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## **Evaluation of the Performance of TDR and Capacitance Techniques for Soil Moisture Measurement**

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### Abstract

Though researchers have employed various techniques (gravimetric, electromagnetic, neutron scattering, heat pulse, micro-wave and optical remote sensing techniques) for soil moisture measurement, dielectric based techniques (Time Domain Reflectometry, TDR, and capacitance technique, CT) have gained much more popularity, mainly due to revolutionary developments in the field of electronics and data communication systems. However, suitability and relative performance of these techniques for moisture measurement of soils is a point of debate. Hence, in order to address this issue, extensive studies were conducted on the soils of entirely different characteristics, compacted at various compaction states (dry density and water content) by employing TDR and capacitance probes. Subsequently, the dielectric constant of the soil and its bulk electrical conductivity were obtained using these probes and compared against each other and that computed from Topp's equation, which is a well-established relationship between the dielectric constant of the soil and its volumetric moisture content. An attempt was also made to correlate  $K_a$  values obtained from the dielectric techniques and Topp's equation with that of Time Propagation (TP) mixing model, which incorporates in it the properties of the soil matrix as well. It has been observed that  $K_{a}$ . TDR matches well with the  $K_{a-Topp}$  and  $K_{a-TP}$ , while the best match has been observed between  $K_{a-TDR}$  and  $K_{a-Topp}$  as compared to the  $K_{a-CT}$ . As such, the study demonstrates, clearly, that Topp's equation, which ignores the soil specific parameters, is capable of determining the soil moisture content appropriately. This study proposes an empirical equation which relates dielectric constants obtained from Topp's equation to those obtained from the TDR, capacitance technique and TP mixing model. Such a relationship can be further utilized for estimating the volumetric soil moisture content.

**Keywords:** soils, dielectric constant, volumetric moisture content, time domain reflectometry, capacitance probe, electrical conductivity.

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1		
2 3 4	Nomencl	lature
5 6	heta	volumetric moisture content
7 8 9	$\gamma_t$	soil bulk unit weight
10 11	γd	dry unit weight of soil
12 13 14	σ	electrical conductivity
15 16	$\sigma_{ m CT}$	electrical conductivity obtained from capacitance technique
17 18	$\sigma_{ m TDR}$	electrical conductivity obtained from Time Domain Reflectometry technique
19 20	ξ	zeta potential
21 22	mS/cm	milli-Siemens per centimeter
23 24 25	w	gravimetric moisture content
26 27	g/cc	gram per centimetre cube
28 29	Ka	dielectric constant
30 31	K <sub>a-CT.</sub>	dielectric constant of the soil mass obtained by employing capacitance
32 33 34		technique
35 36	$K_{a-{ m TDR}}$	dielectric constant of the soil mass obtained by employing Time Domain
37 38		Reflectometry technique
39 40 41	K <sub>a-Topp</sub>	dielectric constant of the soil mass obtained by employing Topp's equation
42 43	$K_{ ext{a-TP}}$	dielectric constant of the soil mass obtained by employing Time Propagation
44 45		mixing model
46 47	Z <sub>TDR</sub>	levels of immersion using Time Domain Reflectometry technique
48 49 50	$Z_{CT}$	levels of immersion using capacitance technique
50 51 52	G	specific gravity
53 54	CEC	Cation Exchange Capacity
55 56	CT	Capacitance Technique
57 58 59		
60		2
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LL	liquid limit
PL	plastic limit
PI	plasticity index
ОМ	organic matter
TDR	Time Domain Reflectometry
TDS	Total Dissolved Solids
ТР	Time Propagation
USCS	Unified Soil Classification System

#### Introduction

Soil moisture content has paramount importance in timely scheduling of irrigation, slope stability analysis, water balance studies and heat and contaminant transport through the soil (Susha et al. 2014). Recently, Susha et al., (2014) have provided a detailed synthesis of various soil moisture measurements techniques (thermo-gravimetric, electro-magnetic, neutron scattering, optical and thermal analysis based) and have discussed about the issues pertaining to the applicability of these techniques for the soils of entirely different characteristics. Though earlier researchers developed various measurement techniques such as gravimetric (ASTM D 2216; Hillel, 1982; Robinson et al. 2008), electromagnetic (Selig et al. 1975; Topp et al. 1980; Topp et al. 1982; Nissen and Moldrup, 1994; Hilhorst 2000; Jones and Or, 2004; Bhat et al. 2007; Tarantino et al. 2008; Rao and Singh 2011), neutron scattering (Elder and Ramussen 1994; Fityus et al. 2011), heat pulse technique (De Vries, 1963; Julie and Jay 1997), optical remote sensing techniques (Robinson et al. 2008; Sayde et al. 2010; Yin et al. 2013; Sadeghi et al. 2015), dielectric based techniques such as Time Domain Reflectometry (TDR) and capacitance techniques (Topp et al. 1980; Bhat et al. 2007; Rao and Singh 2011) have gained much more popularity. This is mainly due to the dependence of the dielectric constant (apparent permittivity or relative permittivity,  $K_a$ ) on the soil moisture content (for dry soils  $K_a$  is between 2-8, while for de-ionized water the same is 81) and revolutionary development in the field of electronics and data communication systems in the recent past (Topp et al. 1980; Bhat et al. 2007; Arulanandan and Smith 1973; Acar and Olivieri 1989; Sreedeep et al. 2004), which facilitated them as instantaneous and non-invasive measurement techniques in various porous materials such as soils, peats, wood, snow and forest litter (Moret-Fernandez et al. 2008; Baudena et al. 2012; Camporese 2006; Canone et al. 2009; Previati et al. 2011; Previati et al. 2012). Incidentally, these techniques not only measure dielectric constant of the soil, but also measure its bulk electrical

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conductivity,  $\sigma$ , which can be correlated with the volumetric moisture content,  $\theta$ , conductivity of the pore-solution,  $\sigma_w$ , fraction of the clay sized particles present and the soil mineralogy (Rhoades et al. 1976; Shainberg et al. 1980; Smith and Arulanandan 1981; Shah and Singh, 2004; Shah and Singh 2005). Though these techniques are used quite frequently, precision of the soil moisture measurement, and suitability and performance of these techniques, for wide range of the soils (in terms of their physical, chemical and mineralogical compositions) has always been a point of debate.

With this in view, efforts were made to compare the relative performance of the TDR (Campbell scientific TDR CS640 probe model) and capacitance technique, CT, (Decagon device 5TE) probes on the soils with different characteristics and compacted to different states (as defined by their dry density and moisture content). In addition to moisture content, the dielectric constant of the soil,  $K_a$ , and its bulk electrical conductivity,  $\sigma$ , were obtained by employing these techniques. The results so obtained were compared against each other and those computed by employing the Topp's equation, which is a well-established relationship between the dielectric constant of the soil and its volumetric moisture content. Details of this study are presented in this paper along with a discussion on the efficiency of the Topp's equation to compute soil moisture content. Furthermore, a hypothesis, which can be employed for estimation of volumetric soil moisture content of soil without resorting to the dielectric techniques, has also been proposed based on this study.

## **Details of the Test Setup**

#### Time domain reflectometry (TDR)

The TDR test setup used in this study consists of a step pulse generator, sampler (consists of a voltmeter and a timing device), an oscilloscope, coaxial cable and a TDR probe. This setup, which facilitates measurement of the delay time between the transmitted and reflected electromagnetic waves, was employed for determining the dielectric constant of the soil. In this study, Campbell scientific TDR CS 640 probe that consists of three prongs, the pointed and projected parts of the probe, of length 7.5 cm, width 4.5cm, diameter 0.159 cm and spacing between the rods 0.84 cm was employed. As specified by the manufacturer, the range of the volumetric moisture content and the bulk electrical conductivity, for which this setup can be employed, are 1-100% and 0- 5mS/cm, respectively. The set up provided the TDR waveforms of the samples and the obtained waveforms were analyzed as described below.

#### Analysis of the TDR waveform

Evett (2000) has reported that the method of interpretation of the TDR waveforms, from which the dielectric constant of the soil,  $K_a$ , is obtained could significantly affect the computed value of the of soil moisture content. The tangent methodology proposed by Heimovaara and Bouten (1990) for the determination of the travel time (= $t_{end} - t_{head}$ ) of the electromagnetic wave up to the head,  $t_{head}$ , and end,  $t_{end}$ , of the probe for computing the  $K_a$ , has been employed in this study (refer Fig. 1(a)). Although, the time at which the reflection occurs from the head of the probe,  $t_{head}$ , is constant, the time at which the reflection occurs from the end of the probe to its head,  $t_{end}$ , depends upon the medium in which the TDR probe is inserted. Fig. 1(a) highlights this fact and it can be noticed that  $t_{head}$  is constant for various media (air, water and wet saline soil). However,  $t_{end}$  for water is higher as compared to its counterparts. This indicates that an increase in moisture content of a medium makes it more conducting and hence  $t_{end}$  decreases. Increase in conductivity of the medium is also responsible for its short circuiting at the surface and hence  $t_{end}$  and  $K_a$  cannot be determined.

#### Volumetric moisture (water) content measurement from the TDR waveform

TDR waveforms for a soil, compacted at different moisture contents and constant target dry density,  $\gamma_d$ , were obtained. From these waveforms, the dielectric constant,  $K_{a-TDR}$ ,

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for different soils, considered in this study, was computed by employing Eq. 1 (Topp et al. 1980) and the results are presented in Fig. 2(a).

(1) 
$$K_{a-TDR} = \left(c \frac{t_{end} - t_{head}}{2L}\right)^2$$

where *c* is the velocity of electromagnetic waves (=  $3 \times 10^8$  m/s), times corresponding to the reflection at the end and head of the probe are  $t_{end}$  and  $t_{head}$ , respectively, and *L* is the effective length of the probe.

Volumetric moisture content and dielectric constant are related by the following Equations 2 and 3 which are proposed by Topp et al. (1980).  $K_{a-Topp}$  can be computed by employing Eq. 2.

(2) 
$$K_{a-Topp} = 3.03 + (9.3 \cdot \theta_c) + (146 \cdot \theta_c^2) - (76.7 \cdot \theta_c^3)$$

where  $\theta_c$  is the volumetric moisture content (in %) =  $w \cdot \frac{\gamma_d}{\gamma_w}$ , w is the gravimetric moisture content (in %) and  $\gamma_d$  and  $\gamma_w$  are the dry density of the soil and density of water (=1 g/cc), respectively.

Topp et al. (1980) have also proposed the following empirical relationship (Eq. 3) and reported that this equation is independent of soil type, soil density, soil temperature and soluble salt content; which most of the dielectric- based techniques (especially TDR and capacitance techniques) employ to determine the volumetric soil moisture content.

(3) 
$$\theta_{\text{Topp}} = 4.3 \times 10^{-6} \cdot K_a^{-3} - 5.5 \times 10^{-4} \cdot K_a^{-2} + 2.92 \times 10^{-2} \cdot K_a - 5.3 \times 10^{-2}$$

#### Electrical conductivity measurement from the TDR waveforms

Topp et al. (1988) have reported that the bulk electrical conductivity,  $\sigma_{TDR}$ , of the soil can be measured using a TDR probe and by employing the following relationship (Giese and Tiemann 1975):

(4) 
$$\sigma_{\rm TDR} = \frac{c \cdot \epsilon_0 \cdot z_p}{z_c \cdot L} \left[ \frac{2V_0}{V_\infty} - 1 \right]$$

where  $\epsilon_0$  is the permittivity of the free space (in F/m), *c* is the velocity of electromagnetic waves (3×10<sup>8</sup> m/s), *L* is the effective length of the probe (in m),  $V_0$  is the input voltage on the head of the probe,  $V_{\infty}$  is the final voltage (of the standing wave) measured by the oscilloscope, after various reflections have occurred, and  $z_c$  (63.3 ohm) and  $z_p$  (183 ohm) correspond to the impedance of the cable tester and the probe, respectively.

As the TDR probe returns the signal recorded by the oscilloscope in terms of reflection coefficient,  $\rho$ , the reflection occurring at infinite time (designated as  $\rho_{\text{max}}$ , refer Fig. 1(b)) can be written as:

$$\rho_{\max} = \frac{V_{\infty} - V_0}{V_0}$$

Hence, Eq. 4 can be rewritten as:

(6) 
$$\sigma_{\text{TDR}} = \frac{K_p}{z_c} \left[ \frac{1 - \rho_{\text{max}}}{1 + \rho_{\text{max}}} \right]$$
where,  $K_p = (c \cdot \varepsilon_0 \cdot z_p)/L$ 

Calibration of the TDR probe should be done when the reflection coefficient measured in air,  $\rho_{air}$ , and water,  $\rho_w$ , and short circuit probe,  $\rho_{sc}$ , are not equal to 1, 1 and -1, respectively (Castiglione and Shouse 2003; Tarantino et al. 2008). Hence reflection coefficient values range between 1 and -1. Wojciech (2008) have also reported that these calibration errors can occur due to the overlapping of incident and reflected pulses. Hence, Castiglione and Shouse (2003) have derived an equation (refer Eq. 7) for correcting the reflection coefficient,  $\rho_{max,corr}$ , to account for these additional losses in the TDR system.

(7) 
$$\rho_{\max,corr} = \frac{2(\rho - \rho_{air})}{(\rho_{air} - \rho_{sc})} + 1$$

Eq. 8 can be modified as given below (Wojciech et al.2008).

(8) 
$$\sigma_{\text{TDR}} = \frac{K_p}{z_c} \left[ \frac{1 - \rho_{\text{max},corr}}{1 + \rho_{\text{max},corr}} \right]$$

Incidentally, from Fig. 1(b), it can be noticed that  $\rho_{max}$  becomes negative as the salinity of the medium increases and hence  $\sigma_{TDR}$  would be high (refer Equations 6 and 8) for

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higher negative values of  $\rho_{\text{max}}$ . However,  $\sigma_{\text{TDR}}$  is negligible for air and de-ionised water as their  $\rho_{\text{max}}$  is almost unity.

#### Capacitance probe

In addition to the TDR measurements, capacitance technique (CT) based probe (Decagon device 5TE, which consists of three prongs of length 5.2cm and employs 70MHz oscillating wave and is manufactured by the Decagon Devices 2012) was also employed for this study. It was used for measuring the dielectric constant (1 to 80),  $K_{a-CT}$ , the volumetric moisture content,  $\theta_{CT}$  (0-100%) and the bulk electrical conductivity,  $\sigma_{CT}$  (<10mS/cm), of the same soil sample on which the TDR measurements were conducted and the value of  $\theta$  was determined by using Eq.3. Incidentally, this probe can also measure the temperature (-40°C -50°C) of the soil and utilises Topp's equation (refer Eq.3) to calculate  $\theta_{CT}$  from  $K_{a-CT}$ . Capacitance technique determines the dielectric constant of a medium by measuring the charging time of a capacitor, which uses this medium as a dielectric. A thermistor in contact with the sensor prongs provides temperature of the soil, while the screws on the surface of the sensor form a two-sensor electrical array, which facilitates electrical conductivity measurements (Decagon Devices 2012).

### **Experimental Investigations**

Seven soils of entirely different physical, chemical and mineralogical properties (refer Tables 1, 2 and3) were used in the present study. Details of their characterization, which facilitates standardization of these soils, are presented in the following.

#### **Physical characterization**

The specific gravity, *G*, of these soils was determined as per the guidelines of ASTM D 5550 by employing an Ultra Pycnometer, (Quantachrome, USA), which utilizes helium gas as the displacing fluid. The gradational characteristics of the soils were determined by using the conventional sieve analysis and hydrometer analysis (ASTM D 422-63). The consistency

limits (viz., liquid limit, *LL*, plastic limit, *PL* and plasticity index, *PI*) of these soils were determined according to the guidelines of ASTM D 4318-10 (2013). The specific surface area (*SSA*) of the soils was determined by Ethylene Glycol Monoethyl Ether, EGME, absorption method (Carter et al. 1986; Cerato and Luteneggaer 2002; Arnepalli et al. 2008). The presence of organic matter in these soils was determined as per ASTM D2974-14 (2014). The physical properties of the soils are presented in Table 1.

## **Chemical characterization**

Chemical composition of these soils (refer Table 2a) was determined by employing an X-ray Fluorescence instrument, XRF (PANalytical PW 2404). The pH, electrical conductivity ( $\sigma$ ) and total dissolved solids (TDS) of these soils, corresponding to liquid to solid ratio, L/S, equal to 20 were measured by employing a water quality analyzer (Oakton® PC 2700) and the results are listed in Table 2(b). The cation-exchange capacity, *CEC* of these soils was determined (refer Table 2(b)) as per the guidelines provided in EPA 9081 (1967). The influence of pore fluid on particle-to-particle interaction in the soil can be investigated by the change in the surface charge potential which is indirectly defined as the zeta potential,  $\xi$  (Sparks 1986; Yukselen and Kaya 2003) which was determined by employing an automated electrophoresis instrument (Zeta PALS, BIC, USA) and the results are presented in Table 2(b).

#### Mineralogical characterization

Qualitative mineralogical composition of these soils was determined by employing an X-ray Diffraction (XRD) Spectrometer (PANalytical X'Pert PRO, The Netherlands) which is fitted with a graphite monochromator and Cu-K $\alpha$  radiation, as the source (Cullity and Stock 2001) and the results are listed in Table 3. The quantitative analysis of the mineralogical composition of the soils was conducted by resorting to Rietveld analysis by employing the X'Pert High Score Plus software with PDF-4+ database.

## **Sample Preparation**

The soil was mixed with nano-filter water (deionized water) and left for maturation for 24 hours, which ensures uniform moisture level of the entire soil. Later, it was compacted to different compaction states (i.e., the gravimetric moisture content, w, and the dry density,  $\gamma_d$ ) in a standard Proctor mould (944 cm<sup>3</sup> in volume with an internal diameter of 10.2 cm and a height of 11.6 cm), as per the guidelines presented by ASTM D1557-12. Tarantino et al. (2008) reported that TDR waveforms would transfer only through the waveguides and measure the volumetric moisture content enclosed within the probe size. Susha et al. (2016) proved that effective magnetic field width (zone of influence) generated across the electrodes (diameter 0.2 cm) would be 2 cm. For the present study, diameter of the TDR probe is 0.159cm and hence, there was no effect of the proctor mould in the electromagnetic waves generated. Moreover, multiple readings of the measurements were taken by the probes which ensured no distorted TDR waveforms (refer Fig. 3) and capacitance probe measurements. Simultaneously, three specimens from the matured soils were used for determining the w, as per ASTM D 2216 (2008). The volumetric moisture content,  $\theta$ , electrical conductivity,  $\sigma$ , and the dielectric constant,  $K_a$  of the compacted soil were determined by employing both TDR and capacitance probes, in a sequential manner.

#### **Results and Discussions**

Calibration of the TDR and capacitance probes was conducted by placing them in different media (water, air and NaCl solutions of different molarities), for which the dielectric constant and electrical conductivity values are known. The resultant TDR waveforms are depicted in Fig. 4. Incidentally, the reproducibility (i.e. multiple waveforms for the same soil sample) of the resultant TDR waveforms was also ascertained, as depicted in Fig. 3. An overlap of the results indicates an excellent reproducibility of the TDR wave forms. It can

also be observed from Fig. 4 that as electrical conductivity of the media increases, the travel time of the TDR wave form decreases.

To understand the performance of the TDR and capacitance probes, comparisons have been made between the obtained  $K_{a-TDR}$  and  $K_{a-CT}$ ,  $\theta_{TDR}$  and  $\theta_{CT}$  and  $\sigma_{TDR}$  and  $\sigma_{CT}$  values corresponding to various compacted states of the soils (S1 to S5, refer Table 1) considered in this study. It can be observed from Figures 2 and 5 that there is a mismatch between the  $K_{a}$ -TDR and  $K_{a-CT}$ ,  $\theta_{TDR}$  and  $\theta_{CT}$ , and  $\sigma_{TDR}$  and  $\sigma_{CT}$ . In fact, as depicted in Fig. 2a, it can be observed that the value of the dielectric constant obtained from the TDR measurements,  $K_{a}$ -<sub>TDR</sub>, is much higher (almost twice) than that obtained from the capacitance (CT) probe,  $K_{a-CT}$ . As a result, the volumetric moisture content obtained from the CT probe,  $\theta_{CT}$ , is about 50% of the value obtained from the TDR probe,  $\theta_{\text{TDR}}$  (refer Fig. 2b). Furthermore, it can be observed from Fig. 5 that the electrical conductivity of the soil obtained from the CT probe,  $\sigma_{CT}$  is 25% higher than that obtained from the TDR probe,  $\sigma_{\text{TDR}}$ . For standardization of these observations, all these variables ( $K_{a-TDR}$  and  $K_{a-CT}$ ) were compared against the calculated volumetric soil moisture content computed,  $\theta_c (=w.\frac{\gamma_a}{\gamma_w}, \text{ refer Eq. 3})$  and the results are depicted in Fig. 6. The trends depicted in Fig. 6, corresponding to the variation of  $K_{a-TDR}$  and  $K_{a-CT}$  with  $\theta_c$ , respectively, are pretty well defined and can be presented in an exponential form  $[K_a = A.e^{\theta c \cdot B}]$ , where A and B are empirical coefficients. As depicted in these figures, an increasing trend between the two parameters (dielectric constant and electrical conductivity) indicates that starting from the dry state of compacted soil samples, which contain air (with lower dielectric constant 1 to 3) in the voids, gets replaced by the water (with higher dielectric constant 81). This in turn results in an increased dielectric constant of the soil. Furthermore, the water (pore-solution) present in the interconnected pores would offer much lower resistance to the flow of current (i.e., an increase in the electrical conductivity,  $\sigma$ . However, if the soil exhibits higher electrical conductivity,  $\sigma$  (refer the data for soil S5 listed

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in Table 2b), due to the presence of higher concentrations of ions in the pore-solution, its dielectric constant would be lesser. In order to verify this, standard sands (soils S6 and S7) were saturated with different molar concentrations of the pore-solutions (viz., 0.05M, 0.1M, 0.2M and 0.5 M NaCl solutions) and the results obtained from the two probes are presented in Fig. 7 and Table 4. From Fig. 7 and Table 4, it can be noticed that, in general, as NaCl concentration increases, the dielectric constant of soils S6 and S7 which are essentially sands decreases. This can be attributed to the fact that, as stated earlier, in case of the TDR probe, an increase in salinity of the medium, increases its conductivity which results in a decreased  $t_{end}$ . Thus due to an increase in conduction of the current through the medium, its dielectric constant,  $K_{a-TDR}$ , reduces. Moreover, dielectric constant and electrical conductivity as a function of frequency take account of the inherent asymmetry and broadness of the dielectric dispersion and polarization effects which are characterised by Debye Relaxation Equation. For higher saline medium, as the medium approaches a relaxation point, the dielectric loss factor increases which corresponds to a drop in the dielectric constant (Robinson et al. 2003). As per the tangent method,  $K_{a-TDR}$  cannot be obtained for the soils S6 and S7, the soils saturated with 0.2 M and 0.5M NaCl solutions, as their end signals of the TDR waveforms are flat which means the electromagnetic wave is dissipated and no reflection could be obtained (refer Fig. 7). Similarly, in case of the capacitance probe, the capacitance of the medium reduces due to an increase in the salinity, and hence  $K_{a-CT}$  decreases. Incidentally, Table 4 also reveals that the electrical conductivity measured by the capacitance probe,  $\sigma_{CT}$ , is higher as compared to  $\sigma_{TDR}$ , for the entire range of volumetric moisture content considered in this study, except for the dried state of the soils S6 and S7, where these measurements are 0 mS/cm and 0.0028 mS/cm, respectively.

As TDR and capacitance probes employ Topp's equation (Eq. 3) to correlate  $K_a$  and  $\theta$ , the  $K_{a-TDR}$  and  $K_{a-CT}$  of the soil samples were also compared with those computed from Eq.

2,  $K_{a-Topp}$ , as depicted in Fig. 8(a) and (b). From these figures, it can be noticed that a linear relationship exists between  $K_{a-Topp}$  and  $K_{a-TDR}$ , and  $K_{a-Topp}$  and  $K_{a-CT}$ , though it appears to be an over-prediction of  $K_{a-TDR}$  and under-prediction of  $K_{a-CT}$  with respect to  $K_{a-Topp}$ . To overcome this situation,  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-Topp}$  were also compared with the  $K_{a-TP}$  (i.e., the dielectric constant obtained from the 'Time Propagation mixing model', which is also referred as TP-Mixing model), as shown in Fig.8 (c), (d) and (e). Knoll (1996) has reported that TP-Mixing model can be effectively employed for estimating the dielectric constant of the heterogeneous materials, especially geologic materials. The TP-Mixing model incorporates soil specific parameters (mineralogical constitution of the soil, porosity and saturation of the soil and presence of various phases, air or water, of the pore solution in the soil) for estimation of the dielectric constant,  $K_{a-TP}$ , as presented by Eq. 9 (Knoll 1996; Bhat et al. 2007; Martinez and Byrnes 2001) and the details of  $K_{a-TP}$  is shown in Table 5. From Fig. 9, it can be noticed that  $K_{a-TP}$  is linearly correlated to  $\theta_c$  (R<sup>2</sup>=0.99) and the intercept is 5.0 which corresponds to the dielectric constant of the dry soil ( $\theta_c=0$  %). However, TP-Mixing model does not account for the effect of frequency of the AC, while computing the effective dielectric constant,  $K_{a-TP}$ . Moreover, the quantification of the minerals present in the soil and estimation of their dielectric constants are arduous tasks. 2,

(9) 
$$\sqrt{K_{a-TP}} = \left[ (1 - \eta) \cdot \left( M_1 \cdot \sqrt{K_{M_1}} + M_2 \cdot \sqrt{K_{M_2}} \right) + \eta \cdot \left( S_r \cdot \sqrt{K_{PF_1}} + (1 - S_r) \cdot \sqrt{K_{PF_2}} \right) \right]$$

where,  $\eta$  is the porosity and  $S_r$  is the degree of saturation (with moisture) of the soil, M corresponds to the percentage of the mineral present in the soil,  $K_M$  corresponds to the dielectric constant of the respective mineral (refer Table 3 and 5) and  $K_{PF}$  corresponds to the dielectric constant of the pore-solutions (viz., air (2) and water (81)) present in the soil.

From Figures 8(c), (d) and (e), it can be noticed that  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-Topp}$  yield good correlations with  $K_{a-TP}$ . The slope of  $K_{a-TDR}$  and  $K_{a-TP}$  (0.89, refer Fig. 8e) relationship is higher as compared to  $K_{a-CT}$  and  $K_{a-TP}$  (0.45, refer Fig. 8d), and  $K_{a-Topp}$  and  $K_{a-TP}$  (0.75, refer

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Fig. 8c), relationships. Hence, it can be inferred that the TDR probe performs better at matching with  $K_{a-TP}$  and  $K_{a-Topp}$  in comparison with  $K_{a-CT}$ . This exercise also indicates that the values of  $K_a$  obtained from various techniques differ and hence  $\theta$ , obtained from Eq. 3, would also vary. As most of the dielectric techniques employ Eq. 3 (Topp et al. 1980), Eq. 10 which is a relationship between  $K_{a-Topp}$  with  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-TP}$  from Figures 8 (a), (b) and (c) was derived. One of the applications of Eq. 10 would be that  $K_{a-Topp}$  can be obtained if  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-Topp}$  can be obtained if  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-Topp}$  can be obtained if  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-TP}$  are known. This in turn would facilitate determination of  $\theta$  of the soil, by employing Eq. 3. Hence, the proposed relationship can be used to estimate dielectric constant and subsequently volumetric moisture content irrespective to the dielectric techniques

(10) 
$$K_{a-Topp} = 0.82 \cdot K_{a-TDR} = 1.64 \cdot K_{a-CT} = 0.75 \cdot K_{a-TP}$$

However, it should be borne in mind that  $K_{a-TDR}$  and  $K_{a-CT}$ , appearing in Eq. 10, are the effective dielectric constants and that would get influenced due to the presence of interfaces, from which the electromagnetic waves would get reflected due to change in the impedance. Such interfaces might develop within the compacted soil sample due to (a) its compaction in multiple layers or (b) the compaction induced moisture migration. Another explanation which could be ascribed to the interface formation in the sample could be the variation in the dry density along the depth of the soil mas since the bottom layers of sample receive higher cumulative compaction as compared to the middle and top layers. Moreover, due to compaction, moisture migration from top to bottom layers or vice versa occurs, which might cause moisture contrast, and hence the contrast in  $K_a$ , along the length of the sample. As such, in all these circumstances, the effective  $K_a$  of the soil would prevail. To address such situations and simulate their effect on the measurement of dielectric constant, an effort was made to realize the influence of an interface (air and water, and the stratification of the soil due to its compaction) media in which the dielectric probes were inserted. The TDR and CT probes were immersed in water corresponding to different insertion levels of the TDR and CT, defined as z<sub>TDR</sub> and z<sub>CT</sub> (in cm), respectively (refer Fig. 10, which presents results for the TDR probe). The TDR waveforms as depicted in Fig. 10 were obtained to determine  $K_{a}$ . TDR and  $\theta_{TDR}$ . The variations of  $z_{TDR}$  show difference in the shape of the TDR waveform and hence the travel time would also differ. This in turn results in a change in the values of  $K_{a-TDR}$ and  $\theta_{TDR}$ . On the contrary, the CT probe would yield only the values of volumetric moisture content,  $\theta_{CT}$  and dielectric constant,  $K_{a-CT}$  and not any wave form. It can also be observed from Fig. 11 that these probes would yield correct values of  $K_a$  (81) and  $\theta$  (100%) for water, when they are completely immersed in a medium. This indicates that due to the presence of an interface (in this case, air and water), the probes would yield an effective dielectric constant of the media. Incidentally, it can also be observed from the Figures 12 (a) and (b) that the time of travel (=  $t_{end}$ - $t_{head}$ ) of the TDR waves increases with an increase in the dry density and the moisture content. However, it can be clearly inferred from Fig. 12 that the travel time is more sensitive to the increase in moisture content and hence the  $K_{a-TDR}$ increases. However, as stated earlier, depending on the soil characteristics (especially saline soils), pore-solution may contain more ions which would enhance the velocity of the electromagnetic waves and hence  $t_{end}$  would decrease. It is worth noting that in case of the capacitance probe, the capacitance of the medium along the length of the soil sample varies due to the change in moisture content and hence  $K_{a-CT}$  changes.

## Conclusions

Detailed investigations on the performance of TDR and capacitance technique, CT, based probes were conducted by measuring the dielectric constant ( $K_a$ ), moisture content ( $\theta$ ) and electrical conductivity ( $\sigma$ ) of the soils of entirely different characteristics compacted at different moisture contents and densities. The obtained dielectric constant values from these instruments (viz.  $K_{a-TDR}$  and  $K_{a-CT}$ ) have been compared with  $K_{a-Topp}$  and  $K_{a-TP}$ . It has been observed that the measured  $K_a$  is not unique and varies with the types of techniques employed

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for the soil moisture measurement. As these dielectric techniques employ Topp's equation for relating  $K_a$  and  $\theta$ , the change in  $K_a$  of different techniques might yield different values of the moisture content for the same state of the soil. An effort was also made to relate  $K_{a-TDR}$ ,  $K_{a-CT}$ ,  $K_{a-TP}$  with  $K_{a-Topp}$  which would help in determining the  $\theta$  of the soil. It has been observed that  $K_{a-TDR}$  matches well with the  $K_{a-Topp}$  and  $K_{a-TP}$ , while the best match has been observed between  $K_{a-TDR}$  and  $K_{a-Topp}$  as compared to the  $K_{a-CT}$ . The study also demonstrates that the Topp's equation, which though lacks the soil specific parameters in it, is capable of predicting the soil moisture content quite effectively. However, utility and efficiency of the relationship developed between  $K_{a-Topp}$ ,  $K_{a-TDR}$ ,  $K_{a-CT}$  and  $K_{a-TP}$  should be further investigated for various soils of the world.

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## Table 1. Physical properties of the soils used in the present study

	$\Upsilon_d$	C	<b>SS</b> A	Size-f	ractio	n (%)			%		
Soll	(g/cc)	G	$(m^{2}/g)$	Sand	Silt	Clay	LL	PL	PI	OM	USCS
<b>S</b> 1	1.2	2.77	160	0	20	80	64	32	32	0	СН
S2	1.2	2.63	62	0	46	54	54	27	27	0	СН
S3	1.3	2.66	358	16	67	17	56	32	24	2	СН
S4	1.3	2.76	216	25	59	16	51	29	22	2	СН
S5	1.1	2.60	359	3	59	38	79	28	51	21	СН
<b>S6</b>	1.5	2.64	9	100	0	0	Not	Annlie	abla	0	SP
<b>S</b> 7	1.5	2.32	6	100	0	0	INOL	Аррис	aute	0	SP

CH: Clay of high plasticity, SP: poorly graded sand

\*The Unified Soil Classification System





Table 2 (a). Chemical composition of the soils used in the present study

Soil	% by weight								
	SiO <sub>2</sub>	Al <sub>2</sub> O <sub>3</sub>	Fe <sub>2</sub> O <sub>3</sub>	CaO	MgO	K <sub>2</sub> O	Na <sub>2</sub> O	TiO <sub>2</sub>	$P_2O_5$
S1	40.59	55.87	1.27	0.03	0.11	1.38	0.69	0.02	0
S2	37.94	52.84	2.52	1.59	0.20	1.84	0.19	2.69	0.03
<b>S</b> 3	48.19	17.69	22.67	5.18	1.49	0.132	1.32	2.72	0.31
S4	42.16	19.77	29.67	1.39	0.50	1.03	0.27	4.31	0.51
S5	29.12	44.39	9.45	5.61	0.97	3.31	5.51	1.21	0.33
<b>S</b> 6	86.88	9.85	1.22	0.14	0.10	0.51	1.03	0.16	0
S7	85.44	10.04	2.43	0.16	0.03	0.35	1.43	0.02	0

Table 2 (b). Chemical characterization of the soils used in the present study

Soil <i>nH</i>		σ	TDS	CEC	ξ
Son	pii	(mS/cm)	(ppm)	(meq./100g)	(-mV)
<b>S</b> 1	7.72	0.142	91.88	10.23	10.66
S2	7.89	0.193	97	14.77	17.5
S3	7.18	0.330	164.2	65.67	16.4
S4	6.95	0.179	90.02	90.8	15.4
S5	7.7	3.429	1736	130	26.47

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S6	7.64	0.093	60.62	0.70	24.19
<b>S</b> 7	7.97	0.0689	44.57	1.15	20.11

Table 3 Mineralogical	characteristics	of the soils	used in the	present study
rable 5. Winteralogical	characteristics	of the solis	used in the	present study

	Table 3. Mineralogical characteristics of the soils used in the present study			
Soils	Minerals			
S1	Kaolinite (99.5%), Laumonite (0.5%)			
S2	Kaolinite (87.5%), Quartz (5.5%), Illite (7.0%)			
S3	Anorthite (66.2%), Montmorillonite (2.2%), Quartz (20.7%), Hematite (10.2%),			
	Dolomite (0.7%)			
S4	Goethite (46.8%), Quartz (41.7%), Montmorillonite (0.3%), Maghemite (7.4%),			
	Hematite (3.8%)			
S5	Orthoclase (38.3%), Anorthite (24.6%), Magnetite (21.0%), Quartz (16.1%),			
S6	Quartz (100%)			
S7				

	K <sub>a-TDR</sub>		K <sub>a-CT</sub>		$\sigma_{\mathrm{T}}$	DR	σ	CT
State of the sample					(mS/cm)			
	<b>S6</b>	<b>S7</b>	<b>S6</b>	<b>S7</b>	<b>S6</b>	<b>S7</b>	<b>S6</b>	<b>S7</b>
Dried state	4.58	5.13	2.02	2.02	0.0028	0.0028	0	0
Saturated with water	26.83	32.74	14.26	17.95	0.062	0.0703	0.100	0.090
Saturated with:								
0.05M NaCl	26.42	31.39	11.34	14.12	1.083	1.471	1.680	2.230
0.1M NaCl	22.85	26.89	17.84	20.44	1.131	2.345	2.430	3.890
0.2M NaCl			29.34	41.34	4.354	3.774	5.630	6.880
0.5M NaCl			63.3	81.88	9.604	13.829	11.300	17.450

Table 4. Comparison of  $K_{a-TDR}$ ,  $K_{a-CT}$ ,  $\sigma_{TDR}$  and  $\sigma_{CT}$  for Soils S6 and S7

Table 5. Details of the	parameters used for	TP-Mixing model
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Soil	$\eta S_r$	percentage of Minerals				Dielectric constant of the minerals					V	
	%	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$	$K_{M1}$	$K_{M2}$	$K_{M3}$	<i>K</i> <sub><i>M</i>4</sub>	$K_{M5}$	Λ <sub>a-TP</sub>
S1	0.58 0.17	0.995	0.005				11.18	7.66				11.99
	0.57 0.23											13.85
	0.57 0.28											15.16
	0.50 0.51											21.83
	0.52 0.55											23.14
	0.55 0.64											27.03
	0.58 0.67											28.60
	0.55 0.75											31.12
S2	0.64 0.10	0.875	0.055									9.24
	0.54 0.31			0.070								16.02
	0.55 0.43						11.18	6.53	10			19.56
	0.54 0.57											24.01
	0.54 0.68											27.93
	0.54 0.76											30.78
	0.54 0.92											37.21
S3	0.49 0.20	0.662	0.022	0.207	0.102	0.007	5.47	8	6.53	60	8.45	8.60
	0.52 0.28											10.57
	0.52 0.37											12.92
	0.51 0.48											16.25
	0.52 0.59											20.29
	0.52 0.70											24.03
S4	0.53 0.12	0.468	0.003	0.417	0.074	0.038	12	8		6 53 20	60	11.30
	0.52 0.27											15.14
	0.54 0.41								6 53			19.04
	0.54 0.52								0.05 20	20	00	22.47
	0.53 0.68											27.81
	0.54 0.83											33.50
<b>S</b> 5	0.57 0.18	0.468	0.003	0.417	0.074		33.7	6.53	6.2	5.47		14.14
	0.57 0.29											17.32
	0.57 0.37											20.23
	0.59 0.42											21.77
	0.57 0.57											27.27

### **List of Figures**

FIG.1. Typical TDR waveforms for finding out  $t_{head}$ ,  $t_{end}$  and  $\rho_{max}$  corresponding to various states of medium

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FIG. 1. Typical TDR waveforms for determining  $t_{head}$ ,  $t_{end}$  and  $\rho_{max}$  (reflection coefficient occurring at infinite time) corresponding to various states of medium





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