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Stabilizing the Higgs potential with a Z^\prime

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ABSTRACT

Current data point toward metastability of the electroweak vacuum within the Standard Model. We study the possibility of stabilizing the Higgs potential in U(1) extensions thereof. A generic Z' boson improves stability of the scalar potential in two ways: it increases the Higgs self-coupling, due to a positive contribution to the beta-function of the latter, and it decreases the top quark Yukawa coupling, which again has a stabilizing effect. We determine the range of U(1) charges which leads to a stable electroweak vacuum. In certain classes of models, such stabilization is possible even if the Z' does not couple to the Higgs and is due entirely to the reduction of the top Yukawa coupling. We also study the effect of the kinetic mixing between the extra U(1) and hypercharge gauge fields.

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1. Introduction

The current preferred values of the Higgs and top quark masses imply that the Higgs quartic coupling turns negative at some intermediate scale, signifying metastability of our electroweak vacuum [1–3]. Although this is not problematic from the low energy perspective, it may lead to difficulties in reconciling the Standard Model (SM) with inflation, which entails large values for scalar fields in the Early Universe. Given the existence of a deep minimum at large Higgs values, the Universe is overwhelmingly likely to evolve to that catastrophic vacuum [4].

This problem can be efficiently addressed by coupling the Higgs to the inflaton [5] thereby modifying the Higgs potential during inflation, yet other stabilizing mechanisms are worth considering. The simplest possibility is to introduce a real [6,7] or complex [8] scalar which couples to the Higgs and makes the scalar potential convex. In this work, we consider the next simplest option: introducing an extra U(1) symmetry [9–11]. The presence of an extra U(1) gauge boson generally has a stabilizing effect on the potential due the positive contribution to the beta-function of the Higgs quartic coupling. We also find an additional positive effect: the top Yukawa coupling decreases with energy and therefore does not reduce the Higgs self-coupling as much as it does in the SM. In the framework of a generic U(1), we identify the main parameters responsible for the stabilization and consequently delineate our parameter space.

To be as general as possible, we avoid working with specific charge assignments, rather we single out important combinations thereof which make the main impact. We allow the "hidden" sector fields to be charged only under the extra U(1). When one assumes a generation-independent charge assignment, anomaly-free models of this type can be parametrized in terms of two parameters [12]. For our purposes this is not essential and our considerations apply to more general models. For example, the charges are allowed to be generation-dependent, if the corresponding Z' is sufficiently heavy, in the range of a few TeV [13]. Also, the extra U(1) may appear anomalous from the low energy perspective: its anomaly can be cancelled, though, by transforming a dilaton-like field, as in the Green–Schwarz mechanism [14]. Such models are ubiquitous in realistic string constructions [15]. Therefore, we will not impose explicitly the U(1) anomaly cancellation conditions and focus on a few charges, essential for our purposes, or combinations thereof.

In what follows, we present the renormalization group equations for the relevant couplings and determine regions of parameter space consistent with stability of the Higgs potential, perturbativity, as well as the experimental constraints on a Z'.

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2. Z' framework

We study extensions of the SM with the gauge group $G_{SM} \times U(1)'$ and additional SM singlet fields, both scalars and fermions. The SM fields generally carry charges under the extra U(1) as do the SM singlets. Allowing for a kinetic mixing between the U(1) and the hypercharge [16], we take the Lagrangian to be of the form

$$\mathcal{L} = \mathcal{L}_{SM} + g_4 B'_{\mu} \sum_{i} Q_i \,\overline{\psi}_{SM_i} \gamma^{\mu} \,\psi_{SM_i} + \sum_{i} D'_{\mu} S^*_i \,D'^{\mu} S_i - \frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} - \frac{\epsilon}{2} F^Y_{\mu\nu} F'^{\mu\nu} + \sum_{i} \overline{\chi}_i (i\partial_{\mu} + g_4 Q'_i B'_{\mu}) \gamma^{\mu} \chi_i \,, \tag{1}$$

where

$$D'_{\mu} = \partial_{\mu} - ig_4 Q' B'_{\mu} , \qquad (2)$$

and B'_{μ} and g_4 are the extra gauge field and its coupling. Here S_i and χ_i are the SM singlet scalars and fermions, respectively; Q_i and Q'_i are the U(1) charges of the SM chiral fermions ψ_{SM_i} and the SM singlets, respectively.

We will further assume the scalar interaction between the Higgs field and the SM singlets as well as the singlet self-interaction to be small:

$$\Delta V = \frac{1}{4} \sum_{ij} \lambda_{s_i s_j} S_i^* S_i S_j^* S_j + \frac{1}{4} \sum_i \lambda_{h s_i} H^{\dagger} H S_i^* S_i ,$$

with $\lambda_{s_i s_j}$, $\lambda_{h s_i} \ll 1$. Also we neglect effects of possible Yukawa couplings in the hidden sector. These assumptions are not crucial, but they allow us to focus on the effects due to gauge interactions. The (stabilizing) effect of the Higgs-portal couplings has been studied elsewhere (see for example [6]).

The extra U(1) gets broken by one or more vacuum expectation values (VEVs) of the singlets

$$\langle S_i \rangle \neq 0. \tag{3}$$

We will not need the specifics of this breaking, except we will assume a single scale at which the hidden sector activates and starts contributing to the RG equations for the SM couplings and g_4 . This scale is associated with the gauge boson (Z') mass. In general, one expects kinetic mixing between the Z' and the Z. Phenomenology of Z' models has been reviewed in [17,18].

3. Synopsis of constraints

In this section, we summarize the most important experimental constraints on a Z' as well as theoretical constraints we impose on our models.

• Bounds from LEP

LEP has set constraints on effective operators of the type

$$\frac{g_{Z'}(i) g_{Z'}(j)}{m_{Z'}^2} \bar{f}_i \gamma^{\mu} f_i \bar{f}_j \gamma_{\mu} f_j \tag{4}$$

for leptons $f_{i,j}$ of various chiralities with the Z' couplings $g_{Z'}(i)$, $g_{Z'}(j)$. The strongest bound is set on the vector-vector interactions [19]:

$$\frac{m_{Z'}}{\sqrt{g_{Z'}(i) g_{Z'}(j)}} > 6.1 \text{ TeV} \,.$$
(5)

Constraints on lepton-quark interactions are somewhat weaker and no useful bounds exist for a leptophobic Z'.

• Bounds from LHC

1. *General couplings*. The most important bounds come from the CMS and ATLAS searches for dileptons with a large invariant mass, which result from $q\bar{q} \rightarrow Z' \rightarrow l^+l^-$. We will use the CMS result [20] as our benchmark constraint. For a sequential Z', that is a Z' with the couplings of the Z boson, the bound is around

$$m_{Z'_{\text{seq}}} > 2.6 \text{ TeV}$$
 (6)

For a more general case, one needs to take into account both the difference in the couplings of the Z' and the Z, and the reduction in the "visible" decay branching ratio due to the presence of new states [21]:

$$\sigma_{l^+l^-} \to \left(\frac{g_{Z'}}{g_Z}\right)^2 \mathsf{BR}_{\mathsf{vis}} \,\sigma_{l^+l^-} \,, \tag{7}$$

where

$$BR_{vis} \simeq \frac{\sum_{i} g_{Z'}(i)^2}{\sum_{i} g_{Z'}(i)^2 + \sum_{\chi_i} g_{Z'}(\chi_i)^2}$$
(8)

with $g_{Z'}(i)$ and $g_{Z'}(\chi_i)$ representing the couplings of the SM and extra fermions, respectively, into which the Z' can decay.¹ As a result, the bound of 2.6 TeV can be relaxed and in some cases becomes as low as 500 GeV [22]. For our applications, we will typically take $m_{Z'} \sim 3$ TeV to be on the safe side.

2. Leptophobic Z'. The bounds on a Z' relax significantly if it does not couple to the leptons. Taking the Z' couplings to be of the electroweak size, for $m_{Z'} > 2m_t$, the typical bounds are around 1 TeV. However, if $m_{Z'} < 2m_t$, the constraints become very weak and the Z' mass in the electroweak range is allowed. A detailed analysis of this issue can be found in [23].

• Stability of the Higgs potential

This is a theoretical bound that we choose to impose,

 $\lambda_h > 0$

(9)

at all scales up to the Planck scale. This ensures that the electroweak minimum is stable. (Here we ignore possible complications associated with the SM singlet directions in the scalar potential: we choose the couplings λ_{hs_i} and λ_{s_i} such that such issues do not arise.)

• Perturbativity

Assuming that the Z' framework is valid up to the Planck scale, one must ensure perturbativity in this scale range. In practice, we impose the condition

$$g_4^2, \lambda_i < 4\pi \tag{10}$$

at the Planck scale, although the allowed parameter space is not sensitive to the exact value of the upper bound as long as it is O(1).

4. RG evolution of the couplings

4.1. The non-diagonal basis

Following the method of [24], we have derived the Renormalization Group Equations (RGEs) for the class of models in question. Given the substantial uncertainties associated with the top-quark mass, for our purposes it suffices to use the 1-loop RGEs for most couplings. In the beta function of g_4 however, we take into account the gauge two-loop contribution proportional to g_4^5 . This is because g_4 becomes substantial in certain regions of parameter space we explore and the two-loop term may be relevant. In general, neglecting the kinetic mixing contributions, two-loop corrections can be incorporated using the numerical tool of [25].

Below we show the equations for the case of a single S and a single chiral fermion χ . In the general case, one replaces²

$$Q_S^2 \to \sum_i Q_{S_i}^2, \quad Q_\chi^2 \to \sum_i Q_{\chi_i}^2.$$
⁽¹¹⁾

This is due to the fact that *S* and χ do not couple to the SM gauge fields and their (additive) contributions are proportional to the charge squared. Therefore, in our discussion it is understood that Q_S^2 and Q_{χ}^2 represent the sums over different species. Furthermore, in the RG equations for g_4 and ϵ , we have also set the U(1) charges to be generation-independent. This can again be trivially generalized.

In the non-diagonal basis, i.e. the basis allowing for the kinetic mixing ϵ , we find

$$16\pi^{2}\frac{d\lambda_{h}}{dt} = \lambda_{h} \left(-9g_{2}^{2} - 12\zeta g_{4}^{2}Q_{h}^{2} + 12\zeta g_{4}\epsilon g_{Y}Q_{h} - 3\zeta g_{Y}^{2} + 24\lambda_{h} + 12y_{t}^{2}\right) + \frac{3}{8}\zeta^{2}g_{Y}^{4} + \frac{3}{4}\zeta g_{2}^{2}g_{Y}^{2} + \frac{9}{8}g_{2}^{4} + \lambda_{hs}^{2} - 6y_{t}^{4} + 6\zeta^{2}g_{4}^{4}Q_{h}^{4} - 12\zeta^{2}g_{4}^{3}\epsilon g_{Y}Q_{h}^{3} + 3\zeta g_{4}^{2}g_{2}^{2}Q_{h}^{2} + 3\zeta^{2}g_{4}^{2}g_{Y}^{2}Q_{h}^{2} + 6\zeta^{2}g_{4}^{2}\epsilon^{2}g_{Y}^{2}Q_{h}^{2} - 3\zeta^{2}g_{4}\epsilon g_{Y}^{3}Q_{h} - 3\zeta g_{4}g_{2}^{2}\epsilon g_{Y}Q_{h},$$

$$16\pi^{2}\frac{d\lambda_{s}}{ds} = 6\zeta^{2}g_{4}^{4}Q_{S}^{4} - 12\zeta g_{4}^{2}Q_{S}^{2}\lambda_{s} + 2\lambda_{hs}^{2} + 20\lambda_{s}^{2},$$

$$\begin{aligned} dt &= y_{1} g_{4}^{2} e_{3}^{2} g_{4}^{2} e_{3}^{2} g_{5}^{4} e_{3}^{2} g_{5}^{2} e_{4}^{2} g_{5}^{2} \\ &= \lambda_{hs} \left(-6\zeta g_{4}^{2} Q_{h}^{2} + 6\zeta g_{4} \epsilon g_{Y} Q_{h} - \frac{9}{2} g_{2}^{2} - 6\zeta g_{4}^{2} Q_{s}^{2} - \frac{3}{2} \zeta g_{Y}^{2} + 12\lambda_{h} + 8\lambda_{s} + 6y_{t}^{2} \right) \\ &\quad + 4\lambda_{hs}^{2} + 12\zeta^{2} g_{4}^{4} Q_{h}^{2} Q_{s}^{2} - 12\zeta^{2} g_{4}^{3} \epsilon g_{Y} Q_{h} Q_{s}^{2} + 3\zeta^{2} g_{4}^{2} \epsilon^{2} g_{Y}^{2} Q_{s}^{2} , \\ &16\pi^{2} \frac{dy_{t}}{dt} = y_{t} \left(-3\zeta g_{4}^{2} Q_{q}^{2} + \zeta g_{4} \epsilon g_{Y} Q_{q} - 3\zeta g_{4}^{2} Q_{t}^{2} + 4\zeta g_{4} \epsilon g_{Y} Q_{t} - \frac{17}{12} \zeta g_{Y}^{2} - \frac{9}{4} g_{2}^{2} - 8g_{3}^{2} + \frac{9}{2} y_{t}^{2} \right) , \\ &16\pi^{2} \frac{dg_{4}}{dt} = g_{4}^{3} \left(6Q_{b}^{2} + \frac{2}{3} Q_{h}^{2} + 4Q_{l}^{2} + 12Q_{q}^{2} + \frac{1}{3} Q_{s}^{2} + 6Q_{t}^{2} + 2Q_{\tau}^{2} + \frac{2}{3} Q_{\chi}^{2} \right) \\ &\quad + \frac{1}{16\pi^{2}} \left(18Q_{b}^{4} + 8Q_{h}^{4} + 12Q_{l}^{4} + 36Q_{q}^{4} + 4Q_{s}^{4} + 18Q_{t}^{4} + 6Q_{\tau}^{4} + 2Q_{\chi}^{4} \right) g_{4}^{5} , \end{aligned}$$

¹ For simplicity we assume that the decay into the scalars is not allowed kinematically.

² In the gauge two loop contribution to g_4 , one replaces $Q_S^4 \rightarrow \sum_i Q_{S_i}^4$, $Q_{\chi}^4 \rightarrow \sum_i Q_{\chi_i}^4$.

$$16\pi^{2}\frac{d\epsilon}{dt} = \epsilon \left(\frac{2}{3}Q_{h}^{2} + 4Q_{l}^{2} + 12Q_{q}^{2} + 6Q_{b}^{2} + \frac{1}{3}Q_{S}^{2} + 6Q_{t}^{2} + 2Q_{\tau}^{2} + \frac{2}{3}Q_{\chi}^{2}\right)g_{4}^{2} + \epsilon \frac{41}{6}g_{Y}^{2} + g_{4}g_{Y}\left(4Q_{b} - \frac{2}{3}Q_{h} + 4Q_{l} - 4Q_{q} - 8Q_{t} + 4Q_{\tau}\right),$$
(12)

where $t = \ln(\mu/m_t)$ is the RG evolution variable and $\zeta = 1/(1 - \epsilon^2)$. The SM gauge coupling RGEs are

$$16\pi^{2} \frac{dg_{Y}}{dt} = \frac{41}{6} g_{Y}^{3} ,$$

$$16\pi^{2} \frac{dg_{2}}{dt} = -\frac{19}{6} g_{2}^{3} ,$$

$$16\pi^{2} \frac{dg_{3}}{dt} = -7g_{3}^{3} ,$$

(13)

with the boundary values given in [6]. The notation for the U(1) charges is straightforward: $Q_{t,b,\tau}$ are the charges for the right-handed fermions, while $Q_{q,l}$ are those for the left-handed fermions. As mentioned above, here we set them to be generation-independent.

The main new contribution to the running of λ_h is due to the positive terms proportional to g_4^2 and g_4^4 (unless ϵ is large). Also y_t receives a new contribution with a definite sign: the g_4^2 -terms reduce the top Yukawa coupling. Both of these effects increase λ_h and tend to stabilize the Higgs potential.

Let us note that λ_{hs} and λ_s are generated by the RG evolution even if their initial values are zero. However, their numerical impact on the evolution of λ_h is not very significant in this case.

4.2. Basis change

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It is often more convenient to work with the gauge fields which are orthogonal at any energy scale. The kinetic mixing term $\frac{\epsilon}{2}F_{\mu\nu}^{Y}F'^{\mu\nu}$ in the Lagrangian can be rotated away so that there is no mixing between B^{Y} and B' (see e.g. [26]). This is achieved by the (RG scaledependent) transformation

$$F^{Y} \to \tilde{F}^{Y} - \frac{\epsilon \tilde{F'}}{\sqrt{1 - \epsilon^{2}}}, \qquad F' \to \frac{\tilde{F'}}{\sqrt{1 - \epsilon^{2}}},$$
(14)

which leads to canonically normalized gauge fields. The covariant derivative now contains the term:

$$g_Y Y \tilde{B}^Y + \left(-\frac{\epsilon g_Y}{\sqrt{1-\epsilon^2}}Y + \frac{g_4}{\sqrt{1-\epsilon^2}}Q\right)\tilde{B}', \qquad (15)$$

which describes the relevant gauge interactions in the diagonal basis. Defining the new coupling \tilde{g} and redefining g_4 by

$$\tilde{g} = -\frac{\epsilon g_Y}{\sqrt{1 - \epsilon^2}}, \qquad \frac{g_4}{\sqrt{1 - \epsilon^2}} \to g_4,$$
(16)

one can rewrite the RG equations in this diagonal basis. Note that no assumption on the smallness of ϵ has been made so far.

4.3. The diagonal basis

In terms of the redefined couplings, the RG equations read:

$$\begin{split} 16\pi^2 \frac{d\lambda_h}{dt} &= -6y_t^4 - 3\left(g_1^2 + 3g_2^2 + \tilde{g}^2 - 8\lambda_h - 4y_t^2\right)\lambda_h + \frac{3}{4}g_1^2 \tilde{g}^2 + \frac{3}{4}g_2^2 \tilde{g}^2 + \frac{3}{8}\tilde{g}^4 + \frac{3}{8}g_1^4 + \frac{9}{8}g_2^4 + \frac{3}{4}g_1^2 g_2^2 + \lambda_{hs}^2 \right) \\ &\quad + 3Q_h \left(g_1^2 + g_2^2 + \tilde{g}^2 - 4\lambda_h + 4Q_h^2 g_4^2\right)g_4 \tilde{g} + 3Q_h^2 \left(g_1^2 + g_2^2 + 3\tilde{g}^2 - 4\lambda_h + 2Q_h^2 g_4^2\right)g_4^2 , \\ 16\pi^2 \frac{d\lambda_s}{dt} &= -12g_4^2 Q_5^2 \lambda_s + 6g_4^4 Q_5^4 + 2\lambda_{hs}^2 + 20\lambda_s^2 , \\ 16\pi^2 \frac{d\lambda_{hs}}{dt} &= \left(6y_t^2 + 8\lambda_s + 4\lambda_{hs} + 12\lambda_h - \frac{3}{2}\tilde{g}^2 - \frac{3}{2}g_1^2 - \frac{9}{2}g_2^2\right)\lambda_{hs} \\ &\quad - 6g_4 \left(\tilde{g}Q_h + g_4 Q_h^2 + g_4 Q_s^2\right)\lambda_{hs} + 3g_4^2 \left(\tilde{g}^2 + 4g_4 \tilde{g}Q_h + 4g_4^2 Q_h^2\right)Q_s^2 , \\ 16\pi^2 \frac{dg_4}{dt} &= \frac{41}{6}g_4 \tilde{g}^2 + \left(-4Q_b + \frac{2}{3}Q_h - 4Q_l + 4Q_q + 8Q_t - 4Q_\tau\right)g_4^2 \tilde{g} \\ &\quad + \left(\overline{6Q_b^2 + \frac{2}{3}}Q_h^2 + 4Q_l^2 + 12Q_q^2 + \frac{1}{3}Q_s^2 + 6Q_t^2 + 2Q_\tau^2 + \frac{2}{3}Q_\chi^2\right)g_4^3 \\ &\quad + \frac{1}{16\pi^2} \left(18Q_b^4 + 8Q_h^4 + 12Q_l^4 + 36Q_q^4 + 4Q_s^4 + 18Q_t^4 + 6Q_\tau^4 + 2Q_\chi^4\right)g_5^5 , \end{split}$$

$$16\pi^{2}\frac{d\tilde{g}}{dt} = \frac{41}{6}\tilde{g}^{3} + \left(-4Q_{b} + \frac{2}{3}Q_{h} - 4Q_{l} + 4Q_{q} + 8Q_{t} - 4Q_{\tau}\right)g_{4}\tilde{g}^{2} + \frac{41}{3}g_{1}^{2}\tilde{g} + \left(6Q_{b}^{2} + \frac{2}{3}Q_{h}^{2} + 4Q_{l}^{2} + 12Q_{q}^{2} + \frac{1}{3}Q_{s}^{2} + 6Q_{t}^{2} + 2Q_{\tau}^{2} + \frac{2}{3}Q_{\chi}^{2}\right)g_{4}^{2}\tilde{g} + \left(-4Q_{b} + \frac{2}{3}Q_{h} - 4Q_{l} + 4Q_{q} + 8Q_{t} - 4Q_{\tau}\right)g_{1}^{2}g_{4}, 16\pi^{2}\frac{dy_{t}}{dt} = y_{t}\left(-g_{4}\tilde{g}(4Q_{t} + Q_{q}) - 3g_{4}^{2}(Q_{q}^{2} + Q_{t}^{2}) - \frac{17}{12}g_{1}^{2} - \frac{9}{4}g_{2}^{2} - 8g_{3}^{2} - \frac{17}{12}\tilde{g}^{2} + \frac{9}{2}y_{t}^{2}\right),$$

with the SM gauge coupling RGEs being the same as in Eq. (13). This result agrees with known special cases such as $U(1)_{B-L}$ [27]. We will mostly use these RG equations in our numerical analysis.

In the beta function of g_4 , the leading term for small Z–Z' mixing is associated with the combination of charges which we call Q_4^2 :

$$Q_4^2 \equiv 6Q_b^2 + \frac{2}{3}Q_h^2 + 4Q_l^2 + 12Q_q^2 + \frac{1}{3}Q_s^2 + 6Q_t^2 + 2Q_\tau^2 + \frac{2}{3}Q_\chi^2 .$$
⁽¹⁷⁾

Therefore, most of the individual charges do not matter for our analysis as long as Q_4 remains the same. The other two important quantities are Q_h and $Q_{t,q}$ for the third generation. The Higgs charge appears explicitly in the beta function for λ_h . Again, for small Z–Z' mixing, it only contributes as Q_h^2 . Similarly, the beta function of the top Yukawa coupling depends on $Q_{q,t}^2$ at leading order. Since Q_q for the third generation and Q_t are related by U(1) invariance of the Yukawa interaction, the essential parameters for our study are

$$Q_h^2, \ Q_{q_3}^2, \ Q_4^2.$$
 (18)

Although we have imposed generation-independent charges in the above equations, it is straightforward to adapt the RGE's to a nonuniversal case. Clearly, what matters for our purposes is the charge assignment for the top quark.

5. Stabilizing the Higgs potential via a U(1)'

The presence of an extra U(1) modifies the Higgs self-coupling λ_h at energies above the Z' mass scale. For small Z–Z' mixing, the effect is always positive. This is because the new contributions to the beta functions increase λ_h at high energies both through a direct one loop contribution to β_{λ_h} and by decreasing the top Yukawa coupling:

$$\Delta \beta_{\lambda_h} \propto g_4^2 Q_h^2 + c \ g_4^4 Q_h^4 ,$$

$$\Delta \beta_{y_t} \propto -g_4^2 (Q_q^2 + Q_t^2) .$$
(19)

(Here the proportionality coefficients are positive at m_t .) This is a general feature of Z' models. Therefore, additional U(1) symmetries tend to stabilize the Higgs potential. In what follows, we study the specifics of this effect.

Note also that the Higgs-singlet coupling has a stabilizing effect too: its contribution to β_{λ_h} is positive and proportional to λ_{hs}^2 . However, such a coupling is not specific to U(1)' models and we choose to minimize this effect by setting $\lambda_{hs} \ll 1$, $\lambda_s \ll 1$ at the electroweak scale. In order for the SM Yukawa couplings to be allowed, the U(1) charges must satisfy the constraints

$$Q_t = Q_q + Q_h, \quad Q_b = Q_q - Q_h, \quad Q_\tau = Q_l - Q_h.$$
 (20)

Eliminating the charges of right-handed fermions, Q₄ takes the form

$$Q_4^2 = \frac{44}{3}Q_h^2 + 24Q_q^2 + \frac{1}{3}Q_S^2 + \frac{2}{3}Q_\chi^2 + 6Q_l^2 - 4Q_hQ_l.$$
⁽²¹⁾

This combination of charges is responsible for most of the running of g_4 , which in turn affects λ_h as shown in Eq. (19).

Apart from their contribution to Q_4 , the remaining charges Q_S , Q_l , and Q_{χ} have very little effect on the running of λ_h . They enter the kinetic mixing and the 2-loop contributions, whose effect is clearly subdominant. Q_S also appears in the beta-functions of λ_s and λ_{hs} . Due to our boundary conditions $\lambda_{hs} \ll 1$, $\lambda_s \ll 1$, these couplings do not make a significant impact on λ_h . Therefore, Q_S affects stability of the Higgs potential almost entirely through Q_4 .

Also, the quark charges for the first two generations $Q_{q_{1,2}}$ are not relevant for our analysis. For clarity however, we make the universality assumption

$$Q_q = Q_{q_3} = Q_{q_{1,2}} . (22)$$

In what follows, we study the numerical impact of Q_h , Q_q and Q_4 .

5.1. Generic Z'

A generic Z' is subject to the strong LEP and LHC constraints of Section 3. For the Z' coupling of electroweak size, we choose $M_{Z'} = 3$ TeV as the reference point. That means we apply the RG equations of Section 4 above this scale, whereas below 3 TeV the running is SM-like. We choose three representative values $g_4 = 0.1$, 0.2, 0.3. For larger g_4 , the couplings become non-perturbative below the Planck scale (for order one charges). In this subsection, we set the kinetic mixing to zero at $M_{Z'}$, that is $\tilde{g}(M_{Z'}) = 0$, and focus entirely on the effect of g_4 .



Fig. 1. Charge assignments consistent with Higgs potential stability and perturbativity for $g_4 = 0.1$ (blue region), $g_4 = 0.2$ (yellow region) and $g_4 = 0.3$ (red region) at $M_{Z'} = 3$ TeV. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)



Fig. 2. Charge assignments consistent with Higgs potential stability and perturbativity for $g_4 = 0.1$ (blue region), $g_4 = 0.2$ (yellow region) and $g_4 = 0.3$ (red region) at $M_{Z'} = m_t$. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Fig. 1 shows regions of parameter space allowed by stability of the Higgs potential and perturbativity (shaded regions). As 3 charges play the most important role, we display our results in two planes: $Q_{q_3}-Q_h$ and Q_4-Q_h . To fix Q_4 , we set $Q_l = Q_{\chi} = 0$, $Q_S = 2$, although, as explained above, the results do not depend on this choice.

The shape of the allowed regions can be easily understood. The lower bound on charges is dictated by stability of the Higgs potential, whereas the upper bound is imposed by perturbativity. The allowed regions shrink as g_4 increases since the couplings reach non-perturbative values sooner. The Q_{q_3} - Q_h panel shows that the stabilization is possible for non-zero Higgs charges only, although such charges can be as small as 10^{-1} . As Q_{q_3} increases, values of the allowed Higgs charges decrease since smaller charges are sufficient to stabilize the Higgs potential on one hand and smaller charges are compatible with perturbativity on the other hand. Above a certain critical Q_{q_3} , no charge assignment leads to a perturbative result.

In the Q_4-Q_h plane, we vary Q_4 by changing Q_{q_3} while keeping the rest of the charges intact. The upper bound on Q_h at a given Q_4 is dictated by positivity of Q_i^2 in Eq. (17) (or Eq. (21)). Large values of Q_4 violate perturbativity, while its low values for a fixed Q_h would fail to stabilize the potential.

5.2. Leptophobic Z'

For a leptophobic Z', the strong LEP and LHC bounds on Z' do not apply, allowing for $M_{Z'} \sim 200$ GeV. In this case, the U(1)' affects the running of the couplings already at the electroweak scale. The shape of the allowed regions remains the same as in the $M_{Z'} = 3$ TeV case (Fig. 2), yet there are important quantitative differences. In particular, the $Q_h = 0$ assignment becomes allowed. In that case, the stabilizing effect is due entirely to the reduction of the top Yukawa coupling. Values of Q_{q_3} between 1 and 3, depending on the gauge coupling, are sufficient to stabilize the scalar potential. The Z' mass plays a crucial role here: the top Yukawa coupling has its strongest effect on λ_h at low energies and reducing y_t in this energy range brings about the desired result. As we have established in the previous subsection, this effect cannot be achieved for a heavy Z': compensating the shorter running range by increasing the charge or g_4 carries the coupling into a non-perturbative territory.

The effect of the top quark charge on the evolution of λ_h is shown in Fig. 3. In the left panel, the Z' has an electroweak mass $\sim m_t$, while in the right panel $M_{Z'} = 3$ TeV. Taking $Q_h = 0$, the Higgs self-coupling turns negative at around 10⁹ GeV if the top quark does not couple to the Z'. Increasing Q_{q_3} to about 2.5 with $g_4(m_t) = 0.1$ makes the Higgs potential stable up to the Planck scale, whereas a



Fig. 3. Evolution of λ_h with energy scale Λ for $M_{Z'} = m_t$ (left) and $M_{Z'} = 3$ TeV (right) in the Higgsophobic case. The blue (lower) curve corresponds to the SM, the green (middle) curve corresponds to the minimal Q_{q_3} which achieves the Higgs potential stabilization, and the red (upper) curve corresponds to the maximal allowed Q_{q_3} consistent with perturbativity. Here $Q_h = 0$, $g_4(M_{Z'}) = 0.1$.



Fig. 4. Effect of the kinetic mixing ϵ on the allowed parameter space for $g_4 = 0.1$ (blue region), $g_4 = 0.2$ (yellow region) and $g_4 = 0.3$ (red region) at $M_{Z'} = 3$ TeV and $Q_h = 1$. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

further increase above 2.9 makes the system non-perturbative. For the heavy Z', perturbativity is violated before stability is achieved. At the critical value $Q_{q_3} = 2.9$, the Higgs self-coupling is positive at the Planck scale, yet it is negative at intermediate scales indicating the existence of a deep minimum at these field values.

We therefore conclude that the Higgs potential can be stabilized even by a *Higgsophobic* U(1), if the corresponding Z' is light enough. The *B*-*L* symmetry however does not fall into this category since Z'_{B-L} is constrained to be rather heavy.

5.3. Effect of the kinetic mixing

Generally, an extra U(1) mixes with the SM hypercharge. That implies, among other things, that even though the charges for the SM fields are zero, the Z' may still couple to SM matter if the kinetic mixing parameter ϵ is non-zero. In this case, ϵ is constrained to be of order 10^{-2} for $M_{Z'}$ of the order of the electroweak scale [28]. The resulting effect on the evolution of λ_h is negligible since for $Q_h = 0$ the kinetic mixing contribution to β_{λ_h} is proportional to ϵ^2 according to Eq. (12). The bound on ϵ relaxes significantly for a heavier Z' allowing $\epsilon \sim \mathcal{O}(10^{-1}) - 1$ at $M_{Z'} \sim 2-3$ TeV (see e.g. [29]). Of course, $\epsilon \sim 1$ can

The bound on ϵ relaxes significantly for a heavier Z' allowing $\epsilon \sim \mathcal{O}(10^{-1}) - 1$ at $M_{Z'} \sim 2-3$ TeV (see e.g. [29]). Of course, $\epsilon \sim 1$ can simply be reinterpreted as a different U(1)' charge assignment with order one charges proportional to the hypercharge (see Eq. (15)). On the other hand, $\epsilon \sim 0.1$ is still meaningful as it corresponds to small charges which otherwise would be unnatural. For such values of the kinetic mixing, the effect on λ_h is substantial only if β_{λ_h} contains linear terms in ϵ , that is if $Q_h \neq 0$. Fig. 4 shows the effect of ϵ on the allowed parameter regions at $Q_h = 1$. The kinetic mixing tends to decrease λ_h due to the ϵ -linear terms in β_{λ_h} of Eq. (12), which shifts the allowed regions to somewhat larger charges. This behaviour is reversed for negative ϵQ_h .

We have also investigated the possibility of stabilizing the Higgs potential entirely due to the kinetic mixing of $U(1)_{B-L}$ and $U(1)_Y$, which belongs to the $Q_h = 0$ category. We find that the required ϵ is too large ($\sim \mathcal{O}(0.5)$) for the B-L interpretation of the charge assignment to make sense. In that case, however, the scalar contribution from λ_{hs} can be efficient in stabilizing the Higgs potential.

6. Conclusion

We have analyzed the possibility of stabilizing the Higgs potential with a Z' boson. We find that a generic Z' improves stability of the potential in two ways: it increases the beta function of the Higgs quartic coupling directly and reduces the top quark Yukawa coupling, which also has a positive effect on λ_h . The Higgs and top quark U(1)' charges play the most important role in this mechanism. The stabilization is achieved for order one charges and the gauge coupling g_4 of the electroweak size. In case of a light Z', $M_{Z'} \sim m_t$, the Higgs potential can be stabilized even if the Z' does not couple to the Higgs, i.e. entirely through a reduction of the top Yukawa coupling. A heavier Z' in the multi-TeV range necessitates a direct coupling to the Higgs boson to achieve the same effect.

We have also analyzed the effect of a kinetic mixing term between the Z' and the hypercharge. We find that the mixing parameter ϵ of order 10^{-1} can have a tangible effect on the allowed parameter space.

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