# Entropy Of Printed Bengali Language Texts 

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#### Abstract

One of the most important sources of information is written and spoken human language. The language that is spoken, written, or signed by humans for general-purpose communication is referred as natural language. Determining the entropy of natural language text is a fundamentally important problem in natural language processing. The study and analysis of the entropy of a language can be a meaningful resource for researchers in linguistics and communication theory. For the purpose of this research we have taken printed Bengali language text as our source of natural language. We have collected a sufficient number of printed Bengali language text samples, and divided them into two classes, Newspaper and Literature. We have studied each class in order to come up with specific entropy for each category and analyzed their characteristics. As a separate study, we collected printed religious Bengali language texts, divided them into two classes, Islamic and Hindu, find out their entropy and studied and analyzed their characteristics. From our research, we have found the Zero and first-order entropy of Bengali language to be 5.52 and 4.55 respectively. And the language uncertainty and redundancy are 0.8242 and $17.58 \%$ respectively. These entropy and redundancy results of the language will be useful to the researchers to help find a better text compression method for Bengali language.


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## Chapter 1

## Introduction

Throughout history, many have reflected on the importance of language. Language is not only a medium of expressing thoughts, perceptions, sentiments, and dreams; it also represents a fundamental expression of social identity. Language is very important in any culture. A language does far more than just enable people to communicate with each other. The language of one country is different from other country and it tells the features of the country which distinguish it from one country to another.

The language that is spoken, written, or signed by humans for general-purpose communication is referred as natural language. And determining the entropy of natural language text is a fundamentally important problem in natural language processing. Entropy is a measure of information. The study and analysis of the entropy of a language can be a meaningful resource for researchers in linguistics and communication theory. The results provide us deeper information about the language; help us in understanding its characteristics better and finding out ways to reduce its redundancy. We can also discover better ways to compress it for digital storage for information processing.

Entropy of a natural language text is the average number of bits per letter of the text that will be required to translate the language into binary bits [1]. From the entropy, the redundancy of a text can be calculated. Higher entropy indicates less redundant and lower entropy indicates a more redundant text. Once we have the redundancy of the language, it will be useful to the research to find out a better text compression method for the language.

### 1.1 Objective and Importance

We have taken printed Bengali texts as the source of our natural language. The objective of our research is to find out the entropy of printed Bengali language texts and study their characteristics.

Researchers have worked on English [2], Arabic [3], Russian [4] language to find out their entropy and thus paved the way for further linguistic and text compression research in those languages, which only helped in the various fields where those languages are used as a medium of communication. With 230 million native speakers, Bengali is one of the most widely spoken languages of the world (ranked seventh) [5] and when we found out that this kind of research has not been done with Bengali language, it inspired us to take this as our research problem. Applying statistical techniques related to information theory, it is possible to compute an estimate of the entropy rate of Bengali, thus investigating the redundancy and enabling further research for finding out the optimal compression of Bengali texts.

In natural languages, entropy is quite hard to measure. The languages whose entropy is calculated so far exhibits lower entropy, and lower entropy indicates higher redundancy. But this high level of redundancy is what allows us to only read the shape of words; what allows us to understand each other even in noisy environments. Computers which recognize human speech [6] try to use this low entropy in order to make sure they didn't misinterpret a sound; but this doesn't always work, as the redundancy only exists because a very large number of rules (phonetic and syntactic) come with the language and it is difficult to give instructions to a computer about all of them.

In fact, Computer Science is one area of applications where the low entropy of a language is a problem. When we are creating some text file or word document or other, it is not only a mere plain text, the text in fact follows the rules of some natural language (such as English), or some programming language (such as C++, Java, etc). Thus all of them contain much redundant information [7]. The compression algorithms try to utilize this redundant information; they take a file with low entropy and convert it into one which has higher entropy, thus saving space.

As stated previously, determining the entropy of natural language text is a fundamentally important problem in natural language processing. The ability to predict characters or words in text as well as a human, is equivalent to solving the artificial intelligence problem.

Entropy is also useful when defining the concept of unicity distance in cryptography. Unicity distance is a term used in cryptography referring to the length of an original ciphertext needed to break the cipher by reducing the number of possible spurious keys to
zero in a brute force attack. When deciphering, if we know what cipher is used, and try each of the keys in turn to decode the secret message and if we know that the decoded message should be in English, then because of English's low entropy, it is highly unlikely there be more than one decoding which actually follows the rules of English [2]; which actually follows the unicity distance concept.

A table of the frequencies of letters in a given language is quite handy for breaking simple substitution ciphers or for devising static Huffman coding tables. Thus, entropy related research with Bengali language will help in Bengali language cryptography also.

### 1.2 Contributions

In our research work we have collected a sufficient number of printed Bengali language text samples (more than 50,000 characters), and divided them into three classes, Newspaper (15395 characters), Literature (14364 characters) and Religious (20388 characters) class. These characters are saved in 24-bit BMP image for high quality text so that we can process them in future. We have studied the characteristic of each class and compared the classes in order to come up with specific entropy for each class and analyzed their characteristic. For the religious class, we subdivided the samples into two religious classes, Islamic and Hindu. We then found out their entropy and redundancy and compared and analyzed their characteristics. We found out the entropy and redundancy of the total sample data and compared it with the entropies of each class. These entropy and redundancy results of the language will be useful to the researchers to find out a better text compression method for the language, and in other areas of information processing and linguistic research. We have created a table of frequencies of
letters of Bengali language that will be helpful for breaking substitution ciphers and for devising static Hoffman coding tables. We have also conducted an analysis of the total sample and find out the frequency distributions of the consonant digraphs.

### 1.3 Thesis Organization

This thesis is organized as follows:

In Chapter 1, along with the introduction, the objective of our research and its objective and importance is discussed. Our contributions and the outline of the thesis are also presented.

In Chapter 2, theoretical background for entropy and language entropy is provided. Maximum and relative entropy, redundancy and previous works in entropy have also been discussed.

In Chapter 3, After an introduction to the Bengali language, A brief history and the characteristics of the language have been discussed. A detail of the language alphabet has been given at the end.

In Chapter 4, our data collection process, source of the data and the methodology of our research have been outlined. Then results of our work and discussions on the result are provided.

In Chapter 5, there is a conclusion emphasizing the significance of the research work accomplished in this thesis. At last, an outlining of the possible future work that can be based on this thesis is provided.

## Chapter 2

## Theoretical Background and Previous Work

### 2.1 Introduction

In information processing and transmission of information research field, one of the most important contributions was made by Claude Shannon through his introduction of mathematical theory of communication [9] and the introduction of a method for estimating the entropy and the redundancy of a language [2].

### 2.2 Entropy

"Entropy" is a widely used term in various research fields of science, where the term "entropy" is generally interpreted in three distinct, but semi-related ways, i.e. classical thermodynamics, statistical thermodynamics and an information theory viewpoint.

Entropy in information theory is a fundamentally different concept from thermodynamic entropy. The fundamental premise of information theory is that the generation of information can be modeled as a probabilistic process that can be measured in a manner that agrees with the intuition [10]. In information theory, there is a term called self information, which gives the information in a single outcome. But in most cases, it is
much more interesting to know the average information content of a source. This average is given by the expected value of the self information with respect to the source's probability distribution. This average of self information is called the source entropy [11]. Generally speaking, the amount of self information attributed to any event $E$ is inversely related to the probability of E . If $P(E)=1$ (that is, the event always occurs), then $I(E)=0$ and no information is attributed to it. That is, because no uncertainty is associated with the event, no information would be transferred by communicating that the event has occurred.

The entropy (average self information) of a discrete random variable X is a function of its probability mass function and is defined as:

$$
\begin{equation*}
\text { Entropy, } H(X)=-\sum_{i=1}^{N} P_{x}\left(\mathrm{x}_{\mathrm{i}}\right) \log _{2}\left(P_{x}\left(\mathrm{x}_{\mathrm{i}}\right)\right) \tag{1}
\end{equation*}
$$

where, N is the number of possible values of X and $P_{x}\left(\mathrm{x}_{\mathrm{i}}\right)=\operatorname{Pr}\left[\mathrm{X}=\mathrm{x}_{\mathrm{i}}\right]$. The probability of $\mathrm{x}_{\mathrm{i}}$ is defined as the number of occurrences favorable for the symbol $\mathrm{x}_{\mathrm{i}}$, over the number of total occurrences of all the symbols. When $\log$ is base 2 then the unit of entropy is bits per (source) symbol. Entropy is a measure of uncertainty in a random variable and a measure of information it can reveal [11].

Again, the word entropy conveys special meaning in different respective research fields of information theory. For example, the entropy of an image is quite different from the concept of language entropy. To understand the different approaches in concepts we start with a short description of Image entropy.

### 2.2.1 Image Entropy

Image entropy is a quantity which is used to describe the amount of information which must be coded for by a compression algorithm. In other words, it gives a measure of how much information content is there in a source image.

Low entropy images, such as those containing a lot of black sky, have very little contrast and large runs of pixels with the same or similar DN values. An image that is perfectly flat (only one color or intensity) will have entropy of zero. Consequently, they can be compressed to a relatively small size.

A Digital Number or DN is the value stored within a pixel or cell of an image. The DN of the pixel represents the amount of light intensity reflected back to the sensor. DN of 0 will appear as black, of 127 will appear gray, and of 255 will appear white.

On the other hand, high entropy images such as an image of heavily cratered areas on the moon have a great deal of contrast from one pixel to the next and consequently cannot be compressed as much as low entropy images.

For an image $x$, quantized to $M$ levels, the entropy $H_{x}$ is defined as [12]:

$$
\begin{equation*}
\text { Entropy, } H_{x}=-\sum_{i=0}^{M-1} P_{i} \log _{2} P_{i} \tag{2}
\end{equation*}
$$

where, $P_{i}, i=0$ to $M-1$, is the probability of the $i^{\text {th }}$ quantizer level being used (often obtained from a histogram of the pixel intensities).
$H_{x}$ represents the average number of bits per pixel with which the quantized image $x$ can be represented using an ideal variable-length entropy code.

In a highly correlated image, the pixels tend to have equiprobable values, which results in maximum entropy. If the transformed pixels are de-correlated, certain pixel values become common, thereby having large probabilities, while others are much less. This results in small entropy [12].

An estimate, called the first-order estimate, of the entropy of the source can be computed with $\mathrm{Eq}^{\mathrm{n}}$. (2). Better estimates of the entropy of the gray-level source that generated the sample image can be computed by examining the relative frequency of pixel blocks [10] in the sample image, where a block is grouping of adjacent pixels.

For example, if we obtain the entropy by computing the relative frequencies of pairs of pixels, that estimate is called the second-order estimate of the source entropy, because it was obtained by computing the relative frequencies of 2-pixel blocks. Although higher order estimates provide even better approximations of source entropy, convergence of these estimates to the true source entropy is slow and computationally involved [10].

### 2.2.2 Language Entropy

The entropy is a statistical parameter which measures, in a certain sense, how much information is produced on the average for each symbol of a text in the language. If the language is translated into binary digits in the most efficient way, the entropy is the average number of binary digits required per letter of the original language [2].

We assume that a single symbol $a_{i}$ occurs in some translated data with probability $P_{i}$. The probability $P_{i}$ is defined as the number of occurrences favorable for the $i$-th symbol, over the number of total occurrences of all the symbols. The entropy of symbol $a_{i}$ is defined as
( $-P_{i} \log _{2} P_{i}$ ), where $P_{i}$ is the probability of occurrence of $a_{i}$ in the data. The entropy of $a_{i}$ is the smallest numbers of bits needed to represent symbol $a_{i}$.

So, if there are n symbols, then the entropy of the data is $-\sum_{1}^{n} P_{i} \log _{2} P_{i}$

The entropy of the data depends on the individual probabilities $\mathrm{P}_{\mathrm{i}}$, and is largest when all n probabilities are equal [12].

Let us assume that we have a language alphabet containing $X$ number of characters. With this, we can write words and arrange them into sentences. Now, if we take a string of these characters of length $y$, how many possible strings exist? $X^{y}$ (because for each character we have $X$ numbers of choices). Now, all of these strings possible are not necessarily legal in a given language. The higher the proportion of legal strings, the higher the entropy.

Binary code again shows us how to measure the entropy of our random language; because it takes $\log _{2} n$ bits to code a $n$-character alphabet, the random language has an entropy per character of 4.8 . That means that a 28 -character alphabet can encode a maximum of 4.8 bits (or pieces) of information with each character [7].

An interesting observation was made by Shannon, he found that the capacity to guess the next letter of a text is a measure of the redundancy of the text. The more guessable the text, more redundant it is and lower the entropy. If the test is perfectly guessable that means zero information and zero entropy [9].

### 2.2.2.1 Maximum Entropy

The maximum entropy concept has a long history. Laplace [13] may be rightly considered the father of maximum entropy, having introduced the underlying theme 200 years ago in his "Principle of Insufficient Reason":
"When one has no information to distinguish between the probabilities of two events, the best strategy is to consider them equally likely."

As E. T. Jaynes [14], a more recent pioneer of maximum entropy put it:


#### Abstract

"The fact that a certain probability distribution maximizes entropy subject to certain constraints representing our incomplete information is the fundamental property which justifies use of that distribution for inference; it agrees with everything that is known, but carefully avoids assuming anything that is not known. It is a transcription into mathematics of an ancient principle of wisdom."


According to the properties of entropy $\mathbf{H}$ [15], maximum entropy is reached when the probabilities of occurrence of the $n$ symbols of a particular sequence are equal, i.e., when $p_{1}=p_{2}=\ldots=p_{n}=l / n$ and therefore:

$$
\begin{equation*}
H \_ \text {maximum }=-n(1 / n) \log _{2}(1 / n)=\log _{2} n \tag{3}
\end{equation*}
$$

Actually, the symbols in a natural language are far from being equiprobable like this, and therefore the first-order entropy H , defined on the base of unconditional probabilities of separate symbols is considerably less than the maximum entropy.

### 2.2.2.2 Relative Entropy and Redundancy

We define the relative entropy or the relative uncertainty as follows:

$$
\begin{equation*}
\text { H_relative }=\frac{\text { H_actual }}{\text { H_maximum }} \tag{4}
\end{equation*}
$$

Where, H_actual refers to the first-order estimate of the entropy and H_maximum is the maximum entropy.

The redundancy can be defined as the difference between H_maximum and H_actual expressed as a fraction of $\mathbf{H}$ _maximum [15]:

$$
\begin{align*}
\text { Redundancy } & =\frac{\text { H_maximum }-\mathrm{H} \_ \text {actual }}{\text { H_maximum }}  \tag{5}\\
& =1-\text { H_relative } \tag{6}
\end{align*}
$$

### 2.3 Previous Works

In information theory, Harvard linguistic professor George Kingsley Zipf [16] first introduced the principle of "least effort" and used this concept to study the economy of words. However, a method for estimating the entropy of language text was first introduced by Claude Shannon [9]. Shannon originally devised the use of entropy to study the amount of information in a transmitted message. According to the definition of information entropy it is expressed in terms of a discrete set of probabilities $p_{i}$. In the case of transmitted messages, these probabilities were the probabilities that a particular message was actually transmitted, and the entropy of the message system was a measure of how much information was in the message.

Shannon estimated the entropy of written English in 1950 by having human subjects guess successive characters in a string of text selected at random from various sources. In one experiment, random passages were selected from Jefferson the Virginian by Dumas Malone. The subject was shown the previous 100 characters of text and asked to guess the next character until successful. The text was reduced to 27 characters (A-Z and space). Subjects were allowed to use a dictionary and character frequency tables (up to trigram) as aids.

Many researchers continued the research started by Shannon and analyzed his empirical results for English text. Grignetti [17] recalculated Shannon's estimate of the average entropy of words in English text, Treisman [18] commented on contextual constraints in language, White [19] used a dictionary encoding technique to achieve compression for printed English and Jamission [20], Wanas [03] discuss entropy of other languages and Miller [21] discussed the effects of meaningful patterns in English text on the entropy calculations.

Some efforts were made to estimate the higher-order entropies of languages by use of word statistics. Kuepfmueller [22] used the statistics of words and syllables (not including the spaces), but his approach suffers from neglecting the combinations of letters belonging to different neighboring words.

Major progress in developing statistical approaches to entropy evaluation for long symbol sequences (not necessarily texts in natural languages) has been achieved by Grassberger [23] who introduced efficient methods based on modifications of the Lempel-Ziv universal coding algorithms [24].

### 2.3.1 Shannon's Prediction method

Shannon [2] proposed a unique method, which overcomes the limitations of the statistical approach, to obtain upper and lower bounds of the conditional entropy for higher order estimates of entropies.

The conditional entropy expresses the uncertainty of a symbol following a set of length L (an L-gram). An L-gram is a string of $L$ consecutive letters all belonging to a standard alphabet. If the entropy is close to zero, it means that the symbol can be predicted almost for certain when the previous L-gram is given. The larger the entropy, the more difficult it is to predict the following symbol. This means, in particular, that the predicted symbol can be wrong, and that more than one attempt may be needed to obtain the right result. It suggests to us that it is possible to go in the opposite direction and to extract information about the value of the entropy from the results of a prediction experiment.

Shannon suggested using a human being - a person experienced in the language - as a predictor for an experiment of this sort. The reason for this in his own words [9]:
"The new method of estimating entropy exploits the fact that anyone speaking in a language possesses, implicitly, an enormous knowledge of the statistics of the language. Familiarity with the words, idioms, clichés and grammar enables him to fill in missing or incorrect letters in proof-reading or to complete an unfinished phrase in the conversation."

One of the most important factor of Shannon's method in comparison with the direct statistical approaches is that the probabilities of L-grams for large L cannot be obtained from statistical data not only because of computational difficulties but also because the
total amount of texts in any language is also limited. Only a small part of all the possible meaningful larger L-grams can be found in published texts. The total length of all the existing texts is not enough in order to find probabilities of long L-grams. However, a human guesser can usually suggest several different continuations of a given possible text which is much larger than the totality that actually exists. In fact, a human being possesses such an enormous variety of possible texts because of his knowledge; and this knowledge, mostly intuitive, brings the guesser by reading a previous text into a state which is close to the state of the source itself, and that enables him to predict efficiently the continuation. [1]

## Chapter 3

## Bengali Language

### 3.1 Introduction

Bengali or Bangla is an Indo-Aryan language of the eastern Indian subcontinent, evolved from the Magadhi Prakrit, Pāli and Sanskrit languages. Its immediate predecessor was 'Magadhi Apabhransha' [5]. From this emerged the three languages - Bengali, Oriya and Assamese. Of these three, Oriya has separate script, while Bengali and Assamese share similar script (except for very few differences).

Bengali is the national language of Bangladesh and one of 18 languages listed in the Indian Constitution. It is the administrative language of the Indian states of Tripura and West Bengal, as well as one of the administrative languages of Kachar district, Assam.

With nearly 230 million native speakers, Bengali is one of the most widely spoken languages in the world, making it the seventh language after Chinese, English, HindiUrdu, Spanish, Russian and Arabic. It is perhaps the only language on the basis of which an independent state was created. Bengali is the main language spoken in Bangladesh; in

India, it is ranked as the second most spoken language. Along with Assamese, it is geographically the most eastern of the Indo-Iranian languages. [5]

### 3.2 History:

Bengali emerged as a new Indo-Aryan language by 900-1000 AD through Magadhi Apabhramsa and Abahattha, two stages of Magadhi Prakrit ( $600 \mathrm{BC}-600 \mathrm{AD}$ ), along with two other Indo-Aryan languages, Oriya and Assamese (Fig. 1). Until the 14th century, there was little linguistic difference between Bengali and Assamese.

The evolution of Bengali may be divided into three historical phases [25]:

1) Old Bengali (900/1000 CE-1400 CE): Texts include Charyapada, devotional songs; emergence of pronouns Ami, tumi, etc; verb inflections -ila, -iba, etc. Oriya and Assamese branch out in this period.
2) Middle Bengali (1400-1800 CE): Major texts of the period include Chandidas's Srikrishnakirtan; elision of word-final $\hat{o}$ sound; spread of compound verbs; Persian influence. Some scholars further divide this period into early and late middle periods.
3) New Bengali (since 1800 CE ): Shortening of verbs and pronouns, among other changes (e.g. tahar $\rightarrow$ tar "his"/"her"; koriyachhilô $\rightarrow$ korechhilo he/she had done).


Figure 1: Evolution of Bengali language [5]

Historically closer to Pali, Bengali saw an increase in Sanskrit influence during the Middle Bengali (Chaitanya era), and also during the Bengal Renaissance. Of the modern Indo-European languages in South Asia, Bengali and Marathi retain a largely Sanskrit vocabulary base while Hindi and others are more influenced by Arabic and Persian.

Until the 18th century, there was no attempt to document the grammar for Bengali. The first written Bengali dictionary/grammar, Vocabolario em idioma Bengalla, e Portuguez dividido em duas partes, was written by the Portuguese missionary Manoel da Assumpcam between 1734 and 1742 while he was serving in Bhawal. Nathaniel Brassey Halhed, a British grammarian, wrote a modern Bengali grammar (A Grammar of the Bengal Language (1778)) that used Bengali types in print for the first time. Raja Ram Mohan Roy, the great Bengali Reformer, also wrote a "Grammar of the Bengali Language" (1832) [26].

During this period, the Choltibhasha form, using simplified inflections and other changes, was emerging from Shadhubhasha (older form) as the form of choice for written Bengali.

Bengali was the focus, in 1951-52, of the Language movement (Bhasha Andolon) in what was then East Pakistan (now Bengalidesh). Although Bengali speakers were more numerous in the population of Pakistan, Urdu was legislated as the sole national language. On February 21, 1952, protesting students and activists walked into military and police fire in Dhaka University and three young students and several others were killed. Subsequently, UNESCO has declared 21 February as International Mother Language Day [26].

### 3.3 Characteristics of the language

### 3.3.1. Influence of other languages

Bengali has been greatly influenced by two non-Aryan languages [5]:
Dravidian and Kol.
Their influence is evident not only in the vocabulary but also in the construction of sentences. A large number of onomatopoeic words, repetitive words and conjunctive verbs in Bengali reveal non-Aryan influence; for example, words such as ghoda-toda (horses etc), kapad-chopad (clothes etc), tuk-tuk, khatkhat, khankha, dhandha, basiya pada (sitting down), lagiya thaka (to persevere), etc. There are plenty of Dravidian and other non-Aryan words in Bengali, especially in place names, indicating that Bengali passed through many stages and was influenced by various other languages.

One of the main influences on Bengali was that of Sanskrit as this language was the vehicle of literature and culture for almost the whole of the subcontinent since the beginning of the Christian era. (The religious discourses of the Buddhists and the Jains were carried on in Pali and Ardhamagadhi respectively.) In the days of old Bengali, many Bengalis used to write poetic works in Sanskrit. Even after the evolution of Bengali, many well-known Bengali poets, such as Jaydev, Umapatidhara and Govardhan Acharya, continued to compose their literary works in Sanskrit. The result was that many pure Sanskrit words entered Bengali from the very early stages.

Following the establishment of Muslim rule in Bengal in the 13th century, Bengali came under the influence of Arabic, Persian and Turkish. Persian was the language of the court
during Muslim rule in the 14th and 15th centuries. Because of this special status as well as other cultural influences, Bengali picked up many Persian words at this time. In the 16th century, with the Portuguese inroads, several Portuguese words entered Bengali; for example, words such as anaras (pineapple), ata (custard-apple) and tamak (tobacco).

| A table comparing the similarities between Bengali, Sanskrit, English \& Latin words |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Language | Word |  |  |  |  |  |
| English | month | mother | new | night | nose | three |
| Latin | mensis | mater | novus | nox | nasus | tres |
| Sanskrit | mãs | matar | nava | nakt | nãs | trayas |
| Bengali | maash | mata | nobo | ratri | naakh | tin |

Table 1: Comparing the similarities between Bengali, Sanskrit, English \& Latin language words [27]

From the 17th century, the Dutch, French and English started arriving in Bengal. As a result, words from these languages started entering Bengali vocabulary; for example, from the French: cartouche, coupon, depot; English: table, chair, lord/lat, general/jadrel, etc. During the 17 th and 18 th centuries effective use of Bengali prose began through the efforts of Christian missionaries.

With the start of British rule in the 18th century and the spread of English education, Bengali started absorbing increasing numbers of English words. Following the establishment of the Bengali Department at Fort William College in Calcutta in 1801, the
efforts of its head, William Carey, and his associate Bengali scholars, made Bengali fit for fine prose.

During the 19th century, the efforts of Bengali writers contributed to the further growth of the language. Among them were Raja Rammohan Roy, Bhabanicharan Bandyopadhyay, Iswar Chandra Vidyasagar, Bankimchandra Chattopadhyay, Michael Mdhusudan Dutt, and Mir Mosharraf Hossain. The 20th century witnessed the elevation of colloquial Bengali to a written literary medium through the work of many talented writers such as Rabindranath Tagore (Nobel Loriete) and Pramatha Chowdhury.

### 3.3.2 Dialects

Regional variation in spoken Bengali constitutes a dialect continuum. Linguist Suniti Kumar Chatterjee grouped these dialects into four large clusters - Radh, Banga, Kamarupa and Varendra. The south-western dialects (Radh) form the basis of standard colloquial Bengali, while Bangali is the dominant dialect group in Bengalidesh. In the dialects prevalent in much of eastern and south-eastern Bengal (Barisal, Chittagong, Dhaka and Sylhet divisions of Bengalidesh), many of the stops and affricates heard in West Bengal are pronounced as fricatives. The influence of Tibeto-Burman languages on the phonology of Eastern Bengali is seen through the lack of nasalized vowels. Some variants of Bengali, particularly Chittagonian and Chakma-Bengali, have contrastive tone; differences in the pitch of the speaker's voice can distinguish words [5].

Rajbangsi, Kharia Thar and Mal Paharia are closely related to Western Bengali dialects, but are typically classified as separate languages. Similarly, Hajong is considered a separate language, although it shares similarities to Northern Bengali dialects.

During the standardization of Bengali in the late 19th and early 20th century, the cultural center of Bengal was its capital Kolkata (then Calcutta). What is accepted as the standard form today in both West Bengal and Bengalidesh is based on the West-Central dialect of Nadia, a district located near Kolkata. There are cases where speakers of Standard Bengali in West Bengal will use a different word than a speaker of Standard Bengali in Bengalidesh, even though both words are of native Bengali descent. For example, nun (salt) in the west corresponds to lôbon in the east.

Even in Standard Bengali, vocabulary items often divide along the split between the Muslim populace and the Hindu populace. Due to cultural and religious traditions, Hindus and Muslims might use, respectively, Sanskrit-derived and Perso-Arabic words. Some examples of lexical alternation between these two forms are:

- hello: nômoshkar (S) corresponds to assalamualaikum/slamalikum (A)
- invitation: nimontron/nimontonno (S) corresponds to daoat (A)
- paternal uncle: kaka ( S ) corresponds to chacha ( $\mathrm{S} / \mathrm{Hindi}$ )
- water : jol (D) corresponds to pani (S)
(here, $\mathrm{S}=$ derived from Sanskrit, $\mathrm{D}=$ deshi; $\mathrm{A}=$ derived from Arabic)


### 3.3.3 Forms of Written Language

Written Bengali has two forms [5]:
a) Sadhu or chaste and
b) Chalita or colloquial or spoken.

The two differ basically in verbs and pronouns. The verbs and pronouns get shortened in the colloquial form. For example: কর্য়য়া (kariya; to do) কর্র (kare); जाशন (tahar; his/hers) তার (tar). The importance of the colloquial form arose at the beginning of the 20th century but the use of chaste Bengali did not disappear totally. Chaste language continued to be used in contemporary newspapers, works of documentation and in statements by the government and on matters of serious import. Colloquial Bengali was the language of the Calcutta gentry, a considerable number of whom used the colloquial form to write literary works.

The parallel currents of chaste and colloquial streams created a unique phenomenon of diglossia in Bengali. Although the main peculiarity of the colloquial stream is the shortened form of verbs and pronouns, their real difference is in temperament. The mix of sadhu and chalita, as used in poetry, has been on the wane since World War II, giving way to the chalita form only. Since March 1965, many Bengali newspapers have adopted the chalita form, discarding the sadhu one. "The ITTEFAQ", which had retained the sadhu form, has also started using the chalita form since 2001.

Hindus and Muslims differ in their ways of using the language, and even West Bengalis and Bengalideshis differ somewhat in their practices. The Muslim rule in Bengal prior to
the British rule led to an extensive development of Bengali and a plentiful influx of Arabic, Persian and Turkish vocabulary. Towards the end of the 18th century, even highcaste Hindus used to cultivate the court language, Persian, allowing their Bengali to be influenced by it. Even today over 2,000 Arabic and Persian words relating to war, taxation, legal and cultural matters, and crafts are in use in Bengali.

Such words and their impact increased substantially in the language of the Muslim rural masses of East Bengal prior to the partition of India in 1947. A major difference exists in the language used by Hindus and Muslims in respect of words that refer to relatives or food. Hindus use Sanskrit and Bengali words, while Muslims use Urdu and Arabic words, eg kaka/chacha (uncle), ma/amma (mother), baba/abba (father), didi/bubu (sister), dada/bhaiya (brother), jal/pani (water), mangsa/gosht (meat).

At the same time, it should be noted that Muslims in the Jessore area also use the socalled 'Hindu terms' of didi and dada. Although the written language of West Bengal and Bengalidesh is more or less similar, spoken Bengali differs widely. There are also many regional Bengali dialects. Some dialects, such as those of Sylhet, Noakhali and Chittagong, differ so greatly from each other and standard Bengali, which people of one region can hardly communicate with people of the other.

### 3.4 Bengali Alphabet

### 3.4.1 Notable features

- To start with Bengali does not have the concept of upper and lower case letters. It is written from left to right and top to bottom as in English.
- In Bengali alphabet each consonant has an inherent vowel and has two different pronunciations, the choice of which is not always easy to determine and which is sometimes not pronounced at all [27].
- Vowels can be written independently or by using specific diacritical marks.
- When two consonants occur together in clusters, they change their original shape and take a special form.


### 3.4.2 The alphabet

There are 11 vowels (Fig. 2), 35 consonants (Fig. 3) and 5 modifier symbols (Fig. 4) in Bengali language alphabet. A selection of conjunct consonants and Numerals are also shown in Fig. 5 and 6 respectively [27].


Figure 2: Vowels and vowel diacritics of Bengali alphabet


Figure 3: Consonants of Bengali alphabet


Figure 4: A selection of conjunct consonants

| $\because$ | hasanta - mutes inherent vowel | ¢ $k[k]$ |
| :---: | :---: | :---: |
| 9 | Khanda-ta - final unaspirated dental | Fe kat [kot] |
| 40 | anusvāra - final velar nasal | ¢9. kam [kכワ] |
| $\cdots$ | visarga - adds voiceless breath after vowel | F: kah [koh] / [ko ] |
| 8 | chandra-bindu - nasalises vowels | $\frac{\stackrel{3}{5}}{4}=k \bar{n}[k n]$ |

Figure 5: Modifier symbols of Bengali alphabet

| $\bigcirc$ | 5 | 2 | 19 | 8 | ( | 15 | 9 | 3 | 2 | So |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| गबा | 96 | $2^{2}$ | 09 | Eld | गाँb | द2 | ग-16 | W6 | जx | T- ${ }^{1}$ |
| sūnya | ek | dui | tin | cār | pn̄ãc | chay | sāt | āt | nay | daś |
| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |

Figure 6: Numerals of Bengali alphabet.

### 3.5 Bengali Language Entropy:

According to Shannon, capacity to guess the next letter of an English text is a measure of the redundancy of English. More guessable the text, it is more redundant and lower the entropy. If the test is perfectly guessable that means zero information and zero entropy.

Example: 4 symbols, অ, আ, র, এ

অ $=00$, आ $=01$, র $=10, ~ এ=11$

In general, with $n$ symbols, codes need to be of length $\log _{2} n$, rounded up. For Bengali text, 46 letters + space $=47$ symbols, length $=6$ since $2^{5}<47<2^{6}$ (replace all punctuation marks by space).

### 3.5.1 First-Order model of Bengali

We know that, if a symbol $S$ has probability $p$, its self-information is

$$
H(S)=\log _{2}(1 / p)=-\log _{2} p
$$

For example:

| $S$ | অ | आ | र | $এ$ |
| :---: | :---: | :---: | :---: | :---: |
| $p$ | .25 | .25 | .25 | .25 |
| $H(S)$ | 2 | 2 | 2 | 2 |
| $p$ | .6 | .2 | .1 | .1 |
| $H(S)$ | .74 | 2.32 | 3.32 | 3.32 |

Table 2: Two sample examples for determining entropy

Now, from $E q^{\text {n }}$ (1),

First-Order Entropy of Source
$=$ Weighted Average Self-Information
$=-\sum_{k=1}^{L} P_{k} \log _{2} P_{k}$

So, for the above examples:

| $S$ | অ | आ | র | $এ$ |
| :---: | :---: | :---: | :---: | :---: |
| $p$ | .25 | .25 | .25 | .25 |
| $-l o g p$ | 2 | 2 | 2 | 2 |
| $-p l o g p$ | .5 | .5 | .5 | .5 |
| $p$ | .6 | .2 | .1 | .1 |
| $-\log p$ | .74 | 2.32 | 3.32 | 3.32 |
| $-p l o g p$ | .444 | .464 | .332 | .332 |

Table 3: Calculations for determining entropy of the Table 2 sample examples.

First Order Entropy for the first case
$=-\sum p \log p=2$

First Order Entropy for the second case
$=-\sum p \log p=1.572$

## Chapter 4

## Simulation and Results

### 4.1 Data Collection

For the purpose of this research we have collected a sufficient number of printed Bengali language text samples containing more than 50,000 numbers of characters. We collected samples representing three classes:

- Newspaper class,
- Literature class and
- Religious class.

Our objective was to find out the entropy of these classes separately and compare them with one another and also with the total sample. We also sub-divided the religious class into two sub-classes, namely Islamic and Hindu class, in order to find out their entropy separately and study and analyze the characteristics of these texts.

The newspaper samples that we used are available on the internet. They are taken from "Prothom Alo" and "Shamokaal", two major daily newspapers of Bangladesh, and from "Anandabazar Patrika", which is the main Bengali daily newspaper of India. Newspaper topics include a wide range of applications such as general news, science, health, sports, politics, travel, weather, etc.

As for the literature, we scanned them from book pages. For literature samples, we chose the material from well known books by distinguished author of Bengali language. Samples are taken from the following books:

- Banaphuler Shrestha Galpa - By Balaichand Mukherjee [28]
- Detective - By Rabindranath Tegore [29]
- Anukul - Satyajit Ray [30]
- Debi - Humayun Ahmed [31]
- Elebele - Humayun Ahmed [32]
- Sanket - Shirshendu Mukhopadhyay [33]
- Maa - Anisul Haque [34]
- Krishnapakhsa - Humayun Ahmed [35]

Samples of Islamic and Hindu religious texts are taken from two sources. From scanned pages of religious books, such as Al-Kuran, Srimadbhagbad Geeta, Saraswati bratakatha, etc; and from Islamic and Hindu religious columns published in newspapers and journals.

Sample texts obtained for Newspaper class contain more than 15000 characters, Literature class contain more than 14000 characters and from Religious class contain more than 20000 characters. The exact number of total characters is 50247 . These samples are saved in 24-bit BMP image for high quality text.

The untagged version of this corpus is uploaded in the following location so that researchers can process them in future:
http://rapidshare.com/files/104424388/Untagged_Corpus_2.zip
There are two versions, one is the main untagged corpus and in the other version each Bengali character is separated by a space for ease of understanding and reading. The untagged file is compressed into a zip file and is password protected, password is "UNBC".

### 4.2 Methodology

For our research we have calculated the entropy of the Bengali religious texts using the basic entropy calculation method described in section 2.2. As there is no previous research work available on finding out the entropy of Bengali language, we stayed with the basic method for entropy calculation. For the Bengali alphabets, we have taken into account all 11 vowels and 35 consonants, a total of 46 characters, and have not considered the modifiers or the spaces in between the words.

For each class text we have:

1) Calculated the total number of characters in the sample texts.
2) Calculated the number of occurrences of each letter of the Bengali alphabet in the sample texts.
3) Generated the frequency table for occurrence of Bengali alphabet.
4) Calculated the probability of each letter in the sample texts.
5) Calculated the entropy of each character in the sample texts.
6) Calculated the entropy of full sample texts.

To calculate the entropy of the Bengali language, total samples are considered and the following is performed:

1) Calculated the total number of characters in total sample texts.
2) Calculated the number of occurrence of each letter of the Bengali alphabet in total sample texts.
3) Generated the frequency table for occurrence of Bengali alphabet characters and study the behavior
4) Calculated the probability of each letter in total sample texts.
5) Calculated the entropy of each character in total sample texts.
6) Calculated the entropy of total sample texts.

For the calculation of the occurrence of characters, we have not used the Unicode system, as there is a basic problem using Unicode for Bengali alphabet. As stated previously in section 3.4.1, the consonants of Bengali alphabet have an inherent vowel and have two different pronunciations, the choice of which is not always easy to determine and which

| Letter | English equivalent | Letter | English equivalent | Letter | English equivalent |
| :---: | :---: | :---: | :---: | :---: | :---: |
| অ | a | উ | u | § | oi |
| আ | aa | ※ | uu | 3 | 0 |
| ই | 1 | ね | ri | ঔ | Ou |
| \% | ii | $এ$ | e |  |  |

(a) English equivalent used for 11 Vowels

| Letter | English equivalent | Letter | English equivalent | Letter | English equivalent |
| :---: | :---: | :---: | :---: | :---: | :---: |
| ক | k | ড | d | ম | m |
| ข | kh | $\zeta$ | dh | य | y |
| গ | g | ๆ | nn | র | r |
| घ | gh | ত | ta | ल | 1 |
| ङ | ng | ข | tha | শ | sh |
| চ | ch | দ | da | ষ | shh |
| ছ | chh | 8 | dha | স | $s$ |
| ऊ | j | ब | n | ई | h |
| 邓 | jh | ฯ | p | ! | ya |
| $\mathfrak{3}$ | na | ए | ph | ড় | rr |
| ট | t | ব | b | ঢ़ | rrr |
| ठ | th | उ | bh |  |  |

(b) English equivalent used for 35 Consonants

Table 4: Template of equivalent English characters used for (a) Vowels and (b) Consonants to convert the Bengali texts into its English equivalent.
is sometimes not pronounced at all. Again, some conjunct consonants take an entirely different shape when occurring together in a word. These are not possible to distinguish in Unicode format separately. For this shape shifting problem and inherent vowel we haven't used the Unicode system; we have implemented the Bengali texts into English text files and carried out the character count by hand. The template of equivalent English characters used for Bengali characters are shown in Table 4. The calculation related programming is implemented in Matlab 7.0 and carried out on a Pentium IV Windows XP workstation.

### 4.3 Results and Discussion

### 4.3.1 Literature Class

The total data samples collected for newspaper class contain 14364 characters. The 4 most frequently occurring vowels and consonants and their frequency rates for the Literature class are shown in Tables 5 and 6 respectively.

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| आ | 1786 | 14364 | 12.70 |
| $\Omega$ | 1558 | 14364 | 12.29 |
| অ | 1476 | 14364 | 8.80 |
| 亏 | 936 | 14364 | 5.64 |

Table 5: 4 Most Frequently Occurred Vowels of Literature Texts and Their Frequency Rates

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| र | 981 | 14364 | 6.83 |
| क | 681 | 14364 | 4.74 |
| व | 664 | 14364 | 4.62 |
| व | 564 | 14364 | 3.93 |

Table 6: 4 Most Frequently Occurred Consonants of Literature Texts and Their Frequency Rates
The top 20 most frequently occurred characters are plotted in a graph (Fig. 7) in the following order (ordered in terms of their frequency):

आ, এ, অ, র, ই, ক, ন, ব, ম, ত, ল, স, উ, ও, ஈ, য, দ, ছ, ট, ছ.


Top 20 most frecuently occurred characters of the Literature class

Figure 7: Histogram of the top 20 characters of literature class.

A more detailed table containing their number of occurrence and frequency is shown in
Table 7:

| Letter | Letter class | Occurrence | Total char | Frequency (\%) |
| :---: | :---: | :---: | :---: | :---: |
| आ | Vowel | 1786 | 14364 | 12.43 |
| a | Vowel | 1558 | 14364 | 10.85 |
| ज | Vowel | 1476 | 14364 | 10.28 |
| র | Consonant | 981 | 14364 | 6.83 |
| \% | Vowel | 936 | 14364 | 6.52 |
| क | Consonant | 681 | 14364 | 4.74 |
| न | Consonant | 664 | 14364 | 4.62 |
| ব | Consonant | 564 | 14364 | 3.93 |
| म | Consonant | 497 | 14364 | 3.46 |
| ত | Consonant | 480 | 14364 | 3.34 |
| ल | Consonant | 478 | 14364 | 3.33 |
| স | Consonant | 422 | 14364 | 2.94 |
| উ | Vowel | 383 | 14364 | 2.67 |
| з | Vowel | 305 | 14364 | 2.12 |
| भ | Consonant | 299 | 14364 | 2.08 |
| 3 | Consonant | 284 | 14364 | 1.98 |
| ち | Consonant | 250 | 14364 | 1.74 |
| ₹ | Consonant | 242 | 14364 | 1.68 |
| ট | Consonant | 224 | 14364 | 1.56 |
| Б | Consonant | 195 | 14364 | 1.36 |

Table 7: Top 20 Most Frequently Occurred Character and Their Frequency (\%) of literature texts.

As evident from Table 7, vowels occupy 4 of the top 5 most frequently occurred characters list. Of all the characters, vowels constitute $45.84 \%$ of the total literature data sample and consonants constitute $54.16 \%$. The top 20 characters constitute $88.46 \%$ of the data sample.

Now H-maximum refers to the theoretical maximum entropy, this being achieved only when the letters of the alphabet are all equiprobable [15]. From (3),

$$
\begin{aligned}
\mathrm{H} \_ \text {maximum } & =\log _{2} 46 \\
& =5.5236
\end{aligned}
$$

From our calculation, the actual entropy or $1^{\text {st }}$ order entropy that we got for literature class is:

$$
\text { H_actual } \quad=4.5232
$$

Hence, from eq ${ }^{\mathrm{n}}$ (4) and (6), for literature class:

$$
\begin{aligned}
\text { H_relative } & =4.5232 / 5.5236 \\
& =0.81889 \\
\text { Redundancy } & =1-0.81889 \\
& =0.18111
\end{aligned}
$$

So, the relative uncertainty is $81.89 \%$ for Literature texts and the redundancy is $18.11 \%$. We will compare it later with the redundancy found for other classes.

### 4.3.1.1 Observation on character frequencies:

As has been mentioned before, in the Bengali alphabet each consonant has an inherent vowel and has two different pronunciations. Most of the time this inherent vowel is " $অ "$ ", and this character is used in Bengali words widespread and can be found occurring in many of the commonly used Bengali words in Literature sample, such as অনেক, অতি, সময়, इल, অপর, কম, নয়, থবর, যথন, তथन, आসल, নকল, etc.

The second most frequently occurred character "আ" is also found in numerous most commonly used words, such as মা, বাবा, আমি, আমার, তোমার, তারা, আभনাকে, সকাল, भा, রাथा, চাকা, হাসभাতাল, নাম, আশা, etc. In many of these words the character when used with consonants changes its shape from "আ" to "○" and the second shape never occurs alone, occurs only after a consonant.

Likewise, other vowels ই, ঈ, উ, ঊ, $\sharp, ~ এ, ~ \supseteq, ~ ও ~ a n d ~ ঔ, ~ w h e n ~ t h e y ~ o c c u r ~ w i t h ~$ consonants, they change their shapes into " $", "$ ", " ", " ", "Q", "ю", "ळ", "ю" and " l ". The dotted circle in the script means that a consonant has to be placed in that space.

Among the rest of the characters of the top 20 table, " $a$ " is found in the commonly used words like ছ্লেল, মেয়ে, যেতে, থেতে, আছে, করে, গিয়ে, পেয়ে, করেছে, গিয়েছে, পেয়েছে, আছে, নেবে, etc. "র" is found in common words like আমার, তোমার, আমরা, তোমরা, করা, করে, করতে, তার, পর, শহর, বছ্র, बিকশা, etc.

These words are very frequently used in common texts. As a result, the characters associated with them are also found to occur more frequently. Similarly,
"३" is found in words like নেই, তাই, চাই, একই, फিল, তিনি, এই, বই, কবি, কমিটি, সমিতি, etc. "ক" is found in words like কি, কে, এক, একা, একক, করা, করে, কর্রেে, করেছে, কম, ঢাকা, etc.
 "ব" is found in words like বাবা, সব, থবর, বই, কবি, নেবে, বন, সুবিধা, হবে, বাকি, বিষয়, etc. "ম" is found in words like মা, आমি, আমার, আমরা, তোমার, সময়, মতো, মন, কম, মেয়, etc. "ত" is found in words like তুমি, তোমান, তাদের, তার, মতো, তিন, হাত, তথন, শেতে, থেতে, etc. "ल" is found in words like সকাল, সকল, দল, কাল, ऊल, आসল, नকল, ছেলে, করছিল, হয়েছ্লি, etc. "স" is found in words like সব, সকল, সময়, সেরা, আসল, সমিতি, সুবিধা, সকাল, সহ, হাসभাতাল, etc. "উ" is found in words like তুমি, দूই, সুবিধা, উচ্তিত, কিছু, शুব, शুসি, মুথ, সুথ, চুभ, নুতন, etc. " 3 " is found in words like ওর, ওরা, যাওয়া থাওয়া, মতো, ওঠ, কোনো, তোমার, তোমরা, ছোট, etc. " $\mathbb{}$ " is found in words like মেয়ে, সময়, হয়, গিহ়ে, यাওয়া, थাওয়া, নিয়ে, দিয়ে, याা়, হয়েছে, etc. "দ" is found in words like দিয়ে, দুই, দেथা, দেথ, দল, তাদের, দিন, আদর, बেদনা, দूनिয়া, etc. "「" is found in words like হয়ে, হয়, হয়েছে, হবে, ছল, শহর, হাসभাতাল, ছাসি, মহিলা, মহল, etc. "ট" is found in words like এটা, সেটা, একটি, দুটি, সাইট, কাটা, কাটিয়ে, টিকে, টানা, টেনে, ছোট, etc.
"ছ্থ" is found in words like ছুলে, আছে, হয়েছে, করেছে, গিয়েছে, পেয়েছে, ছিল, বছ্র, ছোট, কিছু, etc.

### 4.3.2 Newspaper Class

The total data samples collected for newspaper class contain 15395 characters. The 4 most frequently occurring vowels and consonants, and their frequency rates for Newspaper class are shown in Tables 8 and 9 respectively.

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| অ | 1721 | 15395 | 11.18 |
| आ | 1663 | 15395 | 10.80 |
| এ | 1518 | 15395 | 9.86 |
| ই | 1054 | 15395 | 6.85 |

Table 8: 4 Most Frequently Occurred Vowels of Newspaper texts and their frequency rates

| Letter | Occurrence | Total char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| র | 1302 | 15395 | 8.46 |
| क | 785 | 15395 | 5.10 |
| ब | 738 | 15395 | 4.79 |
| उ | 575 | 15395 | 3.73 |

Table 9: 4 Most Frequently Occurred Consonants of Newspaper texts and Their Frequency Rates

The top four most frequently used vowels and consonants are almost same as the one we have found for the literature class before, just with an exception of " $ত$ " occupying the fourth most occurred consonant place in space of "‘". But, if we look at a more detailed table (Table 10), there is not much difference between the occurrence of "ত" and "ব", and "'ব" is the $5^{\text {th }}$ most frequently occurred consonant here.

A detailed table containing the number of occurrence and frequency of top 20 characters are shown in Table 10：

| Letter | Letter class | Occurrence | Total char | Frequency（\％） |
| :---: | :---: | :---: | :---: | :---: |
| ज | Vowel | 1721 | 15395 | 11.18 |
| आ | Vowel | 1663 | 15395 | 10.80 |
| a | Vowel | 1518 | 15395 | 9.86 |
| র | Consonant | 1302 | 15395 | 8.46 |
| 亏 | Vowel | 1054 | 15395 | 6.85 |
| क | Consonant | 785 | 15395 | 5.10 |
| व | Consonant | 738 | 15395 | 4.79 |
| 丁 | Consonant | 575 | 15395 | 3.73 |
| ব | Consonant | 544 | 15395 | 3.53 |
| т | Consonant | 477 | 15395 | 3.10 |
| भ | Consonant | 399 | 15395 | 2.59 |
| ম | Consonant | 380 | 15395 | 2.47 |
| ल | Consonant | 381 | 15395 | 2.47 |
| ！ | Consonant | 376 | 15395 | 2.44 |
| উ | Vowel | 372 | 15395 | 2.42 |
| 3 | Vowel | 340 | 15395 | 2.21 |
| 万 | Consonant | 282 | 15395 | 1.83 |
| ট | Consonant | 223 | 15395 | 1.45 |
| य | Consonant | 220 | 15395 | 1.43 |
| इ | Consonant | 208 | 15395 | 1.35 |

Table 10：Top 20 Most Frequently Occurred Character and Their Frequency（\％）of newspaper texts．

As evident from Table 9, vowels occupy 4 of the top 5 most frequently occurred characters list. Of all the characters, vowels constitute $44.57 \%$ of the total newspaper data sample and consonants constitute $55.43 \%$. And the top 20 characters constitute $88.06 \%$ of the total newspaper sample.

The top 20 most frequently occurred characters are plotted in a graph (Fig. 8) in the following order (ordered in terms of their frequency):

```
অ, आ, এ, র, ই, ক, ন, Ј, ব, স, গ, ম, ল, \̦, উ, ও, দ, ট, य, হ.
```



Top 20 most frequently occurred characters of the Newspaper class

Figure 8: Histogram of the top 20 characters of newspaper class.

When we compare our findings for the newspaper class with the literature class, we find that among the top 20 characters 19 are the same, the different ones are "ছ" for the Literature class and " $য$ " for the newspaper class. Other differences are $অ, ~ आ, ~ a n d ~ এ ~$ which are the top three most frequently occurred characters, they change their positions.

In literature class आ and $コ$ were top two characters, the main reason of this being the use of more casual words and pronouns being used in the literatures such as आমि, आমান, আমরা, তুমি, তোমার, তোমরা, তারা, তাদের, তাহার, হয়েছে, করেছে, গিয়েছে, পেহ্যেছ্, etc. All of these words have these two characters आ and $コ$ occurring in abundance, whereas অ occurring very less here. One more difference in the newspaper class is that here many more words from other languages are used, and also full names of local and foreign people and various organizations. Some foreign words that we found to occur frequently are Cricket, Coach, One-day, Test, Security, Police, Computer, Windows, Internet, Microsoft, Copy, Service, Tool, TV, Audio, Video, Class, etc.

Now H-maximum refers to the theoretical maximum entropy, this being achieved only when the letters of the alphabet are all equiprobable [15]. From eq ${ }^{n}$ (3),

$$
\begin{aligned}
\text { H_maximum } & =\log _{2} 46 \\
& =5.5236
\end{aligned}
$$

From our calculation, the actual entropy or $1^{\text {st }}$ order entropy that we got for newspaper class is:

$$
\text { H_actual } \quad=4.5454
$$

Hence, from eq ${ }^{\mathrm{n}}$ (4) and (6), for literature class:

$$
\begin{aligned}
\text { H_relative } & =4.5454 / 5.5236 \\
& =0.82291 \\
\text { Redundancy } & =1-0.82291 \\
& =0.17709
\end{aligned}
$$

So, the relative uncertainty is $82.29 \%$ for newspaper texts and the redundancy is $\mathbf{1 7 . 7 1 \%}$.
We will compare it later with the redundancy found for other classes.

### 4.3.3. Religious Class

We have subdivided the religious data into two classes, Islamic and Hindu religious texts class. 4 most frequently occurred vowels and consonants and their frequency rates for Hindu and Islamic texts are shown in Tables 11, 12 and 13, 14 respectively.

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| অ | 1619 | 10107 | 16.02 |
| आ | 885 | 10107 | 8.76 |
| a | 709 | 10107 | 7.01 |
| 亏 | 478 | 10107 | 4.73 |

Table 11: 4 Most Frequently Occurred Vowels of Hindu Text and their frequency rates

| Letter | Occurrence | Total char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| उ | 851 | 10107 | 8.42 |
| ব | 505 | 10107 | 5.00 |
| ब | 501 | 10107 | 4.96 |
| उ | 447 | 10107 | 4.42 |

Table 12: 4 Most Frequently Occurred Consonants of Hindu Text and Their Frequency Rates

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| आ | 1318 | 10381 | 12.70 |
| অ | 1276 | 10381 | 12.29 |
| $a$ | 914 | 10381 | 8.80 |
| ₹ | 586 | 10381 | 5.64 |

Table 13: 4 Most Frequently Occurred Vowels Of Islamic Texts and Their Frequency Rates

| Letter | Occurrence | Total <br> char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| ज | 924 | 10381 | 8.90 |
| न | 516 | 10381 | 4.97 |
| उ | 477 | 10381 | 4.59 |
| क | 396 | 10381 | 3.81 |

Table 14: 4 Most Frequently Occurred Consonants of Islamic Texts and Their Frequency Rates

Among top 20 most frequently occurred characters 18 are the same ones, and 4 characters are different taking two from each class. These 18 characters are plotted in a graph (Fig. 9) in the following order (ordered in terms of their frequency in Islamic texts):
आ, অ, র, এ, ই, ন, Ј, ক, ব, ম, দ, ল, স, হ, অ, উ, স, ঈ.

The different ones are $૩$ and $য ়$ for Islamic texts and $\rtimes$ and $\uparrow$ for Hindu texts (Table 14). Actually these characters can also be found in the chart if we just take 25 top chars into account.

And if we have a look at the comparative frequencies of the characters in two classes we find that except 2 characters (char 1 and 2 , namely आ, অ) almost all of the rest of them occurs at close frequencies.


Top 18 common characters among top 20 of the two classes

Figure 9: Graph depicting comparative frequency of the top 18 characters of two classes.

A more detailed table containing the frequency of occurrences (in percentage) of the characters that are common in the top 20 list of the Hindu and Islamic religion class are shown in table 15.

| Islamic Text |  | Hindu Text |  |
| :---: | :---: | :---: | :---: |
| Letter | Frequency <br> (\%) | Letter | Frequency <br> (\%) |
| आ | 12.70 | ज | 16.02 |
| অ | 12.29 | आ | 8.76 |
| к | 8.90 | র | 8.42 |
| 9 | 8.80 | $\square$ | 7.01 |
| ব | 5.64 | ₹ | 5.00 |
| ब | 4.97 | न | 4.96 |
| ₹ | 4.59 | ত | 4.73 |
| অ | 3.81 | क | 4.42 |
| क | 3.68 | ব | 3.27 |
| ম | 3.53 | ম | 2.95 |
| Ј | 2.62 | 3 | 2.90 |
| দ | 2.62 | 万 | 2.59 |
| উ | 2.50 | ल | 2.31 |
| я | 2.38 | Ј | 2.31 |
| औ | 2.18 | ई | 2.08 |
| Ф | 2.04 | य | 1.81 |
| ई | 1.96 | উ | 1.75 |
| ศ | 1.72 | भ | 1.64 |
| গ | 1.68 | T | 1.60 |
| य | 1.18 | ॠ | 1.59 |

Table 15: Top 20 Most Frequently Occurred Character and Their Frequency (\%) of religious texts

आ and ज are top 2 most frequently occured characters in both the classes, but there is a significant difference between the occurence of them in two classes. For the Islami ones their frequency are very close to each other, but in Hindu texts $অ$ is much higher, in fact about double of the second frequent character. Another interesting aspect is that the total frequency of these two characters are about same for both classes $(24.99 \%$ for Islami texts and $24.78 \%$ for Hindu texts). So, from this observation we can colclude that the character $\boldsymbol{\pi}$ occurs more frequently in Hindu religious texts compared to Islamic ones, but at the same time frequency of आ decreases.

|  | Number of occurrences |  |
| :---: | :---: | :---: |
| Letter | Islamic texts | Hindu texts |
| অ | 1276 | 1619 |
| आ | 1318 | 885 |
| ঈ | 123 | 210 |
| भ | 13 | 61 |
| コ | 914 | 709 |
| अ | 272 | 148 |
| $\Im$ | 5 | 24 |
| গ | 95 | 162 |
| $\Im$ | 5 | 52 |
| ए | 23 | 4 |
| उ | 382 | 505 |
| उ | 49 | 114 |
| न | 260 | 166 |

Table 16: Characters with notable differences in occurrence (between the Islamic and Hindu text classes).

After studying the character frequency table we found some interesting characteristics of the texts of two religious classes. The notable differences of the occurrence of characters can be seen in Table 16.

First thing to notice here is the occurrence of $অ$ and आ in the two classes of texts. One of the main reasons of $ञ$ occurring more frequently and m occurring less in Hindu texts than the Islamic one is the usage of Sanskrit words in abundance in Hindu religious texts. The Sanskrit words and also many Hindu religious words have a tendency of using of ज more often after each consonant and especially at the end position of each word. And as has been stated previously, it is evident from study that in Hindu texts whereas the number of occurrences of $অ$ increases, occurrences of $आ$ are found in decreased numbers than the regular usage of the two letters.

Then, the letter ऋ occured more frequently in Hindu texts. One significant reason of this is the usage of a certain word 줘, which is used to address anyone respectfully and is used many times in the Hindu religious books.

There is no specific Islamic word usage that clarifies the occurrence of $a$ and 3 more times in Islamic texts, but we can conclude that the general Bengali words containing these characters are more used in these texts, like তোমাকে, তোমরা, বলো, থেকে, গেছ্, etc.

Three letters $\sharp, ~ ঔ$ and $\Re$ occur much less not only in Islami texts, but in fact these letters or words containing these lettesr are very seldom used in Bengali language. The reason of them happening more frequently in Hindu texts is due to some specific words happening


ए is another character that is very less used in words of Bengali language, the reason of happening of this character more in Islami texts is due to the usage of some specific religious words found in them, like ফिতন, ফिকর, মারূর, etc.

আললাহ and ভগবান ("Allah" \& "Bhagaban") are the two specific words that means God in Islamic and Hindu religion respectively. As a result these two words are found more frequently when these religion's texts are studied. As these two words happen more frequently in their respective texts, some characters found in them are also found in increased numbers in their occurrence table. Like ल in Islami texts and ভ, গ and $\overline{\mathrm{J}}$ in Hindu texts.

Two foreign languages have great influences on these two classes of religious Bengali language texts, Arabic language on Islami texts and Sanskrit on Hindu texts to be specific. Many words from these languages are used without any alteration in Bengali language. Some of these words have now become a part of Bengali language and no other words can be found in the language to represent the same meaning.

| Islamic religious words | আलनाহ, ঈমান, রमूल, बবী, নামাय, जिशাদ, आনनाত, মুमिन, উমমত, হাদীস, আয়াত, এবাদত, ঈদ, রোজা, ঈদ-উল-ফিতর, রমজান, যাকাত, আদব, etc. |
| :---: | :---: |
| Hindu religious words | ভগবান, ক্ষঞ, বিষগু, রাম, দূর্গা, সরসবতী, भूजा, দেবী, ধर्ম, বেদ, त्रী, গীতা, মनত্, ঠाকুর, भরসাদ, মূর্তি, भরণাম, অদবৈত, বৃनদাবন, চেতন, বৈষঙব, মহামায়, त्रীমদভাগবদগীতা, etc |

Table 17: Commonly used Islamic and Hindu religious words

We calculated the Spearman's rank correlation coefficient (nonparametric test) in order to measure the correlation between the ranks of Islamic and Hindu text characters.

We set our hypothesis as:
$H_{0}: \rho=0$ (no correlation between character ranks)
$\mathrm{H}_{\mathrm{a}}: \rho>0$ (positive correlation between character ranks)

Spearman's rank correlation is calculated as,

$$
\rho=1-\frac{6 \sum_{i=1}^{n}\left[R\left(\mathrm{I}_{i}\right)-R\left(\mathrm{H}_{i}\right)\right]^{2}}{n\left(n^{2}-1\right)}
$$

where,
$\rho \quad$ Spearman's rank correlation coefficient
$R\left(\mathrm{I}_{i}\right) \quad$ Ranks of Islamic characters
$R\left(\mathrm{H}_{i}\right) \quad$ Ranks of Hindu characters
$n \quad$ Number of characters ( $n=46$ )

We found that the characters ranks of the Islamic texts are positive correlated $(\rho=0.995)$ with the character ranks of the Hindu texts. The results are significant at the $1 \%$ level. Based on our sample, we conclude that the use of characters is identical in both languages.

Now H-maximum refers to the theoretical maximum entropy, from eq ${ }^{n}$ (3),

$$
\text { H_maximum }=\log _{2} 46=5.5236
$$

From our calculation, the actual entropy or $1^{\text {st }}$ order entropy that we got for each class, and the relative entropy and redundancy are as follows:

|  | Islamic texts | Hindu texts |
| :---: | :---: | :---: |
| H-maximum | 5.5236 | 5.5236 |
| H-actual | 4.5000 | 4.4000 |
| H-relative | 0.8147 | 0.7966 |
| Redundancy | 0.1853 | 0.2034 |

Table 18: Entropy and redundancy of printed religious Bengali texts.

Therefore, the average number of bits per letter required to translate the language into binary are 4.5 and 4.4 for Islamic and Hindu texts respectively.

The relative uncertainty in this ensemble is 81.47 for Islamic texts and 79.66 for Hindu texts. Therefore, the redundancy is $18.53 \%$ for Islamic texts and $20.34 \%$ for Hindu texts.

### 4.3.3. Total sample

The total data samples collected for all classes contain 50247 characters. 4 most frequently occurring vowels and consonants, and their frequency rates for total samples are shown in Tables 19 and 20 respectively.

| Letter | Occurrence | Total char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| অ | 6092 | 50247 | 12.12 |
| आ | 5652 | 50247 | 11.25 |
| এ | 4699 | 50247 | 9.35 |
| ¡ | 3054 | 50247 | 6.08 |

Table 19: 4 most frequently occurred vowels of total sample texts and their frequency rates

| Letter | Occurrence | Total char | Frequency <br> $(\%)$ |
| :---: | :---: | :---: | :---: |
| র | 4058 | 50247 | 8.08 |
| न | 2419 | 50247 | 4.81 |
| क | 2192 | 50247 | 4.36 |
| ব | 1995 | 50247 | 3.97 |

Table 20: 4 most frequently occurred consonants of total sample texts and their frequency rates

A detailed table containing the number of occurrence and frequency of top 20 characters are shown in Table 21:

| Letter | Letter type | Occurrence | Total char | Frequency (\%) |
| :---: | :---: | :---: | :---: | :---: |
| অ | Vowel | 6092 | 50247 | 12.12 |
| आ | Vowel | 5652 | 50247 | 11.25 |
| a | Vowel | 4699 | 50247 | 9.35 |
| র | Consonant | 4058 | 50247 | 8.08 |
| \% | Vowel | 3054 | 50247 | 6.08 |
| ब | Consonant | 2419 | 50247 | 4.81 |
| क | Consonant | 2192 | 50247 | 4.36 |
| ब | Consonant | 1995 | 50247 | 3.97 |
| ত | Consonant | 1979 | 50247 | 3.94 |
| ম | Consonant | 1541 | 50247 | 3.07 |
| স | Consonant | 1439 | 50247 | 2.86 |
| न | Consonant | 1285 | 50247 | 2.56 |
| উ | Vowel | 1191 | 50247 | 2.37 |
| भ | Consonant | 1110 | 50247 | 2.21 |
| 3 | Vowel | 1065 | 50247 | 2.12 |
| 万 | Consonant | 1066 | 50247 | 2.12 |
| T | Consonant | 976 | 50247 | 1.94 |
| 5 | Consonant | 853 | 50247 | 1.70 |
| य | Consonant | 778 | 50247 | 1.55 |
| গ | Consonant | 610 | 50247 | 1.21 |

Table 21: Top 20 most frequently occurred characters and their frequency (\%) of total sample texts.

As evident from Table 21, vowels occupy 4 of the top 5 most frequently occurred characters list. Of all the characters, vowels constitute $45.01 \%$ of the total data sample and consonants constitute $54.99 \%$. And the top 20 characters constitute $87.67 \%$ of the total sample.

When we compare the top 20 most frequently occurred characters of total sample with the separate literature, newspaper, Islamic and Hindu religion classes, we found 15 characters are same in all the top 20 table, they are:

```
অ, आ, এ, র, ই, न, т, ব, э, ম, স, ल, উ, भ, ई
```

The uncommon ones are З, দ, য়, য, গ, इ, ট, ছ, ঈ, শ.

So, in all top 20 tables we have actually 25 characters. It happens actually for specific characteristics of the words used in a class, which has been discussed in the respective sections before.

From the findings of total data sample we have the classified the characters into following groups according to their frequency of occurrence:

| Group | Characters | Frequency (\%) |
| :---: | :---: | :---: |
| Vowels | অ, आ, ই, ঈ, উ, \#, ঋ, এ, ঐ, ૩, ঔ | 45.01 |
| High-Frequency Consonants | র, ন, ক, ব, ত, ম, স, ল, গ, দ | 37.98 |
| Medium-Frequency Consonants | য়, হ, य, গ, শ, ট, Г, ऊ, চ, থ | 12.37 |
| Low-Frequency Consonants | ষ, ভ, ধ, ข, ণ, ড়, ড, ঠ, ఒ, æ, घ, ঙ, ঝ, ঢ, ঢִ | 4.64 |

Table 22: Classification of characters according to their frequency of occurrences

Now we have the maximum entropy, from eq ${ }^{\text {n }}$ (3),

$$
\begin{aligned}
\text { H_maximum } & =\log _{2} 46 \\
& =5.5236
\end{aligned}
$$

From our calculation, the actual entropy or $1^{\text {st }}$ order entropy that we got for total data is:

$$
\text { H_actual } \quad=4.5524
$$

Hence, from eq ${ }^{\mathrm{n}}$ (4) and (6), for literature class:

$$
\begin{aligned}
\text { H_relative } & =4.5524 / 5.5236 \\
& =0.82417 \\
\text { Redundancy } & =1-0.82417 \\
& =0.17583
\end{aligned}
$$

The actual entropy, relative entropy (or uncertainty) and redundancy of all the classes are shown in the following table:

| Class | Maximum <br> Entropy | Actual <br> Entropy | Relative <br> Entropy | Redundancy |
| :--- | :---: | :---: | :---: | :---: |
| Literature | 5.5236 | 4.5232 | 0.8189 | $18.11 \%$ |
| Newspaper | 5.5236 | 4.5454 | 0.8229 | $17.71 \%$ |
| Islamic | 5.5236 | 4.5000 | 0.8147 | $18.53 \%$ |
| Hindu | 5.5236 | 4.4000 | 0.7966 | $20.34 \%$ |
| Total | 5.5236 | 4.5524 | 0.8242 | $17.58 \%$ |

Table 23: Entropy calculation results for total and all the separate classes

From Table 22, we can conclude that the texts of the Hindu class are more redundant, that
means they are more guessable than the other classes. This result is statistically significant. From Shannon's calculation of Entropy of English ( $\mathrm{eq}^{\mathrm{n}}$ 5), we have the redundancy of English language as,

$$
\text { Redundancy }=1-(4.14 / 4.7)=1-0.88085=0.11915 \text { or } 11.91 \%
$$

So, we can find that Bengali language is more redundant compared to the English language. This result is also statistically significant. In fact, Redundancy in a language is actually useful at times, for how else we can discern what is said in a noisy room? The redundancy allows one to understand what is said when only part of a message is available or comes across. But, on information processing point of view, this redundant data is an overhead. This redundant data should be compressed in a way to ensure better storage and transmission of data and save storage space and processing time.

Next, we can have a look at the zero and first order entropies of different languages with the one we calculated for Bengali language in Table 24:

| Language | $\mathrm{F}_{0}$ | $\mathrm{~F}_{1}$ |
| :--- | :---: | :---: |
| English $^{[2]}$ | 4.7 | 4.14 |
| German $^{[22]}$ | 4.7 | 4.1 |
| Russian $^{[4]}$ | 5.00 | 4.35 |
| Arabic $^{[3]}$ | 5.00 | 4.2 |
| Bengali $^{4}$ | 5.52 | 4.55 |

Table 24: Zero and First order entropies of different languages

For the zero-order entropy, we know that it is the maximum entropy of that language and the entropy is at a maximum when all of the states have equal probabilities. And this maximum entropy increases with the increase of number of states (here the number of characters in alphabet). For English language, the one used in the table was originally calculated by Shannon with 26 characters of English alphabet. When spaces are also taken into account the maximum entropy increases to 4.76. As Bengali language alphabet has 46 characters, this explains the much bigger maximum entropy for the language. And from the first-order entropy Bengali language, we can conclude that the average number of bits per letter required transmitting or store Bengali language is 4.55 bits. We haven't tested the statistical significance of the difference between first-order entropy of English and Bengali.

### 4.3.4 Consonant Bigrams

Bigrams are groups of two successive written letters or two symbols and are very commonly used as the basis for simple statistical analysis of text. They are used in one of the most successful language models for speech recognition [36].

There are 35 consonants in Bengali language alphabet, and when Bigrams of all consonants (all Bigrams which consists only consonants) are taken into account they make 1225 different Bigrams. We have calculated all of them, and from our total data sample of 50247 characters we have found 3652 occurrences of consonant Bigrams. Among the 1225 probable Bigrams only 266 different bigrams are found to occur at least once. The top 50 Bigrams, their occurrences and frequency of occurrence are shown in
table 24 ．Of the 1225 bigrams，these top 50 most frequently occurred ones constitute $68.45 \%$ of the total occurrences of Bigrams．

| Bigram | Occurrence | Frequency （\％） |
| :---: | :---: | :---: |
| পর | 192 | 5.26 |
| সত | 105 | 2.88 |
| बত | 104 | 2.85 |
| রब | 102 | 2.79 |
| কষ | 100 | 2.74 |
| তর | 94 | 2.57 |
| बদ | 90 | 2.46 |
| नल | 80 | 2.19 |
| बय | 78 | 2.14 |
| वय | 73 | 2.00 |
| রब | 73 | 2.00 |
| ঙケ | 68 | 0.68 |
| রম | 66 | 1.81 |
| कত | 65 | 1.78 |
| কট | 64 | 1.75 |
| 顷 | 63 | 1.73 |
| ষট | 59 | 1.62 |
| गब | 54 | 1.48 |
| उय | 53 | 1.45 |
| শর | 49 | 1.34 |
| রক | 47 | 1.29 |
| সข | 45 | 1.23 |
| দ\％ | 41 | 1.12 |
| মব | 39 | 1.07 |
| মর | 38 | 1.04 |


| Bigram | Occurrence | Frequency <br> （\％） |
| :---: | :---: | :---: |
| गব | 38 | 1.04 |
| তত | 36 | 0.99 |
| \＆ | 36 | 0.99 |
| গর | 35 | 0.96 |
| দর | 34 | 0.93 |
| הय | 34 | 0.93 |
| দব | 33 | 0.90 |
| তब | 31 | 0.85 |
| রণ | 31 | 0.85 |
| কর | 30 | 0.82 |
| সট | 29 | 0.79 |
| स® | 29 | 0.79 |
| দय | 27 | 0.74 |
| সক | 26 | 0.71 |
| গ® | 25 | 0.68 |
| রদ | 24 | 0.66 |
| लত | 24 | 0.66 |
| लभ | 24 | 0.66 |
| न\％ | 23 | 0.63 |
| नब | 23 | 0.63 |
| রข | 23 | 0.63 |
| 入य | 22 | 0.60 |
| টর | 21 | 0.58 |
| बর | 21 | 0.58 |
| －${ }^{\text {d }}$ | 21 | 0.58 |

Table 25：Top 50 Consonant Bigrams，their occurrence and frequency of occurrence．

A statistics of number of Bigrams starting with a specific consonant（having at least one occurrence），their occurrences and frequency of occurrence are shown in Table 26：

| Letter | No．of Bigrams | Occurrence | Frequency（\％） |
| :---: | :---: | :---: | :---: |
| क | 19 | 353 | 9.67 |
| ข | 06 | 46 | 1.26 |
| গ | 12 | 102 | 2.79 |
| घ | 03 | 03 | 0.08 |
| \＆ | 03 | 70 | 1.92 |
| Б | 09 | 80 | 2.19 |
| Б | 01 | 01 | 0.03 |
| ज | 10 | 37 | 1.01 |
| \％ | 03 | 05 | 0.14 |
| $\Omega_{3}$ | 03 | 29 | 0.79 |
| ট | 10 | 54 | 1.48 |
| ठ | 02 | 08 | 0.22 |
| ড | 04 | 07 | 0.19 |
| ๆ | 07 | 36 | 0.99 |
| す | 07 | 231 | 6.33 |
| ข | 04 | 08 | 0.22 |
| 万 | 11 | 157 | 4.30 |
| 8 | 06 | 49 | 1.34 |
| न | 19 | 421 | 11.53 |
| भ | 10 | 235 | 6.43 |
| ए | 03 | 06 | 0.16 |
| व | 14 | 138 | 3.78 |
| ভ | 03 | 19 | 0.52 |
| म | 20 | 200 | 5.48 |
| य | 01 | 02 | 0.05 |
| র | 26 | 573 | 15.69 |
| न | 16 | 186 | 5.09 |
| ॠ | 11 | 138 | 3.78 |
| 区 | 11 | 144 | 3.94 |
| স | 12 | 314 | 8.60 |

Table 26：Bigrams starting with a specific consonant，their occurrences and frequency of occurrence

From Table 26 we find that $\boldsymbol{\text { , }}$, অ,, , ম, র and স are the top 7 consonants that make most of the Bigrams that have at least one occurrence. Together they have 113 different Bigrams occurring at least once, and have a total of 2327 occurrences, which is the 63.73\% of the total occurrence.

An $n$-gram is a sub-sequence of $n$ items from a given sequence. The items can be letters, words or base pairs according to the application. An n-gram of size 1 is a "unigram"; size 2 is a "bigram" (also called a "digram"); size 3 is a "trigram"; and size 4 or more is simply called an "n-gram". For, 46 characters of Bengali alphabet bigram gives 2116 possible character combinations, trigram gives 97336 combinations and n-gram gives 4477456 combinations, whose frequency count has first to be calculated in order to proceed with further entropy related calculation for all these combinations. It wasn't possible to do this kind of vast amount of calculations within our limited scope and time constraints. Automated software should be built to carry out this kind of huge calculation and that will further enhance research in this field.

## Chapter 5

## Conclusion \& Future Directions

### 5.1 Conclusion

Natural Language is a very important aspect of human life and culture, and researches addressing natural language is not only helpful in information processing of that language but also helps researchers and others understand the language better and provide results that enables them to have a deep insight into the language.

From our research, we have found the Zero and first-order entropy of Bengali language to be 5.52 and 4.55 respectively. And the language uncertainty and redundancy are 0.8242 and $17.58 \%$ respectively. We have also studied three different data classes, namely Literature, Newspaper and Religious class in order to come up with specific entropy for each of them and analyzed their characteristics. There are no studies in the literature to compare our results with, in regarding to Bengali language, which makes our results as a new reference for researchers in this field. But, our results show that the entropy and redundancy values of are larger compared to other languages, such as English (Table 23). This should mean that there is scope for researchers to alleviate this redundancy. We hope that these results will help the researchers in future to further investigate in this field
and find better compression methods to alleviate the redundancy of the language.

### 5.2 Future Directions

There are many probable directions of extending the current research work presented in this thesis. Some possible directions of future work are outlined below:

- We haven't included spaces and some modifier symbols that are character lookalike in our alphabet count, further research can be done including these in total character count.
- A very large number of text databases can be made to further investigate the entropy of Bengali language, which was not possible for us due to time constraints. Moreover, higher order entropies should be calculated and compare these results with other languages.
- We have calculated only consonant Bigrams; research can be done to find out the Bigrams of all the characters. The total number of Bigrams in that case will be 2116, and when vowels are included there will be a lot more occurrences to work with.
- As the redundancy of the language is found out, research can be done to find out how to alleviate this redundancy for a better storage and transmission of Bengali language.
- Due to the problems mentioned in section 4.2 , we couldn't use the Unicode system. This problem and the unavailability of a corpus restricted us from working with more extensive data. An automated program or software should be built to solve this problem and ensure future research with more extensive data.


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