in our model three major types of phosphodiesterases (PDE2, PDE3, and PDE4) found in mouse ventricular myocytes [44]. While a significant amount of PDE1 was found in mouse ventricles, the study of Bode et al. [45] shows that this type of PDE is predominantly located in non-myocyte cells. As in previous models [8,13], we put PDE2, PDE3, and

PDE4 into the caveolae and cytosolic compartments, and PDE2 and PDE4 into the extracaveolae compartment. Such distribution fits available experimental data on their localization [46,47]. For subcellular distribution of the PDE isoforms we used experimental data obtained by Mongillo et al. [48] for rat ventricular myocytes, and the parameters were adjusted to fit experimental data on PDE2, PDE3, and PDE4 activities in mouse hearts [44,49].

PDE2, PDE3, and PDE4 are activated by cAMP molecules, but with different affinities (see Appendix S1). In addition, phosphorylation of PDE3 and PDE4 increases their activities by several folds. These processes are simulated by ordinary differential equations derived for three subcellular compartments (caveolae, extracaveolae, and cytosol, see Appendix S1). Our model also tested the effects of non-specific PDE inhibitor 3-isobutyl-1-methylxanthine (IBMX).

Figure 5A shows experimental and simulated absolute activities of PDE2, PDE3, and PDE4 in mouse and rat hearts. There are some differences in the magnitudes of experimental contributions of different PDE isoforms in total cellular PDE activity obtained by different research groups and between species. However, these



**Figure 4. Adenylyl cyclase activity as a function of isoproterenol.** Panel A: Experimental data on AC activity (in pmol/mg/min) in mouse hearts and ventricular myocytes obtained after 10-minutes exposure to isoproterenol are shown by unfilled circles [42] and filled circles [43]. The solid line shows corresponding simulated AC activities at different concentrations of isoproterenol. Panel B: Desensitization of  $\beta_1$ -ARs. Increase in adenylyl cyclase activities above basal level (in %) are measured at maximum (from 50<sup>th</sup> to 75<sup>th</sup> seconds, control, filled circles) and at two time moments (5 min and 30 min, unfilled circles and unfilled squares, respectively) after exposure to different concentrations of isoproterenol [32]. Corresponding simulated data for the maximum, 5-minute, and 30-minute delays are shown by solid, dashed, and dash-dotted lines, respectively.  
doi:10.1371/journal.pone.0089113.g004

differences are diminished in Fig. 5B for fractional contributions of different PDEs and between species. Our model successfully reproduced both absolute PDE activities and the fractional contributions of PDE2, PDE3, and PDE4 to the total cellular PDE activity. In addition to the cellular activity, we were able to

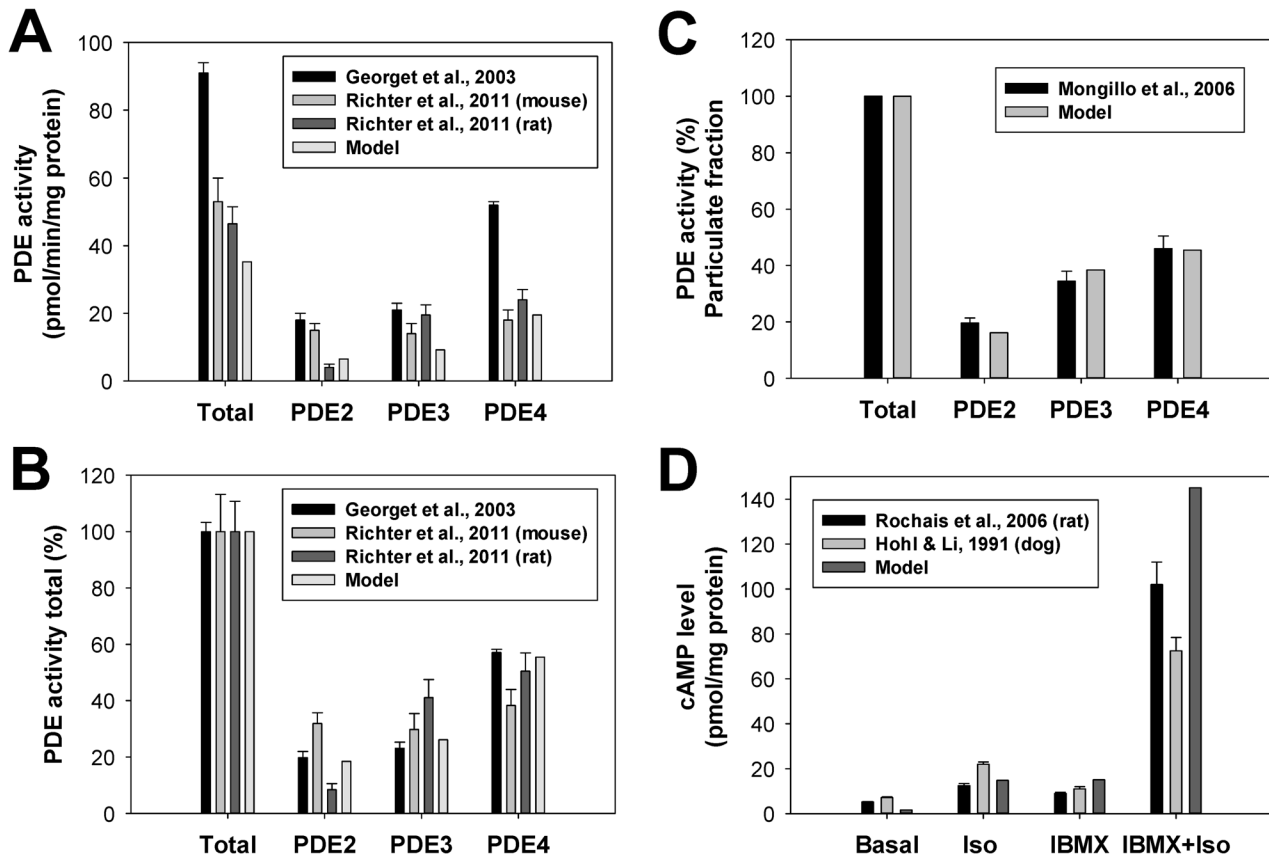
reproduce the partial contributions of different PDE isoforms into the total PDE activity of particulate fraction (Fig. 5C). In this figure, we used experimental data of Mongillo et al. [48] obtained from rat cardiomyocytes.

The effects of the PDE inhibitor IBMX on cAMP production in ventricular myocytes can be estimated by the levels of cAMP at different experimental conditions. Figure 5D shows experimental cAMP levels in ventricular myocytes from the rat and canine hearts at the resting state after application of isoproterenol or IBMX separately and at simultaneous application of IBMX and isoproterenol. It is remarkable that the experimental data from both species are very similar (bars with the errors in Fig. 5D). Our model reproduces the experimental cAMP level after application of different combinations of IBMX and isoproterenol (bars without errors).

**cAMP-PKA module.** cAMP molecules generated in cardiac myocytes by adenylyl cyclases and partially hydrolyzed by phosphodiesterases activate protein kinase A, a major signaling molecule in the  $\beta_1$ -adrenergic signaling system which phosphorylates ion channels and proteins of the  $Ca^{2+}$  handling system. Inactive PKA holoenzyme consists of two regulatory subunits R (both either of type I, RI, or type II, RII) and two catalytic subunits C. Activation of PKA holoenzyme requires binding four cAMP molecules, in general, with different affinities. PKA holoenzyme with bound four cAMP molecules dissociates two catalytic subunits, which phosphorylates target proteins. In our model, we consider identical affinities for all four binding sites of PKA. Two isoforms of PKA holoenzyme are found in mouse ventricular myocytes, PKAI and PKAII, which differ by their regulatory subunits. PKAI is predominantly located in the cytosolic compartment, and PKAII is the predominant isoform in the caveolae and extracaveolae compartments.

PKAI and PKAII differ not only by their location, but also by their half-activation constants,  $K_{PKAI}$  and  $K_{PKAII}$ . Some experimental data suggest half-activation constants for  $K_{PKAI} \sim 0.1 \mu M$  [50,51] and  $K_{PKAII} \sim 0.5 \mu M$  [51], one of which is significantly smaller and the other is comparable to the resting cAMP concentrations in cardiac cells  $\sim 0.5\text{--}1 \mu M$  [52,53]. Under such conditions, almost all PKA in the cytosol and most PKA in the caveolae and extracaveolar compartments must be activated. Other experimental data suggest  $K_{PKAI}$  and  $K_{PKAII}$  in the range  $\sim 1.5\text{--}3 \mu M$  [54,55,56]. As it was pointed out by Dao et al. [55], relatively small values of  $K_{PKAI}$  and  $K_{PKAII}$  in the nanomolar range were obtained in some experiments because they used free regulatory subunits RI or RII instead of PKA holoenzymes. Experimental data with PKA holoenzymes yielded significantly larger dissociation constants, which are used in our model ( $K_{PKAI,1}$  and  $K_{PKAI,2} = 2.9 \mu M$  [55];  $K_{PKAII,1}$  and  $K_{PKAII,2} = 2.5 \mu M$  [8,54]). Activation of PKA holoenzyme is described by ordinary differential equations (see Appendix S1). In addition, the model includes inhibition of PKA by heat-stable protein kinase inhibitor (PKI), the dynamics of which are also described by a differential equation.

Figure 6A shows activation levels of PKAI and PKAII as functions of cAMP concentrations. We used experimental data [54,55] shown by circles (PKAI) and squares (PKAII). Our simulations are displayed by a solid (PKAI) and a dashed (PKAII) line, respectively. They fit reasonably well to the experimental data. We also simulated the cellular PKA activity ratio in control and upon stimulation of the  $\beta_1$ -adrenergic signaling system by  $1 \mu M$  isoproterenol (Fig. 6B). Four simulations were performed for this figure: no isoproterenol/basic cAMP level ( $-cAMP$ ), no isoproterenol/ $3 \mu M$  cAMP ( $+cAMP$ ),  $1 \mu M$  isoproterenol/no externally applied cAMP ( $-cAMP$ ), and  $1 \mu M$  isoproterenol/ $3 \mu M$  cAMP ( $+cAMP$ ). Then, the corresponding PKA( $-cAMP$ )/



**Figure 5. The effects of  $\beta_1$ -adrenoceptor stimulation on PDE activities.** **Panel A:** Absolute total PDE activities and the activities of PDE2, PDE3, and PDE4 obtained experimentally from the mouse and rat hearts (in pmol/min/mg protein, bars with errors [44,49]) and corresponding simulation data (bars without errors). **Panel B:** Fractional activities of PDE2, PDE3, and PDE4 obtained experimentally from the mouse and rat hearts (in %, bars with errors [44,49]) and corresponding simulation data (bars without errors). **Panel C:** Partial activities of PDE2, PDE3, and PDE4 obtained experimentally from the particulate fraction of the rat hearts (in %, bars with errors [48]) and corresponding simulation data (bars without errors). In the experiments and simulations, PDE activities are obtained at fixed cAMP concentrations of 1  $\mu$ M. **Panel D:** The effects of PDE inhibitor IBMX on cAMP levels in ventricular myocytes. Experimental data for rat [147] and canine [148] ventricular myocytes are shown by bars with errors, simulation data are shown by bars without errors. In the experiments with rat ventricular myocytes measurements were performed after 3-minute stimulations (5  $\mu$ M isoproterenol, or 100  $\mu$ M IBMX, or both) [147]. In the experiments with canine ventricular myocytes measurements were performed after 5-minute stimulations (10  $\mu$ M isoproterenol, or 10  $\mu$ M IBMX, or both) [148]. Simulated cAMP level is determined at the 3<sup>rd</sup> minute upon application of 5  $\mu$ M isoproterenol, or 100  $\mu$ M IBMX, or both. doi:10.1371/journal.pone.0089113.g005

PKA(+cAMP) ratios were calculated. The simulations (grey bars) compare well to the experimental data for the rabbit hearts obtained in control and after application of 1  $\mu$ M isoproterenol (black bars [57]).

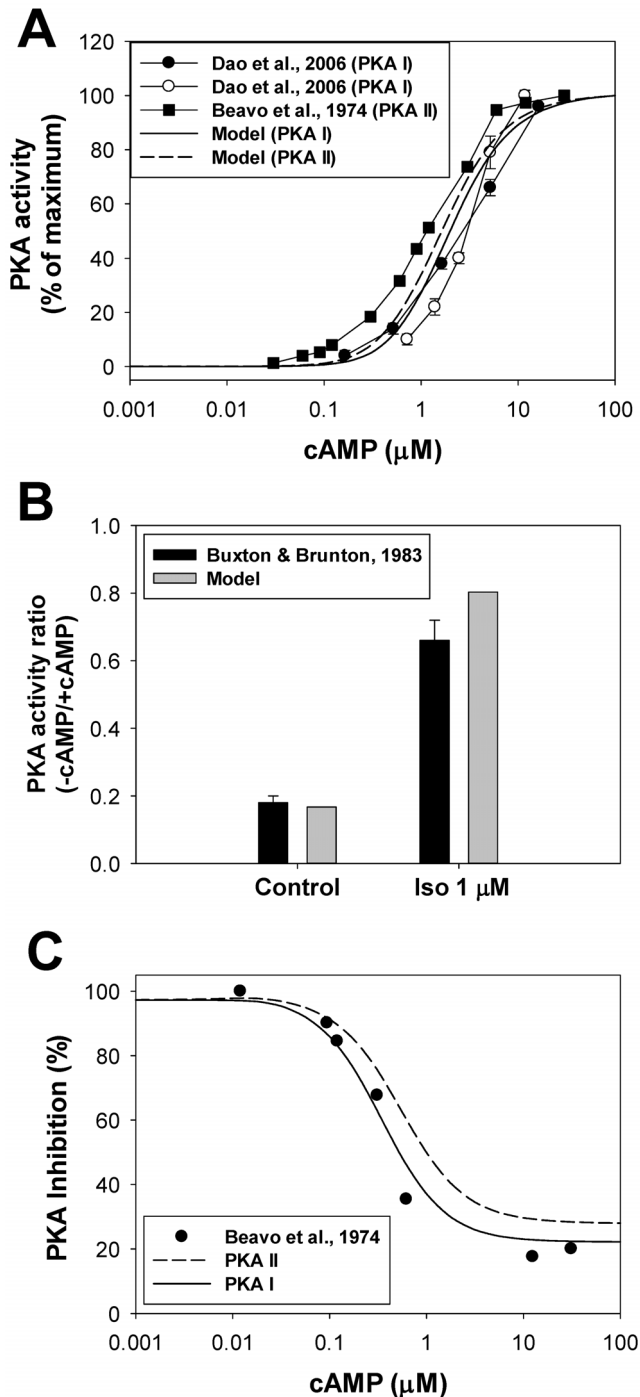
The effect of a heat-stable protein kinase inhibitor (PKI) on the PKA activity is shown in Fig. 6C. Experimental data obtained from [54] for PKA II are shown by filled circles, and simulation results are plotted by a solid line for PKA I and by a dashed line for PKA II. PKA activities are calculated with and without PKI at different concentrations of cAMP, then their ratios were calculated (in %) and subtracted from 100%. As seen from Fig. 6C, model simulations fit reasonably well to the experimental data.

**Protein phosphatases and inhibitor-1 module.** There are two major types of protein phosphatases which are important for cardiac myocyte function, protein phosphatase 1 (PP1) and 2A (PP2A). Localization of PP1 and PP2A in three subcellular compartments can be determined by their co-localization with caveolin-3 and by modulation of their targets. Data of Hescheler et al. [58] and Balijepalli et al. [19] show that the L-type  $Ca^{2+}$  current is inhibited by both PP1 and PP2A, and that the portion of

the L-type  $Ca^{2+}$  channels and PP2A co-localize with caveolin-3, suggesting caveolae localization for both PP1 and PP2A. PP1 and PP2A are also localized in the cytosolic compartment, as they interact with phospholamban and troponin I [59,60]. In mouse hearts, PP1 is the predominant phosphatase, whose contribution to the total phosphatase activity is  $\sim$ 75% [61,62]. As there is no current consensus on whether PP1 or PP2A is predominant in the extracaveolae compartment [63], we assume that only PP1 contributes to phosphatase activity in extracaveolae. We use basically the same molar distribution of PP1 and PP2A in subcellular compartments as Heijman et al. [8] (see Appendix S1), provided that 75% and 25% of cellular phosphatase are of PP1 and PP2A, respectively, as found experimentally in mice [61,62].

In ventricular myocytes, protein phosphatase 1 is regulated by endogenous inhibitor-1 (I-1) [64]. I-1 is localized in the cytosolic compartment and inhibits PP1 activity when phosphorylated. Cellular concentration of I-1 is estimated as  $[Inhib1]_{tot}^{cyt} = 0.08543 \mu$ M [65]. Ablation of I-1 leads to a moderate increase in PP1 activity and impaired  $\beta_1$ -adrenergic function [64,65]. As the affinity of I-1 to PP1 is very high ( $K_{Inhib1} = 1$  nM),





**Figure 6. The effects of  $\beta_1$ -adrenoceptor stimulation on PKA activities.** **Panel A:** PKA I and PKA II activities as functions of cAMP. Experimental data for PKA I obtained by two methods are shown by filled and unfilled circles [55]; data for PKA II obtained by Beavo et al. [54]. Corresponding simulated data are shown by a solid (PKA I) and a dashed (PKA II) line. **Panel B:** PKA activity ratio. Experimental data were obtained without (-cAMP) and with (+cAMP) externally applied 3  $\mu$ M cAMP, both without and with 1  $\mu$ M isoproterenol (black bars [57]). We also performed four simulations: no isoproterenol/basic level cAMP (-cAMP), no isoproterenol/3  $\mu$ M cAMP (+cAMP), 1  $\mu$ M isoproterenol/no externally applied cAMP (-cAMP), and 1  $\mu$ M isoproterenol/3  $\mu$ M cAMP (+cAMP). Then, the corresponding PKA ratios were calculated. **Panel C:** Protein kinase A inhibition by a heat-stable protein kinase inhibitor PKI. Experimentally, PKA activities were measured with and without PKI at different concentrations of cAMP, then their ratio was calculated (in %)

and subtracted from 100% (filled circles, [54]). Corresponding simulation data for PKA I and PKA II are shown by solid and dashed lines. Concentration of  $[PKI]_{tot} = 2 \cdot 0.2 \cdot [PKA]_{tot}$ . doi:10.1371/journal.pone.0089113.g006

we used steady-state approximation to describe I-1-PP1 interaction with corresponding mass conservation relationships:

$$[Inhib1]_{p,tot}^{cyt} = [Inhib1]_p^{cyt} + \frac{[PP1]_f^{cyt} \cdot [Inhib1]_p^{cyt}}{K_{Inhib1}}. \quad (3)$$

$$[PP1]_{tot}^{cyt} = [PP1]_f^{cyt} + \frac{[PP1]_f^{cyt} \cdot [Inhib1]_p^{cyt}}{K_{Inhib1}}. \quad (4)$$

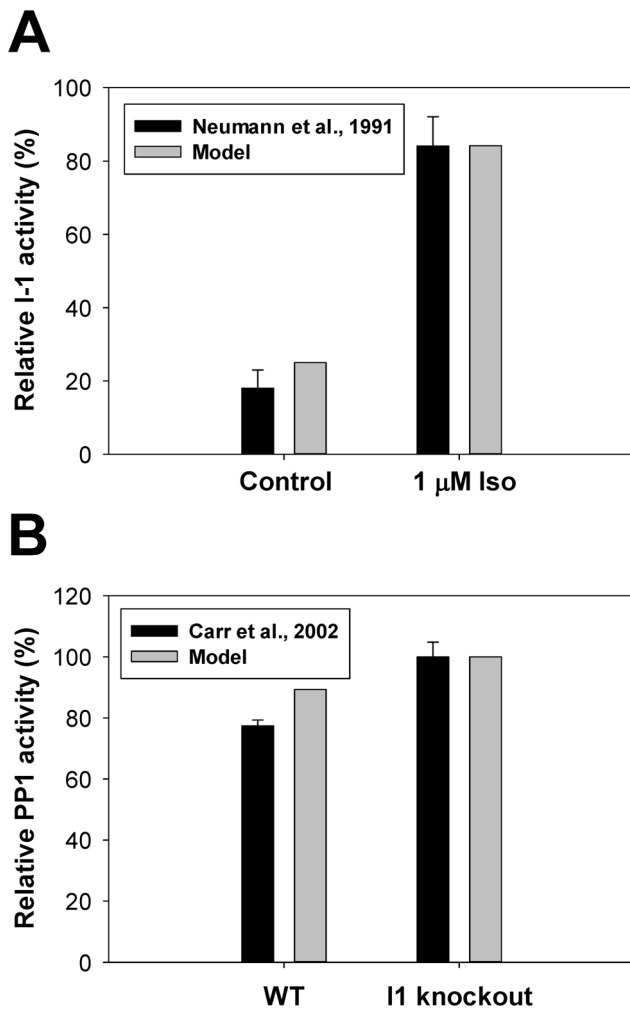
$$[Inhib1]_{tot}^{cyt} = [Inhib1]_f^{cyt} + [Inhib1]_{p,tot}^{cyt}. \quad (5)$$

where  $[Inhib1]_{p,tot}^{cyt}$  is the total concentration of phosphorylated I-1 in cytosol,  $[Inhib1]_p^{cyt}$  is the unbound phosphorylated I-1 concentration,  $[Inhib1]_f^{cyt}$  is the non-phosphorylated I-1 concentration,  $[PP1]_{tot}^{cyt}$  is the total concentration of PP1 in cytosol, and  $[PP1]_f^{cyt}$  is the unbound PP1 concentration. Solution of equations (3) – (5) gives the equations for calculating  $[Inhib1]_f^{cyt}$ ,  $[Inhib1]_p^{cyt}$ , and  $[PP1]_f^{cyt}$  (see equations (A.124) – (A.129) in the Appendix S1). Phosphorylation and dephosphorylation of I-1 occurs by the catalytic subunit of PKA and PP2A, respectively [64,66], and is described by equation (A.130) (see Appendix S1).

Figure 7A shows the effects of activation of the  $\beta_1$ -adrenergic signaling system by 1  $\mu$ M isoproterenol on inhibitor-1 activity. As there is no data for mice, we used the experimental data from guinea pig hearts [67] which shows significant activation of I-1 from ~20% to ~80% of its maximum activity. Our model reproduced the experimental data on I-1 activation. The effects of I-1 on PP1 activity can be estimated from data obtained from WT and I-1 knockout mice [64]. Figure 7B shows a slight increase in PP1 activity upon I-1 ablation (activity of PP1 in I-1 knockout mice is normalized to 100%). In the model, the effect of I-1 knockout is simulated by setting  $[Inhib1]_{tot}^{cyt} = 0$ , which leads to a slightly smaller increase in PP1 activity compared to that found experimentally.

**cAMP dynamics.** cAMP is one of the major signaling small molecules in the  $\beta_1$ -adrenergic signaling system. It moves freely between cellular compartments and has PKA as a major target. cAMP concentration is determined by the balance between cAMP production by adenylyl cyclases, cAMP degradation by phosphodiesterases, and cAMP diffusion between intracellular compartments (caveolae, extracaveolae, and cytosol) (see (A.131)-(A.133) in Appendix S1). Experimental data with unstimulated cells shows cAMP concentrations in mouse ventricular myocytes in the range from 2.4 to 6.0 pmol/mg protein (0.4522–1.13  $\mu$ M) [43,52,53]. Our model gives a background cellular cAMP concentration ~ 0.3  $\mu$ M. This concentration is close to the experimental values and to the values obtained in the models of others [8,11].

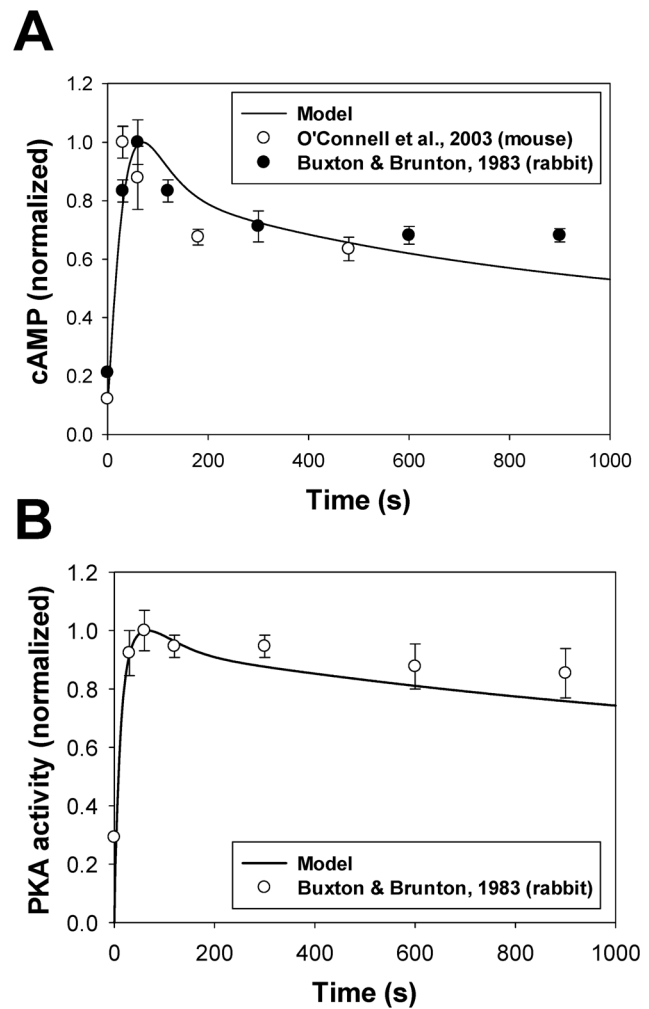
Stimulation of the  $\beta_1$ -adrenergic signaling system results in an increase of cAMP production by adenylyl cyclases and cAMP degradation by phosphodiesterases in the caveolae, extracaveolae, and cytosolic compartments. Figure 8A shows experimental time courses of normalized cAMP in mouse [68] and rabbit [57] ventricular myocytes obtained upon stimulation with 1  $\mu$ M isoproterenol (unfilled and filled circles, respectively). A solid line



**Figure 7. The effects of  $\beta_1$ -adrenoceptor stimulation on activities of I-1 and PP1.** **Panel A:** Relative I-1 activity in ventricular myocytes in control (left bars) and upon stimulation with 1  $\mu$ M isoproterenol (right bars). Experimental data for guinea pig hearts [67] are shown by black bars, simulation data with our model are shown by gray bars. **Panel B:** Relative PP1 activity in WT and I-1 knockout mouse hearts. Experimental data [64] are shown by black bars, our simulations – by gray bars. Experimental PP1 activity from I-1 knockout mouse hearts is normalized to 100%. doi:10.1371/journal.pone.0089113.g007

in Fig. 8A shows corresponding simulated time behavior of cAMP. Both simulated and experimental data show transient increase in cAMP concentration, which is due to changes in cAMP production by adenylyl cyclases, cAMP degradation by phosphodiesterases, cAMP fluxes between compartments, and  $\beta_1$ -ARs desensitization.

**PKA dynamics.** Our model is able to reproduce the time course of the cellular PKA activity, which is determined by the cellular concentration of catalytic subunit (solid line in Fig. 8B). As there is no data for mice, we used data of Buxton and Brunton [57] (unfilled circles in Fig. 8B) obtained for rabbit ventricular myocytes to constrain the model. Similar to cAMP dynamics, both experimental and simulation data for PKA demonstrate transient increase in activation, with subsequent decrease in activity.



**Figure 8. cAMP and PKA dynamics in mouse ventricular myocytes.** **Panel A:** cAMP dynamics in ventricular myocytes. Experimental data of normalized cAMP in mouse [68] and rabbit [57] ventricular myocytes are shown by unfilled and filled circles, respectively; simulation data is shown by a solid line. **Panel B:** PKA dynamics in ventricular myocytes. Experimental data of normalized PKA activity in rabbit [57] ventricular myocytes are shown by unfilled circles; simulation data is shown by a solid line. Data in **Panels A and B** was obtained upon application of 1  $\mu$ M isoproterenol. doi:10.1371/journal.pone.0089113.g008

#### Model Development: Electrophysiological Part

Electrical activity of the mouse ventricular myocytes is described by the equation for transmembrane potential [25]:

$$\frac{dV}{dt} = -\frac{1}{C_m}(I_{CaL} + I_{p(Ca)} + I_{NaCa} + I_{Cab} + I_{Na} + I_{Nab} + I_{NaK} + I_{Kto,f} + I_{K1} + I_{Kur} + I_{Kss} + I_{Kr} + I_{Cl,Ca} - I_{stim}).$$

where  $I_{CaL}$  is the L-type  $Ca^{2+}$  current,  $I_{p(Ca)}$  is the sarcolemmal  $Ca^{2+}$  pump,  $I_{NaCa}$  is the  $Na^+/Ca^{2+}$  exchanger,  $I_{Cab}$  is the  $Ca^{2+}$  background current,  $I_{Na}$  is the fast  $Na^+$  current,  $I_{Nab}$  is the  $Na^+$  background current,  $I_{NaK}$  is the  $Na^+-K^+$  pump,  $I_{Kto,f}$  is the rapidly recovering transient outward  $K^+$  current,  $I_{K1}$  is the time-independent  $K^+$  current,  $I_{Kur}$  is the ultrarapidly activating delayed rectifier  $K^+$  current,  $I_{Kss}$  is the noninactivating steady-state voltage activated  $K^+$  current,  $I_{Kr}$  is the rapid delayed rectifier  $K^+$  current,

$I_{Cl,Ca}$  is the  $Ca^{2+}$ -activated chloride current, and  $I_{stim}$  is the stimulus current.

In our model, we consider four of these currents ( $I_{CaL}$ ,  $I_{Na}$ ,  $I_{Kto,f}$  and  $I_{Kur}$ ) as the substrates of the  $\beta_1$ -adrenergic signaling system. The  $Na^+/K^+$  pump is affected by  $\beta_1$ -ARs through phosphorylation of phospholemman. One more current,  $I_{K1}$ , is also affected by  $\beta_1$ -ARs; however, in the voltage range from about  $-80$  to  $+40$  mV, this current does not change significantly. In addition, there are three other phosphorylation substrates, which are the major players in  $Ca^{2+}$  dynamics and are affected by  $\beta_1$ -ARs: ryanodine receptors, phospholamban, and troponin I. We consider all these  $\beta_1$ -adrenoceptor substrates below as separate modules in the model.

**L-type  $Ca^{2+}$  current module.** As found experimentally, the L-type  $Ca^{2+}$  channels are localized in both the caveolae and the extracaveolae compartments [19,21,22,69]. About 80% of the L-type  $Ca^{2+}$  channels are found within  $Ca^{2+}$  release units, or couplons [21], which are localized in the extracaveolae compartment, contribute directly to excitation-contraction coupling, and are the targets of the  $\beta_1$ -adrenergic signaling system [22,70]. The other 20% of the L-type  $Ca^{2+}$  channels are found in the caveolae [19,22]. The total amount of L-type  $Ca^{2+}$  channel protein can be estimated from the experimental data on the amount of RyRs in the mouse hearts ( $1058 \pm 45$  fmol/mg protein, or  $0.1993 \mu M$  [71]) and dihydropyridine (DHP) receptor-to-RyRs ratio for rats (RyR/DHP = 7.3 [72]), resulting in  $[I_{CaL}]_{tot} = 0.0273 \mu M$ . In the presented model, 20% and 80% of the L-type  $Ca^{2+}$  channels are localized in the caveolae and the extracaveolae compartments, respectively.

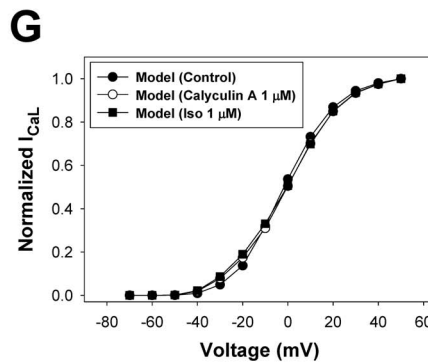
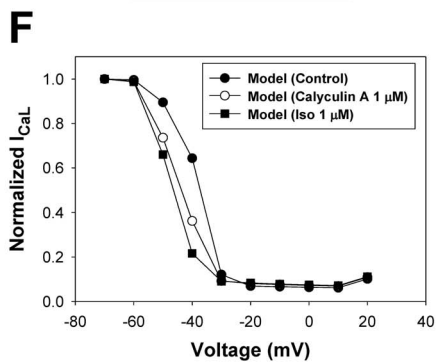
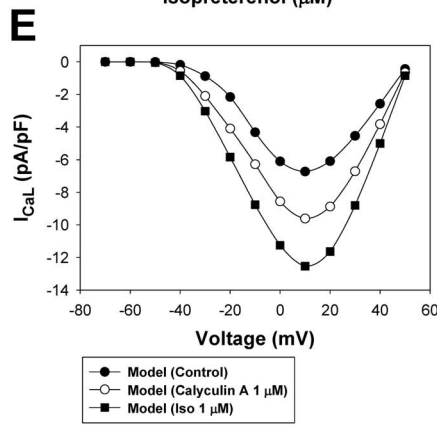
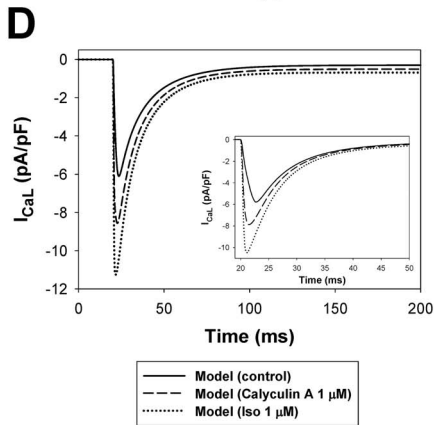
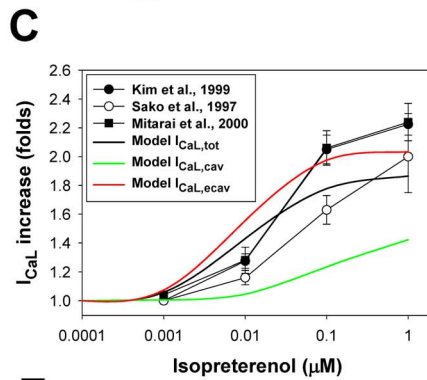
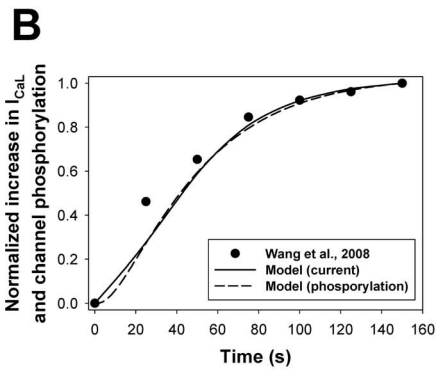
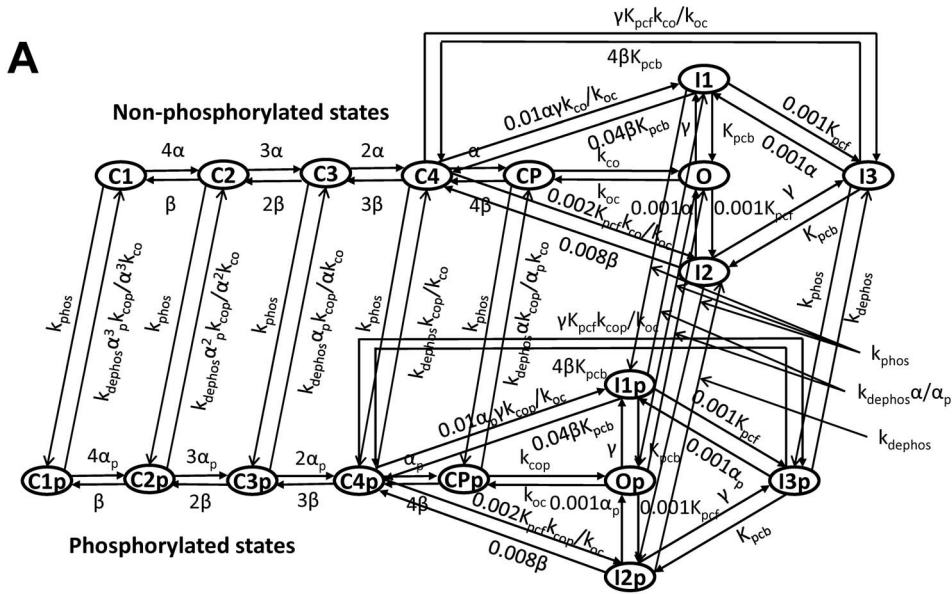
Effects of the  $\beta_1$ -adrenergic signaling system on the L-type  $Ca^{2+}$  channels and channel gating can be described with a Markov model for non-phosphorylated and phosphorylated states (Fig. 9A). The model includes two activation pathways: one for non-phosphorylated and one for phosphorylated channels. Each pathway includes five closed, one open, and three inactivated states. Transitions between non-phosphorylated and phosphorylated states are determined by the rates of phosphorylation by PKA and dephosphorylation by PP1 and PP2A (see Appendix S1). As we were unable to reproduce the experimental data on isoproterenol effects on the L-type  $Ca^{2+}$  channels with the Markov model from [25,26] due to the high maximum opening probability for the channels at large depolarizations, we introduced a voltage-independent rate limiting step and a new closed state ( $C_P$ , closed pre-open state) in the new model (Fig. 9A), which reduced the opening probability for non-phosphorylated channels compared to the models of Bondarenko et al. [25] and Petkova-Kirova et al. [26]. Experimental data show that the stimulation of  $\beta_1$ -ARs increases the magnitude of the L-type  $Ca^{2+}$  current and causes a hyperpolarization shift in normalized channel conductance ( $G/G_{max}$ ) and a steady-state inactivation relationship in mouse ventricular myocytes [73,74,75]. These effects are simulated by several changes to the phosphorylated pathway in the model (see Appendix S1) and an increase in  $G_{CaLp}$  ( $G_{CaLp} = 2.09G_{CaL}$  according to the estimation of an increase in maximum opening probability for cardiac  $Ca^{2+}$  channels from [76]).

Model parameters are adjusted to fit experimental data on both the basal L-type channel phosphorylation level and the time course of the current amplitude upon stimulation with isoproterenol. Experimental data suggest the basal phosphorylation level of the L-type  $Ca^{2+}$  channels in ventricular myocytes to be about 13–20% [77,78]. In our model, a fraction of phosphorylated channels under basal conditions is set to 10.3%. Upon application of  $1 \mu M$  isoproterenol, peak values of  $I_{CaL}$  increase in time upon stimulation with voltage pulses to 0 mV, as is seen from the

experimental data [75] (Fig. 9B). Our model reproduced the time course of the peak current increase under similar stimulations (solid line in Fig. 9B). It is remarkable that the simulated time course of the peak current increase (solid line in Fig. 9B) is very similar to the simulated time course of the relative phosphorylation level of the L-type  $Ca^{2+}$  channels (dashed line in Fig. 9B).

In addition to the time course of  $I_{CaL}$  increase, we simulated magnitudes of  $I_{CaL}$  increase after a 600-second exposure to different concentrations of isoproterenol (Fig. 9C). We evaluated the effects of isoproterenol on the total  $I_{CaL}$  ( $I_{CaL,tot}$ , black bold solid line in Fig. 9C) as well as on  $I_{CaL}$  populations localized in the caveolae ( $I_{CaL,cav}$ , green line in Fig. 9C) and extracaveolae ( $I_{CaL,ecav}$ , red line in Fig. 9C) compartments. The results of simulations for the total  $I_{CaL}$  are in a good agreement with the experimental data obtained by Kim et al. [79], Sako et al. [80], and Mitarai et al. [81] (Fig. 9C). Simulations also show that the effects of  $\beta_1$ -adrenergic receptor agonist is significantly stronger on the channels localized in the extracaveolae compartment (2.03 folds at  $1 \mu M$  Iso) compared to the channels in the caveolae compartment (1.42 folds at  $1 \mu M$  Iso). If the caveolae-located  $I_{CaL}$  is responsible for  $\sim 20\%$  of the total current amplitude in control, after exposure to isoproterenol ( $1 \mu M$ ) this fraction decreases to  $\sim 15\%$ . The results of simulations are in line with the experimental data of [70] who have shown that the  $I_{CaL}$  from the population of channels in the caveolae compartment comprises about 15% of the total current.

In addition to the effects of activation of the  $\beta_1$ -adrenergic signaling system, our model is tested in respect to the effects of inhibition of phosphatase activity on the L-type  $Ca^{2+}$  current. Figure 9D shows simulated  $I_{CaL}$  traces under heavy buffer conditions (with suppression of  $Ca^{2+}$ -induced  $Ca^{2+}$  release) elicited by voltage pulses to 0 mV in control (solid line) and after 1000-s exposure to  $1 \mu M$  Calyculin A (dashed line) and 600-s exposure to  $1 \mu M$  isoproterenol (dotted line). In simulations, we consider that Calyculin A inhibits 65% of the activity of both PP1 and PP2A. As seen from simulations in Fig. 9D, both isoproterenol and Calyculin A increase peak currents to different degrees, suggesting that both activation of PKA and inhibition of PP1 and PP2A increase the L-type  $Ca^{2+}$  current. Fitting simulated time courses from Fig. 9D yields bi-exponential inactivation of  $I_{CaL}$  with two time constants. Fast ( $Ca^{2+}$ -dependent inactivation) and slow (voltage-dependent inactivation) time constants are equal to 7.77 and 22.0 ms, 7.19 and 19.9 ms, and 6.54 and 18.5 ms for control (solid line), after 1000-s exposure to  $1 \mu M$  Calyculin A (dashed line), and 600-s exposure to  $1 \mu M$  isoproterenol (dotted line), respectively. These data show significant increase in  $Ca^{2+}$ -dependent inactivation of  $I_{CaL}$  upon stimulation of the  $\beta_1$ -adrenergic signaling system. Similar behavior of  $I_{CaL}$  is also observed experimentally with BAPTA in pipette solution [73]. Insert in Fig. 9D shows similar simulations with intact  $Ca^{2+}$ -induced  $Ca^{2+}$  release. In the last case, current traces also show bi-exponential decay with the fast and slow time constants 4.83 and 12.4 ms, 4.72 and 12.0 ms, and 4.66 and 12.8 ms for control (solid line), after 1000-s exposure to  $1 \mu M$  Calyculin A (dashed line), and 600-s exposure to  $1 \mu M$  isoproterenol (dotted line), respectively. These data show significant increase in the L-type  $Ca^{2+}$  current inactivation with intact  $Ca^{2+}$  dynamics. Simulations also show that activation of  $\beta_1$ -ARs increases peak current amplitudes by about two-fold (Fig. 9E) and causes a hyperpolarization shift in steady-state inactivation relationships (Fig. 9F) and more moderately in  $G/G_{max}$  data (Fig. 9G). Inhibition of PP1 and PP2A produced an intermediate effect on the  $I_{CaL}$  in terms of an increase in amplitude and a hyperpolarization shift of steady-state inactivation relationships and  $G/G_{max}$ . Similar increases in amplitudes and



**Figure 9. The effects of  $\beta_1$ -adrenoceptor stimulation on the L-type  $\text{Ca}^{2+}$  current. Panel A:** Markov model of the L-type  $\text{Ca}^{2+}$  channel. State diagram consists of two similar sub-diagrams for non-phosphorylated (upper sub-diagram) and phosphorylated states (lower sub-diagram).  $C_1, C_2, C_3, C_4,$  and  $C_p$  are closed states; O is the open state;  $I_1, I_2,$  and  $I_3$  are inactivated states;  $C_{1p}, C_{2p}, C_{3p}, C_{4p},$  and  $C_{pp}$  are closed phosphorylated states;  $O_p$  is the open phosphorylated state; and  $I_{1p}, I_{2p},$  and  $I_{3p}$  are phosphorylated inactivated states. The rate constants  $\alpha, \alpha_p,$  and  $\beta$  are voltage-dependent;  $\gamma$  is calcium dependent;  $k_{co}, k_{oc}, k_{cop}, k_{pcf}$  and  $k_{pcb},$  are voltage-insensitive; and  $k_{phos}$  and  $k_{dephos}$  are the phosphorylation and dephosphorylation rates, respectively (see Appendix S1). **Panel B:** Time course of the peak values of L-type  $\text{Ca}^{2+}$  current and L-type  $\text{Ca}^{2+}$  channel phosphorylation level upon stimulation with 1  $\mu\text{M}$  isoproterenol. Experimental data for peak  $I_{CaL}$  is obtained by a series of pulses to 0 mV for 200 ms from a holding potential of  $-80$  mV with a frequency 0.2 Hz [75]. Modeling data are obtained by a series of pulses to 0 mV for 50 ms from a holding potential of  $-80$  mV with a frequency 0.04 Hz. Increase in phosphorylation level is determined as a fractional increase related to the total increase in phosphorylation of L-type  $\text{Ca}^{2+}$  channels at 150<sup>th</sup> s after application of isoproterenol. **Panel C:** Peak L-type  $\text{Ca}^{2+}$  current as a function of isoproterenol concentration. Experimental data are obtained by Kim et al. [79] (filled circles), Sako et al. [80] (unfilled circles), and Mitarai et al. [81] (filled squares). Simulation data is obtained by a voltage pulse to 0 mV from a holding potential of  $-80$  mV after a 600-second exposure to different concentrations of isoproterenol. Simulation data for the total cellular  $I_{CaL,tot},$  the caveolae-localized  $I_{CaL,cav},$  and the extracaveolae-localized  $I_{CaL,ecav}$  are shown by black, green, and red solid lines, respectively. **Panel D:** Simulated time course of the L-type  $\text{Ca}^{2+}$  currents in control (solid line), after 1000-s exposure to PP1/PP2A inhibitor Calyculin A (65% of PP1/PP2A activity inhibition, dashed line), and after 600-s exposure to 1  $\mu\text{M}$  isoproterenol (dotted line). Currents are obtained by a voltage pulses to 0 mV from a holding potential of  $-80$  mV and without  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release to account for heavy buffer conditions. Insert in **Panel D:** Same simulations performed with intact  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release. **Panel E:** Peak current-voltage (I-V) relationships for  $I_{CaL}$  in control (filled circles) and after exposure to Calyculin A (unfilled circles) and isoproterenol (filled squares). **Panel F:** Steady-state inactivation relationships for  $I_{CaL}$  in control (filled circles) and after exposure to Calyculin A (unfilled circles) and isoproterenol (filled squares). **Panel G:** Normalized maximum conductance ( $G/G_{max}$ ) for  $I_{CaL}$  as functions of voltage in control (filled circles) and after exposure to Calyculin A (unfilled circles) and isoproterenol (filled squares). In **Panels E, F, and G,** currents are obtained by the two-pulse protocols: a 500-ms depolarizing first pulse to between  $-70$  and  $+50$  mV (in 10-mV increment) is applied from a holding potential of  $-80$  mV; this is followed by a second 500-ms pulse to  $+10$  mV. Simulations are performed without  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release to account for heavy buffer conditions. doi:10.1371/journal.pone.0089113.g009

hyperpolarization shifts are also observed experimentally [73]. Therefore, our model for the  $\beta_1$ -adrenergic signaling system is able to simulate the effects of both activation of PKA and inhibition of PP1 and PP2A on the L-type  $\text{Ca}^{2+}$  current,  $I_{CaL}$ .

**Fast  $\text{Na}^+$  current module.** The channels responsible for the fast  $\text{Na}^+$  current,  $I_{Na}$ , which are encoded by Nav1.5 subunit, are found in the caveolae compartment [16,69,82]. Using both immunoblot analysis and imaging technique, Yarbrough et al. [82] provided evidence of co-localization of the fast  $\text{Na}^+$  channels and caveolin-3 in rat cardiomyocytes, suggesting their localization in the caveolae compartment. Similar data were also obtained by Shibata et al. [69] by using immunogold labeling of plasma membranes from rat cardiomyocytes, where Nav1.5 subunits were co-localized on electron microscope images with caveolin-3. In addition, Palygin et al. [83] provided evidence of the involvement of caveolin-3 in isoproterenol-induced enhancement of  $I_{Na}$  in ventricular myocytes.

Activation of the  $\beta_1$ -adrenergic signaling system with isoproterenol leads to an increase in the amplitude of  $I_{Na}$ , however, without the effects on gating properties of the channel [84,85]. Simultaneous activation of several components of the  $\beta_1$ -adrenergic signaling system with cAMP-IBMX-forskolin cocktail or with excessive application of membrane permeant analogue of cAMP, CPTcAMP (5 mM), results in additional small shift in the  $G/G_{max}$  and steady-state inactivation [86,87,88]. Experimental data of Baba et al. [86] also shows that the inhibition of protein phosphatase PP2A causes an increase in  $I_{Na}$ , and the addition of PP2A to pipette solution causes a decrease in  $I_{Na}$ , which link phosphorylation level of  $I_{Na}$  to its magnitude. Mechanism of the changes in  $I_{Na}$  was studied by Zhou et al. [88] in detail. It was shown that, in addition to channel phosphorylation, an increased number of functional fast  $\text{Na}^+$  channels in the cell membrane is due to the channel trafficking. More recent analysis of the effects of PKA on  $I_{Na}$  suggested that phosphorylation and trafficking of  $I_{Na}$  are related processes: channels' phosphorylation increases trafficking of fast  $\text{Na}^+$  channels [89].

To simulate these effects, we developed a Markov model for  $I_{Na}$ , based on the model [25,90], in a similar way as for  $I_{CaL}$ , but with some differences. We consider that the amplification of  $I_{Na}$  occurs through two processes: phosphorylation of the channels and their subsequent trafficking to the cell membrane. As the kinetics of the two processes are indistinguishable in the experiments, we use only

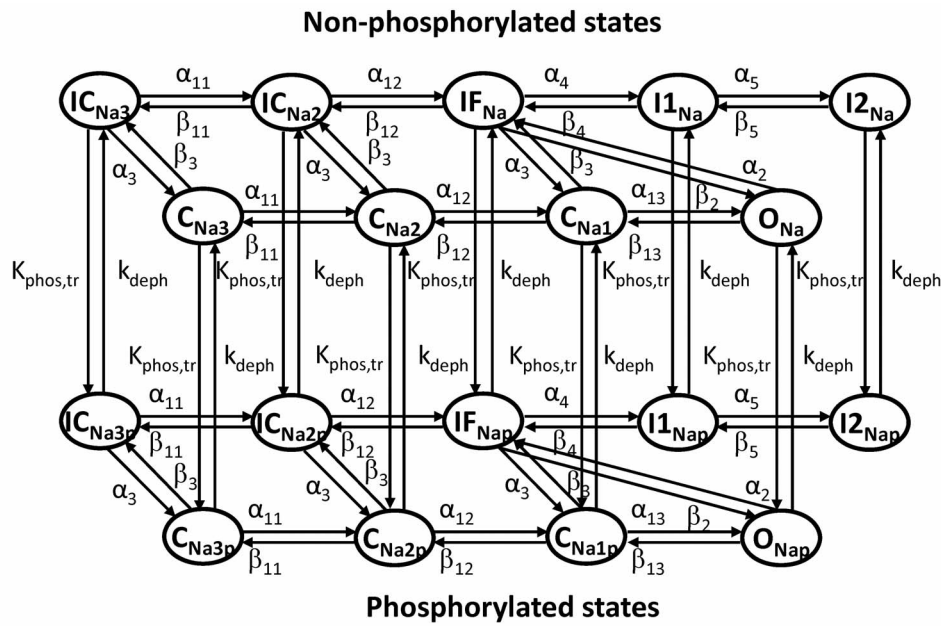
one rate constant to characterize the effect of PKA,  $k_{phos,ir}$ , which includes both channel's phosphorylation and trafficking. Two activation pathways are used, one is for non-phosphorylated channels and another is for phosphorylated-trafficked channels (Fig. 10A). Because isoproterenol does not change the gating properties of  $I_{Na}$ , we use the same rate constants for both non-phosphorylated and phosphorylated-trafficked channels. The larger conductance is used for the phosphorylated-trafficked channels (see the fast  $\text{Na}^+$  current module in Appendix S1). We consider that the fast  $\text{Na}^+$  channels are dephosphorylated by PP1 and PP2A (Fig. 10A, Appendix S1). The set of equations that describes the fast  $\text{Na}^+$  channel gating is provided in Appendix S1 ((A.180) - (A.213)).

The resulting model for the fast  $\text{Na}^+$  current was tested against the experimental data on the time course of  $I_{Na}$  activation, its dependence on the isoproterenol concentration, and voltage-clamp experiments (Fig. 10). As there is no data for mice, we used the experimental time course of the activation of  $I_{Na}$  by 0.1  $\mu\text{M}$  isoproterenol obtained from rabbit ventricular myocytes (filled circles in Fig. 10B). Figure 10B shows a good agreement between the experimental and simulated time dependences of  $I_{Na}$  amplitude upon stimulation of the  $\beta_1$ -adrenergic signaling system. A similar time course is demonstrated by the simulated fraction of phosphorylated and trafficked  $\text{Na}^+$  channels (solid line in Fig. 10B). The model also successfully reproduced the concentration dependence of an increase in  $\text{Na}^+$  channel availability at different concentrations of isoproterenol (Fig. 10C).

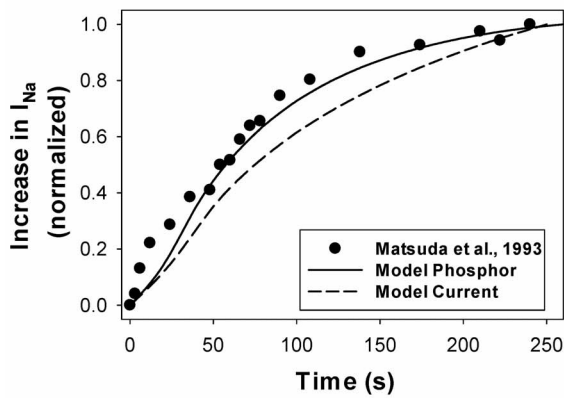
Experimental data shows an increase in the fast  $\text{Na}^+$  current amplitude upon stimulation with 0.1  $\mu\text{M}$  isoproterenol (Fig. 10D, unfilled and filled circles). A similar increase is obtained from our Markov model for  $\text{Na}^+$  channels (solid and dashed lines in Fig. 10D are for control and 0.1  $\mu\text{M}$  isoproterenol, respectively). Neither the experimental data (unfilled and filled circles in Fig. 10E) nor the simulations (solid and dashed lines in Fig. 10E) demonstrate significant changes in steady-state inactivation relationships.

**Ryanodine receptor module.** Experimental studies of ryanodine receptors in rat ventricular myocytes provided evidence of their co-localization in couplons with the L-type  $\text{Ca}^{2+}$  channels (in dyads, or subspace volume  $V_{ss}$ ) or in close proximity to those couplons [21,22,91]. Between 80 to 85% of ryanodine receptors are localized in  $V_{ss}$  and the rest are very close to dyads, which suggests their involvement in  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release [21,91].

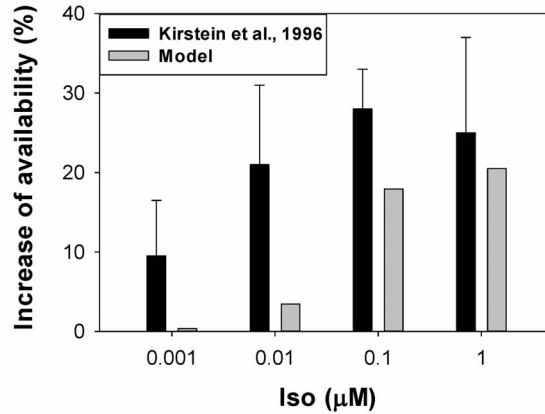
**A**



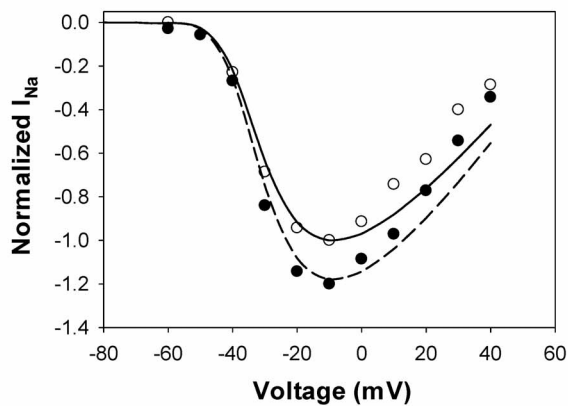
**B**



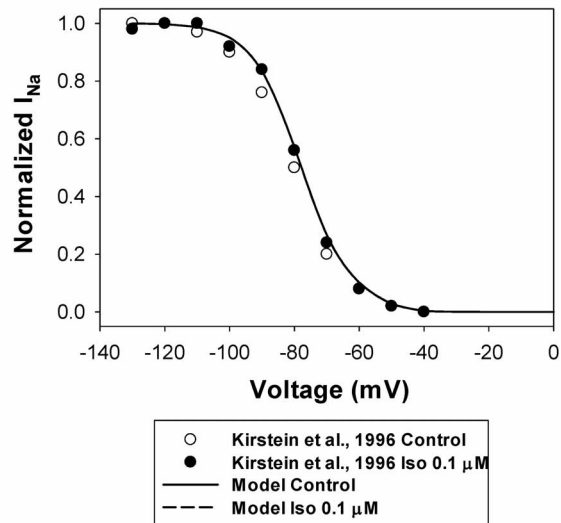
**C**



**D**



**E**



**Figure 10. The effects of  $\beta_1$ -adrenoceptor stimulation on the fast  $\text{Na}^+$  current.** **Panel A:** Markov model of the fast  $\text{Na}^+$  channel. State diagram consists of two similar sub-diagrams for non-phosphorylated (upper sub-diagram) and phosphorylated-trafficked states (lower sub-diagram).  $C_{\text{Na}1}$ ,  $C_{\text{Na}2}$ , and  $C_{\text{Na}3}$  are closed states;  $O_{\text{Na}}$  is the open state;  $I_{\text{Na}f}$ ,  $I_{\text{Na}i}$ , and  $I_{\text{Na}s}$  are the fast, intermediate, and slow inactivated states, respectively;  $IC_{\text{Na}2}$  and  $IC_{\text{Na}3}$  are closed-inactivated states;  $C_{\text{Na}1p}$ ,  $C_{\text{Na}2p}$ , and  $C_{\text{Na}3p}$  are closed phosphorylated states;  $O_{\text{Na}p}$  is the open phosphorylated state; and  $I_{\text{Na}fp}$ ,  $I_{\text{Na}ip}$ ,  $I_{\text{Na}sp}$ ,  $IC_{\text{Na}2p}$ , and  $IC_{\text{Na}3p}$  are phosphorylated inactivated states. The rate constants for activation, deactivation, inactivation, phosphorylation-trafficking, and dephosphorylation are given in Appendix S1. **Panel B:** Time course of the activation of the fast  $\text{Na}^+$  current upon application 0.1  $\mu\text{M}$  isoproterenol. Experimental data of Matsuda et al. [85] obtained for the normalized peak  $I_{\text{Na}}$  in rabbit ventricular myocytes is shown by closed circles. Data is obtained with 40-ms pulses from a holding potential of  $-100$  mV to  $-30$  mV at stimulation frequency 0.2 Hz. A solid line shows the time course of simulated data on relative  $I_{\text{Na}}$  phosphorylation upon application of 0.1  $\mu\text{M}$  isoproterenol. A dashed line shows the time course of the simulated normalized peak  $I_{\text{Na}}$  after application of 0.1  $\mu\text{M}$  isoproterenol. The simulated currents are obtained with 20-ms pulses from a holding potential of  $-140$  mV to  $-30$  mV at stimulation frequency 0.04 Hz. **Panel C:** An increase in peak  $I_{\text{Na}}$  availability upon application of different concentrations of isoproterenol (in %). Experimental data by Kirstein et al. [84] obtained from rat ventricular myocytes are shown by black bars with errors; corresponding simulation data are shown by gray bars. **Panel D:** Peak current-voltage and **Panel E:** steady-state inactivation relationships for the fast  $\text{Na}^+$  current in ventricular myocytes upon stimulation with 0.1  $\mu\text{M}$  isoproterenol. Experimental data for rats in the absence (unfilled circles) and presence (filled circles) of 0.1  $\mu\text{M}$  isoproterenol are obtained by Kirstein et al. [84] (holding potential is  $-100$  mV, conditioning pulse duration is 2,500 ms; isoproterenol data is obtained after 10 min of application). Simulated data are shown by solid (no isoproterenol) and dashed (10 min after application of 0.1  $\mu\text{M}$  isoproterenol) lines (data are obtained by two-pulse protocol, holding potential is  $-140$  mV, first pulse duration is 500 ms for voltages from  $-140$  to  $+40$  mV in 10 mV steps, second pulse duration is 50 ms at voltage  $-20$  mV). Isoproterenol increases  $I_{\text{Na}}$  availability, but does not affect gating properties.  
doi:10.1371/journal.pone.0089113.g010

Very small portions ( $\sim 3.5$ – $9.2\%$ ) of ryanodine receptors in mouse ventricular myocytes are shown to co-localize with caveolin-3, but outside of couplons, but their functional significance is unclear [35,92]. Therefore, in the model, we put ryanodine receptors in the extracaveolae compartment. The receptors are subjects of phosphorylation by PKA and dephosphorylation by PP1. The total concentration of RyRs in mouse ventricular myocytes was determined experimentally by Chu et al. [71] and is equal to 0.1993  $\mu\text{M}$ .

A Markov model for ryanodine receptor gating, which includes phosphorylation-dephosphorylation processes, is shown in Fig. 11A. As for two other substrates,  $I_{\text{CaL}}$  and  $I_{\text{Na}}$ , we developed a Markov model that consists of two populations of the channels, non-phosphorylated and phosphorylated. For non-phosphorylated channels, we employed our previously developed Markov model for RyRs, which contains two closed ( $C_1$  and  $C_2$ ) and two open ( $O_1$  and  $O_2$ ) states [25]. We added two closed-phosphorylated ( $C_{1p}$  and  $C_{2p}$ ) and two open phosphorylated ( $O_{1p}$  and  $O_{2p}$ ) states to the model and the transitions between corresponding non-phosphorylated and phosphorylated states (Fig. 11A). Because experimental data suggest slightly increased sensitivity of RyRs to cytosolic  $\text{Ca}^{2+}$  concentration [93], we sped up the forward transition rates to a greater magnitude than the backward transition rates for the phosphorylated channels (see Appendix S1). Differential equations, which describe the time behavior of the RyRs' probabilities in closed and open states, are shown in Appendix S1 (Eqs. (A.214)–(A.222)).

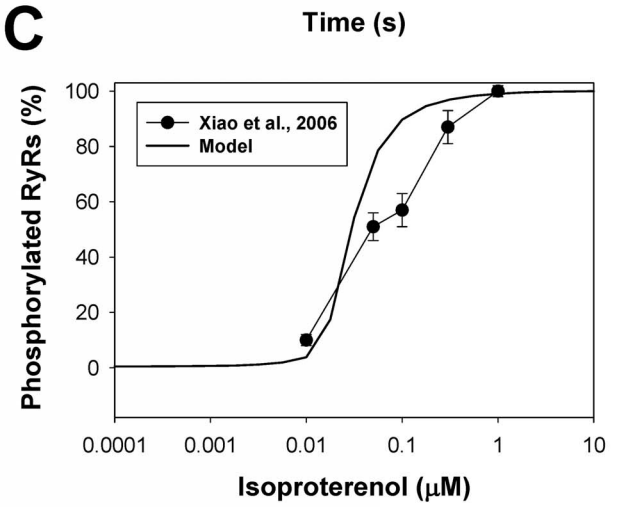
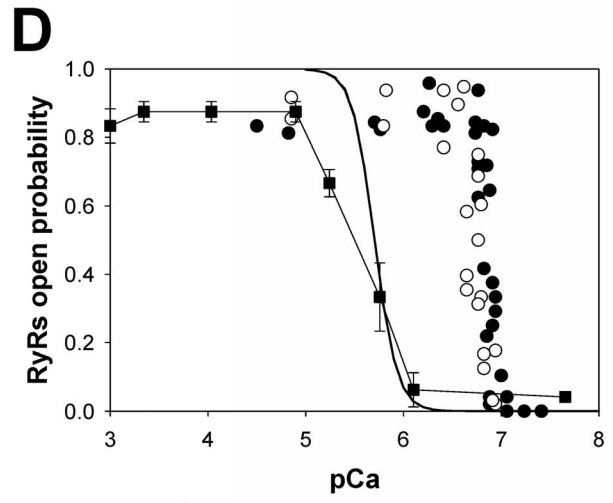
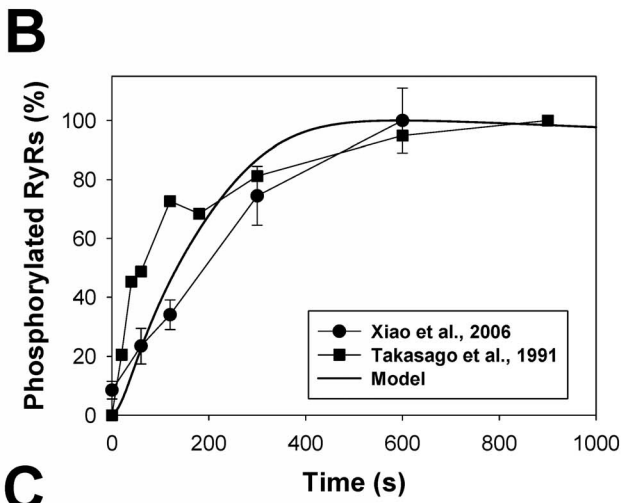
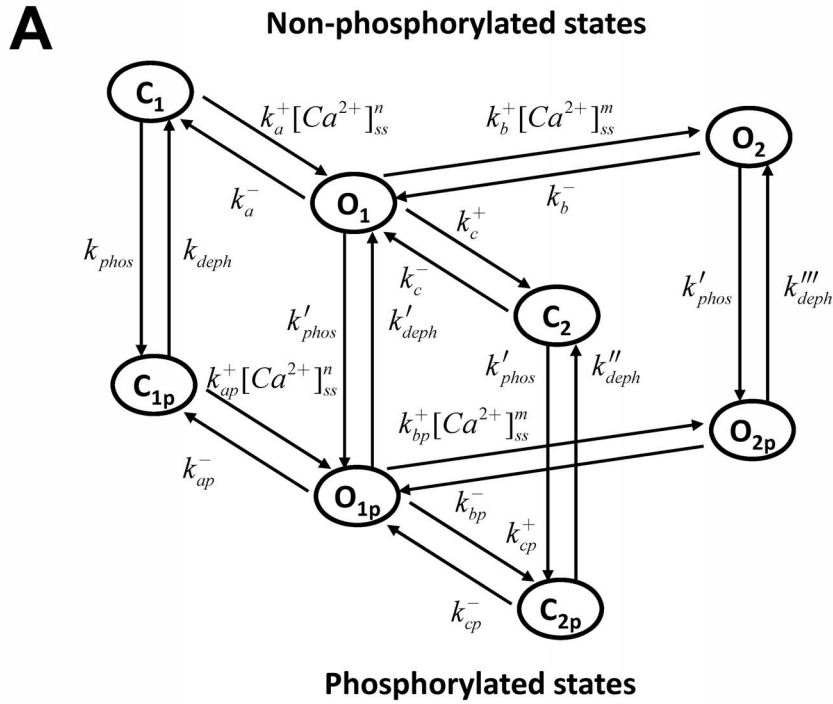
Our model successfully reproduced the time course of the ryanodine receptor phosphorylation upon stimulation of  $\beta_1$ -adrenoceptors. Figure 11B shows experimental time behavior of the relative phosphorylation level of RyRs in rat ventricular myocytes during exposure to 1  $\mu\text{M}$  isoproterenol [94]. A similar time course is demonstrated by our model (solid line in Fig. 11B) and by the experimental data which used a different technique of RyR phosphorylation (by endogenous PKA in canine ventricular myocytes upon application of  $[\gamma\text{-}^{32}\text{P}]\text{ATP}$  [95]). Figure 11C (filled circles) shows experimental data on the phosphorylation level of RyRs at different concentrations of isoproterenol [94]. Our model is able to reproduce this dependence as well (solid line in Fig. 11C).

In addition, the model simulated dependence of the RyRs open probability as a function of intracellular  $\text{Ca}^{2+}$  concentration for non-phosphorylated and phosphorylated channels (Fig. 11D). The experimental data on the effects of PKA on RyRs shows a tiny shift of the dependence of phosphorylated RyRs' opening probability towards a smaller cytosolic  $\text{Ca}^{2+}$  concentration [93].

However, such data were obtained at relatively small luminal  $\text{Ca}^{2+}$  concentrations (45 nM), which increased sensitivity of RyRs by an order of magnitude compared to normal physiological conditions (compare the data shown by filled and unfilled circles (small luminal  $\text{Ca}^{2+}$  concentrations) with the data shown by filled squares (normal physiological luminal  $\text{Ca}^{2+}$  [96])). To estimate the effects of PKA on RyRs, we simulated two dependences of RyRs opening probabilities on cytosolic  $\text{Ca}^{2+}$ : the first is obtained by stimulation of the cell with intact PKA (solid line in Fig. 11D), the second is obtained by setting  $[\text{PKA}]_{\text{tot}} = 0$   $\mu\text{M}$ . Our model shows a reasonable agreement of the  $\text{Ca}^{2+}$ -dependence of the RyRs opening probability with the experimental data [96], but virtually no change in the sensitivity of phosphorylated RyRs to cytosolic  $\text{Ca}^{2+}$  concentration. Some deviations between the experimental (filled squares) and simulated (solid line) data at relatively large cytosolic  $\text{Ca}^{2+}$  concentrations can be due to the method of estimation of the opening probabilities: in the simulations, we used the maximum values of the channel's opening probabilities, without consideration of the effects of ryanodine receptor inactivation, while in the single-channel experiments, such inactivation is always present and can potentially reduce measured opening probability.

**Phospholemman and the  $\text{Na}^+\text{-K}^+$  pump module.** Experimental data on the localization of the  $\text{Na}^+\text{-K}^+$  pump shows that  $\sim 30$ – $40\%$  of  $\alpha_1$ -subunits and  $80$ – $90\%$  of  $\beta_1$ -subunits are localized in the caveolae-rich membrane fractions [97]. Another study provided similar data on the  $\text{Na}^+\text{-K}^+$  pump and caveolin-3 co-localization, where  $\sim 70\%$  of those proteins are found in the same fractions [98]. Moreover, almost all the  $\text{Na}^+\text{-K}^+$  pump activity was found in caveolae [97,99].

In our model, the phospholemman, which regulates the  $\text{Na}^+\text{-K}^+$  pump, is the third substrate of the  $\beta_1$ -adrenergic signaling system located in the caveolae compartment. Activation of  $\beta_1$ -ARs increases the function of the  $\text{Na}^+\text{-K}^+$  pump by phosphorylation of phospholemman (PLM) through the effective change in dissociation constant  $K_{\text{m,Na}}$  [12], thereby decreasing intracellular  $[\text{Na}^+]_i$  concentration [100]. An experimental time course of a relative decrease in  $[\text{Na}^+]_i$  in mouse ventricular myocytes after application of 1  $\mu\text{M}$  isoproterenol is shown in Fig. 12A by filled circles. A corresponding simulated time course of a relative PLM phosphorylation level is shown by a solid line. An increase in the phosphorylation level of PLM decreases the  $\text{Na}^+$  half-saturation constant for the current and effectively increases the pumping rate of  $\text{Na}^+$  outside the cell. Both time dependences demonstrate similar behavior.





**Figure 11. The effects of  $\beta_1$ -adrenoceptor stimulation on ryanodine receptors. Panel A:** Markov model of ryanodine receptors. State diagram consists of two similar sub-diagrams for non-phosphorylated (upper sub-diagram) and phosphorylated states (lower sub-diagram).  $C_1$  and  $C_2$  are closed states;  $O_1$  and  $O_2$  are open states;  $C_{1p}$  and  $C_{2p}$  are closed phosphorylated states;  $O_{1p}$  and  $O_{2p}$  are open phosphorylated states. The rate constants from  $C_1$  to  $O_1$ , from  $O_1$  to  $O_2$ , from  $C_{1p}$  to  $O_{1p}$ , and from  $O_{1p}$  to  $O_{2p}$  are  $Ca^{2+}$ -dependent; and  $k_{phos}$  and  $k_{deph}$  are the phosphorylation and dephosphorylation rates, respectively (see Appendix S1). **Panel B:** Time course of the relative phosphorylation level of RyRs upon activation of the  $\beta_1$ -adrenergic signaling system. Experimental data of Xiao et al. [94] (filled circles) are obtained upon stimulation of rat ventricular myocytes with 1  $\mu$ M isoproterenol; experimental data of Takasago et al. [95] (filled squares) are obtained from canine ventricular myocytes with endogenous PKA by application of [ $\gamma$ - $^{32}$ P]ATP. Modeling data are obtained by application of 1  $\mu$ M isoproterenol. Increase in phosphorylation level is determined as a fractional increase related to the maximum increase in phosphorylation of RyRs after activation of the  $\beta_1$ -adrenergic signaling system. **Panel C:** Relative phosphorylation level of RyRs at different concentrations of isoproterenol. Experimental data of Xiao et al. [94] (filled circles) obtained upon stimulation of rat ventricular myocytes for 15 minutes. Simulation data are obtained after 10-minute exposure to different concentrations of isoproterenol. **Panel D:** Effects of PKA on opening probability of RyRs as function of cytosolic  $Ca^{2+}$  concentration. Experimental data of Xiao et al. [93] are obtained for cardiac RyRs upon application of active (filled circles) and boiled (unfilled circles) PKA at relatively small luminal  $Ca^{2+}$  of 45 nM; experimental data of Xiao et al. [96] (filled squares) for RyRs are obtained from mouse ventricular myocytes. Simulation data for mouse ventricular myocytes in the absence and presence of PKA are obtained at intracellular  $[Ca^{2+}]_i$  concentration ranged from 0.01 to 10  $\mu$ M and are shown by dashed and solid lines. Experimental data obtained at small luminal  $Ca^{2+}$  concentration shows larger sensitivity of RyRs to cytosolic  $Ca^{2+}$ . doi:10.1371/journal.pone.0089113.g011

Figure 12B shows the experimental dependence of the relative increase in  $I_{NaK}$  as a function of isoproterenol concentration obtained from guinea pig ventricular myocytes (filled circles [101]). We compared the experimental data to our simulations of a relative increase in the phosphorylation level for phospholemman (solid line in Fig. 12B). In general, simulation data has a dependence on isoproterenol concentration similar to the experimental data, except for a point at 0.01  $\mu$ M isoproterenol. Such deviation could be due to the species differences.

Finally, our model successfully reproduced the experimental behavior of intracellular  $[Na^+]_i$  concentration in mouse ventricular myocytes measured before and 10 minutes after an application of 1  $\mu$ M isoproterenol (Fig. 12C, [100]). Both the experimental and simulation data show relatively small, but significant decreases in  $[Na^+]_i$  after stimulation of the  $\beta_1$ -adrenergic signaling system.

**Ultra-rapidly activating delayed rectifier  $K^+$  current module.** The ultra-rapidly activating delayed rectifier  $K^+$  current,  $I_{Kur}$ , is the substrate of PKA in the extracaveolae compartment in cardiomyocytes [15,102].  $I_{Kur}$  is predominantly encoded by Kv1.5 channels [103]. It is also localized mostly in lipid rafts, which lack caveolin-3 [104], pointing to the extracaveolae compartment (however, see also [105,106], where localization of Kv1.5 channels is debated). Similar to the Heijman et al. model [8], we put the  $I_{Kur}$  current in the extracaveolae compartment.

Stimulation of  $\beta_1$ -ARs increases the function of  $I_{Kur}$  [107]. Figure 13A show an experimental time course of  $I_{Kur}$  activation in human atrial myocytes upon application of 1  $\mu$ M isoproterenol (solid lines with circles, [107]). We adjusted model parameters and performed simulations to fit the experimental time behavior (solid line in Fig. 13A). Our model also reproduced an increase in  $I_{Kur}$  at different concentrations of isoproterenol (Fig. 13B). The saturation of the current amplitude found experimentally is observed at isoproterenol concentrations of 0.1 to 1  $\mu$ M (solid lines with circles [108]). Similar data is obtained from simulations (solid line in Fig. 13B).

Experimental voltage dependence of the peak ultra-rapidly activating delayed rectifier  $K^+$  current in response to depolarizations in the interval from  $-40$  to  $+50$  mV for control conditions and after application of 1  $\mu$ M isoproterenol is shown in Fig. 13C [107]. As in [25], simulated data show activation of  $I_{Kur}$  at slightly more hyperpolarized potentials to offset the effects of divalent cations, which are used in the experiments to block  $I_{CaL}$ . However, both simulated and experimental data show similar increases in peak current amplitude upon stimulation of  $\beta_1$ -ARs (solid and dashed lines in Fig. 13C).

**Rapidly recovering transient outward  $K^+$  current module.** The other substrate of PKA in the extracaveolae

compartment in our model is the rapidly recovering transient outward  $K^+$  current,  $I_{Kto,f}$ .  $I_{Kto,f}$  is found in lipid rafts that lack caveolin-3 pointing to non-caveolae localization [15,69,105]. Heijman et al. [8] also placed  $I_{to1}$ , which is encoded by *Shal*-type  $K^+$  channels (Kv4.2/Kv4.3), to the extracaveolae compartment.

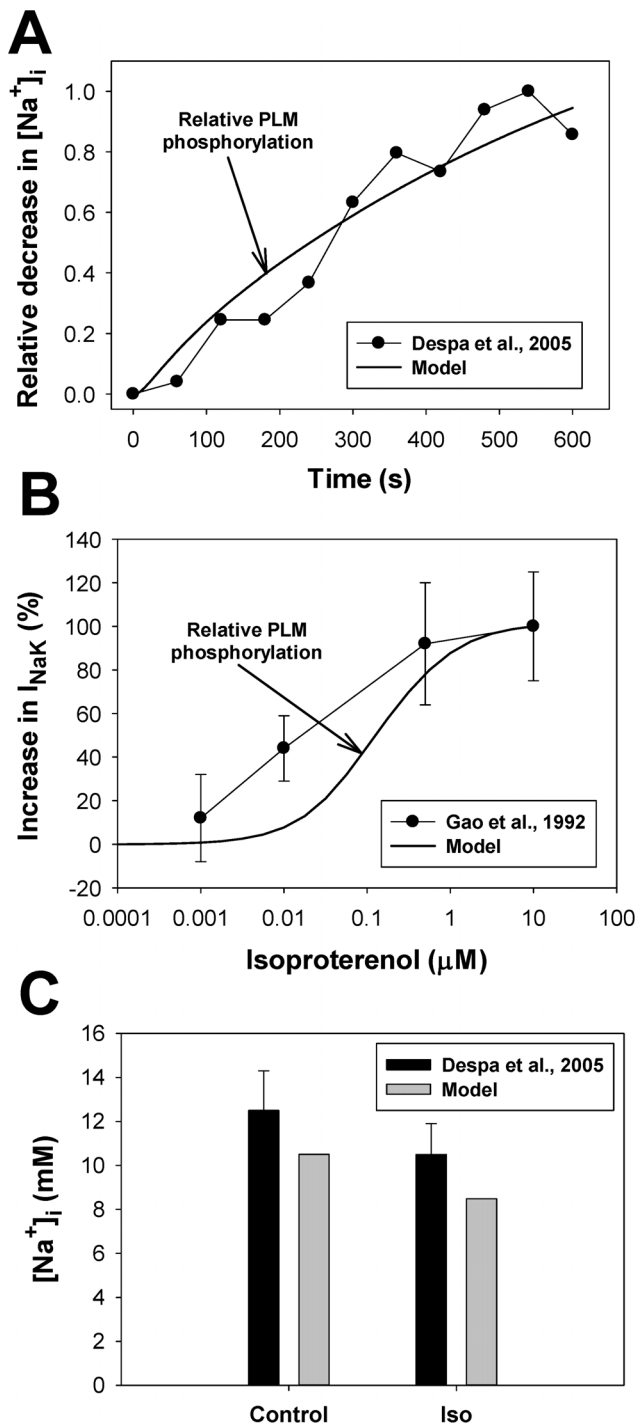
There are only a few qualitative experimental data on the effects of activation of the  $\beta_1$ -adrenergic signaling system on  $I_{Kto,f}$  in cardiac cells [109]. Experimental data of Gonzalez de la Fuente et al. [109] shows clear inhibition of  $I_{to1}$  by isoproterenol (0.1  $\mu$ M) in human left and right atrial myocytes by about 40–50%. Similar inhibition is obtained in neural cells [110] for A-type  $K^+$  current,  $I_A$ , which is also encoded by *Shal*-type  $K^+$  channels (Kv4.2), after application of 8-br-cAMP (100  $\mu$ M), and Schwann cells [111] after application of bradykinin (5  $\mu$ M), forskolin (1  $\mu$ M), or db-cAMP (10  $\mu$ M). Our simulation data shows about a two-fold decrease in peak  $I_{Kto,f}$  at saturating concentrations of isoproterenol (Fig. 13E).

Figure 13D shows experimental time courses of  $I_A$ -current inhibition by forskolin (1  $\mu$ M) or db-cAMP (10  $\mu$ M) obtained in Schwann cells [111] (filled and unfilled circles, respectively). Our simulation, shown by a solid line for the saturating concentration of isoproterenol (10  $\mu$ M), gives a reasonable agreement with the experimental data. The saturating concentration of isoproterenol was chosen in the simulation to obtain cAMP concentration in the extracaveolae compartment similar to the experimental values and maximum activation of PKA.

Simulated time courses of  $I_{Kto,f}$  in control and after application of 10  $\mu$ M isoproterenol are shown in Fig. 13E by solid and dashed lines, respectively. Calculations demonstrate about a two-fold inhibition of peak current after stimulation of  $\beta_1$ -ARs. A similar level of inhibition of  $I_A$  is obtained by activation of PKA with saturating concentrations of 8-br-cAMP (100  $\mu$ M) in neural cells [110], and  $I_{to1}$  after application of saturating concentrations of isoproterenol in human left and right atrial cells [109]. Simulations also demonstrate depolarization shifts in voltage dependences of  $G/G_{max}$  (13 mV) and steady-state inactivation (6 mV) for isoproterenol-stimulated compared to control cells (Fig. 13F), which is similar to the experimental data from [110] obtained for neural cells.

**Time-independent  $K^+$  current module.** While experimental data shows the effects of activation of the  $\beta_1$ -adrenergic signaling system on the time-independent current  $I_{K1}$ , such effects are clear only at potentials below  $-80$  mV [112,113]. Therefore, we did not include modulation of  $I_{K1}$  by  $\beta_1$ -ARs in our model.

**Phospholamban module.** Phospholamban is the first PKA substrate in the cytosolic compartment, which is included in our model [114]. Its major role is the regulation of SERCA pump activity by changing the affinity of the latter. Activation of the



**Figure 12. The effects of  $\beta_1$ -adrenoceptor stimulation on the  $Na^+K^+$  pump.** Panel A: Experimental time course of a relative decrease in the intracellular  $[Na^+]_i$  concentration (filled circles) obtained by Despa et al. [100] from mouse ventricular myocytes after application of 1  $\mu M$  isoproterenol and corresponding simulated time course of an increase in relative phosphorylation level of phospholemman obtained using our model (solid line). Panel B: Experimental data on a relative increase in  $I_{NaK}$  current (filled circles) obtained by Gao et al. [101] from guinea pig ventricular myocytes at different concentrations of isoproterenol. Corresponding simulation data with our model on a relative increase in phosphorylation of phospholemman is shown by a solid line. Panel C: Experimental (black bars with errors [100]) and simulated (gray bars) data on intracellular  $[Na^+]_i$  concentration before (control) and after 10-minutes application of 1  $\mu M$  isoproterenol (Iso). doi:10.1371/journal.pone.0089113.g012

$\beta_1$ -adrenergic signaling system leads to an increased phosphorylation of PLB by PKA, resulting in an increase in the SERCA pumping rate of  $Ca^{2+}$  from the cytosol to the SR. Dephosphorylation of PLB occurs by protein phosphatase 1 only [59,115].

Figure 14A shows experimental and simulated time courses of PLB phosphorylation (in %) after stimulation of the  $\beta_1$ -adrenergic signaling system. Experimental data were obtained from rat hearts by application of 0.5  $\mu M$  PKA catalytic subunit (unfilled squares, [116]) or 1  $\mu M$  isoproterenol (filled circles, [117]). Data of Li et al. [118] obtained from mouse ventricular myocytes with application of 1  $\mu M$  isoproterenol is shown by unfilled circles. Phosphorylation occurs rapidly, within one to two minutes of exposure to agonists. The time course is reasonably well reproduced by the model (solid line in Fig. 14A).

Relative phosphorylation levels of PLB after stimulation with different concentrations of isoproterenol are shown in Fig. 14B. Experimental data obtained from rat [116,117] and guinea pig [119] hearts and from rat ventricular myocytes [120] consistently show similar half-activation isoproterenol concentration in the range from 0.003 to 0.01  $\mu M$ . A similar dependence of PLB phosphorylation levels is obtained from the model after 2-minute exposure to different concentrations of isoproterenol (solid line in Fig. 14B).

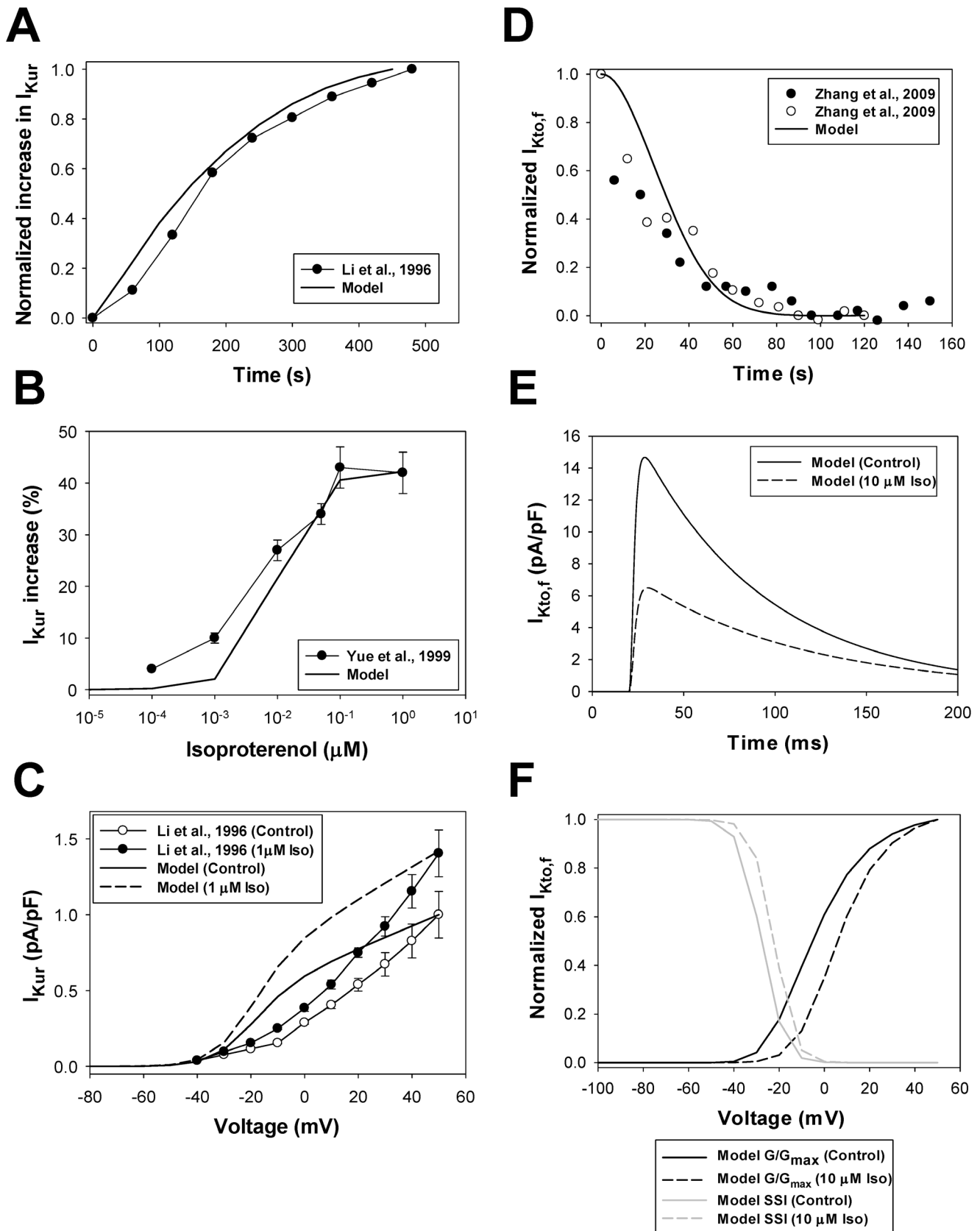
**Troponin I module.** Troponin I (inhibitory subunit of troponin complex) is the second substrate that is phosphorylated by PKA in the cytosolic compartment [27]. Phosphorylation of troponin I increases the  $Ca^{2+}$  unbinding rate by 50% [121], thereby decreasing the corresponding dissociation constant. Dephosphorylation of troponin I occurs by protein phosphatase 2A [61,115].

Figure 14C shows experimental and simulated data of the time course of the relative phosphorylation level of troponin I for mouse ventricular myocytes. Experimental data were obtained by Li et al. [118] upon stimulation of cardiac cells with 1  $\mu M$  isoproterenol. Both experimental and simulated data demonstrate a significant phosphorylation level of TnI without stimulation of the  $\beta_1$ -adrenergic signaling system. Upon application of isoproterenol, both experimental data and simulations show saturating TnI phosphorylation levels within 2 minutes of stimulation (Fig. 14C).

Dependence of the relative phosphorylation level of TnI as a function of isoproterenol concentration is shown in Fig. 14D. Both our simulations and experimental data obtained by Sulakhe and Vo [120] show a significant phosphorylation level of TnI at very low concentrations of isoproterenol. Data also demonstrates that 0.1  $\mu M$  isoproterenol causes almost complete TnI phosphorylation.

### Method of Simulation

The resulting model contains 141 ordinary differential equations solved by a fourth-order Runge-Kutta method, with different time steps. A relatively small time step of 0.000002 ms is used during the 10 milliseconds after the initiation of the stimulus current; the rest of the time, the time step is 0.0001 ms. Such small time steps are mainly determined by the very fast activation time constants of ryanodine receptors [25,122]. For simulation of the cellular behavior without electrical stimulation the time step of 0.1 ms is used. The model is implemented as a program code in FORTRAN 90, which runs on a single processor under SUSE Linux 11 on a Dell Precision Workstation T3500 with six-core Intel Xeon CPU W3670 (3.2 GHz, 12 GB RAM). Simulation of one second of the activity of an electrically stimulated cell runs approximately 3 minutes on this workstation. All model equations, model parameters, and initial conditions are given in Appendix S1. The model is developed for a room temperature of 25°C ( $T = 298^{\circ}K$ ). Steady-state initial conditions were obtained by



**Figure 13. The effects of  $\beta_1$ -adrenoceptor stimulation on  $I_{Kur}$  and  $I_{Kto,f}$ .** Panel A: Experimental time course of the relative increase in the ultra-rapidly activating delayed-rectifier  $K^+$  current  $I_{Kur}$  obtained by Li et al. [107] from human atrial myocytes after application of  $1\mu\text{M}$  isoproterenol (line with filled circles) and corresponding simulated time course of an increase in  $I_{Kur}$  obtained with our model (solid line). Simulation data is

obtained with 200-ms pulses from a holding potential of  $-100$  mV to  $+40$  mV at stimulation frequency  $0.02$  Hz. **Panel B:** Experimental data on a relative increase in  $I_{Kur}$  current (filled circles) obtained by Yue et al. [108] from canine atrial myocytes at different concentrations of isoproterenol. Corresponding simulation data with our model on relative increase in  $I_{Kur}$  are shown by a solid line. Simulation data is obtained with 4.5-s pulses from a holding potential of  $-90$  mV to  $0$  mV after 800-s exposure to different concentrations of isoproterenol. **Panel C:** Experimental (human atrial myocytes [107], solid lines with circles) and simulated (solid and dashed lines) data on current-voltage relationships for  $I_{Kur}$  current. Experimental data for control conditions and those obtained after application of  $1$   $\mu$ M isoproterenol are shown by unfilled and filled circles, respectively. Simulated data for control conditions are shown by a solid line, and  $1$   $\mu$ M isoproterenol simulations are shown by a dashed line. Simulated currents are obtained by 4.5-s depolarizing pulses to between  $-80$  and  $+50$  mV (in  $10$ -mV increment) from a holding potential of  $-90$  mV. **Panel D:** Experimental time course of the relative decrease in the rapidly recovering transient outward  $K^+$  current  $I_{K_{to,f}}$  obtained by Zhang et al. [111] from mouse Schwann cells after application of  $1$   $\mu$ M forskolin (filled circles) or  $10$   $\mu$ M db-cAMP (unfilled circles), and corresponding simulated time course of a relative decrease in  $I_{K_{to,f}}$  phosphorylation obtained with our model after stimulation with  $10$   $\mu$ M isoproterenol (solid line). **Panel E:** Simulated time course of  $I_{K_{to,f}}$  traces obtained by depolarization pulses to  $-5$  mV from a holding potential of  $-100$  mV for control (solid line) and after stimulation with  $10$   $\mu$ M isoproterenol (dashed line). **Panel F:** Simulated data for  $G/G_{max}$  (black lines) and steady-state inactivation relationships (gray lines) obtained for  $I_{K_{to,f}}$  with two-pulse protocol (P1 stimuli from  $-100$  to  $+50$  mV in  $10$  mV intervals for  $500$  ms, following P2 pulse to  $+50$  mV for  $500$  ms; holding potential is  $-100$  mV) in control (solid lines) and after application of  $10$   $\mu$ M isoproterenol (dashed lines).  
doi:10.1371/journal.pone.0089113.g013

running the model equations without electrical stimulations until changes in each variable did not exceed  $0.01\%$ . To generate action potentials, a stimulus current,  $I_{stim}$ , was applied ( $I_{stim} = 80$  pA/pF,  $\tau_{stim} = 1$  ms) with the frequencies from  $1$  to  $5$  Hz (electrical stimulation). Voltage-clamp protocols for ionic currents are described in corresponding figure legends.

## Results

In this paper, our model for action potential and  $Ca^{2+}$  dynamics in an apical mouse cardiac cell [25,26] was extended to include a  $\beta_1$ -adrenergic signaling system by using, in considerable part, the methodology from the previously published models [8,10,11,12,13]. Unlike models [10,11,12], our model represents a compartmentalized  $\beta_1$ -adrenergic signaling system. While the model of Hejman et al. [8] also includes a compartmentalized  $\beta_1$ -adrenergic signaling system, it is developed for larger species (dog) and is verified with a different set of experimental data. In particular, our model differs from the Hejman et al. model [8] in the following: 1) our model was verified in significant part by the experimental data from mice; 2) the model was developed for a different species (mouse) and includes a significantly different set of ionic currents; 3) the model considers non-zero phosphorylation levels of the protein kinase A substrates before activation of the  $\beta_1$ -adrenergic signaling system; 4) the model includes additional modulation of adenylyl cyclases by  $\beta\gamma$ -subunits of stimulatory G-protein,  $G_s$ ; 5) the model data is compared in significant part with both absolute and relative magnitudes of the activities of major signaling molecules of the  $\beta_1$ -adrenergic signaling system; 6) the model includes two subpopulations of the L-type  $Ca^{2+}$  channels located both in the caveolae and extracaveolae compartments; 7) ryanodine receptors are localized in the extracaveolae compartment. Our model also differs from the recently published Yang and Saucerman model [12] for mouse ventricular myocytes in the following: 1) compartmentalization of  $\beta_1$ -adrenergic signaling system; 2) inclusion of different types of adenylyl cyclases (AC4–7) and phosphodiesterases (PDE2–4), their compartmentalization and specific regulation by drugs (e.g., rolipram, Ro 20–1724, cilostamide, milrione); 3) multicompartmental distribution of protein kinase A targets and the possibility of their separate regulation by drugs; 4) the effects of  $\beta_1$ -adrenergic signaling system not only on  $Ca^{2+}$  dynamics, but also on action potential.

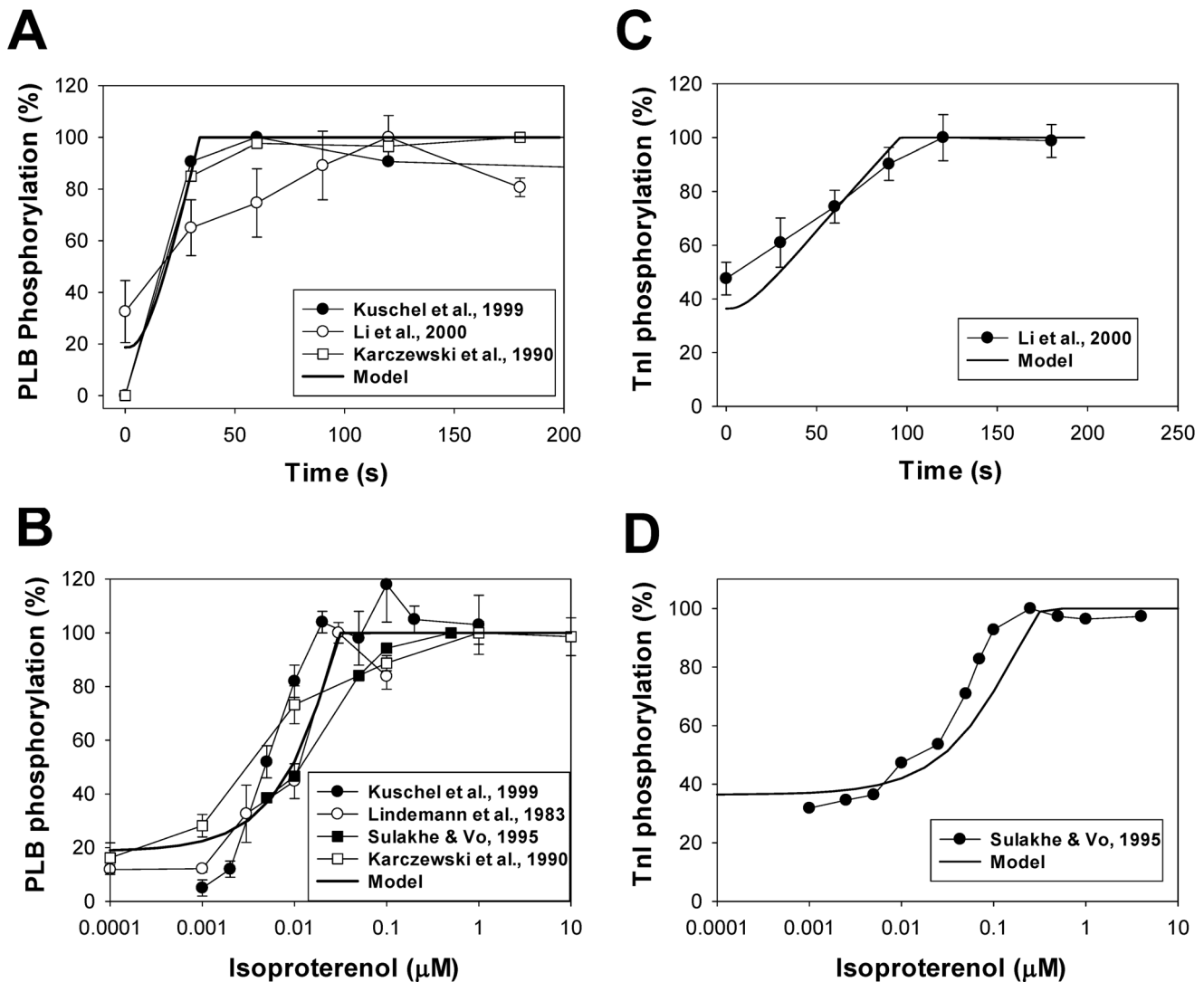
### cAMP Dynamics During Activation of $\beta_1$ -adrenergic Signaling System: the Effects of Phosphodiesterases

First, we investigated the behavior of cAMP and PKA catalytic subunit concentrations in different cellular compartments in response to the activation of the  $\beta_1$ -adrenergic signaling system

with isoproterenol. In non-stimulated cells, cAMP concentrations in caveolae, extracaveolae, and cytosol are equal to  $0.2534$   $\mu$ M,  $0.5079$   $\mu$ M, and  $0.4078$   $\mu$ M, respectively. Such steady state concentrations are determined by the balance between cAMP production by adenylyl cyclases, cAMP degradation by phosphodiesterases, and cAMP fluxes between the compartments. The steady-state concentrations of cAMP were obtained by running the model equations without electrical stimulations until changes in each variable did not exceed  $0.01\%$ . The steady-state distribution of cAMP concentrations are qualitatively similar to the values obtained by Iancu et al. [13] and Hejman et al. [8]. Iancu et al. [13] data gives  $0.1$   $\mu$ M and  $1$   $\mu$ M of caveolar and cellular cAMP concentrations; Hejman et al. [8] data shows  $0.3471$   $\mu$ M,  $9.6236$   $\mu$ M, and  $0.47408$   $\mu$ M of cAMP in the caveolae, extracaveolae, and cytosolic compartments, respectively. All simulated cellular cAMP concentrations are close to the resting cellular cAMP concentrations ( $\sim 0.5$ – $1$   $\mu$ M) obtained experimentally [52,53].

Figure 15A shows the simulated time courses of cAMP concentrations in different subcellular compartments in response to  $1$   $\mu$ M isoproterenol. All cAMP transients show relatively fast rising (time-to peak is  $35$ – $70$  s) and initial decaying phases due to the activation of ACs and PDEs (Fig. 15C), and relatively slow decay due to desensitization of  $\beta_1$ -ARs. The fastest cAMP transient is observed in the caveolae compartment because of the larger relative activities of ACs and PDEs in this compartment (see Appendix S1). In caveolae, cAMP also decays to the smaller quasi-steady-state values during desensitization of  $\beta_1$ -ARs. In the extracaveolae compartment, cAMP rises and decays somewhat slower than in the caveolae compartment and approaches the largest quasi-steady-state values at later times. cAMP transient in the cytosolic compartment has the largest time-to-peak value and the largest amplitude. It predominantly determines the behavior of cAMP in the cardiac cell (thick solid line). Note that the cellular cAMP concentration transient has a somewhat smaller amplitude due to its normalization to the whole cell volume  $V^{cell}$ .

Figures 15C and 15D demonstrate major factors that affect cAMP transient development. cAMP increases upon relatively fast activation of adenylyl cyclases by the alpha subunit of the stimulatory G protein ( $G_{s\alpha}$ ) in all subcellular compartments (time-to-peak is  $\sim 10$  s). This process is accompanied by activation of phosphodiesterases, with some delay, due to the rising cAMP concentration and phosphorylation of PDEs by catalytic subunits of PKA. The interaction between ACs and PDEs reaches quasi-steady-state by  $\sim 200$  s, when their activities become close to each other. The slower part of cAMP transient is determined by the desensitization of  $\beta_1$ -ARs when the concentration of  $G_{s\alpha}$  decreases due to its smaller production and faster re-association with  $G_{s\beta\gamma}$ . In addition to the interaction of ACs and PDEs,



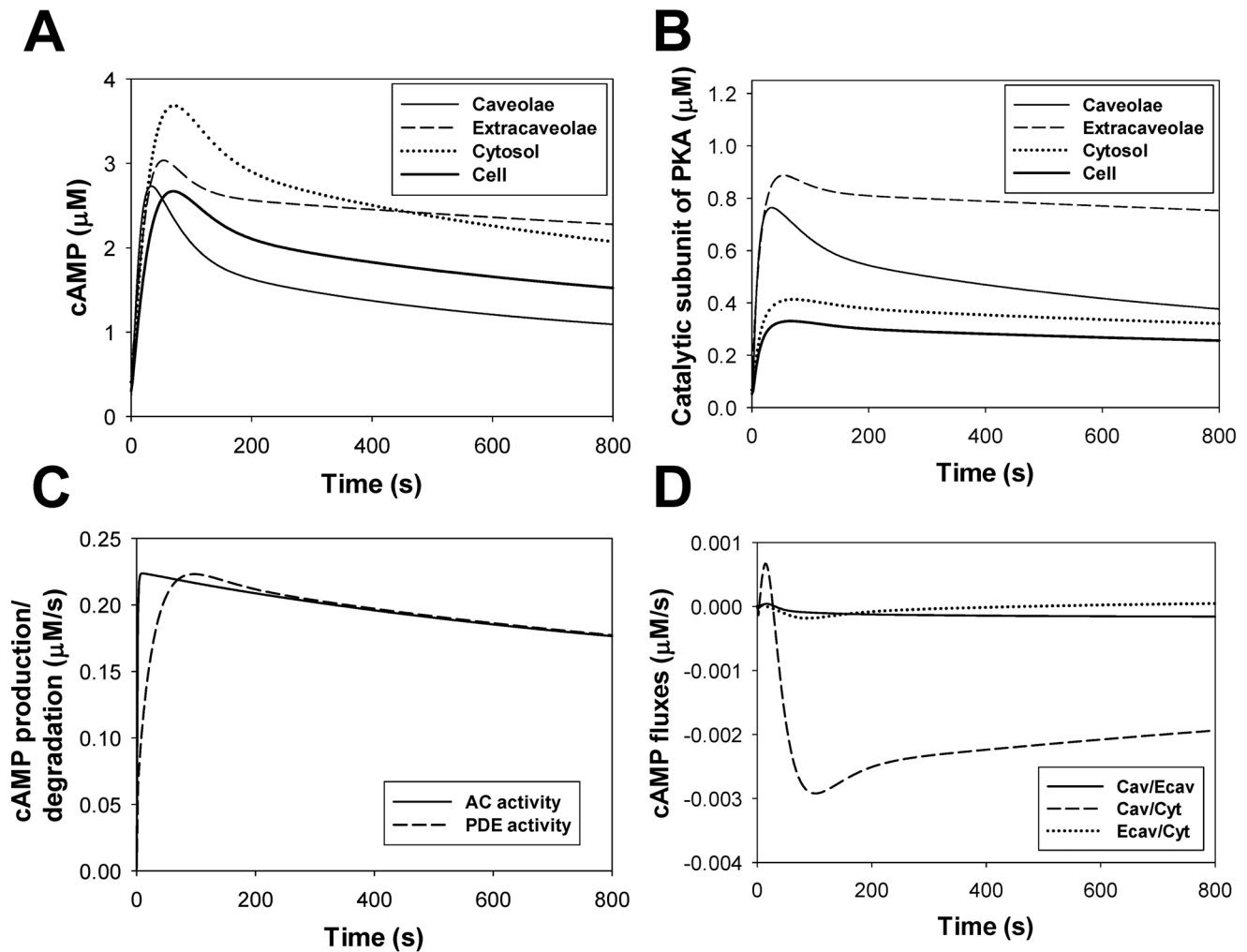
**Figure 14. The effects of  $\beta_1$ -adrenoceptor stimulation on phospholamban and troponin I.** **Panel A:** Experimental time courses of the phospholamban phosphorylation (in %) obtained from rat hearts [116,117] and mouse ventricular myocytes [118]. Data Karczewski et al. [116] are obtained with application of 0.5  $\mu$ M PKA catalytic subunit; data Kuschel et al. [117] and Li et al. [118] are obtained with application of 1  $\mu$ M isoproterenol. Simulated time course of PLB phosphorylation is shown by a solid line. **Panel B:** PLB phosphorylation (in %) as functions of isoproterenol concentration. Experimental data from rat hearts [116,117] were obtained after 2-minute exposure to isoproterenol; data from guinea pig hearts [119] were obtained after 1-minute exposure to isoproterenol; and data from rat ventricular myocytes [120] were obtained after 3-minute exposure to isoproterenol. Simulated data after 2-minute exposure to different concentrations of isoproterenol is shown by a solid line. **Panel C:** Experimental time courses of the troponin I phosphorylation (in %) obtained from mouse ventricular myocytes [118] after application of 1  $\mu$ M isoproterenol. Simulated time course of troponin I phosphorylation is shown by a solid line. **Panel D:** Troponin I phosphorylation (in %) as functions of isoproterenol concentration. Experimental data from rat ventricular myocytes [120] were obtained after 3-minute exposure to isoproterenol. Simulated data after 2-minute exposure to different concentrations of isoproterenol is shown by a solid line.  
doi:10.1371/journal.pone.0089113.g014

cAMP fluxes between the subcellular compartments contribute to cAMP transients (Fig. 15D). At early times, up to  $\sim 30$  s, the largest flux is from the caveolae to the cytosolic compartment, which is determined by the largest rising rate of cAMP in caveolae. Then this flux changes direction, and a significant amount of cAMP flows from cytosol to caveolae (dashed line in Fig. 15D). Smaller fluxes, from extracaveolae to caveolae and from cytosol to extracaveolae, are also observed during this stage of activation of  $\beta_1$ -ARs.

In our model, in contrast to cAMP, PKA does not move between the compartments. Its activation is determined by the type of PKA (PKAI or PKAII) and the level of cAMP in each

compartment (Fig. 15B). Concentrations of catalytic subunits of PKA decay relatively slowly in extracaveolae and cytosolic compartments (dashed and dotted lines in Fig. 15B, respectively) compared to those in caveolae compartment (thin solid line in Fig. 15B), despite the relatively fast decay of cAMP concentrations in both caveolae and cytosol (Fig. 15A). Such relatively fast return of cAMP and PKA concentrations to their resting values in caveolae points to an important role of this compartment in the fast cAMP-mediated signal transduction within the  $\beta_1$ -adrenergic signaling system.

In addition to control conditions, we also simulated the effects of PDE3 and PDE4 inhibition on cAMP dynamics (Fig. 16). As there

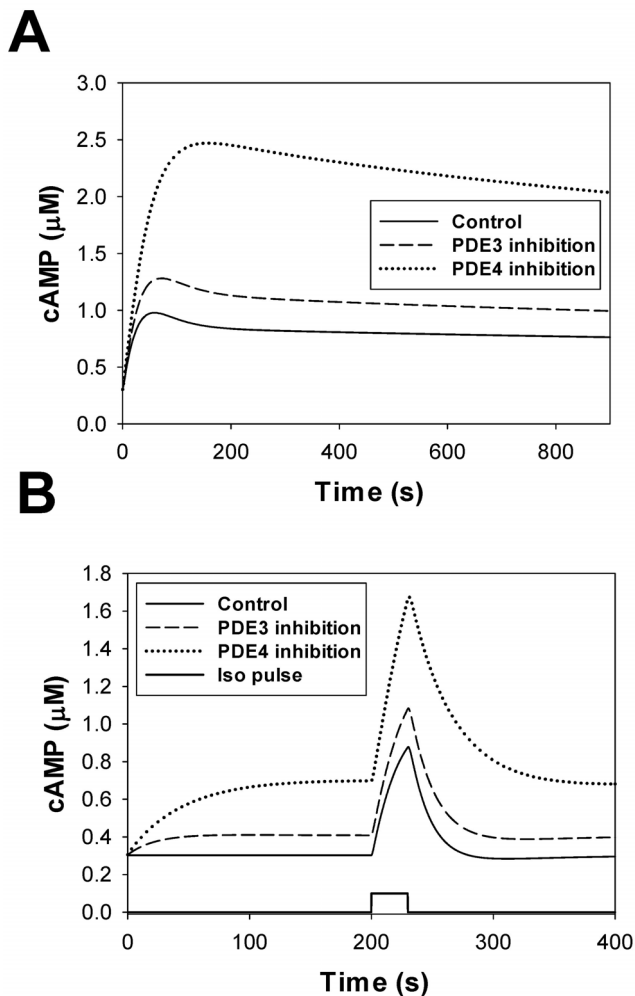


**Figure 15. The effects of  $\beta_1$ -adrenoceptor stimulation on the dynamics of cAMP and PKA.** **Panel A:** Simulated time courses of cAMP concentrations in caveolae (thin solid line), extracaveolae (dashed line), and cytosolic compartments (dotted line), and in the whole cell volume (bold solid line) after application of 1  $\mu$ M isoproterenol. **Panel B:** Simulated time courses of PKA catalytic subunit concentrations in caveolae (thin solid line), extracaveolae (dashed line), and cytosolic compartments (dotted line), and in the whole cell volume (bold solid line) after application of 1  $\mu$ M isoproterenol. **Panel C:** Simulated time courses of cAMP production rate by adenylyl cyclases (solid line) and cAMP degradation rate by phosphodiesterases (dashed line) after application of 1  $\mu$ M isoproterenol. **Panel D:** Simulated time course of cAMP fluxes between caveolae and extracaveolae (solid line), and extracaveolae and cytosol (dotted line), and caveolae and cytosol (dashed line) after application of 1  $\mu$ M isoproterenol. Fluxes are normalized to the cell volume  $V^{cell}$ . doi:10.1371/journal.pone.0089113.g015

is no detailed experimental data on cAMP dynamics during PDE inhibition in mouse ventricular myocytes, we compared qualitatively the simulated cellular response to the data obtained for rats [123]. The data for rats shows that the selective inhibition of PDE3 by cilostamide has significantly smaller effects on cAMP transient than the selective inhibition of PDE4 by Ro 20-1724. We simulated two different methods of cAMP transient production during inhibition of PDE3 or PDE4: with continuous and pulsed application of 0.1  $\mu$ M isoproterenol. Figure 16A shows that continuous application of isoproterenol from  $t=0$  s with simultaneous selective inhibition of PDE3 (90% inhibition) leads to an increase in peak cAMP transient by about 30%. In contrast, simultaneous application of isoproterenol and selective inhibition of PDE4 (90% inhibition) increases peak cAMP value by about ~150%. This result points to the primary role of PDE4 in cAMP degradation compared to PDE3. Similar results were obtained experimentally in rats [123,124]. It needs to be determined

experimentally whether such predicted effect will be observed in mouse ventricular myocytes as well.

In another set of simulations, the cells were first affected by the selective inhibitor of PDE3 (or PDE4), and then a pulse of 0.1  $\mu$ M isoproterenol was applied at  $t=200$  s for 30 s (thick solid line in Fig. 16B). In the time interval from 0 to 200 s, the selective inhibition of PDE3 or PDE4 (both by 90%) increases steady-state cellular cAMP concentrations by ~35% and ~130% (Fig. 16B). Pulsed application of isoproterenol produces relatively short cAMP transients, which decay to the pre-pulse quasi-steady-state levels. When PDE3 is selectively inhibited, cAMP transient amplitude is equal to 0.6754  $\mu$ M, which is ~17% larger than the cAMP transient in control (0.5763  $\mu$ M). Selective inhibition of PDE4 results in the larger cAMP transient of 0.9780  $\mu$ M, or ~69.7% larger than in control. Experimental data with pulsed application of isoproterenol and selective inhibition of PDE3 and PDE4 obtained from rat ventricular myocytes show qualitatively similar



**Figure 16. The effects of PDE3 and PDE4 inhibition on cAMP dynamics upon activation of  $\beta_1$ -adrenergic receptors. Panel A:** Simulated time courses of cellular cAMP concentrations for control conditions (solid line), upon inhibition of PDE3 (dashed line), and upon inhibition of PDE4 (dotted line) after sustained application of 0.1  $\mu\text{M}$  isoproterenol at time moment  $t=0$  s. Activities of PDE3 or PDE4 are inhibited by 90% to simulate the effects of corresponding selective inhibitors, cilostamide or milrine for PDE3, or rolipam or Ro 20-1724 for PDE4. **Panel B:** Simulated time courses of cellular cAMP concentrations for control conditions (solid line), upon inhibition of PDE3 (dashed line), and upon inhibition of PDE4 (dotted line) after pulsed application of 0.1  $\mu\text{M}$  isoproterenol at time moment  $t=200$  s for 30 s (thick solid line). The degrees of inhibition of PDE3 and PDE4 are the same as in Panel A.  
doi:10.1371/journal.pone.0089113.g016

behavior [123]. Further experiments are necessary to determine whether similar effects can be observed in mice.

### The Effects of Activation of the $\beta_1$ -adrenergic Signaling System on Mouse Action Potential

Experimental data obtained from mouse ventricular myocytes shows that the activation of the  $\beta_1$ -adrenergic signaling system affects action potential shape and duration [75,125,126]. To simulate these effects, we simulated the model cell with current pulses ( $I_{\text{stim}} = 80$  pA/pF,  $\tau_{\text{stim}} = 1.0$  ms) at frequencies 1 and 5 Hz for 300 s without and with application of 1  $\mu\text{M}$  isoproterenol. Figure 17A shows corresponding action potentials obtained by 1 Hz stimulation. Simulated data shows that isoproterenol

prolongs mouse action potential at different degrees of repolarization. Table 1 shows the comparison of the simulated prolongations of the action potentials with the experimental data. For example,  $\text{APD}_{50}$  and  $\text{APD}_{90}$  are prolonged by 21.67% and 14.90%, respectively. The simulated data for  $\text{APD}_{50}$  prolongation is close to the corresponding experimental data,  $13.5 \pm 4\%$  [126] and 18% [125] prolongation, but somewhat smaller than 48% prolongation obtained by Wang et al. [75]. In addition, the simulated data for  $\text{APD}_{90}$  prolongation is within the experimental data variation ( $5 \pm 7\%$  [126], 9% [125], and 51% [75]).

It is remarkable that such relatively small AP prolongation due to activation of  $\beta_1$ -ARs is accompanied by significant changes in underlying ionic currents (Fig. 17). Simulations elucidate the mechanism of this prolongation. The four major currents are responsible for the changes in AP shape at an early stage of repolarization. The fast  $\text{Na}^+$  current,  $I_{\text{Na}}$ , changes only slightly, which leads to a small increase in AP amplitude (from 114.3 mV in control to 117.8 mV after Iso). The L-type  $\text{Ca}^{2+}$  current,  $I_{\text{CaL}}$ , increases almost twice upon stimulation of  $\beta_1$ -ARs, and promotes AP prolongation. There is also a decrease in the amplitude of the rapidly recovering transient outward  $\text{K}^+$  current,  $I_{\text{Kto}}$ , which also contributes to AP prolongation. An increase in the amplitude of the ultrarapidly activating  $\text{K}^+$  current,  $I_{\text{Kur}}$ , is the major opposing effect to AP prolongation, resulting in a relatively small total effect. At 90% of repolarization, four other, relatively small currents contribute to repolarization: the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger current,  $I_{\text{NaCa}}$ , the time-independent  $\text{K}^+$  current,  $I_{\text{K1}}$ , the  $\text{Na}^+/\text{K}^+$  pump,  $I_{\text{NaK}}$ , and the  $\text{Na}^+$  background current,  $I_{\text{Nab}}$ . (Fig. 17, D and E). Significant increase in the magnitude of  $I_{\text{NaCa}}$  current upon application of isoproterenol (Fig. 17E) is one of the additional factors that cause action potential prolongation at 90% repolarization.

Simulation data obtained at stimulation frequency 5 Hz (Fig. 17, F–J) shows very similar behavior to the data for 1 Hz. The only

**Table 1. Simulated and experimental prolongations (in %) of the action potentials in mouse ventricular myocytes at different repolarizations and stimulation frequencies (1  $\mu\text{M}$  Iso).**

	$\text{APD}_{25\%}$ ms	$\text{APD}_{50\%}$ ms	$\text{APD}_{75\%}$ ms	$\text{APD}_{90\%}$ ms
Experimental values				
Wu et al. [126] *		$13.5 \pm 4$		$5 \pm 7$
Tong et al. [125] **		18		9
Tong et al. [125] ***		38		28
Wang et al. [75] ****		48		51
Simulated values (this paper)				
1 Hz	7.65	21.67	19.10	14.90
2 Hz	8.09	22.58	17.20	15.95
3 Hz	9.14	24.76	18.77	16.73
4 Hz	9.04	26.09	18.04	13.16
5 Hz	8.33	27.27	17.00	10.37

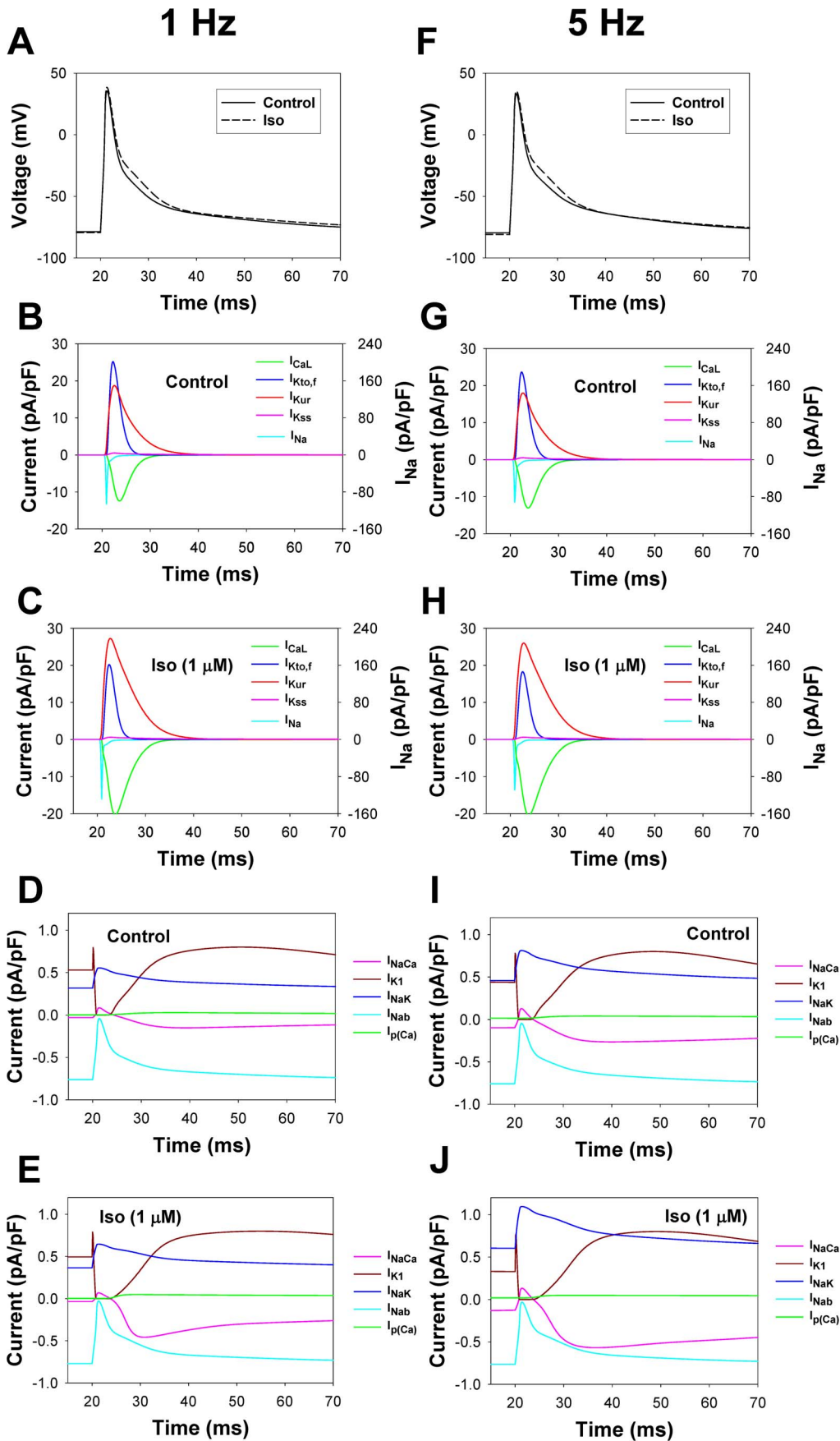
\* Experimental data are obtained at 0.5 Hz stimulation and 2  $\mu\text{M}$  isoproterenol.

\*\* Experimental data are obtained at 2 Hz stimulation.

\*\*\* Experimental data are obtained at 4 Hz stimulation.

\*\*\*\* Experimental data are obtained at 1 Hz stimulation.

doi:10.1371/journal.pone.0089113.t001





**Figure 17. Simulated action potentials and underlying ionic currents of the isolated ventricular cell model.** Simulated action potentials and underlying ionic currents are shown for control conditions and after application of 1  $\mu\text{M}$  isoproterenol at two pacing frequencies 1 Hz (**Panels A–E**) and 5 Hz (**Panels F–J**) ( $I_{\text{stim}} = 80 \text{ pA/pF}$ ,  $\tau_{\text{stim}} = 1.0 \text{ ms}$ ). **Panels A and F:** Simulated action potentials for control conditions (solid line) and after isoproterenol application (dashed line). **Panels B, D, G, and I:** Currents underlying the AP for control condition. **Panel C, E, H, and J:** Currents underlying the AP after isoproterenol application. The scales for the relatively large fast  $\text{Na}^+$  current,  $I_{\text{Na}}$ , are given on the right axis in **Panels B, C, G and H**. APs and ionic currents are shown after 300 s stimulation. In **Panels A, C, E, F, H, and J** 1  $\mu\text{M}$  isoproterenol is applied at time  $t = 0 \text{ s}$ . doi:10.1371/journal.pone.0089113.g017

significant change is in the peak amplitudes of the fast  $\text{Na}^+$  current,  $I_{\text{Na}}$ , which are decreased during stimulation with 5 Hz. A smaller decrease is observed for  $\text{K}^+$  currents  $I_{\text{Kto,f}}$  and  $I_{\text{Kur}}$  at 5-Hz stimulations. Simulation of application of 1  $\mu\text{M}$  isoproterenol at 5 Hz stimulation prolongs  $\text{APD}_{50}$  and  $\text{APD}_{90}$  by 27.27% and 10.37%, respectively (Table 1). These prolongations are compared to the experimental data of Tong et al. [125] obtained at 4 Hz stimulation (38% and 28% prolongation for  $\text{APD}_{50}$  and  $\text{APD}_{90}$ , respectively). Simulation data shows a correct trend of  $\text{APD}_{50}$  prolongation, which increases with stimulation frequency. However, simulated prolongation of  $\text{APD}_{90}$  at 5 Hz-stimulation shows somewhat smaller magnitude compared to 4 Hz-data of Tong et al. [125].

We have also simulated the effects of isoproterenol on action potential durations (APDs) at the frequencies ranged from 1 to 5 Hz. Simulation data shows relatively small increase in APDs at different levels of repolarization with stimulation frequency. For example, without isoproterenol,  $\text{APD}_{50}$  changes from 3.0 to 3.3 ms and  $\text{APD}_{90}$  changes from 25.5 to 27.0 ms when stimulation frequency increases from 1 to 5 Hz. Upon exposure to isoproterenol,  $\text{APD}_{50}$  increases from 3.65 to 4.2 ms and  $\text{APD}_{90}$  ranges from 29.3 to 30.7 ms during the same increase in stimulation frequency. Prolongation of cardiac action potential durations upon application of isoproterenol is consistently observed experimentally in mouse ventricular myocytes [75,125,126] (Table 1).

### The Effects of Activation of the $\beta_1$ -adrenergic Signaling System on $\text{Ca}^{2+}$ Dynamics

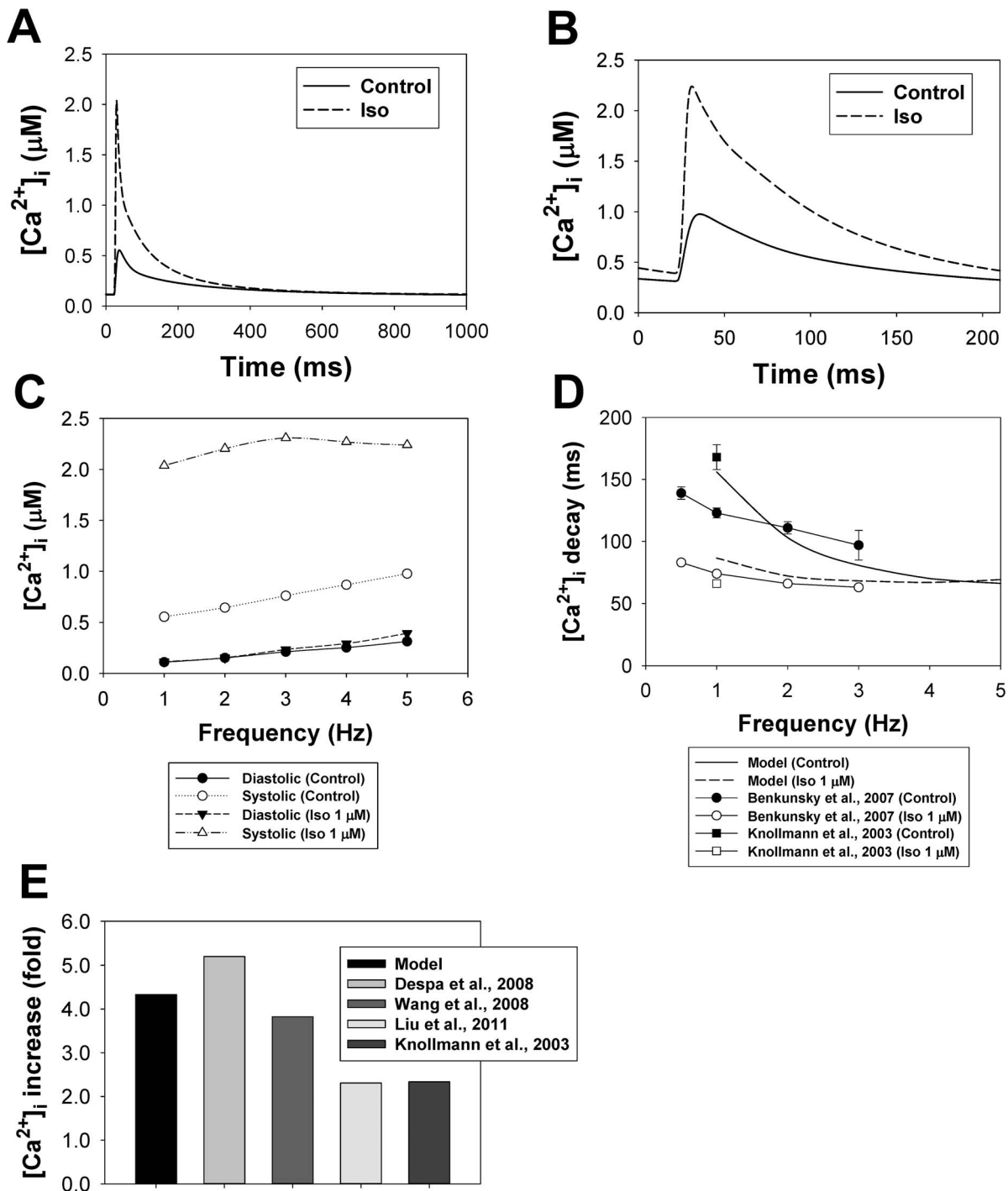
Experimental data obtained with micromolar concentrations of isoproterenol demonstrates significant (up to 5-fold) increase in intracellular  $[\text{Ca}^{2+}]_i$  transients obtained from mouse ventricular myocytes (Fig. 18, [75,127,128,129]). Our simulations are able to reproduce this behavior. Figure 18, A and B, shows simulated  $[\text{Ca}^{2+}]_i$  transients, obtained without and with 1  $\mu\text{M}$  isoproterenol at stimulation frequencies 1 and 5 Hz. Stimulation of the  $\beta_1$ -adrenergic signaling system increases the simulated amplitudes of  $[\text{Ca}^{2+}]_i$  at 1 Hz-stimulation from 0.44  $\mu\text{M}$  to 1.92  $\mu\text{M}$  (Fig. 18A), or by 4.33 fold. At larger stimulation frequency 5 Hz,  $[\text{Ca}^{2+}]_i$  increases from 0.66  $\mu\text{M}$  to 1.85  $\mu\text{M}$  (Fig. 18B), or by 2.79 fold. These values are in good agreement with the experimental data [75,127,128,129], which ranges from 2.3 to 5.2-folds increase. Frequency dependence of the diastolic and systolic  $[\text{Ca}^{2+}]_i$  (Fig. 18C) demonstrates an increase of their magnitudes, with the exclusion of peak  $[\text{Ca}^{2+}]_i$  at 1  $\mu\text{M}$  isoproterenol and stimulation frequencies 4 and 5 Hz. It is remarkable that the model reproduces experimentally found feature such as independence of diastolic  $[\text{Ca}^{2+}]_i$  from the  $\beta_1$ -adrenergic stimulation [128,130].

Our model also provides appropriate time constants for the decay of intracellular  $[\text{Ca}^{2+}]_i$  and corresponding acceleration of the decay upon application of isoproterenol. Simulated and experimental frequency dependences of the decay of intracellular  $[\text{Ca}^{2+}]_i$  without and with 1  $\mu\text{M}$  isoproterenol are shown in Fig. 18D. The simulated time constants for the decay decrease with the stimulation frequency without and with isoproterenol and reasonably well approximate experimental data [128,131]. Note,

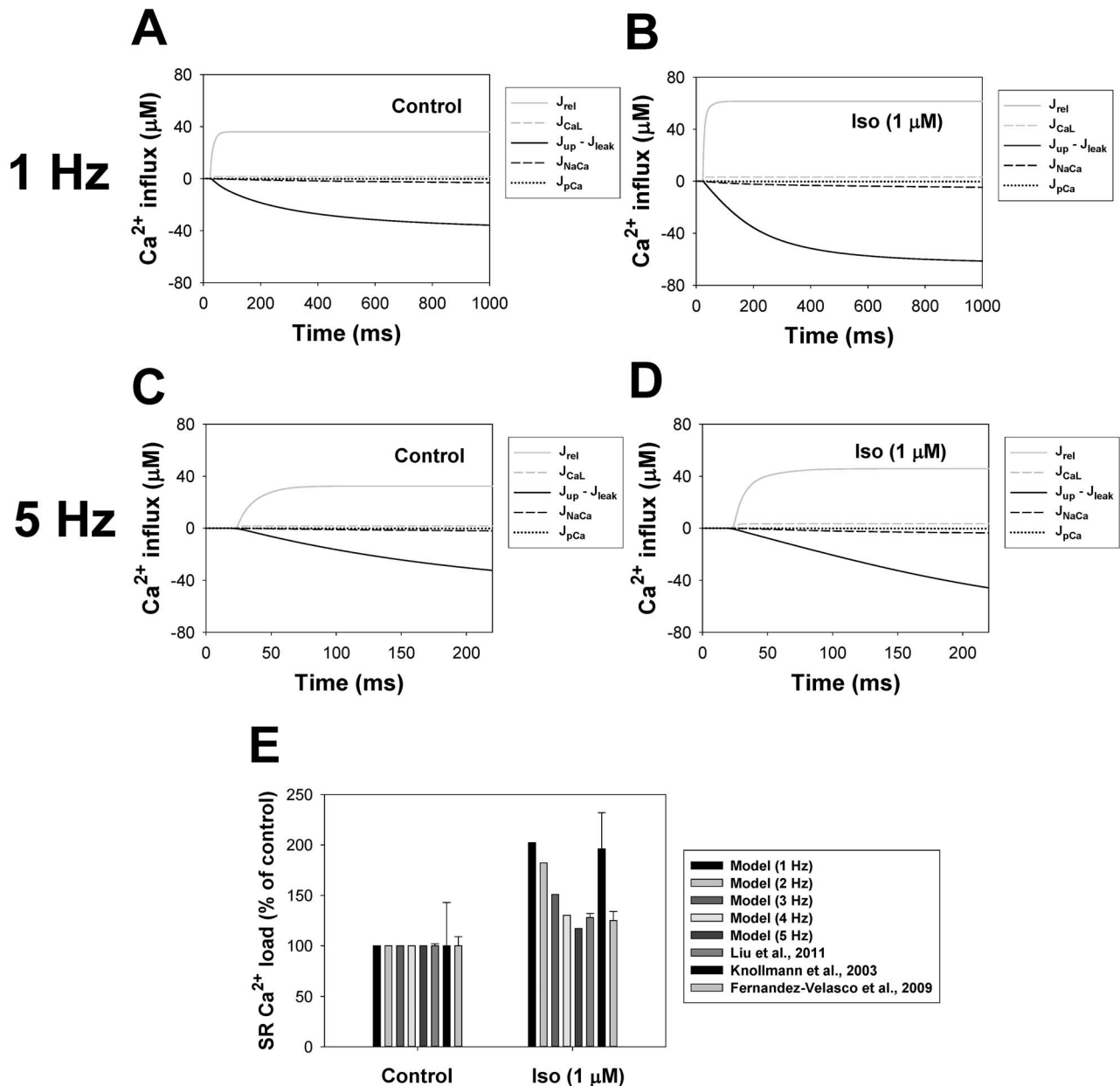
however, that the absolute values of  $[\text{Ca}^{2+}]_i$  relaxation constants obtained by Wang et al. [75] without and with isoproterenol are significantly longer, 267 and 147 ms, respectively, but their ratio ( $\sim 1.8$ ) is very close to the corresponding simulated value.

Our model allows for evaluation of various  $\text{Ca}^{2+}$  fluxes and their modifications by isoproterenol. Figure 19 shows simulated  $\text{Ca}^{2+}$  fluxes obtained at 1 and 5 Hz stimulations without and with 1  $\mu\text{M}$  isoproterenol. Simulations show that the activation of the  $\beta_1$ -adrenergic signaling system leads to a significant increase in  $\text{Ca}^{2+}$  influx through the L-type  $\text{Ca}^{2+}$  channels during action potential from 1.6  $\mu\text{M}$  (4.5% of released  $\text{Ca}^{2+}$  from the SR) to 3.3  $\mu\text{M}$  (5.3%) at 1 Hz and from 1.8  $\mu\text{M}$  (5.5%) to 3.5  $\mu\text{M}$  (7.6%) at 5 Hz during cardiac cycles. Increase in  $\text{Ca}^{2+}$  influx results in an increase in the SR  $\text{Ca}^{2+}$  load, from 919  $\mu\text{M}$  to 1860  $\mu\text{M}$  at 1 Hz (Fig. 19E, an increase which is comparable to the experimental findings [128,129,132]), resulting in a growth of  $\text{Ca}^{2+}$ -induced  $\text{Ca}^{2+}$  release from 36  $\mu\text{M}$  to 61  $\mu\text{M}$ . Smaller increase in the SR  $\text{Ca}^{2+}$  load is obtained at 5 Hz, from 1367  $\mu\text{M}$  to 1602  $\mu\text{M}$ , which results in an increase of  $\text{Ca}^{2+}$  release from 32  $\mu\text{M}$  to 46  $\mu\text{M}$ . An increase in intracellular  $[\text{Ca}^{2+}]_i$  transients after application of isoproterenol also increases  $\text{Ca}^{2+}$  extrusion from the cytosol by the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger from 3.1  $\mu\text{M}$  (8.6%) to 4.6  $\mu\text{M}$  (7.6%) at 1 Hz and from 1.9  $\mu\text{M}$  (6.0%) to 3.6  $\mu\text{M}$  (7.8%) at 5 Hz; however, this increase does not completely compensate for the  $\text{Ca}^{2+}$  entry into the cell, which ultimately leads to an increase in the SR  $\text{Ca}^{2+}$  load. Only 0.18  $\mu\text{M}$  and 0.28  $\mu\text{M}$  (1 Hz stimulation) and 0.16  $\mu\text{M}$  and 0.22  $\mu\text{M}$  (5 Hz stimulation) of  $\text{Ca}^{2+}$  are extruded from the cell by a slow mechanism through the sarcolemmal  $\text{Ca}^{2+}$  pump for control conditions and after application of isoproterenol, respectively, which is about 0.5% of the released  $\text{Ca}^{2+}$  in all cases. Our model also includes background  $\text{Ca}^{2+}$  influx of  $\sim 1.7 \mu\text{M}$  (1 Hz) and  $\sim 0.3 \mu\text{M}$  (5 Hz) due to a very large  $\text{Ca}^{2+}$  gradient across the membrane, which does not change upon stimulation of  $\beta_1$ -ARs.

Figure 20 shows the time behavior of the peak values of intracellular  $[\text{Ca}^{2+}]_i$  transients and intracellular  $[\text{Na}^+]_i$  concentration for control conditions and after application of 1  $\mu\text{M}$  isoproterenol upon stimulation with frequency 1 Hz. In control,  $[\text{Ca}^{2+}]_i$  transients approach quasi-steady-state values after a short-time initial decay (negative staircase effect). After application of isoproterenol,  $[\text{Ca}^{2+}]_i$  transients relatively rapidly increase in amplitude during the first  $\sim 300$  seconds, and then they slowly decay. Such behavior of  $[\text{Ca}^{2+}]_i$  transients is similar to the experimental data obtained by Despa et al. [127]. Initial increase in  $[\text{Ca}^{2+}]_i$  transients is due to the rapid activation of  $\beta_1$ -adrenoceptors and cAMP accumulation; relatively slow decay of peak  $[\text{Ca}^{2+}]_i$  is due to  $\beta_1$ -adrenoceptors desensitization. In addition, Despa et al. [127] have shown that the stimulation of  $\beta_1$ -ARs decreases intracellular  $[\text{Na}^+]_i$  concentration due to an increased function of the  $\text{Na}^+/\text{K}^+$  pump. Our simulation data reproduced this behavior. In control, stimulation of the model cell leads to a slight increase in  $[\text{Na}^+]_i$  to saturating values (solid line in Fig. 20B). However, the behavior of  $[\text{Na}^+]_i$  changes after application of isoproterenol (dashed line in Fig. 20B): after a small initial increase until peak value,  $[\text{Na}^+]_i$  decreases subsequently in time until quasi-steady-state level. Simulated  $[\text{Na}^+]_i$  concentration begins to decay at approximately the same time as  $[\text{Ca}^{2+}]_i$  achieves



**Figure 18. Simulated and experimental  $[Ca^{2+}]_i$  transients and their characteristics in an isolated ventricular cell for control conditions and after application of isoproterenol.** **Panel A:** Simulated  $[Ca^{2+}]_i$  transients for control conditions (solid line) and after 1  $\mu M$  isoproterenol application (dashed line) obtained with 1 Hz-stimulation. **Panel B:** Simulated  $[Ca^{2+}]_i$  transients for control conditions (solid line) and after 1  $\mu M$  isoproterenol application (dashed line) obtained with 5 Hz-stimulation. **Panel C:** Simulated diastolic (filled symbols) and systolic (unfilled symbols)  $[Ca^{2+}]_i$  magnitudes for control conditions (circles) and after 1  $\mu M$  isoproterenol application (triangles) as functions of stimulation frequency. **Panel D:** Decay time constants for intracellular  $[Ca^{2+}]_i$  transients for control conditions and after 1  $\mu M$  isoproterenol application as functions of stimulation frequency. Simulated data are shown by solid (control) and dashed (1  $\mu M$  isoproterenol) lines. The lines with symbols show experimental data from Benkunsy et al. [131]; experimental data from Knollmann et al. [128] are shown by squares. **Panel E:** Increase in  $[Ca^{2+}]_i$  transient amplitudes after application of isoproterenol (folds). Model data and data of Wang et al. [75] and Liu et al. [129] are obtained at 1 Hz and 1  $\mu M$  isoproterenol; data of Despa et al. [127] are obtained at 2 Hz and 1  $\mu M$  isoproterenol; data of Knollmann et al. [128] are obtained at 1 Hz and 0.5  $\mu M$  isoproterenol. All simulation data in this figure are obtained after 300-s stimulations and exposure to 1  $\mu M$  isoproterenol. doi:10.1371/journal.pone.0089113.g018

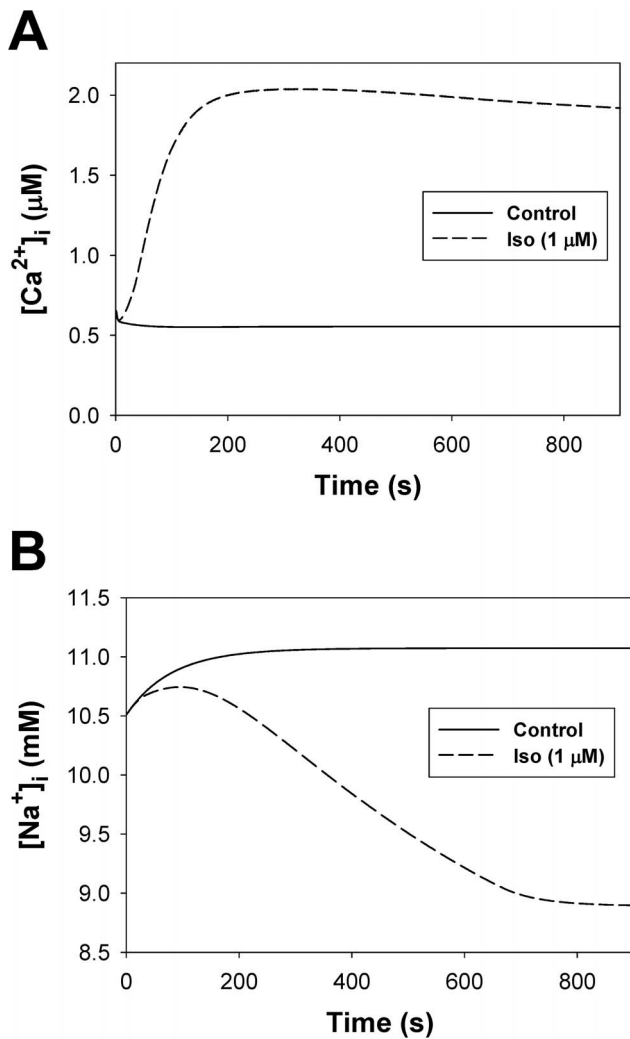


**Figure 19. Ca<sup>2+</sup> fluxes and the SR Ca<sup>2+</sup> load.** Simulated major integral Ca<sup>2+</sup> fluxes during one cardiac cycle in the isolated ventricular cell model for control conditions (Panels A and C) and after application of 1 μM isoproterenol (Panels B and D). Pacing frequencies are 1 Hz (Panels A and B) and 5 Hz (Panels C and D). Major integral Ca<sup>2+</sup> fluxes are shown after 300 s of stimulation. In Panels B and D 1 μM isoproterenol is applied at time t = 0 s. Here, J<sub>CaL</sub> is the Ca<sup>2+</sup> entering the cell through L-type Ca<sup>2+</sup> channels; J<sub>up</sub> - J<sub>leak</sub> is the uptake Ca<sup>2+</sup> from the cytosol to the network SR with subtracted Ca<sup>2+</sup> leak from the SR to the cytosol; J<sub>NaCa</sub> is the Ca<sup>2+</sup> outflux from the cytosol through the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger; and J<sub>pCa</sub> is the Ca<sup>2+</sup> outflux through the sarcolemmal Ca<sup>2+</sup> pump. Panel E: Increase in the SR Ca<sup>2+</sup> load after 300-s application of isoproterenol. Model data are shown for stimulation frequencies 1, 2, 3, 4, and 5 Hz; experimental data of Liu et al. [129] and Fernandez-Velasco et al. [132] are obtained at 1 μM isoproterenol; data of Knollmann et al. [128] are obtained at 0.5 μM isoproterenol. doi:10.1371/journal.pone.0089113.g019

its maximum value. Experimental data shows a plateau in concentration of [Na<sup>+</sup>]<sub>i</sub> for a short time after application of isoproterenol, which is replaced by a decay after [Ca<sup>2+</sup>]<sub>i</sub> achieves the maximum value [127].

Finally, experimental data demonstrates the absence of the negative staircase effect in [Ca<sup>2+</sup>]<sub>i</sub> transients which are elicited by stimulation of a quiescent cell after application of isoproterenol [27]. The experimental data are obtained for rat ventricular myocytes, whose Ca<sup>2+</sup> handling system is similar to that for mice.

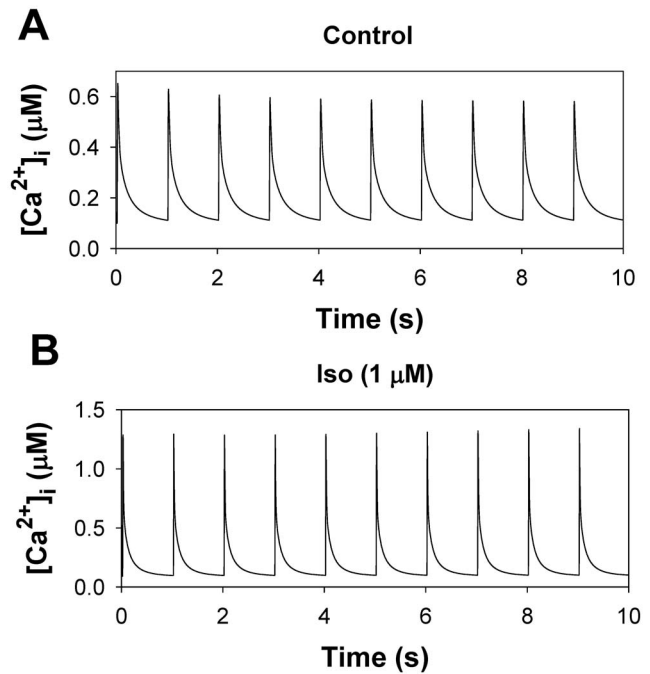
Our model for mouse ventricular myocytes reproduced this behavior. Figure 21A shows [Ca<sup>2+</sup>]<sub>i</sub> transients upon stimulation of the quiescent cell with the frequency of 1 Hz in the control cell. The [Ca<sup>2+</sup>]<sub>i</sub> decrease in time, clearly shows a negative staircase effect. In another simulation (Fig. 21B), 1 μM isoproterenol is applied to the quiescent cell for 600 seconds, and then the cell is electrically stimulated with the frequency of 1 Hz. The simulation data does not show a decrease in [Ca<sup>2+</sup>]<sub>i</sub> transient amplitudes,



**Figure 20. Dynamics of [Ca<sup>2+</sup>]<sub>i</sub> transients and [Na<sup>+</sup>]<sub>i</sub> concentrations upon stimulation of β<sub>1</sub>-adrenoceptors. Panel A:** Simulated peak values of [Ca<sup>2+</sup>]<sub>i</sub> transient as function of time for control conditions (solid line) and after 1 μM isoproterenol application at *t*=0 s (dashed line). **Panel B:** Simulated intracellular [Na<sup>+</sup>]<sub>i</sub> concentrations as function of time for control conditions (solid line) and after 1 μM isoproterenol application at *t*=0 s (dashed line). In both panels, stimulation frequency is 1 Hz. doi:10.1371/journal.pone.0089113.g020

thereby confirming the absence of a negative staircase effect after stimulation of the β<sub>1</sub>-adrenergic signaling system.

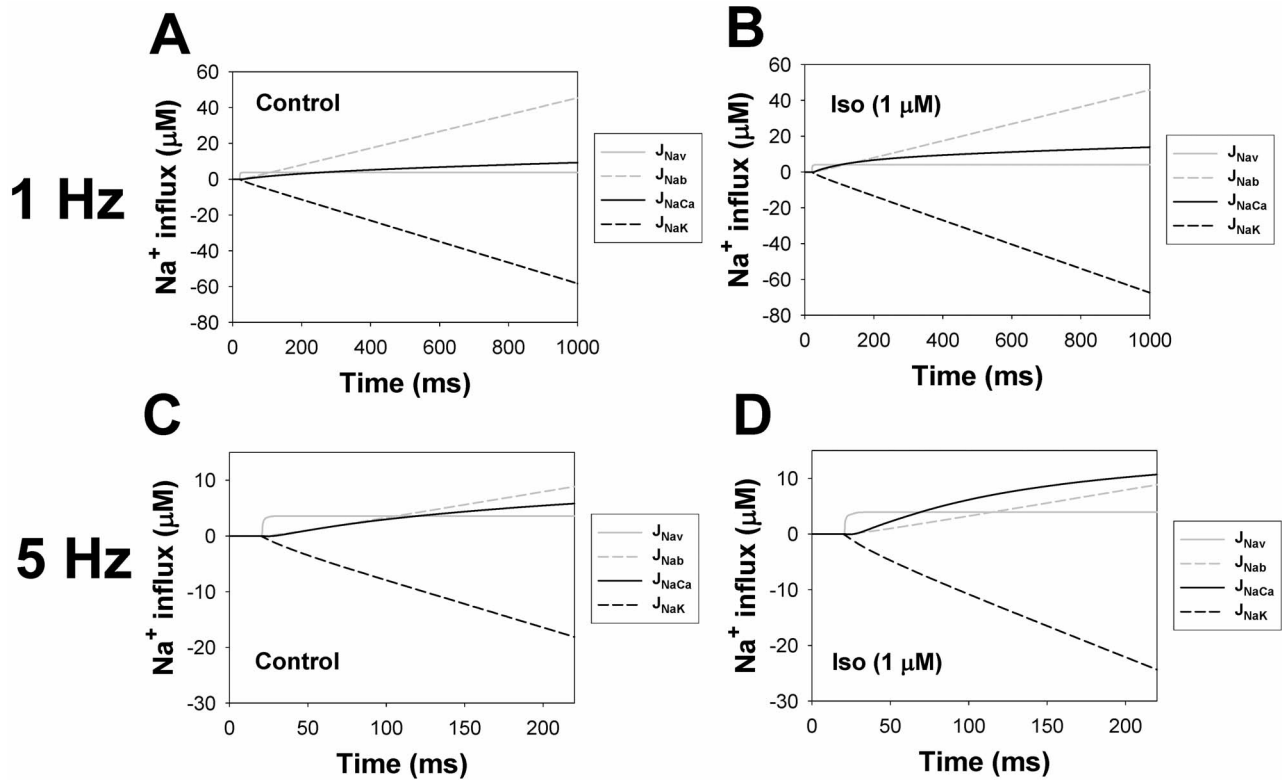
The mechanism of two different types of behavior is explained by the analysis of the input and output Ca<sup>2+</sup> fluxes without and with application of isoproterenol. Our simulations of the case without isoproterenol show that the stimulation of the quiescent myocyte increases total intracellular Ca<sup>2+</sup> loss and decreases the SR Ca<sup>2+</sup> load, resulting in continuous decrease in [Ca<sup>2+</sup>]<sub>i</sub> transient (Fig. 21A). If the simulated cell is first pretreated with isoproterenol in the quiescent state for 600 seconds and then the electrical stimulation is applied, the Ca<sup>2+</sup> fluxes inside and outside the cell remain balanced due to the predominant increase in the L-type Ca<sup>2+</sup> current. The result is that the SR Ca<sup>2+</sup> load is not decreased, resulting in the absence of negative staircase effect.



**Figure 21. The effects of isoproterenol on negative staircase of [Ca<sup>2+</sup>]<sub>i</sub> transients. Panel A:** Simulated [Ca<sup>2+</sup>]<sub>i</sub> transients as function of time for control conditions show clear negative staircase effect. **Panel B:** Simulated [Ca<sup>2+</sup>]<sub>i</sub> transients as function of time after 1 μM isoproterenol application at *t*=0 s does not show negative staircase effect. In both panels, stimulation frequency is 1 Hz. doi:10.1371/journal.pone.0089113.g021

### The Effects of Activation of the β<sub>1</sub>-adrenergic Signaling System on Na<sup>+</sup> Fluxes

Experimental data shows the effects of the β<sub>1</sub>-adrenergic signaling system on Na<sup>+</sup> dynamics in ventricular myocytes [100,127]. In particular, in mouse ventricular myocytes, [Na<sup>+</sup>]<sub>i</sub> decreases upon stimulation of β<sub>1</sub>-adrenergic receptors. Such behavior was reproduced by our model as well (Fig. 20B). In addition, our model is able to predict major Na<sup>+</sup> fluxes into and out of the mouse ventricular myocytes. Simulated Na<sup>+</sup> fluxes for control conditions and after application of 1 μM isoproterenol for stimulation frequencies of 1 and 5 Hz (*I*<sub>stim</sub> = 80 pA/pF, τ<sub>stim</sub> = 1 ms) are shown in Fig. 22. Na<sup>+</sup> enters the cell through the fast Na<sup>+</sup> channels, Na<sup>+</sup>/Ca<sup>2+</sup> exchanger, and background mechanisms (large Na<sup>+</sup> gradient and other exchangers and co-transporters [133]), and is pumped out of the cell by the Na<sup>+</sup>-K<sup>+</sup> pump. Without isoproterenol and at 1 Hz stimulation, 3.8 μM of Na<sup>+</sup> enter the cell during action potential through the fast Na<sup>+</sup> channels (6.5% of the total Na<sup>+</sup> influx), 9.3 μM of Na<sup>+</sup> through the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger (16%), and 45.5 μM of Na<sup>+</sup> through the background mechanism (77.5%), giving total Na<sup>+</sup> influx of 58.6 μM. After application of 1 μM isoproterenol and 1 Hz stimulation, the total Na<sup>+</sup> influx into the cell increases to 64.0 μM, resulting in proportional changes of Na<sup>+</sup> influx through the fast Na<sup>+</sup> channels (4.2 μM, or 6.5%), increased influx through the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger (13.9 μM, or 22%), and unchanged Na<sup>+</sup> influx through the background mechanism (45.9 μM, or 71.5%). At the larger stimulation frequency (5 Hz), the contribution of the different Na<sup>+</sup> entry mechanisms changes. Without isoproterenol, 3.6 μM of Na<sup>+</sup> enter the cell during action potential through the fast Na<sup>+</sup> channels (20% of the total Na<sup>+</sup> influx), 5.8 μM of Na<sup>+</sup> through the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger (32%), and 8.9 μM of Na<sup>+</sup> through the background mechanism (48%), yielding total Na<sup>+</sup>



**Figure 22. The effects of isoproterenol on integral Na<sup>+</sup> fluxes.** Simulated major integral Na<sup>+</sup> fluxes during one cardiac cycle in the isolated ventricular cell model are shown for control conditions (Panels A and C) and after application of 1 µM isoproterenol (Panels B and D). Pacing frequencies are 1 Hz (Panels A and B) and 5 Hz (Panels C and D). Major integral Na<sup>+</sup> fluxes are shown after 300 s of stimulation. In Panels B and D 1 µM isoproterenol is applied at time  $t=0$  s. Here,  $J_{Nav}$  is the Na<sup>+</sup> entering the caveolae compartment through the fast Na<sup>+</sup> channels;  $J_{Nab}$  is the background Na<sup>+</sup> influx;  $J_{NaCa}$  is the Na<sup>+</sup> influx to the cytosol through the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger; and  $J_{NaK}$  is the Na<sup>+</sup> outflux through the Na<sup>+</sup>-K<sup>+</sup> pump. doi:10.1371/journal.pone.0089113.g022

influx of 18.3 µM. Application of 1 µM isoproterenol increases the total Na<sup>+</sup> influx into the cell to 24.4 µM, resulting in an increase of Na<sup>+</sup> influx through the fast Na<sup>+</sup> channels (3.9 µM, or 17%) and the Na<sup>+</sup>/Ca<sup>2+</sup> exchanger (10.7 µM, or 46%), and unchanged Na<sup>+</sup> influx through the background mechanism (8.9 µM, or 37%).

Thus, our simulations allow for the estimation of Na<sup>+</sup> fluxes and dynamics, and their modifications by the β<sub>1</sub>-adrenergic signaling system. The model data shows an increased fraction of voltage-dependent Na<sup>+</sup> entry into the cell at higher stimulation frequencies and the shift of the balance of the Na<sup>+</sup> fluxes upon application of isoproterenol towards outside the cell due to an increased function of the Na<sup>+</sup>-K<sup>+</sup> pump.

### The Effects of the Block of Different Populations of I<sub>CaL</sub> on the Action Potential and [Ca<sup>2+</sup>]<sub>i</sub> Transients

Experimental data shows that two different populations of the L-type Ca<sup>2+</sup> channels, in caveolin-3-rich and caveolin-3-free membrane fractions, affects differently [Ca<sup>2+</sup>]<sub>i</sub> transients and cellular contraction [70]. Such investigations were performed by a specific block of the caveolae-linked L-type Ca<sup>2+</sup> channels. While the experiments show a 10% decrease in the mean values of the peak of [Ca<sup>2+</sup>]<sub>i</sub> transients in the myocytes with blocked caveolae-located L-type Ca<sup>2+</sup> channels compared to control, such decrease did not reach statistical significance. Similar small, but not significant, decrease was also observed in myocyte contraction.

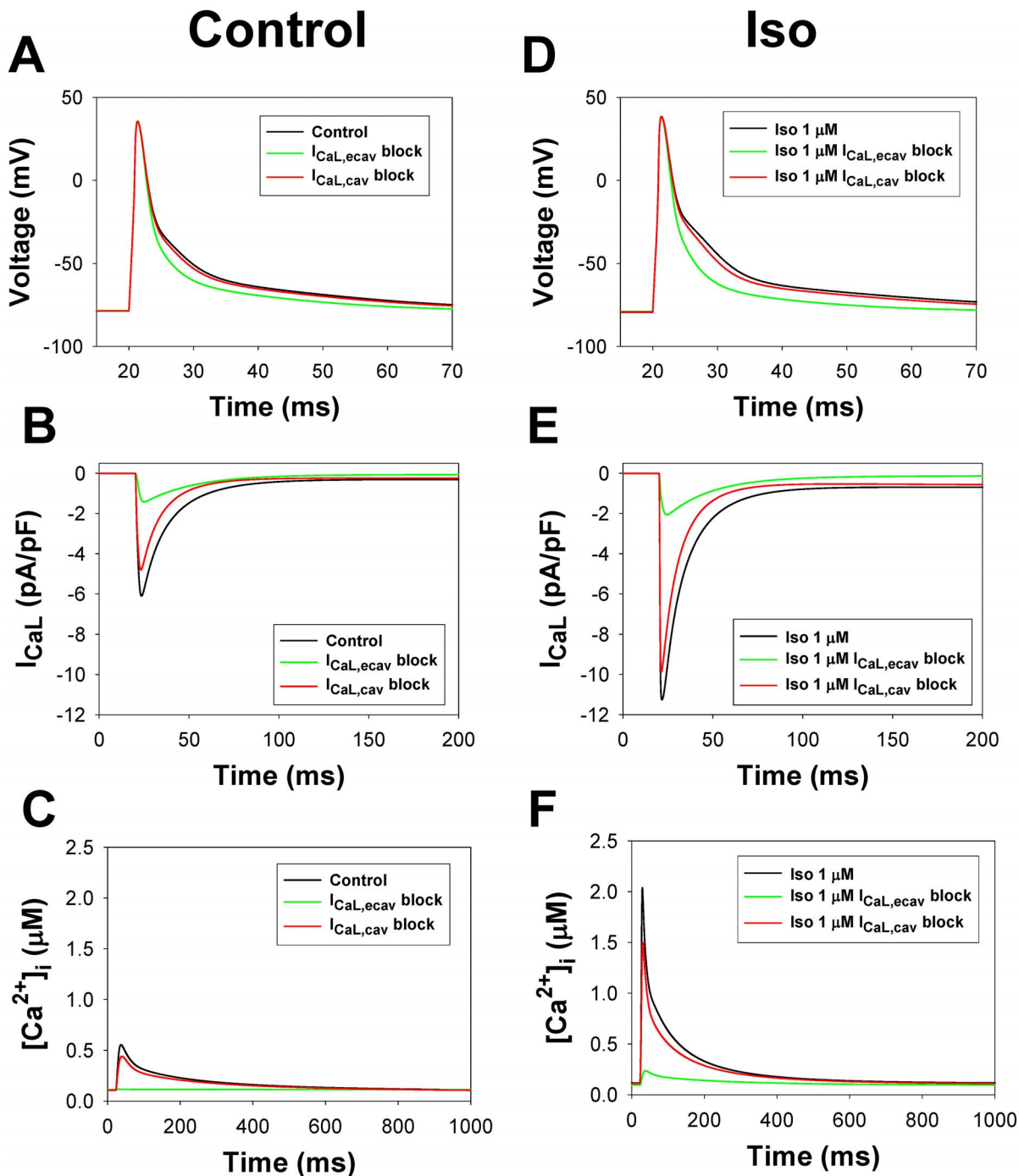
We used the model to investigate the effects of the L-type Ca<sup>2+</sup> channel block in different cellular compartments on the action potential and [Ca<sup>2+</sup>]<sub>i</sub> transients in control and after application of

1 µM isoproterenol (Fig. 23). The model cells are electrically stimulated at the frequency 1 Hz. In control, we observed a little change in action potential shape when the caveolae-linked I<sub>CaL</sub> (I<sub>CaL,cav</sub>) is blocked (APD<sub>50</sub> decreased by only 2%), whereas a much larger change in the AP is observed during block of I<sub>CaL</sub> in the extracaveolae compartment (I<sub>CaL,ecav</sub>) (APD<sub>50</sub> decreased by 14%) (Fig. 23, A). The magnitude of the total I<sub>CaL</sub> changed by ~20% during the block of I<sub>CaL,cav</sub>, while the I<sub>CaL</sub> is almost abolished by the block of I<sub>CaL,ecav</sub> (Fig. 23, B). The I<sub>CaL,cav</sub> block relatively slightly (by 25%) decreases [Ca<sup>2+</sup>]<sub>i</sub> transients, similar to the experimental finding by [70], while at the I<sub>CaL,ecav</sub> block such transient is not present (Fig. 23, C).

When the model cell is stimulated by isoproterenol, the specific block of I<sub>CaL,cav</sub> only slightly decreased the total cellular I<sub>CaL</sub> (Fig. 23, E), resulting in more pronounced shortening of APD<sub>50</sub> (by 8%, Fig. 23, D) compared to control. Even larger AP shortening is obtained with the specific block of I<sub>CaL,ecav</sub> (by 28%). More significant effect of I<sub>CaL,cav</sub> block on [Ca<sup>2+</sup>]<sub>i</sub> transients is predicted by simulations with isoproterenol than for control conditions (a decrease by 28%), and [Ca<sup>2+</sup>]<sub>i</sub> transients is almost abolished with the I<sub>CaL,ecav</sub> block (Fig. 23, F). Further experiments on the effects of different populations of the L-type Ca<sup>2+</sup> channels on the action potential and [Ca<sup>2+</sup>]<sub>i</sub> transients are necessary to verify model predictions.

### Discussion

In this paper, a new compartmentalized model for the β<sub>1</sub>-adrenergic signaling system in mouse ventricular myocytes is



**Figure 23. The effects of two subpopulations of the L-type  $Ca^{2+}$  current block on the action potentials and  $[Ca^{2+}]_i$  transients.** Simulated effects of two subpopulations of the L-type  $Ca^{2+}$  current block on the action potentials and  $[Ca^{2+}]_i$  transients in the isolated ventricular cell model are shown for control conditions and after application of 1  $\mu$ M isoproterenol at pacing frequency 1 Hz ( $I_{stim} = 80$  pA/pF,  $\tau_{stim} = 1.0$  ms). **Panels A–C:** Control conditions; **Panels D–F:** Isoproterenol is applied. **Panels A and D:** Simulated action potentials for control conditions (solid black line), after  $I_{CaL,ecav}$  block (green line), and after  $I_{CaL,cav}$  block (red line). **Panels B and E:** Simulated  $I_{CaL}$  currents. **Panel C and F:** Simulated  $[Ca^{2+}]_i$  transients. APs and ionic currents are shown after 300 s stimulation. 1  $\mu$ M isoproterenol is applied at time  $t = 0$  s. doi:10.1371/journal.pone.0089113.g023

developed. This model is based on our previously published model for an apical cardiac cell [25,26], which includes a comprehensive description of action potential, ionic currents, and  $Ca^{2+}$  dynamics. The new model includes biochemical and electrophysiological parts of the  $\beta_1$ -adrenergic signaling pathway, which are extensively verified by the existing experimental data. The model successfully

reproduces cAMP dynamics, activation of adenylyl cyclases and phosphodiesterases, protein kinase A and its targets, voltage-clamp protocols for major repolarization currents, action potential modification, and changes in the  $Ca^{2+}$  handling mechanism upon stimulation of the  $\beta_1$ -adrenergic signaling system. The model allows for elucidation of the mechanisms of action potential

prolongation and increase in  $[Ca^{2+}]_i$  transients. Simulations also show the absence of the negative staircase effect in  $[Ca^{2+}]_i$  transients upon stimulation of  $\beta_1$ -adrenoceptors, which was found experimentally. The model also allows for some testable predictions, such as frequency dependences of action potential durations and  $[Ca^{2+}]_i$  transient amplitudes. The model highlights the importance of compartmentalization of the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes by the description of the two populations of the L-type  $Ca^{2+}$  channels, in caveolae and extracaveolae compartments, and their distinct functional role in myocyte function, as well as the differential localization and function of other PKA targets.

### Compartmentalization of the $\beta_1$ -adrenergic Signaling System

The  $\beta$ -adrenergic signaling system plays a significant role in the function of the heart. There are two types of  $\beta$ -adrenergic receptors in cardiomyocytes ( $\beta_1$ - and  $\beta_2$ -adrenergic receptors), which are different in their cellular localization and function. Experimental data from rat ventricular myocytes by Rybin et al. [20] shows that  $\beta_1$ -adrenergic receptors are distributed between caveolae, non-caveolae membrane fractions, and internal membranes, with the majority of the  $\beta_1$ -adrenergic receptors being found outside of the caveolae compartment. In contrast,  $\beta_2$ -adrenergic receptors ( $\beta_2$ -ARs) are localized in the caveolae compartment [20]. Similar data were obtained for mouse ventricular myocytes [19]. According to the experimental finding, our model includes only 1% of  $\beta_1$ -adrenergic receptors in the caveolae compartment, with the majority of them distributed between the extracaveolae and cytosolic compartments. Such localization suggests different functional consequences: selective activation of  $\beta_1$ -adrenergic receptors with isoproterenol in mouse ventricular myocytes leads to a significant increase in  $[Ca^{2+}]_i$  transient and myocyte contraction, while selective activation of  $\beta_2$ -adrenergic receptors with zinterol does not have any effect on myocyte contractility [134]. Activation of  $\beta_1$ -adrenergic receptors also results in phosphorylation of major cytosolic proteins, such as phospholamban and troponin I, while stimulation of  $\beta_2$ -adrenergic receptors does not produce this effect [135].

In addition to differential localization of  $\beta_1$ - and  $\beta_2$ -adrenergic receptors, experimental data also demonstrates differential localization of signaling proteins involved in the  $\beta_1$ -adrenergic signaling pathway, suggesting that even activation of one signaling system is a complex process, which proceeds differently in separate compartments. It has been found that adenylyl cyclases of type V/VI are predominantly localized in caveolae, while types IV and VII are located in non-caveolae membrane fractions and cytosol [28,35,36]. There is also differential distribution of three major types of phosphodiesterases in subcellular compartments (PDE2, PDE3, and PDE4 [48]), which also causes different effects on cAMP degradation [123]. Our model successfully reproduces the activities of ACs and PDEs in different compartments, and the differential effects of PDE3 and PDE4 inhibition in production of cAMP transients. For example, steady-state cAMP concentration is smaller and cAMP transient is less prolonged in the caveolae compartment than in the extracaveolae and cytosol (Fig. 15), suggesting larger activity of PDEs in the caveolae.

Finally, the major protein kinase A phosphorylation targets are also localized in different subcellular compartments. Two of them are found predominantly in the caveolae compartment (the fast  $Na^+$  current and the phospholemman, which regulates the  $Na^+$ - $K^+$  pump), five others ( $I_{CaL}$ ,  $I_{Kto,f}$ ,  $I_{Kur}$ ,  $I_{K1}$ , and ryanodine receptors) are predominantly expressed in non-caveolae membrane domains, and phospholamban and troponin I are located in the cytosol (see

Methods for details). It is remarkable that one of the PKA targets, the L-type  $Ca^{2+}$  channel, is expressed in both the caveolae and extracaveolae compartments, with different a physiological role in each domain. In addition to the different distribution of two major protein kinase A isoforms (PKAI and PKAII), there is also a different localization of the major dephosphorylation proteins (protein phosphatase 1 and protein phosphatase 2A). Both PP1 and PP2A are found in the caveolae and cytosolic compartments, however, only PP1 plays an important functional role in the extracaveolae. Such distribution of the targets results in their different phosphorylation kinetics and magnitude, producing a very complex interaction relationship in the effects on action potential and  $[Ca^{2+}]_i$  transients.

Our model of the  $\beta_1$ -adrenergic signaling system includes differential subcellular localization of both signaling and target proteins, and is able to reproduce both phosphorylation kinetics and concentration-dependence of protein phosphorylation by isoproterenol (see Methods). Several non-compartmentalized models were developed for  $\beta_1$ -adrenergic signaling system in different species, including mice [9,10,11,12]. The models were extensively verified by the available experimental data on the effects of activation of  $\beta_1$ -adrenergic receptors on electrical activity and ionic homeostasis. However, as the experimental technique is improving and the new data on subcellular organization of signaling systems is accumulating, more comprehensive models are required for more precise description of the cellular functions. Such important findings include differential localization of the isoforms of the major signaling proteins in the  $\beta_1$ -adrenergic signaling system: adenylyl cyclases, phosphodiesterases, and protein kinase A [10,36,46]. Discovery of the differential localization of the targets of PKA, such as the ionic currents and contractile proteins, requires more demands on the models of cardiac cells to include multiple subcellular compartments. One of the recent experimental findings of the two populations of the L-type  $Ca^{2+}$  channels, the major players in cardiac excitation-contraction coupling, and their differential physiological role in cellular function highlights the needs in compartmentalized models of cardiac myocytes [21,22]. One such model was developed recently for canine ventricular myocytes and includes three signaling systems,  $\beta_1$ - and  $\beta_2$ -adrenergic, and CaMKII-mediated signaling systems [8]. The model described well extensive experimental data and the effects of different signaling systems on the cardiac action potential and  $[Ca^{2+}]_i$  transients. Our model of the  $\beta_1$ -adrenergic signaling system consists of some elements of the model of Heijman et al. [8], but with significant differences, as outlined above. In particular, the presented model includes differential localization of ryanodine receptors and describes two populations of the L-type  $Ca^{2+}$  channels based on the most recent experimental data [21,22]. While the major role of compartmentalization of the components in the  $\beta_1$ -adrenergic signaling system is clear – separation of the effects of different signaling proteins – the particular role of the signaling molecules in the mechanisms of regulation of the target proteins still needs to be determined.

### The Effects of the $\beta_1$ -adrenergic Signaling System on Action Potential

Experimental data shows that the activation of the  $\beta_1$ -adrenergic signaling system moderately prolongs action potentials duration in mouse ventricular myocytes (Table 1, [125,126]). Our previous simulation data using the models of mouse ventricular myocytes and ventricular tissues show that the prolongation of action potential can be a pro-arrhythmic factor causing a loss of stability at the cellular level [136] or action

potential block at the tissue level at fast pacing rates [137]. Our model reproduces action potential prolongation and elucidates its mechanism. We found that the major effect on action potential at 25% and 50% repolarization comes from an increase in the inward L-type  $\text{Ca}^{2+}$  current,  $I_{\text{CaL}}$ , and the fast  $\text{Na}^+$  current,  $I_{\text{Na}}$ , and a decrease in the rapidly recovering transient outward  $\text{K}^+$  current,  $I_{\text{K}_{10,f}}$  which tend to prolong action potential, and an increase in the ultra-rapidly activating current,  $I_{\text{K}_{ur}}$ , whose role is in action potential shortening (Fig. 17). At 75% and 90% repolarization, more currents, such as the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger current, the  $\text{Na}^+-\text{K}^+$  pump current, the time-independent  $\text{K}^+$  current,  $I_{\text{K}_1}$ , and the  $\text{Na}^+$  background current,  $I_{\text{Na}b}$ , are brought into play (Fig. 17). The total result of interaction is the moderate prolongation of action potential duration. Note that similar prolongation of the action potential duration upon stimulation of the  $\beta_1$ -adrenergic signaling system was found in rat ventricular cells [10], however, the mechanism of the action potential prolongation and the role of major contributing currents were not investigated.

Frequency dependences of the action potential duration at different levels of repolarization show their different prolongations upon stimulation with isoproterenol (Table 1). While the prolongations of  $\text{APD}_{50}$  increase with the stimulation frequency, the prolongations of  $\text{APD}_{75}$  and  $\text{APD}_{90}$  demonstrate more complex behavior. Such differences are explained by the different major contributing currents to AP duration at different levels of repolarization without and with isoproterenol. A decrease in the prolongation magnitude of  $\text{APD}_{90}$  compared to  $\text{APD}_{50}$  upon application of isoproterenol is also observed in some experiments [125,126]; however, data of Wang et al. [75] demonstrated similar prolongations both for  $\text{APD}_{90}$  and  $\text{APD}_{50}$ . Further experiments are necessary to investigate this phenomenon.

This effect of  $\beta_1$ -adrenergic receptor stimulation on action potential is different from that in larger species [8,11]. Experimental data shows that stimulation of  $\beta_1$ -ARs reduces action potential duration in rabbits and dogs wild type ventricular myocytes [11,138]. The data of Volders et al. [138] shows that one of the major contributing factors in action potential shortening is an increase in the slow delayed-rectifier current,  $I_{\text{K}_s}$ , upon activation of  $\beta_1$ -ARs. The increase in  $I_{\text{K}_s}$  overcomes the tendency of action potential to prolongation due to an increase in the L-type  $\text{Ca}^{2+}$  current,  $I_{\text{CaL}}$  [138]. This result was also confirmed by simulations using models for rabbit and canine action potential which include the  $\beta_1$ -adrenergic signaling system [8,11].

Thus, our model for the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes and the models of others for canine and rabbit cardiac cells [8,11] demonstrate different effects of  $\beta_1$ -adrenoceptor stimulations on the action potential durations, elucidate the mechanisms of these effects, and reveal the different ionic currents which are responsible for the changes.

### The Effects of the $\beta_1$ -adrenergic Signaling System on $\text{Ca}^{2+}$ Dynamics

As found experimentally, activation of the  $\beta_1$ -adrenergic signaling system significantly increases the magnitude of intracellular  $[\text{Ca}^{2+}]_i$  transients, depending on the concentration of  $\beta_1$ -ARs agonist [75,127,128,129,139]. The effect is more pronounced in rodent ventricular cells where the increase can reach up to 5 times [127], and a smaller effect is observed in larger species, such as rabbit and dog [139,140]. In addition to an increase in  $[\text{Ca}^{2+}]_i$  transient amplitude,  $\beta_1$ -AR agonists increase the rate of  $[\text{Ca}^{2+}]_i$  decline.

There are several points of view on what is the major cause of the inotropy and lusitropy in the heart. It is clear that

phosphorylation of phospholamban increases the pumping of  $\text{Ca}^{2+}$  into the SR upon stimulation of  $\beta_1$ -AR and is considered a crucial regulator of cardiac function [27,141]. However, this phospholamban phosphorylation is not the only reason for such increase. Recently Eisner et al. [142] analyzed the major contributing factor to positive cardiac inotropy upon stimulation of  $\beta_1$ -ARs. They considered four proteins that are affected by adrenergic stimulation: ryanodine receptors, SERCA pump, L-type  $\text{Ca}^{2+}$  channels, and troponin. Their analysis has shown that the L-type  $\text{Ca}^{2+}$  current is a major player that leads to positive cardiac inotropy. In our model, stimulation of the  $\beta_1$ -adrenergic signaling system increases  $I_{\text{CaL}}$  by about twice compared to control cells (Fig. 9 [79,80,81]). This increase approximately doubles  $\text{Ca}^{2+}$  influx into the myocyte (see also our simulation data in Fig. 19), while  $\text{Ca}^{2+}$  extrusion from the myocyte, predominantly by the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger, does not increase to the same degree. The resulting effect is an increase in  $\text{Ca}^{2+}$  influx into cell until a new dynamic quasi-steady-state is reached. Thus, our modeling data supports the view that the L-type  $\text{Ca}^{2+}$  current is a major player in cardiac inotropy in mouse ventricular myocytes, as also suggested by Eisner et al. [142].

Our model also supports the idea that the key contributor to cardiac lusitropy upon stimulation of  $\beta_1$ -ARs is the SERCA  $\text{Ca}^{2+}$  pump. In mouse and rat ventricular myocytes, about 90% of the released  $\text{Ca}^{2+}$  is pumped back to the sarcoplasmic reticulum compared to about 70% in rabbits and larger species [27]. An estimation of  $\text{Ca}^{2+}$  influx into the SR by the SERCA pump during one cardiac cycle (1 Hz stimulation) before and after activation of the  $\beta_1$ -adrenergic signaling system is 36  $\mu\text{M}$  and 61  $\mu\text{M}$ , respectively. This estimation correlates with about a two-fold decrease in the time constant of  $[\text{Ca}^{2+}]_i$  relaxation (Fig. 18). While the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger also contributes to the  $[\text{Ca}^{2+}]_i$  relaxation, its contribution in mouse ventricular myocytes is less than 10%. In larger species, the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger can make a larger contribution to the lusitropic effect, as its share is about 25–30% of the total released  $\text{Ca}^{2+}$ .

There is also a long-term dispute among two groups of scientists who study ryanodine receptors (Marks group on the one hand and Valdivia and Houser group on the other) related to the physiological role of RyR phosphorylation in cardiac function [143]. Experimental data of Marks and co-authors demonstrated that enhanced phosphorylation of RyRs at S2808 in failing hearts results in an increased  $\text{Ca}^{2+}$  leak from the SR and leads to an increased arrhythmias [143,144]. The Houser and Valdivia group have shown opposite results: they found that RyR phosphorylation site S2808 does not produce significant physiological effects neither in wild type nor in infarcted mouse hearts [145]. Our simulations shows that phosphorylation of RyRs does not change  $\text{Ca}^{2+}$  sensitivity and does not produce significant physiological effect during stimulation of the  $\beta_1$ -adrenergic signaling system, the results which are in line with the data from Houser and Valdivia group.

### The Effects of the $\beta_1$ -adrenergic Signaling System on $\text{Na}^+$ Fluxes

Our model of the  $\beta_1$ -adrenergic signaling system in mouse ventricular myocytes is able to reproduce experimental data on a decrease in  $[\text{Na}^+]_i$  concentration upon activation of  $\beta_1$ -ARs (Fig. 20, [100,127]). We also estimated a contribution of the different mechanisms of the  $\text{Na}^+$  entry and extrusion from the cell, experimental data for which are not available yet. Simulations at physiological frequency 5 Hz and without application of isoproterenol suggest that about 20% of  $\text{Na}^+$  enter the cell through the fast  $\text{Na}^+$  current, 32% through the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger, and 48%



through the background mechanisms (large  $\text{Na}^+$  gradient, the  $\text{Na}^+/\text{H}^+$  exchanger, the  $\text{Na}^+/\text{HCO}_3^-$  co-transporter, etc.). With application of isoproterenol, the fraction of  $\text{Na}^+$  entry decreases for the fast  $\text{Na}^+$  current to 17%, increases to 46% for the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger, and decreases to 37% for the background mechanism. These fractions are different from those estimated for the larger species, such as rabbits [133]. For rabbits, about 22% of  $\text{Na}^+$  enter the cell through the fast  $\text{Na}^+$  current (which is similar to our estimations for mice), 60% through the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger, and 18% through the background mechanisms, suggesting the  $\text{Na}^+/\text{Ca}^{2+}$  exchanger to be the major player in the  $\text{Na}^+$  transport into the cell. Further experiments are necessary to verify  $\text{Na}^+$  fluxes structure in mouse ventricular cells without and with application of isoproterenol estimated from the presented model.

### Model Limitations

Despite that the presented model was extensively verified by the experimental data and reproduced most effects which result from stimulation of the  $\beta_1$ -adrenergic signaling system, it has some limitations. One of these limitations is that some experimental data used for the model verification were obtained from different species, such as rats, canine, and rabbits. In this respect, some of the model parameters can be adjusted to fit the data obtained from mouse ventricular myocytes, when such data becomes available. A second source of the errors in model parameters is the low accuracy of biochemical experiments, which can vary by an order of magnitude (see for example data on PKA activation by cAMP). However, investigations by Soltis and Saucerman [146] are very encouraging about this issue. They have shown that the  $\beta_1$ -adrenergic signaling system is robust, at least in steady-state, even when the model parameters change by 1–2 orders of magnitude. Third, not all model parameters are measured directly in the experiments, and, therefore, are adjusted numerically to fit the experimental data downstream in the signaling pathway. Finally, a fourth limitation comes from the availability of at least

two other,  $\beta_2$ -adrenergic and CaMKII-mediated, signaling systems that can potentially interact with the  $\beta_1$ -adrenergic system. Experimental data with mice shows that the  $\beta_2$ -adrenergic signaling system does not affect the  $\beta_1$ -adrenergic system in control and upon application of isoproterenol [7]. This phenomenon is explained by the significantly larger concentration of the inhibitory G protein,  $G_i$ , compared to  $G_s$  in mouse ventricular cells, which inhibits the stimulatory effects of the  $\beta_2$ -ARs. The effects of  $\beta_2$ -ARs can only be revealed upon additional application of pertussis toxin which suppresses the activity of  $G_i$  [7]. While the effects of the CaMKII-mediated signaling system are not taken into account in the presented model, the model of the  $\beta_1$ -adrenergic signaling system still describes reasonably well most of the available experimental data on mouse ventricular myocytes. The author considers this model as the first step in the development of a more comprehensive compartmentalized model of the adrenergic signaling system in mouse ventricular myocytes.

### Supporting Information

**Appendix S1 Model equations and parameters.**  
(PDF)

### Acknowledgments

The author would like to thank Drs. H. Abriel, S. O. Døskeland, A. El-Armouche, J. Heijman, A. N. Lopatin, L. S. Maier, M. J. Morales, R. L. Rasmusson, and J. J. Saucerman for their valuable comments related to the different subjects of this paper, Brent Wooldridge for drawing the scheme of the  $\beta_1$ -adrenergic signaling system, and Paula D. Mullins for careful reading of the manuscript.

### Author Contributions

Conceived and designed the experiments: VEB. Performed the experiments: VEB. Analyzed the data: VEB. Contributed reagents/materials/analysis tools: VEB. Wrote the paper: VEB.

### References

- Rudy Y, Ackerman MJ, Bers DM, Clancy CE, Houser SR, et al. (2008) System approach to understanding electromechanical activity in the human heart: a National Heart, Lung, and Blood Institute workshop summary. *Circulation* 118: 1202–1211.
- Schaub MC, Hefti MA, Zaugg M (2006) Integration of calcium with the signaling network in cardiac myocytes. *J Mol Cell Cardiol* 41: 183–214.
- Wachter SB, Gilbert EM (2012) Beta-adrenergic receptors, from their discovery and characterization through their manipulation to beneficial clinical application. *Cardiology* 122: 104–112.
- Ho D, Yan L, Iwatsubo K, Vatner DE, Vatner SF (2010) Modulation of  $\beta$ -adrenergic receptor signaling in heart failure and longevity: targeting adenylyl cyclase type 5. *Heart Fail Rev* 15: 495–512.
- Reincober J, Tscheschner H, Pleger ST, Most P, Katus HA, et al. (2012) Targeting GRK2 by gene therapy for heart failure: benefits above  $\beta$ -blockade. *Gene Ther* 19: 686–693.
- Shah AM, Mann DL (2011) In search of new therapeutic targets and strategies for heart failure: recent advances in basic science. *Lancet* 378: 704–712.
- Xiao RP, Zhu W, Zheng M, Chakir K, Bond R, et al. (2004) Subtype-specific  $\beta$ -adrenoceptor signaling pathways in the heart and their potential clinical implications. *Trends Pharmacol Sci* 25: 358–365.
- Heijman J, Volders PGA, Westra RL, Rudy Y (2011) Local control of  $\beta$ -adrenergic stimulation: effects on ventricular myocyte electrophysiology and  $\text{Ca}^{2+}$  transient. *J Mol Cell Cardiol* 50: 863–871.
- Kuzumoto M, Takeuchi A, Nakai H, Oka C, Noma A, et al. (2008) Simulation analysis of intracellular  $\text{Na}^+$  and  $\text{Cl}^-$  homeostasis during  $\beta_1$ -adrenergic stimulation of cardiac myocytes. *Prog Biophys Mol Biol* 96: 171–186.
- Saucerman JJ, Brunton LL, Michailova AP, McCulloch AD (2003) Modeling  $\beta$ -adrenergic control of cardiac myocyte contractility *in silico*. *J Biol Chem* 278: 47997–48003.
- Saucerman JJ, Healy SN, Belik ME, Puglisi JL, McCulloch AD (2004) Proarrhythmic consequences of a KCNQ1 AKAP-binding domain mutation: computational models of whole cells and heterogeneous tissue. *Circ Res* 95: 1216–1224.
- Yang JH, Saucerman JJ (2012) Phospholemman is a negative feed-forward regulator of  $\text{Ca}^{2+}$  in  $\beta$ -adrenergic signaling, accelerating  $\beta$ -adrenergic inotropy. *J Mol Cell Cardiol* 52: 1048–1055.
- Iancu RV, Jones SW, Harvey RD (2007) Compartmentation of cAMP signaling in cardiac myocytes: a computational study. *Biophys J* 92: 3317–3331.
- Iancu RV, Ramamurthy G, Warrior S, Nikolaev VO, Lohse MJ, et al. (2008) Cytoplasmic cAMP concentrations in intact cardiac myocytes. *Am J Physiol Cell Physiol* 295: C414–C422.
- Maguy A, Hebert TE, Nattel S (2006) Involvement of lipid rafts and caveolae in cardiac ion channel function. *Cardiovasc Res* 69: 798–807.
- Balijepalli RC, Kamp TJ (2008) Caveolae, ion channels and cardiac arrhythmias. *Prog Biophys Mol Biol* 98: 149–160.
- Harvey RD, Calaghan SC (2012) Caveolae create local signalling domains through their distinct protein content, lipid profile and morphology. *J Mol Cell Cardiol* 52: 366–375.
- Weiss S, Oz S, Benmocha A, Dascal N (2013) Regulation of cardiac L-type  $\text{Ca}^{2+}$  channel  $\text{Ca}_v1.2$  via the  $\beta$ -adrenergic-cAMP-protein kinase A pathway. Old dogmas, advances, and new uncertainties. *Circ Res* 113: 617–631.
- Balijepalli RC, Foell JD, Hall DD, Hell JW, Kamp TJ (2006) Localization of cardiac L-type  $\text{Ca}^{2+}$  channels to a caveolar macromolecular signaling complex is required for  $\beta_2$ -adrenergic regulation. *Proc Natl Acad Sci USA* 103: 7500–7505.
- Rybin VO, Xu X, Lisanti MP, Steinberg SF (2000) Differential targeting of  $\beta$ -adrenergic receptor subtypes and adenylyl cyclase to cardiomyocyte caveolae: a mechanism to functionally regulate the cAMP signaling pathway. *J Biol Chem* 275: 41447–41457.
- Scriven DRL, Asghari P, Schulson MN, Moore EDW (2010) Analysis of  $\text{Ca}_v1.2$  and ryanodine receptor clusters in rat ventricular myocytes. *Biophys J* 99: 3923–3929.
- Best JM, Kamp TJ (2012) Different subcellular populations of L-type  $\text{Ca}^{2+}$  channels exhibit unique regulation and functional roles in cardiomyocytes. *J Mol Cell Cardiol* 52: 376–387.

23. Engelhardt S, Hein L, Wiesmann F, Lohse MJ (1999) Progressive hypertrophy and heart failure in  $\beta_1$ -adrenergic receptor transgenic mice. *Proc Natl Acad Sci USA* 96: 7059–7064.
24. Milano CA, Allen LF, Rockman HA, Dolber PC, McMinn TR, et al. (1994) Enhanced myocardial function in transgenic mice overexpressing the  $\beta_2$ -adrenergic receptor. *Science* 264: 582–586.
25. Bondarenko VE, Sziget G, Bett GCL, Kim SJ, Rasmusson RL (2004) Computer model of action potential: of mouse ventricular myocytes. *Am J Physiol Heart Circ Physiol* 287: H1378–H1403.
26. Petkova-Kirova PS, London B, Salama G, Rasmusson RL, Bondarenko VE (2012) Mathematical modeling mechanisms of arrhythmias in transgenic mouse heart overexpressing TNF- $\alpha$ . *Am J Physiol Heart Circ Physiol* 302: H934–H952.
27. Bers DM (2001) Excitation-Contraction Coupling and Cardiac Contractile Force (2<sup>nd</sup> ed.). Dordrecht, The Netherlands: Kluwer Academic. 427 p.
28. Steinberg SF (2004)  $\beta_2$ -adrenergic receptor signaling complexes in cardiomyocyte caveolae/lipid rafts. *J Mol Cell Cardiol* 37: 407–415.
29. Hilal-Dandan R, Kanter JR, Brunton LL (2000) Characterization of G-protein signaling in ventricular myocytes from the adult mouse heart: differences from the rat. *J Mol Cell Cardiol* 32: 1211–1221.
30. Nikolaev VO, Moshkov A, Lyon AR, Miragoli M, Noval P, et al. (2010)  $\beta_2$ -adrenergic receptor redistribution in heart failure changes cAMP compartmentation. *Science* 327: 1653–1657.
31. Lohse MJ, Hein P, Hoffmann C, Nikolaev VO, Vilaridaga JP, et al. (2008) Kinetics of G-protein-coupled receptor signals in intact cells. *Br J Pharmacol* 153: S125–S132.
32. Freedman NJ, Liggett SB, Drachman DE, Pei G, Caron MG, et al. (1995) Phosphorylation and desensitization of the human  $\beta_1$ -adrenergic receptor: involvement of G protein-coupled receptor kinases and cAMP-dependent protein kinase. *J Biol Chem* 270: 17953–17961.
33. Göttle M, Geduhn J, König B, Gille A, Höcherl K, et al. (2009) Characterization of mouse heart adenylyl cyclase. *J Pharmacol Exp Ther* 329: 1156–1165.
34. Tang T, Gao MH, Lai NC, Firth AL, Takahashi T, et al. (2008) Adenylyl cyclase type 6 deletion decreases left ventricular function via impaired calcium handling. *Circulation* 117: 61–69.
35. Head BP, Patel HH, Roth DM, Lai NC, Niesman IR, et al. (2005) G-protein-coupled receptor signaling components localize in both sarcolemmal and intracellular caveolin-3-associated microdomains in adult cardiac myocytes. *J Biol Chem* 280: 31036–31044.
36. Ostrom RS, Insel PA (2004) The evolving role of lipid rafts and caveolae in G protein-coupled receptor signaling: implications for molecular pharmacology. *Br J Pharmacol* 143: 235–245.
37. Chen-Goodspeed M, Lukan AN, Dessauer CW (2005) Modeling of  $G_{\alpha_s}$  and  $G_{\alpha_i}$  regulation of human type V and VI adenylyl cyclase. *J Biol Chem* 280: 1808–1816.
38. Gao B, Gilman AG (1991) Cloning and expression of a widely distributed (type IV) adenylyl cyclase. *Proc Natl Acad Sci USA* 88: 10178–10182.
39. Gao X, Sadana R, Dessauer CW, Patel TB (2007) Conditional stimulation of type V and VI adenylyl cyclases by G protein  $\beta\gamma$  subunits. *J Biol Chem* 282: 294–302.
40. Zimmermann G, Taussig R (1996) Protein kinase C alters the responsiveness of adenylyl cyclases to G protein  $\alpha$  and  $\beta\gamma$  subunits. *J Biol Chem* 271: 27161–27166.
41. Post SR, Hilal-Dandan R, Urasawa K, Brunton LL, Insel PA (1995) Quantification of signaling components and amplification in the  $\beta$ -adrenergic-receptor-adenylyl cyclase pathway in isolated adult rat ventricular myocytes. *Biochem J* 311: 75–80.
42. Tepe NM, Liggett SB (1999) Transgenic replacement of type V adenylyl cyclase identifies a critical mechanism of  $\beta$ -adrenergic receptor dysfunction in the  $G_{\alpha_q}$  overexpressing mouse. *FEBS Lett* 458: 236–240.
43. Lemire I, Allen BG, Rindt H, Hebert TE (1998) Cardiac-specific overexpression of  $\alpha_{1B}$ AR regulates  $\beta$ AR activity via molecular crosstalk. *J Mol Cell Cardiol* 30: 1827–1839.
44. Richter W, Xie M, Scheitner C, Krall J, Movsesian MA, et al. (2011) Conserved expression and functions of PDE4 in rodent and human heart. *Basic Res Cardiol* 106: 249–262.
45. Bode DC, Kanter JR, Brunton LL (1991) Cellular distribution of phosphodiesterase isoforms in rat cardiac tissue. *Circ Res* 68: 1070–1079.
46. Fischmeister R, Castro LRV, Abi-Gerges A, Rochais F, Jurevičius J, et al. (2006) Compartmentation of cyclic nucleotide signaling in the heart: the role of cyclic nucleotide phosphodiesterases. *Circ Res* 99: 816–828.
47. Osadchii OE (2007) Myocardial phosphodiesterases and regulation of cardiac contractility in health and cardiac disease. *Cardiovasc Drugs Ther* 21: 171–194.
48. Mongillo M, Tocchetti CG, Terrin A, Lissandron V, Cheung YF, et al. (2006) Compartmentalized phosphodiesterase-2 activity blunts  $\beta$ -adrenergic cardiac inotropy via an NO/cGMP-dependent pathway. *Circ Res* 98: 226–234.
49. Georget M, Mateo P, Vandecasteele G, Lipskaia L, Defier N, et al. (2003) Cyclic AMP compartmentation due to increase cAMP-phosphodiesterase activity in transgenic mice with a cardiac-directed expression of the human adenylyl cyclase type 8 (AC8). *FASEB J* 17: 1380–1391.
50. Adams SR, Harootyan AT, Buechler YJ, Taylor SS, Tsien RY (1991) Fluorescence ratio imaging of cyclic AMP in single cell. *Nature* 349: 694–697.
51. Dostmann WRG, Taylor SS (1991) Identifying the molecular switches that determine whether ( $R_p$ )-cAMPS functions as an antagonist or an agonist in the activation of cAMP-dependent protein kinase I. *Biochemistry* 30: 8710–8716.
52. Lin F, Owens A, Chen S, Stevens ME, Kesteven S, et al. (2001) Targeted  $\alpha_{1A}$ -adrenergic receptor overexpression induces enhanced cardiac contractility but not hypertrophy. *Circ Res* 89: 343–350.
53. Roman BB, Goldspink PH, Spaite E, Urboniene D, McKinney R, et al. (2004) Inhibition of PKC phosphorylation of TnI improves cardiac performance in vivo. *Am J Physiol Heart Circ Physiol* 286: H2089–H2095.
54. Beavo JA, Bechtel PJ, Krebs EG (1974) Activation of protein kinase by physiological concentrations of cyclic AMP. *Proc Natl Acad Sci USA* 71: 3580–3583.
55. Dao KK, Teigen K, Kopperud R, Hodneland E, Schwede F, et al. (2006) Epacl and cAMP-dependent protein kinase holoenzyme have similar cAMP affinity, but their cAMP domains have distinct structural features and cyclic nucleotide recognition. *J Biol Chem* 281: 21500–21511.
56. Hofmann F, Beavo JA, Bechtel PJ, Krebs EG (1975) Comparison of adenosine 3': 5'-monophosphate-dependent protein kinase from rabbit skeletal and bovine heart muscle. *J Biol Chem* 250: 7795–7801.
57. Buxton ILO, Brunton LL (1983) Compartments of cyclic AMP and protein kinase in mammalian cardiomyocytes. *J Biol Chem* 258: 10233–10239.
58. Hescheler J, Kameyama M, Trautwein W, Mieskes G, Söling HD (1987) Regulation of the cardiac calcium channel by protein phosphatases. *Eur J Biochem* 165: 261–266.
59. MacDougall LK, Jones LR, Cohen P (1991) Identification of the major protein phosphatases in mammalian cardiac muscle which dephosphorylate phospholamban. *Eur J Biochem* 196: 725–734.
60. Neumann J, Boknik P, Herzig S, Schmitz W, Scholz H, et al. (1993) Evidence for physiological functions of protein phosphatases in the heart: evaluation with okadaic acid. *Am J Physiol Heart Circ Physiol* 265: H257–H266.
61. duBell WH, Gigena MS, Guatimosim S, Long X, Lederer WJ, et al. (2002) Effects of PPI/PP2A inhibitor calyculin A on the E-C coupling cascade in murine ventricular myocytes. *Am J Physiol Heart Circ Physiol* 282: H38–H48.
62. Müller FU, Lewin G, Baba HA, Boknik P, Fabritz L, et al. (2005) Heart-directed expression of a human cardiac isoform of cAMP-response element modulator in transgenic mice. *J Biol Chem* 280: 6906–6914.
63. Herzig S, Neumann J (2000) Effects of serine/threonine protein phosphatases on ion channels in excitable membranes. *Physiol Res* 80: 173–210.
64. Carr AN, Schmidt AG, Suzuki Y, del Monte F, Sato Y, et al. (2002) Type 1 phosphatase, a negative regulator of cardiac function. *Mol Cell Biol* 22: 4124–4135.
65. El-Armouche A, Wittköpper K, Degenhardt F, Weinberger F, Didić M, et al. (2008) Phosphatase inhibitor-1-deficient mice are protected from catecholamine-induced arrhythmias and myocardial hypertrophy. *Cardiovasc Res* 80: 396–406.
66. Nicolaou P, Hajjar RJ, Kranias EG (2009) Role of protein phosphatase-1 inhibitor-1 in cardiac physiology and pathophysiology. *J Mol Cell Cardiol* 47: 365–371.
67. Neumann J, Gupta RC, Schmitz W, Scholz H, Nairn AC, et al. (1991) Evidence for isoproterenol-induced phosphorylation of phosphatase inhibitor-1 in the intact heart. *Circ Res* 69: 1450–1457.
68. O'Connell TD, Ni YG, Lin KM, Han H, Yan Z (2003) Isolation and culture of adult mouse cardiac myocytes for signaling studies. *AICS Research Reports* 1: CM0005.
69. Shibata EF, Brown TLY, Washburn ZW, Bai J, Revak TJ, et al. (2006) Autonomic regulation of voltage-gated cardiac ion channels. *J Cardiovasc Electrophysiol (Suppl 1)*: S34–S42.
70. Makarewich CA, Correll RN, Gao H, Zhang H, Yang B, et al. (2012) A caveolae-targeted L-type  $Ca^{2+}$  channel antagonist inhibits hypertrophic signaling without reducing cardiac contractility. *Circ Res* 110: 669–674.
71. Chu G, Luo W, Slack JP, Tilgmann C, Sweet WE, et al. (1996) Compensatory mechanisms associated with the hyperdynamic function of phospholamban-deficient mouse hearts. *Circ Res* 79: 1064–1076.
72. Bers DM, Stüffel VM (1993) Ratio of ryanodine to dihydropyridine receptors in cardiac and skeletal muscle and implications for E-C coupling. *Am J Physiol Cell Physiol* 264: C1587–C1593.
73. Bracken N, ElKadri M, Hart G, Hussain M (2006) The role of constitutive PKA-mediated phosphorylation in the regulation of basal  $I_{Ca}$  in isolated rat cardiac myocytes. *Br J Pharmacol* 148: 1108–1115.
74. Tang M, Zhang X, Li Y, Guan Y, Ai X, et al. (2010) Enhanced basal contractility but reduced excitation-contraction coupling efficiency and  $\beta$ -adrenergic reserve of hearts with increased Cav1.2 activity. *Am J Physiol Heart Circ Physiol* 299: H519–H528.
75. Wang H, Kohr MJ, Wheeler DG, Ziolo MT (2008) Endothelial nitric oxide synthase decreases  $\beta$ -adrenergic responsiveness via inhibition of the L-type  $Ca^{2+}$  current. *Am J Physiol Heart Circ Physiol* 294: H1473–H1480.
76. Tsien RW, Bean BP, Hess P, Lansman JB, Nilius B, et al. (1986) Mechanisms of calcium channel modulation by  $\beta$ -adrenergic agents and dihydropyridine calcium agonists. *J Mol Cell Cardiol* 18: 691–710.
77. Hulme JT, Westenbroek RE, Scheuer T, Catterall WA (2006) Phosphorylation of serine 1928 in the distal C-terminal domain of cardiac  $Ca_v1.2$  channels during  $\beta_1$ -adrenergic regulation. *Proc Natl Acad Sci USA* 103: 16574–16579.

78. Kameyama M, Hescheler J, Hofmann F, Trautwein W (1986) Modulation of Ca current during the phosphorylation cycle in the guinea pig heart. *Pflügers Arch* 407: 123–128.
79. Kim SJ, Yatani A, Vatner DE, Yamamoto S, Ishikawa Y, et al. (1999) Differential regulation of inotropy and lusitropy in overexpressed  $G_{\alpha}$  myocytes through cAMP and  $Ca^{2+}$  channel pathways. *J Clin Invest* 103: 1089–1097.
80. Sako H, Green SA, Kranias EG, Yatani A (1997) Modulation of cardiac  $Ca^{2+}$  channels by isoproterenol studied in transgenic mice with altered SR  $Ca^{2+}$  content. *Am J Physiol Cell Physiol* 273: C1666–C1672.
81. Mitarai S, Reed TD, Yatani A (2000) Changes in ionic currents and  $\beta$ -adrenergic receptor signaling in hypertrophied myocytes overexpressing  $G_{\alpha_q}$ . *Am J Physiol Heart Circ Physiol* 279: H139–H148.
82. Yarbrough TL, Lu T, Lee HC, Shibata EF (2002) Localization of cardiac sodium channels in caveolin-rich membrane domains. Regulation of sodium current amplitude. *Circ Res* 90: 443–449.
83. Palygin OA, Pettus JM, Shibata EF (2008) Regulation of caveolar cardiac sodium current by a single  $G_{\alpha}$  histidine residue. *Am J Physiol Heart Circ Physiol* 294: H1693–H1699.
84. Kirstein M, Eickhorn R, Kochsiek K, Langenfeld H (1996) Dose-dependent alteration of rat cardiac sodium current by isoproterenol: results from direct measurements on multicellular preparations. *Pflügers Arch* 431: 395–401.
85. Matsuda JJ, Lee HC, Shibata EF (1993) Acetylcholine reversal of isoproterenol-stimulated sodium currents in rabbit ventricular myocytes. *Circ Res* 72: 517–525.
86. Baba S, Dun W, Boyden PA (2004) Can PKA activators rescue  $Na^{+}$  channel function in epicardial border zone cells that survive in the infarcted canine heart? *Cardiovasc Res* 64: 260–267.
87. Ono K, Fozzard HA, Hanck DA (1993) Mechanism of cAMP-dependent modulation of cardiac sodium channel current kinetics. *Circ Res* 72: 807–815.
88. Zhou J, Yi J, Hu NN, George AL Jr, Murray KT (2000) Activation of protein kinase A modulates trafficking of the human cardiac sodium channel in *Xenopus* oocytes. *Circ Res* 87: 33–38.
89. Rook MB, Evers MM, Vos MA, Bierhuizen MFA (2012) Biology of cardiac sodium channel  $Na_{v}1.5$  expression. *Cardiovasc Res* 93: 12–23.
90. Clancy CE, Rudy Y (2002)  $Na^{+}$  channel mutation that causes both Brugada and long-QT syndrome phenotypes: a simulation study of mechanism. *Circulation* 105: 1208–1213.
91. Jayasinghe ID, Cannell MB, Soeller C (2009) Organization of ryanodine receptors, transverse tubules, and sodium-calcium exchanger in rat myocytes. *Biophys J* 97: 2664–2673.
92. Wong J, Baddeley D, Bushong EA, Yu Z, Ellisman MH, et al. (2013) Nanoscale distribution of ryanodine receptors and caveolin-3 in mouse ventricular myocytes: Dilatation of t-tubules near junctions. *Biophys J* 104: L22–L24.
93. Xiao B, Tian X, Xie W, Jones PP, Cai S, et al. (2007) Functional consequence of protein kinase A-dependent phosphorylation of the cardiac ryanodine receptor: sensitization of store overload-induced  $Ca^{2+}$  release. *J Biol Chem* 282: 30256–30264.
94. Xiao B, Zhong G, Obayashi M, Yang D, Chen K, et al. (2006) Ser-2030, but not Ser-2808, is the major phosphorylation site in cardiac ryanodine receptors responding to protein kinase A activation upon  $\beta$ -adrenergic stimulation in normal and failing hearts. *Biochem J* 396: 7–16.
95. Takasago T, Imagawa T, Furukawa KI, Ogurusu T, Shigekawa M (1991) Regulation of the cardiac ryanodine receptor by protein kinase-dependent phosphorylation. *J Biochem* 109: 163–170.
96. Xiao J, Tian X, Jones PP, Bolstad J, Kong H, et al. (2007) Removal of FKBP12.6 does not alter the conductance and activation of the cardiac ryanodine receptor or the susceptibility to stress-induced ventricular arrhythmias. *J Biol Chem* 282: 34828–34838.
97. Liu L, Askari A (2006)  $\beta$ -Subunit of cardiac  $Na^{+}$ - $K^{+}$ -ATPase dictates the concentration of the functional enzyme in caveolae. *Am J Physiol Cell Physiol* 291: C569–C578.
98. Fuller W, Eaton P, Medina RA, Bell J, Shattock MJ (2001) Differential centrifugation separates cardiac sarcolemmal and endosomal membranes from Langendorff-perfused rat hearts. *Anal Biochem* 293: 216–223.
99. Fuller W, Tulloch LB, Shattock MJ, Calaghan SC, Howie J, et al. (2013) Regulation of the cardiac sodium pump. *Cell Mol Life Sci* 70: 1357–1380.
100. Despa S, Bossuyt J, Han F, Ginsburg KS, Jia LG, et al. (2005) Phospholemman-phosphorylation mediates the  $\beta$ -adrenergic effects on Na/K pump function in cardiac myocytes. *Circ Res* 97: 252–259.
101. Gao J, Mathias RT, Cohen IS, Baldo GJ (1992) Isoprenaline,  $Ca^{2+}$  and the  $Na^{+}$ - $K^{+}$  pump in guinea-pig ventricular myocytes. *J Physiol* 449: 689–704.
102. Abi-Char J, Maguy A, Coulombe A, Balse E, Ratajczak P, et al. (2007) Membrane cholesterol modulates Kv1.5 potassium channel distribution and function in rat cardiomyocytes. *J Physiol* 582: 1205–1217.
103. Ravens U, Wettwer E (2011) Ultra-rapid delayed rectifier channels: molecular basis and therapeutic implications. *Cardiovasc Res* 89: 776–785.
104. Folco EJ, Liu GX, Koren G (2004) Caveolin-3 and SAP97 form a scaffolding protein complex that regulates the voltage-gated potassium channel Kv1.5. *Am J Physiol Heart Circ Physiol* 287: H681–H690.
105. Martens JR, Sakamoto N, Sullivan SA, Grobaski TD, Tamkun MM (2001) Isoform-specific localization of voltage-gated  $K^{+}$  channels to distinct lipid raft populations: targeting of Kv1.5 to caveolae. *J Biol Chem* 276: 8409–8414.
106. Martínez-Mármol R, Villalonga N, Solé L, Vicente R, Tamkun MM, et al. (2008) Multiple Kv1.5 targeting to membrane surface microdomains. *J Cell Physiol* 217: 667–673.
107. Li GR, Feng J, Wang Z, Fermi B, Nattel S (1996) Adrenergic modulation of ultrarapid delayed rectifier  $K^{+}$  current in human atrial myocytes. *Circ Res* 78: 903–915.
108. Yue L, Feng J, Wang Z, Nattel S (1999) Adrenergic control of the ultrarapid delayed rectifier current in canine atrial myocytes. *J Physiol* 516: 385–398.
109. González de la Fuente M, Barana A, Gómez R, Amorós I, Dolz-Gaitón P, et al. (2013) Chronic atrial fibrillation up-regulates  $\beta$ 1-adrenoceptors affecting repolarizing currents and action potential duration. *Cardiovasc Res* 97: 379–388.
110. Hoffman DA, Johnson D (1998) Downregulation of transient  $K^{+}$  channels in dendrites of hippocampal CA1 pyramidal neurons by activation of PKA and PKC. *J Neurosci* 18: 3521–3528.
111. Zhang M, Fei XW, He YL, Yang G, Mei YA (2009) Bradykinin inhibits the transient outward  $K^{+}$  current in mouse Schwann cells via the cAMP/PKA pathway. *Am J Physiol Cell Physiol* 296: C1364–C1372.
112. Anumonwo JMB, Lopatin AN (2010) Cardiac strong inward rectifier potassium channels. *J Mol Cell Cardiol* 48: 45–54.
113. Vaidyanathan R, Taffet SM, Vikstrom KL, Anumonwo JMB (2010) Regulation of cardiac inward rectifier potassium current ( $I_{K1}$ ) by synapse-associated protein-97. *J Biol Chem* 285: 28000–28009.
114. Simmerman HKB, Jones LR (1998) Phospholamban: protein structure, mechanism of action, and role in cardiac function. *Physiol Rev* 78: 921–947.
115. Wolska BM (2009) Calcineurin and cardiac function: is more or less better for the heart? *Am J Physiol Heart Circ Physiol* 297: H1576–H1577.
116. Karczewski P, Bartel S, Krause EG (1990) Differential sensitivity to isoprenaline of troponin I and phospholamban phosphorylation in isolated rat hearts. *Biochem J* 266: 115–122.
117. Kuschel M, Karczewski P, Hempel P, Schlegel WP, Krause EG, et al. (1999) Ser<sup>16</sup> prevails over Thr<sup>17</sup> phospholamban phosphorylation in the  $\beta$ -adrenergic regulation of cardiac relaxation. *Am J Physiol Heart Circ Physiol* 276: H1625–H1633.
118. Li L, Desantiago J, Chu G, Kranias EG, Bers DM (2000) Phosphorylation of phospholamban and troponin I in  $\beta$ -adrenergic-induced acceleration of cardiac relaxation. *Am J Physiol Heart Circ Physiol* 278: H769–H779.
119. Lindemann JP, Jones LR, Hathaway DR, Henry BG, Watanabe AM (1983)  $\beta$ -adrenergic stimulation of phospholamban phosphorylation and  $Ca^{2+}$ -ATPase activity in guinea pig ventricles. *J Biol Chem* 258: 464–471.
120. Sulakhe PV, Vo XT (1995) Regulation of phospholamban and troponin-I phosphorylation in the intact rat cardiomyocytes by adrenergic and cholinergic stimuli: roles of cyclic nucleotides, calcium, protein kinases and phosphatases and depolarization. *Mol Cell Biochem* 149/150: 103–126.
121. Robertson SP, Johnson JD, Holroyde MJ, Kranias EG, Potter JD, et al. (1982) The effect of troponin I phosphorylation on the  $Ca^{2+}$ -binding properties of the  $Ca^{2+}$ -regulatory site of bovine cardiac troponin. *J Biol Chem* 257: 260–263.
122. Bondarenko VE, Bett GCL, Rasmusson RL (2004) A model of graded calcium release and L-type  $Ca^{2+}$  channel inactivation in cardiac muscle. *Am J Physiol Heart Circ Physiol* 286: H1154–H1169.
123. Leroy J, Abi-Gerges A, Nikolaev VO, Richter W, Lechêne P, et al. (2008) Spatiotemporal dynamics of  $\beta$ -adrenergic cAMP signals and L-type  $Ca^{2+}$  channel regulation in adult rat ventricular myocytes: role of phosphodiesterases. *Circ Res* 102: 1091–1100.
124. Mongillo M, McSorley T, Evellin S, Sood A, Lissandron V, et al. (2004) Fluorescence resonance energy transfer-based analysis of cAMP dynamics in live neonatal rat cardiac myocytes reveals distinct functions of compartmentalized phosphodiesterases. *Circ Res* 95: 67–75.
125. Tong XY, Porter LM, Liu GX, Dhar-Chowdhury P, Srivastava S, et al. (2006) Consequences of cardiac myocyte-specific ablation of  $K_{ATP}$  channels in transgenic mice expressing dominant negative Kir6 subunits. *Am J Physiol Heart Circ Physiol* 291: H543–H551.
126. Wu Y, Temple J, Zhang R, Dzhura I, Zhang W, et al. (2002) Calmodulin kinase II and arrhythmias in a mouse model of cardiac hypertrophy. *Circulation* 106: 1288–1293.
127. Despa S, Tucker AL, Bers DM (2008) Phospholemman-mediated activation of Na/K-ATPase limits [Na<sub>i</sub>], and inotropic state during  $\beta$ -adrenergic stimulation in mouse ventricular myocytes. *Circulation* 117: 1849–1855.
128. Knollmann BC, Kirchhof P, Sirenko SG, Degen H, Greene AE, et al. (2003) Familial hypertrophic cardiomyopathy-linked mutant troponin T causes stress-induced ventricular tachycardia and  $Ca^{2+}$ -dependent action potential remodeling. *Circ Res* 92: 428–436.
129. Liu N, Denegri M, Ruan Y, Avelino-Cruz JE, Perissi A, et al. (2011) Short communication: Flecainide exerts an antiarrhythmic effect in a mouse model of catecholaminergic polymorphic ventricular tachycardia by increasing the threshold for triggered activity. *Circ Res* 109: 291–295.
130. Song J, Gao E, Wang JF, Zhang XQ, Chan TO, et al. (2012) Constitutive overexpression of phosphomimetic phospholemman S68E mutant results in arrhythmias, early mortality, and heart failure: potential involvement of  $Na^{+}$ / $Ca^{2+}$  exchanger. *Am J Physiol Heart Circ Physiol* 302: H770–H781.
131. Benkusky NA, Weber CS, Scherman JA, Farrell EF, Hacker TA, et al. (2007) Intact  $\beta$ -adrenergic response and unmodified progression toward heart failure in mice with genetic ablation of a major protein kinase A phosphorylation site in the cardiac ryanodine receptor. *Circ Res* 101: 819–829.

132. Fernández-Velasco M, Rueda A, Rizzi N, Benitah JP, Colombi B, et al. (2009) Increased  $\text{Ca}^{2+}$  sensitivity of the ryanodine receptor mutant RyR<sub>2</sub><sup>R4496C</sup> underlies catecholaminergic polymorphic ventricular tachycardia. *Circ Res* 104: 201–209.
133. Despa S, Bers DM (2013)  $\text{Na}^+$  transport in the normal and failing heart – Remember the balance. *J Mol Cell Cardiol* 61: 2–10.
134. Xiao RP, Avdonin P, Zhou YY, Cheng H, Akhter SA, et al. (1999) Coupling of  $\beta_2$ -adrenoceptor to  $G_i$  proteins and its physiological relevance in murine cardiac myocytes. *Circ Res* 84: 43–52.
135. Bers DM (2002) Cardiac excitation-contraction coupling. *Nature* 415: 198–205.
136. Bondarenko VE, Rasmusson RL (2010) Transmural heterogeneity of repolarization and  $\text{Ca}^{2+}$  handling in a model of mouse ventricular tissue. *Am J Physiol Heart Circ Physiol* 299: H454–H469.
137. Bondarenko VE, Rasmusson RL (2007) Simulations of propagated mouse ventricular action potentials: effects of molecular heterogeneity. *Am J Physiol Heart Circ Physiol* 293: H1816–H1832.
138. Volders PGA, Stengl M, van Opstal JM, Gerlach U, Spätjens RLHMG, et al. (2003) Probing the contribution of  $I_{Ks}$  to canine ventricular repolarization: key role for  $\beta$ -adrenergic receptor stimulation. *Circulation* 107: 2753–2760.
139. Pogwizd SM, Schlotthauer K, Li L, Yuan W, Bers DM (2001) Arrhythmogenesis and contractile dysfunction in heart failure: roles of sodium-calcium exchange, inward rectifier potassium current, and residual  $\beta$ -adrenergic responsiveness. *Circ Res* 88: 1159–1167.
140. Yamada KA, Corr PB (1992) Effects of  $\beta$ -adrenergic receptor activation on intracellular calcium and membrane potential in adult cardiac myocytes. *J Cardiovasc Electrophysiol* 3: 209–224.
141. MacLennan DH, Kranias EG (2003) Phospholamban: a crucial regulator of cardiac contractility. *Nat Rev Mol Cell Biol* 4: 566–577.
142. Eisner D, Bode E, Venetucci L, Trafford A (2013) Calcium flux balance in the heart. *J Mol Cell Cardiol* 58: 110–117.
143. Bers DM (2012) Ryanodine receptor S2808 phosphorylation in heart failure. Smoking gun or red herring. *Circ Res* 110: 796–799.
144. Marx SO, Reiken S, Hisamatsu Y, Jayaraman T, Burkhoff D, et al. (2000) PKA phosphorylation dissociates FKBP12.6 from the calcium release channel (ryanodine receptor): defective regulation in failing hearts. *Cell* 101: 365–376.
145. Zhang H, Makarewich CA, Kubo H, Wang W, Duran JM, et al. (2012) Hyperphosphorylation of the cardiac ryanodine receptor at serine 2808 is not involved in cardiac dysfunction after myocardial infarction. *Circ Res* 110: 831–840.
146. Soltis AR, Saucerman JJ (2011) Robustness portraits of diverse biological networks conserved despite order-of-magnitude parameter uncertainty. *Bioinformatics* 27: 2888–2894.
147. Rochais F, Abi-Gerges A, Horner K, Lefebvre F, Cooper DMF, et al. (2006) A specific pattern of phosphodiesterases controls the cAMP signals generated by different  $G_s$ -coupled receptors in adult rat ventricular myocytes. *Circ Res* 98: 1081–1088.
148. Hohl CM, Li Q (1991) Compartmentation of cAMP in adult canine ventricular myocytes: relation to single-cell free  $\text{Ca}^{2+}$  transients. *Circ Res* 69: 1369–1379.