

# *Interdisciplinary Team Work*

## *Applying working methods to a math project*

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**Abstract** — In this work, we describe an interdisciplinary teaching experiment involving three subjects of the scientific area of Mathematics and a fourth one in the area of Management. Using only one project, the students developed skills, in an integrated way, in the fields of the subjects involved.

The structure of the project is described in detail. It is shown how the knowledge obtained in the different subjects is needed and how it connects together to answer the proposed challenges.

We report the progress of the students' work, the main difficulties and the skills developed during this process. We conclude with a reflection on the main problems and gains that may arise in projects of this kind.

**Keywords** — *interdisciplinarity; soft skills; team work; mathematics teaching; working methods.*

## **I. Introduction**

This paper aims to present the results of a teaching experiment performed in the Electrical Engineering – Power Systems degree of the School of Engineering –Polytechnic of Porto (ISEP). The goal of this experiment was to carry out an interdisciplinary project involving four subjects of the first year of the degree, three of which from the scientific area of Mathematics - Mathematics I (MATE1), Mathematics Laboratory I (LMAT1), Linear Algebra and Analytic Geometry (ALGAN) - and one subject in the area of Management: Working Methods in Engineering (MTENG).

In recent times, the theme of interdisciplinarity has gained popularity in different circles. Despite the skepticism in some education environments, the supporters of its application to school contexts have been increasing [1].

“Interdisciplinarity is a means to integrate knowledge and methods in the interest of problem solving” [2]. Crossing disciplinary boundaries is particularly important for a future engineer, because he will be called to solve complex problems. This requires not only crossing boundaries horizontally (across subjects) but also vertically (across experts, policymakers, practitioners, and the public) [3] [4].

The advantages of interdisciplinary studies are widely accepted by teachers and researchers. Some authors refer that interdisciplinary works use knowledge that comes from different curriculum areas that offer different perspectives on a particular problem, making the curriculum more compact and more consistent. Furthermore, interdisciplinary works provide the students with relevant, challenging and enjoyable learning experiences [1] [5].

*Chettiparamb* [1] refer that “Interdisciplinary pedagogy fosters in students a sense of self-authorship and a situated, partial and perspectival notion of knowledge that they can use to respond to complex questions, issues or problems. While it necessarily entails the cultivation of the many cognitive skills such as differentiating, reconciling, and synthesising [...] it also involves much more, including the promotion of student's interpersonal and intrapersonal learning.”

Using only one project work, we intended to create the opportunity for students to develop skills, in an integrated way, in the fields of the involved subjects. Students were challenged to perform a set of tasks by applying concepts and skills developed in the four aforementioned subjects. Specific objectives were proposed for this work in each subject.

The experiment took place during twelve weeks of the first semester of the first year of the degree.

Students were assessed by three outcomes: one report, one oral presentation with discussion and a MatLab© script. They faced initial difficulties in dealing with the interdisciplinary challenge, and with developing the soft skills required in the project. The main challenges were:

- to gain experience in teamwork as means to solve the interdisciplinary problems;
- to acquire insight in their own behavior and understand how it influences collaboration in the team;
- to acquire and understand their competence and realize how it may be used for the benefit of the team.

This led to considerable gains of learning. In this paper we will make a reflection on these gains and the benefits of carrying out a single project involving different subjects. We explore the main objectives of this interdisciplinary work, as well as the methodology and its main results.

We conclude this text with a reflection on the main lessons learned as well as with some suggestions for future multidisciplinary work involving these or other scientific areas.

## II. The Project

Interdisciplinary projects are encouraged and very welcome in the first degrees of ISEP. Using some past experiences, a group of four teachers – responsible for three subjects of the scientific area of Mathematics and a fourth one in the area of Management – proposed to the students of the Electrical Engineering – Power Systems degree an interdisciplinary work.

### A. Organizing the project

The purpose of this project was to give an integrated view of the several subjects of Mathematics, as well as to develop in students a number of soft skills that are pointed out as fundamental by the employers of graduated students.

In interdisciplinary research, success depends largely on the personality and attitudes of researchers. Useful characteristics are:

- curiosity about, and willingness to learn from other subjects;
- flexibility, adaptability, creativity;
- an open mind to ideas coming from other subjects and experiences;
- good communication and listening skills;
- an ability to bridge the gap between theory and practice;
- a good team worker.

The following additional abilities are very important:

- understanding (not necessarily in depth) across the project's main subject domains;
- understanding application areas, namely, Electrical Engineering, for project outcomes;
- respect for other subjects and some understanding of their general principles;
- focus on team work and on practical results, to overcome differences among subjects.

These abilities are highly relevant to achieve a good project management.

In addition to this, specific objectives were proposed in each subject.

In the subject of Working Methods in Engineering, the project had as objective to develop skills in the areas of:

- Project management, including planning and project control;
- Writing reports;
- Public communication;
- Teamwork.

Mathematics Laboratory I is inserted in the first semester of the first year of the Degree in Electrical Engineering - Electric Energy Systems' syllabus. It is a scientific subject of the Mathematics area that intends to provide the skills for solving typical problems in engineering algebraically and numerically, using numerical methods (see, for example, [6] and [7]) and computer algebra systems.

As main goals of this subject, it is intended that students obtain reasoning and abstraction skills in order to:

- implement methods of algebraic and numeric resolution of problems;
- model engineering problems related to the degree mathematically;
- acquire critical sense, deductive reasoning and graphic interpretation;
- be critical in the use of computer algebra software and numeric tools;
- do the integration between the nuclear subjects of Mathematics and Electrical Engineering.

As specific goals it is intended that a student should be able to:

- implement methodologies for solving problems using the algebraic and numeric tools (Matlab, Python and/or Matlab clone);
- understand the benefits and limitations of the algebraic and numeric tools (Matlab software, Python and/or Matlab clone);
- find and implement alternative methodologies to solve the problems;
- understand the several ways in which error can be introduced in the solution of the problem;
- solve equations of one variable numerically;
- use iterative methods in finding the solution sets of linear systems;
- evaluate derivatives and integrals numerically.

The subject contents are: the software introduction and error analysis; numerical methods for solving equations; methods for solving systems of equations and numerical differentiation and integration.

Mathematics I is a traditional one variable analysis subject (see, for example, [8] and [9]) with the following objectives:

- to characterize and manipulate real-valued functions in one variable;
- to use the techniques of differential calculus;
- to understand the notion of primitive of a function and to compute the primitive of functions using several methods;
- to understand the concept of definite integral and to use it to compute areas;
- to work with series of real numbers and with Taylor series, realizing its importance and its application to Engineering problems.

Linear Algebra and Analytic Geometry aims to complement and consolidate the mathematics training of students gained during their academic life and develop the abstraction and reasoning ability of students. The subjects of ALGAN also aims the development of a mathematical language and the acquisition of critical spirit. It intends to give basic training in linear algebra and analytic geometry in order to enable the creation and solving mathematical models applied to Engineering (see [10]).

After attending the subject of ALGAN, students should be able to:

- perform basic operations on matrices, compute determinants and solve matrix equations;
- use matrices and determinants in the resolution and discussion of systems of linear equations;
- identify and generate vector fields and check linear dependence on the vectors; identify linear transformations and compute the associated matrices, eigenvalues and eigenvectors;
- give analytical expressions for lines and planes; study intersections of lines and planes and identify geometrical spaces that satisfy some pre-determined conditions.

Teams of four students were formed in the beginning of the scholar year, in the classes of Mathematics Laboratory I (LMAT1). Students without LMAT1, but attending one of the other three subjects, would not have interest in participating in this project, as it needed a lot of support given in the classes of LMAT1. For these students, an alternative assessment was defined.

Each team received a project worksheet. The worksheets were not equal for all teams, but they proposed similar tasks.

*B. Planning for implementation of the tasks(weekly)*

An overview of the project milestones and tasks is shown in Table 1. Task 1 included the study of a real-valued function of one real variable and solving some equations numerically. This was performed during the four weeks of October, the first month of the project.

TABLE I. TASKS SCHEDULING (WEEKLY)

Tasks	October	November				December				January (2016)	
	During 4 weeks	1 <sup>st</sup>	2 <sup>nd</sup>	3 <sup>rd</sup>	4 <sup>th</sup>	1 <sup>st</sup>	2 <sup>nd</sup>	3 <sup>rd</sup>	4 <sup>th</sup>	1 <sup>st</sup>	2 <sup>nd</sup>
MATE 1 Task1: Real-valued function of a real variable											
LMAT 1 Task1: Solve equations numerically											
ALGAN Task2: Solve systems of linear equations											
LMAT 1 Task2: Solve systems of linear equations numerically											
MATE 1 Task3: Sequences/ Series/Integration.											
LMAT1 Task 3: Numerical integration											
Results/ display resolution: task 1											
Results/display resolution: task 2											
Results / display resolution: task3											
Report delivery											
Presentation/Discussion											

A preliminary report was delivered at the end of the second week of November. This was followed by the task of solving systems of linear equations using algebraic and numerical methods. The preliminary report of this task was delivered at the end of the first week of December.

Finally, the problem involving sequences, Taylor series and symbolic and numerical integration was addressed in the second and third weeks of December. The preliminary report about this task was delivered at the end of the third week of December. The final report was delivered in the last week of December.

*C. Main tasks developed in the project*

The first task to be developed in this project involved real valued functions of one real variable. The proposed functions were the voltages across the capacitor component and the charge/discharge of the capacitor in the RLC circuit (Fig. 1). The analytic expression involved the sum of various exponential functions. Some questions concerning real-valued functions were addressed at the beginning. Then, the students were challenged to solve some equations, obtaining, in some cases, algebraic solutions and in other cases numerical solutions. The bisection and Newton–Raphson methods were

used to solve equations numerically. In the second task it was given an electrical circuit (Fig. 2) where the Kirchoff's voltage law is applied. A system of linear equations was obtained. Then, the students were challenged to solve the system using algebraic methods such as Gaussian elimination and the Cramer's rule. Next, iterative numerical Jacobi and Gauss-Sidel methods were used. The last task concerned an integral calculus problem where symbolic integration was not possible. Therefore, the problem should be solved using Taylor series/polynomials, in order to obtain an approximation of the integral. In addition, the Simpson and trapezoidal rules were proposed to obtain the integral using numerical quadrature. We focus that these tasks led to the simultaneous use of algebraic and numerical methods.

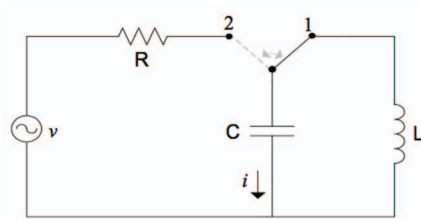


Figure 1: RLC circuit analyzed in Task 1.

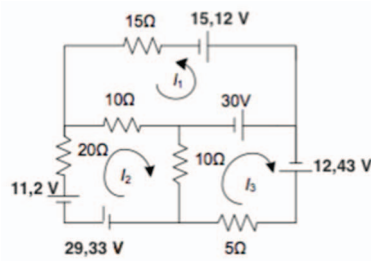


Figure 2: Electrical circuit solved in Task 2.

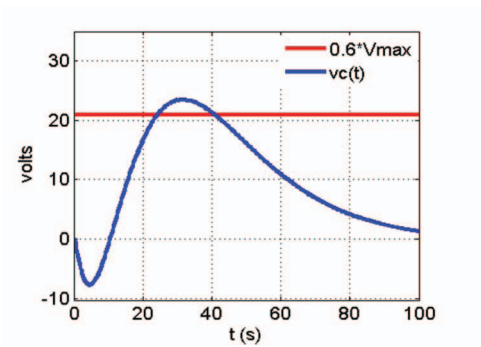


Figure 3: Graphic interpretation used in Task 1.

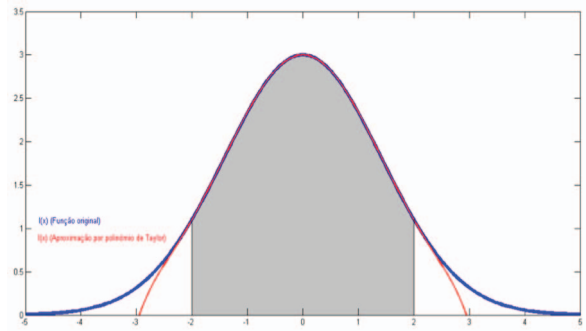


Figure 4: Numerical Integration.

We also highlight the use of the software MatLab© and its symbolic and numeric toolboxes to support the study. Furthermore, the graphical interpretation done by the students was improved by exploiting the graphical capabilities of the software. For instance, the graph presented in Fig. 3 (obtained with MatLab©) provides a better insight of the equation to be solved numerically while the graphic presented in Fig. 4 provides an insight concerning the integral to be computed.

#### D. Interdisciplinarity

The interdisciplinarity present in the project proposed to students is shown in the flowchart in Fig. 5. The system of linear equations obtained from Kirchoff's voltage law application is commonly addressed on Mathematics Laboratory I (LMAT1) and Linear Algebra and Analytic Geometry (ALGAN). Algebraic methods, such as Gaussian elimination and Cramer's rule, had been studied in ALGAN. Numerical methods, such as Jacobi and Gauss-Sidel iterative methods, were implemented in LMAT1. The issue of real-valued functions of one real variable, including the voltages across the capacitor component or the charge/discharge of the capacitor in the RLC circuit, was addressed in Mathematics I (MATE1) and in LMAT1.

The study of real valued functions was done analytically in the MATE1 subject. Some equations were solved numerically in LMAT1. The numerical methods used were the bisection and Newton-Raphson methods. Another topic involves the integration of functions without any symbolic primitive. This problem was addressed in MATE1 and LMAT1. Taylor series/polynomial were used to find an approximation of the integrand function and so to obtain an approximation of the integral. In LMAT1, the Simpson and trapezoidal rules were used for numerical integration. The management and guidance for performing the reports and presentations was carried out in the Working Methods in Engineering (MTENG) subject. This general issue had also the contribution of all participant subjects.

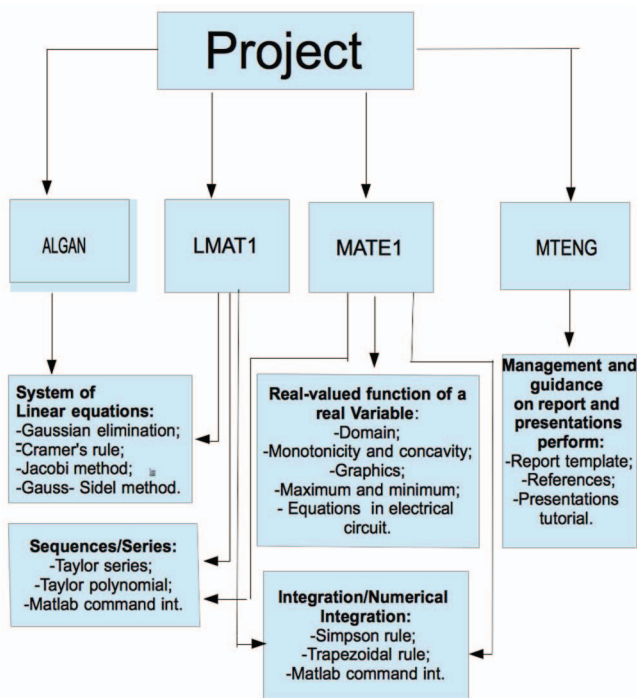


Figure 5: Topics and problems split into four different subjects

Prerequisite skills needed for the execution of the project are rather minimal. Students are required to have Mathematics education of secondary school. They should have some knowledge of basic electrical circuits. Some programming experience in Matlab or other higher-level language is helpful, but not required.

#### E. Using the e-Learning platform Moodle

The Moodle e-Learning platform was used for communication with students, providing supporting material and for the delivery of the final work. A proper space, accessible to all persons involved, was created in this platform to help the management of the process of delivery of the final work and its logistics.

#### F. Transferability to other interdisciplinary projects

This work emerged from the desire of a group of teachers and the conviction that they have - grounded in the literature - that this kind of projects brings significant gains for students. These are challenged to integrate knowledge that is often presented to them in a disintegrated form giving the idea of fragmentation of knowledge. But this type of work presents challenges, not only for students. Teachers are also challenged to think globally, to overcome the limits of their subject, to integrate its specific knowledge with other areas and to coordinate their work with other teachers.

Everyone involved in this experience - teachers and students - shares the opinion that it should be repeated and, furthermore, there should be conditions to transfer it to other contexts and to

other areas. In order to facilitate this transferability, we leave some practices that we consider essential to the success of future experiments in this context:

1. Project Planning - Phase essential to the success of the project. It should involve communication between teachers from different subjects in order to i) describe goals for each subject, ii) define tasks to be developed by students, iii) define moments and assessment tools and respective criteria, iv) prepare the project worksheet and v) set a plan of regular control meetings.

2. Project presentation to students - The project must be presented to students in detail, in the context of class, through the delivery of a project worksheet which should include i) project goals, ii) detailed tasks and deadlines iii) materials and tools necessary for the tasks implementation and iv) assessment moments, tools and respective criteria.

3. Teams definition - teams should be defined at the beginning of the work by the students.

4. Teachers monitoring - Teachers should accompany the group throughout the implementation of the project, acquainting themselves from problems that arise and supporting students to solve it.

5. Coordination of the teaching staff - It is essential that teachers talk to students well coordinated. For this purpose, project control meetings are very important.

6. Communication Platform for teachers / students - The use of a communication platform (in this case, the Moodle) seems to us essential to the success of the project.

7. Final Evaluation - It is important that, in the end of the project, teachers and students have time to evaluate the process in which they were involved and reflect on the key lessons learned and define adjustments for the project replication.

8. Presence of all teachers in the oral presentation of projects - If we want to convey the message of interdisciplinarity, it is important that teachers are an example of commitment and networking.

### III. Results and Conclusions

The results obtained by the participating students were generally positive. Students' involvement in the project was notorious. The percentage of relative involvement of each student in the project was evaluated by his partners in the group. This information was asked to students in the moment of presentation and discussion of each team work.

Students had to integrate subjects that were apparently independent. The interdisciplinarity has implied a change of students' attitudes in the search for the development of integrated knowledge.

With this kind of challenge, students had the opportunity to develop a reflexive thought to overcome difficulties and, in this way, to develop knowledge and skills.

In fact, many different skills have been developed by students throughout the execution of this project. As an example, we can point out the ability to work with others, to

solve problems and conflicts, to integrate knowledge from different fields, to write a report using the citation rules and also the ability to make public presentations. This type of work also puts great demands on the teachers involved in the project, particularly in terms of flexibility to integrate knowledge. Nevertheless, we think that the results in terms of benefits to the students justify all efforts that can be done to develop interdisciplinary work.

The results of the assessment of this project were used to evaluate students in the different subjects. The weight given to this project by each subject was different from subject to subjects. As each subject has established different goals to achieve with this interdisciplinary project, it has also defined its own assessment criteria as well as the weight of the project in the overall evaluation of the subject.

By the end of the project, students' opinions regarding the challenge they had faced was assessed using a survey in the form of a questionnaire. In this survey, students were asked to give their opinion about the nature of the project and its objectives (question 1); about their satisfaction concerning their personal involvement in the project (question 2); about the impact of the project in motivating them to learn mathematics related subjects (question 3), and about the project contribution to develop personal and team work skills (question 4). Students were also asked to provide general feedback on the project as well as to identify strengths and weaknesses. Except for this last open question, all the other questions were assessed using a Likert scale, being 1 "somewhat satisfied", and 5 "very satisfied". Thirty-six students answered the questionnaire. The average score was over 3.9 considering all the questions, reaching 4.1 in those questions where students assessed the objectives of the project, and 4.2 in the ones concerning students' opinion about the project contribution to the development of personal and team work skills (Fig. 6). As for strengths, students highlighted the relevance of the project for developing those skills and also for learning and consolidating mathematics-related subjects.

Although many of the respondent students did not mention any weakness, some pointed out the workload, and the short time period to develop the work as aspects to be improved in future editions.

Therefore, we may conclude that students recognized the importance of this project not only to develop personal and teamwork skills, but also to consolidate knowledge of the several subjects involved in the project.

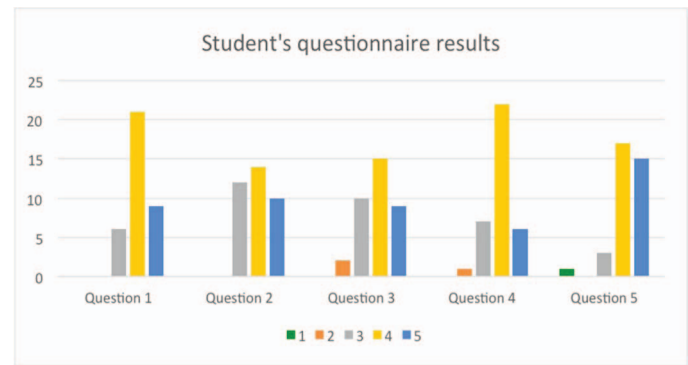


Figure 6: Students' questionnaire results

Despite the major benefits we believe this project has brought to the students, we are aware of the need to improve some aspects regarding planning and execution. At this stage, the coordination between the different involved teachers, the support provided to students during the project execution, and the management of the time students have dedicated to the project are the most challenging aspects, and those with major impact in the success of the final project.

Taking into account the characteristics of this project and the context of the degree in which it is integrated (Electrical Engineer) it is important, in future experiences, to involve the subjects of Physics and Electrical Engineering. Their absence was one of the weaknesses of this experiment.

## References

- [1] A. Chettiparamb, Inter-disciplinarity in teaching: probing urban studies. *Journal for Education in the Built Environment*, 6:1, 68-90. 2011.
- [2] S. G. Clark and R. L. Wallace, Integration and interdisciplinarity: concepts, frameworks, and education. *Policy Sciences*, 48, 233-255. 2015.
- [3] S. Lélé and R. B. Norgaard, Practicing interdisciplinarity. *BioScience*, 55, 967. 2005.
- [4] J. C. Schmidt, What is a problem?: on problem-oriented interdisciplinarity. *Poiesis Prax*, 7, 249-274. 2011.
- [5] I.-B. Păvăloiu, I. Petrescu and C. Dragomirescu, Interdisciplinary project-based laboratory works. *Procedia - Social and Behavioral Sciences*, 180, 1145-1151. 2015.
- [6] Richard L. Burden, J. Douglas Faires. *Numerical Analysis*, 9th edition, Cengage Learning, 2011.
- [7] J. Stoer and R. Bulirsch, *Introduction to Numerical Analysis*. 3<sup>rd</sup> ed. Springer, 2002.
- [8] Larson, Hostetler and Edwards, *Cálculo*, 8th edition, vol. 1, McGrawHill, 2011.
- [9] J. Stewart, *Cálculo*, 7th edition, vol. I, Cengage Learning, 2013.
- [10] G. Strang, *Introduction to Linear Algebra*, 4th edition, Wellesley-Cambridge Press, 2010.