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# Investigations into structure and properties of atomicallyprecise transition metal-chalcogenide clusters of CrTe and ligated Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub>

A Dissertation Submitted in Partial Fulfillment of the Requirements for the Degree of Doctor of Philosophy in Nanoscience & Nanotechnology at Virginia Commonwealth University

by

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> > July, 2017

# Contents

L	ist of	Figures		iv	
A	bstra	.ct		viii	
1	Introduction				
	1.1 Novel Materials and Magic Clusters				
	1.2 Transition Metal—Chalcogenides: Filled Electronic Valence in Periodic Syste				
	1.3	Perio	dic Solids with Ligated Transition Metal—Chalcogenides	10	
		1.3.1	Motivation	10	
		1.3.2	Superatomic Clusters and Their Solids	10	
		1.3.3	Alterations Upon Electronic Properties of Superatomic Clusters	14	
	1.4 Transition Metal-Chalcogenides at The Extremum: Chromium and Tellurium, Purpos of the Present Study			-	
	1.5	Orgai	nization of This Thesis	18	
2	Computational Approach			20	
	2.1	Overv	view	20	
	2.2	2.2 Background		20	
		2.2.1	The Electronic Problem & The Born—Oppenheimer Approximation	20	
		2.2.2	Pauli	24	
		2.2.3	The Hartree—Fock Approximation	25	
	2.3	2.3 Density Functional Theory		27	
		2.3.1	Overview	27	
		2.3.2	The Hohenberg—Kohn Theorems	28	
		2.3.3	The Kohn—Sham Formulation	31	
		2.3.4	Exchange—Correlation Functionals	34	
		2.3.5	Mulliken Population and Hirschfeld Charge Analyses	35	
	2.4	Comp	putational Methods	37	
3	Atomically-Precise Binary CrxTey Clusters			40	
	3.1	3.1 Overview & Two-Dimensional CrTe		40	
	3.2	Pure	Systems of Chromium, and Tellurium	42	
		3.2.1	Overview	42	
		3.2.2	Tellurium Clusters	42	
		3.2.3	A Brief History of Small Chromium Clusters	43	

	3.2.4	Small Clusters of Pure Chromium	47
	3.2.5	Summary	49
3.3	3 The C	Cr <sub>x</sub> Te <sub>y</sub> Clusters	51
	3.3.1	Overview	51
	3.3.2	Geometries & Structure	52
	3.3.3	Summary	64
3.4	Cr <sub>x</sub> Te	ey Series Properties	66
	3.4.1 Chrom	Hirshfeld Charge Density, Average Bond Distances, and "Malleability" of ium	
	3.4.2	Removal Energies & Fragmentation Pathways	70
	3.4.3	Summary	74
3.5	5 Cr <sub>x</sub> Te	ey Electronic Properties	76
	3.5.1	Overview	76
	3.5.2	$Cr_1 Te_y (y=1-4)$	77
	3.5.3	$Cr_2Te_y (y = 1 - 4)$	81
	3.5.4	$Cr_3Te_y (y = 1 - 5)$	85
	3.5.5	$Cr_4Te_y (y = 1 - 6)$	87
	3.5.6	$Cr_5 Te_y (y = 1 - 7)$	96
	3.5.7	$Cr_6Te_y (y = 1 - 6)$	99
	3.5.8	$Cr_6Te_y (y = 7, 8)$	102
3.6	5 Discu	ssion & Conclusions	108
4	Electronic Properties of <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> and Alteration Through Ligand Exchange		110
4.1	Over	view	110
4.2	2 Chan	ge of Basis Set	110
4.3	3 The <sup>7</sup>	Cr6Te8 Metal Core: QZ4P vs. TZ2P (Frozen Core)	112
4.4	1 The <sup>7</sup>	Cr6Te8(PEt3)6 Cluster	116
	4.4.1	Robustness of <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub>	121
4.5	5 Ligar	nd Exchange	123
4.6	5 Discu	ussion & Conclusions	131
5	Summar	y & Future Directions	132
Appe	endix A	Cr <sub>x</sub> Bond Lengths	135
• •	endix B	Cr <sub>x</sub> Te <sub>y</sub> Bond Distances	
Refei	rences	-	

# **List of Figures**

Figure 1-1. Etching reaction of aluminum anions $(Al_{5} - Al_{24})$ with oxygen	5
Figure 1-2. Superatomic Orbitals and Al <sub>13</sub> .	5
Figure 1-3. Ligated Transition Metal-Chalcogenide Clusters and Their Assemblies	11
Figure 1-4. Magnetic behavior of the [Ni9Te6(PEt3)8][C60] cluster assembly.	12
Figure 1-5. Inverse magnetic susceptibility versus temperature measurements	16
Figure 1-6. The evolution of the ZFC-FC magnetization vs. temperature for Sm <sub>2</sub> Ba <sub>3</sub> Fe <sub>5</sub> O	15-δ 17
Figure 3-1. Magnetic moments per atom $\mu$ for chromium clusters of N = 20 – 133	44
Figure 3-2. Groundstate clusters of pure $Cr_n$ , $n = 1 - 6$	48
Figure 3-3. Groundstate structures of Cr <sub>1</sub> Te <sub>1-4</sub> .	52
Figure 3-4. Groundstate structures of Cr <sub>2</sub> Te <sub>1-4</sub> .	53
Figure 3-5. Groundstate structures of Cr <sub>3</sub> Te <sub>1-5</sub> .	54
Figure 3-6. Groundstate structures of Cr <sub>4</sub> Te <sub>1-6</sub> .	56
Figure 3-7. Groundstate structures of Cr5Te1-7.	59
Figure 3-8. Groundstate structures of Cr <sub>6</sub> Te <sub>1-6</sub> .	62
Figure 3-9. Groundstate structures of Cr <sub>6</sub> Te <sub>7,8</sub> .	63
Figure 3-10. Basic properties of the Cr <sub>x</sub> Te <sub>y</sub> binary clusters.	66
Figure 3-11. Magnetic moments for the Cr <sub>x</sub> Te <sub>y</sub> cluster series.	67
Figure 3-12. Hirshfeld Charge Deviation and Bond Distance Averages	69
Figure 3-13. Removal Energies for solitary, and complexed, Chromium and Tellurium	71
Figure 3-14. Mulliken spin populations for Cr <sub>1</sub> Te <sub>1-4</sub> .	77
Figure 3-15. Level diagrams for $CrTe_n$ , $n = 1 - 4$ .	

Figure 3-16. <sup>3</sup> CrTe <sub>3</sub> Atomic Orbital (AO) level diagram.	79
Figure 3-17. <sup>3</sup> CrTe <sub>4</sub> Atomic Orbital (AO) level diagram.	80
Figure 3-18. Density of States (DOS) for Cr <sub>1</sub> Te <sub>3,4</sub> .	80
Figure 3-19. Mulliken spin populations for Cr <sub>2</sub> Te <sub>1-4</sub>	82
Figure 3-20. <sup>1</sup> Cr <sub>2</sub> Te <sub>3</sub> Atomic Orbital (AO) level diagram.	83
Figure 3-21. <sup>1</sup> Cr <sub>2</sub> Te <sub>4</sub> Atomic Orbital (AO) level diagram.	83
Figure 3-22. Density of States for Cr <sub>2</sub> Te <sub>3</sub>	84
Figure 3-23. Density of States (DOS), and OPDOS for <sup>1</sup> Cr <sub>2</sub> Te <sub>4</sub>	84
Figure 3-24. Mulliken spin populations for Cr <sub>3</sub> Te <sub>1-5</sub>	85
Figure 3-25. <sup>7</sup> Cr <sub>3</sub> Te <sub>3</sub> Atomic Orbital (AO) level diagram.	86
Figure 3-26. Density of States (DOS) & OPDOS for <sup>7</sup> Cr <sub>3</sub> Te <sub>3</sub>	87
Figure 3-27. Mulliken spin populations for Cr <sub>4</sub> Te <sub>1-3</sub>	88
Figure 3-28. Mulliken spin populations for Cr <sub>4</sub> Te <sub>4-6</sub>	88
Figure 3-29. Mulliken spin populations for the Cr <sub>4</sub> Te <sub>4</sub> and Cr <sub>4</sub> Te <sub>6</sub> geometries	
Figure 3-30. <sup>7</sup> Cr <sub>4</sub> Te <sub>4</sub> & <sup>9</sup> Cr <sub>4</sub> Te <sub>5</sub> Atomic Orbital (AO) level diagrams	91
Figure 3-31. Atomic Orbital (AO) level diagram for Cr <sub>4</sub> Te <sub>6</sub>	
Figure 3-32. Atomic Orbital (AO) level diagrams for $Cr_4Te_y$ , $y = 4 - 6$	
Figure 3-33. Density of States (DOS) & OPDOS for <sup>7</sup> Cr <sub>4</sub> Te <sub>4</sub>	
Figure 3-34. Density of States (DOS) for <sup>9</sup> Cr <sub>4</sub> Te <sub>5</sub>	
Figure 3-35. Density of States (DOS) for <sup>3</sup> Cr <sub>4</sub> Te <sub>6</sub> .	
Figure 3-36. Mulliken spin populations for Cr <sub>5</sub> Te <sub>1-7</sub>	
Figure 3-37. Atomic Orbital (AO) level diagram for <sup>7</sup> Cr <sub>5</sub> Te <sub>5</sub> .	
Figure 3-38. Density of States (DOS) & OPDOS for <sup>7</sup> Cr <sub>5</sub> Te <sub>5</sub>	

Figure 3-39. Mulliken spin populations for Cr <sub>6</sub> Te <sub>1-8</sub> .	99
Figure 3-40. <sup>1</sup> Cr <sub>6</sub> Te <sub>5</sub> Atomic Orbital (AO) level diagram.	100
Figure 3-41. <sup>9</sup> Cr <sub>6</sub> Te <sub>6</sub> Atomic Orbital (AO) level diagram.	101
Figure 3-42. Density of States (DOS) & OPDOS for <sup>9</sup> Cr <sub>6</sub> Te <sub>6</sub>	101
Figure 3-43. Groundstate geometries of <sup>1</sup> Cr <sub>6</sub> Te <sub>7</sub> and <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> .	102
Figure 3-44. Geometry of the central Cr <sub>4</sub> subunits for <sup>1</sup> Cr <sub>6</sub> Te <sub>7</sub> and <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> clusters	103
Figure 3-45. Mulliken spin populations for <sup>1</sup> Cr <sub>6</sub> Te <sub>7</sub> and <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> .	103
Figure 3-46. <sup>1</sup> Cr <sub>6</sub> Te <sub>7</sub> Atomic Orbital (AO) level diagram.	105
Figure 3-47. <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> Atomic Orbital (AO) level diagram.	105
Figure 3-48. Density of States for unligated <sup>7</sup> Cr <sub>7</sub> Te <sub>8</sub>	106
Figure 3-49. Cluster energetics for ${}^{(x+1)}Cr_6Te_8$ across various values of total $\mu_B$	107
Figure 4-1. Groundstate geometries of <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> utilizing different Basis Sets	113
Figure 4-2. Mulliken spin populations per QZ4P and TZ2P (Large Core) basis set comput	ted
groundstates of the <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> cluster	114
Figure 4-3. Atomic Orbital (AO) level diagram for <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> as computed using the TZ2P (	Large
Core) basis set.	115
Figure 4-4. Density of States for the <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> cluster as computed using the TZ2P (Large C	Core)
basis set	115
Figure 4-5. The groundstate structure of the <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> cluster	116
Figure 4-6. Groundstate geometries for <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> , and core of the <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> cluster	117
Figure 4-7. Mulliken spin populations for <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub>	117
Figure 4-8. <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> Atomic Orbital (AO) level diagram, total	118
Figure 4-9. <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> Atomic Orbital (AO) level diagram, scaled	119

Figure 4-10.	Density of states (DOS) for the Bare and PEt <sub>3</sub> ligated <sup>7</sup> Cr <sub>6</sub> Te <sub>8</sub> clusters12	0
Figure 4-11.	Starting and final Cr spin moment arrangements for the two singlet state	
	permutations of ${}^{1}Cr_{6}Te_{8}(PEt_{3})_{6}$ . 12	1
Figure 4-12.	Cluster energetics for <sup>x</sup> Cr <sub>6</sub> Te <sub>8</sub> (PEt <sub>3</sub> ) <sub>6</sub> across various values of total µ <sub>B</sub> 12	2
Figure 4-13.	Mulliken spin populations for individual chromium atoms within the ligated	
	systems of $L = PH_3$ , CO, and CN	4
Figure 4-14.	Average bond distances, HOMO-LUMO level positions, Hirshfeld Charge Density	,
	Adiabatic Ionization Potential and Electron Affinity energies, for none and various	
	ligands12	5
Figure 4-15.	Atomic Orbital (AO) level diagrams for Bare and Ligated <sup>x</sup> Cr <sub>6</sub> Te <sub>8</sub> cluster cores. 12	8
Figure 4-16.	Density of States for various ligated Cr6Te8(L)6 clusters	0

## Abstract

#### INVESTIGATIONS INTO STRUCTURE AND PROPERTIES OF ATOMICALLY-PRECISE TRANSITION METAL-CHALCOGENIDE CLUSTERS OF CRTE AND LIGATED CR6TE8(PET3)6

By Anthony Filippo Pedicini, Ph.D.

A dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in Nanoscience & Nanotechnology at Virginia Commonwealth University.

Virginia Commonwealth University, 2017

Major Director: Shiv N. Khanna, Ph.D. Commonwealth Professor and Chairman, Department of Physics

The complete understanding of a clusters electronic structure, the primary mechanisms for its properties and stabilization is necessary in order to functionalize them for use as building blocks within novel materials. First principle theoretical studies have been carried out upon the electronic properties of  $Cr_xTe_y$  (x = 1 - 6, y = 0 - 8,  $x + y \le 14$ ), as well as for the larger triethylphosphine (PEt<sub>3</sub>) ligated cluster system of  $Cr_6Te_8$ (PEt<sub>3</sub>)<sub>6</sub>. Together, we aim to use the information garnered from the smaller clusters to address the underlying behavior of the ligated  $Cr_6Te_8$ (PEt<sub>3</sub>)<sub>6</sub>. Additionally, the properties of this larger cluster will be used to further understand its role when paired with  $C_{60}$  within the binary cluster assembled material. The stability and macroscopic properties of the  $Cr_6Te_8$ (PEt<sub>3</sub>)<sub>6</sub> cluster, have been found to be sensitive to type of passivating ligand.

As will be shown, the ground state structures of  $Cr_n$  atoms are sensitive to both the number and position of bonded Te atoms. Moreover, that this sensitivity carries over into larger cluster sizes, and at several size intervals produces clusters with high magnetization. To this, we add the investigation into the manipulation of the  $Cr_6Te_8$  cluster geometry and its properties through various ligands, such as PH<sub>3</sub>, CO, and CN. It will show, that in altering these ligands there is a modification to the clusters valence shell count, which in turn alters its ionization potential and electron affinity. Additionally, although the ionization potential and electron affinity have changed for the  $Cr_6Te_8(PEt_3)_6$  cluster, it has been found that its high magnetization does not.

## **1** Introduction

### 1.1 Novel Materials and Magic Clusters

Systematic study of atomic clusters offers a gateway to understanding the complexity in their properties and the unique phenomena that are present only at these small sizes. The next challenge, is to protect and magnify these properties into large, periodic, systems. Novel materials built in this manner, are purposely synthesized and optimized for the harnessing of a specific property, or function. Materials for specialized microelectronic devices such as spintronics, and new types of computer processors. As well as, new applications within superconductivity, photocatalysis, and nonlinear optical materials.

The building blocks of matter commonly found in nature are atoms or molecules. Depending on their chemistry and the physical conditions present, including pressure and temperature, these atoms/molecules frequently arrange themselves into crystalline solids of welldefined arrays. The properties of the crystals often depend strongly on the chemical nature of the atoms as well as on their arrangement. Consider, as a simple example, two such crystalsdiamond, and graphite. Although both of these materials are built from carbon atoms, their mechanical, electronic, chemical and optical properties are very different due their atomic structure. Molecular crystals, on the other hand, exhibit unique properties because molecules and not atoms are the fundamental building blocks. An example of this is that of ice, that is even though neither hydrogen nor oxygen condenses at 0°C, H<sub>2</sub>O molecules will freeze together. While the examples above demonstrate that by changing the building blocks and/or their arrangements one can create new materials, nature however does not offer pathways to synthesize all such materials.

Advances in experimental techniques over the past three decades have enabled researchers to make clusters of atoms containing few to thousands of atoms. The properties of these sub-nanoscale units are found to be different from the bulk, and change with size and composition. For example, while bulk gold is a noble element, small clusters of Au<sub>n</sub> are found to be highly effective catalysts for a variety of reactions including conversion of CO to CO<sub>2</sub>.<sup>1</sup> Additionally, while bulk aluminum is highly reactive with oxygen, an Al<sub>13</sub><sup>-</sup> cluster is found to be resistant to etching by oxygen.<sup>2</sup> Also, while bulk Rh is paramagnetic, small Rh<sub>n</sub> clusters are found to display ferromagnetic coupling with appreciable moments.<sup>3</sup> What is important is that the properties can change significantly with size. In fact, the reactivity of Fe<sub>n</sub> clusters has been found to change by orders of magnitude by adding just a single atom.<sup>4-6</sup>

The above findings have led to a new and promising direction within nanoscience, namely, using clusters as the basis for new materials, instead of atoms, is the very idea behind Cluster-Assembled Materials (CAMs).<sup>12–17</sup> Like molecular crystals, it is expected that cluster-crystals may possess unique properties hitherto unknown to man. The use of clusters as the main building block, or *motif*, introduces yet another method for tuning properties within a periodic solid. Moreover, since the properties of clusters themselves can be controlled by size, composition, and the charge state, cluster assemblies offer a unique prospect in constructing tailored materials.<sup>7–11</sup> This idea of custom materials encompasses a great deal and offers even more, but creating small clusters is often a difficult task on the road to realizing these materials. Thus, two fundamental hurdles are to be surmounted before continuing; (1), formation and characterization of the cluster motif itself, pure or ligated; and (2), understanding its interactions,

stability, preferred arrangement, and orientation, within a periodic system. Addressing both of these points, to identify new and stable species of interest, as well as facilitate the formation of novel materials, is of the utmost importance.

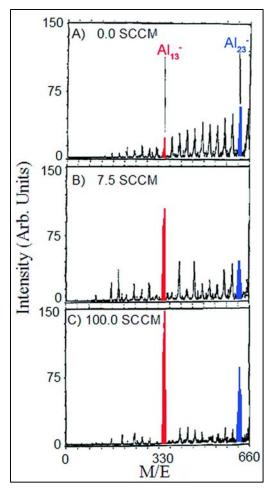
A major downfall in the synthesis of materials using clusters is their intrinsic instability, and desire to coalesce. At these larger sizes, the novel properties seen in smaller versions are then destroyed. One approach to realizing the possibility of novel materials is therefore to identify clusters that are stable and would maintain their identity when assembled. These stable clusters have become known as *Superatoms*, and the prospect of making cluster materials has started a vigorous search for these species.<sup>2,14,18–28</sup> The first step in this direction is to identify the factors that control the stability of clusters themselves.

Just over two decades ago, Khanna and Jena discussed the possibility of designing these stable metallic clusters.<sup>13</sup> Their arguments were derived from the experiments on the mass spectra of simple metal clusters.<sup>29</sup> Specifically, the mass spectra of small sodium clusters observed by Knight and co-workers showed that clusters containing 2, 8, 18, 20, 34, 40... atoms were more prominent than the other sizes. In order to explain the enhanced stability of these *magic* clusters, Knight and co-workers then proposed the *spherical jellium model*.<sup>29–31</sup> In brief, one imagines that the positive charge of all ions present in the cluster is distributed uniformly over a sphere. The electronic levels associated with this charge distribution correspond to  $1S^21P^61D^{10}2S^21F^{14}2P^6$ , etc., much like the electronic states of an atom.<sup>19,31–34</sup>

Like noble gas atoms, the magic numbers (2, 8, 18, etc.) thus correspond to filled electronic shells, thereby indicating the role of electronic counts on the stability. The possibility of describing the electronic structure of clusters, in terms of electronic shells, raised the interesting possibility that clusters themselves could be regarded as superatoms, as well. There

are several reasons for such an analogy. The ionization potentials of simple metal clusters were found to exhibit peaks at sizes corresponding to filled electronic shells much in the same way as atoms. In another series of experiments, it was quite surprisingly found that the chemical behavior of clusters could also be predicted by the shell model.<sup>35–38</sup>

Further proof of this concept came from the experiments by Leuchtner, Harms, and Castleman, who studied the reactivity of Al<sub>n</sub><sup>-</sup> clusters with oxygen.<sup>39</sup> They showed that while other sizes were etched away by oxygen, the mass spectra of the reacted species exhibited a marked peak at Al<sub>13</sub><sup>-</sup>, as well as Al<sub>23</sub><sup>-</sup>and Al<sub>37</sub><sup>-</sup>. **Figure 1-1** below shows the observed mass spectra, while **Figure 1-2** shows the groundstate structure of Al<sub>13</sub><sup>-</sup>. Since Al<sub>13</sub><sup>-</sup> has 40 valence electrons, its inertness can be understood in terms of a closed electronic shell, (as well as the 23-and 37-atom containing systems that also have closed electronic configurations).



**Figure 1-1.** Etching reaction of aluminum anions  $(Al_5 - Al_{24})$  with oxygen. (A) 0.0 sccm oxygen, (B) 7.5 sccm oxygen, (C) 100.0 sccm oxygen.<sup>16,39</sup>

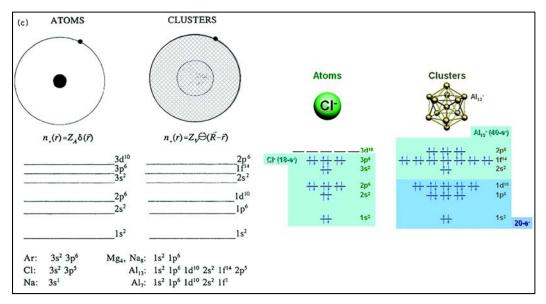


Figure 1-2. Superatomic Orbitals and Al13.

Similarities between atomic and superatomic orbital levels (left), Closed shell Cl<sup>-</sup> compared to Al<sub>13</sub><sup>-</sup> groundstate with closed shell and 40 electron count (right). (Reproduced with permission.)<sup>16</sup> These and other observations have shown that the jellium picture, though extremely simplistic, is amazingly successful in describing many of the globally observed electronic features in a variety of systems and that certain metallic clusters could be described as superatoms. Moreover, later experiments and companion theoretical calculations have proven that aluminum clusters can also behave as halogens and alkaline earth metals, enabling the possibility of forming a class of superatoms with analogies to various elements of the periodic table.<sup>2,37,40–42</sup> It is important to emphasize that although the electronic shells were introduced via the jellium model, the existence of electronic shells of fermionic systems is known to occur for a far wider range of potentials.

## 1.2 Transition Metal—Chalcogenides: Filled Electronic Valence in Periodic Systems

A full valence shell is not only used to understand the stability of free clusters, but also within solid state systems as well. Specifically, systems of crystalline and amorphous semiconductors, where valence shell properties have a large influence on a materials macroscopic electronic behavior. Alterations upon these intrinsic properties are more readily seen when applied to amorphous semiconductors, which they themselves can be divided into two classifications. The first, being the *chalcogenide glasses*; and second, *hydrogenated amorphous* silicon (a-Si:H) and other related solids.<sup>43</sup> (Here, we discuss materials and solids based on the former; and comprising one, or several, chalcogenides.) The term chalcogenides denote dianionic elements from group 16 (VIA), of the periodic table; namely, sulfur, S<sup>2-</sup>; selenium, Se<sup>2-</sup> ; and tellurium, Te<sup>2-</sup>. Oxygen, while still a chalcogen, and along with other oxide based materials, is not discussed here. Moreover, the term "ideal glass" is often given to a material in which within it "all atoms satisfy their valence requirements". In this definition, valence is referred to classically; the number of single covalent bonds an atom requires to complete its outer shell. From the context, an atom that completes its shell of eight electrons is obeying the 8-N rule when N > 4, and N is equal to the number of valence electrons. Binary chalcogenides are typically of two forms, As-Chalcogenide and amorphous (e.g. As<sub>2</sub>Se<sub>3</sub>); or Ge-Chalcogenide and crystalline (e.g. GeSe<sub>2</sub>). Of course, this "ideal" situation is only perfectly suited to describe short-range ordering when long-range (i.e. crystalline) ordering is absent. However, the 8-N rule was first proposed for chalcogenide glasses in an effort to account for the observation that these glasses were insensitive to alteration upon their electronic structure from a third element, purposely introduced into the system, i.e. doping. The term "8-N rule" is often interchanged

with that of "*Mott rule*", attributed to the first person to observe this phenomena, Sir Nevill F. Mott.<sup>44,45</sup>

Knowing the intrinsic nature of chalcogenides, the intention now is to create novel materials based on them. Exercising their high dependence of the 8-N rule, and deviations upon it, we can now begin to discuss using an elemental pairing with the chalcogenides alternative to those of group 15 (VI), i.e. the pnictogens. In doing so, introduces a method of manipulating coordination through choice of that second element, which leads to interesting stoichiometric modifications upon the original concept of these materials and its properties. Along these lines, chalcogenides have been paired with elements from, and studied, across all areas of the periodic table, including; the lanthanides, actinides, transition metals, and other main group elements.

The versatility in creating new materials with transition-metals and chalcogenides, rather than oxides, stems from several advantages present at the atomic level between chalcogens and oxygen. The major differences can be stated simply that chalcogens are: larger and heavier, less electronegative, and further down the group, possess inner *d*-orbitals. This alternate bonding pattern displays; a more covalent bond between metal-chalcogen than metal-oxygen; bonds that may involve *d*-orbitals of the chalcogen; within a compound, oxygen is in its formal oxidation state (-2), while the chalcogen is less negative (-1); and, the chalcogenide ions are more polarizable.<sup>46</sup> This covalent nature of the bonds between metal and chalcogen produces a material which possesses broad valence and conduction bands, while still maintaining a band gap. This gap grows smaller, and may even close, as the chalcogen element of choice moves down the group, from sulfur to tellurium.<sup>46</sup>

The specific choice in using high-spin 3d transition-metals paired with chalcogenides is deliberate. As a result, numerous pairings have produced compounds that each vary wildly in

optical, magnetic, and electronic properties, all sensitive to impurities and/or vacancies.<sup>47</sup> Within these compounds, the mixing between the metal *d*-orbitals with the *s* and *p* of the chalcogen can no longer be ignored. Because, after mixing, the degeneracy in *d*-orbitals between metal and chalcogen has been lifted, and the exact separation between those orbitals is now dependent upon the geometry of the chalcogen. Moreover, the orbital involvement of the chalcogenide in covalent bonding also introduces effects upon the coordination of the chalcogenide, as well. It has been shown previously, that chalcogenides in the *d*<sup>0</sup> (and even *d*<sup>1</sup>, or the spin-paired *d*<sup>2</sup>) configuration prefer a trigonal-prismatic configuration.<sup>46,48</sup> Thus, in conjunction with a particular metal, this type of bonding is seen in many MCs, and often produces a NiAs-type crystal (or, something close to it) when bonded to many of the transition-metals and/or lanthanides.<sup>49</sup> This type of bonding also gives rise to individual cluster units with formula M<sub>6</sub>E<sub>8</sub> (M = transition-metal; E = chalcogenide)<sup>50</sup>, formed through combination of a transition-metal octahedron surrounded by an X<sub>8</sub> cube.<sup>51</sup> Each of these units are often described as a (distorted) fragment of its associated periodic compound.

As mentioned previously, in order to create novel materials based on solitary clusters, a degree of stabilization is required in order to prevent agglomeration. Additionally, a form of isolation from its surroundings as a means to stop growth at a particular cluster size and maintain its properties. Production of ligated-TMC (LTMC) cluster was first completed in an effort to understand the pathways in which reagents combined together to form an extended solid.<sup>51,52–64</sup> This marked something of a beginning in an effort to understand how macroscopic properties of these elemental combinations are transformed, or altered, after ligation at small sizes; resulting in a new type of cluster family with formula  $M_6E_8L_6$  (L = phosphine ligand), (LTMCs, MEL-686, or simply MELs).<sup>60–63,65</sup>

## 1.3 Periodic Solids with Ligated Transition Metal— Chalcogenides

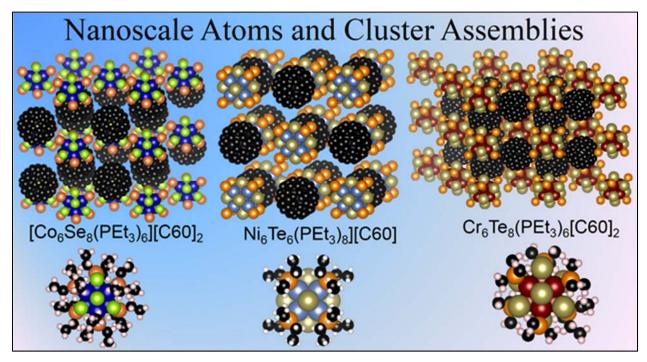
#### 1.3.1 Motivation

One form of constructing larger systems using molecular clusters is through binary stabilization. An example of this can already be seen in every day table salt, NaCl. This *binary-system* method is not new, and can be found throughout the literature.<sup>12,13,15,40,66–69</sup> However, building regularly periodic systems comprised of ligated clusters, who they themselves are composed of transition metal-chalcogenides (TMCs), is a new direction.

#### 1.3.2 Superatomic Clusters and Their Solids

As mentioned above, the first foray into ligated TMCs began with the desire to understand the exact nature of how the bonding between metals and its associated chalcogenide created a periodic network.<sup>63</sup> Investigations into a close relative of the LTMCs are the unligated ternary metal-chalcogenides, with 868 stoichiometry, better known as the *Chevrel Phase* clusters, and formula  $M_x$ Mo<sub>6</sub> $X_8$  (X = S, Se, Te; M = cation).<sup>57,70–76</sup> These have been a source of special attention as they were considered to be the first superconducting ternary system to possess high critical temperatures.<sup>72,77</sup> The overlap, if not similarity, between these two cluster types is not difficult to miss as they have sometimes been discussed together, in explaining the transition from bare cluster to extended system.<sup>57–59,65,72,75</sup>

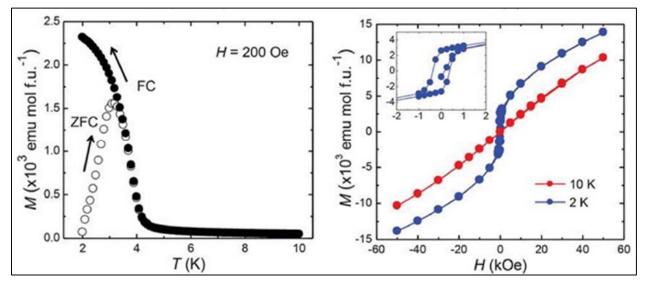
Below, **Figure 1-3** highlights some recent developments along these lines, into novel binary solids, undertaken by Roy *et al.*<sup>78</sup> Within this study, they have resynthesized a selection of LTMCs taken from the literature, specifically Co<sub>6</sub>Se<sub>8</sub>(PEt<sub>3</sub>)<sub>8</sub>, Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>8</sub>, and Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub>, with the express intention of using them as motifs in construction of novel binary solids. Pairing these clusters with fullerenes, i.e. C<sub>60</sub>, as their counterion, forms two different ionic solids. The clusters of Co<sub>6</sub>Se<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> and Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> will form a structure resembling CdI<sub>2</sub>, while Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub> forms the classic NaCl type structure.



**Figure 1-3.** Ligated Transition Metal-Chalcogenide Clusters and Their Assemblies. Atomistic representations of the three metal-chalcogenide clusters, and combinations with the C<sub>60</sub> fullerene complex, left to right. The systems of Co/Se•2C<sub>60</sub>, Ni/Te•C<sub>60</sub>, and Cr/Te•C<sub>60</sub>. (Reproduced and edited with permission.)<sup>78</sup>

These assemblies, built from different transition metal-chalcogenides and counterions, offer a new avenue within areas of photovoltaics, spintronics, and single molecule electrical circuits. Moreover, their electronic and magnetic properties raise new and intriguing questions. Consider the [Ni9Te<sub>6</sub>(PEt<sub>3</sub>)8][C<sub>60</sub>] assembly, which consists of Ni9Te<sub>6</sub>(PEt<sub>3</sub>)8 clusters, built from a Ni9Te<sub>6</sub> core decorated with eight tri-ethylphosphine ligands bonded to the Ni sites. This cluster had been previously isolated as an intermediate species during the synthesis of bulk NiTe from organometallic precursors serving as sources for Ni and Te. However, Roy *et al.* have demonstrated, for the first time, that Ni9Te<sub>6</sub>(PEt<sub>3</sub>)8 forms a rock-salt (i.e. NaCl) structure, where the ligated cluster takes on the role of electron donor when combined with C<sub>60</sub> as an electron acceptor. Experiments indicate that this ionic solid is magnetic and undergoes a ferromagnetic

phase transition at low temperatures (4 K), while exhibiting Curie-Weiss behavior at higher temperatures (T > 10 K), both can be seen below in **Figure 1-4**, left and right respectively.



**Figure 1-4.** Magnetic behavior of the  $[Ni_9Te_6(PEt_3)_8][C_{60}]$  cluster assembly. Temperature dependence of the ZFC and FC magnetization (left), and magnetization as a function of applied field (right). (Reproduced with permission.)<sup>78</sup>

Later, Lee *et al.* experimentally synthesized this binary cluster assembled material again in order to further examine the magnetic behavior at these small temperatures. Results obtained from Superconducting Quantum Interface Device (SQUID) and Muon spin relaxation (MuSR) measurements have shown that these individual clusters behave like isolated magnets, with magnetic moment around 5.4  $\mu_B$  per functional unit in an applied field of 1 Tesla.<sup>79</sup> Moreover, that static ordering of the magnetic moments occurs at a temperature of ~4 K.

First-principles theoretical investigations by Chauhan *et al.* have provided an electronic and magnetic characterization of the [Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub>][C<sub>60</sub>] ionic assembly.<sup>80</sup> This study has shown that despite the large ionization potentials of both cluster and ligand, there exist a charge transfer from ligand to the cluster. Consequently, the PEt<sub>3</sub> ligands create an internal, coulombic, potential-well that lifts the quantum states of the Ni<sub>9</sub>Te<sub>6</sub> cluster, in turn lowering its ionization energy to 3.39 eV, creating a superalkali motif. The metallic core has a magnetic spin moment of 5.3  $\mu$ B, in agreement with experiments. But, the cluster is marked by a low Magnetic Anisotropy Energy (MAE) of 2.72 meV and a larger intra-exchange coupling, which exceeds 0.2 eV. These results showed that the observed paramagnetic behavior around 10 K is due to superparamagnetic relaxations. Additionally, these magnetic cluster motifs, separated by C<sub>60</sub>, experience a weak superexchange that stabilizes in a ferromagnetic groundstate around 2 K. The calculated MAE was sensitive to the charge state (multiplicity), which could account for the observed change in magnetic transition temperature due to the size of the ligands or anions.

All of these properties, and across all binary types of cores, can be considered macroscopic, to which are then used as the starting point for development in an upward fashion toward larger materials. With an eye toward a new functionality for these, and many other, LTMC clusters, it is also necessary to fill the newly formed gap that has emerged between the understanding of atomically precise clusters and these LTMCs. That is, despite their size, a 14element binary-core with six ligands, studies into the exciting properties expected of smallnumbered clusters seems nonexistent, and neither its modifications due to the passivating ligand. Moreover, alternatively to the discussions of the preceding paragraphs, study into the origins of the central bare clusters electronic stability and its formation routes, are rarely, if ever, discussed. The discussions typically found regarding the properties of those smaller cluster variants are completed only in context, as a supportive step for their parent, extended solid, and bulk versions in an "upwards" fashion.

What remains to be seen is the reverse connection, the origin of properties found at the LTMC scale based from the point of view and study of binary cluster growth. In that regard, we aim to answer a few questions, namely; Are the properties of these ligated clusters simply taken

to be a given, as result of their size? Or, are they all that remain after growth and ligation? We shall see below, in chapter 3 and 4, that it is the latter.

#### **1.3.3 Alterations Upon Electronic Properties of Superatomic Clusters**

Above, we briefly mentioned the alteration of a TMC clusters macroscopic properties due to ligand exchange. The sequence of events in the synthesis procedure of LTMCs can vary from system to system, however post synthesis procedures offer another variable in the building of periodic systems. The alteration of the capping ligand in question upon a metal cluster is done to stabilize the metal core, and specifically control the total number of valence electrons. In manipulating this electron count, one can alter the system's ability to donate or accept charge to the external environment, that is, the clusters ionization potential and electron affinity. Such a procedure has been studied and verified on several occasions within the literature.<sup>13,14,16,29,68</sup> Ionization potential and electronic affinity, together, are two of the most fundamental properties in any system. Clusters with full electronic shells exhibit large ionization potentials and a lower electron affinity. Alternatively, clusters deviating from a full valence by one electron, either lacking or in excess, experience the opposite effect, a lowered ionization potential and high electron affinity. The stability of these cluster species is often described within the superatomic framework.<sup>13,16,23</sup>

The triethylphosphine (PEt<sub>3</sub>) ligands attached to metal sites of these LMTC clusters, highlighted above, bond by creating a charge transfer complex. The cluster and ligand, once together, form an ionic compound when paired with C<sub>60</sub>, with the LMTC clusters serving as the electron donors.<sup>78</sup> Some clusters have an open electronic shell, and stability is dictated by their geometric structure rather than a closed electronic shell. Because of this, the addition of a ligand may not close the electronic shell in question, but does change the electronic spectrum of the

cluster itself.<sup>81</sup> The idea of altering the TMC core electronics through ligand exchange arose through the investigations into the [Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub>][C<sub>60</sub>] system, where previous studies have shown the Ni<sub>9</sub>Te<sub>6</sub> core and Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub> to possess the same magnetic moment; with the core becoming superalkali when passivated with ligands.<sup>80,81</sup> Moreover, the magnetic solid undergoes a ferromagnetic phase transition at extremely low temperatures (4 K), but then exhibits Curie— Weiss behavior upon temperature increase.<sup>79</sup>

The argument described above for the Ni/Te clusters system is the same for that based upon chromium. How does the underlying electronic behavior change with respect to the use of different capping ligands? Moreover, can Cr<sub>6</sub>Te<sub>8</sub> be described in a similar fashion to Ni<sub>9</sub>Te<sub>6</sub>? That is, in the process of stabilization, do both geometry and electronic structure, dictate the overall properties of the system; or only electronic?

## 1.4 Transition Metal-Chalcogenides at The Extremum: Chromium and Tellurium, Purpose of the Present Study

Using the preceding sections for the line of inquiry, it is necessary to now understand how two elements at the extremum of the transition metal-chalcogenide bonding argument, chromium and tellurium, can vary so wildly from its TMC molecular cluster compatriots. The same magnetic measurements performed by Roy *et al.* upon the systems  $Co_6Se_8(PEt_3)_6$  and  $Cr_6Te_8(PEt_3)_6$  based solids displayed a drastically smaller, if almost nonexistent, magnetic moment for the  $Cr_6Te_8(PEt_3)_6^{2+}$  system.<sup>78</sup> The inverse magnetic susceptibility measurements shown in **Figure 1-5** highlights the differences between these two cluster assemblies. While the  $Co_6Se_8(PEt_3)_6$  based assembly shows Curie-Weiss behavior,  $Cr_6Te_8(PEt_3)_6$  displays an initial increase followed by saturation. Previous magnetic susceptibility measurements have shown that the solid constructed solely of the  $Cr_6Te_8(PEt_3)_6^{2+}$  cluster to be paramagnetic, with an effective

moment,  $\mu_{eff}$ , of ~2.6 - 2.8  $\mu_B$  between 100 and 300 K, but the electronic structure yielding this moment was not detailed.<sup>51</sup>

It was surmised by Hessen *et al.* that the  $Cr_6Te_8(PEt_3)_6$  cluster is the solid-state relative of  $Cr_3Te_4$ , whose periodic structure is indeed a distorted metal-deficient NiAs type. The periodic solid of  $Cr_3Te_4$  itself has been studied extensively for many years<sup>82–86</sup> and has been found to be one of many stoichiometric combinations of chromium and tellurium to form a periodic solid, each forming their own macroscopic, 2D, properties.<sup>87–110</sup>

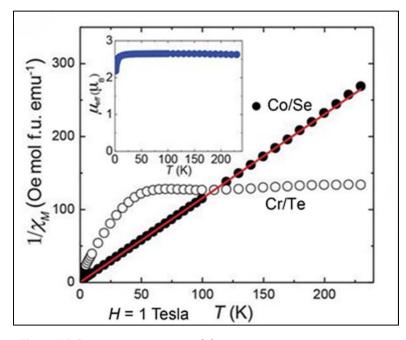
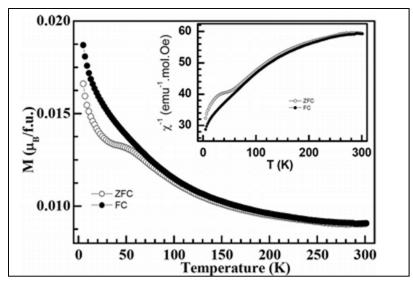


Figure 1-5. Inverse magnetic susceptibility versus temperature measurements.
The Co/Se cluster assembly (black circles) and Cr/Te cluster assembly (open circles) in an applied external field H = 1T. Curie-Weiss fit for Co/Se in red. Inset shows effective moment versus temperature for Co/Se. (Reproduced with permission.)<sup>78</sup>
While the literature details the properties of these numerous stoichiometrys of chromium and tellurium in the two-dimensional solid form, there is little to no discussion as to the origin of said properties based upon smaller constituents.<sup>82–85,87–91,93–113</sup> As such, the precise nature of free, binary CrTe clusters has not been established and is to be remedied.



**Figure 1-6.** The evolution of the ZFC-FC magnetization vs. temperature for  $Sm_2Ba_3Fe_5O_{15-\delta}$ . Inset shows the inverse magnetization vs. temperature in question. (Figure 12. of Reproduced.)<sup>114</sup>

The shape of the inverse magnetic susceptibility plot in **Figure 1-5** for Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> is something that has been seen before within the work of Raveau and Seikh, pertaining to magnetic perovskites. The plots of Zero Field Cooled – Field Cooled (ZFC-FC) and inverse magnetic susceptibility vs temperature measurements (inset) for the quintuple perovskite of Sm<sub>2</sub>Ba<sub>3</sub>Fe<sub>5</sub>O<sub>15-8</sub> are shown above in **Figure 1-6**.<sup>114</sup> The behavior of this perovskite phase as seen in its ZFC magnetization plot shows a large irreversibility as well as an unusual hump at 50 K. This was investigated and from the linear behavior of the M(H) vs temperature plot (not shown) it was determined that the ZFC results do not originate from superparamagnetism. The total of this collected data showed that the magnetization of the perovskite does not involve ferromagnetism, but is in fact due to intra- and interdomain antiferromagnetic interactions. This point was confirmed by the fact that there was no linear dependence in the inverse magnetic susceptibility vs temperature plot (inset, **Figure 1-6**). The behavior of this plot reflects the absence of free spins through the probed temperature range.

With this information, we can deduce that our system of  $Cr_6Te_8(PEt_3)_6$  and  $C_{60}$  is behaving in the same manner. That the magnetic behavior of individual  $Cr_6Te_8(PEt_3)_6$  and its

arrangement within the larger solid dictates the overall behavior seen experiment. Thus, we aim to investigate and establish, if any, the clusters magnetic properties.

Furthermore, the present study seeks to determine if the high magnetization of solitary chromium, and the alternating pattern of magnetization present within its small cluster sizes, is hindered, maximized, or indifferent to the introduction of tellurium. This will be determined through the systematic search of groundstate structures after the sequential addition of both elemental chromium and tellurium atoms. Additionally, we aim to investigate the mechanisms which alter the ionization potential, electronic affinity, and overall magnetic moment in the final  $Cr_6Te_8$  metal core through the exchange with various ligands.

The resultant clusters will be compared to one another, using their electronic stability to determine any fragmentation pathways. Furthermore, analysis of the bonding between the elements, using alterations upon the Hirshfeld Charge densities, as well as molecular orbital (MO) analysis of particularly interesting clusters. Moreover, the oxidation of chromium and movement of electronic charge, which can be seen through the diagrams of both the MOs, and the Mulliken Population charge density graphs of the chromium orbitals.

### 1.5 **Organization of This Thesis**

In Chapter 2, an outline of the theoretical basis behind Density Functional Theory (DFT) is presented, as well as some specifics regarding electronic methods to further investigate binary and ligated CrTe. Chapter 3 will be divided into four portions; the first, overall details of the entire  $Cr_xTe_y$  binary cluster systems. Here, we discuss results pertaining to magnetic moments of the total system, as well as the individual chromium atoms. Additionally, the change of other macroscopic properties, such as bond-lengths, charge movements, and some fragmentation pathways. Within parts two, three, and four, the stability, electronic properties, charge, and

molecular orbital analysis of systems  $Cr_xTe_y$  (x = 1 – 2, y = 1 – 4); (x = 3, y = 0 – 5) & (x = 4, y = 0 – 6); and, (x = 5, y = 0 – 7) & (x = 6, y = 0 – 8), respectively. Chapter 4 discusses the properties discovered for the ligated  $Cr_6Te_8(PEt_3)_{6}$ , as well as how those properties change through substitution of the triethyl-phosphine (PEt<sub>3</sub>) vs. PH<sub>3</sub>, Carbon Monoxide (CO), and Cyanide (CN). Finally, Chapter 5 summarizes the preceding chapters and discusses future directions.

## **2** Computational Approach

## 2.1 Overview

The methods of theoretically calculating the properties, characteristics of, and interactions between solitary atoms, clusters, compounds, molecules, and solids has been formulated, expanded upon, and refined over a very long period of time. These calculations are performed for two reasons: (1), to establish the origins of intrinsic properties seen in those various systems; and (2), to predict those properties within new materials. The very basis behind these powerful methods and tools rests upon the accurate representation of electrons moving in and around a group of point nuclei.

Calculating basic properties, through a process which has been termed in the past and shall be referred to again here as "the electronic problem", is the cornerstone of quantum chemistry and the origins of its most widely used tool today, Density Functional Theory (DFT). This chapter is intended to give a brief introduction to the history, and overview of, the theoretical methods behind DFT and its origins. We conclude this chapter with a discussion regarding the implementation taken within this present study.

## 2.2 Background

#### 2.2.1 The Electronic Problem & The Born—Oppenheimer Approximation

The usage of DFT in finding basic properties of chemicals and compounds arises from the need to approximately solve the time-independent Schrödinger Equation,

$$\hat{H}\Psi = E\Psi, \qquad (2.1)$$

a partial differential equation of order two, where in this context  $\hat{H}$  is the Hamiltonian operator for a system of nuclei and electrons. From this equation, we can solve for the energy E given some wavefunction  $\Psi$ . The Hamiltonian itself contains five terms, each incorporating different aspects of the overall system, and has the form

$$\hat{H} = -\frac{\hbar^2}{2m_e} \sum_i \nabla_i^2 - \frac{\hbar}{2} \sum_a \frac{1}{m_a} \nabla_a^2 + \sum_a \sum_{b>a} \frac{Z_a Z_b e^2}{4\pi\varepsilon_0 r_{ab}} - \sum_a \sum_i \frac{Z_a e^2}{4\pi\varepsilon_0 r_{ia}} + \sum_j \sum_{i>j} \frac{e^2}{4\pi\varepsilon_0 r_{ij}}, \quad (2.2)$$

where indices *a* and *b* denote nuclei, while *i* and *j*, the electrons. The terms specifically, moving left to right in Equation (2.2), are the kinetic energy of the electrons, kinetic energy of the nuclei, nuclei-nuclei repulsion, Coulombic attraction between nuclei and electrons, and finally, the electron-electron repulsion.<sup>115,116</sup> The solution to this Hamiltonian operator involves a wavefunction of which depends on the explicit knowledge in the position of every electron in the system, as well as parametric dependence of the positions of every nucleus. Our problem is further complicated, in three-dimensions, with *N* total number of electrons, and *M* total nuclei; the wavefunction  $\Psi$  for our system is then dependent upon 3*N* coordinates of space for the electrons, *N* coordinates of spin, and 3*M* spatial coordinates for the nuclei. One can immediately deduce that calculating the interactions between every subatomic unit with their counterparts using this wavefunction can become quite large and solving for the groundstate of such a system grows uncontrollably, even with today's computational resources.

In order to scale computations of this kind we can make a simplification, in exercising the fact that nuclei are significantly heavier than the electrons. Knowing this, we consider the electrons around the nuclei to be in their optimal, lowest energy, configuration, which then allows us claim the nuclei are stationary. The motions of both can now, in effect, be considered decoupled from one another and the system in question can be treated as a group of electrons in motion around a group of point nuclei. The procedure we have outlined here is referred to as the

Born—Oppenheimer approximation, and with this we can effectively shorten Equation (2.2).

With stationary nuclei, the second term can be set equal to zero, the terms of their kinetic energy and interactions between one another. Furthermore, the third term detailing the interactions between the nuclei is simply now a constant. What remains of Equation (2.2) is called the electronic Hamiltonian,

$$\hat{H}_{el} = -\frac{\hbar^2}{2m_e} \sum_i \nabla_i^2 - \sum_a \sum_i \frac{Z_a e^2}{4\pi\varepsilon_0 r_{ia}} + \sum_j \sum_{i>j} \frac{e^2}{4\pi\varepsilon_0 r_{ij}} = \hat{T} + \hat{V}_{Ne} + \hat{V}_{ee} , \qquad (2.3)$$

and operates on the electronic wavefunction  $\Psi_{el}$  to obtain energy  $E_{el}$ . If we include coordinates for the electrons  $q_i$  along with those of the nuclei  $q_a$ , the wavefunction can be written as

$$\Psi_{el} = \Psi_{el,n} \left( q_i; q_a \right) . \tag{2.4}$$

The total energy of the system being calculated can be found by simply summing together Equation (2.3) with the constant potential for the interacting nuclei,

$$V_{NN} = \sum_{a} \sum_{b>a} \frac{Z_a Z_b e^2}{4\pi\varepsilon_0 r_{ab}} , \qquad (2.5)$$

which produces

$$(\hat{H}_{el} + V_{NN}) \Psi_{el} = (E_{el} + V_{NN}) \Psi_{el} = U \Psi_{el}$$

$$U = E_{el} + V_{NN}$$
(2.6)

It has been proven in the past, that omission of a constant from the Hamiltonian does not change the wavefunction, so we can now rewrite the Schrödinger Equation as

$$\hat{H}_{el}\Psi_{el} = E_{el}\Psi_{el} \ . \tag{2.7}$$

Once we find  $E_{el}$  and  $V_{NN}$ , we can then obtain U of Equation (2.6), and finally

reincorporate the nuclear motion into these equations. We know the nuclei are in some position  $q_a$ , then change their configuration slightly and move to position  $q'_a$ , and again to position  $q''_a$ , etc. Together, the total number of these motions can be considered strictly as one, i.e.

$$q_a \xrightarrow{\Delta} q'_a \xrightarrow{\Delta} q'_a \xrightarrow{\Delta} q''_a \Rightarrow q_a \xrightarrow{\Delta} q''_a .$$
(2.8)

From the picture we have constructed in the previous paragraphs, the electrons move much more rapidly than the nuclei. When the nuclei change slightly in the manner as shown in Equation 2.8, the electrons immediately adjust to this change, altering the electronic wavefunction,  $\Psi(q_i;q_a) \Rightarrow \Psi(q_i;q_a'')$ , as well as the electronic energy,  $U(q_a) \Rightarrow U(q_a'')$ . Thus, as nuclei move, the electronic energy changes smoothly, with  $U(q_a)$  effectively becoming a form of potential energy. Taking this nuclear potential energy and adding it to the kinetic from Equation (2.2), we obtain the nuclear Hamiltonian

$$\hat{H}_{N} = -\frac{\hbar^{2}}{2} \sum_{a} \frac{1}{m_{a}} \nabla_{a}^{2} + U(q_{a})$$
(2.9)

which is used to calculate the energy of the moving nuclei within

$$\hat{H}_N \Psi_N = E \Psi_N , \qquad (2.10)$$

termed the nuclear Schrödinger Equation.

Compiling together the information from our discussion above, we see that the electronic wavefunction can now be treated as the product between electron and nuclear parts, as originally prescribe by Born and Oppenheimer. Their treatment of the mathematics in calculating properties of molecules have shown that the true wavefunction can be approximated as,

$$\Psi(q_i, q_a) = \Psi_{el}(q_i; q_a) \Psi_N(q_a), \qquad (2.11)$$

if  $(m_e/m_a)^{1/4} \ll 1.^{116}$  Justifications of, and corrections to, the Born—Oppenheimer approximation are outside the scope of this document, and can be found elsewhere. Moreover, those arguments do not address the omissions inherent of the approximation itself. Specifically, one will notice that there is no discussion above regarding the explicit position or coupling of the electrons around and between their individual nuclei. Additionally, there has been no discussion involving the interactions between the electrons themselves, or how those interactions are varied when we incorporate their spin. Thus, the Born—Oppenheimer Approximation is only the beginning when discussing molecular calculations, as we shall see below in subsequent sections.

#### 2.2.2 Pauli

The inclusion of an electrons spin into the calculation of the energy,  $E[\Psi]$ , further expands the wavefunction through necessity. From here, we must address the obvious nature in the physical interactions involving two electrons, with or without the same spin, alternating positions with one another in space. Recalling from above, the electronic Hamiltonian involves only the spatial coordinates of the electrons. We now introduce an additional variable  $\omega$  to accommodate the spin direction, up or down, and further combine this with the electrons three spatial coordinates ( $\vec{r}$ ) into one new variable, denoted as  $\vec{x} = {\vec{r}, \omega}$ . In creating this new variable, we can now write an *N*-electron wavefunction simply as

$$\Psi(\vec{x}_{1},...,\vec{x}_{i},...,\vec{x}_{i},...,\vec{x}_{N}) . \qquad (2.12)$$

For electrons to maintain their indistinguishability from one another requires that their total probability density to not change through the exchange in position, ( $\vec{r}$ ), between any two said electrons. Fermions, all particles with  $\frac{1}{2}$  spin, including electrons, possess an antisymmetric wavefunction, thus any change in the state between two electrons further necessitates a change of

sign to the total wavefunction. This was first outlined by Wolfgang Pauli, and is now known as The Pauli Exclusion Principle, which states that no two electrons may occupy the same state. We can write this in terms of equations as

$$\Psi\left(\vec{x}_{1},\ldots,\vec{x}_{i},\ldots,\vec{x}_{j},\ldots,\vec{x}_{N}\right) = -\Psi\left(\vec{x}_{1},\ldots,\vec{x}_{j},\ldots,\vec{x}_{i},\ldots,\vec{x}_{N}\right), \qquad (2.13)$$

and it is the antisymmetry principle that thereby enforces the exclusion principle.

#### 2.2.3 The Hartree—Fock Approximation

Searching for the wavefunction of a system that yields its groundstate, the minimum energy ( $E_0$ ), is an impossible task. The methods as outlined by Hartree and Fock, provide a practical method to approximate the wavefunction and solve the Schrödinger equation. Within this method the incorporation and enforcement of the antisymmetry principle into the wavefunction is done through the use of a Slater Determinant. Defining the spatial orbital to be  $\psi_i(\vec{r})$ , and the spin orbital  $\chi(\vec{x})$  as the product between spatial orbital and spin functions,  $\psi_i(\vec{r})\alpha(\omega)$  or  $\psi_i(\vec{r})\beta(\omega)$ . Using these, we can write the Slater determinant in matrix form as

$$\Psi_{0}(\vec{x}_{1},\vec{x}_{2},...,\vec{x}_{N}) \cong \Psi_{SD} = (N!)^{-1/2} \begin{vmatrix} \chi_{i}(\vec{x}_{1}) & \chi_{j}(\vec{x}_{1}) & \cdots & \chi_{k}(\vec{x}_{1}) \\ \chi_{i}(\vec{x}_{2}) & \chi_{j}(\vec{x}_{2}) & \cdots & \chi_{k}(\vec{x}_{2}) \\ \vdots & \vdots & \ddots & \vdots \\ \chi_{i}(\vec{x}_{N}) & \chi_{j}(\vec{x}_{N}) & \cdots & \chi_{k}(\vec{x}_{N}) \end{vmatrix} .$$
(2.14)

The antisymmetric nature of the determinant arises from the property that exchanging either two rows or columns, the determinant changes its sign.<sup>117</sup>

The Hartree—Fock energy is obtained through calculating the expectation value of the Hamiltonian constructed using the Slater determinant. This expression for the molecular electronic energy of the system in question can be written as

$$E_{HF} = \left\langle \Psi_{SD} \left| \hat{H}_{el} + V_{NN} \right| \Psi_{SD} \right\rangle = 2 \sum_{i=1}^{n/2} H_{ii}^{CORE} + \sum_{i=1}^{n/2} \sum_{j=1}^{n/2} \left( 2J_{ij} - K_{ij} \right) + V_{NN} \quad , \tag{2.15}$$

where

$$H_{ii}^{CORE} = \left\langle \phi(1) \middle| \hat{H}^{CORE}(1) \middle| \phi(1) \right\rangle = \left\langle \phi_i(1) \middle| -\frac{1}{2} \nabla_1^2 - \sum_{\alpha} \frac{Z_{\alpha}}{r_{1\alpha}} \middle| \phi_i(1) \right\rangle , \qquad (2.16)$$

$$J_{ij} = \left\langle \phi_i\left(1\right)\phi_j\left(2\right) \left| \frac{1}{r_{12}} \right| \phi_i\left(1\right)\phi_j\left(2\right) \right\rangle , \qquad (2.17)$$

and

$$K_{ij} = \left\langle \phi_i(1)\phi_j(2) \middle| \frac{1}{r_{12}} \middle| \phi_j(1)\phi_i(2) \right\rangle .$$
(2.18)

Equation (2.16) is the sum of electron kinetic energy and electron-nuclear attraction terms. Equations (2.17) and (2.18) represent the Coulomb and Exchange integrals, respectively. Both equations sum together to form the Hartree—Fock potential,  $V_{HF}$ , experienced by the electron. The Coulomb term describes the energy between interacting electrons *i* and *j* in their respective positions and spin states. While the Exchange term is due to the possibility of an exchange occurring between those two electrons into their respective partners position and state. We must note that orthonormality of the spin orbitals renders this term zero for electrons in different spin states, and electron exchange only exists for electrons with similar spin. Moreover, the convenient removal within the equations above of the *self-interaction* term, when i = j. In this situation, Equations (2.17) and (2.18) cancel out one anther within (2.15). This *self-interaction* 

The Hartree—Fock Approximation offers a practical method for solving the Schrödinger equation in a simplified and reasonable representation of the wavefunction. Using the Slater determinant within this approximation, the problem of calculating the interactions between all N

electrons is reduced to simply one involving those electrons interacting with their surrounding environment. Finally, this HF method introduces the concept of the self-consistent field (SCF) approximation for iteratively solving the HF equations. Where an initial guess to the wavefunction is successively made more exact through calculation of the energy and continual update. This process serves at the very heart of DFT, and both will be outlined in the following section.

## 2.3 **Density Functional Theory**

#### 2.3.1 Overview

From above, we recall that the wavefunction of an *N* electron molecule depends on 3*N* coordinates and *N* spin coordinates. However, the electronic Hamiltonian involves only one- and two-electron spatial terms. This implies that the molecular energy of the system can be written in terms of integrals involving only six spatial coordinates. This leaves us with some disturbing facts, namely, that the many-electron wavefunction contains more information than we need, and it lacks any direct physical significance. Resolving this has led to the search of new wavefunctions, and has even introduced the concept of replacing the wavefunction as the primary construct with that of the electron density  $\rho(\vec{r})$ . We shall see below that the density can be used to construct everything necessary within a calculation, and solved self consistently to reach a unique groundstate energy. There is no universal method for computing a groundstate from the electron density, however the purpose of DFT is to approximate it.

The electron density is defined as

$$\rho(\vec{r}) = N \int \cdots \int |\Psi(\vec{x}_1, \vec{x}_2, \vec{x}_3, \dots, \vec{x}_N)|^2 d\vec{x}_1 d\vec{x}_2 d\vec{x}_3 \cdots d\vec{x}_N, \qquad (2.19)$$

and represents the probability of finding the  $i^{th}$  electron at any point within the volume of total electrons  $d\vec{r}$ . It has the property of

$$\int \rho(\vec{r}) d\vec{r} = N \quad , \tag{2.20}$$

which states that integration over the volume elements yields the total number of electrons N.

A precursor to DFT, and one of the first examples to outline calculation methods based upon the density, was the work of Thomas and Fermi in 1927, the Thomas—Fermi Model.<sup>121</sup> Based upon the model of a Uniform Electron Gas (UEG), they proposed a description for the kinetic energy of electrons to be

$$T_{TF}\left[\rho(\vec{r})\right] = \frac{3}{10} \left(3\pi^2\right)^{\frac{2}{3}} \int \rho^{\frac{5}{3}}(\vec{r}) d\vec{r} , \qquad (2.21)$$

and the total energy of an atom by the equation

$$E_{TF}\left[\rho(\vec{r})\right] = \frac{3}{10} \left(3\pi^2\right)^{\frac{2}{3}} \int \rho^{\frac{5}{3}}(\vec{r}) - Z \int \frac{\rho(\vec{r})}{r} d\vec{r} + \iint \frac{\rho(\vec{r}_1)\rho(\vec{r}_2)}{r_{12}} d\vec{r}_1 d\vec{r}_2 \quad .$$
(2.22)

The first term is the kinetic energy, and is derived from the statistical behavior of interacting electrons. The second and third terms describe the interactions of nuclei-electron and electron-electron repulsion. Within the third term above, one can be see that there is no incorporation of the exchange between electrons. In addition to this, the Thomas—Fermi Model itself is not very accurate. However, our concern here is not with its accuracy, but with the fact that the model has now shown it to be possible to use the electron density as a parameter in performing calculations.

### 2.3.2 The Hohenberg—Kohn Theorems

The next point in the history of DFT first began with the two theorems of Hohenberg and Kohn, in 1964, which together establish the basic framework for describing exactly how the electron density can be incorporated into a variational procedure.<sup>122,123</sup> Their work proved for a

molecule with non-degenerate (only one) groundstate, that the energy, wavefunction, and all other properties, are uniquely determined by its electron probability density.

The first theorem states:

The external potential,  $V_{ext}(\vec{r})$ , (to within some trivial additive constant) is determined by the electron density  $\rho(\vec{r})$ ; because this potential fixes a particular Hamiltonian, and one can find that the full many particle groundstate is a functional of the density.

Establishing this point solidifies the use of the density as a parameter for determining the interaction potential between nuclei and electrons. The Hamiltonian this theorem applies to can be written as

$$\hat{H} = -\frac{1}{2} \sum_{i=1}^{n} \nabla_{i}^{2} + \sum_{i=1}^{n} v(\vec{r}_{i}) + \sum_{j} \sum_{i>j} \frac{1}{r_{ij}} , \qquad (2.23)$$

where

$$v(\vec{r}_i) = V_{ext}(\vec{r}_i) = -\sum_{\alpha} \frac{Z_{\alpha}}{r_{i\alpha}} \equiv V_{Ne}(\vec{r}) , \qquad (2.24)$$

and using the property described in Equation (2.20), we can determine this external potential of Equation (2.24). From here, we can now find the remaining properties of the system, such as kinetic and potential energies, and the total energy  $E_V^{HK}$  for some potential V, all utilizing the density as a variable, written as

$$E_{V}^{HK}[\rho] = E_{Ne}[\rho] + T[\rho] + E_{ee}[\rho] = \int \rho(\vec{r}) V_{Ne}(\vec{r}) d\vec{r} + F_{HK}[\rho], \qquad (2.25)$$

where

$$F_{HK}[\rho] = T[\rho] + V_{ee}[\rho]$$
(2.26)

is Hohenberg—Kohn functional. When this functional operates upon a given density, it produces values for the kinetic  $\hat{T}$  and electron-electron repulsion  $\hat{V}_{ee}$  within the groundstates wavefunction.

The Hohenberg—Kohn functional is what one would need to solve the Schrödinger equation exactly. However, the explicit form of the two terms on the righthand side of Equation (2.26) are completely unknown and must be found. But, we can rewrite the latter term in its classical analogue form of

$$V_{ee}[\rho] = \frac{1}{2} \iint \frac{\rho(\vec{r}_{1})\rho(\vec{r}_{2})}{r_{12}} d\vec{r}_{1} d\vec{r}_{2} + V_{ncl}[\rho], \qquad (2.27)$$
$$V_{ee}[\rho] = J[\rho] + V_{ncl}[\rho]$$

where the  $V_{ncl}[\rho]$  term encapsulates the non-classical contributions within electron-electron interaction, such as the self-interaction correction, exchange, and Coulomb correlation.

The second theorem states:

The functional that delivers the groundstate energy of a system, that energy is the groundstate if-and-only-if the input density is the actual groundstate.

This means that for some trial electron density which is greater than zero and associated with some external potential, the energy obtained using Equation (2.25) will be an upper-bound to the true groundstate. That is, the particular density that minimizes this energy obtained will then be the exact groundstate.

These two theorems developed by Hohenberg and Kohn solidify the usefulness of the electron density as a viable construct and parameter to replace the explicit wavefunction when computing the groundstate energy through the variational principle. However, these two theorems do not establish a routine in which to solve the Schrödinger Equation, and it was not

until later, in 1965, within the work of Kohn and Sham where they would devise a solution to this problem, through the use of a universal functional.<sup>124</sup>

#### 2.3.3 The Kohn—Sham Formulation

Modern density functional theory holds its origins in the implementation of the procedures as outlined by Kohn and Sham, where calculation of many-body properties can be completed through independent particle methods. Within their work they replace the many-particle interacting system with that of an auxiliary system, comprised of non-interacting particles, specifically the electrons. This fictitious auxiliary system then effectively allows one to split the behavior of the electrons into two components which can be treated individually: the first, where their kinetic energy is computed exactly; the second, the electron correlation, and repulsion, which is to be approximated.

To elaborate, let us suppose a system of *N* electrons. Furthermore, that they do not interact with the surrounding nuclei, but with some potential  $V_s(\vec{r})$ . We intentionally create this potential in a manner that fosters a density that does not change, i.e.  $\rho = \rho_0$ . Assuming this potential exists, we can find  $\rho$ . This density is constructed from single electron orbitals, the Kohn—Sham spinorbitals, to form the Slater determinant in a similar fashion to that of the Hartree—Fock approximation, and is written

$$\rho = \sum_{i}^{N} \left| \psi_{i}^{KS} \right|^{2} . \tag{2.28}$$

Now, because the electrons do not interact with one another, we only need to iteratively solve for the energy of the individual one-electron Hamiltonians as an eigenvalue problem of the form

$$\hat{h}_i^{KS} \boldsymbol{\psi}_i^{KS} = \boldsymbol{\varepsilon}_i^{KS} \boldsymbol{\psi}_i^{KS} , \qquad (2.29)$$

where this describes the energy of a particular electron in orbital *i*. The total number of oneelectron orbitals, their Hamiltonians, and energies, are summed together to effectively obtain that of the total system, and can be seen in the expressions of

$$\hat{H}_{S} = \sum_{i=1}^{n} \left[ -\frac{1}{2} \nabla_{i}^{2} + V_{s}\left(\vec{r}_{i}\right) \right] \equiv \sum_{i=1}^{n} \hat{h}_{i}^{KS}$$

$$\Psi_{s,0} = \left| u_{1}^{KS} u_{2}^{KS} \cdots u_{n}^{KS} \right|, \text{ with } u_{i}^{KS} = \psi_{i}^{KS}\left(\vec{r}_{i}\right) \sigma_{i}$$
(2.30)

where  $\sigma_i$  is the spin coordinate of the *i*<sup>th</sup> electron, and  $\varepsilon_i^{KS}$  the *Kohn—Sham energy eigenvalues*.

The total energy for the groundstate as computed under the Kohn—Sham formalism can be written as

$$E_{KS} = T_0[\rho] + E_{Ne}[\rho] + J[\rho] + E_{xc}[\rho] , \qquad (2.31)$$

where

$$T_0[\rho] = -\frac{1}{2} \sum_{i=1}^{N} \left\langle \psi_i^{KS} \left| \nabla \psi_i^{KS} \right\rangle \right\rangle, \qquad (2.32)$$

is the exact kinetic energy of the auxiliary system,

$$E_{Ne}[\rho] = \int V(\vec{r}) \rho(\vec{r}) d\vec{r} = \sum_{i}^{N} \int \sum_{A}^{M} \frac{Z_{A}}{r_{1A}} |\psi_{i}^{KS}(\vec{r}_{1})|^{2} d\vec{r}_{1}$$
(2.33)

represents the Coulomb Nuclear-electron attraction, and

$$J[\rho] = \frac{1}{2} \iint \frac{\rho(\vec{r}_1) \rho(\vec{r}_2)}{|\vec{r}_1 - \vec{r}_2|} d\vec{r}_1 d\vec{r}_2 , \qquad (2.34)$$

is the Coulomb repulsion integral.

The final term in Equation (2.31) ,  $E_{xc}[\rho]$  , is termed the exchange-correlation energy,

which can be written as

$$E_{xc}[\rho] \equiv \Delta T[\rho] + \Delta J[\rho], \qquad (2.35)$$

and represents the sum of two separate discrepancies. The first is the inherent difference in energy between this fictitiously constructed one-electron schematic and the actual kinetic energy of the system in question,  $\Delta T[\rho] \equiv \overline{T}[\rho] - T_0[\rho]$ . The second, is the energy that arises between interacting electrons, termed the *correlation* energy or Hartree Energy (as calculated by the Coulomb repulsion and interaction term),  $\Delta J[\rho] \equiv \overline{J}[\rho] - J[\rho]$ .

The utility of the Kohn—Sham approach is in the ability to turn the problem of solving a complicated many-particle system into an independent-particle one, despite these discrepancies. The exact contributions of the kinetic and potential energies are readily calculated, while the remaining contributions arising from these discrepancies are placed within  $E_{xc}$ , whose exact form is unknown and must be approximated at the time of calculation. Much progress has gone into devising new and all-encompassing forms for the  $E_{xc}$  term, resulting in many available choices, and improving them is a continual effort.

Iteratively solving for a systems electron density and energy using the Kohn—Sham formalism (the SCF procedure) can be outlined as follows; (1) Choose a Basis-Set (detailed below), an *exchange-correlation functional*, and calculate the electronic density of the system; (2) Using this density, calculate the exchange—correlation potential of the system, and all of the one-electron Hamiltonians with their individual energies; (3) calculate the Kohn—Sham (KS) matrix elements (i.e. the interactions between orbitals); (4) Solve the KS equations for their coefficients and the total energy of the system; (5) Use the coefficients to update and improve upon the previously calculated electron density; (6) Return to (2), and continue until the density and energy of the system does not change with appreciable difference. This energy difference is termed the *convergence criterion*, and is often taken to be 1E-3 eV (electron-volts). Specifically, a system is deemed isolated, or *converged*, when the difference between its calculated energy of the previous cycle and energy from that of the current one, is less than or equal to 0.001 eV.<sup>125</sup>

### 2.3.4 Exchange—Correlation Functionals

The Kohn-Sham equations, since their publication, have served as the starting point for any and all DFT calculations, and has proven itself time and time again. What remains, is to further devise an appropriate exchange-correlation functional which eliminates all the unknowns within a calculation. The true analytical form of the functional is itself unknown, but over the decades, there have been numerous undertakings in the derivation of new functionals, each aimed specifically at further refinement or the inclusion of another aspect in the behavior of electrons. This have given rise to functionals that vary wildly in theory and extent, and dependent upon a functionals complexity it can be classified with its counterparts in what has affectionately been termed the "Jacob's Ladder" of functionals.<sup>126</sup> The first rung being the simplest, with the top rung reserved for functionals deemed closest to representing the actual electronic density of a system, found in nature.

Within the first rung of this ladder resides the basis for all exchange—correlation functionals, the *Local Density Approximation* (LDA). The functional describes the reduction of the complex arrangement of molecules within a system to a simpler argument, to one involving a uniform electron gas within a known fixed volume. This approximation assumes homogeneity, and divides the volume containing the electronic gas into smaller regions. This division then reduces the calculation of determining the exchange—correlation energy contribution to the overall system into nothing more than the multiplicative product of the small volumes and the density within them. The algebraic expression for the exchange portion was originally derived by Bloch and Dirac, and the correlation originally fitted through Quantum-Monte Carlo

simulation by Vosko, Wilk, and Nusair (VWN), with several variants upon it in later years.<sup>125,127–131</sup> The properties of systems obtained using LDA have made it insufficient for many applications in chemistry, however. It has been shown to give reasonable ionization, dissociation, and cohesive energies to within 10-20 %. But, bond lengths of molecules and solids to an accuracy of ~2%. The functional cannot be relied upon for use in systems that are dominated by electron-electron interaction effects, such as transition metal-oxides, as well.

An improvement upon LDA, on the next rung upwards of our ladder, resides the *generalized gradient approximation* (GGA) functionals. Functionals here add an extra term to their exchange portion, to include not only the position of the electrons of the one-electron system, but also their gradient. Such an inclusion effectively reduces the errors of LDA by a factor of 3 when calculating atomization energies for small molecules. Moving up in complexity, we highlight the Hybrid functionals. These functionals marriage together the exchange portion derived separately, or taken from another functional, with the correlation of yet another (derived or taken from). The exact procedure for creating functionals is beyond the scope of this dissertation, but Scuderia and Staroverov give a detailed outline and brief overview of the complexity at each level of formalism and provide starting points for review of the literature.<sup>132</sup>

### 2.3.5 Mulliken Population and Hirschfeld Charge Analyses

Using the capabilities of first-principles DFT, or rather "onsite" DFT, which involves computation at the atomic orbital level, we can compute a number of useful electronic values. In doing so, we aim to complete two aspects in this investigation. The first, is to understand the emergence and eventual collapse of magnetization in the progression from small, binary, Cr-Te clusters, up to the larger ligated  $Cr_6Te_8(PEt_3)_6$  system. The second, to establish basic electronic information that can be used to describe behavior of these clusters on the macroscopic level; either in a large periodic system, where onsite DFT is impossible, or in a top-down approach through experimental measurements. We bridge these two ideas together through the methods of *Mulliken Population Analysis* (MPA), *Hirshfeld Charge Analysis* (HCA).

Briefly mentioned above, Mulliken Population Analysis is the oldest and best-known definition in describing atomic charge. It is completed using the optimized atomic orbitals and their coefficients, found during the calculation, which are then used to form the resultant electron "density matrix". Thus, this density matrix possesses all the information of the system, specifically with regards to every atom, its orbitals, electron occupations, and orbital overlap with its neighbors.<sup>133–137</sup> Because MPA involves such detail, we can obtain information regarding both, the density of charge present on an atomic site, as well as the spin direction and number of electrons. Within this study, we shall only concern ourselves with the population of spin for each element, and how that spin population is distributed across all of its orbitals. We can easily deduce that applying MPA to large systems can become computationally taxing, very quickly, and only applied to onsite DFT. But, we can continue with methods of charge analysis which are based on the electron density, as a function of space, regardless of how that density is computed.

Hirshfeld Charge Analysis, involves effectively two densities, one for the total molecule itself, and a fictitious density constructed from each of the elements within that molecule. Atomic charges obtained by this method are a result of distributing, among all the atoms in the molecule, the total electronic probability density, which can be seen in

$$\rho_{A}(x, y, z) = \frac{\rho_{A}^{0}(x, y, z)}{\sum_{A} \rho_{A}^{0}(x, y, z)} \rho_{mol}(x, y, z) , \qquad (2.36)$$

where  $\rho_{mol}(x, y, z)$  is the electronic probability density at some point,  $\rho_A(x, y, z)$  the amount of density at (x, y, z) being assigned to atom A,  $\rho_A^0(x, y, z)$  is the electronic density of the isolated atom A (which has been calculated using the same method and basis set to obtain  $\rho_{mol}(x, y, z)$ ), and the sum in the denominator of Equation (2.36) is over all the probability densities of the isolated atom types found within the molecule. Finally, the Hirshfeld Charge for an atom A can be written as

$$Q_A = Z_A - \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \rho_A dx dy dz \quad , \tag{2.37}$$

where  $Z_A$  is the atomic number of atom A.<sup>116,137–142</sup> Doing this analysis allows one to view density movement on a larger scale, across the entire molecule. Moreover, the individual Hirschfeld charges on each atom provides the means to view a molecules effective dipole strength and its direction.

## 2.4 **Computational Methods**

All geometries below have been found, and their properties calculated, under the framework of DFT utilizing the exchange and correlation components of the generalized-gradient approximation (GGA) functional as derived and outlined by Perdew, Burke, and Ernzerhof (PBE).<sup>127,143</sup> All calculations and property investigations are completed using the *Amsterdam Density Functional* (ADF 2016.104) set of codes.<sup>144–146</sup> Here, the molecular orbitals are represented as linear combinations of atomic orbitals (LCAO) centered on the atomic sites. These onsite one-electron orbitals are generated in the fashion outlined by John C. Slater, the Slater-type orbitals (STOs).<sup>147–149</sup> Moreover, geometry optimizations have been done under

ADFs *Zeroth-Order Regular Approximation* (ZORA) representation, a modification to the solution of the four-component Dirac equation, to effectively treat relativistic effects.<sup>150–154</sup>

In addition to the choice of exchange-correlation functional, one is also afforded a choice in the size of the Basis-Set, or simply basis, to use within a calculation. The Basis Set file is nothing more than a table, or list, of which there is one file for each element on the periodic table, with a minimum of one pair of numbers, one for each orbital of that element. The first number is the fitting constant, designed to calibrate that particular orbitals behavior and contribution to the overall wavefunction. The second number in this Basis file is the "Slater orbital exponent",  $\zeta$  (zeta), which is a fitting constant used to accurately represent the long-range behavior of the orbital it is associated with. Of course, there are a fixed number of physical orbitals, but there is no limit to the number orbitals we can use in order to construct the full MO of a particular system. Thus, depending on the calculation, one can choose a basis set with a single zeta coefficient (SZ) (one orbital coefficient, and one zeta parameter) to represent atomic orbitals, or as many as four, quadruple-zeta (QZ) (eight coefficients, and eight zeta parameters), for every element. Obviously, the choice of basis set size has a direct effect on the final Molecular-Orbital (MO) representation. As such, when using local atomic orbitals to build a larger MO, the basis plays a very important role in calculating individual electron contributions to the system. Moreover, all charge analysis methods upon the system in question will involve one or several aspects of the basis and the final computed coefficients.

Within ADF, the various geometries of Cr<sub>x</sub>Te<sub>y</sub> stoichiometry outlined below (unless otherwise noted) have been computed using the QZ4P basis set (Quadruple Zeta, Quadruple Polarized; all-electron) basis.<sup>155</sup> This basis consists of 13S, 8P, 5D, and 3F functions for Cr; and 18S, 15P, 8D, and 3F functions for Te. The 4P designation represents the addition of functions

(coefficients and zeta exponents) to the basis in order to appropriately represent the stretching, or polarization, and modification of orbitals due to bonding and other effects.

These atoms within the clusters will be moved in the direction of forces until those forces are reduced to 0.001 Hartree (0.027 eV) per Å, and total bonding energy reduced to 0.001 eV per geometry iteration, at which time the cluster is considered to have converged and thus reached its groundstate. Converged geometries are visualized using the Discovery Studio Client as provided by Dessault Systems, Inc. (Formerly Accelrys), and the ADF Graphical User Interface (ADF GUI). The ADF GUI will be used to visualize molecular orbitals, and help in detailing other properties such as Hirshfeld and Mulliken Populations (HPA and MPA). Both of these analysis techniques are employed in order to ascertain the spin density of individual atoms as well as the underlying charge movement between the various atoms, and cluster fragments. An isosurface value varying between 0.01 and 0.03 electrons will be applied and used throughout to better view the molecular orbitals.

The structures found in the search for binary atomically-precise CrTe, in addition to their Mulliken Populations, Hirshfeld Charges, and other basic cluster properties, will be discussed during the presentation of results in Chapter 3. And similarly, for ligated versions of Cr<sub>6</sub>Te<sub>8</sub> within Chapter 4.

# **3** Atomically-Precise Binary Cr<sub>x</sub>Te<sub>y</sub> Clusters

# 3.1 Overview & Two-Dimensional CrTe

While small binary clusters of chromium and tellurium are nonexistent in the literature, there are several reports describing the fundamental unit cells of various two-dimensional, periodic systems. Chevreton, amongst a handful of others, were first to describe the magnetic behavior and crystallographic properties within systems containing the basic units of CrTe and  $Cr_3X_4$  (X = S, Se, Te).<sup>82–85</sup> Around this time it was first proposed by Khoi & Veillet in their study of  $Cr_3Te_4$ , and later seen in the NMR studies of Hashimoto & Yamaguchi upon  $Cr_7Te_8$ , the presence of two different kinds of internal electric fields.<sup>85,87</sup> It was inferred that both systems were comprised of two chromium oxidation states, specifically  $Cr^{2+}$  and  $Cr^{3+}$ . Moreover, in addition to  $Cr_3Te_4$  and  $Cr_7Te_8$ , Chevreton also discovered that the Cr-Te umbrella encapsulates another homogeneous compound,  $Cr_2Te_3$ .<sup>82</sup> That same year, Van Con & Suchet would go further and state that the Cr-Te family possessed more than three homogeneous compounds, but many more nonstoichiometric counterparts in the composition range of 52-61 at.% Te.<sup>83</sup>

The very early studies of Cr<sub>7</sub>Te<sub>8</sub> showed its fundamental unit cell to be of the NiAsstructure with associated Cr-vacancies. The NiAs crystal structure is hexagonal, with a layering scheme between the two element types representative of an ABABAB... stacking, with atom A in the octahedral coordination, and atom B in the trigonal prismatic. The vacancies described are the literal absence of an element within the lattice, typically chromium, and tends to occur every two layers within the superstructure. In a two-step thermal treatment procedure of this crystal, Hashimoto & Yamaguchi succeeded in producing two phases, an ordered, monoclinic; and disordered, hexagonal. Each with a different arrangement of those vacancies. Their saturation magnetization experiments reported a slightly higher Curie temperature and effective Bohr magneton number for the disordered phase than that of the ordered; 361 K vs. 350 K, and 2.5  $\mu$ B vs. 1.8  $\mu$ B.<sup>87</sup>

Obviously, this opened the door for many more studies into the Cr-Te systems, in both strictly pure binary forms, and even doped<sup>108,113</sup> versions. Early investigations delved into the magnetic properties of Cr<sub>2-8</sub>Te<sub>3</sub><sup>88,89</sup>, as well as further studies into previously known structures and into newly found compositions, such as; CrTe, Cr<sub>23</sub>Te<sub>24</sub>, Cr<sub>7</sub>Te<sub>8</sub>, Cr<sub>5</sub>Te<sub>6</sub>, and Cr<sub>3</sub>Te<sub>4</sub><sup>90</sup>. Within the same year of this comprehensive magnetism study, Klepp & Ipser in 1982, report their discovery of the never before seen CrTe<sub>3</sub> crystal phase.<sup>91</sup> Its electronic structure, and underlying role of tellurium, was not detailed until five years later.<sup>94</sup> Some years prior, in 1987 Yuzuri *et al.* detail their findings involving the effects of pressure upon the magnetic properties of Cr<sub>2</sub>S<sub>3</sub> and Cr<sub>2</sub>Te<sub>3</sub>.<sup>92</sup> In 1989 with Dijkstra et al. they discuss band-structure, magnetism, and transport within CrTe, Cr<sub>3</sub>Te<sub>4</sub>, and Cr<sub>2</sub>Te<sub>3</sub>.<sup>86</sup> A year later, yet another phase, CrTe<sub>2</sub>, is newly discovered.<sup>93</sup> Finally, in 1991 through the work of Steigerwald *et al.*, a report appears detailing the differences between our cluster, Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub>, and the connection to its periodic ancestry of Chevrel clusters and the NiAs structure.<sup>57</sup> Later, a discussion of the clusters' synthesis and its connection to the two-dimensional Cr<sub>3</sub>Te<sub>4</sub> system by Hessen *et al.* in 1993.<sup>51</sup> The study of Cr-Te systems continues, up until today, with literature discussing everything from solidifying the nature of its crystal structure<sup>96</sup>, pressure induced transformations<sup>97–100</sup>, and underlying magnetic origins and overall electronic behavior.<sup>95,101–104,106,109,110,112</sup>

Despite the vast number of investigations into periodic CrTe, the magnetism, structural behavior, and electronic subsystem of atomically-precise CrTe clusters has yet to be understood.

To fully understand the complications in theoretically finding groundstate structures, electronic, and magnetic properties for CrTe based systems, it is necessary to first discuss and highlight a few previous results, and difficulties, when finding those same properties within pure clusters of those elements.

# 3.2 **Pure Systems of Chromium, and Tellurium**

### 3.2.1 Overview

Firstly, to establish a unifying and overall framework in which to discuss new clusters based on chromium, a gap appears that must be addressed. Specifically, in regards to chromium clusters, between i) the computational results within this document; and ii), those of both theoretical computation and experiments previously completed. To bridge this gap, groundstates for pure chromium clusters,  $Cr_{n} n = 1 - 6$ , have been obtained within the formalism as outlined above in Chapters 2, namely; PBE GGA functional, (Scalar Relativistic) ZORA, QZ4P Basis, and without symmetry constraints. Thus, before introducing clusters of binary CrTe, we first briefly introduce pure tellurium clusters, followed by discussion of chromium. Finally, address the newly obtained small clusters of chromium.

### 3.2.2 Tellurium Clusters

The inherent complexity needed for chromium cluster calculations can be easily transferred to those for pure tellurium, as well. Stable structures formed from elements of group-16 on the periodic table display transformations from diatomic species of oxygen, up through rings of sulfur, selenium chains, and tellurium helices, with an increase in strength of single bonds versus double.<sup>156,157</sup> Elements of this group are known to have two lone electrons; each the sole occupant of a non-bonding orbital. These orbitals are directional, and lie at the top of

the valence band, with divalent tendencies and a preference for twofold coordination. The behavior of these elements with regards to their orbital interactions, results in various groundstate geometries of ring and/or chain-like structures, which is exemplified by the small clusters of tellurium.<sup>158–163</sup>

Specific cluster isomers for  $Te_n n = 6$  were obtained by Igel-Mann *et al.* in 1993 under Hartree-Fock methods, and found changes in the ordering of these isomers after inclusion of correlation and configuration interactions.<sup>164</sup> Additionally, density functional calculations of Ten (n = 2 - 4) clusters completed by Goddard *et al.* in 1999 displayed a high dependence on the choice of basis-set used (more about this below) on the resultant structure and vibrational frequencies. But, in all instances, the isomers of Te<sub>3</sub> ( $C_{2\nu}$ ) and Te<sub>3</sub> ( $D_{3h}$ ) were found to be almost degenerate, and similarly for the isomers of Te<sub>4</sub> ( $C_{2\nu}$ ) and Te<sub>4</sub> ( $D_{2h}$ ).<sup>159,160</sup> Subsequent theoretical studies into geometries and frequencies by Pan in 2002, n = 2 - 8, was completed using three different types of xc-functionals to complete their calculations, in turn finding several isomers for n = 4 - 6.<sup>161</sup> This dependence on *xc*-functional was also accounted for in the work of Akola & Jones, while investigating amorphous tellurium and clusters  $n \leq 16$ . Using four different *xc*functionals, they showed the energy difference between two- and threefold coordination of tellurium atoms to be sensitive to the particular xc-functional used, as well.<sup>157</sup> We do not delve further into the nature of tellurium or its clusters, but the references mentioned here (and those therein) do provide sufficient introduction.<sup>165</sup>

### 3.2.3 A Brief History of Small Chromium Clusters

Chromium, for many years has been known to be an antiferromagnetic substance. However, even within large cluster systems, chromium behavior is very complex and has drawn a lot of interest. Thanks to the work of Payne *et al.*<sup>166</sup> just over a decade ago, they have measured the magnetic moments of free  $Cr_n$  clusters reaching over 100 atoms in size showing there are two different magnetic behaviors that develop as a function of size. This can be seen below in **Figure 3-1**, which for the clusters  $Cr_{30}$ , and  $Cr_{34} - Cr_{133}$  have two magnetically distinguishable isomers, hence the two plots. However, at the small scale, the antiferromagnetic character does not persist and on some occasions, leads to systems possessing a ferromagnetic high spin polarization.<sup>167,168</sup> It is this ferromagnetism that is to be harnessed and maintained into the macroscopic regime. But, obtaining systems of this type can be difficult, due to the tendency of transition metals with a nearly half-filled shell, i.e.  $Mn_n$  and  $Cr_n$ , to align in an antiparallel manner with the nearest neighbor.<sup>169</sup> Understanding these findings is still somewhat of a challenge, with many theoretical investigations having already been conducted to study magnetism as related to structure, and vice versa.<sup>170–174</sup>

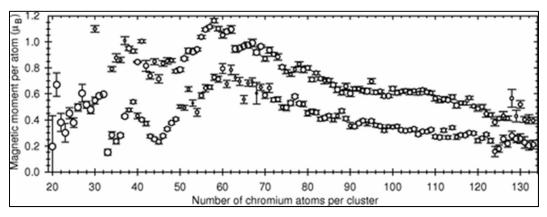


Figure 3-1. Magnetic moments per atom  $\mu$  for chromium clusters of N = 20 - 133. (Reused with permission, Copyright American Physical Society)<sup>166</sup>

At the smaller scale, it has been confirmed in experiments of solitary Cr that it possesses a groundstate of  ${}^{7}S_{3}$ , in a  $3d^{5}4s^{1}$  configuration.<sup>175–177</sup> A configuration found similarly within the present study. Additionally, in the investigation of chromium clusters, extensive attention has been placed upon that of Cr<sub>2</sub>, both theoretically and experimentally.<sup>171,178–185</sup> Across these studies it has been experimentally found that the groundstate is formed by two chromium atoms coupling antiferromagnetically. This bond is comprised entirely between the *s*- and *d*-orbitals, with length of 1.6788 Å; drastically shorter than found in bulk, 2.50 Å.<sup>172,186</sup> Ideally, with each Cr atom supplying six unpaired electrons, this should in principle produce a dimer with six bonds. Due to the size difference between the 4s and 3d orbitals, as well as the influence from exchange energy, this bond is very weak and has a low binding energy ( $1.53 \pm 0.05 \text{ eV}$ ).<sup>187,188</sup> Accordingly, it has been found through bond order analysis that the dimer has an effective bond order of 3.5, instead of the ideal six.<sup>189</sup> In this present investigation, the Cr<sub>2</sub> cluster has a calculated bond length of 1.71 Å, and dissociation energy of  $D_e = 0.735 \text{ eV}$ , both in fair agreement with experimental data.

The extensive studies into the electronic properties of Cr<sub>2</sub> have often been used as a benchmark when discussing the specific magnetic and bonding characteristics of larger, polyatomic chromium. This understanding of Cr<sub>2</sub> has lead Cheng & Wang in 1996 to propose a dimeric growth route for clusters up to Cr<sub>11</sub>, in an effort to explain the widely alternating spin multiplicities between even and odd numbered clusters, as well as antiferromagnetic ordering and structural transitions.<sup>172</sup> Later calculations at a higher level of theory by Wang *et al.*, in search of Cr<sub>n</sub> (n = 2 - 5) equilibrium geometries, have reported small chromium clusters are antiferromagnetically coupled, and found no dimer-growth route for clusters larger than n = 3.<sup>174,190</sup> This was confirmed later in 2010 by Ge *et al.*, reporting no dimeric-growth for metastable isomers of Cr<sub>n</sub> (n = 2 - 9), under the same, higher level, of theory.<sup>191</sup>

Clearly, as computational methods become more complex and encompassing, it is advantageous to determine, at these higher levels of theory, what exactly is the behavior of small chromium. This lack of complexity in formalism and/or availability of adequate orbital representation can be followed up into the present day, as told through previous literature reports. The wealth of information from these studies has yielded a multitude results that are extremely

diverse. Moreover, some of the claims made in regards to the electronic properties of small chromium are drastically different from the experimental data, in regards to bond lengths and dissociation energies.

It is important to remember, and bears some emphasis, in the desire to create new materials with novel properties and use clusters to do so, calculation of fundamental properties must obviously be of the utmost of quality. Thus, choice of *xc*-functional and matching basis-set are the two main variables for these calculations. Within this study, the choice of PBE functional was based upon its history of successful usage in predicting and verifying both properties and structure of various clusters, as well as periodic solids and CAMs. Moreover, the basis-set of QZ4P was chosen not only for its completeness in numerical representation and optimization for use with the ZORA formalism within ADF, but also as a type of benchmark. Performing these cluster optimizations in this manner serves as a useful reference for comparing past results, as well as future DFT calculations of this type. Specifically, those utilizing GGA or meta-GGA functionals and/or *Slater-type orbitals* (STO); despite the concentration of this investigation placed solely upon neutral species with collinear spins.

A modern investigation into the most suitable combination between the DFT functionals of GGA PBE and meta-GGA TPSS, and various basis sets was undertaken recently by López-Estrada *et al.* in 2016.<sup>192</sup> This was done in search for the best description to verify experimental findings regarding the properties of  $Cr_n$ , n = 1 - 4, and highlighted a  $Cr_4$  cluster with S = 6 spin state. Prior to this, a more comprehensive investigation into the most suitable functional and basis pairing was performed by Würdemann *et al.*<sup>193</sup> Within that study, a compendium of information derived from numerous basis set combinations with functionals from GGA and meta-GGA levels was undertaken in order to solidify the electronic properties of  $Cr_2$  and  $Cr_3$ , which is then compared with vast amounts of experimental data found in the literature. Furthermore, these newly found results are applied upwards toward larger sized chromium in an effort to put all calculated  $Cr_n$  data on the same footing.

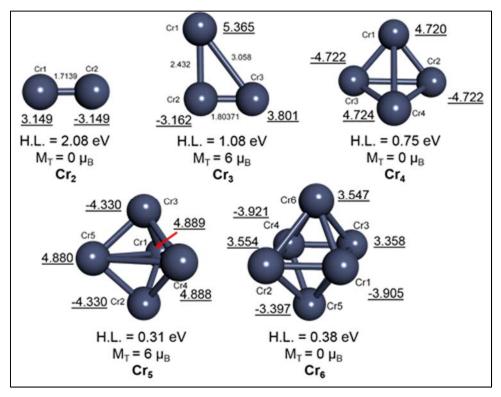
#### 3.2.4 Small Clusters of Pure Chromium

The groundstate structures of pure chromium clusters found in this study are shown below, in **Figure 3-2**, while their respective bond lengths and level diagrams are given in Appendix A. Interestingly enough, their total magnetic moments vary between 0 and 6  $\mu$ B, depending on even or odd number of Cr atoms, respectively. Macroscopic properties of the Cr<sub>2</sub> dimer have already been discussed above, and we shall save the remainder of its analysis until reaching the sections of Te addition.

Thus, we begin with the trimer which we can see below. Different possible geometries without symmetry constraints, and across several spin states were considered initially, but only the groundstate geometry is given below. The lowest energy geometry is in the septuplet spin state, M = 7. The local moment for each chromium is listed (negative = downward). The first isomer appearing at higher energy is the quintuplet, and at a difference in energy of ~0.46 eV. A competition between M = 5 and M = 7 groundstates has been seen before.<sup>192</sup> López-Estrada *et al.* have performed computations upon small chromium and have claimed their energy difference to be ~0.2 eV. Within that report, the authors have also deemed the cluster of M = 7 to be groundstate, based upon pervious experimental results.

With regards to geometry, the triangle formed below follows along the lines of previously reported geometries for the trimer, possessing a right triangle shape formed as a dimer plus adatom formation. The presence of a lengthened bond exists between Cr2 and Cr3 at 1.803 Å, and is slightly larger than other geometries whom report lengths closer to the original dimer

when using GGA functions. Together, this bond, along with the Cr2-Cr3 bond of 2.432 Å, form an angle at 91.19°.



**Figure 3-2.** Groundstate clusters of pure  $Cr_n$ , n = 1 - 6. With HOMO-LUMO gap, and magnetic moments for individual Cr, and total cluster ( $M_T$ ).

The chromium tetramer has been obtained from various initial geometries and spin states. The groundstate is a singlet, M = 1, with three atoms forming a right triangle base and the fourth atom bonding similarly to share the hypotenuse. From there, this structure remains as a distorted tetrahedron, as the fourth atom does not reach an apex above the remaining three. The resultant dihedral formed has angle of 113.24°. The bond distances between Cr1 and Cr4, & Cr2 and Cr3 are ~3.01 Å, while the remaining bonds are ~2.35 Å. In this arrangement, the chromium atoms are antiferromagnetically arranged, with near equal charge density. The next geometry higher in energy can be found at ~0.60 eV away, however there is a competition between structures in the triplet spin state and that with higher multiplicity of M = 13; with the triplet state only ~24 meV lower in energy. This again has been reported on previously<sup>192</sup>, but in that publication the

position of the fourth Cr atom at the apex dose not yield any singlet spin state geometry and has brought the groundstate to a discussion between the triplet and M = 13 states. The competition between those two spin states has been attributed to their close geometries, which facilitates a spin-flip due to spin-orbit coupling.

Trends of this type, based on differences in energy, bond distances, and magnetic coupling continue upwards into the larger size of chromium. The pentamer of chromium begins to display a form of regularity with respect to bond distances. The triangle formed of Cr1, 4, and 5, have lengths of ~3.03 Å; with the remaining distances at ~2.40 Å. Apex atoms together are antiferro with respect to the central triangle, but sum total of spin moments results in a ferrimagnetic cluster with septuplet multiplicity. Additionally, the cluster of Cr<sub>6</sub> is highly distorted from an ideal tetragonal bipyramid structure with all bond distances lying within the range of 2.33 - 2.77 Å, with the shortest being found joining the four atoms of the center square. The distortion appears now to be a result of the individual moments of the atoms, and despite their differing magnitudes the overall cluster is in the singlet state. This is affirmed, as the next highest pair of geometries are ~0.33 eV higher in energy. Here, the two geometries in question are those with multiplicity of M = 9, and M = 11. Both geometries are highly similar in structure, with only minute differences in bond lengths.

### 3.2.5 Summary

Together, all the clusters above are in reasonably good agreement with current, modern, literature reports and serve as suitable starting points for comparison with their tellurium paired variants. Using these new results, as well as our knowledge of elemental tellurium behavior from the prior discussions, we begin to address binary CrTe. Specifically, what we now lack is a concrete formulation detailing the transition of properties between the two; small clusters of

chromium, and those of tellurium, together. More importantly, how their overall magnetic and electronic behavior change when moving into the macroscopic scale. Moreover, despite the large magnetic moment of elemental chromium, and its small clusters, how and why does that magnetic moment enhance, stabilize, or diminish in the presence of tellurium. The apparent lack of any robust magnetism on a large scale regarding the  $Cr_6Te_8(PEt_3)_6$  cluster, and overall solid itself as shown in experiment, can be traced back to these small cluster sizes of binary Cr/Te, and shall be addressed in the next section.

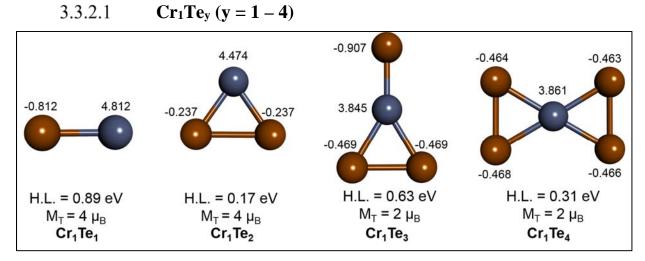
# 3.3 The Cr<sub>x</sub>Te<sub>y</sub> Clusters

#### 3.3.1 Overview

We further divide the remainder of this chapter effectively into three parts. The first, discusses the clusters, their structures, bond distances, etc. Within the second, overall properties pertaining to the entire series. Electronic properties such as HOMO-LUMO Gap, trends of the individual bond distances, magnetism, Hirshfeld Charge analysis, and removal energies. Lastly, the bonding patterns between chromium and surrounding tellurium, as seen through levels diagrams, the density of states, and Mulliken spin density movement. All cluster geometries can be seen below in **Figure 3-3** through **Figure 3-9**, with labels and associated labels bond lengths in Appendix B.

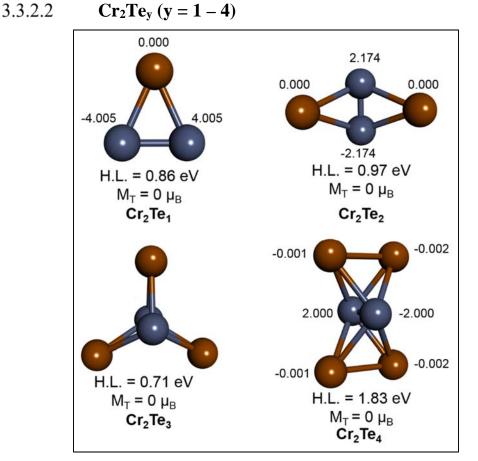
It should be noted, that although there are numerous interpretations and results for small chromium geometries and associated isomers, that number pales in comparison to those of small CrTe. For each groundstate shown below, there are numerous higher energy isomers within 1.00 eV. One can deduce, this number grows even larger depending on the total number of Cr and Te atoms within a cluster. For example, smaller CrTe systems have approximately five higher energy isomers; while the larger can have upwards of eight or more. For the groundstate and low-lying isomers, full convergence was guaranteed through frequency analysis. After such analysis, any geometry displaying a frequency which is negative, in any vibrational mode, would subsequently be reoptimized under a tighter geometry convergence criterion; 10<sup>-5</sup> eV, rather than the standard, 10<sup>-3</sup>. Tests involving geometry optimizations incorporating both a tighter convergence criterion and integration grid (ADF 2016.104: "verygood" vs "good") have shown the modified geometry criterion (10<sup>-5</sup>) to be sufficient when used alone.

### 3.3.2 Geometries & Structure



**Figure 3-3.** Groundstate structures of Cr<sub>1</sub>Te<sub>1-4</sub>. With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment, M<sub>T</sub>. (Cr:Blue; Te:Beige)

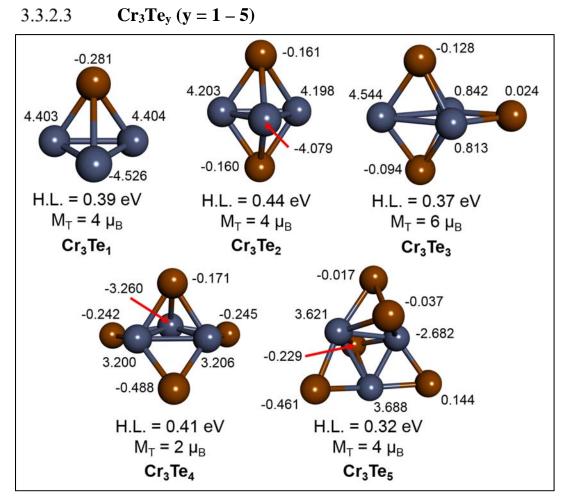
Ascertaining the effect of bonded tellurium is best understood through its imposition upon the free atom and dimer of chromium. The groundstate geometries for Cr<sub>1</sub>Te<sub>1-4</sub> are shown in **Figure 3-3**, accompanied by their total magnetic moment, M<sub>T</sub>, as well as individual spin moment contributions from chromium and tellurium. What can be seen immediately is the systematic decline of spin density of the central chromium atom, and the fall of the total moment. The bond length within Cr<sub>1</sub>Te<sub>1</sub> is 2.453 Å. The closest geometry higher in energy to CrTe is in the septuplet state, at a difference of 0.55 eV. For CrTe<sub>2</sub>, the two tellurium atoms bonded to solitary Cr form an isosceles triangle with a bond length of 2.874 Å between the tellurium. As the number of Te atoms increase, we can see they take on something close to a square planar arrangement around Cr. Bond lengths now are ~2.62 Å between Cr and Te, and ~2.70 Å between the Te. The nearest geometry higher in energy to CrTe<sub>2</sub> is in the triplet state, and <60 meV away. Similarly, the first isomer of CrTe<sub>3</sub> is 0.17 eV higher and in the quintuplet state; while for CrTe<sub>4</sub>, the first isomer is ~0.13 eV higher, but still in the triplet state.



**Figure 3-4.** Groundstate structures of  $Cr_2Te_{1-4}$ . With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment,  $M_T$ . (Cr:Blue; Te:Beige)

Interesting geometrical effects can be seen on the dimer of chromium through the sequential addition of Te atoms in **Figure 3-4**. Firstly, all geometries are in the singlet state, with virtually no spin density in the Te atoms. Placing a single Te atom upon Cr<sub>2</sub> stretches the bond from 1.7138 Å to 2.102 Å, and this Te atom is now closer to both Cr atoms at a distance of 2.555 Å. A second Te atom reduces the Cr<sub>2</sub> bond back downward to 1.838 Å. Both Te atoms are in a butterfly position, out of plane in the dihedral, but each maintain bond lengths of 2.559 Å and 2.561 Å. A third Te atom in CrTe<sub>3</sub> now brings the Cr dimer to a bond length to 1.769 Å, and all Te atoms are in the range of 2.565 – 2.570 Å. More importantly, the spin moments on both Cr atoms are now completely quenched. Finally, a total of four Te atoms, in Cr<sub>2</sub>Te<sub>4</sub>, encircling the central Cr<sub>2</sub> leaves the metal bond at 1.792 Å, bonds between Cr and Te are now in the range

of 2.708 - 2.715 Å, with Te atoms forming two dimers, each with length of 2.781 Å. Here, the spin moments are antiferromagnetic to one another.



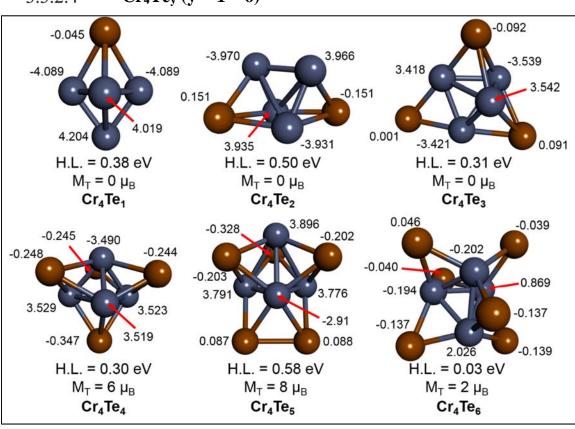
**Figure 3-5.** Groundstate structures of Cr<sub>3</sub>Te<sub>1-5</sub>. With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment, M<sub>T</sub>. (Cr:Blue; Te:Beige)

Groundstate geometries for the chromium trimer series can be seen in **Figure 3-5**. All structures possess a quintuplet multiplicity, with the exceptions of  $Cr_3Te_3$  (M = 7) and  $Cr_3Te_4$  (M = 3). The central  $Cr_3$  atoms remain in their isosceles formation throughout the series, with varying degrees of bond length, except for  $Cr_3Te_5$  when all Cr atoms are stretched to their furthest positions. Each central trimer takes on the behavior of the pure  $Cr_3$  structure, in that there remains one Cr with downward spin, excluding  $Cr_3Te_3$ .

A single Te atom atop Cr<sub>3</sub> effectively takes the position of the fourth Cr atom of the pure Cr<sub>4</sub> geometry. It resides 2.594 Å away from the spin-up Cr atoms, but 2.903 Å from the Cr of downward spin. The Cr bond distances are 2.921 Å between the spin-up chromium, and 2.312 Å between spin-up and spin-down chromium. The spin density of the lone Te atom reaches -0.281. Addition of two Te atoms to Cr<sub>3</sub> stretches the metal bonds only slightly, ~0.05 Å for each bond. However, each Te atoms is mirrored by its partner, both are a distance of ~2.66 Å from the spin-up Cr atoms, but ~2.72 Å from the spin-down. The two Te atoms are effectively balancing their distances across of all bond lengths.

The geometry of Cr<sub>3</sub>Te<sub>3</sub> can be best described as Cr<sub>2</sub>Te<sub>3</sub> with a third Cr atom attached. In adding this Cr, only one Te atom remains with two-coordination. Moreover, the triangle formed by Cr<sub>3</sub> becomes highly irregular. The two Cr atoms which are bonded to the total number of tellurium, compress their bond distance to 1.821 Å. These two Cr bond to the third with distances of 2.839 Å, and 2.846 Å, respectively. The two-coordinated Te atom forms bond distances of ~2.54 Å, while the remaining two Te atoms bond within the range of 2.652 Å – 2.678 Å. The spin density analysis shows that the entire system is a ferromagnet, with the majority of spins located upon the least coordinated Cr atom.

The Cr<sub>3</sub>Te<sub>4</sub> complex effectively rearranges itself to accommodate the increase in Te number. Only the Te atom forming the apex above Cr<sub>3</sub> forms three bonds, while the remaining three are two-coordinated on the edges. When compared to complexes of Cr<sub>3</sub>Te<sub>1</sub> and Cr<sub>3</sub>Te<sub>2</sub>, four Te atoms move the central Cr<sub>3</sub> complex closer to an equilateral triangle, with the least coordinated Cr atom forming the peak. This atom is 2.421 Å and 2.424 Å away from the remaining two Cr atoms, which are separated by a length of 2.829 Å. The Te atom bonded to both these Cr has spin-down density of 0.488, the maximum of all Te atoms across the Cr<sub>3</sub> series. Further addition of Te produces a complex with a Te-Te bond, Cr<sub>3</sub>Te<sub>5</sub>. The central Cr<sub>3</sub> has bonds of all different length, with the shortest located between the Cr atom that is spin-down and Cr atom that is least coordinated to Te, at 2.457 Å. Opposite this bond, between the spin-up Cr atoms, the length reaches 2.859 Å. The third is at length 2.604 Å. Once again, the lone two-coordinated Te atom bonded to two ferromagnetically coupled Cr atoms has the largest amount of spin density.



3.3.2.4  $Cr_4Te_v (y = 1 - 6)$ 

**Figure 3-6.** Groundstate structures of Cr<sub>4</sub>Te<sub>1-6</sub>. With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment, M<sub>T</sub>. (Cr:Blue; Te:Beige)

Geometries for the  $Cr_4Te_y$  (y = 1 - 6) series are found in above in **Figure 3-6**. For  $Cr_4Te_1$ , the first Te atom forms the second apex of the trigonal bipyramid, is bonded to both the spin-down Cr atoms at 2.74 Å, and forms the third bond at 2.640 Å. The system is in the singlet state. The pure  $Cr_4$  geometry has a larger average bond length between Cr atoms, thus lending

evidence to the idea of Te absorbing charge and manipulating the underlying chromium. Moreover, the local spin moments have diminished through the bonding of Te versus pure Cr<sub>4</sub>.

In Cr<sub>4</sub>Te<sub>2</sub> the two Te atoms are bonded in the furthest possible positions from one another, and heavily distorting the underlying Cr<sub>4</sub> pyramid. Despite only two Te atoms, the longest bonds between Cr atoms have reached lengths of  $\sim$ 3.01 Å, while the remainder fall in the range of 2.270 – 2.465 Å. The three-coordinated Te atoms bond onto their nearest Cr<sub>3</sub> triangle, and of the Cr atoms forming this triangle, only one is opposite in spin to the other two. The four Cr atoms are antiferromagnetically arranged, leaving the total cluster in the singlet state.

What is interesting to see, with regards to the spin moment localized on the Te atoms, as the cluster size grows the effect of the Te atom varies with this size, as well. This results in clusters that have Te atoms all in the spin down state, or a mixture of both up and down, depending on the total number and arrangement of those Te atoms. In Cr<sub>4</sub>Te<sub>2</sub>, we can see both Te atoms have the same amount of spin density, but in opposite directions. This continues into Cr<sub>4</sub>Te<sub>3</sub>, where the maximally coordinated Te atoms are equal and opposite, while the third possesses virtually no change in spin density.

The Cr<sub>4</sub>Te<sub>3</sub> geometry, as stated above, two Te atoms that are maximally coordinated and a third which is doubly so. The three-coordinated Te atoms have bond distances within 2.650 - 2.716 Å, and the two-coordinated bonds are of length 2.575 Å, each. The addition of a third Te atom has diminished the effective spin moments on all Cr atoms, but the system remains in the singlet state. The overall geometry of the Cr<sub>4</sub> structure is now less distorted than that of Cr<sub>4</sub>Te<sub>2</sub>, but bond distances remain elongated, ranging between 2.238 - 2.748 Å.

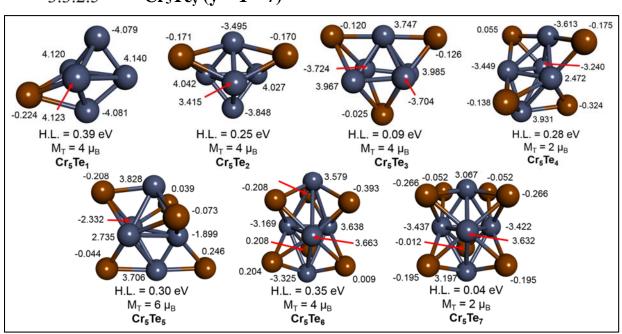
The structure of Cr<sub>4</sub>Te<sub>4</sub> marks the beginning of a rise in the total magnetic moment of the Cr<sub>4</sub> series. The triangle formed by the spin-up Cr atoms can be considered equilateral, with

distances 2.847 – 2.852 Å. The apex, spin-down, Cr atom bonds effectively equally, in the range 2.449 – 2.458 Å. Moreover, all Te atoms are now maximally coordinated, with the Te atom bonded to the spin-up Cr<sub>3</sub> triangle possessing the maximum amount of downward spin density. Contrary to Cr<sub>4</sub>Te<sub>2</sub> and Cr<sub>4</sub>Te<sub>3</sub>, all Te atoms herein have spin-down (negative spin) density. Together, the Cr atoms are ferrimagnetic, producing a system in the septuplet state. What is interesting within this particular size of clusters is the Cr<sub>4</sub>Te<sub>4</sub> groundstate, and up to the fifth highest isomer, is all Cr atoms form a tetrahedron with the Te atoms on the faces. The major difference between them are the bond lengths between the Cr atoms, creating isomers that are +0.08 eV, +0.16 eV, +0.38 eV, and +0.39 eV, with total magnetic moments of 0  $\mu$ B, 8  $\mu$ B, 2  $\mu$ B, and 4  $\mu$ B, respectively.

This magnetization further increases in the groundstate system of Cr<sub>4</sub>Te<sub>5</sub>. The fifth Te atom bonds to two Cr atom sites, and effectively moves the fourth into the same position opposite itself. Together, forming a Te-Te bond at 2.809 Å. This has had a negative effect upon the Cr-Cr bonds. The Cr<sub>3</sub> base triangle has two shortened bonds at ~2.35 Å, and although two Cr atoms have increased in spin density the third has fallen drastically and flipped downward, -2.91. The distortion of the system has increased the spin density, and changed the direction, of the apex Cr atom. As a result, the total system now has multiplicity of M = 9. The next geometry is 0.31 eV higher in energy, and in the septuplet state.

Following this, the Cr<sub>4</sub>Te<sub>6</sub> cluster system now loses this high magnetization, and is in the triplet state. From the figure, we can see that there is little area remaining for the Te atoms, and for each to be separated from one another all must bond in the two-coordination on the edges of the Cr<sub>4</sub> pyramid. As a result, large amounts of charge transfer between Te and Cr cannot occur, leaving all atoms with a diminished localized spin moment. Moreover, the Cr-Cr bond distances

have contracted, into the range of 2.277 - 2.575 Å, with the largest bond distance between the spin-up Cr atoms. The next geometry is 0.38 eV higher in energy, in the quintuplet state.



3.3.2.5  $Cr_5Te_v (y = 1 - 7)$ 

**Figure 3-7.** Groundstate structures of  $Cr_5Te_{1-7}$ . With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment,  $M_T$ . (Cr:Blue; Te:Beige)

Groundstates pertaining to the  $Cr_5Te_y$  (y = 1 - 7) series are shown in **Figure 3-7**. A glance over the entire figure shows the numerous contortions of the underlying  $Cr_5$  structure. For most, this structure remains as a trigonal bipyramid with the exception of  $Cr_5Te_3$  when it takes on the shape of tetragonal pyramid. Moreover, due to the larger number of bonding sites for Te, only within  $Cr_5Te_4$  and  $Cr_5Te_5$  does a two-coordinated Te atom appear. In all other geometries, Te atoms are three-coordinated, either with Cr, or both Cr and Te atoms. The  $Cr_5Te_5$  cluster also has the highest multiplicity of the entire series, at M = 7.

The  $Cr_5Te$  geometry displays a similar behavior to the pure  $Cr_5$  geometry, with three spin-up Cr atoms forming the center  $Cr_3$  substructure and two spin-down Cr atoms bonded on the opposing faces. Albeit, these moments are lower than found in pure  $Cr_5$ . The movement of spin density toward the adatom of Te contracts all Cr-Cr bonds, bringing average bond length down from 2.611 Å to 2.52 Å, while the three bonds of Te are 2.656 Å, 2.654 Å, and 2.787 Å. What is most interesting, is the spin-up Cr atoms form a near perfect equilateral triangle, at 2.839 Å, 2.831 Å, and 2.843 Å, respectively.

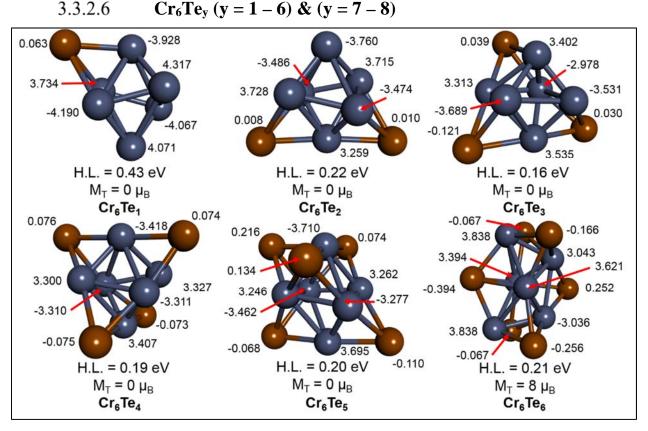
The geometry of  $Cr_5Te_2$  continues in the same manner as that of  $Cr_5Te_1$ , maintain the quintuplet multiplicity, and with the average bond distances between Cr atoms contracting further, to 2.49 Å, while Cr-Te bond distances persist. Here, the central Cr<sub>3</sub> substructure containing the spin-up chromium, forms its own equilateral triangle, at 2.750 Å, 2.753 Å, and 2.780 Å, respectively. With the remaining Cr atoms bonding at the apex's in the range of 2.299 – 2.448 Å. Both Te atoms are now equal in spin density, and spin down. The spin density of the Cr atoms occurs in pairs, with the exception of the fifth Cr which has spin density valued near the average per chromium. Addition of three Te to Crs subsequently breaks one of the Cr-Cr bonds, and produces a cluster whose center region is effectively open, and exposed. This is done by Te to obtain a coordination of three. Subsequently, Cr average bond distances are now enlarging, and equal that of CrsTe1. Moreover, the Cr4 center effectively forms a rectangle that has been elongated in the direction of the apex bonded Te atoms. A feature producing two antiferromagnetically coupled dimers held together by an apex Cr, and equally spaced perimeter of Te.

The presence of four Te atoms produces a cluster geometry with one of the smallest multiplicities of the  $Cr_5$  series, M = 3. In an effort to maintain their distance from one another, there are equal number of Te atoms in the two- and three-coordinated patterns. As a result, spin density uptake by the surrounding Te is uneven and incomplete. This then produces an arrangement where the Cr atoms involved in three-coordinated Te bonding elongate their

distance from the Cr atoms of the two-coordinated. The maximum of such elongation, between lower apex and equatorial Cr atoms, has a bond length of 2.972 Å. Additionally, between equatorial and upper apex Cr, the maximum bond is 2.836 Å.

The situation seen in Cr<sub>5</sub>Te<sub>4</sub> reproduces itself within Cr<sub>5</sub>Te<sub>5</sub>, but to the opposite effect. The system is in the septuplet multiplicity, with majority spin density contribution from the apex Cr atoms. The bonding pattern of the surrounding Te atoms now increases the number of threecoordinated atoms to four, with the fifth in a two-coordinated scheme. This increase in Te count now brings the average Cr-Cr bond distance to 2.64 Å. We can also see the spin density of individual Te are occurring in near antiferromagnetic pairings.

It is not until reaching  $Cr_5Te_6$  in which all Te atoms bond in the three-coordinate scheme, occupying all the faces. This produces a central  $Cr_3$  triangle with bond distances on average to those seen previously, but apex Cr bond distances in the range of 3.016 - 3.296 Å. These large bond distances further support the notion that the Cr-Cr interactions are managed through the bonded Te. Upon arriving at the structure for  $Cr_5Te_7$ , in the triplet multiplicity, it can be seen that the additional Te atom must form its third bond with the neighboring Te. In doing so, breaks the symmetry of the cluster. Once completed, each Te atom, with the exception of one, has a partner with equal spin density. The redistribution of charge has now allowed the structure to compress along the z-axis, bringing the apex Cr atoms closer to the center. This results in an average Cr-Cr bond distance of 2.75 Å.

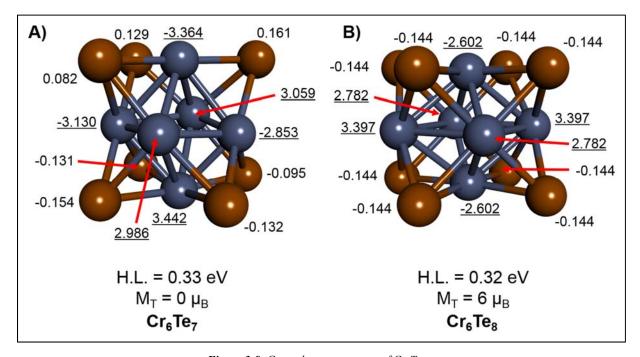


**Figure 3-8.** Groundstate structures of Cr<sub>6</sub>Te<sub>1-6</sub>. With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment, M<sub>T</sub>. (Cr:Blue; Te:Beige)

The series of  $Cr_6Te_y$ , y = 1 - 6 above in **Figure 3-8**, takes on a similar tone with regards to structural deformation and spin density through the increase of Te atoms, as we have seen above in smaller geometries. The major difference here is the tetragonal bipyramid structure persists, resulting in antiferromagnetic clusters in the singlet state. The exception to this occurs in the system of  $Cr_6Te_6$ , when the center  $Cr_4$  subunit contracts and bonds. This then allows an increased number of Cr atoms to ferromagnetically couple, and produce a geometry with M = 9 multiplicity. The likelihood of such a geometry to maintain itself in this high magnetic state is very small, the next geometry is <0.14 eV higher in energy, is in the singlet state, and has the tetragonal bipyramid form.

It is easier to see within this series, that the Te atoms are sharing and balancing their effect upon the Cr structure. This can be seen plainly within the geometry of Cr<sub>6</sub>Te<sub>4</sub>, in which all

spin densities are nearly equal and divided between spin-up and spin-down. Moreover, their overall effect is now maximized, as each Te atom is able to bond with its preferred bonding site on the face formed by three Cr atom, due to the fact that a compact geometry for Cr<sub>6</sub> is now less likely. The result, there is an alteration between odd and even numbered of Te atoms in the average bond lengths of Cr which continues into larger numbers of Te. However, after Cr<sub>6</sub>Te<sub>4</sub> this average bond distance never falls again below 2.55 Å; Cr<sub>6</sub>Te<sub>4</sub>, 2.552 Å; Cr<sub>6</sub>Te<sub>5</sub>, 2.637 Å; Cr<sub>6</sub>Te<sub>6</sub>, 2.717 Å; Cr<sub>6</sub>Te<sub>7</sub>, 2.678 Å; Cr<sub>6</sub>Te<sub>8</sub>, 2.783 Å.



**Figure 3-9.** Groundstate structures of  $Cr_6Te_{7,8}$ . Te = 7 (A), 8 (B). With HOMO-LUMO gap, individual Mulliken Spin Density, and total magnetic moment,  $M_T$ . (Cr:Blue; Te:Beige)

Above in **Figure 3-9**, we find the structures for  $Cr_6Te_7$  (**A**) and  $Cr_6Te_8$  (**B**). We can clearly see that the necessity for the  $Cr_6$  geometry to maintain its high multiplicity rests not only upon the distance between the individual Cr atoms, but also on a form of symmetry in the structure itself. The addition of another Te atom to  $Cr_6Te_7$  rearranges the overall spin density, forming a  $Cr_6$  structure comprised of four spin-up Cr atoms in the center, capped by two spin-

down Cr atoms in the apex positions. Moreover, the spin density of all Te atoms within Cr<sub>6</sub>Te<sub>8</sub> are equal and in the spin-down configuration.

Higher energy isomers for  $Cr_6Te_7$  begin at a difference of only 0.03 eV, and is in the quintuplet state. This very small distance between ground and first isomer highlights the ease in which the chromium complex can distort to remove any kind of electronic frustration from the overall system. The second isomer is 0.08 eV higher in energy (0.11 eV higher than ground), with triplet multiplicity. There is a marked increase in stability in the  $Cr_6Te_8$  cluster due to the extra Te atom. The first isomer is 0.07 eV higher in energy, and in a higher magnetic state of M = 9. Again, due to the cooperative effects of all Te atoms balanced across the entire cluster, an even number in this arrangement would better restrict movement of the Cr atoms.

#### 3.3.3 Summary

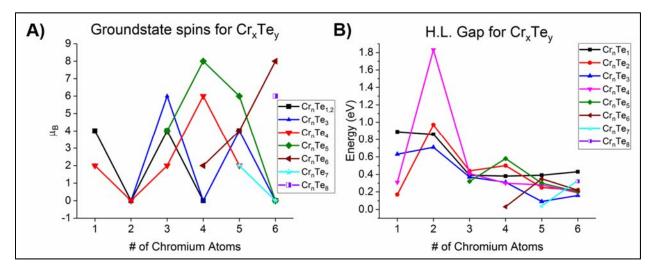
Upon closer examination of all geometries above, we can see that the behavior of pure chromium persists until a small number of Te are bonded. Moreover, this number changes depending on the size of the Cr cluster. With this now made obvious, the effect of said Te atoms can be varied to view a host of changes upon the underlying Cr complex. In pure chromium clusters, after complexation, to effectively reduce the distance between two Cr atoms back toward its free Cr<sub>2</sub> bond length, one must remove all electronic effects which drive the two atoms apart. This is rather difficult to do, and as the total number of Cr atoms increase, so do the number of *d*-orbitals and their degeneracies. Thus, introducing atoms of Te, the two incoming lone-pair orbitals in  $5p^4$  covalently bond to Cr (*d*) and in doing so can effectively weaken, or remove, the local spin moment on the Cr atom. Such a scheme is made apparent within the Cr<sub>2</sub>Te<sub>3</sub> cluster, and broken in the Cr<sub>2</sub>Te<sub>4</sub> geometry. The modification of spin density and

bonding lead the rearrangement of an already weakly bound chromium atoms into vastly different geometric shapes, seen in the above.

As the number of chromium atoms increase, the role of tellurium changes as well. Not only does it continue withdrawing charge from Cr, but also begins to play a key role in stabilizing the overall structure. The removal of charge from Cr drives their bond distances upwards, and becomes reliant upon the nearby Te atoms to balance the overall structure. With that process complete, Cr can now take on different arrangements in spin. The sensitivity of the underlying Cr system to the decorated Te various at all scales, and these overall properties are something we discuss in the next section.

# 3.4 Cr<sub>x</sub>Te<sub>y</sub> Series Properties

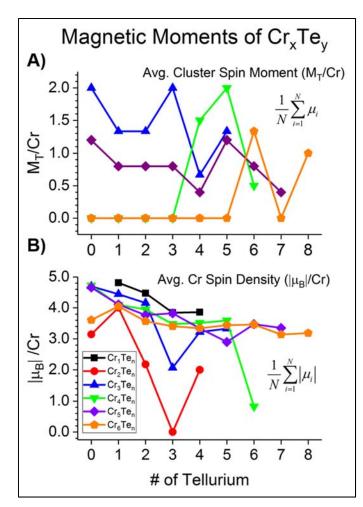
An overview of electronic properties for the entirety of the  $Cr_xTe_y$  series can be best summarized using **Figure 3-10**, and **Figure 3-11**. At first glance, we can immediately see special characteristics and traits in numerous Cr/Te combinations and sizes. Specifically, beginning with their total magnetic moments of **Figure 3-10** (**A**), moving left-to-right, that the overall magnetic moments mimic those of bare chromium clusters, in their alteration between high and no magnetization.<sup>166,169,194,195</sup> However, this pattern is broken, and magnetization appears to even be enhanced, beginning with clusters comprised of equal, or greater, number chromium vs. tellurium atoms. The clusters of  $Cr_3Te_3$ ,  $Cr_4Te_4$ , and  $Cr_5Te_5$ , each display a total magnetic moment, M<sub>T</sub>, of 6 µ<sub>B</sub>; as well as the  $Cr_6Te_8$  cluster core of  $Cr_6Te_8$ (PEt<sub>3</sub>)<sub>6</sub>, discussed later. This moment continues to increase within the clusters of  $Cr_4Te_5$  and  $Cr_6Te_6$ , whose M<sub>T</sub> both equal 8 µ<sub>B</sub>.



*Figure 3-10.* Basic properties of the Cr<sub>x</sub>Te<sub>y</sub> binary clusters. (A) Total magnetic moments, and (B) Distance between Highest Occupied Molecular Orbital (HOMO) and Lowest Unoccupied Molecular Orbital (LUMO), i.e. the HOMO-LUMO Gap.

The large magnetic moments are expected within odd numbered chromium, as often with those of the even numbered the magnetic moments of individual chromium atoms are

antiferromagnetically couple to one another, yielding an overall moment of  $0 \mu_B$ . However, this scheme no longer holds within (44) or (66), something we shall discuss in Secs. 3.5.4 and 3.5.6. Another interesting discovery is that of the HOMO-LUMO gap energies for the Cr/Te series, shown in **Figure 3-10 (B)**. Specifically, for that of the chromium dimer which is enhanced from solitary chromium, when decorated with two or more atoms of tellurium.



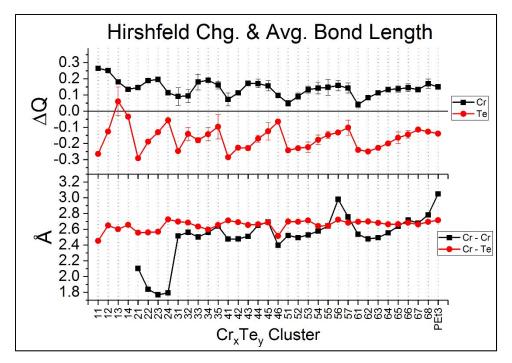
*Figure 3-11. Magnetic moments for the* Cr<sub>x</sub>Te<sub>y</sub> *cluster series.* 

Averages tabulated under two different schemes; Total cluster moment divided by number of Cr atoms (A), and summed absolute value of individual Cr atoms by different schemes. (Insets show equation used: N, total number of Cr;  $\mu_i$ , local spin of the  $i^{th}$  Cr)

In an effort to link the results presented to those of previous theoretical and experimental investigations, magnetic moments are presented in two different forms within **Figure 3-11**. Panel (**A**) highlights the total magnetic moment of a particular cluster, M<sub>T</sub>, as divided over the total number of Cr atoms present. In (**B**), to fully understand the sequential addition of tellurium upon the individual chromium atoms within a cluster, the same procedure of panel (**A**) is carried out using the absolute value of each individual Cr atom. Together, provide a better overall picture as to the electronic and magnetic behavior. Panel (**A**) highlights our discussion of the previous sections, in that major changes to the total magnetic moment are not likely to occur until there are equal or greater number of Te atoms when counted against the number of Cr, and similarly for the conservation, creation, or enhancement of any magnetic moment within a cluster. Within panel (**B**), each individual chromium appears to maintain a large magnetic moment, with the exception of a few cluster species; namely, Cr<sub>2</sub>Te<sub>3</sub>, Cr<sub>3</sub>Te<sub>3</sub>, and Cr<sub>4</sub>Te<sub>6</sub>. Moreover, clusters with a very high magnetization are void of any symmetry and whose total magnetic moments are closely linked with arrangement of tellurium around chromium.

## 3.4.1 Hirshfeld Charge Density, Average Bond Distances, and "Malleability" of Chromium

The idea that individual tellurium decorates chromium and affects the underlying metal system can be further illustrated in **Figure 3-12**, below. Atop shows the effective average Hirshfeld Charge density change, for both chromium (black) and tellurium (red), within each cluster combination. Additionally, the bottom portion shows the average bond distances between chromium's and chromium-tellurium.



**Figure 3-12.** Hirshfeld Charge Deviation and Bond Distance Averages. Deviations for individual chromium and tellurium atoms (top), average Cr—Cr and Cr—Te distances (bottom); for  $Cr_1Te_1 - Cr_6Te_8$ ,  $Cr_6Te_8$ (PEt<sub>3</sub>)<sub>6</sub>. (First number:x, Second:y)

We can see, in all clusters, that chromium is losing charge to tellurium, with the exception of CrTe<sub>3</sub>. Specifically, the amount of charge density possessed by a free, solitary chromium atom is larger when compared to that amount found upon a chromium atom within its associated cluster complex. Thus, chromium bonded with tellurium results in a positive change to its Hirshfeld charge density; and, vice versa for tellurium. Additionally, and most notably, the effect of tellurium removing charge from chromium is balanced across all the tellurium present within the complex itself. This can readily be seen by choosing any number of chromium, and sequentially adding tellurium atoms. In doing so, produces a graph of the saw-tooth variety.

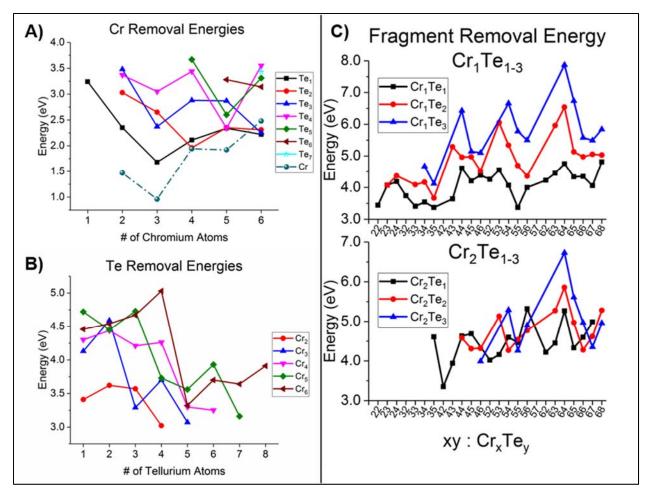
This charge balancing and movement has also a noticeable effect upon the bond distances within each cluster. Across the entire series, bond distances between Cr and Te deviated only minutely after  $Cr_3Te_x$ , with the exception of  $Cr_4Te_6$ . However, this is the opposite case for Cr - Cr bond distances, and especially so when discussing  $Cr_1Te_1 - Cr_2Te_4$ . If we call from above,

from experimental studies, is has been proven that the  $Cr_2$  dimer has an equilibrium bond length of ~1.678 Å.<sup>185,186</sup> Additionally, and despite this close bond distance,  $Cr_2$  has a dissociation energy of 0.72 eV/atom.<sup>196</sup>

Previous experiments have shown Cr<sub>2</sub> to possess a potential energy surface with an unusual shape (see, for example, Figure 1 of *Bauschlicher*<sup>171</sup>), with a broad shoulder on its outerwall.<sup>185</sup> Subsequent calculations have proven that this outer wall portion corresponds to 4s orbitals bonding with the 3d electrons on each center; while the inner portion to be the region corresponding to 3d orbital bonding.<sup>170,187,197</sup> The energy difference between these two regions is on the order of ~0.4 eV. Thus, one can expect that unless the 4s and 3d are both participating in a bond or bonding pattern, the distance between the chromium atoms will be significantly greater than 1.678 Å. It is precisely this scheme and mechanism behind the widely different properties, seen above, for the C<sub>2</sub>Te<sub>x</sub> series, which we shall discuss below, in Sec. 3.5.3. Similarly, due to the weak bonding nature inherent between chromium sond lengths and on some occasions, is driven even further due to the increased number of tellurium.

#### 3.4.2 **Removal Energies & Fragmentation Pathways**

Alluding to our discussion of weakly bonding chromium, there is however an increase in stability of the overall cluster system due an increasing Te number, with the slight exception of the Cr<sub>6</sub>Te<sub>x</sub> series, readily seen in **Figure 3-13** (**A**). At first glance, the increasing Cr removal energies appears to occur in a regular fashion for clusters of  $Cr_n n = 2 - 4$  clusters when compared to those of n = 5 & 6. Upon closer inspection, this is not the case for any number of Cr atoms. However, the most stable complexes are those with an even number of Cr. Specifically, Cr<sub>2</sub>Te<sub>3</sub> & Cr<sub>2</sub>Te<sub>4</sub>, Cr<sub>4</sub>Te<sub>4</sub> & Cr<sub>4</sub>Te<sub>5</sub>, and Cr<sub>6</sub>Te<sub>x</sub> (x = 4 - 7).



*Figure 3-13. Removal Energies for solitary, and complexed, Chromium and Tellurium. Solitary chromium (A), and tellurium (B). Fragmentation energies of Cr/Te complexes at various sizes (C).* 

The bonding of one Te atom effectively smooths the graph of removal energy versus that of pure Cr, and raises this energy for all clusters with the exception of Cr<sub>6</sub>Te. A second Te atom raises this bond energy within Cr<sub>6</sub>Te, but not to the level of the pure case. Adding another Te has virtually no effect upon Cr<sub>5</sub>Te, and actually reduces the effective bond energy for Cr<sub>4</sub>Te<sub>2</sub> back to that of pure Cr<sub>4</sub>. Increasing the number of Te atoms however does further stabilize Cr<sub>2</sub>Te and Cr<sub>3</sub>Te clusters by approximately 0.65 eV and 1.00 eV, respectively. Comparing this increased stability with the figure of average bond lengths, **Figure 3-12**, we can see that through sequential addition of Te to the Cr<sub>2</sub>Te<sub>x</sub> series, the Cr – Cr bond is becoming shorter and approaches approximately the same value for that of pure Cr<sub>2</sub>. With the exception of Cr<sub>3</sub>Te<sub>3</sub> and Cr<sub>6</sub>Te<sub>3</sub>, the presence of three Te atoms raises the stability of pure Cr clusters even further. Cr<sub>3</sub>Te<sub>2</sub> is weakened, versus Cr<sub>3</sub>Te<sub>3</sub>, through the addition of Te by ~ 0.28 eV. Continuing this process, the clusters of Cr<sub>3</sub>Te<sub>y</sub>, Cr<sub>6</sub>Te<sub>y</sub> all reach a maximum in their respective series when y = 4. While within Cr<sub>4</sub>Te<sub>y</sub>, for y = 4, this cluster reaches nearly 3.50 eV in removal energy, and then proceeds to increase that number for y = 5.

Of course, the increase in decoration of bare chromium with tellurium does raise its overall stability. However, this stability is only maximized when each Cr series reaches a certain number of Te atoms. Moreover, in achieving this stability, across the entire series of  $Cr_xTe_y$ , there is first a point within each cluster where its overall stability falls before increasing again. For example, the  $Cr_2$  series reaches a maximum at  $Cr_2Te_3$ , which is then diminished through addition of another Te atom. Similarly, in the  $Cr_3$  series as mentioned above, and  $Cr_3Te_3$  is less stable than  $Cr_3Te_2$ . But, neither are as stable when compared to  $Cr_3Te_4$ . Within  $Cr_4$ , its stability immediately begins an upward increase after  $Cr_4Te_2$ .

This sequence becomes obvious when discussing  $Cr_5Te_y$  and  $Cr_6Te_y$ . For  $Cr_5Te_y$ , there is virtually no change in energy between y = 1 - 2, 4. However, a spike in stability appears for y = 3, and removal energy continues upwards for y = 5, 6. In the  $Cr_6Te_y$  case, after y = 1, energy remains at approximately 2.30 eV. Not until y = 4, when this series reaches its maximum, does the  $Cr_6$  series raise this energy into the region of 3.00 - 3.50 eV, for y = 4 - 7. Moreover, within both of these  $Cr_6Te_y$  subseries, the apparent rise-and-fall of the energy value occurs within each of them, thus effectively twice for the entire  $Cr_6Te_y$  series. We can see from the figure, for y = 1 - 3,  $Cr_6Te_2$  is a maximum, and again within y = 4 - 7,  $Cr_6Te_4$  is the dominant species. From careful analysis of Cr removal energies, it can be readily deduced that there is a delicate balance between the number of Cr and Te atoms. Thus, in sequentially adding Te, it has been found that

there is what can effectively be called a tipping point in stabilization within each of the pure Cr series.

In turning our attention to the Te removal energies of **Figure 3-13** (**B**), there is additional evidence highlighting the delicate stability within these clusters. What can immediately be seen is the scale of the graph itself, where all Te removal energies are above 3.0 eV. Moreover, the effective reduction of the Te removal energy within all clusters falls below 4.0 eV upon reaching y = 5. Most importantly, for many chromium sizes, after a certain number of tellurium have been added, their removal energies become lower than that for removing solitary tellurium from pure chromium clusters.

The sequence of events upon how these clusters all diminish below these thresholds occurs differently depending upon the exact number of Cr present. For Cr<sub>2</sub>, Te removal energy peaks at Cr<sub>2</sub>Te<sub>2</sub> and then falls for subsequent Te, but always remains within the window of 3.10 - 3.60 eV. This almost gentle illustration is again seen of the Cr<sub>4</sub> series, but is not maintained across the entire series. For y = 1 - 4, energies remain in the region of approximately 4.25 eV. However, upon addition of five tellurium's, this binding energy falls nearly an entire electronvolt downward to  $\sim 3.30 \text{ eV}$ . The drastic alteration of Te binding energy seen in the Cr<sub>4</sub> series marks only the beginning. Within the cluster series of Cr<sub>3</sub> and Cr<sub>5</sub>, stability of tellurium removal rises and falls on two occasions. For Cr<sub>3</sub>, stability is maximized with two and six Te atoms. While for Cr<sub>5</sub>, that number is three and six tellurium. The largest of tellurium removal energy occurs for C<sub>6</sub>Te<sub>4</sub>. Within this cluster, each tellurium forms three bonds upon one of the Cr<sub>6</sub> octahedron faces, in a staggered configuration.

These wildly varying binding energies, and across various numbers of tellurium, can be explained as a matter of the underlying geometry of the Cr atoms. Depending on that geometry,

the cluster can only accommodate a fixed number of Te on its surface. This is further made true due to the inherent behavior of Te to first form two bonds, using its two lone-pair orbitals, and in the case of Cr clusters, often followed by yet another bond, into three-coordination. Additionally, the apparent balancing across all Te atoms present in the charge removal from the central Cr cluster results in CrTe mixed clusters groundstates with Te atoms that are as far away from one another as possible. Exceptions to this are the clusters of Cr<sub>2</sub>Te<sub>2</sub>, Cr<sub>5</sub>Te<sub>2</sub>, and Cr<sub>6</sub>Te<sub>2</sub>, where electronic effects of the Cr cluster dictate that the second Te atom be bonded nearby to the first. We shall see below, clusters decorated with Te atoms that are two-coordinated, threecoordinated, as well as those with a mixture of both.

Continuing along these lines of cluster stability, we turn our attention to the fragment removal energies of **Figure 3-13** (**C**). Here, it can be seen the various possible avenues for a particular cluster to dissociate into two smaller complexes. In comparing upper and lower panels, a particular cluster is more likely to lose Te atoms when Te is also accompanied by a single Cr, shown in the upper panel (black line). With this in mind, the most stable clusters are those that possess the most aligned graph peaks. Specifically, the clusters of  $Cr_4Te_4$  and  $Cr_6Te_4$ . And, when looking to the discussion above with regards to individual atomization, are the two clusters which have the highest removal energies. In  $Cr_4Te_4$ , the Cr atoms are bonded in a compacted pyramid structure, with each Te atom forming three bonds on the faces, effectively protecting Cr4 from dissociation.

#### 3.4.3 Summary

Across all of the macroscopic properties discussed thus far for small clusters of CrTe, it has been shown that stability and magnetic properties are highly dependent on both numbers of atoms. Moreover, as we shall see below, these properties are closely linked and can be modified,

or supported, through their individual arrangements. The overall effect of introducing Te atoms onto pure Cr clusters is this, the Te pulls and modifies the nearby charge distribution of chromium by specifically bonding to the *d*-orbitals. As a result, it drives the expansion of the bond distance of those involved chromium's. This then allows the individual Cr atoms to maintain their large spin density, and produces binary clusters with higher overall magnetization than their pure cluster variants. What we shall see below, is this effect produced by additional tellurium has a very large and noticeable effect on the smaller clusters of chromium. This charge modification performed by tellurium continues upwards into the larger clusters, and further solidifies itself as both a key structural and electrical component.

# 3.5 Cr<sub>x</sub>Te<sub>y</sub> Electronic Properties

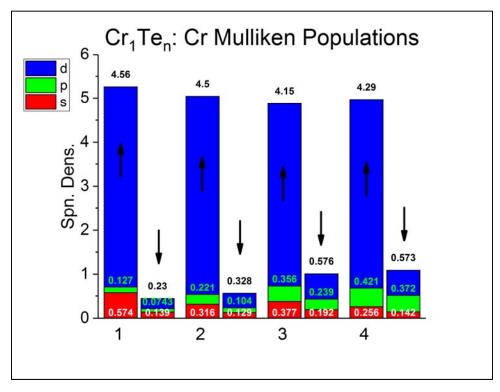
#### 3.5.1 Overview

The above results outlined the modification of chromium clusters through sequential addition of tellurium atoms. Moreover, until a cluster is decorated with a larger number of tellurium only minute effects will be witnessed. In witnessing such effects, we can directly view the contribution to the total magnetic moment through the alteration of each Cr atom, individually. Additionally, within each atom, we can view the change to the individual spin moment through the contributions and changes within each orbital. We do this by graphing the spin density of each cluster, with respect to each chromium, as calculated using Mulliken Population Analysis (MPA). Although MPA may not be the most suitable method for population analysis, it does serve as a very useful tool in ascertaining any changes and deviations from the ideal representation of the orbitals in question. And, because of our strict use of QZ4P in the search for groundstate geometries, we can be assured that the representation below captures any and all information, due to MPAs high dependence on the Basis Set. Because of such a large Basis Set is used throughout these calculations, it is expected that results obtained using other methods of population analysis based on the electronic density, namely that of Natural Population Analysis (NPA), should not deviate too far from those presented.<sup>198–204</sup>

For the graphs below, each chromium population has been normalized to valence. That is, in this representation, the sum of alpha and beta spin populations reaches a maximum of six electrons, representing the  $4s^{1}3d^{5}$  orbitals. With the  $3p^{6}$  orbitals of chromium taken to be part of the core electrons, any deviation from these maximums in the population density will be readily noticeable and traceable.

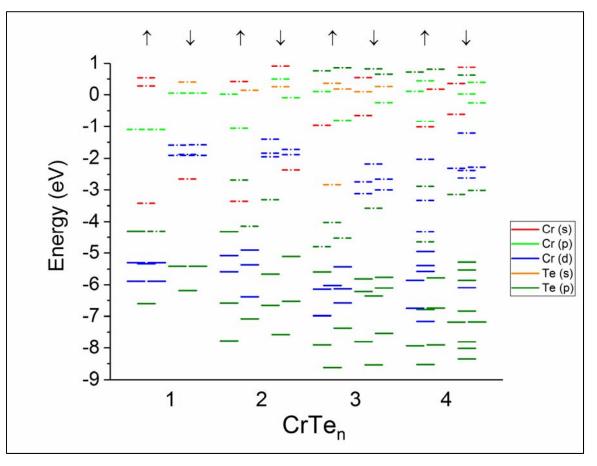
## 3.5.2 $Cr_1Te_y (y=1-4)$

The Mulliken populations for the  $Cr_1Te_{1-4}$  series are shown below in **Figure 3-14**. What can be seen immediately is the slow decline and leveling of the alpha spin channel and slow increase in the beta spin, of Cr (d). Additionally, the slow decline of Cr (s) and increase in the hybridization of Cr (p). The decline of population in Cr (s) can be attributed to its increased use in hybridization when the lone Cr atom is accommodating additional Te atoms. What is also evident, is the persistence of the Cr (d) orbital. This is due to the fact that, although tellurium does pull charge from chromium, it cannot do so alone. To that effect, the increase in beta channel population only manifests itself when there are four Te atoms present, creating a total of four Cr-Te bonds.



*Figure 3-14. Mulliken spin populations for Cr1Te1-4.* (For each n; Arrows mark direction of both spin channels for each Cr atom.)

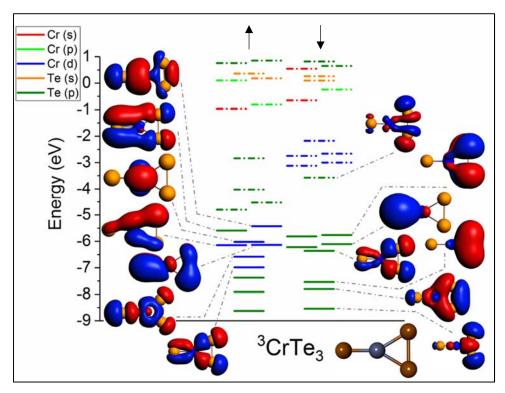
Furthermore, the atomic orbital level diagrams for the Cr<sub>1</sub> series can be found in **Figure 3-15**. Within it, we can see the splitting of the Cr (d) levels to varying degrees and across all sizes. The HOMO level of Cr1Te1 is formed by a degenerate, half-empty, Te (p) orbital, and is the reason for the overlap of HOMO and LUMO levels. The Cr (d) levels of HOMO-1 through HOMO-3 form bonds directly with two of the remaining Te (p) orbitals. A similar situation arises within the Cr1Te2 cluster, where the second Te atom splits the Cr (d) orbitals even further, and bonds to both Cr and Te. Subsequent addition of three Te atoms continues to drive downward the total number of Te (p) orbitals in both the alpha and beta spin channels. The central Cr atom is now flanked by a Te dimer on one side, and a lone Te on the other. The fourth Te atom effectively forms a bond with its neighbor Te and the central Cr, and whose orbitals are subsequently pushed further downward and increases the hybridization of the Cr atom.



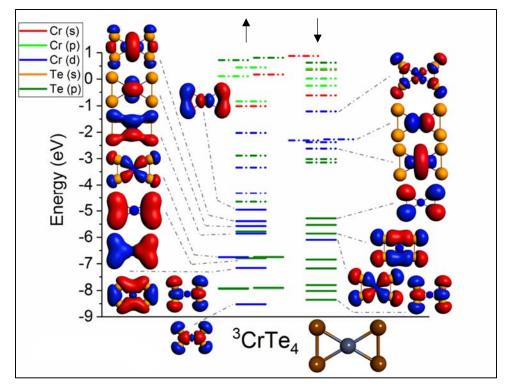
**Figure 3-15**. Level diagrams for  $CrTe_n$ , n = 1 - 4. Spin-up and Spin-down channels labelled with associated arrows

The atomic orbitals for CrTe<sub>3</sub> and CrTe<sub>4</sub> are further elaborated upon in Figure 3-16 and

**Figure 3-17**, respectively, as well as plots for their density of states (DOS) in **Figure 3-18**. Within both figures are the levels diagrams found within **Figure 3-15**, but now contain diagrams of the associated molecular orbitals (MO) for a selection of levels. Within **Figure 3-16** we can see that Te does not form the requisite number of bonds to fully quench the Cr atom, the HOMO-5 level is comprised solely of Cr  $dz^2$ . Bonds around the HOMO level and comprised of Te (p) and Cr (d) are antibonding. This continues within the structure of CrTe4, in **Figure 3-17**. For HOMO through HOMO-3, Cr (d) and Te (p) in the alpha spin channel are antibonding, while Te (p) in the beta channel are driven further downward in energy.



*Figure 3-16.* <sup>3</sup>*CrTe3 Atomic Orbital (AO) level diagram. Left column represents spin-up (alpha) channel. Right; spin-down (beta).* 



*Figure 3-17.* <sup>3</sup>*CrTe*<sup>4</sup> *Atomic Orbital (AO) level diagram. Left column represents spin-up (alpha) channel. Right; spin-down (beta).* 

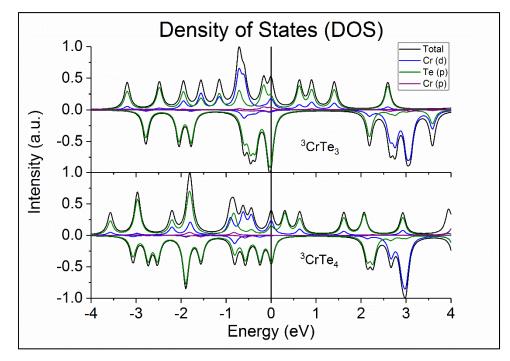
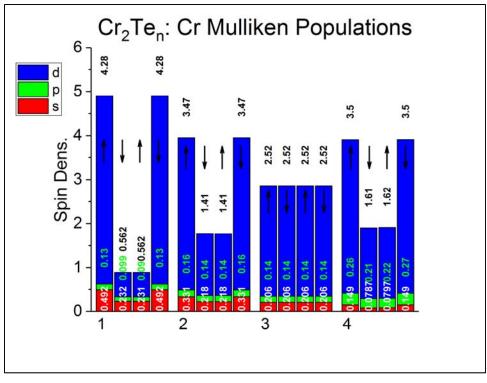


Figure 3-18. Density of States (DOS) for Cr<sub>1</sub>Te<sub>3,4</sub>.

### 3.5.3 $Cr_2Te_y (y = 1 - 4)$

The Mulliken spin populations for the  $Cr_2$  series is shown in **Figure 3-19**. Here we can watch a drastic change occur to the central  $Cr_2$  dimer with increasing number of Te atoms. Within  $Cr_2Te$ , we know from previously that the bond is stretched beyond equilibrium, thus the increase in spin density for each Cr atoms alpha and beta channel, respectively. Moreover, a there is still a quite sizeable amount of Cr (s) remaining on each atom, and virtually no Cr (p) involvement. The second Te atom bonds to Cr (d), driving both populations slightly downward, as well as those of Cr (s). It is the third Te atom which fully quenches the total spin density of  $Cr_2Te_3$ . The central  $Cr_2$  forms a total of two bonds between each Cr atom, while the remaining orbitals bond directly to the incoming Te (p) lone-pairs or are now diffused over the surface of the cluster. In adding the fourth Te atom, the spin density on both chromium atoms reemerges. The  $Cr_2$  dimer now forms three bonds between the two chromium atoms, leaving the incoming Te (p) orbitals bond and hybridize with the remaining orbitals and opening the HOMO-LUMO gap.



**Figure 3-19.** Mulliken spin populations for  $Cr_2Te_{1-4}$ . (For each n; Arrows mark direction of both spin channels for each Cr atom.)

All of the charge movement and bonding within the Cr<sub>2</sub>Te<sub>3</sub> and Cr<sub>2</sub>Te<sub>4</sub> cluster systems can be seen in the level and molecular orbital diagrams, as well as the density of states found in **Figure 3-20** through **Figure 3-23**, we can see the HOMO for Cr<sub>2</sub>Te<sub>3</sub> is highly delocalized and primarily comprised of Te lone-pair orbitals. Additionally, many orbitals are antibonding in nature, for both Cr<sub>2</sub>Te<sub>3</sub> and Cr<sub>2</sub>Te<sub>4</sub>. This is made clear in **Figure 3-21**, in which orbitals as far down as 1 eV below the HOMO are antibonding, and between Cr (d) and Te (p) orbitals specifically. This is confirmed in the plot of the Overlap Population Density of States (OPDOS), seen in **Figure 3-23**.

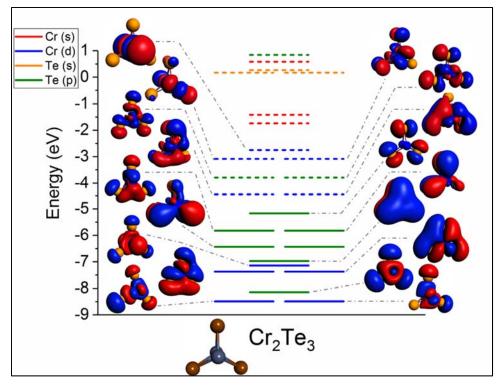
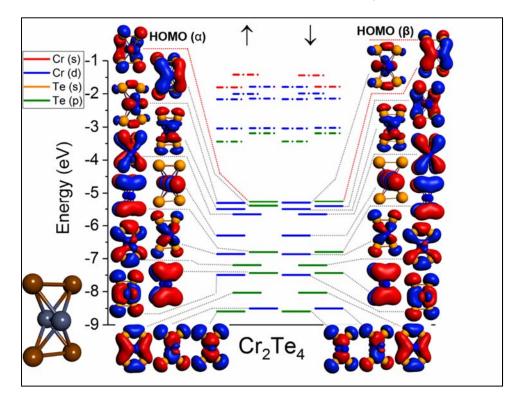


Figure 3-20. <sup>1</sup>Cr<sub>2</sub>Te<sub>3</sub> Atomic Orbital (AO) level diagram.



**Figure 3-21.** <sup>1</sup>Cr<sub>2</sub>Te<sub>4</sub> Atomic Orbital (AO) level diagram. Left column represents spin-up (alpha) channel. Right; spin-down (beta).

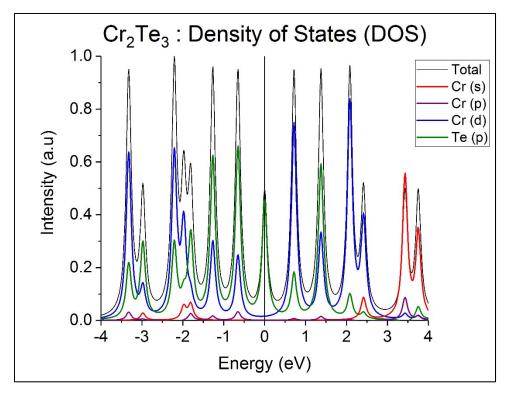
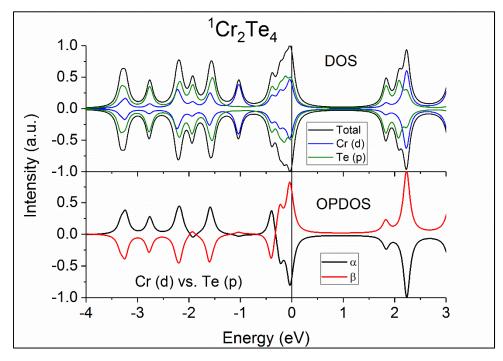


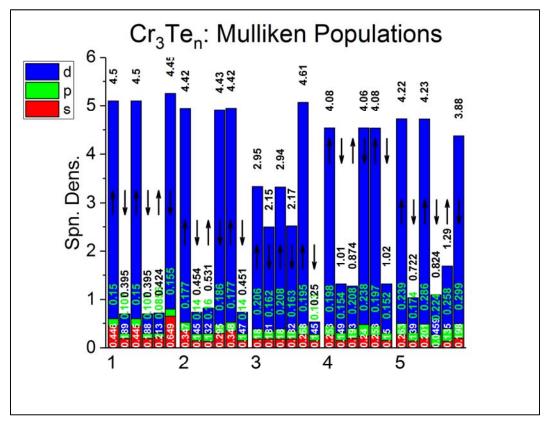
Figure 3-22. Density of States for Cr<sub>2</sub>Te<sub>3</sub>.



*Figure 3-23.* Density of States (DOS), and OPDOS for <sup>1</sup>Cr<sub>2</sub>Te<sub>4</sub>. (OPDOS: Overlap Population Density of States. Positive indicates bonding; Negative: antibonding. Beta inverted for clarity.)

## 3.5.4 $Cr_3Te_y (y = 1 - 5)$

In turning our attention to the Cr<sub>3</sub> series, the Mulliken populations are shown in **Figure 3-24**. The Cr<sub>3</sub> series marks the first that experiences fluctuations in the Cr-Cr bond distance due to excess Te atoms, but fluctuations that do not vary wildly as compared to the later Cr series. Sequential addition of Te atoms does not modify greatly the amount Cr (d) spin density, with the exception of Cr<sub>3</sub>Te<sub>3</sub>, until reaching Cr<sub>3</sub>Te<sub>5</sub>. The modification of the Cr (p) orbitals slowly increase through successive addition of Te, while the Cr (s) contribution decreases substantially.

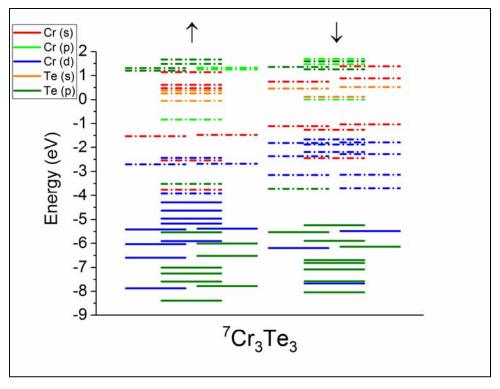


**Figure 3-24.** Mulliken spin populations for Cr<sub>3</sub>Te<sub>1-5</sub>. (For each n; Arrows mark direction of both spin channels for each Cr atom.)

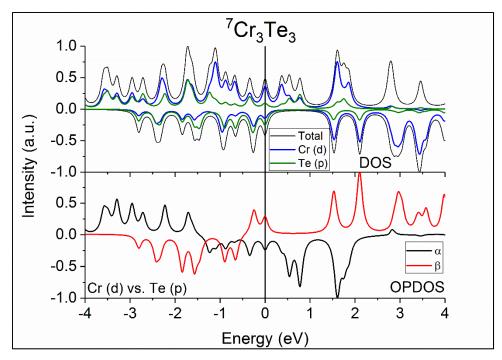
The total magnetic moment reaches a maximum in the cluster of  $Cr_3Te_3$ , which has the majority of its spin localized on the third Cr atom, seen in **Figure 3-24**. This structure is closely linked with that of  $Cr_2Te_3$ , where the third Cr atom bonds within one of that clusters open

regions. The third Cr atom introduces a change in the bonding pattern, away from the perfectly quenched Cr<sub>2</sub>Te<sub>3</sub>, and into a structure where all Cr atoms are spin-up.

Comparing the level diagram of  $Cr_2Te_3$  in **Figure 3-20**, with that of  $Cr_3Te_3$  in **Figure 3-25**, we can see that the alpha channel of  $Cr_3Te_3$  is becomes densely more populated due to the additional Cr (d) states, combined with a significant amount of shifting in the *s* and *p* levels. This addition and shifting can also be seen in the Density of States, between **Figure 3-22** and **Figure 3-26**. Of the Cr<sub>2</sub>Te<sub>3</sub> cluster, the region around the HOMO level is devoid of Cr (d) states, contrary to the HOMO region of Cr<sub>3</sub>Te<sub>3</sub>. This region within Cr<sub>3</sub>Te<sub>3</sub> is also antibonding in nature, and has expanded into the range of 1.5 eV below the HOMO level, as seen in the OPDOS of **Figure 3-26**, indicating very weak bonds.



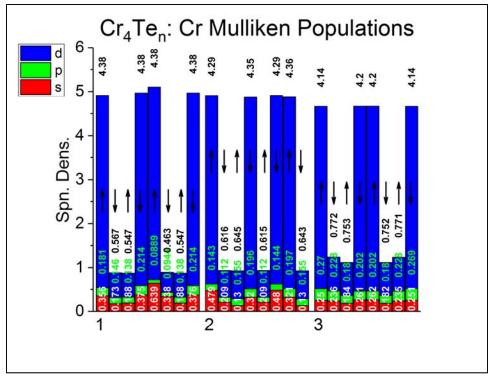
*Figure 3-25.* <sup>7</sup>*Cr*<sub>3</sub>*Te*<sub>3</sub> *Atomic Orbital (AO) level diagram. Left column represents spin-up (alpha) channel. Right; spin-down (beta).* 



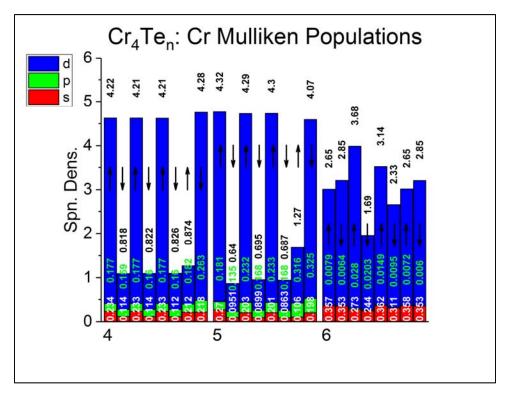
*Figure 3-26.* Density of States (DOS) & OPDOS for <sup>7</sup>Cr<sub>3</sub>Te<sub>3</sub>. (OPDOS: Overlap Population Density of States. Positive indicates bonding; Negative: antibonding. Beta inverted for clarity.)

# 3.5.5 $Cr_4Te_y (y = 1 - 6)$

As our chromium cluster grows larger, the overall effects of bonded Te on the Cr cluster become weaker and necessitates more Te to effect change. This is seen in the population densities of  $Cr_4Te_{1-3}$  and  $Cr_4Te_{4-6}$ , within **Figure 3-27** and **Figure 3-28**, respectively. The increase in Te atoms elongates the Cr-Cr bonds and reduces the presence of localized Cr (s) orbitals on the participating Cr atoms. This then allows the Cr (s) to further hybridize with the nearby orbitals. The only exception to this is that of  $Cr_4Te_6$ , which returns the Cr (s) orbitals back and then participate in the intermetallic bonding process. Moreover, what we now see is the total absence of the Cr *p*-orbitals. This is something that we must address now, and will further our discussion with regards to the choice of Basis Set and mainly the analysis method based upon it.



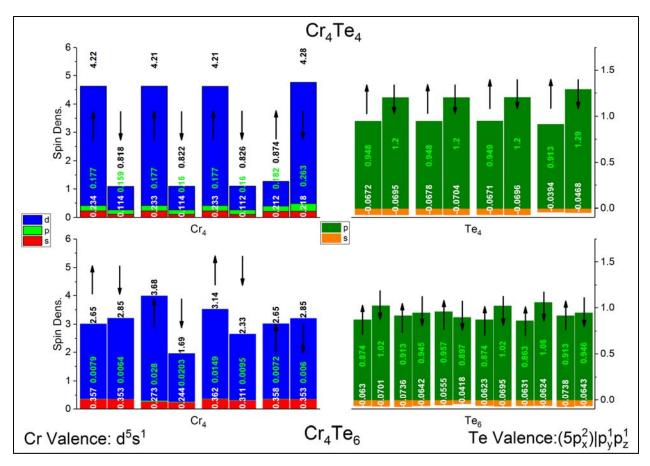
**Figure 3-27.** Mulliken spin populations for  $Cr_4Te_{1-3}$ . (For each n; Arrows mark direction of both spin channels for each Cr atom.)



**Figure 3-28.** Mulliken spin populations for  $Cr_4Te_{4-6}$ . (For each n; Arrows mark direction of both spin channels for each Cr atom.)

This apparent depletion within the Cr (p) orbitals, specifically within the geometry of Cr<sub>4</sub>Te<sub>6</sub>, can be associated primarily with two sources. The first of which is that the Cr (p) orbitals are no longer needed for bonding with Te. The second, an often scenario that arises when using Mulliken Population Analysis (MPA), where the Cr (p) orbitals have been overestimated, lets evaluate. If we look back upon the geometry Cr<sub>4</sub>Te<sub>4</sub> we see all Te atoms are three-coordinated to the faces of the pyramid formed by Cr<sub>4</sub>. Alternatively, the geometry of Cr<sub>4</sub>Te<sub>6</sub> shows that all Te atoms are all two-coordinated, and strictly bonding with the *d* orbitals of chromium. We detail the overall effect of Te on the Cr<sub>4</sub> substructure, and vice versa, in both these clusters within the upper and lower panels of **Figure 3-29**, respectively.

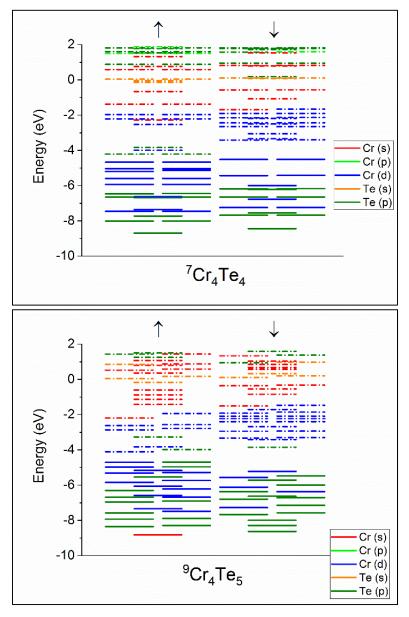
Below, the valence orbitals for the chromium are taken in the usual manner,  $3d^{5}4s^{1}$ . However, for tellurium we go a step further. Instead of the traditional 5p<sup>4</sup> we separate alpha and beta spin channels into two electron counts. The total electron count within the *p* orbitals in a solitary Te atoms is 22, the alpha channel consists of twelve electrons, while there are ten electrons in beta. From here, if we were to subtract nine electron pairs from the *p* orbitals of Te, we would obtain the typical 5p<sup>4</sup> valence scheme. However, below we subtract a total of ten electrons from each channel, all of the electrons which are paired, producing an effective  $5p^{1}p^{1}$ valence. In doing so, we can strictly discuss the modification of the empty, unoccupied, lonepair orbitals of Te (p). Similar to our earlier outline for treatment of the chromium spin populations, we now sum the alpha and beta spins of Te. This number will reach a maximum of two electrons in the alpha spin channel, and zero in the beta. A completely filled 5p orbital of tellurium in this scheme would thus be represented below as both alpha and beta channels equal to a spin density value of two (together then totaling four electrons, i.e.  $p_y^2 p_z^2$ ). Deviations from these totals display the contribution of Te (p) to the overall system.



**Figure 3-29.** Mulliken spin populations for the Cr<sub>4</sub>Te<sub>4</sub> and Cr<sub>4</sub>Te<sub>6</sub> geometries. Upper and Lower, respectively. (Arrows mark direction of both spin channels for every Cr and Te atom, respectively.) (Te valence taken to be the two electrons of the lone-pair orbitals, 5p<sub>v</sub><sup>1</sup>p<sub>z</sub><sup>1</sup>)

For  $Cr_4Te_4$  (upper) there is a significant amount of Te (p) spin density increased as a result of additional bonding with Cr, in the beta channel. While for  $Cr_4Te_6$  (lower), the Te (p) density is maintaining approximately its original valence electron count. The movement between Cr (p) levels, across all the geometries outlined in this document, can be best described as the involvement of Cr (p) in the bonding scheme, and as an attempt of the calculation to fully represent the interactions between Te (p) and Cr (d).

Without too much elaboration, the presence of this artifact in calculations arises from using a finite sized basis set to describe (supra)molecular orbitals (i.e. from using localized orbitals in describing and constructing diffuse, molecular orbitals). This approach amplifies these shortcomings when computing the interaction energy between two subspecies of a molecule. Or, as in our case between two atoms. That subspecies will then attempt to improve upon this by effectively "borrowing" basis functions from another subspecies (tellurium) within that system.<sup>205,206</sup> Thus, the Cr (p) Mulliken Spin Densities graphed for these clusters, those previous and those below in subsequent sections, are slightly increased (10<sup>-3</sup>) in their totals. This slight increase in the Cr (p) is not enough to alter their description, but warrants a brief mention.



*Figure 3-30.* <sup>7</sup>*Cr*<sub>4</sub>*Te*<sub>4</sub> & <sup>9</sup>*Cr*<sub>4</sub>*Te*<sub>5</sub> *Atomic Orbital (AO) level diagrams. Left column represents spin-up (alpha) channel. Right; spin-down (beta).* 

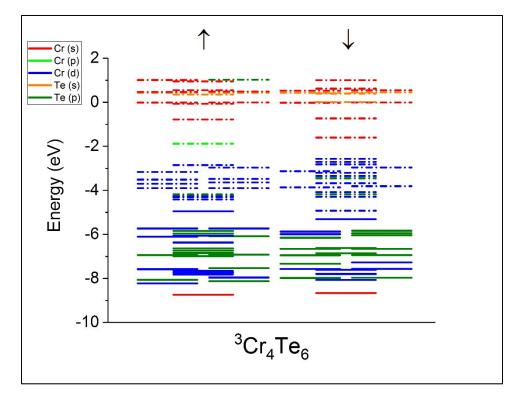


Figure 3-31. Atomic Orbital (AO) level diagram for Cr<sub>4</sub>Te<sub>6</sub>.

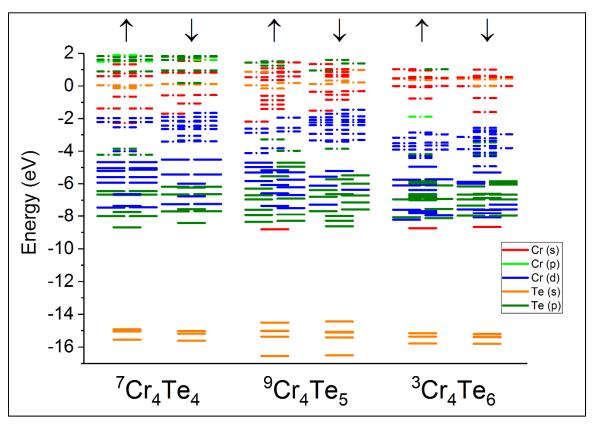


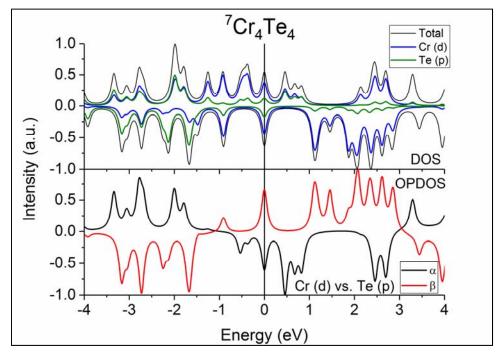
Figure 3-32. Atomic Orbital (AO) level diagrams for  $Cr_4Te_y$ , y = 4 - 6. (left to right, respectively.)

The atomic orbital (AO) level diagrams for  $Cr_4Te_4$  and  $Cr_4Te_5$  are shown in **Figure 3-30** and  $Cr_4Te_6$  in **Figure 3-31**. Additionally, all are shown together in series, with corresponding Te (s) orbitals, within **Figure 3-32**. The density of states for these clusters are shown below in **Figure 3-33** through **Figure 3-35**. Across all of these figures can be highlighted the distortion of Cr, and rearrangement of the Te atoms. With a diminished bond order between the orbitals of Cr (d) and Te (p), the chromium atoms are now forming stronger bonds between each other. This results in structures with chromium arrangements and bond lengths that closely mimic those found within the pure clusters of chromium of the same number. This behavior can be seen between the structures of  $Cr_4$  in **Figure 3-2** and  $Cr_4Te_6$  in **Figure 3-6**.

Furthermore, if we recall the graphs of Average Bond Distances and the change in Hirshfeld Charge densities from **Figure 3-12**. From that figure, we can see that the absence of a third bond from Te has allowed the average bond distances between the Cr atoms to fall to the lowest of all geometries composed of three or more chromium. Additionally, compared to the previous Cr<sub>4</sub>Te<sub>x</sub> clusters, both chromium and tellurium atoms within Cr<sub>4</sub>Te<sub>6</sub> experience the least amount of change to their Hirshfeld charge densities. The bonding of Te (p) with Cr (d) across all of these clusters can be seen below in their respective DOS. For Cr<sub>4</sub>Te<sub>4</sub> and Cr<sub>4</sub>Te<sub>5</sub>, **Figure 3-33** and **Figure 3-34**, we can see that the Te (p) do not completely eliminate the spins of Cr (d). Alternatively, for Cr<sub>4</sub>Te<sub>6</sub>, Te (p) primarily bonds to Cr (d) and drives the total magnetic moment of the cluster downward.

Thanks in part to its size, the continual addition of Te atoms onto Cr<sub>4</sub> produces clusters with an alternating bonding scheme for the Te atoms. That is, for an even number of Te each bond in the three-coordination, and for odd number all will be three-coordinated with the exception of one Te. This occurs in a few of the smaller sized chromium structures, but becomes

a regularity and more apparent within  $Cr_4Te_y$ . Especially so for the clusters of  $Cr_4Te_3$ ,  $Cr_4Te_4$ , and  $Cr_4Te_5$ . The cluster of  $Cr_4Te_6$  is thus a special case.



*Figure 3-33.* Density of States (DOS) & OPDOS for  ${}^{7}Cr_{4}Te_{4}$ . (OPDOS: Overlap Population Density of States. Positive indicates bonding; Negative: antibonding. Beta inverted for clarity.)

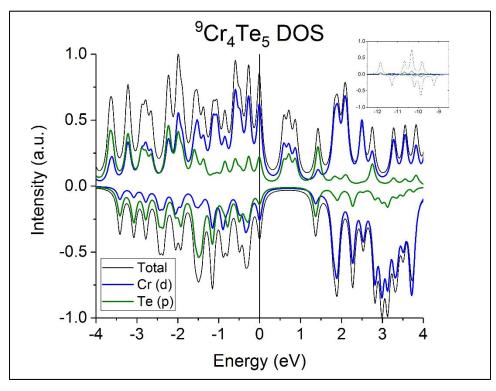


Figure 3-34. Density of States (DOS) for <sup>9</sup>Cr<sub>4</sub>Te<sub>5</sub>.

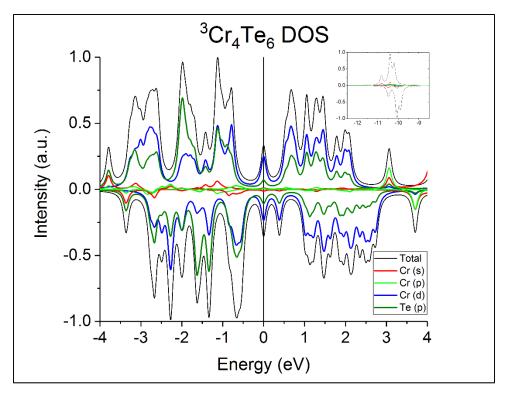
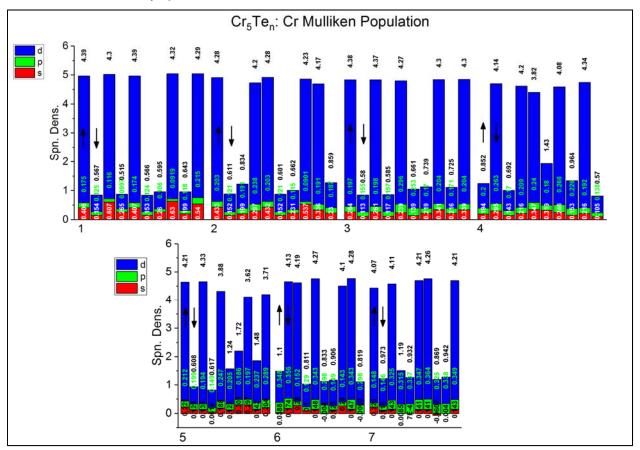


Figure 3-35. Density of States (DOS) for <sup>3</sup>Cr<sub>4</sub>Te<sub>6</sub>.





*Figure 3-36.* Mulliken spin populations for  $Cr_5Te_{1-7}$ . (Arrows mark direction of both spin channels for each Cr atom, respectively. For clarity, only the first atom is marked.)

The Mulliken spin populations for each Cr atom within the Cr<sub>5</sub>Te<sub>7</sub> series can be seen in **Figure 3-36**. Here we can clearly see on a larger scale both the total effect of added Te atoms, as well as the diminishment in population density of the Cr (s) orbitals, as well as the slight increase in the filling of the Cr (d) beta channel . In this series, as in all others, the bond lengths between the Cr atoms increases. In addition to this, the result of odd numbered Cr atoms further increases the likelihood of their distortion and rearrangement through sequential addition of Te atoms. Furthermore, increased distortion and bond lengths grow in accordance with the number of Te present.

Because of the odd number of Te, the underlying Cr<sub>5</sub> structure is not entirely decorated by three-coordinated Te, but possess a single Te in the two-coordination. This occurs as a matter of necessity, as the Te atoms desire to be farthest away from one another. The result of which is an arrangement of the Cr in a manner that the apex atoms are both spin-up, with a minimal loss of their spin densities. The large number of Cr (d) orbitals involved in this process can be seen in the alpha channel of **Figure 3-37**. Moreover, this effect can be seen within the DOS of **Figure 3-38**, where Te (p) is not fully occupying all available Cr (d) between the HOMO level and down to -1 eV below HOMO. Within this region, we find that the Overlap Population Density of States (OPDOS) between Te (p) and Cr (d) again, as we have seen before in these clusters, to be antibonding in nature, plotted in the lower panel of **Figure 3-38**.

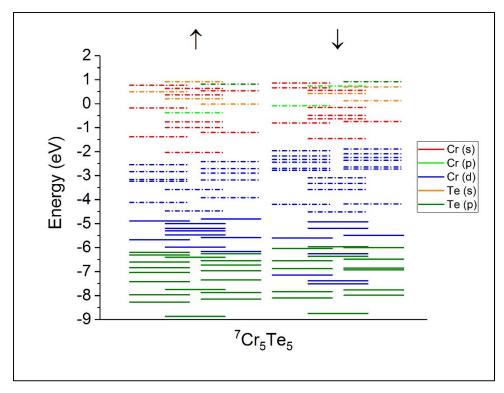
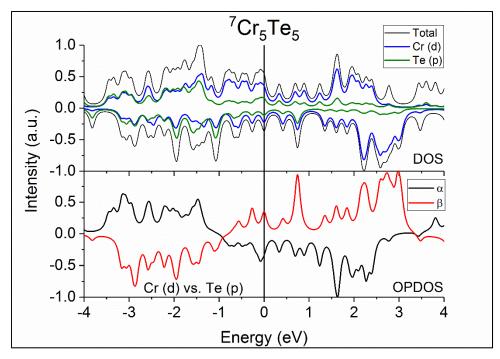
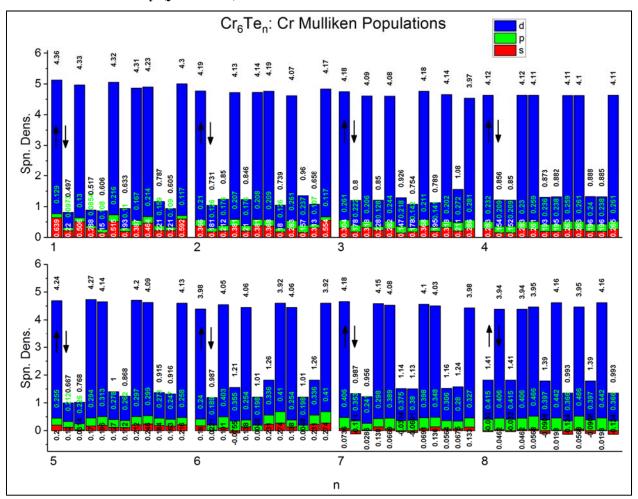


Figure 3-37. Atomic Orbital (AO) level diagram for <sup>7</sup>Cr<sub>5</sub>Te<sub>5</sub>.



*Figure 3-38.* Density of States (DOS) & OPDOS for <sup>7</sup>Cr<sub>5</sub>Te<sub>5</sub>. (OPDOS: Overlap Population Density of States. Positive indicates bonding; Negative: antibonding. Beta inverted for clarity.)

The  $Cr_5$  series can effectively be thought of as marking a transition between the compact structures of  $Cr_4$  and those of the larger  $Cr_6$ . This transition not only highlights the continual influence of Te within the cluster, but also changes within the  $Cr_xTe_y$  series arising due to this newly achieved cluster size specifically. A persistent property seen at all cluster sizes is the effective decrease in the total number of Te atoms that can be supported. However, the current  $Cr_5$  series marks the beginning of the geometries in which all the added Te atoms, with the exception of  $Cr_5Te_5$ , are bonded with three-coordination. This may seem trivial, but this added coordination, and with fewer Te atoms, allows the larger cluster to now become effectively closed and reduces the number of open sites which further protects the cluster from the environment. Moreover, the remaining active sites begin to enforce a form of directionality in the cluster, as their locations dictate the positions available for ligand bonding upon the surface. All of these properties and concepts can be found within the  $Cr_6Te_y$  series as well, in the following section. 3.5.7  $Cr_6Te_y (y = 1 - 6)$ 



*Figure 3-39.* Mulliken spin populations for  $Cr_6Te_{1-8}$ . (Arrows mark direction of both spin channels for each Cr atom, respectively. For clarity, only the first atom is marked.)

As we have discussed above in regards to the  $Cr_5Te_y$  series, when viewing the Mulliken spin populations of  $Cr_6Te_y$  in **Figure 3-39** the same effects can be seen. The increased decoration of Te atoms driving the Cr atoms away from one another, changing the overall contributions and bonding patterns of the Cr orbitals. Additionally, over the entire series, we can see again the slight increase in filling of the beta channel in the Cr (d) orbitals. As we have noted above, in Section 3.3.2.6, all Cr atoms within the Cr<sub>6</sub> series bond together to form an antiferromagnetic cluster in the singlet state, with the exception of  $Cr_6Te_6$  which has fundamentally altered its geometry to avoid this. We can compare the clusters of  ${}^1Cr_6Te_5$  and <sup>7</sup>Cr<sub>6</sub>Te<sub>6</sub> below using their level diagrams within **Figure 3-40** and **Figure 3-41**, respectively. In **Figure 3-40**, we can see the Cr (d) orbitals near the HOMO level to be bonding with each other, facilitating the antiferromagnetic behavior of the total cluster. In the compact geometry of <sup>7</sup>Cr<sub>6</sub>Te<sub>6</sub>, all Cr atoms are maximally coordinated with the surrounding Te atoms as well as each other. This then allows the Cr atoms to arrange their spins in a manner similar to what we have seen above in the smaller CrTe clusters, and maximize the total magnetic moment of the cluster. The level diagram of **Figure 3-41** shows the number of Cr (d) orbitals of the alpha channel densely populated near the HOMO level, without equal number to those of the beta channel. Moreover, **Figure 3-42** shows us, again, that Te (p) does not entirely fill the Cr (d) orbitals within the cluster, and as far as one electron-volt below the HOMO level the antibonding behavior persists, as well.

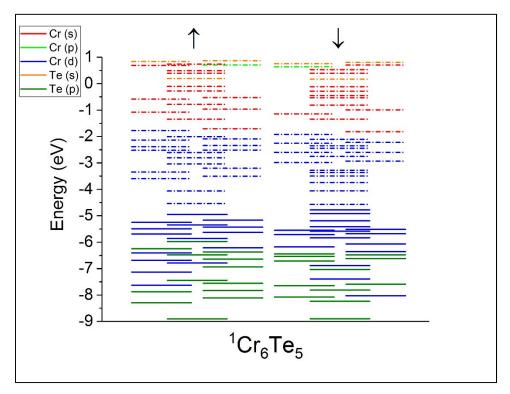


Figure 3-40. <sup>1</sup>Cr<sub>6</sub>Te<sub>5</sub> Atomic Orbital (AO) level diagram.

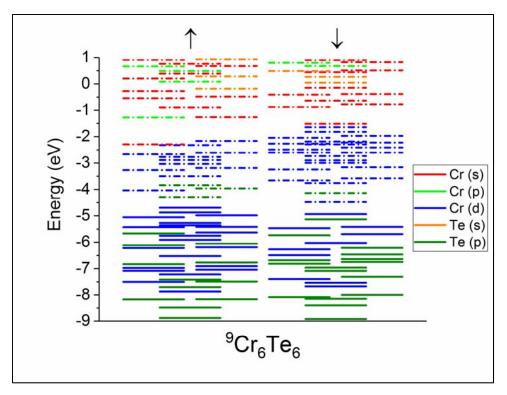
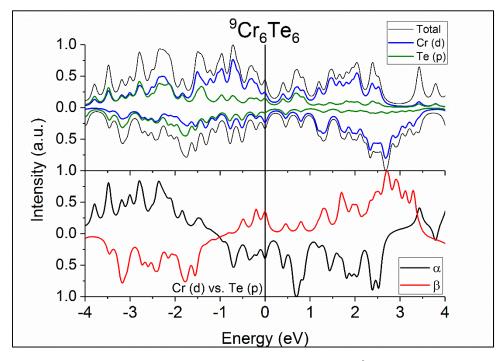


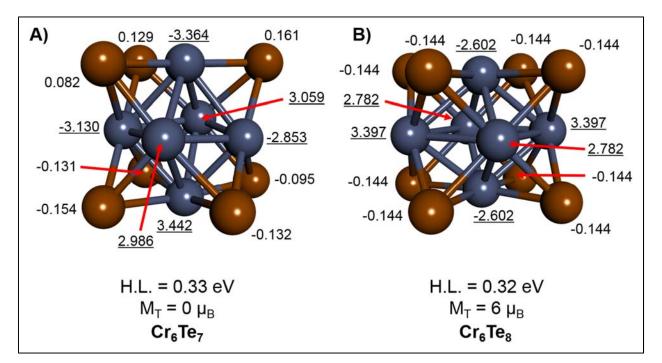
Figure 3-41. <sup>9</sup>Cr<sub>6</sub>Te<sub>6</sub> Atomic Orbital (AO) level diagram.



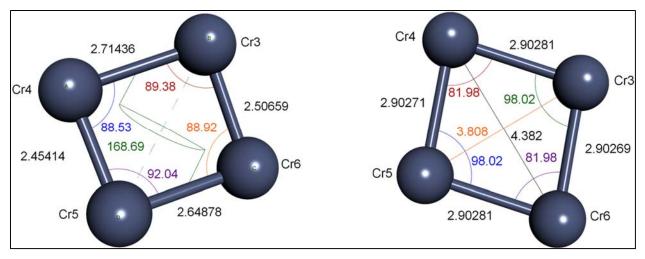
*Figure 3-42.* Density of States (DOS) & OPDOS for <sup>9</sup>Cr<sub>6</sub>Te<sub>6</sub>. (OPDOS: Overlap Population Density of States. Positive indicates bonding; Negative: antibonding. Beta inverted for clarity.)

#### 3.5.8 $Cr_6Te_y$ (y = 7, 8)

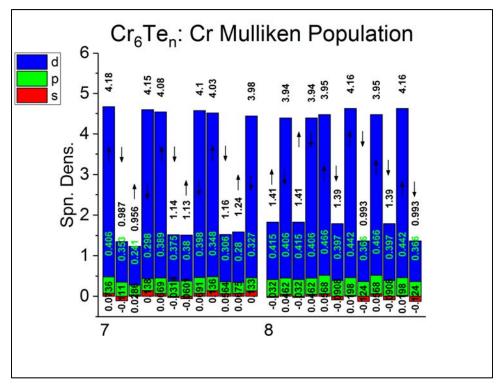
We conclude our discussions of small binary CrTe clusters by further examining Cr<sub>6</sub>Te<sub>7</sub> and Cr<sub>6</sub>Te<sub>8</sub>. Geometries for both clusters are shown in **Figure 3-43** (**A**) and (**B**). The major difference between these two can be first be seen in their spin states, M = 1 and M = 7, respectively. Without the addition of the eighth Te atom, Cr<sub>6</sub>Te<sub>7</sub> takes on a configuration which is highly distorted. This configuration is exemplified in the central Cr<sub>4</sub> substructure of both clusters, seen in **Figure 3-44**, left and right, respectively. For Cr<sub>6</sub>Te<sub>7</sub>, all central Cr bonds are of different length and, because these four atoms are out-of-plane in the dihedral with angle 168.69°, can maintain bonding angles close or very near to 90°. Alternatively, the Cr<sub>6</sub>Te<sub>8</sub> central Cr<sub>4</sub> unit remains planar, and with near equal bond lengths of ~2.902 Å. However, to maintain this configuration the atoms are merely deformed, forming two pairs of angles 81.98° and 98.02°.



**Figure 3-43.** Groundstate geometries of <sup>1</sup>Cr<sub>6</sub>Te<sub>7</sub> and <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>. (Reproduced from above.)



**Figure 3-44.** Geometry of the central  $Cr_4$  subunits for  ${}^1Cr_6Te_7$  and  ${}^7Cr_6Te_8$  clusters. (left and right, respectively.)



**Figure 3-45.** Mulliken spin populations for  ${}^{1}Cr_{6}Te_{7}$  and  ${}^{7}Cr_{6}Te_{8}$ . (Arrows mark direction of both spin channels for each Cr atom, respectively.)

Furthermore, the Cr<sub>6</sub>Te<sub>7</sub> cluster can be described easily with an argument typically found previously in the literature for describing this type of cluster; as the antiferromagnetic result of the union between two ferromagnetic *nido*- clusters, Cr<sub>3</sub>Te<sub>3</sub> and Cr<sub>3</sub>Te<sub>4</sub>. The addition of the eighth Te atom, in Cr<sub>6</sub>Te<sub>8</sub>, slightly relieves the distortion of the central Cr<sub>4</sub> geometry, which alters the arrangements of the nearby Cr atoms. This results in a cluster with a total magnetic moment of 6  $\mu$ B, constructed by Cr atoms in a ferrimagnetic arrangement formed across three separate regions of the cluster, the apex Cr of top and bottom, both spin down, and the middle Cr4, all spin up. All of this has been labelled above in **Figure 3-43**, and can be seen in the spin density graph of **Figure 3-45**.

The change in the bonding of nearby chromium atoms through addition of tellurium can be seen below in the level diagrams of **Figure 3-46** and **Figure 3-47**. Structural deformation is apparent in both figures. The Cr<sub>6</sub>Te<sub>7</sub> cluster employs nearby Cr (p) and Cr (s) orbitals, and as mentioned in the Cr<sub>4</sub>Te<sub>6</sub> cluster, near mimicking the properties found in the pure Cr<sub>6</sub> cluster variant. The Cr<sub>6</sub>Te<sub>8</sub> cluster is not only distorted in its Cr<sub>4</sub> subunit, but also compressed along the z-axis direction. Much of the deformation in both of these clusters can be attributed to Jahn-Teller distortion, where the numerous *d*-orbitals must break their degeneracy through either modification of the electronic shells, or the structure itself.<sup>207–213</sup> The result of all of this rearrangement drives both average Cr and Cr-Te bond lengths in Cr<sub>6</sub>Te<sub>8</sub> upwards, and drastically so for Cr-Cr. This then allows underlying orbitals to participate in bonding, while Cr (d) maintain their spin densities, and can be seen in the density of states of **Figure 3-48**.

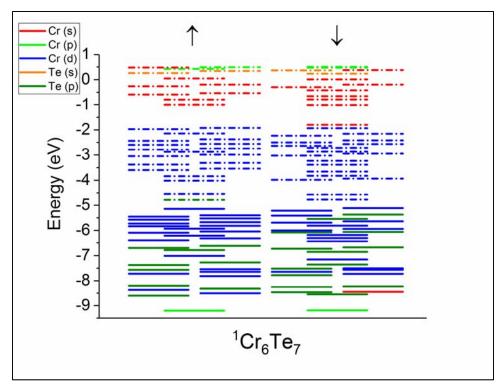


Figure 3-46. <sup>1</sup>Cr<sub>6</sub>Te<sub>7</sub> Atomic Orbital (AO) level diagram.

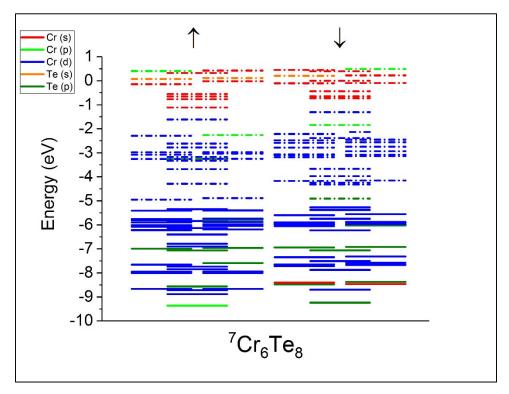
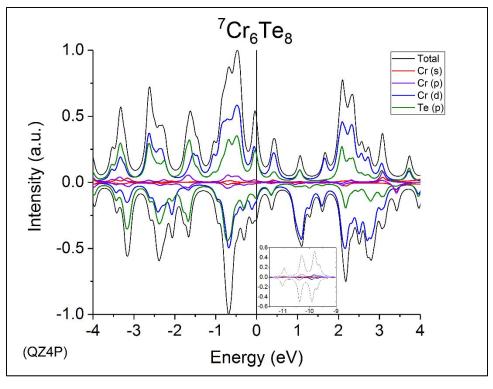
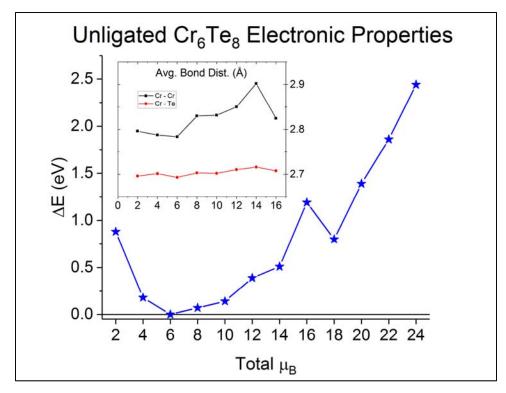


Figure 3-47. <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> Atomic Orbital (AO) level diagram.



*Figure 3-48.* Density of States for unligated <sup>7</sup>Cr<sub>7</sub>Te<sub>8</sub>. Inset shows location of the lower Te (s) orbitals

The stability of the bare  $Cr_6Te_8$  can be further expressed using the information within **Figure 3-49**, below. Here, we have plotted the lowest energy geometry for each magnetic moment, with inset showing the average Cr-Cr and Cr-Te bond distances. The groundstate magnetic moment for the  $Cr_6Te_8$  is the septuplet, as shown above in previous sections. From the plot, we can deduce that to deviate from this magnetic moment, the  $Cr_6Te_8$  cluster would favor the M = 9 multiplicity. However, even though this is energetically favorable, it is not structurally, as the bond distance between Cr atoms would need to be elongated to a drastic degree to produce such a charge state. Knowing this information regarding the  $Cr_6Te_8$  cluster further confirms that the septuplet multiplicity is correct.



**Figure 3-49.** Cluster energetics for  ${}^{(x+1)}Cr_6Te_8$  across various values of total  $\mu_B$ . Cluster energies have been normalized to groundstate. Inset shows average Cr-Cr and Cr-Te bond distances.

#### 3.6 **Discussion & Conclusions**

From the analysis and results above, ranging across all sizes in the combination of chromium and tellurium, we can make definitive conclusions on a number points. The first of these is in regard to the overall structures. The weakness of the chromium bond is made more apparent and exploited through addition of tellurium, but the overall cluster is made stronger as a result. Additionally, within all clusters, chromium atoms still prefer to bond with each other, of course, and structurally, comprise the main clusters component.

The effect of Te on the underlying properties of Cr is apparent at all sizes. However, this effect is made especially noticeable between the two species when Cr has yet to be decorated with sufficient number of Te. This situation is typical of the intermediate cluster sizes, where the number of bonding sites is lacking. It is within those clusters we can see an attempt, and some success, of the chromium atoms to return to properties found in their pure versions. In regards to Te bonding, pure tellurium is known for its ability to form two- and three-coordinated configurations, and the effect of Te itself is not maximized until it engages this third bond upon the cluster, further influencing the underlying chromium.

Secondly, growing to larger cluster sizes, the resulting expansion of bond lengths between chromium atoms is due in part to the bonded tellurium atoms. Because of this expansion, the Cr bonds are driven to lengths that can be considered an extremum. These extended lengths seen between the metal atoms has led previous experimental reports in the literature on 686-cluster types to describe the metal-metal bonds as mediated by the nearby, capping, atom. From what we have shown above in previous sections, this description lacks conclusiveness, can be misleading, and fails to highlight the underlying cluster behavior. We saw above in describing the  $Cr_6Te_8$  cluster, that all bonds formed are covalent, and the bonding of Te upon the faces of the  $Cr_6$  octahedron deform the structure and thus becomes another structural component. This indicates that the added Te atoms are integral to the stability of the overall cluster, more than merely dictating the behavior of the underlying metal-metal bond. This role of bonded Te atoms has been seen at all sizes of cluster, and is not applicable strictly to the cluster of  $Cr_6Te_8$ .

Using the information and results of this chapter we now carry forward an understanding of the  $Cr_6Te_8$  structure as necessary for our discussion in utilizing it as a cluster motif. We can further the discussion of ligated atomically precise binary transition metal—chalcogenides as it pertains to the union between the elements at the extremums of both these classifications. Thus, in Chapter 4, below, we describe the alteration of properties in the pure  $^7Cr_6Te_8$  through ligation with triethylphosphine (PEt<sub>3</sub>), whose structure has been experimentally reported in the literature previously. Moreover, how these properties are varied through passivation of the cluster with alternate ligands; specifically, PH<sub>3</sub>, CN, and CO.

# 4 Electronic Properties of <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> and Alteration Through Ligand Exchange

#### 4.1 **Overview**

If we recall from chapter one, the passivation of a bare metal cluster is first done to stop its the growth into larger sizes, and preserve any atomic scale properties. Moreover, we also know that is it is possible to manipulate these properties by adjusting the electron count of its valence shell through the use of various ligands. We shall see below that the attachment of triethylphosphine (PEt<sub>3</sub>) ligands alters both the structure and electronic properties of the Cr<sub>6</sub>Te<sub>8</sub> core, while also preserving its overall magnetic moment in the septuplet state. But, before moving into the ligated cluster, we must first discuss briefly about DFT formalism.

## 4.2 Change of Basis Set

Calculations upon the larger ligated cluster were again performed utilizing the methods describe in the previous chapters. However, in the interest of time and resources, the basis set has been changed from the original all-electron quadruple-zeta with four added polarization terms (QZ4P). The new basis set utilized below, for the ligated core, is the triple-zeta with double polarization (TZ2P), and under the frozen core approximation. The "frozen core" approximation allows one to hold fixed the coefficients and exponents that construct an atomic orbital comprised within a chosen basis set. Keeping the values constant will thus mean they do not update during the SCF cycles between geometry updates (i.e. not computed), and translates to a reduced computation time. The "frozen core approximation" itself and how it is

implemented within ADF will not be detailed here, but can be found within the literature for those interested.<sup>154</sup>

To assuage any doubt or discrepancy between this switch in formalism, we compute the Cr<sub>6</sub>Te<sub>8</sub> core yet again with an additional two basis sets, and maintaining the PBE functional, to finally obtain the core geometry most comparable to the ligated version. The basis set list is as follows; (1) QZ4P (from above), (2) TZ2P (All Electron, without frozen core), (3) PBE:TZ2P (Large Frozen Core). A keen eye will immediately see the reduction in basis set size when moving from (1) to (2), followed by the reduction in the number of basis set coefficients to compute, from (2) to (3).

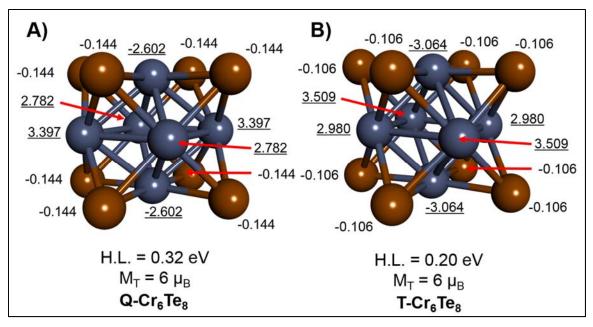
The sizes of these basis sets vary between each element, of course, depending on the number of orbitals it possesses. Thus, for the chromium atom  $(1s^2 2s^2 2p^6 3s^2 3p^6 4s^1 3d^5)$ , the ZORA QZ4P basis is constructed using coefficients totaling 13S 8P 5D 3F, for their respective orbitals. That is, 13 coefficients for the total number of *s* orbitals, eight for *p*, five for *d*, and three for *f*. For tellurium  $(1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 4d^{10} 5p^4)$ , 18S 15P 8D 3F. Under ZORA TZ2P, all electron; chromium, 9S 6P 3D 1F; and tellurium, 12S 10P 7D 1F.

In ADFs frozen core approximation, one is afforded three options; small, medium, large. Each choice utilizes a different basis, adjusting the number of atomic orbital coefficients to hold fixed. For a few elements, some of these choices have similar effect. For example, for both Cr and Te atoms the "medium" and "large" options perform in the same manner. However, for an element such as phosphorus, all options are equal. Specifically, when choosing a "large" frozen core when calculating Cr, the coefficients representing the orbitals  $1s^2 2s^2 2p^6 3s^2 3p^6$  are kept fixed, effectively making them the "core" orbitals, while  $4s^13d^5$  are then treated as "valence". The TZ2P large frozen core basis set now reads as 3S 2P | 3S 1P 3D 1F, where 3S 2P terms have been used to represent the "core". In tellurium,  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 4d^{10}$  are treated as the "core", and only  $5p^4$  as "valence". The basis for this configuration is 4S 3P 2D | 3S 3P 1D 1F.

After all of these changes, it should be noted that the groundstate geometry and isomer series of the  $Cr_6Te_8$  cluster remains unchanged. That is geometry, across all calculations, is in the M = 7 multiplicity. Within the next section we shall highlight any differences that should arise when changing the basis, and maintain that there are a larger number of similarities between them.

## 4.3 The <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> Metal Core: QZ4P vs. TZ2P (Frozen Core)

The groundstate structure for Cr<sub>6</sub>Te<sub>8</sub>, as computed with QZ4P and Large Frozen Core TZ2P, can be seen below in **Figure 4-1** (**A**) and (**B**), respectively. Major differences between the two can first be seen in the spin moments of the individual Cr atoms, specifically those of the apex atoms. In moving from a sizeable all-electron basis to the smaller, and then utilizing the "frozen core approximation" there is an increase in magnitude by approximately 0.5  $\mu$ B in each atom. Although not to the same magnitude, there is also an increase in the spin moments of the individual chromium atoms comprising the central Cr<sub>4</sub> square structure. Additionally, a decrease in the magnitude all the Te atoms, -0.144 to -0.106. Moreover, an increase in average bond distances between Cr-Cr and Cr-Te, 2.713 Å to 2.783 Å, and 2.651 Å to 2.693 Å, respectively.

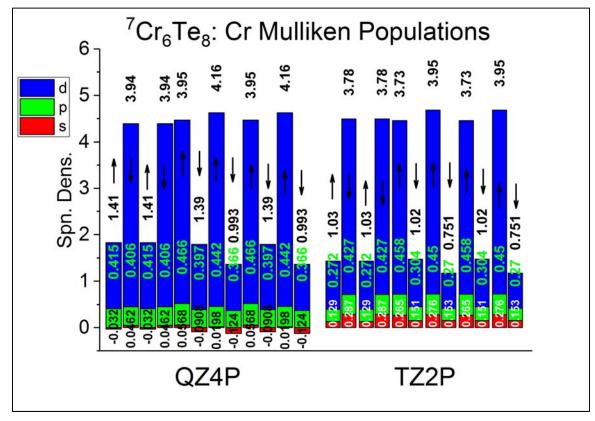


*Figure 4-1.* Groundstate geometries of <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> utilizing different Basis Sets. QZ4P (A), TZ2P Large Frozen Core (B).

All of these changes can be attributed mainly to the restriction of the involved Cr (s) orbitals within the computation below the  $4s^1$  level, and to a smaller degree the Cr (p) orbitals. The distortion and charge movement can be attributed to the behavior of the individual Cr atoms, and placing this restriction upon them effectively disallows further *s* (*p*) orbital movement to participate in bonding. Thus, the presence of Cr (s) from the TZ2P calculation can be seen in both its level diagram and density of states, **Figure 4-3** and **Figure 4-4**. The change in basis set and orbital involvements can also be easily seen in the spin populations of **Figure 4-2**.

Moreover, calculations utilizing the TZ2P basis without the frozen core approximation, TZ2P all-electron, have yielded a cluster with similar results and properties to that of QZ4P. This then confirms not the size of the basis set, but correct overall treatment and representation of the orbitals in the calculation to be of more importance. However, in our current context, the differences between the two cluster representations becomes mute due to the fact that upon ligation of the  $Cr_6Te_8$  cluster this distortion is removed(!). Given the required computation time, ligated  $Cr_6Te_8$  clusters as computed with QZ4P can be expected to achieve a representation

similar to that found with the TZ2P Large Core. Thus, making the Cr<sub>6</sub>Te<sub>8</sub> cluster and its ligated counterparts as computed below sufficiently represented.



*Figure 4-2.* Mulliken spin populations per QZ4P and TZ2P (Large Core) basis set computed groundstates of the <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> cluster. (Arrows mark direction of the both spin channels for each Cr atom, respectively.)

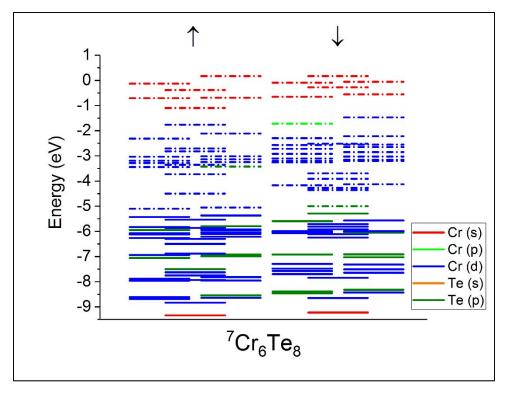
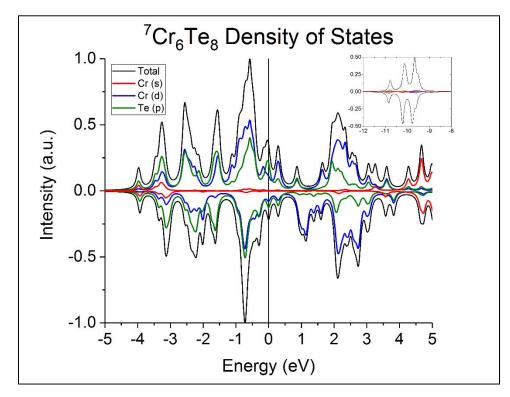
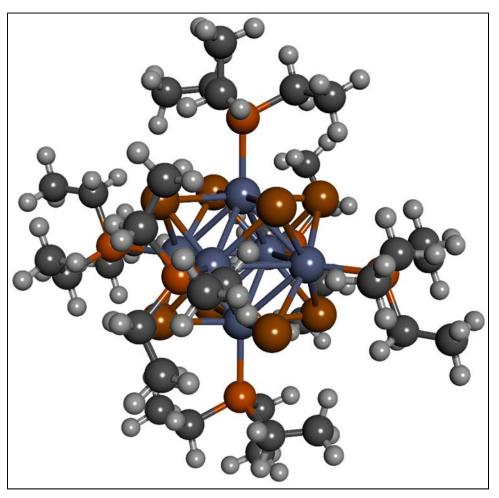


Figure 4-3. Atomic Orbital (AO) level diagram for <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> as computed using the TZ2P (Large Core) basis set.



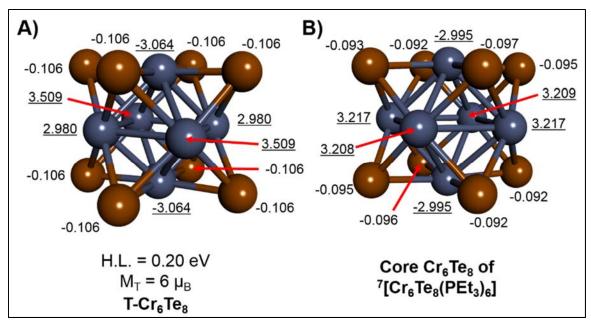
*Figure 4-4.* Density of States for the <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> cluster as computed using the TZ2P (Large Core) basis set. (Inset shows location of Te(s). HOMO adjusted to zero eV.)

## 4.4 The <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> Cluster

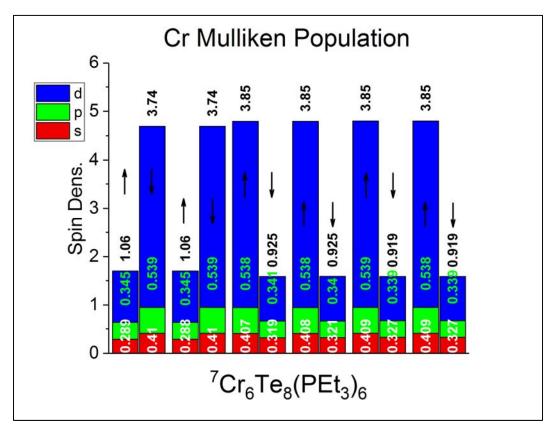


*Figure 4-5.* The groundstate structure of the  ${}^{7}Cr_{6}Te_{8}(PEt_{3})_{6}$  cluster.

The stabilization of the Cr<sub>6</sub>Te<sub>8</sub> structure as completed within the previous sections serves as the starting point for its passivation with various ligands. The groundstate structure for the <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>) cluster is shown above in **Figure 4-5**. More importantly, effects of introducing PEt<sub>3</sub> onto the surface of <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> can be seen below in **Figure 4-6** (**A**) and (**B**). The overall spin arrangement is maintained, across both Cr and Te atoms, with the spin up Cr atoms forming and maintaining the center Cr<sub>4</sub> subunit, with spin-down Cr atoms at the apex positions. We can see that upon passivation, the range in which we find the individual Cr spin moments has now narrowed and each fall between  $| 2.99 - 3.21 \mu_B |$ , respectively.



**Figure 4-6.** Groundstate geometries for <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>, and core of the <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> cluster. (A) and (B), respectively. (With HOMO-LUMO gap energies and individual spin moments. Cr spins are underlined.)



**Figure 4-7.** Mulliken spin populations for <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6.</sub> (Arrows mark direction of both spin channels for each Cr atom, respectively.)

In comparing the Cr atom Mulliken populations of the ligated cluster in **Figure 4-7** with that of the bare <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> (TZ2P-Large Core) cluster found in **Figure 4-2**, there is a clear difference. The PEt<sub>3</sub> ligands are bonding to Cr by way of both *s* and *d*-orbitals. Due to the introduction of electrons from PEt<sub>3</sub> ligand, the Cr (s) electrons no longer participate in the Cr-Cr bonding, and as a result there is an increase of the average bond distances between Cr atoms, to 3.050 Å. But, more importantly, the Cr atoms maintain their *d*-orbital spin density magnitudes to a relative degree in the spin up, and increase slightly in the spin-down. Confirmation of this effect caused by the added PEt<sub>3</sub> can be viewed within the clusters level diagrams and density of states, **Figure 4-8**, **Figure 4-9**, and **Figure 4-10**.

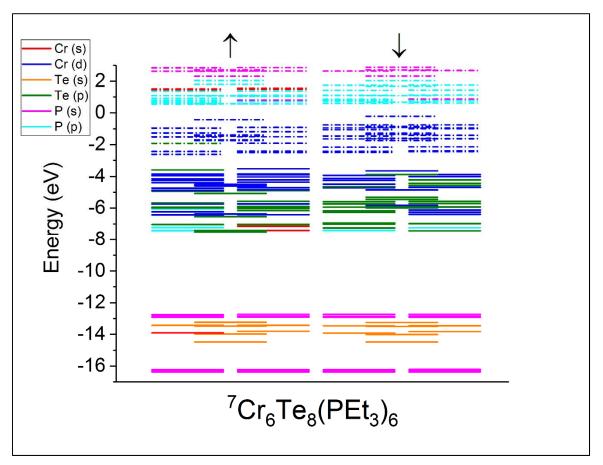
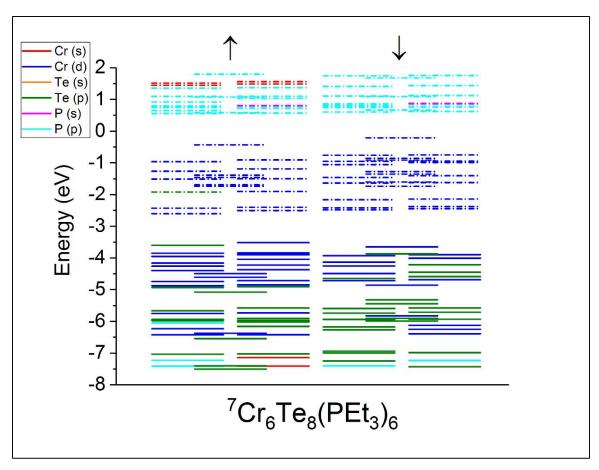
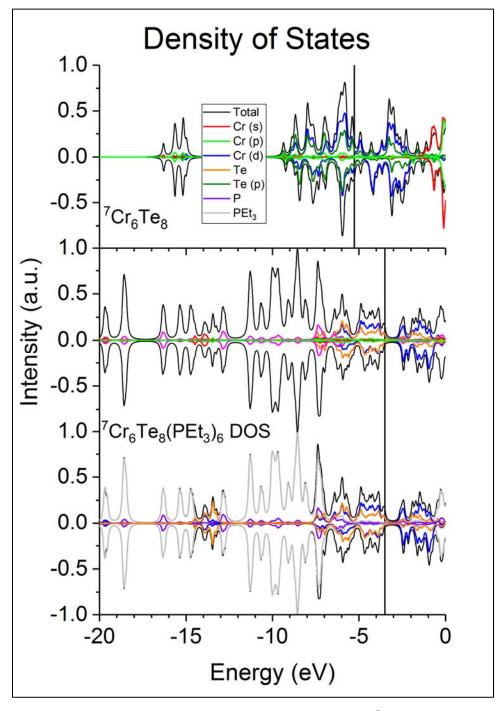


Figure 4-8. <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> Atomic Orbital (AO) level diagram, total. (Carbon and Hydrogen orbitals removed for clarity.)



*Figure 4-9.* <sup>7</sup>*Cr*<sub>6</sub>*Te*<sub>8</sub>(*PEt*<sub>3</sub>)<sub>6</sub> *Atomic Orbital (AO) level diagram, scaled.* (*Carbon and Hydrogen orbitals removed for clarity.*)

The level diagram of **Figure 4-9** clearly shows confirms our earlier assessment, but we find further that the P (p) orbitals are bonding with both the *d* and *s* orbitals of chromium. Specifically, in the region of -7 to -8 eV, the bonds are comprised of a mixture between Cr (s) – T (p) – P (p), while the region of -5.5 to -6.5 eV comprises the region where the bonds are constructed of a mixture between Cr (d) – Te (p) – P (p). The total effect shifts the electronic levels upwards when compared with bare  $^{7}Cr_{6}Te_{8}$  in **Figure 4-3**, note the scale used for both figures. Further evidence for the behavior between Cr<sub>6</sub>Te<sub>8</sub> and PEt<sub>3</sub> continues within the density of states below in **Figure 4-10**. The donation of charge from PEt<sub>3</sub> is shown to reorganize the effective bonding orbitals involved between Cr (d) and Te (p). This also is another reason for expansion in the bond distances between Cr-Cr atoms. Additional details regarding the electronic substructure of the <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub> cluster will be elaborated upon below, in Sec. 4.5.



*Figure 4-10.* Density of states (DOS) for the Bare and PEt<sub>3</sub> ligated <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> clusters. Top and Bottom, respectively. (Solid line represents HOMO of alpha spin channel.)

## 4.4.1 Robustness of <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>6</sub>

To verify the M = 7 multiplicity is truly the groundstate geometry for the ligated cluster, additional calculations have been performed. Specifically, in addition to the sequential series where the total magnetic moment of the system was varied, there are a handful of permutations regarding the arrangement of Cr spin moments that must be eliminated in terms of their energy. Due to the large, and more importantly, even number of Cr atoms present, these additional calculations are deemed necessary. Thus, these permutations strictly produce clusters where the Cr atoms are arranged antiferromagnetically throughout, and will then leave the overall cluster system in the singlet state, M = 1. In terms of calculation method, using the valence electrons, each individual Cr atom was given a maximal spin moment (6  $\mu$ B) which was then directed to point in either the spin-up or spin-down direction, together totaling a net 0  $\mu$ B. From that point forward, the geometry is allowed to fully relax without restriction or constraints.

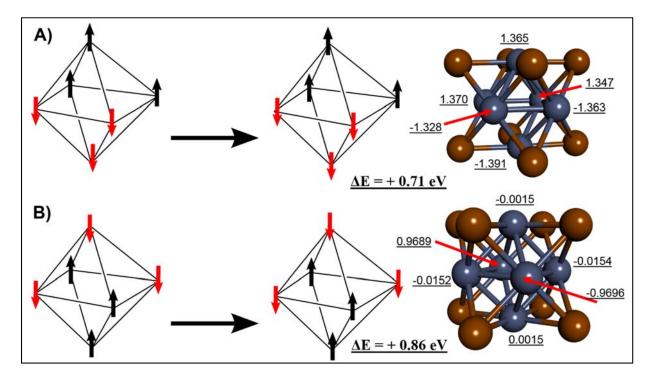


Figure 4-11. Starting and final Cr spin moment arrangements for the two singlet state permutations of  ${}^{1}Cr_{6}Te_{8}(PEt_{3})_{6}$ . Each with distance in energy from groundstate, core geometry, and individual Cr moments labelled. (The PEt<sub>3</sub> ligands have been removed for clarity.)

Two permutations of spin moments have been calculated, and the results of this exercise are shown in **Figure 4-11** (**A**), and (**B**). The first arrangement possible for the M = 1 configuration is two complexes of trigonal chromium coupling antiferromagnetically, effectively two faces of the Cr<sub>6</sub>Te<sub>8</sub> core. The start (left) and final (middle) spin moment arrangement is shown for both, as well as the cluster geometry and labelled associated spin moments for the individual chromium atoms (right). The PEt<sub>3</sub> ligands have been removed for clarity.

In addition to the above verification process, the  $Cr_6Te_8(PEt_3)_6$  cluster has also been found for a variety of spin moments. The energies for each, as they compare to the groundstate, can be seen below in **Figure 4-12**. Noting the scale, the figure clearly highlights a preference for the total cluster to remain in the central, 2, 4, and 6  $\mu_B$  spin states. Above, we have established the 0  $\mu_B$  antiferromagnetic spin state to be unfavorable, and we now confirm the same for the quenched singlet state. Moreover, the difference between high and low spin states, 6 and 4  $\mu_B$ , is approximately 0.20 eV.

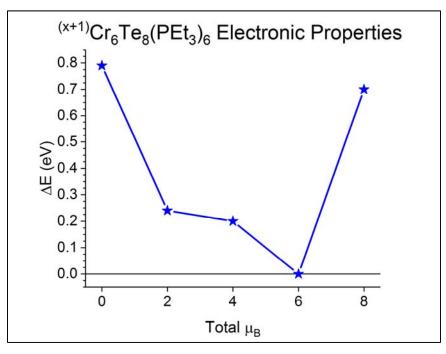


Figure 4-12. Cluster energetics for  ${}^{x}Cr_{6}Te_{8}(PEt_{3})_{6}$  across various values of total  $\mu_{B}$ . Cluster energies have been normalized to groundstate.

### 4.5 Ligand Exchange

Recalling the discussion above in Chapter 1, where periodic solids are constructed through leveraging a clusters fundamental properties of ionization potential and electron affinity. Specifically, we can manipulate those properties through alteration of the clusters valence electron count. A particular strategy to tune electron count, as well as stabilize the cluster core, is to attach ligands. In addition to passivating the metallic core, ligands form covalent bonds that also change the valence electron count. This type of cluster electron count has been completed previously in the literature, where a large number of solids composed of pure or mixed ligated clusters of gold have been used as motifs who are subsequently arranged into periodic solids.<sup>15,17,41,66,214–218</sup> The stability of these cluster motif systems is rationalized within the superatom framework.<sup>16,23</sup> That is, the stable species formed from this process as its valence count obtains a value corresponding to a filled valence and large HOMO – LUMO gap.

Knowing now the structural form of  ${}^{7}Cr_{6}Te_{8}$  cluster, as well as its counterpart within the  ${}^{7}Cr_{6}Te_{8}(PEt_{3})_{6}$ , we aim to now demonstrate within this chapter that ligands can be used to significantly alter the ionization potential and electron affinity of the total cluster. In altering these properties, we can thereby enable this metallic core to behave as either an electron donor or acceptor. The study carried out within this chapter, utilizing the same formalisms established above, further incorporate a variety of alternate ligands, belonging to two different classes. The electron donor of PH<sub>3</sub>, and electron acceptors such as carbon monoxide (CO) and cyanide (CN). Note the chemical formula for cyanide is actually CN<sup>-</sup>, but here we take the neutral, effectively the cation. The reason for this is to view any possible changes between the CO and CN decorated cluster by strategically removing a solitary electron from each bonding site. Once the calculations regarding the total cluster of  ${}^{7}Cr_{6}Te_{8}(PEt_{3})_{6}$  had been completed, it was a trivial

matter (in terms of setup, calculations, time, and resources) in exchanging the ligand for smaller versions. Our main objective is to now examine the effect of each ligand upon the electronic spectrum of the overall cluster. We can view these effects not only through spin population density, but also in the modification of the density of states, as we have done in the previous chapter.

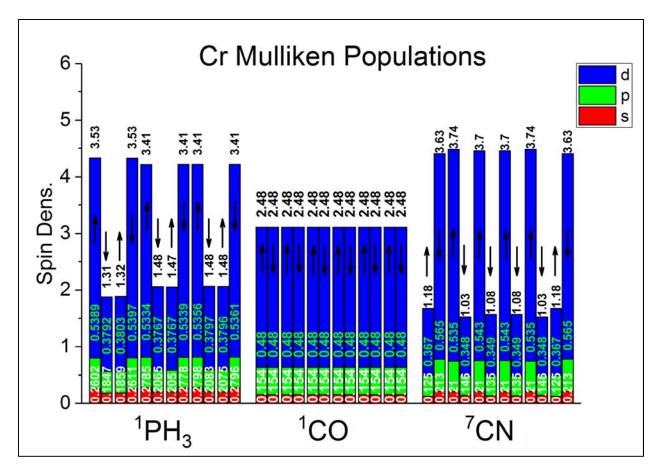


Figure 4-13. Mulliken spin populations for individual chromium atoms within the ligated systems of  $L = PH_3$ , CO, and CN. (left-to-right, respectively. Superscript designates total system multiplicity.)

An immediate change that is visible across these clusters is there total magnetic moment, and how that moment is comprised from the individual spin moments of the Cr atoms. We can see those changes above in **Figure 4-13**, for each of the ligands PH<sub>3</sub>, CO, and CN, left-to-right, respectively. There are immediately a few points to address, the first being the total absent of a total magnetic moment for both PH<sub>3</sub> and CO cluster variants. Moreover, that the Cr atoms

within the PH<sub>3</sub> cluster are antiferromagnetically arranged, while in the CO case, those same moments are quenched and thus totally absent. Additionally, the cluster decorated by CN maintains the original M = 7 groundstate found in the PEt<sub>3</sub> cluster. It should also be noted, that while the clusters of CO and PH<sub>3</sub> closely maintain the central core structure of the Cr and Te atoms, this is however not the case for the CN cluster whose core is now heavily distorted. Moreover, that the spin moments of the underlying Cr atoms now fall within the region of | 2.73 – 2.96 |  $\mu$ B, which is only a slight difference from those found within the PEt<sub>3</sub> cluster, whose moments are in the range of | 3.00 – 3.22 |  $\mu$ B.

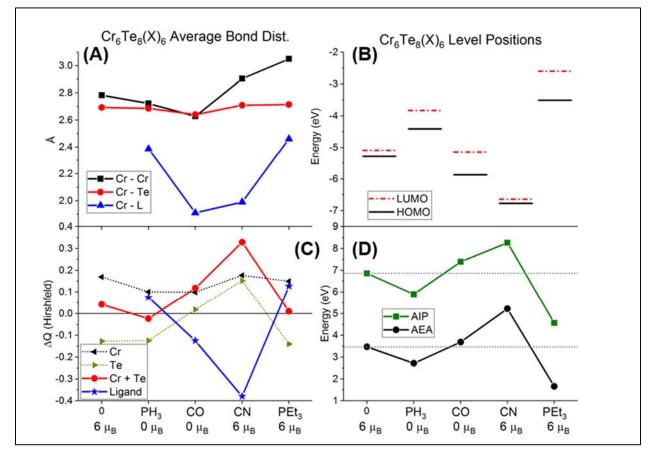


Figure 4-14. Average bond distances, HOMO-LUMO level positions, Hirshfeld Charge Density, Adiabatic Ionization Potential and Electron Affinity energies, for none and various ligands.
(A) – (D), respectively. (Spin moments are in reference to the groundstate structure of that system.)

The plots of the basic electronic properties we aim to alter with ligand substitution are

given above in Figure 4-14. Here we can see, the average bond lengths between Cr-Cr, Cr-Te

atoms, as well as the length between Cr and ligand. The associated HOMO and LUMO levels for all of our clusters. The change in Hirshfeld charge density for Cr, Te, and Ligand. Finally, the change in value for both ionization potential and electron affinity. In panel (**A**) of **Figure 4-14**, we can see the overall effect of the ligand upon the central cluster core. The most intriguing plot here is the average bond lengths between the Cr, which are significantly altered and highly dependent upon the type of ligand. Moreover, there is a significant difference between those bond lengths found when comparing PH<sub>3</sub> and PEt<sub>3</sub> cluster variants as well. Additionally, remembering from above, that although CN and PEt<sub>3</sub> clusters have large Cr bond distances, the CN cluster system does not maintain its geometry. The Cr bond distances for the PEt<sub>3</sub> cluster fall within the region of 2.972 - 3.153 Å, while for the CN geometry 2.678 - 3.068Å, two wildly different ranges in length.

Despite these large variations in bond lengths between the Cr atoms, their Hirshfeld charge densities deviate the least when compared to the Te atoms and Ligands, **Figure 4-14 (C)**. Upon addition of PH<sub>3</sub> there is a slight decrease in charge density of the Cr, 0.169 to 0.101 e<sup>-</sup>, meaning there is a significant amount of donation from the ligand. This is confirmed by the positive density experienced by the PH<sub>3</sub> ligand. The addition of CO oddly does not modify the charge density of the Cr as compared to PH<sub>3</sub>, but does drastically alter that of Te whose role has changed from charge removal to charge donation, from -0.125 to 0.019 e<sup>-</sup>. This charge movement is further maximized in the attachment of CN. Charges for both Cr and Te atoms are diminished, a net positive charge of 0.176 e<sup>-</sup> for Cr, close to its value of the bare <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> cluster, and 0.152 e<sup>-</sup> for Te. These effects upon Cr and Te are exactly inverse to that of the ligand, of course, which for both CO and CN can be seen to be accepting this charge (blue line, **Figure 4-14 (C)**). Things appear to return to "normal" with the addition of PEt<sub>3</sub>, where charge density

126

values return closely to those found in the bare and PH<sub>3</sub> ligated cores. Interestingly enough, the Hirshfeld charge density of the P atoms in both the PH<sub>3</sub> and PEt<sub>3</sub> clusters are drastically different. Although in both systems it is donating charge, within the PH<sub>3</sub> system it has density of 0.080 e<sup>-</sup>, while in PEt<sub>3</sub> it has a density of 0.206 e<sup>-</sup>. Highlighting the fact that these two ligands are not as similar as one might initially expect.

The bare <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub> cluster has a high ionization potential (IP) of 6.96 eV and electron affinity (EA) of 3.47 eV, Figure 4-14 (D). Both of these number are some degree higher than those found in the literature for the bare <sup>7</sup>Ni<sub>9</sub>Te<sub>6</sub> cluster, 6.33 eV and 2.63 eV; and even more so for bare <sup>2</sup>Co<sub>9</sub>Te<sub>6</sub>, 5.82 eV and 2.38 eV, respectively.<sup>81</sup> We further find an IP of 5.95 eV and 2.72 eV EA values for the PH<sub>3</sub> system. An effective lowering from the bare cluster, resulting in the raising of the HOMO and LUMO levels, Figure 4-14 (B). And, as expected, the raising of IP and EA values in both CO and CN systems, as well as the resultant lowering of their respective HOMO-LUMO levels. In CO, the IP has reached 7.39 eV and EA of 3.69 eV. This pales in comparison to the CN system, whose IP has value of 8.27 eV and an EA of 5.22 eV. We go further, and compare these values to the PEt<sub>3</sub> system, which has IP of 4.49 eV and EA of 1.74 eV. Both numbers significantly smaller than its ligated counterparts. To give a frame of reference for these values, as a means of comparison, the IP of Sodium (Na) is 5.14 eV and EA of Chlorine (Cl) is 3.61 eV. We have focused our attention in these calculations to AEA and AIP, as these clusters will relax when paired with a counterion in forming a cluster assembly. Thus, across all of these calculated values and properties, it has been shown that these clusters are capable of such an assembly, in the role of either donor or acceptor.

127

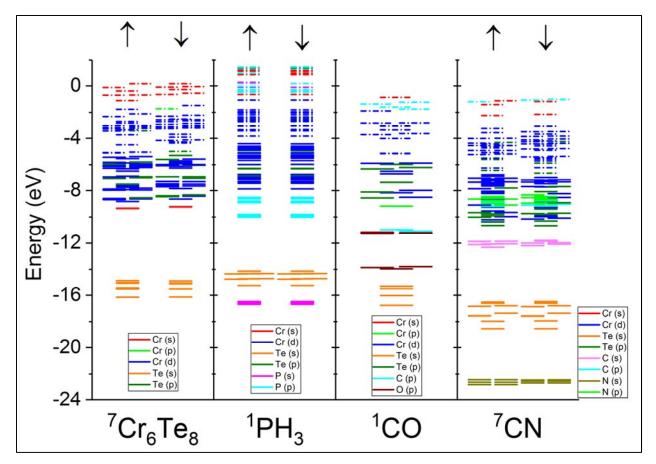
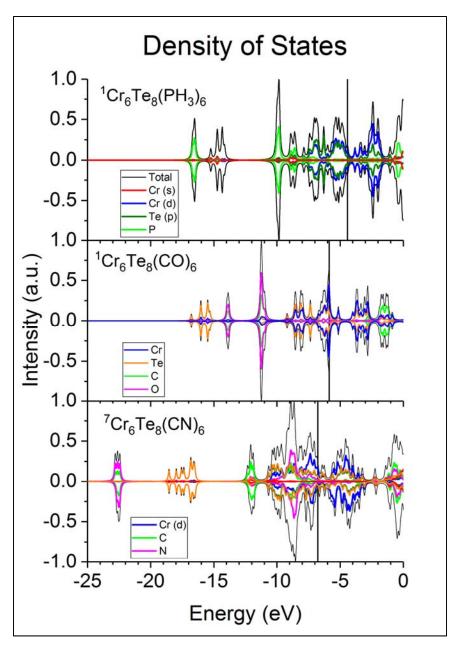
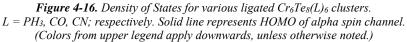


Figure 4-15. Atomic Orbital (AO) level diagrams for Bare and Ligated <sup>x</sup>Cr<sub>6</sub>Te<sub>8</sub> cluster cores. Bare <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>, with PH<sub>3</sub>, CO, and CN versions, left-to-right respectively. (Each with individual legend. Superscript designates total cluster multiplicity. Degeneracies of CO not labelled.)

In considering the atomic changes yielding these alterations to the IP and EA values, the entirety of the atomic orbital energy levels for each cluster, compared to those seen in **Figure 4-14 (C)**, have now been plotted in **Figure 4-15**. There are significant changes to these levels through the alteration of these ligands. The addition of PH<sub>3</sub> shifts upwards the HOMO and LUMO (HL) levels of the bare cluster from -5.29 eV and -5.09 eV, to -4.42 eV and -3.82 eV. The HL gap has now doubled in size. The addition of CO however lowers HOMO level of the bare cluster to -5.87 eV, and increases the HL gap to 0.73 eV. This lowering of the HOMO levels continues with the addition of CN, and can be found at -6.77 eV. But, the CN cluster now has a HL gap of 0.13 eV which is almost half of that in the bare cluster.

In addition to the one electron orbitals above, we can view the movement of the orbitals within the Density of States (DOS) plots of **Figure 4-16**. Within that figure, as well as the DOS plot of the bare and PEt<sub>3</sub> clusters in **Figure 4-10** above, we can readily see the lowering and alteration of the HOMO level (vertical line) through the addition of various ligands. Moreover, although the region near the HOMO level is still comprised of Cr (d) orbitals for all of these clusters, the diminishment of charge on the Te atom can readily be seen in the cluster of CN, where its contributions to the total system have now moved lower in energy.





#### 4.6 **Discussion & Conclusions**

To summarize, the theoretical studies above have illustrated a number of points. The first being in regards to our original cluster of  ${}^{7}Cr_{6}Te_{8}(PEt_{3})_{6}$  and the bare  ${}^{7}Cr_{6}Te_{8}$  core. The ligation of this core does not modify the overall magnetic moment, but does have an influence upon the bond lengths, ionization potential, and electron affinity. Moreover, despite this ligation the energy difference between the groundstate 6  $\mu_{B}$  and next higher isomer of 4  $\mu_{B}$ , remains nearly the same in both of these systems at approximately 0.20 eV. Further adaptability of the bare cluster has been shown in the alteration of the attached ligand. We have shown how these ligands can be utilized in changing the strength of electron withdrawal or donation of the cluster. And, depending on the ligand, fundamentally alter both the physical and electronic structure of the total cluster. The addition of PH<sub>3</sub> and PEt<sub>3</sub> drive the cluster to electron donation, each to a differing degree, however, the addition of CO and CN ligands drives the total cluster toward electron acceptor.

Combining the information of the previous sections together, we have found the PEt<sub>3</sub> donor ligand to be the most desirable in this investigation. This is chiefly due to the bare cluster maintaining its large magnetic moment. But, also due to the fact that the cluster is now more stable after ligation, as well as a better electron donor. Two properties which further solidify it as a suitable building block in cluster assembled materials.

## **5** Summary & Future Directions

During this thesis we have focused on the evolution of bonding as the Cr atoms are mixed with Te so as to provide insight into the stability and magnetic properties of the  $Cr_6Te_8(PEt_3)_6$ cluster that forms a periodic  $[Cr_6Te_8(PEt_3)_6][C_{60}]$  cluster assembled solid. Our results on small  $Cr_xTe_y$  cluster indicate that while pure  $Cr_n$  clusters display antiferromagnetic coupling, the bonding and the nature of coupling evolve as Te is added. Furthermore, that the addition of Te results in a stronger binding with Cr that in turn destabilizes the weaker Cr-Cr metal bonds. Initially, the addition of Te leads to a  $Cr_2Te_3$  cluster with quenched Cr spin moments. This situation only occurs in this particular size and changes as one goes to larger clusters where the Cr sites continue to carry spin magnetic moments.

The manipulation of the underlying Cr cluster structure by the addition of Te atoms involves two aspects. The first, is the bonding of the incoming Te (p) orbitals upon those of Cr (d). The second, is the specific coordination of Te in forming either two of three bonds. Consequently, the bonding of Te results in cluster geometries consisting of two-coordinated, three-coordinated, and a mixture of both, depending on the size of the total cluster. In fact, as a general observation, clusters that contain an abundance of triply coordinated Te are the more stable. The twofold coordination of Te atoms is mostly seen in clusters of up to four Cr, for larger sizes, Te bonds with triple coordination. The balance between Cr and Te atoms exemplifies itself within the geometry of  $Cr_6Te_8$ . Here, we have shown, that it has a high magnetization that can be linked to the symmetrical structure, which is reliant upon the equal number of Te atoms distributed around the cluster. Moreover, this cluster maintains its magnetization upon ligation with the triethylphosphine (PEt<sub>3</sub>) ligands.

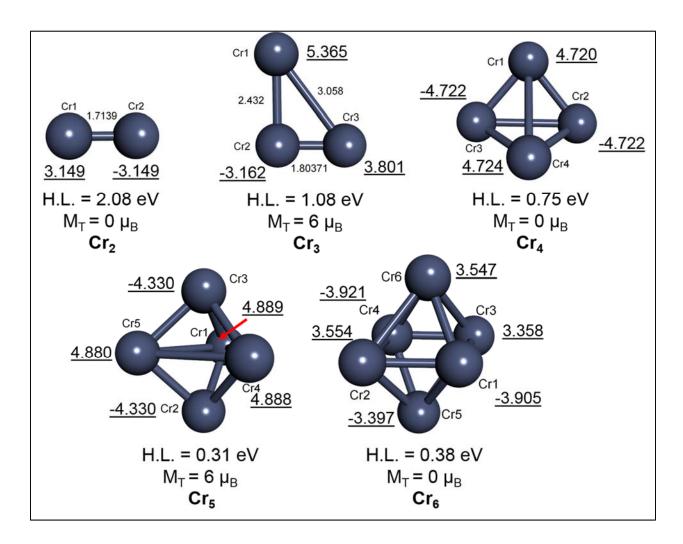
The studies upon the ligated cluster shows that the stability of the bare Cr<sub>6</sub>Te<sub>8</sub> core carries over to the ligated species, making it a suitable building block for synthesis in constructing cluster assembled materials. This aspect was demonstrated within Chapter 4, where we investigated the stability of the properties found in the ligated cluster across a variety of ligands having donor or acceptor characteristics. In particular, the  $^{7}Cr_{6}Te_{8}(PEt_{3})_{3}$  cluster is not only highly stable, due to its large HOMO-LUMO gap, but also maintains its high magnetization within its first cation, 5  $\mu$ B. This finding allows us to make a first step towards understanding the magnetic properties of the  $[^{7}Cr_{6}Te_{8}(PEt_{3})_{3}][C_{60}]$  periodic solid. Note that although <sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>3</sub> has a net magnetic moment, the local spins at two Cr sites are antiferromagnetically coupled to the remaining four. This inter-antiferromagnetic coupling is indicative of the clusters behavior after entering into a periodic solid with C<sub>60</sub>. The previous studies upon the companion cluster system of [Ni<sub>9</sub>Te<sub>6</sub>(PEt<sub>3</sub>)<sub>8</sub>][C<sub>60</sub>] have shown only a weak antiferromagnetic coupling.<sup>219</sup> Although, we have not investigated this aspect within [<sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>3</sub>][C<sub>60</sub>], the presence of a similar coupling could mark a system with both interand intra-antiferromagnetic coupling and as previous studies on perovskites have indicated, these types of systems can show an inverse susceptibility vs temperature plot which saturates at higher temperature. This could account for the observed saturation of the inverse susceptibility of the [<sup>7</sup>Cr<sub>6</sub>Te<sub>8</sub>(PEt<sub>3</sub>)<sub>3</sub>][C<sub>60</sub>] system seen in experiment.

The implications of the theoretical results and studies found within the previous chapters can be summarized in two points. The first, knowing the history of two-dimensional CrTe solids with their numerous stoichiometric versions and properties, we can conclude that those properties continue downward into the atomic scale and their binary clusters. The number and arrangement of Te around Cr both play an important role. Additionally, the studies herein show

133

that the cluster of Cr<sub>6</sub>Te<sub>8</sub> retains the flexibility in its properties most often seen within twodimensional CrTe, and this flexibility and adaptability is now being exploited in a manner to construct novel materials.

## Appendix A Cr<sub>x</sub> Bond Lengths

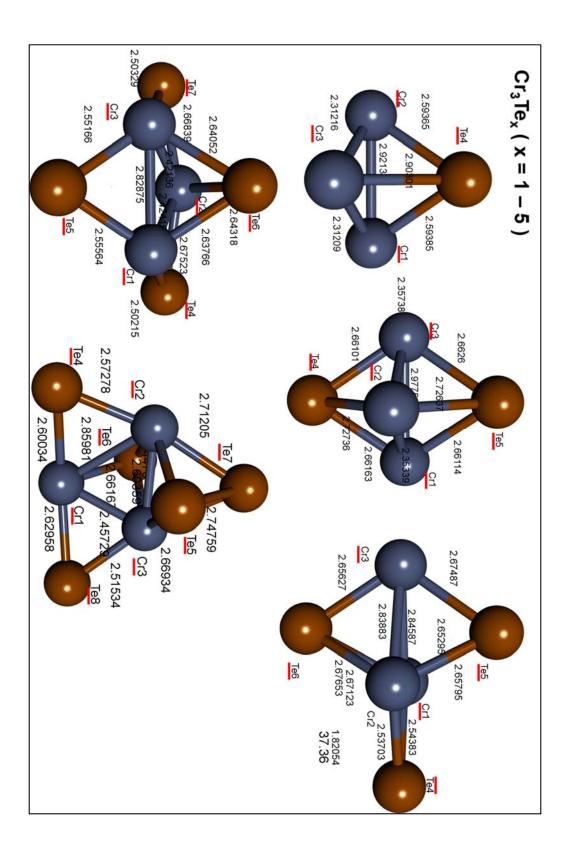


2		3		4	
Cr1-Cr2	1.7138	Cr1 - Cr3	3.0580	Cr1 - Cr2	2.3506
		Cr1 - Cr2	2.4320	Cr1 - Cr3	2.3473
		Cr3 - Cr2	1.8037	Cr1 - Cr4	3.0121
				Cr2 - Cr3	3.0118
				Cr4 - Cr2	2.3486
				Cr4 - Cr3	2.3518
5		6		7	
	2 2026		2 2452		2 4254
Cr1 - Cr2	2.3936	Cr3 - Cr4	2.3452	Cr6 - Cr1	2.4354
Cr3 - Cr1	2.4016	Cr4 - Cr2	2.3767	Cr3 - Cr1	2.4640
Cr3 - Cr4	2.3916	Cr2 - Cr1	2.3777	Cr5 - Cr1	2.4505
Cr3 - Cr5	2.3935	Cr3 - Cr1	2.3430	Cr3 - Cr6	2.8215
Cr4 - Cr1	3.0382	Cr6 - Cr3	2.5563	Cr4 - Cr3	2.2444
Cr4 - Cr2	2.4025	Cr6 - Cr4	2.3714	Cr4 - Cr6	2.4304
Cr5 - Cr1	3.0444	Cr2 - Cr6	2.7607	Cr2 - Cr4	2.8613
Cr5 - Cr2	2.3926	Cr6 - Cr1	2.3866	Cr2 - Cr6	2.4196
Cr5 - Cr4	3.0426	Cr1 - Cr5	2.3375	Cr5 - Cr2	2.4308
		Cr2 - Cr5	2.5562	Cr5 - Cr3	2.8205
		Cr4 - Cr5	2.3633	Cr5 - Cr4	2.4210
		Cr3 - Cr5	2.7068	Cr6 - Cr7	2.8241
				Cr7 - Cr1	2.4588
				Cr7 - Cr2	2.2580
				Cr7 - Cr5	2.8183

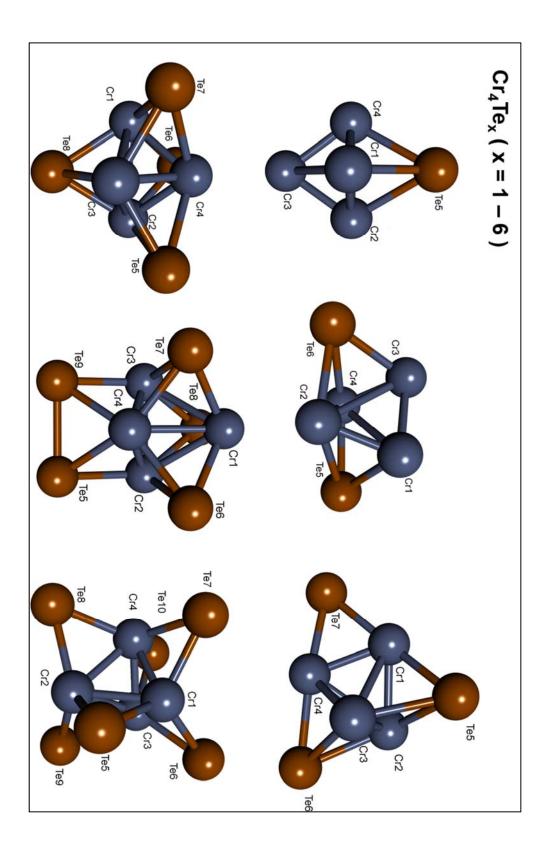
## $Cr_1Te_x (x = 1 - 4)$ 2.62762 Te4 2.44173 Ę 2.70159 59.05 61.85 2.6291 Z 52.69 C12 1.76895 2.5552 2.56686 2.56957 2 2.56979 2.10229 5.71 65. 2.56833 2.56534 2.5552 Cr2 2.56744 2 22880 $Cr_2Te_x (x = 1 - 4)$ 22 Cr2 2,78122 1503 71284 Ē

## Appendix B Cr<sub>x</sub>Te<sub>y</sub> Bond Distances

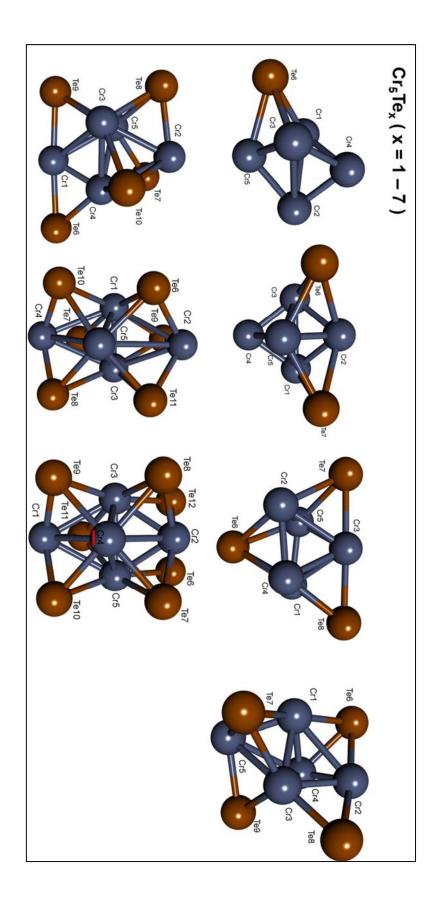
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Cr1 - Te2	2.453	Cr1 - Te2	2.536	Cr2 - Te3	2.629	Cr1 - Te3	2.634
		Cr1 - Te3	2.535	Cr2 - Te4	2.628	Cr1 - Te5	2.63
		Te2 - Te3	2.874	Tel - Cr2	2.442	Te2 - Cr1	2.63
				Te3 - Te4	2.702	Te2 - Te3	2.68
						Te4 - Cr1	2.63
						Te4 - Te5	2.691
21		22		23		24	
Cr2 - Cr1	2.102	Cr1 - Cr2	1.838	Cr1 - Cr2	1.769	Cr2 - Cr1	1.7921
Cr2 - Te3	2.555	Te3 - Cr1	2.556	Cr1 - Te3	2.570	Te3 - Cr1	2.71503
Te3 - Cr1	2.555	Te3 - Cr2	2.561	Te3 - Cr2	2.565	Te3 - Cr2	2.7084
		Te4 - Cr1	2.561	Cr1 - Te4	2.567	Te3 - Te4	2.781
		Te4 - Cr2	2.559	Cr2 - Te4	2.568	Te4 - Cr1	2.7128
				Cr1 - Te5	2.567	Te4 - Cr2	2.7076
				Cr2 - Te5	2.570	Te5 - Cr1	2.7128
						Te5 - Cr2	2.7076
						Te5 - Te6	2.7812
						Teó - Cr1	2.7150
						Teo - Cr2	2.708



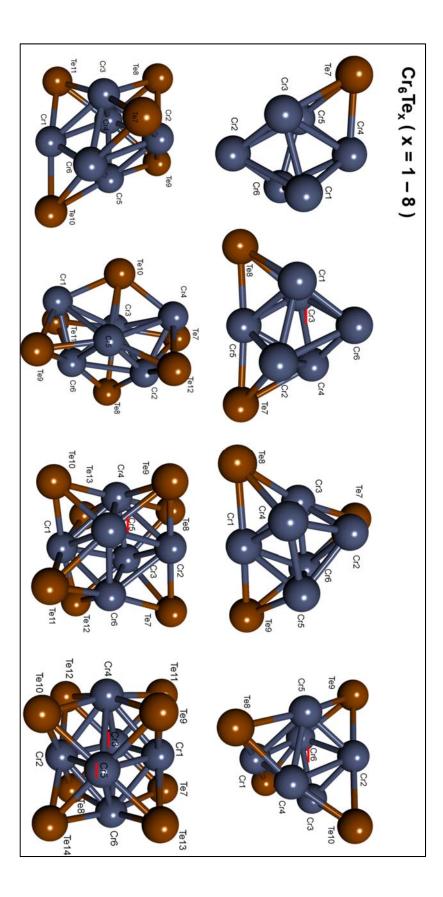
31		32		33		34		35	
Cr1 - Cr2	2.921	Cr1 - Cr2	2.353	Cr1 - Cr2	1.821	Cr3 - Cr1	2.829	Cr1 - Cr2	2.85981
Cr1 - Cr3	2.312	Cr1 - Cr3	2.978	Cr1 - Cr3	2.846	Cr3 - Cr2	2.421	Cr1 - Cr3	2.45729
Cr2 - Cr3	2.312	Cr3 - Cr2	2.357	Cr3 - Cr2	2.839	Cr2 - Cr1	2.424	Cr2 - Cr3	2.60359
Te4 - Cr2	2.594	Cr1 - Te4	2.662	Cr1 - Te4	2.544	Cr1 - Te5	2.556	Cr2 - Te5	2.71205
Te4 - Cr3	2.903	Cr3 - Te4	2.661	Cr1 - Te6	2.671	Cr3 - Te5	2.552	Cr2 - Te7	2.71205
Te4 - Cr1	2.594	Cr2 - Te4	2.727	Cr2 - Te6	2.677	Te6 - Cr3	2.641	Cr3 - Te5	2.66934
		Te5 - Cr3	2.663	Cr3 - Te6	2.656	Te6 - Cr2	2.643	Cr3 - Te7	2.72974
		Te5 - Cr1	2.661	Te5 - Cr1	2.658	Te6 - Cr1	2.638	Te4 - Cr1	2.60034
		Te5 - Cr2	2.726	Te5 - Cr3	2.675	Te4 - Cr1	2.502	Te4 - Cr2	2.57278
				Te5 - Cr2	2.653	Te4 - Cr2	2.675	Te5 - Te7	2.74759
				Te4 - Cr2	2.537	Te7 - Cr3	2.503	Te6 - Cr1	2.66167
						Te7 - Cr2	2.668	Te6 - Cr2	2.64475
								Te6 - Cr3	2.64333
								Te8 - Cr1	2.62958
								T-8 - C+2	3 51534



41		42		43	
Cr1 - Cr3	2.841	Cr2 - Cr3	3.014	Cr1 - Cr3	2.745
Cr2 - Cr3	2.331	Cr2 - Cr1	2.270	Cr1 - Cr4	2.409
Cr2 - Cr4	2.690	Cr1 - Cr3	2.465	Cr2 - Cr1	2.460
Cr4 - Cr1	2.330	Cr4 - Cr2	2.372	Cr2 - Cr4	2.748
Cr2 - Cr1	2.327	Cr4 - Cr3	2.273	Cr3 - Cr2	2.238
Cr4 - Cr3	2.328	Cr1 - Cr4	3.014	Cr3 - Cr4	2.460
Te5 - Cr2	2.746	Te5 - Cr2	2.791	Cr1 - Te7	2.575
Te5 - Cr4	2.748	Te5 - Cr1	2.610	Cr2 - Te6	2.716
Te5 - Cr1	2.640	Te5 - Cr4	2.666	Cr3 - Te6	2.675
		Cr4 - Te6	2.791	Cr4 - Te6	2.650
		Cr2 - Te6	2.670	Te5 - Cr1	2.651
		Cr3 - Te6	2.605	Te5 - Cr2	2.674
				Te5 - Cr3	2.717
				Te7 - Cr4	2.576
44		45		46	
Cr1 - Cr3	2.850	Cr1 - Cr3	2.931	Cr1 - Cr3	2.277
Cr2 - Cr1	2.852	Cr2 - Cr1	2.928	Cr1 - Cr2	2.465
Cr2 - Cr3	2.847	Cr2 - Cr4	2.354	Cr3 - Cr2	2.575
Cr3 - Cr4	2.449	Cr3 - Cr2	2.819	Cr4 - Cr3	2.275
Cr4 - Cr1	2.458	Cr3 - Cr4	2.362	Cr4 - Cr1	2.320
Cr4 - Cr2	2.450	Cr4 - Cr1	2.751	Cr4 - Cr2	2.467
Te5 - Cr2	2.648	Cr2 - Te5	2.688	Cr2 - Te8	2.505
Te5 - Cr3	2.643	Cr2 - Te6	2.670	Cr4 - Te8	2.526
Te5 - Cr4	2.704	Cr3 - Te9	2.691	Te5 - Cr2	2.506
Te6 - Cr1	2.648	Cr4 - Te5	2.717	Te5 - Cr1	2.527
Te6 - Cr2	2.647	Cr4 - Te9	2.713	Te7 - Cr1	2.510
Te6 - Cr4	2.700	Te6 - Cr1	2.594	Te7 - Cr4	2.511
Te7 - Cr1	2.644	Te6 - Cr4	2.717	Te10 - Cr4	2.509
Te7 - Cr3	2.649	Te7 - Cr1	2.593	Te10 - Cr3	2.516
Te7 - Cr4	2.704	Te7 - Cr3	2.673	Te6 - Cr1	2.509
	2.654	Te7 - Cr4	2.715	Te6 - Cr3	2.516
Te8 - Cr1	2.652	Te8 - Cr1	2.653	Cr3 - Te9	2.532
Te8 - Cr1 Te8 - Cr2			2 600	Cr2 - Te9	2.511
	2.652	Te8 - Cr2	2.688	C12 - 169	2.2.4
Te8 - Cr2		Te8 - Cr2 Te8 - Cr3	2.686	012 - 109	2.011



51		52		53		54		20		50		57	
Cr2 - Cr1	2.83986	Cr1 - Cr3	2.780	Cr1 - Cr3	2.817	Cr1 - Cr5	2.332	Cr2 - Cr3	2.826	Cr2 - Cr5	3.296	Cr2 - Cr3	2.61
Cr1 - Cr3	2.83067	Cr1 - Cr4	2.299	Cr1 - Cr4	2.370	Cr2 - Cr1	2.836	Cr2 - Cr4	2.881	Cr2 - Cr3	3.016	Cr2 - Cr4	2.76
Cr2 - Cr3	2.8433	Cr3 - Cr4	2.306	Cr3 - Cr2	2.803	Cr2 - Cr3	2.457	Cr2 - Cr5	2.770	Cr3 - Cr1	2.482	Cr2 - Cr5	2.602
Cr4 - Cr1	2.41487	Cr5 - Cr4	2.421	Cr3 - Cr4	2.454	Cr4 - Cr1	2.390	Cr3 - Cr4	2.740	Cr5 - Cr1	2.836	Cr3 - Cr1	2.92
Cr4 - Cr2	2.27203	Cr2 - Cr5	2.253	Cr5 - Cr1	2.467	Cr4 - Cr2	2.249	Cr3 - Cr1	2.887	Cr2 - Cr1	3.287	Cr3 - Cr4	2.58
Cr4 - Cr3	2.41858	Cr2 - Cr1	2.443	Cr3 - Cr5	2.467	Cr3 - Cr1	2.539	Cr3 - Cr5	2.056	Cr5 - Cr3	2.488	Cr3 - Cr5	2.85
Cr2 - Cr5	2.39858	Cr2 - Cr3	2.448	Cr5 - Cr2	2.376	Cr4 - Cr3	2.656	Cr5 - Cr1	2.749	Cr3 - Cr4	3.149	Cr4 - Cr1	2.96
Cr3 - Cr5	2.33463	Cr5 - Cr3	2.753	Cr2 - Cr4	2.464	Cr3 - Cr5	2.778	Cr4 - Cr1	2.225	Cr1 - Cr4	3.128	Cr4 - Te9	2.76
Crl - Cr5	2.33464	Cr5 - Cr1	2.750	Cr3 - Te8	2.647	Cr4 - Cr5	2.972	Cr5 - Cr4	2.637	Cr5 - Cr4	3.129	Cr5 - Cr1	2.92
Te6 - Cr1	2.656	Cr5 - Te6	2.704	Cr4 - Te6	2.739	Cr1 - Te7	2.670	Te7 - Cr4	2.625	Te6 - Cr5	2.819	Cr5 - Cr4	2.58
Te6 - Cr3	2.654	Cr2 - Te6	2.727	Cr2 - Te6	2.741	Cr3 - Te7	2.619	Te7 - Cr2	2.655	Cr2 - Te6	2.593	Te10 - Cr1	2.54
Te6 - Cr5	2.787	Te7 - Cr1	2.650	Cr5 - Te6	2.744	Cr5 - Te7	2.645	Te7 - Cr5	2.657	Te6 - Cr1	2.815	Te10 - Cr4	2.76
		Te7 - Cr2	2.725	Cr1 - Teó	2.745	Te8 - Cr2	2.654	Cr5 - Te9	2.683	Cr1 - Te10	2.805	Te10 - Cr5	2.72
		Te7 - Cr5	2.707	Te7 - Cr5	2.715	Te8 - Cr3	2.491	Cr3 - Te9	2.644	Cr5 - Te10	2.799	Tel1 - Cr1	2.53
		Teo - Cr3	2.652	Te7 - Cr2	2.706	Cr3 - Te9	2.668	Te9 - Cr1	2.680	Te10 - Cr4	2.588	Tel1 - Cr3	2.74
				Cr3 - Te7	2.652	Cr4 - Te9	2.645	Te6 - Cr4	2.471	Cr4 - Te7	2.568	Tell - Cr5	2.74
				Te8 - Cr1	2.705	Te9 - Cr5	2.652	Te6 - Cr1	2.687	Cr3 - Te7	2.806	Te12 - Cr2	2.65
				Te8 - Cr4	2.719	Te6 - Cr4	2.648	Te10 - Cr2	2.677	Crl - Te7	2.783	Te12 - Cr3	2.74
						Te6 - Cr2	2.700	Te10 - Cr4	2.604	Te9 - Cr3	2.787	Te6 - Cr2	2.6
						Te6 - Cr1	2.667	Te10 - Cr3	2.695	Te9 - Cr2	2.589	Te6 - Cr5	2.74
								Te8 - Cr5	2.662	Te9 - Cr1	2.752	Te6 - Te12	2.81
								Te8 - Cr2	2.629	Tel1 - Cr2	2.589	Te7 - Cr2	2.58
								Te8 - Cr3	2.643	Tell - Cr3	2.787	Te7 - Cr4	2.75
										Tell - Cr5	2.751	Te7 - Cr5	2.70
										Cr5 - Te8	2.780	Te8 - Cr2	2.58
										Cr3 - Te8	2.804	Te8 - Cr3	2.70
										Te8 - Cr4	2.567	Te8 - Cr4	2.75
												Te9 - Cr1	2.53
												Te9 - Cr3	2.72



2.659	Tell - Crl														
2.633	Tell - Cr3														
2.66	Cr4 - Tel1														
2.659	Te9 - Cr1	2.573	Te9 - Cr5												
2.633	Te9 - Cr5	2.782	Te9 - Cr4												
2.661	Te9 - Cr4	2.691	Te8 - Cr4	2.688	Cr6 - Tel1										
2.633	Te13 - Cr5	2.672	Te8 - Cr3	2.644	Cr5 - Te9										
2.659	Te13 - Cr1	2.619	Te8 - Cr2	2.889	Cr3 - Te8										
2.66	Te13 - Cr6	2.606	Te7 - Cr6	2.757	Cr3 - Tel1										
2.66	Te7 - Cr6	2.844	Te7 - Cr3	2.673	Te9 - Cr5	2.791	Te9 - Cr4								
2.65	Te7 - Cr1	2.573	Te7 - Cr2	2.650	Te9 - Crl	2.569	Te9 - Cr5								
2.63	Te7 - Cr3	2.665	Te13 - Cr1	2.606	Te8 - Cr6	2.707	Te9 - Cr2								
2.65	Te14 - Cr2	2.597	Te12 - Cr6	2.606	Te8 - Cr2	2.652	Te8 - Cr3	2.701	Cr5 - Te8						
2.661	Cr6 - Te14	2.699	Te12 - Cr3	2.577	Te7 - Cr4	2.633	Te8 - Cr2	2.637	Cr1 - Te8						
2.63	Cr5 - Tel4	2.656	Te12 - Cr1	2.759	Te7 - Cr3	2.695	Te8 - Cr4	2.639	Te8 - Cr4						
2.63	Cr3 - Te12	2.713	Tell - Crl	2.687	Te7 - Cr2	2.648	Te11 - Cr1	2.676	Cr4 - Te10	2.687	Cr4 - Te8				
2.63	Te8 - Cr3	2.640	Te10 - Cr5	2.644	Te12 - Cr5	2.652	Cr4 - Te11	2.674	Cr3 - Te10	2.666	Te9 - Cró				
2.65	Te8 - Cr2	2.678	Te10 - Cr1	2.648	Te12 - Cr4	2.692	Cr3 - Te11	2.637	Cr2 - Te10	2.661	Te9 - Cr5				
2.66	Te8 - Cr6	2.602	Cr6 - Te11	2.670	Te12 - Cr2	2.661	Tel0 - Cr5	2.647	Cr6 - Te7	2.693	Te9 - Cr1	2.651	Cr2 - Te7		
2.66	Te12 - Cr4	2.676	Cr5 - Tell	2.576	Te11 - Cr1	2.636	Te10 - Cr1	2.719	Te7 - Cr3	2.651	Te8 - Cr3	2.777	Cr4 - Te7		
2.65	Te12 - Cr2	2.645	Cr4 - Te13	2.787	Te10 - Cr5	2.659	Cr6 - Te10	2.680	Te9 - Cr6	2.707	Te8 - Cr1	2.667	Cr5 - Te7		
2.65	Te10 - Cr2	2.643	Cr4 - Te10	2.659	Te10 - Cr4	2.646	Te7 - Cr6	2.626	Te9 - Cr2	2.622	Te7 - Cr6	2,672	Cr5 - Te8	2.755	Te7 - Cr3
2.633	Tel0 - Cr5	2.672	Cr3 - Te13	2.785	Te10 - Cr3	2.683	Te7 - Cr3	2.681	Te9 - Cr5	2.665	Te7 - Cr3	2.776	Cr1 - Te8	2,650	Te7 - Cr4
2.66	Cr4 - Te10	2.648	Cr2 - Te9	2.660	Te10 - Cr1	2.645	Te7 - Cr2	2.636	Te7 - Cr1	2.768	Te7 - Cr2	2.648	Cr3 - Te8	2.681	Te7 - Cr5
2.764	Cr2 - Cr4	2.649	Cr6 - Cr5	2.574	Cr5 - Cr6	2.824	Cr2 - Cr6	2.562	Cr5 - Cr4	2.387	Cr6 - Cr3	2.300	Cr3 - Cr5	2.744	Cr5 - Cr2
2.76	Cr6 - Cr2	2.593	Cr6 - Cr1	2.581	Cr5 - Cr2	2.566	Cr2 - Cr3	2.720	Cr2 - Cr4	2.552	Cr6 - Cr1	2.700	Cr6 - Cr3	2.251	Cr6 - Cr2
2.53	Cr3 - Cr2	2.776	Cr5 - Cr1	2.851	Cr5 - Cr1	2.631	Cr2 - Cr5	2.553	Cr3 - Cr4	2.666	Cr5 - Cr6	2.706	Cr4 - Cr5	2.429	Cr3 - Cr2
2.53	Cr2 - Cr5	2.454	Cr4 - Cr5	2.850	Cr4 - Cr5	2.876	Cr2 - Cr4	2.554	Cr6 - Cr3	2.326	Cr5 - Cr1	2.512	Cr4 - Cr3	2.806	Cr6 - Cr4
2.76	Cr1 - Cr6	2.785	Cr4 - Cr1	2.926	Cr4 - Cr3	2.372	Cr5 - Cr6	2.719	Cr6 - Cr2	2.706	Cr4 - Cr5	2.706	Cr6 - Cr2	2.519	Cr5 - Cr6
2.53	Cr1 - Cr5	2.507	Cr3 - Cr6	2.553	Cr4 - Cr2	2.659	Cr3 - Cr6	2.525	Cr6 - Cr5	2.475	Cr4-Cr1	2.328	Cr6 - Cr1	2.878	Cr4 - Cr3
2.76	Cr1 - Cr4	2.714	Cr3 - Cr4	2.954	Cr6 - Cr2	2.459	Cr4 - Cr3	2.314	Cr6 - Cr1	2.286	Cr3 - Cr4	2.323	Cr4 - Cr6	2.307	Cr5 - Cr4
2.539	Cr1 - Cr3	2.836	Cr3 - Cr1	2.450	Cr3 - Cr6	2.551	Cr5 - Cr4	2.464	Cr2 - Cr3	2.744	Cr3 - Cr1	2.296	Cr2 - Cr5	2.342	Cr5 - Cr3
2.835	Cr3 - Cr6	2.788	Cr2 - Cr6	2.923	Cr3 - Cr5	2.864	Cr4 - Cr1	2.437	Cr2 - Cr5	2.327	Cr2 - Cr6	2.317	Cr4 - Cr2	2.867	Cr1 - Cr2
2.83	Cr5 - Cr6	2.693	Cr2 - Cr5	2.927	Cr3 - Cr1	2.760	Cr3 - Cr1	2.332	Cr1 - Cr4	2.356	Cr2 - Cr5	2.515	Cr2 - Cr1	2.371	Cr1 - Cr4
2.835	Cr4 - Cr5	2.781	Cr2 - Cr4	2.455	Cr2 - Cr3	2.359	Cr6 - Cr1	2.725	Cr1 - Cr3	2.432	Cr2 - Cr4	2.322	Cr1 - Cr3	2.421	Cr1 - Cr6
2.835	Cr3 - Cr4	2.561	Cr2 - Cr3	2.556	Cr1 - Cr6	2.734	Cr5 - Cr1	2.723	Cr1 - Cr5	2.661	Cr2 - Cr3	2.704	Cr1 - Cr5	2.489	Cr1 - Cr3

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