

ABSTRACT

PAPR REDUCTION IN OFDM USING HYBRID METHOD

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Orthogonal frequency division multiplexing (OFDM) is a modulation technique which revolutionized the field of communications and paved the way for the modern-day 4G LTE communications. OFDM technique is used in both wired and wireless communications. This type of modulation technique offers low intersymbol interference and provides high data rates. Due to these advantages of OFDM it is used in various applications like 4G LTE communications, wireless networks and digital TV. Besides these advantages, a major disadvantage of OFDM system is high peak to average power ratio due to addition of sinusoidal waves in communication which result in peaks in the output and cause signal degradation. In order to reduce the PAPR, a hybrid technique which combines Hadamard transform and Hamming peak windowing is developed. This technique is compared with the PAPR results obtained for OFDM, Hamming windowing, and companding. The bit error rates of all the above methods are compared passing the OFDM signal through AWGN (additive white Gaussian noise) channel.

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PAPR REDUCTION IN OFDM USING HYBRID METHOD

BY

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CHAPTER 1: INTRODUCTION

1.1 Background

The field of communication has been part of great revolution in the later parts of twentieth century. It has switched from wired communications to wireless communications. Wireless communication started with the introduction of photo phone by Alexander Graham Bell and has come so far to smart phones used today. Wireless communications are used in many fields such as satellite communications, telephony, medical and military.

The hierarchy of the wireless communications starts with the 2G (2nd generation) wireless communication systems such as GSM (global system for mobile communications), CDMA (code division for multiple access), GPRS (general packet radio service) and EDGE (enhanced data for GSM revolution). From the above standards GSM and CDMA were used for mobile calling with voice data rate of 10 kbps and GPRS and EDGE were used for internet access with data rates ranging from 50 kbps to 200 kbps. The need for high data rates led to the introduction of 3G (3rd generation) wireless communication which offers data rates as high as 384 kbps to 30 mbps. CDMA forms the base for the 3G communications, which have various wireless standards such as WCDMA (wideband CDMA), CDMA 2000 and HSDPA/HSUPA (high-speed down link/uplink packet access). The desire for more bandwidth and data rates led to the development of the 4G (4th generation) communications which have wireless standards such as LTE (long-term evolution) and WIMAX (worldwide interoperability for microwave access) and offer data rates from 100 -200 mbps.

Orthogonal frequency division multiplexing (OFDM) is the modulation technique used to realize the 4G standards. In the OFDM scheme of modulation a single carrier is divided into subcarriers to carry information. The sub carriers are closely spaced and orthogonal to each other.

The subcarriers are modulated using IFFT (inverse fast Fourier transform) at the transmitter and demodulated using FFT (fast Fourier transform) which is very simple compared to bank of modulators and demodulators in MCM (multicarrier modulation) systems, which reduces the complexity of system in OFDM. The introduction of cyclic prefix in OFDM system reduces ISI (intersymbol interference).

Besides the advantages of OFDM systems such as low complexity, better spectral efficiency and low intersymbol interference, one major setback is high peak to average power ratio which arises due to the peaks in the output due to constructive addition of sinusoidal signals.

1.2 Problem Statement

PAPR is the ratio between the instantaneous powers to the average powers of the signals in the OFDM systems. PAPR occurs during the preprocessing phase of the OFDM where the signals are enhanced and they add up constructively to produce peaks and deviate from average power. PAPR occurs in multicarrier system if different subcarriers are out of phase with each other; at that instant when all the points achieve maximum value and add up constructively, this leads to the peaks in the output envelope of the OFDM system. This drives the power amplifier into saturation and causes intercarrier interference. High PAPR leads to the application of the

high-power amplifiers which increases the complexity of the system. There are many methods for the reduction of PAPR such as clipping and companding, which degrades the bit error rate and introduces self-interference. Hence a hybrid model is developed combining the Hadamard transform and advanced peak windowing to reduce PAPR significantly. The hybrid model is compared with companding and windowing in this thesis.

1.3 Thesis Structure

This thesis is organized as follows

- Chapter 2 explains basic communication systems. The basic OFDM system and its advantages are discussed.
- Chapter 3 discusses peak to average power ratio (PAPR) problem and its effects on OFDM systems. CCDF function used to represent PAPR is also discussed
- Chapter 4 briefly describes the technique of companding.
- Chapter 5 describes the hybrid model which includes the description of Hadamard transform and advanced peak windowing.
- Chapter 6 contains the simulation parameters and results of PAPR reduction techniques mentioned in Chapters 4 and 5.
- Chapter 7 concludes the thesis and suggests future work .

CHAPTER 2: OFDM SYSTEM

Efficient utilization of a communication system depends on the efficient utilization of the signal bandwidth. The quest for the effective utilization of the channel bandwidth led to the birth of OFDM systems. The idea for the implementation of OFDM systems evolved from the traditional FDM technique.

2.1 Frequency Division Multiplexing

FDM technique is that in which a single channel is divided into various subchannels and each subchannel is modulated to separate symbol, after which it undergoes frequency multiplexing where each symbol is assigned different carrier frequencies (Figure 2.1). These carrier systems are aligned such that they do not overlap with each other by inserting guard bits, i.e., empty spectral regions which are placed in between sub carriers such that they do not overlap with each other with the help of filters at the receiver.

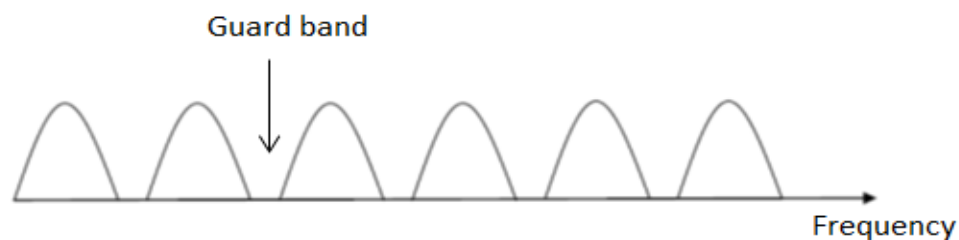


Figure 2.1 Spectrum of frequency division multiplexing system

The major drawback of frequency division multiplexing is poor spectral efficiency of system compared to the single wideband transceiver due to the addition of the guard bits. Besides this the implementation of the system is complex and requires high implementation expenditure. This wideband scheme is prone to inter-symbol interference caused by distortion in the frequency band.

2.2 Single Carrier Communication System

In a single carrier communication system, entire bandwidth is occupied by a single carrier.

Let us consider the channel bandwidth as 'B' and symbol time as 'T'.

$$\text{Symbol time (T)} = 1/B$$

$$\text{Symbol rate} = B$$

In a single carrier system one symbol is transmitted for every 'T' sec.

2.3 Multicarrier Modulation

In multicarrier modulation, a single carrier is divided into 'N' subcarriers. Each subcarrier is equally spaced with an interval of B/N . Each subcarrier carries a data stream so N subcarriers carries 'N' data streams (Figure 2.2).

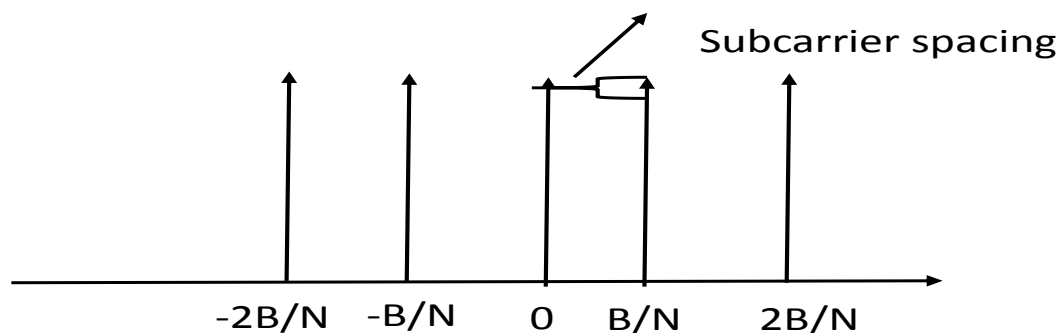


Figure 2.2 Schematic of sub carrier mapping

2.3.1 Multicarrier Transmission and Reception

In multicarrier transmission phase, symbols are fed to serial to parallel converter bank of modulators are employed to map N symbols onto N subcarriers and all the subcarriers are fed to summer to produce a composite signal (Figure 2.3).

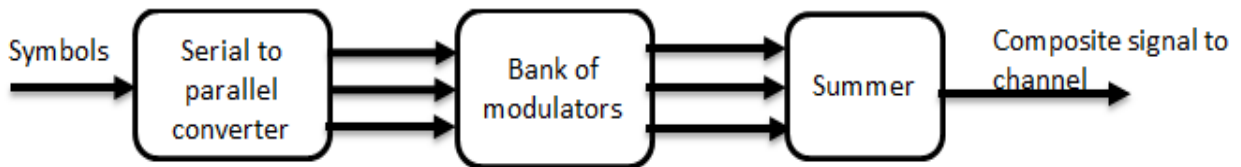


Figure 2.3 Block diagram of multicarrier transmitter

In the receiver phase the composite signal is fed to repeaters and demodulated by using bank of demodulators. After demodulating the symbols are converted to serial using multiplexer (Figure 2.4).

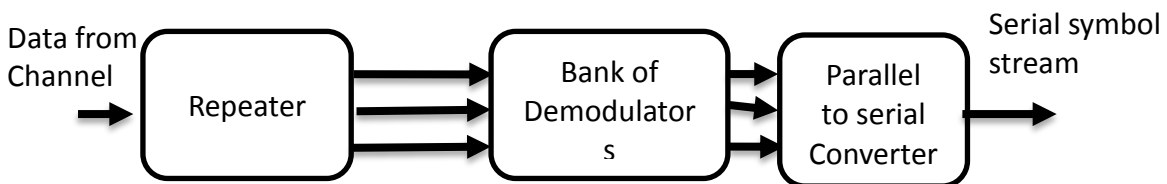


Figure 2.4 Block diagram of multicarrier receiver

2.4 Orthogonal Frequency Division Multiplexing

The idea of OFDM was developed from the publications of Weinstein and Ebert in 1970 [1]. According to them, a composite signal which is obtained from the multicarrier system can be obtained by using IDFT and DFT at the transmitter and receiver respectively instead of bank of modulators and demodulators. This reduces the complexity of the system and decreases costs for implementation.

OFDM system is a special case of multicarrier systems in which a single carrier is divided into large number of closely spaced orthogonal subcarriers. Data is transmitted on different parallel data streams with low signal rate. The total signal rate of the system the same as single carrier system.

2.4.1 OFDM Transmitter

In the OFDM transmission bits are fed to serial to parallel converter. The de-multiplexed bits are modulated using different modulation schemes like quadrature amplitude modulation, phase shift keying, quadrature phase shift keying, binary phase shift keying and the modulated symbols are mounted on subcarriers. The sub carriers undergo inverse fast Fourier transform and pass through the multiplexer which converts parallel data streams to serial data. Serial data is passed through the channel (Figure 2.5).

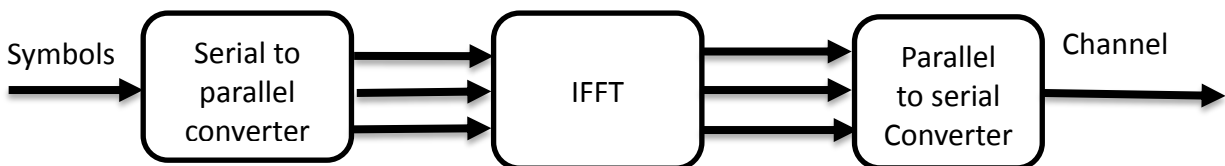


Fig 2.5 Schematic of OFDM transmitter

2.4.2 OFDM Receiver

In the OFDM receiver the data which comes from the channel is converted to parallel data using de-multiplexer. The de-multiplexed data undergoes fast Fourier transform operation to coherently detect the symbols on each subcarrier. The detected symbols received which are in parallel are converted to serial using a multiplexer. The serial data is received at the mobile station by the user (Figure 2.6).

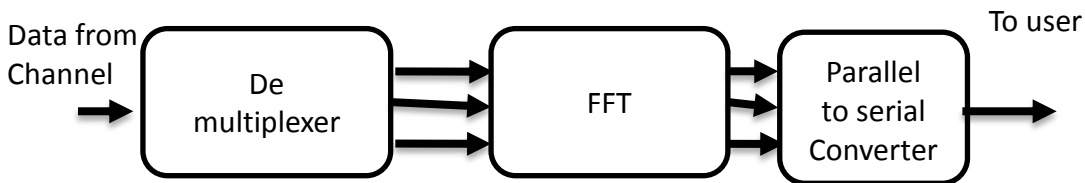


Fig 2.6 Schematic of OFDM receiver

In OFDM the subcarriers are closely spaced and orthogonal. The condition of orthogonality is very important in transmission of the symbols in OFDM. When the subcarriers are closely spaced and overlapping there is chance for the carrier frequency offset. Presence of frequency offset can introduce severe distortions in an OFDM system and lead to the loss of orthogonality among sub carriers. The overlapping of subcarriers may lead to the intersymbol interference. This problem introduces the concept of cyclic prefix in an OFDM system.

2.5 Cyclic Prefix

In OFDM transmission system cyclic prefix is used to ensure orthogonality of subcarrier signals even in multipath channel. The composite transmitted symbol or the OFDM symbol $\{x(0), x(1), \dots, x(N-1)\}$ corresponds to the IFFT of $X(0), X(1), \dots, X(N-1)$ transmitted at rate B .

The previous OFDM symbol consists of input symbols and current OFDM symbol comprises input symbols. Consider frequency selective channel which can be modeled as multipath channel or FIR filter $h(0), h(1), \dots, h(L-1)$ with L taps. Initial received signals corresponding to current OFDM symbol block are affected by ISI from previous OFDM block as shown in Figure 2.7.

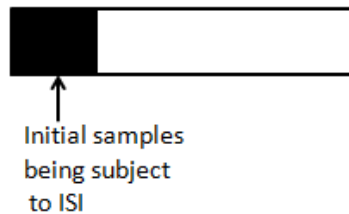


Figure 2.7: Intersymbol interference due to multipath fading

The initial samples are being subject to ISI as there is interference from previous OFDM symbol. To overcome this is problem we use cyclic prefix by taking the last 'L' data symbols from the current OFDM symbol and prefixing it as shown below:

$$x(N-L+1), x(N-L), \dots, x(N-1) \quad x(0), x(1), x(2), \dots, x(N-L+1), x(N-L), \dots, x(N-1)$$

The received symbols $y(0), y(1), \dots, y(N-1)$ are free from ISI after applying cyclic prefix (Figure 2.8). So by prefixing current OFDM symbol we have removed ISI from previous OFDM symbol. This can also be seen as circular convolution as 'x' is circularly shifted.

$$Y(k) = H(k) * X(k) \dots \dots (2.1)$$

where $Y(k)$ is received symbol across k^{th} subcarrier, $H(k)$ is channel coefficient corresponding to k^{th} subcarrier and $X(k)$ are modulated information symbols (QAM, PSK, BPSK etc.) loaded onto k^{th} subcarrier.

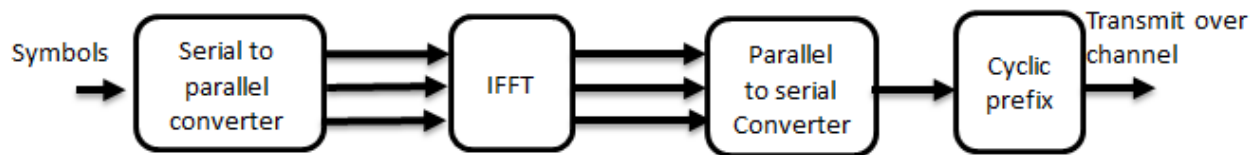


Fig 2.8 OFDM transmitter with cyclic prefix

The output is therefore channel multiplied by symbol coefficient. Hence the frequency selective channel is converted into a group narrowband flat fading channel with one channel across each sub carrier.

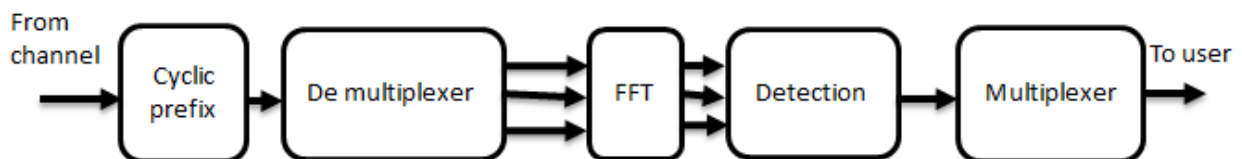


Fig 2.9 OFDM Receiver with cyclic prefix

A simple detection scheme can now be employed for $X(k)$ using zero forcing (ZF), minimum mean squared error equalizer (MMSE) or matched filter. The length of cyclic prefix should be greater than delay spread of channel. Since we are repeating the symbol, there is low transmitter efficiency.

Hence as N increases, the loss in efficiency becomes closer to zero and only a smaller fraction is affected by ISI, but OFDM symbol time also increases, leading to decoding delay of the system. In order to overcome multipath fading, cyclic prefix time should be more than the delay spread.

2.6 Advantages of OFDM

- OFDM system has overlapping orthogonal subcarriers compared to multicarrier systems which have guard bits separating them so it uses spectrum efficiently.
- In OFDM a frequency selective channel is converted to parallel flat fading channels which increases transmission rate.
- Intersymbol interference is removed by adding cyclic prefix.
- In OFDM we use FFT operation which coherently detects the bits which makes channel equalization simple compared to multicarrier systems which use bank of demodulators.

2.7 Drawbacks of OFDM

- Carrier frequency offset can introduce severe distortion in OFDM system resulting in loss of orthogonal behavior among subcarriers [2].
- The high peak to average power ratio (PAPR) of transmitted signals reduces the system efficiency and affects the sensitivity of power amplifier which increases the need for high-power amplifiers which in turn increases system cost.

2.8 Applications of OFDM

OFDM has been adopted in many wireless communication standards listed below [3]:

- IEEE 802.11a/g/n (Wi-Fi) Wireless LANs
- IEEE 802.15.3a Ultra Wideband (UWB) Wireless PAN
- IEEE 802.16d/e (WiMAX), WiBro, and HiperMAN, Wireless MANs
- IEEE 802.20 Mobile Broadband Wireless Access (MBWA)
- DVB (Digital Video Broadcast), DAB (Digital Audio Broadcast) systems
- Downlink of 3GPP UMTS, 3GPP LTE (Long-Term Evolution), and 4G communication systems.

CHAPTER 3: PEAK TO AVERAGE POWER RATIO (PAPR)

3.1 PAPR Definition

PAPR stands for peak to average power ratio. It is the ratio between instantaneous powers to average power represented as follows:

$$\text{PAPR} = \frac{\text{Instantaneous or peak power}}{\text{average power}} \dots\dots\dots (3.1)$$

In an OFDM system multiple subcarriers carry data and a composite signal is generated by addition of data signals from each sub carrier. Peak to average power ratio increases with the number of subcarriers. When signals from each sub carrier are added it may lead to high peak power and it deviates from the average power; when signals add up constructively it leads to peaks which increase the PAPR value. High PAPR is undesirable in OFDM systems.

3.2 Effects of PAPR in OFDM:

High PAPR has following effects on OFDM systems:

- In OFDM when the peak power deviates from the average power significantly the signal level moves outside dynamic linear range of the power amplifier and it is driven into saturation region. This leads to intercarrier interference.
- Intercarrier interference leads to loss of data bits and thereby reduces the system efficiency.

- In order to overcome the high PAPR we have to employ high-power amplifiers which increase system costs.
- It reduces efficiency of RF power amplifiers as they have to operate with large backoffs.
- It increases the complexity of the multiplexers and de-multiplexers.

PAPR in OFDM is characterized using CCDF function.

3.3 CCDF Function:

CCDF is complementary cumulative distribution function. CCDF representation of OFDM gives information to the user about the probability by which the peak value exceeds the threshold. CCDF is denoted as:

$$F_X(x)=P(X>x).....(3.2)$$

Where X denotes PAPR, x is threshold, $F_X(x)$ is distribution function. CCDF plot of an OFDM system is shown in Figure 3.1

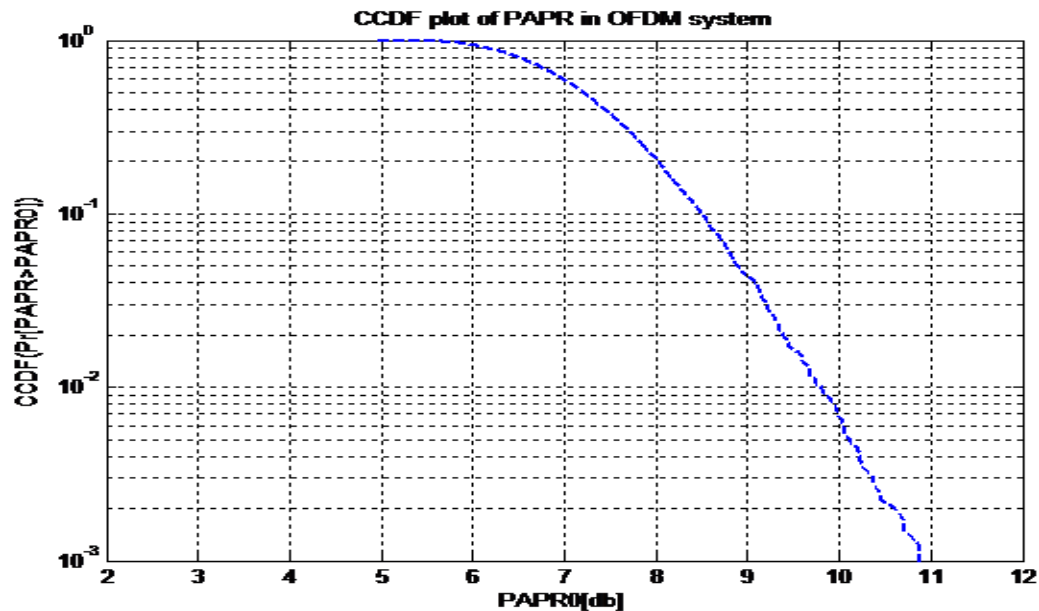


Figure: 3.1 CCDF plot of PAPR

3.4 Factors Influencing PAPR

The factors that influence PAPR are listed below [4]:

- PAPR varies with different modulation schemes used like BSP, QPSK, QAM, etc., but the difference between them is very small. Hence modulation scheme doesn't have a huge influence on PAPR as shown in Figure 3.2.
- PAPR increases as the number of subcarriers increase. This can be seen from the equation CCDF equation of PAPR which follows chi-squared distribution. Simulation results below show the variation of PAPR with different values of N as shown in Figure 3.3.

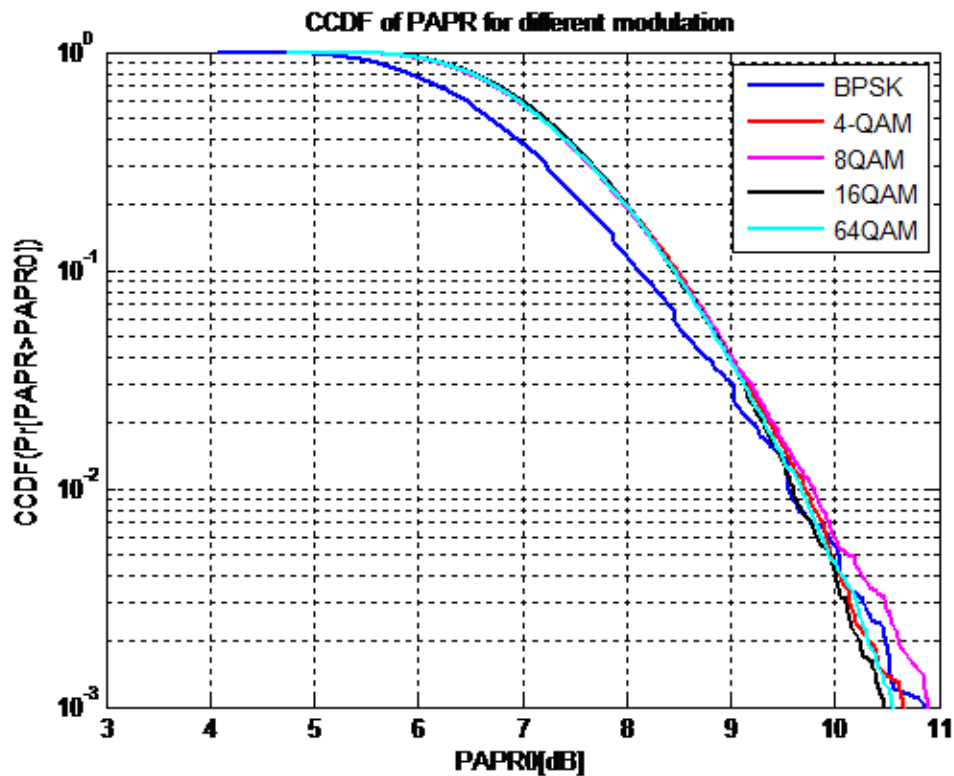


Figure 3.2: Comparison of PAPR reduction for different modulation schemes

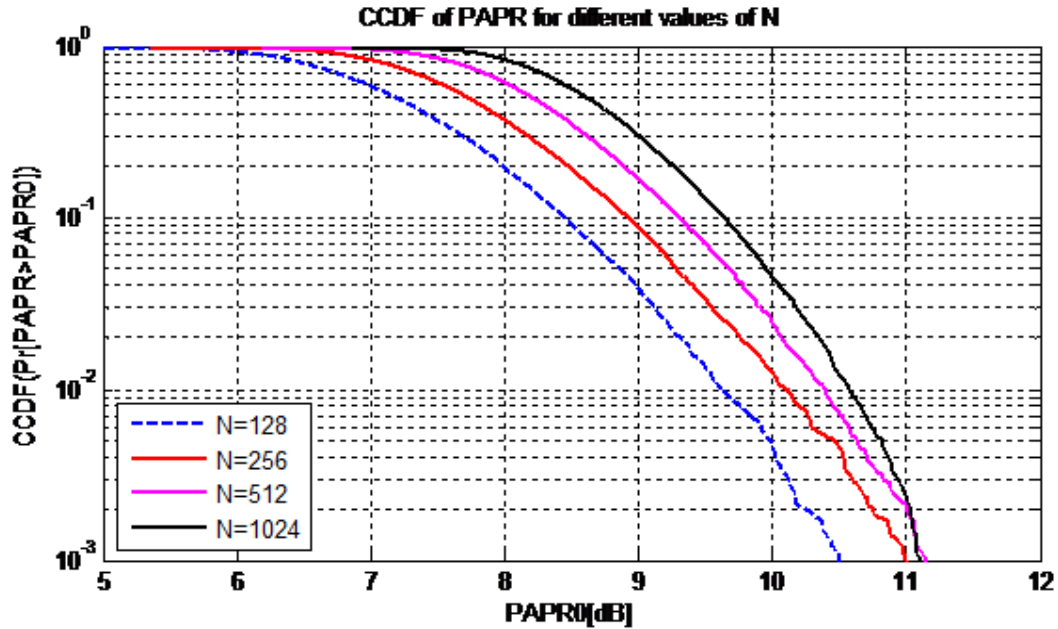


Figure 3.3: Comparison of PAPR reduction for different values of N

3.5 PAPR Reduction Techniques

Many techniques have been proposed to reduce the PAPR problem in OFDM. They are classified into different approaches as follows:

- Signal distortion technique
- Coding technique
- Scrambling technique

3.5.1 Signal Distortion Techniques

Signal distortion techniques distort the signal. Signal distortion techniques include clipping, filtering, companding and windowing.

Clipping is the simplest of distortion methods where the signal peaks are clipped are beyond a certain threshold. The drawback of clipping is the loss of the signal information.

Filtering is a technique where the signal is passed through a filter. Only frequencies which are in pass band range of filter are passed and other frequencies are attenuated. Filtering also has the same disadvantage as clipping where information is lost.

Companding is a technique where the signal is compressed and sent. This method may induce self-interference in the system and may lead to loss of information bits.

Windowing is a method where the signal is passed through the windows such as rectangular, Kaiser, Hanning and Hamming window; the major drawback of windowing is the signal deteriorates with increase of window size. The system also fails when the peaks exceed half of window size.

To overcome the drawbacks of windowing technique where the entire envelope is multiplied with the window, an alternate method of peak windowing was proposed. In the peak windowing method when the signal exceeds its threshold then it is multiplied with the window. This method improves the margin of signal degradation.

CHAPTER 4: PAPR REDUCTION IN OFDM USING COMPANDING

PAPR in OFDM system can be reduced by using companding transform. In the method of companding the data is compressed using a compander at the transmitter and expander at the receiver where the signals are recovered.

There are many companding methods like U law companding and A law companding.

4.1 U Law Companding

In the U law companding, a compressor is used at the transmitter end after the IFFT phase and an expander is used at the receiver end before the FFT process to expand the compressed signal from the channel. U law coefficient gives information about the extent of companding done to the signal.

4.1.1 Transmission Phase:

The input signal is converted from serial to parallel and mapped using 4 QAM constellations. The mapped data is mounted on parallel subcarriers and sent to IFFT phase. The input signal after the IFFT phase passes through companding. The transformed signal after the IFFT phase as follows:

$$C\{x(n)\} = \frac{vx(n)}{\ln(1+u)|x(n)|} \ln\left(1 + \frac{u}{v}|x(n)|\right) \dots \dots \dots (4.1)$$

where $x(n)$ is the input signal, v is the average amplitude of the signal and u is the companding factor.

The companding transform should satisfy following conditions for the implementation:

$$E(|s(n)|^2) = E(|x(n)|^2)$$

$$|s(n)| \geq |x(n)| \text{ when } |x(n)| \leq v$$

$$|s(n)| \leq |x(n)| \text{ when } |x(n)| \geq v$$

4.1.2 Receiver Phase

The signal which comes from the transmitter phase passes through the channel and at the receiver the signal undergoes inverse operation to that of transmitter. The signal at the receiver after inverse companding transform is:

$$C'\{x(n)\} = \frac{vr(n)}{u|r(n)|} \left[\exp\left(\frac{|r(n)| \ln(1+u)}{v} - 1\right) \right] \dots \dots \dots (4.2)$$

where $x(n)$ is the input signal and v is the average amplitude of the signal.

Companding is a decent method for reducing PAPR; however, there are major disadvantages using the method: signal completely loses its shape from the transmitted signal at the receiver end, which leads to loss in the information.

In Figure 4.1, the symbol from the transmitter is converted from serial to parallel and then undergoes inverse fast Fourier transform which converts the frequency domain signal to time domain and then the signal undergoes companding and passes through the AWGN channel.

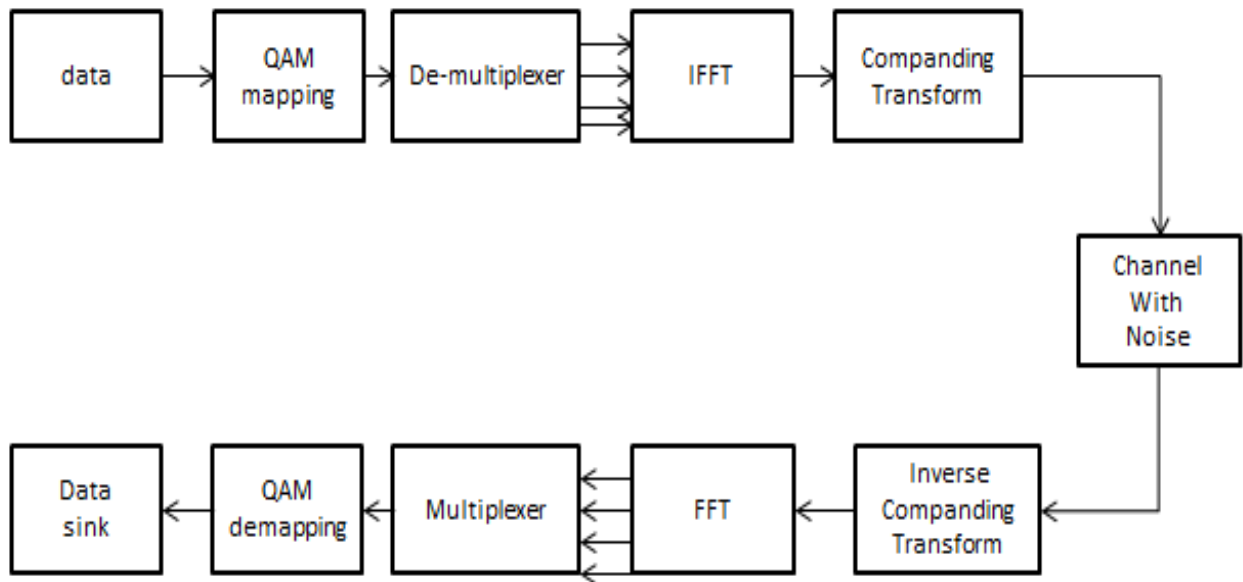


Fig 4.1 Block diagram of PAPR reduction of OFDM using companding

At the receiver the signal from the channel undergoes inverse companding and converts from frequency domain to time domain using fast Fourier transform. The time domain signal is converted from parallel to serial using multiplexer and sent to the receiver.

4.2 Simulation Steps

- As a part of this thesis, PAPR characteristics of the OFDM using companding have been studied.

- In the simulation 128 symbols are mapped on to 16 sub carriers using 4 QAM modulations and are IFFT sampled.
- The OFDM signal after IFFT undergoes companding with a companding factor ($u=2$).
- The signal after companding passes through an AWGN channel which then is expanded using inverse companding transform at the receiver.
- The signal after compression is 128 FFT sampled and sent to the receiver.

CHAPTER 5: HYBRID MODEL FOR PAPR REDUCTION IN OFDM

In this section we discuss the hybrid model for PAPR reduction in OFDM using Hadamard transform and Hamming peak windowing. Before discussing the model we will discuss the Hadamard transform and Hamming peak windowing.

5.1 Hadamard Transform:

Hadamard transform is also known as Walsh-Hadamard transform. It transforms 2^n real numbers or complex numbers into 2^n real numbers using a normalizing factor. Hadamard transform is done using a Hadamard matrix, which is an orthogonal matrix of order $2^m * 2^n$ which consists of 1 and -1 as its elements. The Hadamard matrix of order $2*2$ is given as follows:

$$H_1 = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \dots\dots\dots (5.1)$$

The generalized equation can be written as:

$$(H_n) = \frac{1}{2^{\frac{n}{2}}} (-1)^{m.n} \dots\dots\dots (5.2)$$

where 'm' and 'n' are the subscripts of the matrix, m.n is the bitwise dot product of elements of m, n.

The reason for the use of the Hadamard transform is that Hadamard matrix has one similar characteristic with OFDM, orthogonality. The elements in the Hadamard matrix are orthogonal to each other.

$$H^*H^T=I.....(5.3)$$

where H is the Hadamard matrix, H^T is transpose of the Hadamard matrix and I is the Identity matrix.

The input signal at the transmitter which is mapped and modulated is transformed using Hadamard transform before the IFFT sampling and at the receiver the signal is recovered using inverse Hadamard transform which converts Hadamard transformed signal back to the original signal. Inverse Hadamard transform is performed after FFT sampling at the receiver. Hadamard matrix is used in the proposed method to reduce the input correlation of the input signal which reduces the peaks at the transmission. Reduction of peaks at the transmitter reduces the peak to average power ratio.

5.2 Peak Windowing:

Peak windowing is one of the signal distortion techniques which are used for the PAPR reduction in OFDM. It is extensively used in the PAPR reduction applications due to its advantages over the other signal distortion techniques like clipping, companding and windowing.

This method evolved from the idea of the windowing. Peak windowing method overcomes the drawback of the conventional method by identifying the instantaneous peaks within the signal and suppressing them to threshold.

Peak windowing can be realized as the product of the window function and input signal.

Let us consider the peak windowed signal as $X(n)$:

$$X(n) = w(n) \cdot x(n) \dots\dots\dots(5.4)$$

where $w(n)$ is the window function (i.e., window function can be any window like Hamming window, Hanning window, Kaiser, etc.) and $x(n)$ is the input signal.

In advanced peak windowing method the above equation is slightly modified using the weighing coefficient. Now the equation (5.4) becomes

$$X(n) = s(n) \cdot x(n) \dots\dots\dots (5.5)$$

where $s(n)$ is the product of the weighing factor and window function:

$$s(n) = y(n) \cdot w(n) \dots\dots\dots(5.6)$$

$y(n)$ is the weighing factor and $w(n)$ is the window function.

To apply the scaling factor $s(n)$ the input signal value should be set to the threshold so that window function can be applied to it to reduce the peaks.

5.3 Hybrid Model

Hybrid model of PAPR reduction in OFDM uses both Hadamard transform and advanced peak windowing.

5.3.1 Hybrid Model Transmitter

At the transmitter the input signal is mapped onto the subcarriers and then modulated using 4 QAM or QPSK modulation technique. The QPSK modulated signal is Hadamard transformed before IFFT operation. The signal which is Hadamard transformed is then IFFT sampled. IFFT sampling converts the signal from the frequency domain to the time domain. The signal in time domain undergoes Hamming peak windowing. The peak windowed signal passes through AWGN (additive white gaussian noise) channel.

5.3.2 Hybrid Model Receiver:

The time domain windowed signal from the channel is converted back to frequency domain by FFT operation at the receiver. The signal is decoded at the receiver using inverse Hadamard transform at the receiver. Now the signal is demapped and demodulated. The demodulated signal is given to the base station.

The block diagram for the hybrid scheme is shown in Figure 5.1.

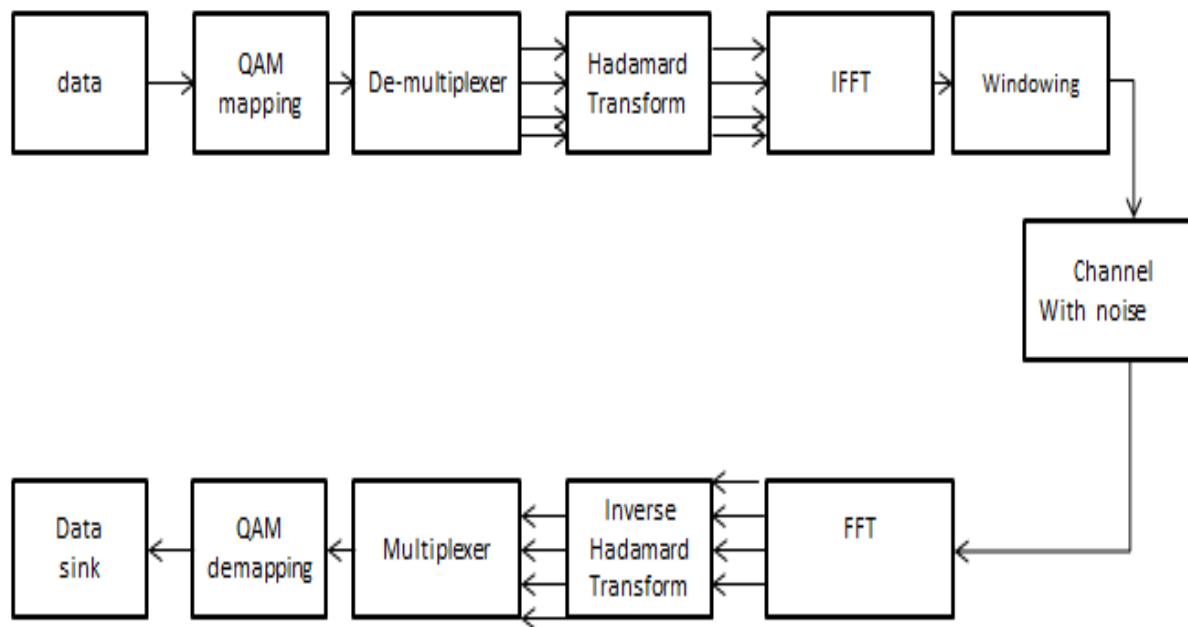


Fig 5.1 Block diagram of hybrid model

The algorithm for the hybrid model implementation is as follows:

Let $x(n)$ be the input signal. $Y(n)$ is the transformed signal

$$Y(n) = H \cdot x(n) \dots \dots \dots (5.7)$$

where H is Hadamard matrix.

- The hadamard transformed data which is IFFT sampled becomes

$$Y(n) = [y(1) \ y(2) \ y(3) \ \dots \ y(n)] \dots \dots \dots (5.8)$$

- The IFFT sampled signal undergoes Hamming peak windowing. A certain threshold is set based on the mean of the total signal samples. When the signal exceeds the threshold then it is multiplied with the window function.

- If $Y(n) > \text{threshold}$ then $Y(n) = y(n) * w(n)$

where $w(n)$ is window function ,i.e., Hamming window function in this thesis.

$$\text{Else } Y(n) = y(n)$$

- The received signal is FFT sampled; let the received signal be $r(n)$:

$$Z = \text{FFT}(r(n)) \dots \dots \dots (5.9)$$

CHAPTER 6: SIMULATION RESULTS AND COMPARISON

The PAPR reduction performance of OFDM systems using Companding techniques and hybrid techniques discussed in Chapters 4 and 5 were simulated and analyzed using MATLAB R2012b.

6.1 Companding Techniques

In the simulation of companding method of PAPR reduction of OFDM at the transmitter, 128 symbols are mapped onto the 16 subcarriers and modulated using 4 QAM or QPSK modulation. The modulated subcarriers undergo inverse fast Fourier transform. The IFFT sampled signals are sent to compander where they are compressed with companding factor of $2(u=2)$ and then passed to the AWGN channel. The signal from AWGN channel at the receiver undergoes inverse of companding operation and it is FFT sampled. The FFT-sampled signal is converted from parallel to serial to transmit it to the receiver. The PAPR characteristics are plotted using CCDF function. The PAPR characteristics are compared with that of OFDM, windowing and Hadamard transform.

6.2 Hybrid Method:

In the simulation of companding method of PAPR reduction of OFDM at the transmitter the symbols are converted from serial to parallel then 128 symbols are mapped onto the 16 subcarriers and modulated using 4 QAM or QPSK modulation. The modulated subcarriers undergo Hadamard transform. They are multiplied with Hadamard matrix. The Hadamard-transformed symbols are IFFT sampled and then passed to the AWGN channel. The signal from

AWGN channel at the receiver undergoes inverse of operation. The symbols are FFT sampled and they undergo inverse hadamard transform. The symbols then are converted from parallel to serial data. The PAPR characteristics are plotted using CCDF function. The PAPR characteristics are compared with that of OFDM, companding, windowing and hadamard transform, plotted in Figures 6.1-6.3.

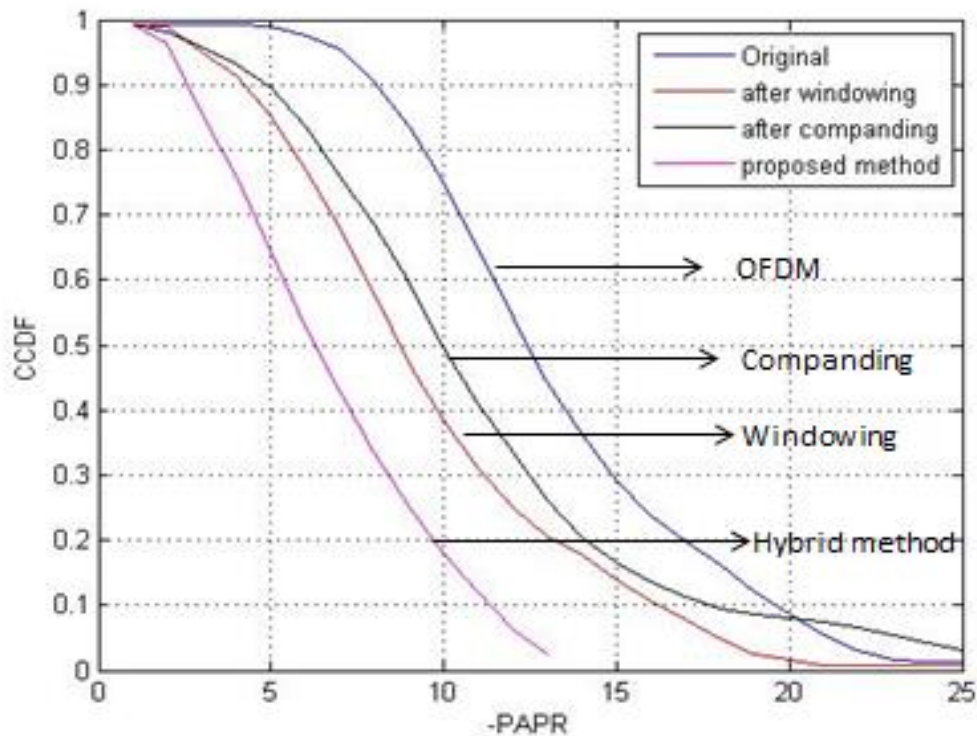


Figure 6.1: Comparison of PAPR reduction for different schemes for 128 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=128

Modulation: 4 QAM

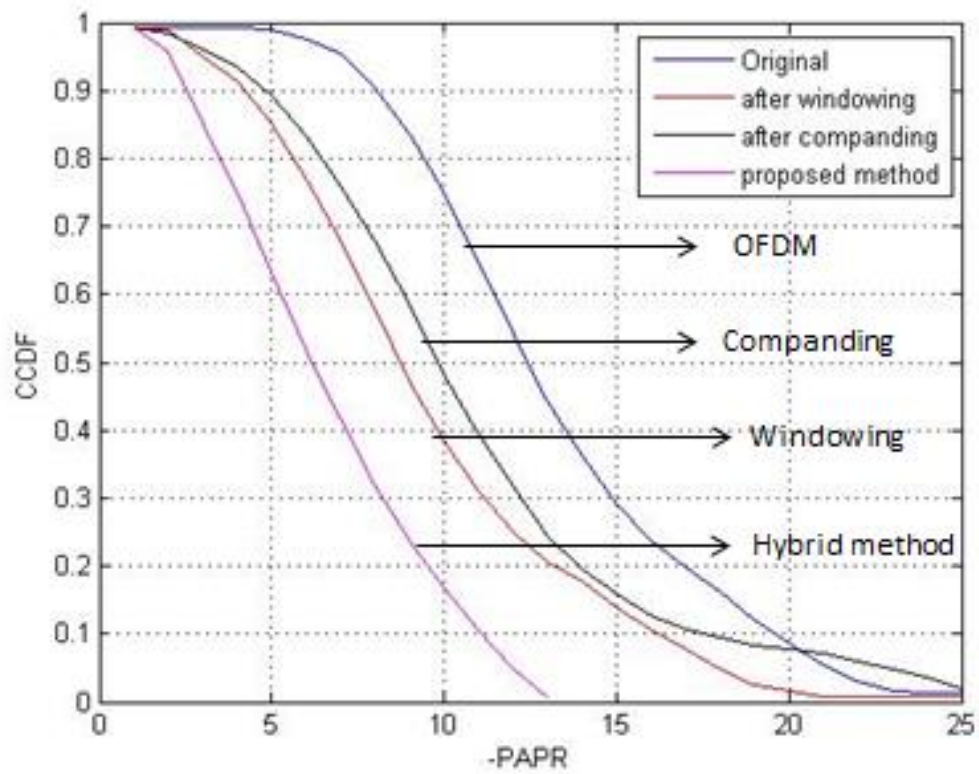


Fig 6.2 Comparison of PAPR reduction for different schemes for 256 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=256

Modulation: 4 QAM

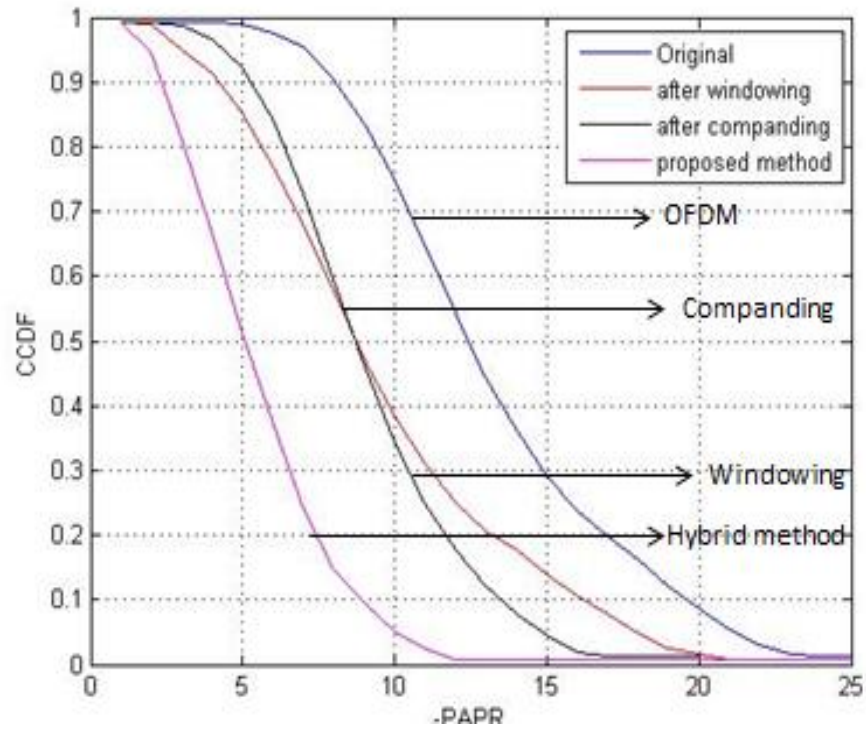


Figure 6.3: Comparison of PAPR reduction for different schemes for 512 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=512

Modulation: 4 QAM

6.3 Simulation Results of Hybrid Method

In the simulation of companding method of PAPR reduction of OFDM at the transmitter, the symbols are converted from serial to parallel then 128 symbols are mapped onto the 128 subcarriers and modulated using 4 QAM or QPSK modulation. The modulated subcarriers undergo Hadamard transform. They are multiplied with Hadamard matrix. The Hadamard-transformed symbols are IFFT sampled and then passed to the AWGN channel. The signal from AWGN channel at the receiver undergoes inverse of operation. The symbols are FFT sampled and they undergo inverse Hadamard transform. The symbols then are converted from parallel to serial to transmit it to the receiver. The PAPR characteristics are plotted using CCDF function. The PAPR characteristics are compared with that of OFDM, companding and windowing.

The bit error rate characteristics for OFDM with companding, Hamming windowing and hybrid proposed method are plotted in Figures 6.4-6.6

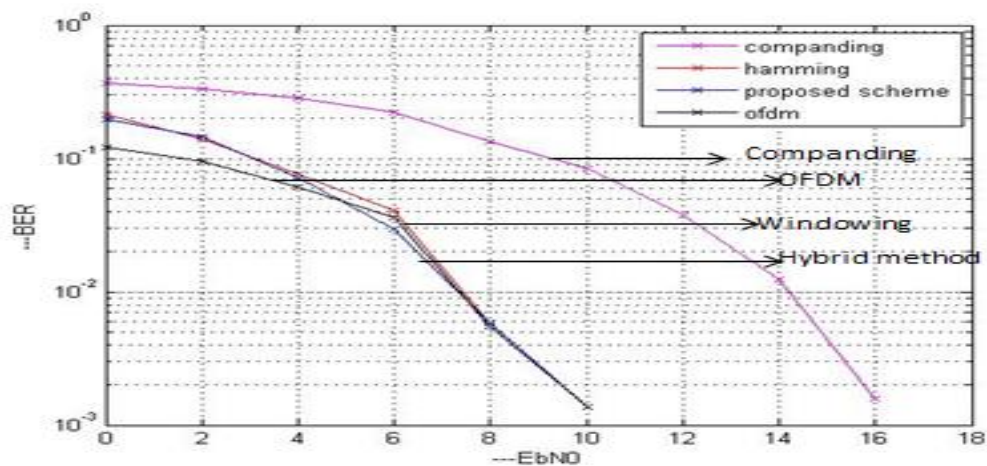


Fig 6.4: Comparison of BER for different schemes for 128 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=128

Modulation: 4 QAM

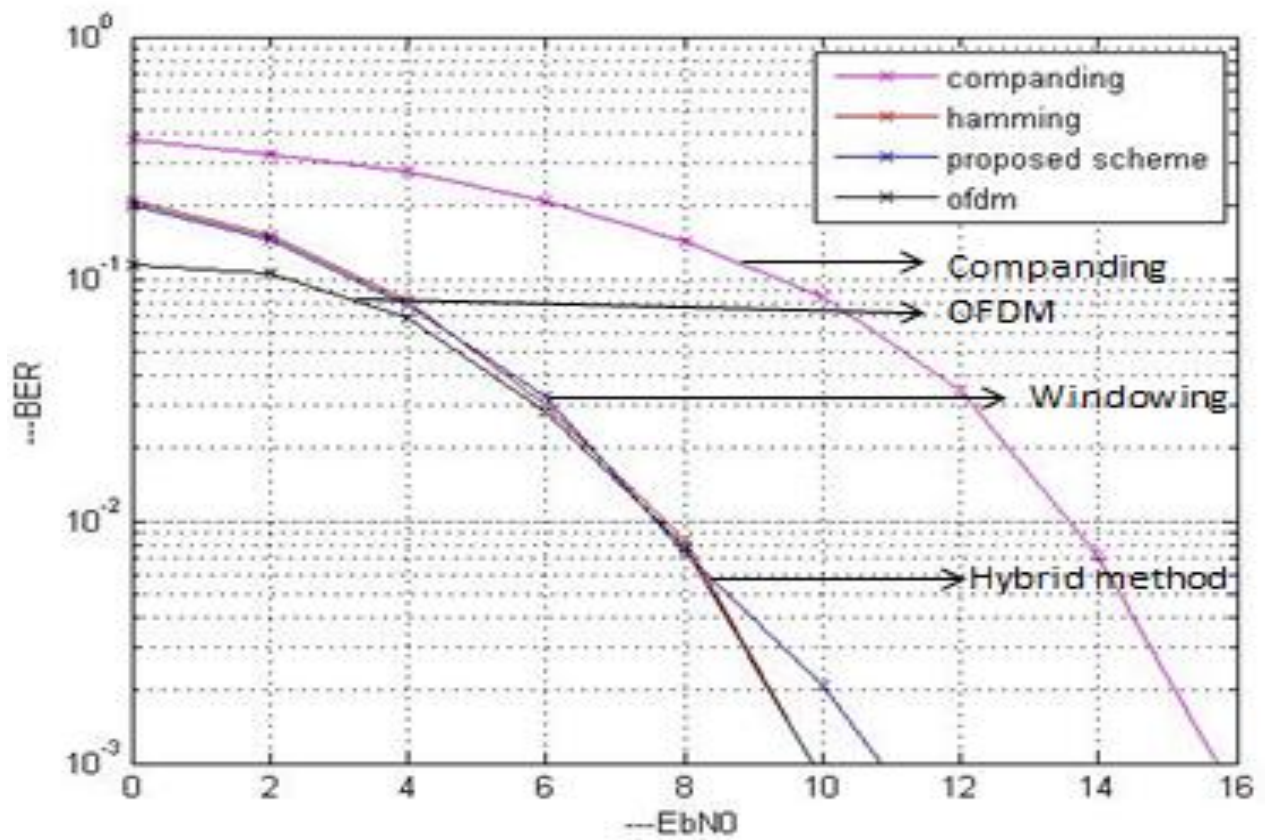


Fig 6.5: Comparison of BER for different schemes for 256 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=256

Modulation: 4 QAM

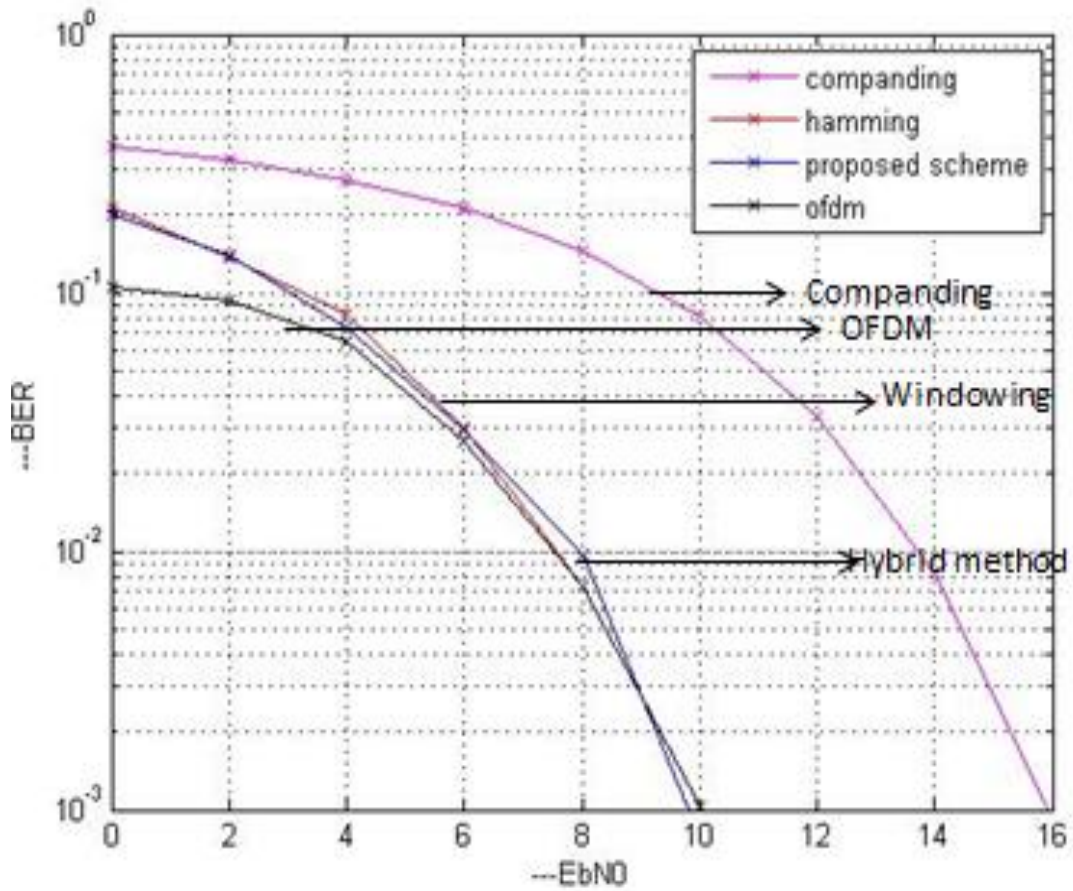


Fig 6.6: Comparison of BER for different schemes for 512 symbols

Simulation Parameters:

Number of sub carriers=16

Number of symbols=512

Modulation: 4 QAM

Chapter 7 CONCLUSION AND FUTURE WORK

7.1 Conclusion

PAPR reduction techniques for OFDM system are simulated and compared. The hybrid technique gave better PAPR reduction when compared to companding and windowing technique. Hybrid scheme gave the best PAPR reduction among all the techniques. The use of Hadamard transform at the transmitter reduces the peaks significantly due to the reduction of the input correlation and further the use of peak windowing gives better signal characteristics compared to conventional windowing methods.

The bit error rate (BER) of companding, windowing and hybrid schemes were simulated and compared. From the simulation we observe

- number of points exceeding threshold in case of 128 symbols and 16 subcarriers=697 out of 2048
- number of points exceeding threshold in case of 256 symbols and 16 subcarriers=1228 out of 4096
- number of points exceeding threshold in case of 512 symbols and 16 subcarriers= 2051 out of 8192

7.2 Future Work

The future work may include the use of different combinations of signal scrambling and signal distortion techniques. Channel estimation can be done.

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