



Tafreshi, S.N. Moghaddas and Khalaj, Omid and Dawson, Andrew (2014) Repeated loading of soil containing granulated rubber and multiple geocell layers. *Geotextiles and Geomembranes*, 42 (1). pp. 25-38. ISSN 0266-1144

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1 Repeated loading of soil containing granulated rubber and multiple 2 geocell layers

3 S.N. Moghaddas Tafreshi^{1,*} (Corresponding Author), O. Khalaj², A.R. Dawson³

4 ^{1,*}*Corresponding Author*, Associate Professor, Department of Civil Engineering, K.N. Toosi University of Technology,
5 Valiasr St., Mirdamad Cr., Tehran, Iran. Tel: +982188779473; Fax: +982188779476; E-mail address:
6 nas_moghaddas@kntu.ac.ir

7 ²*Department of Civil Engineering, PhD Candidate, K.N. Toosi University of Technology, Tehran, Iran. Tel:*
8 *+982188779473; Fax: +982188779476; Email: o_khalaj@yahoo.com*

9 ³*Associate Professor, Nottingham Transportation Engineering Centre, University of Nottingham, Nottingham, UK. Tel:*
10 *+44 115 951 3902; fax: +44 115 951 3909. E-mail address: andrew.dawson@nottingham.ac.uk*

11

12 **ABSTRACT:** Sandy soil/aggregate, such as might be required in a pavement foundation over a soft area, was treated by
13 the addition of one or more geocell layers and granulated rubber. It was then subjected to cyclic loading by a 300 mm
14 diameter plate simulative of vehicle passes. After an initial study (that established both the optimum depth of the
15 uppermost geocell layer and of the geocell inter-layer spacing should be 0.2 times plate diameter), repeated loading was
16 applied to installations in which the number of geocell layers and the presence or absence of shredded rubber layers in the
17 backfill was changed. The results of the testing reveal the ability of the composite geocell-rubber-soil systems to
18 ‘shakedown’ to a fully resilient behavior after a period of plastic deformation except when there is little or no
19 reinforcement and the applied repeated stresses are large. When shakedown response is observed, then both the
20 accumulated plastic deformation prior to a steady-state response being obtained and the resilient deformations thereafter
21 are reduced. Efficiency of reinforcement is shown to decrease with number of reinforcement layers for all applied stress
22 levels and number of cycles of applied loading. The use of granulated rubber layers are shown to reduce the plastic
23 deformations and to increase the resilient displacements compared to the comparable non-rubber construction. By optimal
24 use of geocells and granulated rubber, deformations can be reduced by 60-70% compared with the unreinforced case
25 while stresses in the foundation soil are spread much more effectively. On the basis of the study, the concept of combining
26 several geocell layers with shredded rubber reinforcement is recommended for larger scale trials and for economic study.

27

28 **Keywords:** Pavement foundation, Repeated loading; Multiple geocell layers; Rubber-soil mixture layer; Residual and
29 resilient deformations.

30

31 **1. Introduction**

32 Geosynthetic-reinforced soil offers economy, ease of installation, performance and reliability in many areas
33 of geotechnical engineering e.g., construction of footings over soft soil, stable embankments, slope and earth
34 stabilization, road construction layers, and pavement system (e.g., [Hufenus et al., 2006](#); [Dash et al., 2007](#);
35 [Bathurst et al., 2009](#); [Madhavi Latha and Somwanshi, 2009](#); [Zhang et al., 2010](#); [Pokharel et al., 2010](#);
36 [Moghaddas Tafreshi and Dawson, 2012](#); [Boushehrian et al., 2011](#); [Lambert et al., 2011](#); [Koerner, 2012](#). [Yang](#)
37 [et al. 2012](#); [Thakur et al., 2012](#); [Tavakoli et al., 2012](#); [Leshchinsky and Ling, 2013](#); [Tanyu et al., 2013](#), [Chen](#)
38 [et al., 2013](#)).

39 [Boushehrian et al. \(2011\)](#) investigated the cyclic behavior of three-dimensional (a grid-anchor
40 reinforcement system) reinforced sand by conducting a series of field tests. They reported the benefit of the
41 three-dimensional reinforced system over the conventional geomesh system in reducing the settlements of
42 foundations rested on sand bed. [Thakur et al. \(2012\)](#) investigated the performance of single geocell-reinforced
43 recycled asphalt pavement (RAP) bases, reporting that the geocell-reinforced RAP bases had much smaller
44 permanent deformations and smaller vertical stresses than unreinforced base, at the interface between base
45 and subgrade.

46 Overall, geosynthetic inclusions would be most effective if used in the zone significantly stressed by the
47 loading surface (e.g., footing or tire wheel) – which may be over a depth of 1 or 2 width/diameters beneath the
48 footing/tire wheel – i.e. over a depth of approximately 0.6 – 2 m for typical footing widths and over a depth of
49 0.3 – 0.6 m for typical tire wheel widths. Since, the heights of commercially produced geocells are usually
50 standard and manufacturers of geocell produce them at heights less than 200 mm (available cell depths
51 produced by two key manufacturers in Europe and the USA), using a 0.6 to 2 m single thick layer of geocell
52 beneath the footing and tire wheel is not possible for field construction. Even if it were, such a thick geocell
53 layer would likely make compaction of cell-fill extremely difficult ([Thakur et al. \(2012\)](#) and as has been
54 demonstrated by the authors' observation and the result of tests not reported here), consequently decreasing
55 the performance of a thick single layer of geocell. Hence, if such a thickness of soil were to be reinforced by
56 geocells, it would require, say, 3 or 4 layers with thickness ≤ 200 mm.

57 In the last decades, the volume of used tire rubbers in the world have been significantly increased due to
58 the developing industry and growing population ([WRAP, 2007](#); [RMA, 2007](#); [RRI, 2009](#)) and their disposals
59 have, therefore, become a major environmental problem worldwide. Large numbers of scrap tires are either

60 dumped in landfills or stockpiled across the landscape in huge volume (Cetin et al., 2006; Chiu, 2008). It
61 makes them harder and more expensive to dispose of safely without threatening human health and
62 environment. For instance, stockpiled waste tires are flammable, prone to fires with toxic fumes and may then
63 cause a major health hazard for both human beings and animals (Attom, 2006).

64 Hence, to consider the environmental concerns and a greater willingness, the use of waste tires in the
65 form of strips, chips, and granules, are now considered as construction materials (Tanchaisawat et al., 2010;
66 Lovisa et al., 2010; Tavakoli et al., 2012; Moghaddas Tafreshi et al., 2012; Edinçliler and Cagatay, 2013).
67 When the chipped, shredded and granulated tire rubbers are mixed with soil (or the strips of tire used as
68 reinforcement), the mixture can behave as a composite material. It becomes a form of reinforced soil, similar
69 to geosynthetic-reinforced soil, that can be advantageously employed to increase soil strength (Yoon et al.,
70 2008; Tavakoli et al., 2012). The cyclic load response of rubber-soil mixtures (e.g. as identified by Bosscher
71 et al., 1997; Feng and Sutter 2000; Edinçliler et al., 2004; Prasad and Prasada Raju, 2009) has shown the
72 material's potential as a composite material, particularly in applications in roads, highways, and
73 embankments. Bosscher et al. (1997) used tire-chips in soil to form a laboratory model embankment which
74 was then subjected to simulated, repeated traffic loads. Less surface plastic displacement was reported when
75 the tire-chips were covered by a relatively thick soil-only layer than when the tire-chips were placed in the
76 whole of the fill. The soil cap over the tire-chips not only reduces the on-going settlement, but also prevents
77 tire shreds from possible ignition.

78 On the basis of this review, the present authors considered that there could be potential for combining
79 these two techniques (combining the layers of geocell with rubber-soil mixture layers) to improve the strength
80 and to reduce the deformation within pavement foundations and, specifically, weak locations in these layers
81 (e.g. trench reinstatements).

82 However, the economic evaluation of a complex rubber-soil mixture together with multiple geocell layers
83 would be an essential consideration of any practical project. So far this has not been investigated in any recent
84 research and, regrettably, space doesn't allow this aspect to be investigated here. In Europe at least, the ban on
85 land-filling of old tires makes, in principle, economic sense of the beneficial reuse of rubber and the economic
86 incentive to provide safe, post-consumer uses of rubber may be sufficient to partially finance the geocell
87 reinforcement. This possibility should be studied further. With the evident benefit of using multiple geotextile

88 or geogrid layers (e.g. [Sitharam and Sireesh, 2005](#)), the use of multiple geocell layers could be effective.
89 Although it might be anticipated that more geocell layers in a foundation bed reduce the deformations, but
90 there is much detail of the use of multiple geocell layers with and without rubber-soil combinations under
91 repeatedly applied loads which has not been investigated by researchers. Consequently, this paper seeks to
92 address the concept of the reinforcing benefit of the added rubber in association with the geocell layers which
93 would have application, potentially, to pavement foundation (or machine support) systems.

94 **2. Objectives**

95 The overall goal was to demonstrate the benefits of introducing multi-layered geocell and combining this
96 with rubber reinforcement to address weak spots in pavement foundations (e.g. at trench reinstatements).
97 Cyclic loading conditions were selected as these are of particular concern for pavement (or machine
98 foundation) problems where localized soil reinforcement might be appropriate. Thus a total of 21 independent
99 cyclic plate load tests (plus 13 repeated tests) of a pavement foundation supported on unreinforced soil or soil
100 reinforced with geocell and rubber were performed in a test pit measuring 2000×2000 mm in plane and 700
101 mm in depth using a 300 mm diameter rigid steel plate. Testing was arranged so as to determine the
102 parameters controlling best usage. The specific aims were to study (The numbers in parentheses
103 indicated the relevant results section):

- 104 • the optimal depth of the top geocell layer (6.1),
- 105 • the optimal vertical spacing between successive layers of geocell (6.2),
- 106 • the effects of the number of geocell layers on residual and resilient settlements (6.3.1 and 6.3.2),
- 107 • the effects of the geocell layers on the stress profile with depth (6.3.3), and
- 108 • the additional effect of the rubber-soil mixture layers on the residual and resilient settlements (6.4.1
109 and 6.4.2) and on the stress profile (6.4.3).

110 **3. Test Materials**

111 **3.1. Soil materials**

112 The backfill soil selected for the testing program was sourced from a local quarry and satisfies the criteria
113 and limitations recommended in [ASTM D 2940-09](#). It was a sandy soil passing through the 38 mm sieve (see
114 Fig. 1) with a specific gravity, G_s , of 2.65. According to the Unified Soil Classification System ([ASTM D](#)
115 [2487-11](#)), the sand is classified as well graded sand with letter symbol *SW*. According to the modified proctor
116 compaction tests ([ASTM D 1557-12](#)), the maximum dry density was about 20.62 kN/m³, which corresponds
117 to an optimum moisture content of 5.7%. The angle of internal friction (ϕ) of sand obtained through triaxial
118 compression tests at a wet density of 19.58 kN/m³ (corresponding to 90% of maximum dry density) was
119 40.5°. This soil was used to fill the cells of the polymeric reinforcement and, when required, mixed with
120 rubber for use between the geocell layers.

121 The natural ground soil, at the bottom and four side walls of the test pit, has a maximum particle size of
122 about 20 mm and a specific gravity, G_s , of 2.62. This soil is classified as SP in the Unified Soil Classification
123 System ([ASTM D 2487-11](#)). The wet density and the natural moisture content of this soil were measured as
124 17.9 kN/m³ (it corresponds to 90% of maximum dry density of 20.25 kN/m³) and 9%, respectively. The angle
125 of internal friction (ϕ) of the natural soil at a wet density of 17.9 kN/m³ was 32.5°. The dimensions of the
126 excavated test pit relative to the loading plate diameter are sufficient to minimize boundary effects. The
127 natural ground soils were selected so as not be excessively soft and weak. In this way the assessment of
128 reinforcing benefit from the installations investigated might be conservative. However, the use of a softer
129 subgrade might show the benefits of rubber-soil with geocells to be even better.

130 **3.2. Geocell reinforcement**

131 A geocell was chosen that had been fabricated from a non-woven geotextile by thermo-welding so as to
132 form a “honeycomb” arrangement (Fig. 2). When filled with soil this geocell provides confinement chambers
133 for the soil, thereby developing frictional strength in the soil and shear resistance at the soil-geocell interfaces
134 due to locally high passive earth pressure. The overall effect is to restrict lateral displacement of infill, to
135 increase the bearing pressure, and to limit the subsidence of the foundation. Strong welds and parent material
136 are required to ensure reliably high load-bearing capacity, otherwise rupture of the reinforced soil could result
137 ([Moghaddas Tafreshi and Dawson, 2012](#)). According to the manufacturer, the strength and stiffness of the
138 geocell joint is higher or similar to that of the geocell wall material (i.e. geotextile). The engineering

139 properties of the geotextile from which geocell is formed and the geometry of the geocell, as listed by the
140 manufacturer, are presented in Table 1. Geocell pocket size ($d=110\text{ mm}$), loading plate diameter ($D=300\text{ mm}$)
141 and height of geocell ($H_g=100\text{ mm}$) were kept constant. However, the d/D ratio adopted may not be the
142 optimum value and a change in d/D might change the results. The effect of d/D could be investigated in future
143 studies.

144 **3.3. Rubber**

145 The rubber used in the study comprised granulated particles with a specific gravity, G_s , of 1.17, between
146 2 mm and 25 mm sieve size, and a mean particle size of 14 mm. The rubber particles were clean and free of
147 any steel and cord. Fig. 1 and Fig. 3 show, respectively, the grading and a photograph of this material. When
148 required (see Section 5), to form the combined soil and rubber mixtures placed between the layers of geocell,
149 the backfill soil and the rubber were carefully blended into the soil using a mixer, with manual intervention if
150 necessary, so as to produce a reasonably uniform, non-segregated, rubber-soil mixture.

151 **4. Full scale model test**

152 To evaluate the performance improvement in the deformation and the stress profile of pavements supported
153 by layers of geocell and by layers of rubber-soil mixture, and to provide realistic test conditions, a full scale
154 model test of a standard plate load was conducted. The schematic cross-section of the test set-up of the
155 foundation bed containing a model test pit trench, geocell-reinforcement layers, rubber-soil mixture layers, the
156 loading plate model, loading system and data measurement system (dial gauges and soil pressure cells), the
157 geometry of the test configurations, and location of three soil pressure cells, is shown in Fig. 4.

158 **4.1. Test pit and instrumentation**

159 All plate load tests were conducted in an outdoor test pit (see Acknowledgements). The test pit, measuring
160 $2000\text{ mm} \times 2000\text{ mm}$ in plan, and 700 mm in depth, was excavated in natural ground to construct the geocell
161 layers, rubber-soil mixture layers and to install the pressure cell at specified depths. The load application
162 system was an hydraulic jack imposed by a manually-operated pump and supported against a strong reaction
163 beam spanning the width of the test pit. The steel rigid circular plate of 300 mm in diameter and 25 mm in
164 thickness was placed on the surface at the center of the installation. An additional 10 mm thick rubber base

165 was attached at the bottom of the loading plate to simulate the rubber tire contact with the ground surface. To
166 measure the movement of the plate, throughout the tests, three linear dial gauges with an accuracy of 0.01%
167 of full range (100 mm) were attached to a reference beam and their tips placed about 10 mm inwards from the
168 edge of the plate. Also, to measure the vertical stress inside the foundation bed, it was instrumented with three
169 full bridged, 50 mm diameter diaphragm-type soil pressure cells (SPC). These had an accuracy of 0.1% of full
170 range of 1000 kPa according to the manufacturer. The top soil pressure cell (abbreviated to “T.SPC”), middle
171 soil pressure cell (“M.SPC”), and bottom soil pressure cell (“B.SPC”) are located at 190 mm, 350 mm, and
172 510 mm beneath the center of loading plate (Fig. 4). The instruments’ output was recorded in mV and then
173 converted to stress units using established calibrations for the sensors. To ensure an accurate reading, all of
174 the devices were calibrated prior to each test series.

175 Since the pressure cells are located at the middle of soil layers or at the middle of the rubber-soil mixture
176 layers (see Fig. 4), to simulate the real test condition and to obtain the calibrations for the pressure cells, a 300
177 mm-diameter and 200 mm-high cylinder container made of very soft textile was filled with the soil/soil-
178 rubber mixture and each cell was placed, in turn, in the middle. The container was then placed in a
179 compression machine and the cells were calibrated for different levels of cyclic applied pressure. A
180 photograph of the test installation prior to testing, showing the reaction beam, load plate, hydraulic jack and
181 three dial gauges is presented as Fig. 5.

182 **4.2. Backfill compaction**

183 In order to compact the layers of the foundation including unreinforced soil, geocell-reinforced layers and
184 rubber-reinforced layers, a walk-behind vibrating plate compactor, 450 mm in width, was used. In all the
185 tests, the compactor passed over the backfill at ten levels being 0, 60, 160, 220, 320, 380, 480, 540, 640, and
186 700 mm from the level of the base of the loading plate. To achieve the required density of soil that filled the
187 geocell pockets (see Table 2), more passes of the compactor were needed compared to the unreinforced layer.
188 Hence, the unreinforced layers, geocell reinforced layers and rubber soil mixture layers were compacted at an
189 optimum moisture content of 5.7% with two, three and three passes, respectively so that the compactive
190 effort, and consequently compaction energy, was kept the same for all passes of the compactor. To better
191 assess the layers’ compaction, three sand cone tests in accordance with [ASTM D 1557-12](#) were conducted in

192 some installations and after layer compaction, to measure the densities and moisture content of compacted soil
193 layers, rubber-soil mixture layers and the density of the soil filled into the geocell pockets. The density values
194 measured in the three cone tests revealed a close match with maximum differences in results of only a rather
195 small 1-1.5%. The average measured (recovered) moisture content of the layers was between 5.2% and 5.7%.
196 To prevent loss of moisture from the backfill during the load test, the exposed backfill was covered to a
197 distance of 1.8 m from the circumference of the bearing plate with a waterproof paper. Table 2 shows the
198 average measured dry densities (average of three sand cone tests) of unreinforced soil, the soil filled in geocell
199 pockets, and rubber-soil mixture after compaction of each layers. Note the reduction in density as a
200 consequence of compaction inside geocell pockets and due to the partial replacement of mineral by the less
201 dense rubber particles and of the differing void ratios.

202 ***4.3. Loading system and simulated tire pressure***

203 The loading arrangements were chosen to represent the tires of typical trucks on a pavement. While general
204 traffic loading will not be applied to the geocell-aggregate layers but millions of times to overlying asphalt
205 layers, such loading will be applied for a few traffic passages during construction and this will, likely, be the
206 most demanding time for the reinforced foundation. In addition, [AASHTO T 221-90](#) and [ASTM D D1195-09](#)
207 recommend application a few load cycles using repetitive static plate load tests of flexible pavement for use in
208 evaluation and design of airport and highway pavements. It is this loading which was simulated in the work
209 described here by distributing wheel loads over an equivalent circular area at the appropriate tire pressure
210 ([Brito et al., 2009](#)).

211

212 Hence, in order to simulate the effect of wheel loading, unloading and reloading were imposed through the
213 plate at a rate of 1.5 kPa per second. The maximum applied pressure was chosen to replicate that of a heavy
214 vehicle half-axle with “Super-Single” tire, as used on a common heavy trailer (6 axles and a mean pressure
215 792 kPa) ([Brito et al., 2009](#)) and was divided into two stages being 400 and 800 kPa to simulate half and full
216 traffic loadings. For each stage, fifteen loading and unloading cycles were applied. Preliminary repeated load
217 tests (which are not reported in the paper) showed that (regardless of the number of geocell layers, number of
218 rubber-soil mixture layers and the amplitude of applied load) with increase in the number of load cycles, the

219 rate of change of loaded surface deformations reduces, so that their response has become, approximately,
220 stable within fifteen load cycles. This implies that a large number of cyclic load applications were not
221 essential.

222 Although, the rotating stress field applied by a wheel passage is rather different from the cyclic axial
223 loading applied in these tests, yet [Kim and Tutumluer \(2005\)](#) showed that cyclic plate load tests can deliver
224 useful results in the absence of moving wheel load test. Thus, any benefits of the geocell and rubber
225 reinforcements arrangements discovered in the present study may be anticipated to under-estimate those that
226 might be experienced under wheeled traffic. Therefore, this limitation in the present work isn't expected to be
227 very influential on the outcomes.

228 **5. Test program**

229 Five test series for the unreinforced bed, the multi-layered geocell and the combined use of geocell
230 reinforcement layers and rubber-soil mixtures reinforcement layers were conducted (see Table 3 for details).
231 Test Series 1 provided reference, unreinforced, performance data. Test Series 2 and 3 were performed to
232 obtain the optimum values of the depth of the first layer of geocell reinforcement beneath the loading plate
233 (u), and the vertical spacing of the geocell layers (h). To investigate the effect of number of geocell layers on
234 the deformation response of pavement, Test Series 4 was conducted by varying the number of geocell layers
235 ($N_g=1, 2, 3, 4$), when the layers of geocell were placed at the optimum values of u/D and h/D ($u/D=h/D=0.2$)
236 previously identified by Test Series 2 and 3.

237 To investigate the beneficial effect of combined use of geocell reinforcement layers and rubber-soil
238 mixtures reinforcement layers on deformation of loading plate and on the stress profile with depth, Test Series
239 5 was conducted. In these tests equal numbers of layers of each type (i.e., $N_g=N_{rs}=1$; $N_g=N_{rs}=2$; $N_g=N_{rs}=3$ and
240 $N_g=N_{rs}=4$) were used, where N_{rs} is the number of soil-rubber layers. In the Test Series 5, the soil layers
241 between the geocell layers (with thickness of h) are substituted by mixed rubber-soil layers (with thickness of
242 h_{rs}), so that $h/D=h_{rs}/D=0.2$. Granulated rubber was used at a mass replacement rate of 8% (a value based on
243 the findings of the authors in earlier work ([Moghaddas Tafreshi et al., 2013](#)) which used static plate loading of
244 a combined multi-layered geocell and rubber reinforced foundation to determine the optimum replacement

245 proportion) in the middle of the rates of 6% and 10% recommended, respectively, by Prasad and Prasada Raju
246 (2009) and Munoli et al (2013).

247 The width of the both geocell and rubber-soil mixture layers (b) and the depth to the top of the first geocell
248 layer below the footing (u) are expressed in non-dimensional form with respect to loading plate diameter
249 ($D=300\text{ mm}$) as, b/D and u/D . In line with the findings of Dash et al., (2003), Yoon et al., (2008) and Thakur et al.,
250 (2012), the parameter b/D was held constant in all the tests at $b/D=5$. The variable parameter, h , is used to
251 describe the vertical spacing between the bottom of the previous layer of geocell and the top of the next layer.
252 It is expressed in non-dimensional form with respect to loading plate diameter (D) as h/D , whereas the height
253 of geocell layers (H_g) is expressed in dimensional form (100 mm) and the height of the rubber-soil mixture
254 layers (h_{rs}) is considered equal to h (the vertical spacing between the bottom of the previous layer of geocell
255 and the top of the next layer).

256 In order to assess the utility of the apparatus, the accuracy of the measurements, the repeatability of the
257 system, the reliability of the results and finally to verify the consistency of the test data, many of the tests
258 described in Table 3 were repeated at least twice. The results obtained revealed a close match between results
259 of the two or three trial tests with maximum differences in results of around 6-8%. This difference was
260 considered to be small and is subsequently neglected. The consistency of the results demonstrates that the
261 mixture of soil and rubber, the test procedure and technique adopted can produce repeatable tests within the
262 bounds that may be expected from geotechnical and pavement testing apparatus.

263 **6. Results and discussion**

264 In this section, the results of cyclic plate load tests are presented along with a discussion highlighting the
265 effects of the different parameters. The performance improvement of the reinforced bed is represented here by
266 variations in the plate settlement and the distributed pressure at depth of the pavement foundation beds. Note
267 that, in order to save time in Test Series 2 and 3, only one load cycle for each of the six cyclic pressures (150,
268 300, 400, 600, 700, and 800 kPa) was applied on the same section used for each installation with a particular
269 u/D and h/D ratio. In Test Series 1, 4 and 5, fifteen cycles of loading and unloading at 400 and 800 kPa
270 pressure were applied on the same section used in each test.

271 **6.1. The optimum value of the depth of the first layer of geocell layer (u/D ratio)**

272 Variation of residual plastic deformation of the loading plate (averaged from three dial gauges) as a
273 function of the depth of the first layer of geocell reinforcement beneath the loading plate (u/D ratio) with a
274 single layer of geocell reinforcement ($N_g=1$) at different amplitudes of cyclic load (=150, 300, 400, 600, 700,
275 800 kPa) is shown in Fig. 6 (Test Series 2). In these tests, only one cycle of load was applied at the surface of
276 loading plate. This figure shows that the value of plastic deformation increases with increase in the applied
277 cyclic pressure, irrespective of the u/D ratio. From this figure, it is found that the minimum value of plastic
278 deformation was obtained at a u/D value of approximately 0.2, irrespective of amplitude of cyclic load. The
279 figure shows the plastic deformation of the geocell reinforced bed initially decreases while the depth of
280 placement increases from $u/D=0$ to $u/D\approx 0.2$, but that, thereafter, with increase in the u/D ratio, the value of
281 plastic deformation increases again. The slight increase in performance improvement until $u/D\approx 0.2$ could be
282 due to the surface soil layer, above the first geocell layer, acting as a cushion, preventing the direct contact of
283 the loading plate base with the cell walls and distributing the applied pressure more uniformly over the
284 cellular geocell. The other probable reason why a small cover thickness is desirable is that the confinement
285 provided by the soil above the geocell layer helps to develop frictional resistance between the geocell and the
286 soil. Similar findings, under monotonic loading have been reported by [Sitharam and Sireesh \(2005\)](#) and [Yoon
287 et al. \(2008\)](#),

288 Likewise, as the value of u/D increases beyond 0.2 (toward 0.6), the top geocell layer moves out of the
289 zone where it can most successfully interrupt the applied stress field and, hence, the plastic deformation
290 increases. Finally, as expected, with increase in u/D ratio to about one, the geocell layer lies almost entirely
291 outside of the significantly stressed zone under the loading plate so that the influence of reinforcement
292 becomes negligible, and the overall response approaches that of an unreinforced pavement foundation.

293 Although the optimum u/D value might be a function of loading plate size, the height of geocell layers,
294 the geocell pocket size, type of soil and the number of geocell layers, in the present study, in all the
295 subsequent plate load tests, the geocell reinforcement was placed at $u/D=0.2$. [Yoon et al. \(2008\)](#), in their
296 studies using a circular plate of diameter (D) 350 mm resting on sand reinforced with multiple layers of
297 ‘Tirecell’ (made from treads of waste tires), reported a similar finding for a u/D ratio ($u/D=0.2$). Therefore, in
298 the present study, use of u/D ratio of 0.2 appears defensible.

299 **6.2. The optimum value of the vertical spacing of the geocell layers (h/D ratio)**

300 Fig. 7 illustrates the variation of residual plastic deformation of loading surface with vertical spacing of
301 the geocell layers (h/D ratio) for two layers of geocell ($N_g=2$) at different amplitudes of cyclic load (= 150,
302 300, 400, 600, 700, 800 kPa) - the results of Test Series 3. In these tests only one cycle of load was applied.
303 From this figure, it can be seen that, regardless of the amplitude of cyclic load, the plastic deformation is
304 minimized when the h/D ratio is approximately, 0.2. The reduction in plastic deformation at h/D of 0.2 may
305 be attributed to the behavior of the soil layer between the first and the second layers of geocell. At small
306 thicknesses it provides effective load spreading without deforming much laterally as it is confined by the
307 geocell reinforcement above and below. However, if the reinforcing layers become too widely spaced, then
308 the material between the geocell layers can be displaced, weakening the overall response. [Yoon et al. \(2008\)](#)
309 in their studies using static plate loading test (see end of section 6.1, above) reported that the effective
310 placement of 'Tirecell' reinforcement was best at a vertical spacing of reinforcement layers of 0.2 times the
311 plate diameter. It is of interest to note that, in spite of differences between the present study and the studies of
312 [Yoon et al. \(2008\)](#) in the footing size, the soil properties, type of 3D reinforcement, the geometric dimensions
313 of the reinforcement, and the type of loading (they used the monotonic loading whereas this study also
314 investigates unloading) the optimum values of u/D and h/D from the present study are consistent with those
315 reported by [Yoon et al. \(2008\)](#).

316 In addition, it can be seen from Fig. 7 that the effect of geocell-reinforcement spacing is more significant
317 at higher amplitudes of cyclic load, whereas for the low amplitude of cyclic load, the improvement in plastic
318 deformation does not vary much with the variation in reinforcement spacing. It indicates that at low stress
319 amplitude levels the second layer of geocell has hardly been strained by the load applied to the soil surface
320 and, consequently, has little beneficial effect.

321 Likewise, Fig. 7 shows an increase in the plastic deformation, regardless of the amplitudes of cyclic load,
322 with increasing h/D beyond the optimum value. It would be expected that, when the value of h/D reaches a
323 thickness of 0.8-1 times the loading plate diameter, the second geocell layer would be, largely, outside of the
324 zone of significant stress due to the surface loading, so that its influence on foundation bed behavior would
325 become negligible and the behavior of a reinforced system with two layers of geocell would tend to that of a
326 reinforced system supported by a single layer of geocell. The results of experimental studies conducted by

327 [Chen et al. \(2013\)](#) and [Abu-Farsakh et al. \(2008\)](#) indicated that the vertical spacing of planar reinforcement
328 layers needs to be less than 0.5 times of footing width to prevent the failure between reinforcement layers
329 from occurring.

330 Hence, in the present study, and in order to investigate the effect of multi-layered geocell and to
331 investigate the effect of rubber-soil mixture layers between geocell layers on the behavior of reinforced
332 system, the h/D ratio was subsequently maintained at 0.2.

333 **6.3. The effect of the number of geocell layers on the behavior of the pavement foundation**

334 The effect of the number of geocell layers on total deformation, permanent plastic deformation, and
335 resilient displacement of loading plate, and on the pressure distributed through the pavement foundation bed
336 (the results of Test Series 5) is the subject of this section. In this Test Series thirty loading and unloading
337 cycles were applied. Fifteen first cycles and fifteen second cycles were applied to the loading plate with
338 amplitudes of 400 and 800 kPa, respectively. As the preliminary tests had shown that 15 cycles of loading
339 were sufficient to obtain a fully resilient response at the low level of cyclic pressure (400 kPa), the interest
340 was to establish the likelihood of such a response being disturbed by a greater cyclic pressure (800 kPa) .

341 *6.3.1. The effect of geocell layers on deformation of the pavement foundation*

342 The variation of the loading plate deformation (including the accumulated residual (plastic) deformation
343 and resilient (elastic rebound) displacement) with the number of load cycles for the unreinforced system and
344 the multi-layered geocell reinforced system with one, two, three, and four layers of geocell ($N_g=1, 2, 3, 4$),
345 when the layers of geocell were placed at the optimum values of u/D and h/D ($u/D=h/D=0.2$), is shown in Fig
346 8a. Also, the residual plastic deformation of the unreinforced and reinforced bases with the number of loading
347 cycles is shown in Fig. 8b. This figure shows that for the unreinforced and reinforced bases, an initial, rapid
348 total deformation (Fig. 8a) and rapid residual deformation (Fig. 8b) during the first load applications is
349 followed by secondary deformation that develops at a slower rate. Both the total and plastic deformations
350 caused by the first cycle of applied load form a large portion of the final deformation after all cycles. Overall,
351 in most of the tests performed on the unreinforced and the geocell reinforced foundation, the initial, rapid
352 deformation that took place due to the first cycle of loading gave rise to between 25% and 70% of the
353 accumulated plastic deformation. This ratio is greater for the unreinforced foundation than for the reinforced

354 foundation. The actual proportion appears to depend on the mass of reinforcement and on the magnitude of
355 the applied cyclic load.

356 Fig. 8 shows that the total and residual deformations of the unreinforced pavement foundation material
357 tend to increase with the number of load cycles. There is a non-stabilizing response; eventually leading to
358 plastic failure, particularly at higher levels of cyclic loads (i.e., 800 kPa). The authors note that a large
359 deformation in these tests is not the primary means of judging unsuitability of the arrangements under test but,
360 rather, a non-stabilizing response. Large deformations could largely be dealt with in practice by compaction,
361 whereas instability responses are destructive.

362 For the reinforced bases, regardless of the number of geocell layers, the rate of change of both total and
363 the residual deformation of the loaded surface reduces as the number of load cycles increases, so that their
364 response has become, approximately, stable after fifteen load cycles (of both 400 and 800 kPa applied load),
365 particularly for the reinforced bases with three and four layers of geocell. The performance of geocell
366 reinforcement in decreasing the deformations may be attributed to the superior confinement offered by the
367 geocell layers in all directions. Thus the multi-cell geometry allows the soil in the cells to develop a passive
368 resistance that increases the soil's bearing capacity and decreases the deformations within the pavement
369 foundation. This behavior is a consequence of the shakedown process as the granular structure of the sand
370 becomes arranged into a progressively more stable arrangement better able to behave resiliently without
371 undergoing plastic deformation. It implies that the reinforced system as compared with unreinforced system
372 (Fig. 8) is storing energy (and releasing it in resilient recovery) rather than the energy being used to cause
373 further damage. This stabilizing response suggests that the early process of reorientation of particles inside the
374 geocell layers, causing local fill stiffening, ceases relative rapidly and the system then reaches a "plastic
375 shakedown" condition, in which subsequent deformation is fully recovered in each cycle. In such a case no
376 yield condition is reached at conventional stress levels. The final deformation value can be referred to either
377 as the "maximum deformation" or the "shakedown deformation (settlement)" (Werkmeister et al. (2001)). The
378 behavioral patterns observed in these tests (Fig. 8) is in-line with those observed in the repeated load testing
379 of unreinforced granular materials as observed by several authors (e.g. [Werkmeister et al., 2001, 2005](#); [Pérez
380 et al., 2006](#)) and as predicted from mechanical interaction considerations ([García-Rojo and Herrmann, 2005](#)).

381 From Fig. 8, it may be clearly observed that, as the number of geocell layers increases (i.e., the increase in
382 the depth of the reinforced zone beneath the loading surface), both the peak and residual deformations of these
383 pavement foundation installations decrease substantially. In order to have a clear comparison of the results for
384 the unreinforced and multi-layered geocell reinforced bases, plots of the peak deformation and residual plastic
385 deformation at load cycle number of 1, 5, 10, and 10 ($n=1, 5, 10, 15$), for the two applied load levels of 400
386 and 800 kPa, with the number of geocell layers (N_g) are shown in Fig. 9.

387 The results in Figs. 8 and 9 depict that, the maximum and residual deformations of the loading plate are
388 considerably decreased relative to the unreinforced deformation as a consequence of the increase in the
389 number of geocell layers, regardless of the level of applied repeated load and the load cycle number. For
390 example, from Fig. 9b at 800 kPa amplitude of applied load and at load cycle number of 15, the residual
391 deformation values are about 41.03, 33.02, 23.10, 17.43, and 15.39 mm for unreinforced bed, and reinforced
392 bed with one, two, three and four layers of geocell, respectively. This example provides clear illustration how
393 the rate of reduction in the residual plastic deformation (and also the total deformation, in Fig. 9a) reduces
394 with increase in the number of geocell layers (N_g). [Thakur et al. \(2012\)](#) reported similar results of the total and
395 residual deformations with number of loading cycles and with height of single geocell-reinforced bed.

396 No marked further decrease in the total and residual deformations would be expected, at both amplitudes
397 of 400 and 800 kPa of cyclic load, if the number of geocell layers were to increase to 5 layers. Obviously, the
398 greater number of geocell reinforcement layer may only be justified at the highest amplitude of cyclic load if
399 at all.

400 The effect of the amplitude of the cyclic load on the deformations of the loading surface of unreinforced
401 and geocell-reinforced foundations is clear from Fig. 8. As expected, the increase in the cyclic load magnitude
402 causes a direct increase in deformation for both unreinforced and reinforced systems, irrespective of the
403 number of geocell layers. Consider, for example, the residual plastic deformations for the reinforced bed with
404 four layers of geocell ($N_g=4$). At the end of loading deformations are 5.53 and 15.39 mm for magnitudes of
405 cyclic load that are 400 and 800 kPa, respectively. This example shows that the residual plastic deformation
406 varies non-linearly with amplitude of load cycle (the deformation grew by a factor of about three whereas the
407 amplitude of load cycle only doubled).

408 Also, from Fig. 9, it can be seen that the rate of enhancement in both maximum and residual plastic
409 deformations decreases steadily with increase in the number of load cycles (the distance between the curves
410 decreases with increase in the number of load cycles). Consequently, one can anticipate that the enhancement
411 rates will become almost insignificant with further increase in the number of load cycles or in the number of
412 geocell layers (N_g).

413 6.3.2. *The effect of geocell layers on resilient displacement ratios*

414 The resilient displacement (i.e. elastic rebound, defined as the difference between the deformation under
415 loading and under the corresponding unloading condition), due to storing energy, plays a key role to decrease
416 the accumulated residual plastic deformation of pavement foundation. To show this role, the variation of
417 resilient displacement ratio during unloading cycles (defined as the ratio of resilient displacement at each
418 cycle to the total deformation from the first cycle) for the unreinforced and geocell reinforced systems with
419 one, two, three, and four layers of geocell, is shown in Fig. 10. This figure shows that, regardless of the mass
420 of geocell reinforcement, the proportion of resilient displacement decreases rapidly during the first few
421 loading cycles but stabilizes quickly to a constant value with increase in the load cycle number (probably
422 indicative of a densifying effect). However, the reinforced pavement foundations show a much better
423 performance (in decreasing the proportion of resilient displacement and promoting shakedown to a steady-
424 state condition) with increase in the load cycle number as compared to the unreinforced base.

425 As anticipated, the reinforced base with four layers of geocell shows the highest proportion of resilient
426 displacement while the unreinforced base shows the lowest proportion for all the pavement foundations
427 tested. On the other hand, with increase in the number of geocell reinforcement layers, the proportion of
428 resilient displacement increases, irrespective of the amplitude and number of load cycles. For example for the
429 last cycle of loading and unloading (15th cycle of applied load level of 800 kPa), the resilient displacements
430 are 4.63%, 11.47%, 15.75%, 20.70%, and 22.66% of the total deformation for unreinforced and reinforced
431 beds with one, two, three, and four layers of geocell, respectively. A similar resilient response was reported
432 for a recycled asphalt pavement base by [Thakur et al. \(2012\)](#) where the geocell significantly increased the
433 proportion of deformation.

434 Overall, the tests results reveal that the geocell reinforcement improves the resilient behavior in addition to
435 the reduction of the accumulated plastic and total deformation of the pavement foundation. It may be
436 attributed to the increase in the rigidity of the system, restraining the soil against lateral movement with
437 locking-up of the geocell framework.

438 *6.3.3. The effect of geocell layers on stress in the pavement foundation*

439 The variation of maximum measured stress with the number of load cycles, inside the foundation at the
440 three levels of 190 mm (T.SPC) , 350 mm (M.SPC), and 510 mm (B.SPC) beneath the center of loading plate
441 (see Fig. 4) for the unreinforced system and the multi-layered geocell reinforced system is illustrated in Fig.
442 11. For the unreinforced installation and the reinforced installation with one layer of geocell, the top, middle,
443 and bottom soil pressure cells (“T.SPC”, “M.SPC”, and “B.SPC”) are installed and the variation of soil
444 pressure are measured during the cyclic load tests. In order to prevent damage to the soil pressure cells, for the
445 reinforced bases with two layers of geocell, only the middle and bottom soil pressure cells (“M.SPC” and
446 “B.SPC”), and for the reinforced bases with three layers of geocell, only the bottom soil pressure cells
447 (B.SPC”) are installed. For the reinforced bases with four layers of geocell, no pressure cells are installed.

448 The readings of the three soil pressure cells for unreinforced and reinforced bases show an immediate
449 large increase in the vertical stress when the first cycle of loading is applied and then a further, smaller
450 increase over the next 6-8 cycles of loading, thereafter stabilizing to a constant value. This pattern is observed
451 irrespective of applied pressure or of cell depth.

452 The figure also demonstrates the performance of geocell layers, as anticipated, in reducing the pressure
453 transferred through the pavement foundation. For instance, as can be seen in Fig. 11c, with increase in the
454 number of geocell layers from one layer to three, the vertical stress transferred to a depth of 510 mm beneath
455 the center of loading surface, as measured by the bottom soil pressure cell (“B.SPC”), almost halves. For
456 example, under the applied cyclic pressure of 800 kPa, at the end of the load cycles (cycle number 30), the
457 stress measured at 510 mm depth (“B.SPC”) is about 284.5, 223.5, 159.7, 125.2 kPa for unreinforced and the
458 reinforced pavement foundations with one, two and three layers of geocell, respectively. This comparison
459 illustrates the excellent performance of the geocell reinforcement, so that the pressure at a depth of 510 mm
460 decreases to about 35.6%, 27.9%, 20%, and 15.7% of the applied surface pressure (=800 kPa) for the same

461 sequence of constructions. Thus as reinforcing geocell layers are added, the effective load spreading continues
 462 to improve, consequently delivering a better performance, as compared with unreinforced base. On the whole,
 463 the data presented in Figs. 11 and Fig. 9 (variation of residual plastic deformation with the number of geocell
 464 layers) show that multiple geocell layers, particularly the use of three and four layers of geocell, are able to
 465 limit the soil surface deformation and the soil pressure through the depth of the reinforced pavement
 466 foundation. Consequently an increase in road life may be anticipated under the same heavy traffic loading.

467 Considering both the deformation and stress effect, it appears that, cell-pocket structure of the geocell
 468 layer prevents the encased soil from easily moving away from the point of load application. Very probably,
 469 this is achieved by hoop confinement provided by the pocket walls. Thereby the infill cannot easily spread
 470 laterally; hence the shear strength of the composite system is increased.

471 This mechanism would allow the geocell layer to act like a soft plate with high flexural stiffness,
 472 spreading the applied load over an extended area, and decreasing the stress at depth in the pavement
 473 foundation (Moghaddas Tafreshi and Dawson, 2012; Thakur et al., 2012). This stated another way; the
 474 geocell seems able to effectively attenuate the vertical applied stress in the soil because it provides a good
 475 connection between the loaded area and anchorages on both sides of the loaded area (Tavakoli et al., 2012).

476 **6.4. The combined effect of geocell layers and rubber-soil mixture layers**

477 To investigate the beneficial effect of mixing reinforcing rubber with soil so as to improve the response of
 478 the pavement foundations to cyclic load, this section concentrates on comparing the effect of multiple layers
 479 of geocell reinforcement system with inter-layer rubber reinforced soil. The tests combined of the same
 480 number of layers of each reinforcement type ($N_g=N_{rs}=1$; $N_g=N_{rs}=2$; $N_g=N_{rs}=3$ and $N_g=N_{rs}=4$). To evaluate the
 481 response, each combined installation is compared to comparable geocell-only installation, i.e. $N_g=1$ is
 482 compared to $N_g=N_{rs}=1$, $N_g=2$ to $N_g=N_{rs}=2$, $N_g=3$ to $N_g=N_{rs}=3$, and $N_g=4$ to $N_g=N_{rs}=4$.

483 **6.4.1. The effect of rubber-soil mixture with geocell layers on deformation of pavement foundations**

484 Fig. 12 compares the variation of the loading plate deformation with the number of load cycles for the
 485 unreinforced system, the multi-layered geocell reinforced system and combined geocell and rubber-reinforced
 486 system. To more clearly demonstrate the performance of the rubber-reinforced soil layers, the same data, but

487 only the residual plastic deformation, is shown in Fig. 13. From these figures, it can clearly be observed that
488 replacing the unreinforced soil beneath the geocell layers with a rubber reinforced soil layer considerably
489 decreases both the total and residual plastic deformations of the loading plate, compared with the response of
490 the unreinforced bed and geocell-reinforced bed, irrespective of the number of reinforcement layers, the level
491 of applied repeated load or the load cycle number.

492 For a more quantitative comparison, and to show more clearly the effect of the rubber soil mixture on the
493 behavior of foundation bed, the values of maximum and residual plastic deformations, as well as the
494 proportion of deformations that are recoverable (i.e., resilient), are tabulated in Table 4. These values are
495 shown for the last cycle of loading (15th load cycle) of the two levels of applied cyclic loads (= 400 and 800
496 kPa).

497 The data presented as Table 4 shows clearly that, as anticipated, both the peak and residual plastic
498 deformations decrease and the proportion of the deformation that is resilient increases with the number of
499 geocell layers. The further benefit to the deformation behavior of combining geocell with granulated rubber-
500 soil layers is also evident. Comparison of the deformation performance of the combined rubber-soil and
501 geocell layer installations with those reinforced by geocell layers alone, reveals that the addition of the rubber
502 treatment cause both the maximum and the residual (plastic) deformations to decrease substantially. For
503 example, consider the second row within the 800 kPa loading section of Table 4 and the $N_g=3 / N_g=N_{rs}=3$
504 cases in this row. In this comparison the residual, plastic, deformation of the pavement foundation reinforced
505 by three geocell layers drops by about 57% compared to that of the unreinforced case and by 68% when
506 reinforced with three layers of geocell and three layers of rubber-soil mixture. For the same installations, the
507 last row in Table 4 shows that all the reinforced installations exhibit greater proportion of deformations (that
508 is resilient) than does the unreinforced pavement foundation and that the combined geocell and rubber
509 reinforcement layers increase the proportion of deformations from the values obtained for the geocell layers-
510 only installation. Thus all the reinforced installations appear to reduce plastic deformations, in part, by storing
511 energy in resilient deformation, but this effect is increased by the addition multiple rubber-treated soil layers.
512 Given the reduction in plastic deformation at the same time as the resilient deformation increases, it follows
513 that the pavement foundations are becoming much more resilient installations – the proportion of
514 deformations increases by about 2.5-5 times over that of the unreinforced installation, irrespective of the

515 reinforcement type or applied load. As energy is absorbed through the deformation of the rubber particles
516 themselves (Feng and Sutter, 2000, Tavakoli Mehrjardi et al., 2012), it is, perhaps, surprising that the addition
517 of the rubber in the study described here does not lead to much greater deformations as a result of the
518 reinforcement effect of the rubber in the mixture.

519 6.4.2. *The effect of rubber-soil mixture with geocell layers on pressure distribution*

520 Fig. 14 illustrates the variation of stress inside the pavement foundation bed at two depths, 190 and 350
521 mm, beneath the center of loading plate (“T.SPC” and “M.SPC” in Fig. 4), with the number of load cycles.
522 Results are presented for the unreinforced, the geocell-reinforced and the combination reinforced pavement
523 foundations. Due to equipment availability and the need to protect them from stress concentrations, it was not
524 possible to monitor the stresses at all depths in all installations.

525 Fig. 14 depicts a further aspect of the improvement caused by the treatments – the reduction in stress with
526 depth. For example, as can be seen in Fig. 14b, for the applied cyclic pressure of 400 kPa at the soil surface,
527 by the end of the 15th load cycle the pressure at a depth of 350 mm measured by the middle soil pressure cell
528 (“M.SPC”) is about 181.1, 120.1, and 75.30 kPa for unreinforced, reinforced bed with two layers of geocell
529 ($N_g=2$), and the combined rubber and geocell-reinforced bed (two layers of each: $N_g=N_{rs}=2$), respectively. The
530 values above are about 0.45, 0.3, and 0.19 times the applied surface pressure of 400 kPa, with the installation
531 containing the combination two geocell and two rubber-soil mixture layers ($N_g=N_{rs}=2$) delivering a 37.3%
532 reduction in stress compared with the performance offered by the installation with two geocell layers only
533 ($N_g=2$).

534 Thus the addition of the rubber-soil mixture effect allows more load-spreading, consequently delivering
535 an improved performance. The beneficial effect of the rubber-soil mixture beneath the geocell layers may be
536 attributed to two reasons:

537 (1) the granulated rubber has a reinforcement effect, although the reasons for this are not clear. It may be
538 that the particle-scale heterogeneity allows tensile loads to be carried between granular particles via adjacent,
539 extensible, rubber particles. It may be for some other reason;

540 (2) the rubber-soil mixture layer is able to absorb more energy than the soil alone. Consequently, plastic
541 deformations are reduced and load spreading increased, the latter effect leading to reduction of stress with
542 depth.

543 In addition, to the benefits identified above, the inclusion of rubber would also, in principle, cause
544 considerable increase in environmental and economic benefits by reusing otherwise waste rubber. Despite the
545 benefits identified, it is expected that the contribution of the rubber to the treated soil's performance will be
546 highly dependent on the size of the rubber fragments, the type of rubber and the proportion added to the soil.

547 **7. Summary and conclusion**

548 A series of cyclic plate load tests was conducted to assess the concept of geocell-reinforced layers and
549 rubber-soil mixture layers as potential pavement foundation improvement techniques. Based on the results of
550 the test program described in this paper, the following conclusions can be made:

551 (1) The optimum embedded depth of the first layer of geocell beneath the loading plate and the optimum
552 vertical spacing of geocell layers, under repeated loads, based on plate settlement, are both approximately 0.2
553 times loading plate diameter ($u/D \approx h/D \approx 0.2$).

554 (2) With increase in the number of load cycles, the maximum and plastic deformations tend to increase.
555 For two levels of amplitude of cyclic load (400 kPa and 800 kPa), a large proportion of the total deformation
556 (25-70%) occurred during the first cycle of load. The actual proportion appears to depend on the mass of
557 reinforcement and on the magnitude of the applied cyclic load.

558 (3) The rate at which further deformation then accumulates is much slower than under the first few cycles
559 of loading. If or when deformation accumulation ceases altogether, then a resilient response condition, known
560 as plastic shakedown, may be achieved. Its occurrence appears to depend on both the mass of reinforcement
561 and the magnitude of the cyclic load applied to the loading plate.

562 • At the low level of cyclic load (400 kPa), under fifteen load cycles applied to the loading plate,
563 plastic shakedown occurs in all installations, irrespective of the reinforcement mass beneath the
564 loading surface.

565 • At the high level of cyclic load (800 kPa), for the test performed on the unreinforced pavement
566 foundation, the surface deformation is relatively large and non-stabilizing at the end of cyclic

567 loading. For the tests performed with a high reinforcement mass ($N_g=3, 4$ and $N_g=N_{rs}=3, 4$), plastic
568 shakedown occurs. When using the low ($N_g=1$ and $N_g=N_{rs}=1$) and moderate ($N_g=2$ and $N_g=N_{rs}=2$)
569 reinforcement mass, the rate at which deformation accumulates under cyclic loading is significantly
570 reduced. Shakedown was not experienced during the testing (15 cycles) but is anticipated after
571 further cycling.

572 (4) As the number of geocell and rubber-soil mixture layers increases, the loading surface deformation of
573 the pavement foundation decreases due, in part, to better load spreading of the composite system. Combined
574 geocell layers and rubber soil mixture layers reinforce the pavement foundation more effectively – reducing
575 the surface deformation – than the same number of geocell layers acting alone. Under the last cycle of loading
576 at 800 kPa with three layers of geocell ($N_g=3$), the residual, plastic, deformation is only about 42% of the
577 value for the unreinforced case and this ratio drops to only 32% when the same number of rubber-soil layers
578 ($N_g=N_{rs}=3$) is added.

579 (5) After several load cycles, for the reinforced beds, the proportion of deformation bed that is resilient
580 tends to a constant value due to densification, irrespective of mass, type or number of reinforcements.
581 Ultimately, only resilient deformation is observed during a cycle of loading. Shakedown has then been
582 achieved.

583 (6) Resilient deformation forms a greater proportion of the total deformation as the number of geocell and
584 rubber-soil mixture layers increases. The combined geocell and rubber-soil layers are most effective at
585 increasing the proportion of deformation that is resilient, presumably due to the elastic property of the rubber
586 particles that were added.

587 (7) The vertical stress that is spread through the pavement foundation, takes several cycles before
588 reaching a level at which it becomes approximately constant.

589 (8) The inclusion of the geocell and rubber-soil mixture layers beneath the loading plate acts to prevent
590 the punching shear observed in the surface of unreinforced installation and leads to significant reduction in the
591 vertical stress spread through the pavement foundation by distributing the load over a wider area. At a depth
592 about $2/3^{\text{rds}}$ of the loaded plate diameter, the vertical stress was about 97% of the applied 800 kPa stress when

593 the foundation was unreinforced and only about 73% of this value when reinforced with one layer of geocell
594 and one layer of rubber-soil mixture ($N_g=N_{rs}=1$).

595 (9) Under cyclic loading, use of the combined geocell and rubber soil mixture layers is more effective
596 than geocell layers alone in reducing the stress distributed down into the pavement foundation. At a depth, a
597 little greater than the loading plate diameter (i.e., depth of 350 mm), the vertical stress transferred from a
598 cyclic surface load of 800 kPa is reduced by 41% when two geocell layers and two rubber-soil mixture layers
599 ($N_g=N_{rs}=2$) are combined compared with the stress at the same point when two geocell layers ($N_g=2$) are used
600 alone.

601 The results provide considerable encouragement for the use of multiple layers of geocell reinforcement,
602 especially in combination with inter-layers of rubber-soil mixture, for addressing localized soft pavement
603 foundation conditions. The tests results are obtained for only one type of soil, one type of geocell with one
604 pocket size, one type and size of rubber, and one load diameter. Generalization may be needed, therefore,
605 before these findings may be directly applied. Using rubber reinforcement derived from scrap tires as a
606 reinforcing agent has the potential to deliver considerable environmental and economic benefit, although
607 economic assessments of the production and placement of soil-rubber mixtures, together with geocells, at
608 commercial scale would need to be performed to assure users of the applicability of the findings in every
609 situation.

610 **Acknowledgements**

611 The geocell used in this study was provided by DuPont de Nemours Company in the UK (the holder of
612 the trademark on the GroundGrid™ and Typar® products). Also, Dr. T. Amirsoleymani, the managing
613 director of Mandro Consulting Engineer, in Iran and their technicians provided the loading system, pit and
614 some of the instrumentations and provided great assistance during the tests. The authors appreciate all the
615 above support.

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721 **Nomenclature**

| | |
|----------|---|
| b | Width of the both geocell and rubber-soil mixture layers |
| C_u | Coefficient of uniformity |
| C_c | Coefficient of curvature |
| D | Loading plate diameter |
| D_{10} | Effective grain size (mm) |
| D_{30} | Diameter through which 30% of the total soil mass is passing (mm) |
| D_{60} | Diameter through which 60% of the total soil mass is passing (mm) |
| G_s | Specific gravity of soil |
| d | Geocell pocket size |
| ϕ | Angle of shearing resistance of soil being reinforced |
| u | Embedded depth of the geocell |
| H_g | Height of geocell layers |
| h | Vertical spacing of the geocell layers |
| h_{rs} | Height of the rubber-soil mixture layers |
| N_g | Number of geocell reinforcement layers |
| N_{rs} | Number of soil-rubber mixture reinforcement layers |
| SPC | Soil pressure cell |
| T.SPC | Top Soil Pressure Cell |
| M.SPC | Middle Soil Pressure Cell |

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Fig. 3. A view of granulated tire rubber used.

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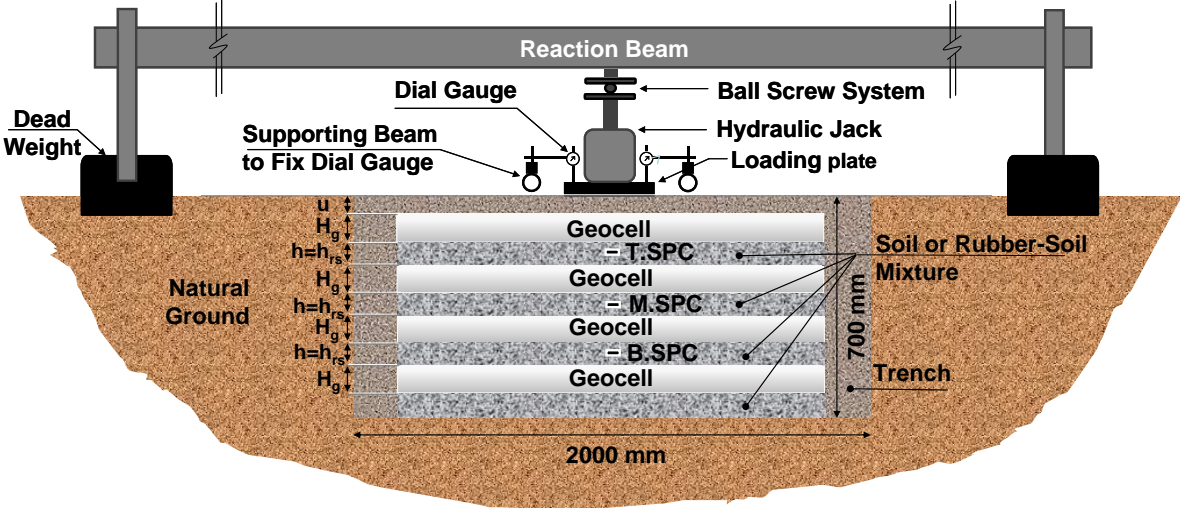


Fig. 4. Schematic cross-section of the test set-up (not to scale), “T.SPC”, “M.SPC”, and “B.SPC” indicate the location of soil pressure cells.

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Fig. 5. Photograph of test installation prior to loading include reaction beam, load plate, hydraulic jack and three dial gauges.

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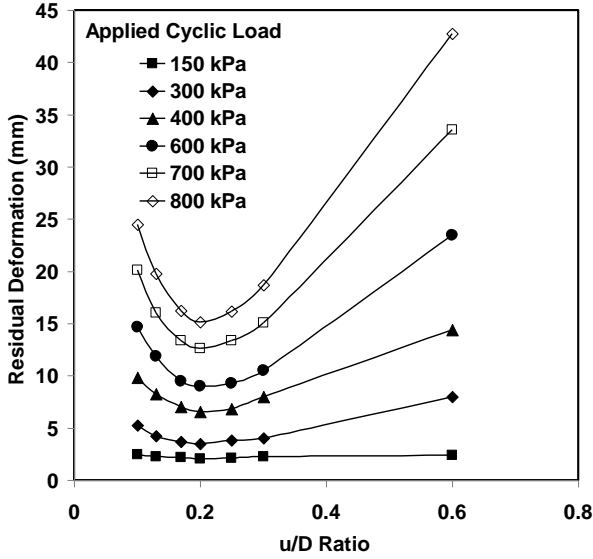


Fig. 6. Variation of residual plastic deformation with u/D ratio at different amplitudes of cyclic load.

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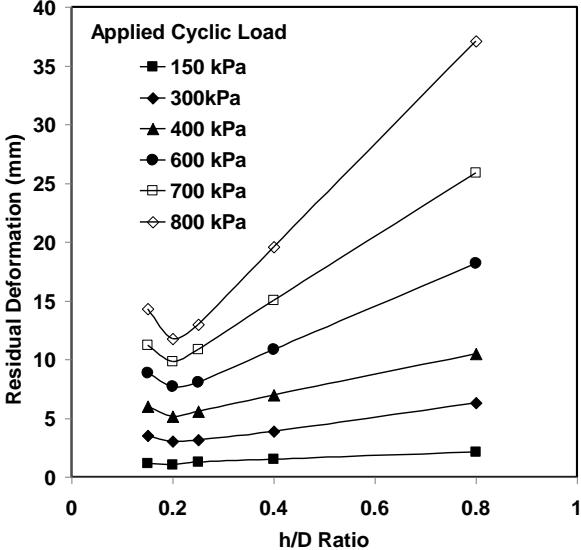


Fig. 7. Variation of residual plastic deformation with h/D ratio at different amplitudes of cyclic load.

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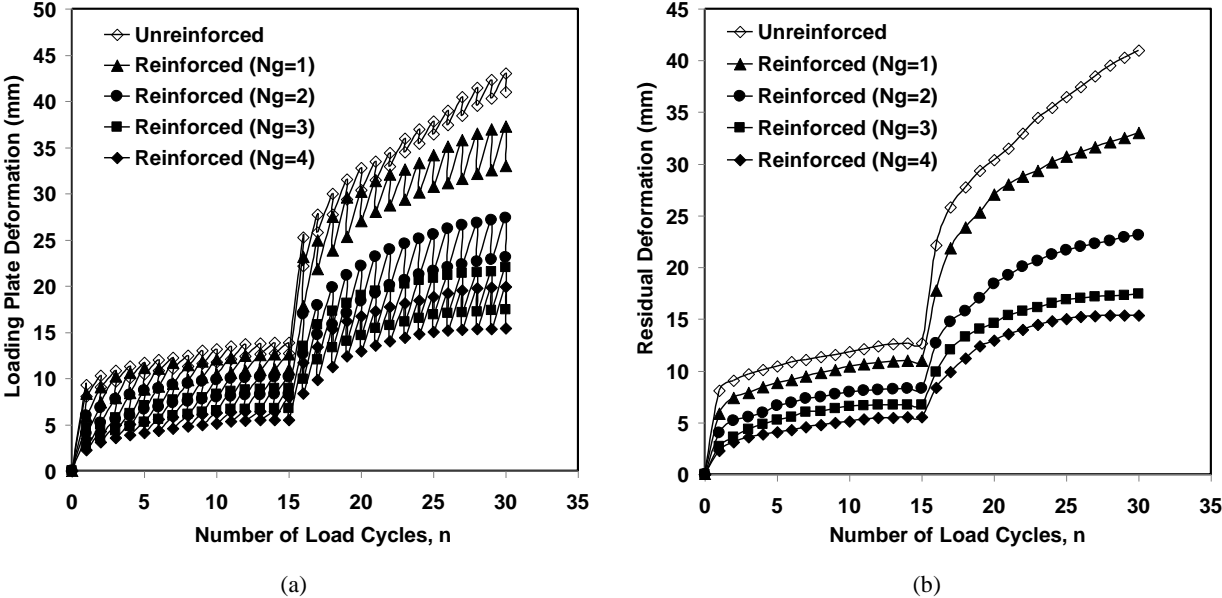


Fig. 8. Variation of (a) loading plate deformation, and (b) residual deformation with number of applied load cycles for the unreinforced and geocell reinforced systems with one, two, three, and four layers of geocell. The fifteen first cycles and the fifteen second cycles were applied with amplitudes of 400 and 800 kPa, respectively.

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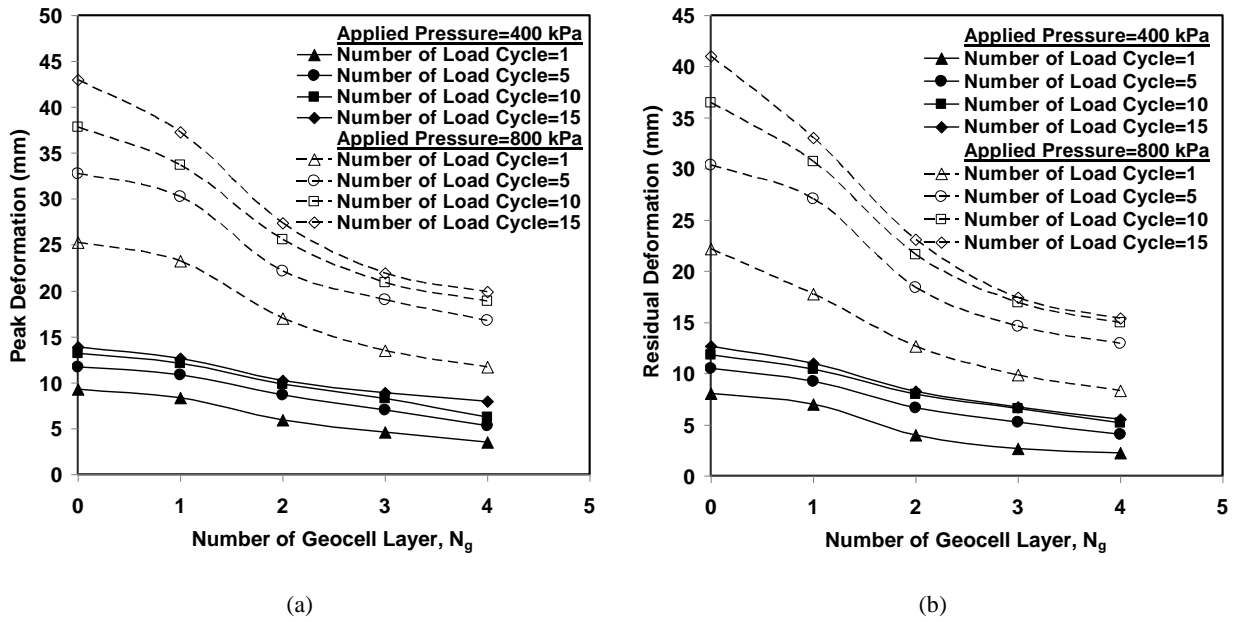


Fig. 9. Variation of (a) peak, and (b) residual deformation with number of geocell layers for two levels of applied repeated load (400 and 800 kPa) at load cycle of 1, 5, 10, and 15.

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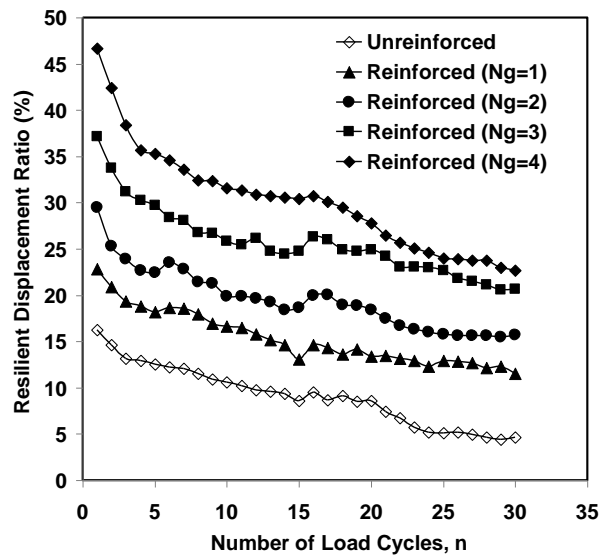
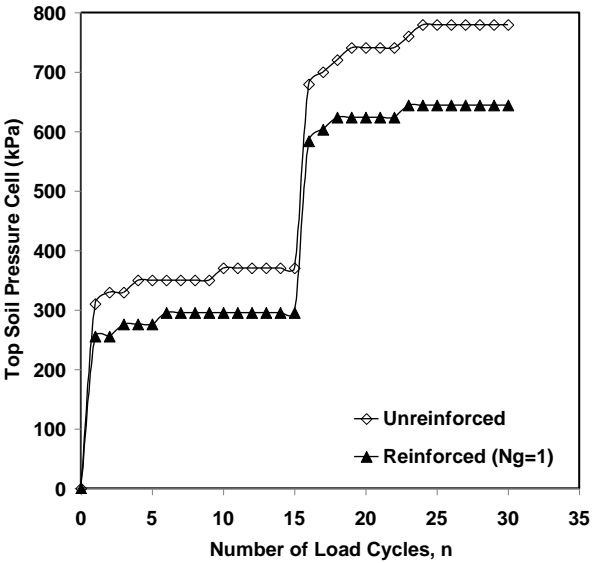
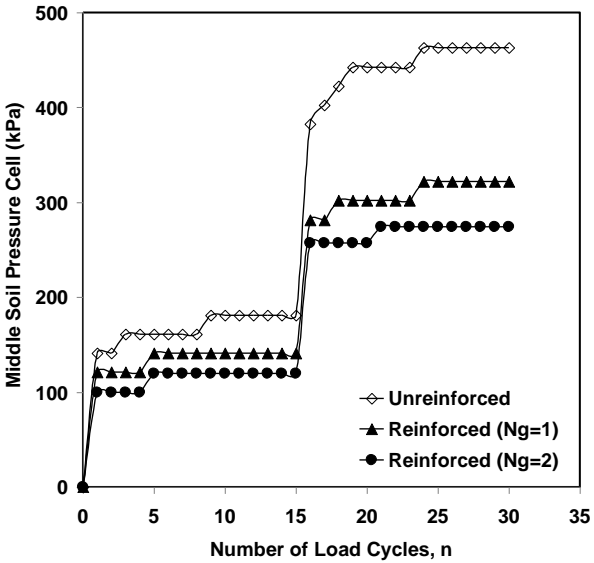


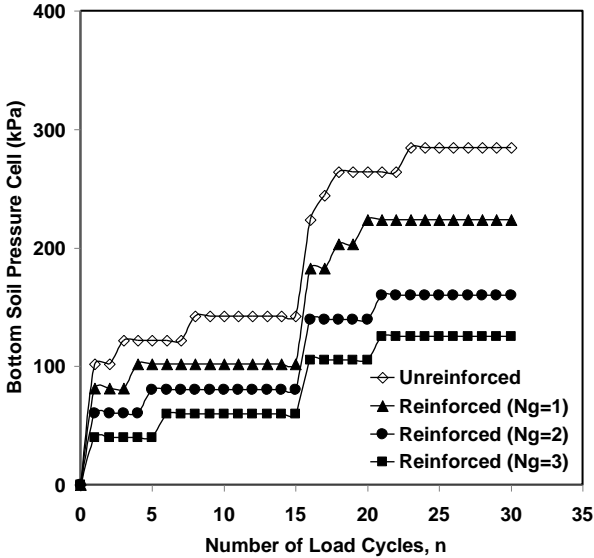
Fig. 10. Variation of resilient displacement ratio with number of applied load cycles for the unreinforced and geocell reinforced systems with one, two, three, and four layers of geocell. The fifteen first cycles and the fifteen second cycles were applied with amplitudes of 400 and 800 kPa, respectively.



(a)



(b)



(c)

Fig. 11. Variation of transferred pressure with number of applied load cycles at different depths in the geocell-reinforced and unreinforced pavement foundations (a) at a depth of 190 mm (T.SPC), (b) at a depth of 350 mm (M.SPC), and (c) at a depth of 510 mm (B.SPC). The fifteen first cycles and the fifteen second cycles were applied with amplitudes of 400 and 800 kPa, respectively.

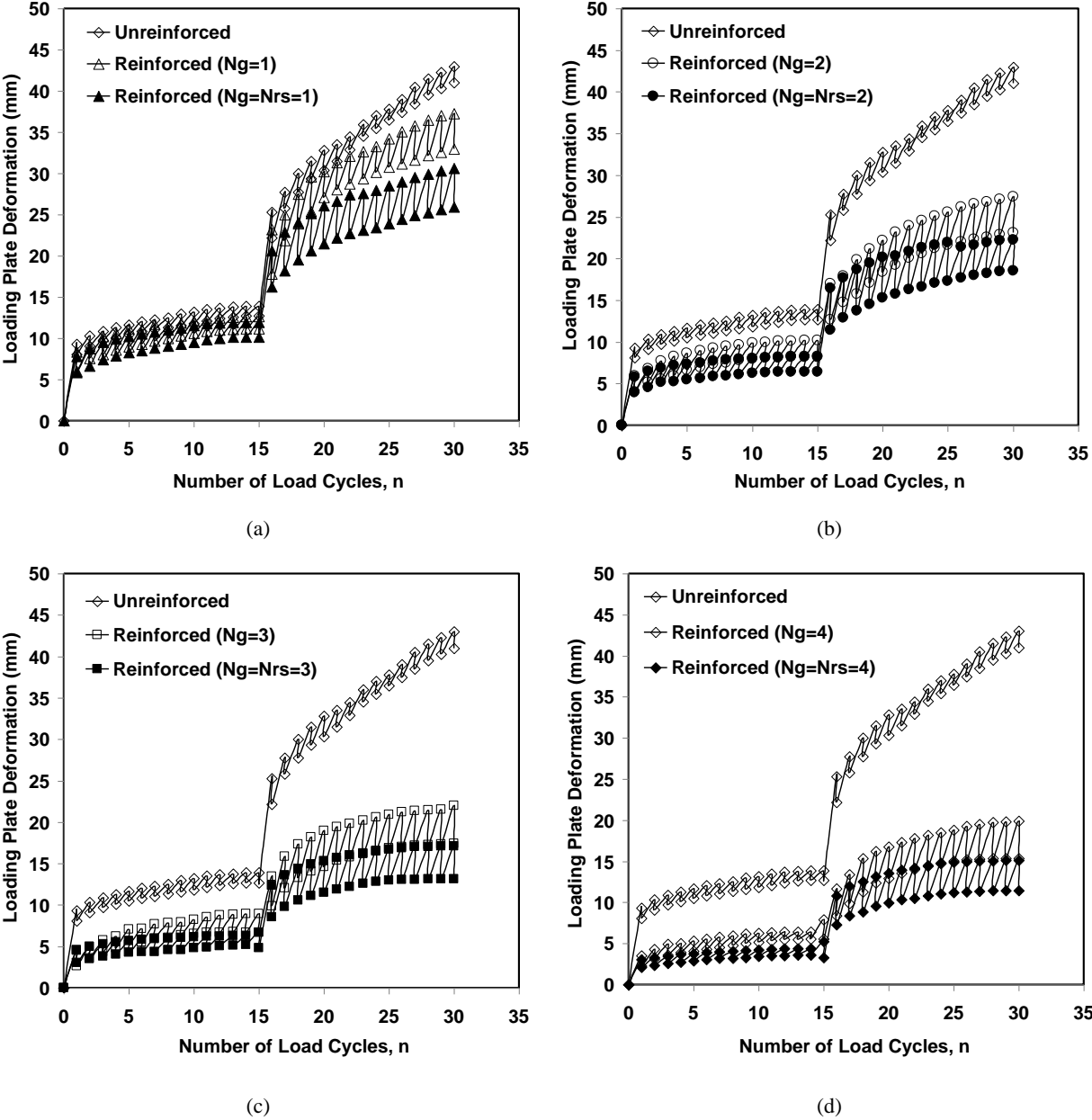
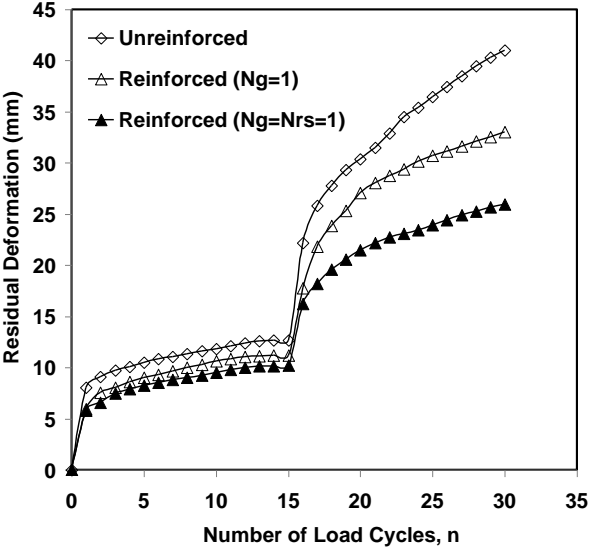
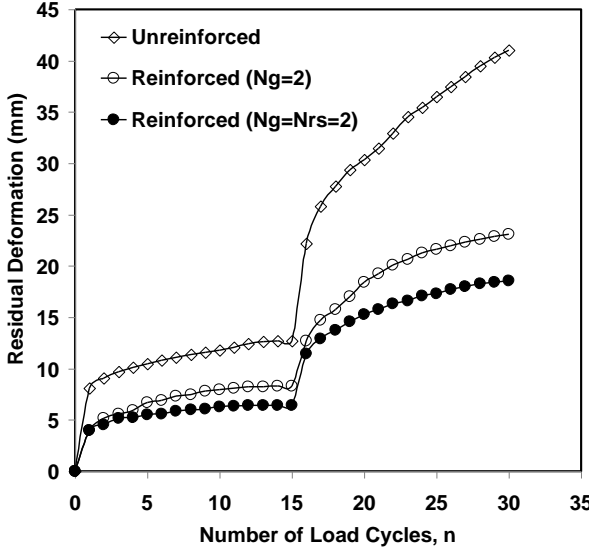


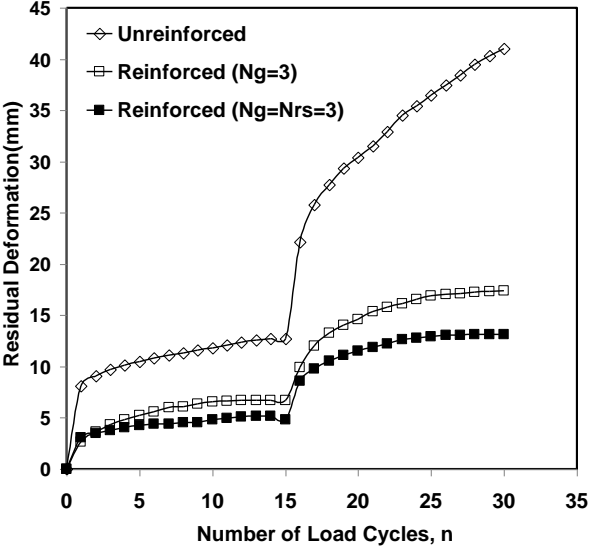
Fig. 12. Variation of loading plate deformation with number of applied load cycles for the unreinforced, geocell reinforced, and combined geocell and rubber-reinforced systems (a) $N_g=1$ and $N_{rs}=1$, (b) $N_g=2$ and $N_{rs}=2$, (c) $N_g=3$ and $N_{rs}=3$, and (d) $N_g=4$ and $N_{rs}=4$. The fifteen first cycles and the fifteen second cycles were applied with amplitudes of 400 and 800 kPa, respectively.



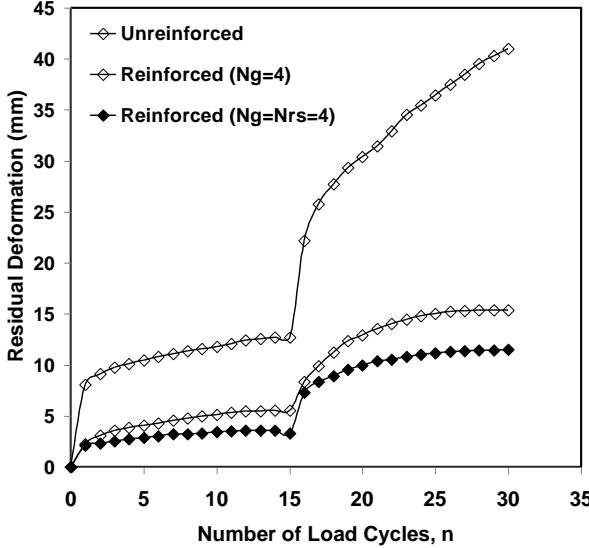
(a)



(b)



(c)



(d)

Fig. 13. Variation of residual plastic deformation with number of applied load cycles for the unreinforced, geocell reinforced, and combined geocell and rubber-reinforced systems (a) $N_g=1$ and $N_g=N_{rs}=1$, (b) $N_g=2$ and $N_g=N_{rs}=2$, (c) $N_g=3$ and $N_g=N_{rs}=3$, and (d) $N_g=4$ and $N_g=N_{rs}=4$. The fifteen first cycles and the fifteen second cycles were applied with amplitudes of 400 and 800 kPa, respectively.

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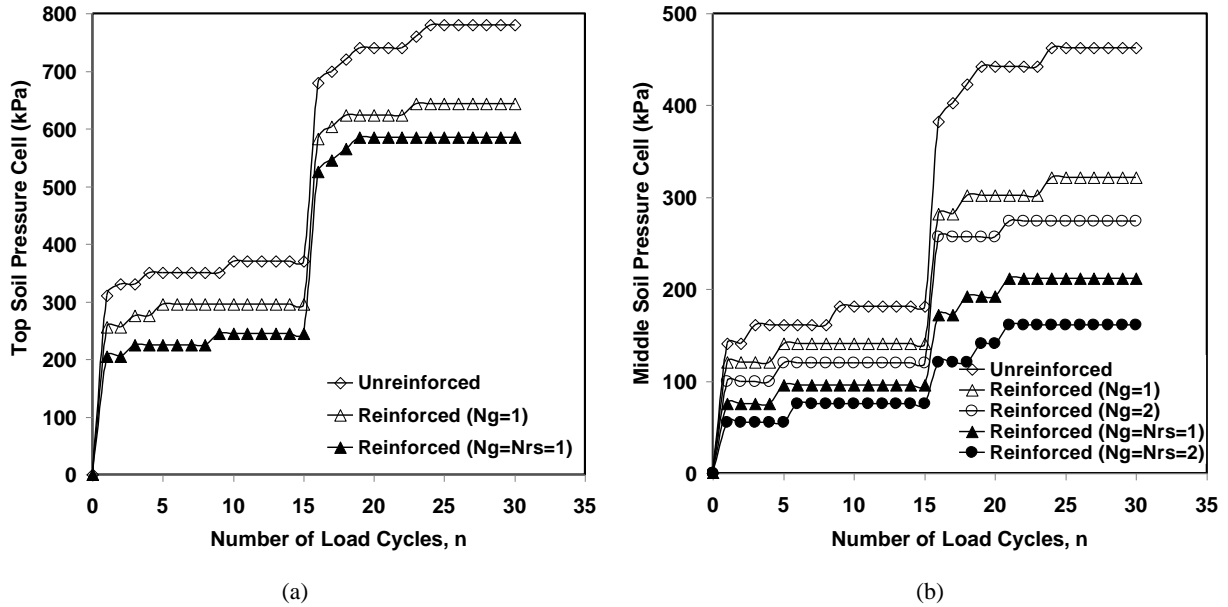


Fig. 14. Variation of stress in the pavement foundation with number of applied load cycles at different depths for unreinforced, geocell-only-reinforced and combined geocell and rubber-reinforced soil (a) at depth of 190 mm (T.SPC), (b) at depth of 350 mm (M.SPC). The fifteen first cycles and the second fifteen cycles were applied with amplitude of 400 and 800 kPa, respectively.

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Table 1

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The engineering properties of the geotextile used in the tests.

| Description | Value |
|---|---------------|
| Type of geotextile | Non-woven |
| Material | Polypropylene |
| Mass per unit area (gr/m^2) | 190 |
| Thickness under $2 \text{ kN}/\text{m}^2$ (mm) | 0.57 |
| Thickness under $200 \text{ kN}/\text{m}^2$ (mm) | 0.47 |
| Tensile strength (kN/m) | 13.1 |
| Strength at 5% (kN/m) | 5.7 |
| Effective opening size (mm) | 0.08 |
| Height of cells, H_g (mm) | 100 |
| Geocell pocket size (Width and length of cells), d (mm) | 110 |

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757

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Table 2

759

Densities of different materials after compaction (ASTM D 1557-12).

| Type of material | Rubber content (%) | Dry density (kN/m ³) |
|---------------------------|--------------------|----------------------------------|
| Unreinforced soil layer | No rubber | ≈18.56* |
| Geocell reinforced layer | No rubber | Between 18 and 18.5 |
| Rubber-soil mixture layer | 8 | ≈13.6 |

760

* approximately 90% of maximum dry density – see Section 3.1

761 **Table 3**

762 Scheme of the cyclic plate load tests for unreinforced pavement, multi-layered geocell pavement and combined multi-

763 layered geocell and rubber-reinforced pavement.

| Test Series | Type of test | N_g | N_{rs} | u/D | h/D .OR. h_{rs}/D | No. of Tests | Purpose of the tests |
|-------------|--|------------|----------|--------------------------------------|---------------------------|--------------|--|
| 1 | Unreinforced | ----- | ----- | ----- | | 1+2* | To quantify the improvements due to reinforcements |
| **2 | Geocell reinforced | 1 | ----- | 0.1, 0.13, 0.17, 0.2, 0.25, 0.3, 0.6 | ----- | 7+3* | To arrive at the optimum values of u/D and h/D |
| **3 | | 2 | ----- | 0.2 | 0.15, 0.2, 0.25, 0.4, 0.8 | 5+2* | |
| 4 | | 1, 2, 3, 4 | ----- | 0.2 | 0.2 | 4+2* | To study the effect of the number of geocell layers |
| 5 | Geocell Reinforced + Rubber-soil mixture | 1 | 1 | 0.2 | 0.2 | 4+4* | To investigate the effect of combined use of geocell reinforcement and rubber-soil mixtures. |
| | | 2 | 2 | | | | |
| | | 3 | 3 | | | | |
| | | 4 | 4 | | | | |

764

*The tests which were performed two or three times to verify the repeatability of the test data

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**in order to save time, only one load cycle of 150, 300, 400, 600, 700, and 800 kPa pressure were applied.

766 **Table 4.** The maximum deformation, residual deformation, and proportion of deformation (that is resilient) of
 767 unreinforced bed, reinforced bed with geocell layers, and reinforced bed with combination of geocell and rubber-soil
 768 mixture layers at the last cycle of loading (15th load cycle) of two levels of applied loads (= 400 and 800 kPa).

| Applied cyclic load | Parameters | Unreinforced bed | Reinforced bed with geocell | | | | Reinforced bed with geocell and rubber | | | |
|---------------------|---|------------------|-----------------------------|---------|---------|---------|--|----------------|----------------|----------------|
| | | | $N_g=1$ | $N_g=2$ | $N_g=3$ | $N_g=4$ | $N_g=N_{rs}=1$ | $N_g=N_{rs}=2$ | $N_g=N_{rs}=3$ | $N_g=N_{rs}=4$ |
| 400 kPa | Maximum deformation (mm) | 13.90 | 12.63 | 10.18 | 8.92 | 7.95 | 11.98 | 8.21 | 6.68 | 5.25 |
| | Residual plastic deformation (mm) | 12.70 | 10.98 | 8.28 | 6.71 | 5.53 | 10.19 | 6.45 | 4.84 | 3.33 |
| | Proportion of deformation that is resilient (%) | 8.63 | 13.07 | 18.66 | 24.77 | 30.44 | 14.94 | 21.44 | 27.55 | 36.57 |
| 800 kPa | Maximum deformation (mm) | 43.02 | 37.30 | 27.42 | 21.98 | 19.90 | 30.60 | 23.22 | 17.10 | 15.12 |
| | Residual plastic deformation (mm) | 41.03 | 33.02 | 23.10 | 17.43 | 15.39 | 25.94 | 18.54 | 13.14 | 11.48 |
| | Proportion of deformation that is resilient (%) | 4.63 | 11.47 | 15.75 | 20.70 | 22.66 | 15.23 | 20.16 | 23.16 | 24.07 |

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